An optical receiver may include a unitary transformation operator to receive an n-symbol optical codeword associated with a codebook, and to perform a unitary transformation on the received optical codeword to generate a transformed optical codeword, where the unitary transformation is based on the codebook. The optical receiver may further include n optical detectors, where a particular one of the n optical detectors is to detect a particular optical symbol of the transformed optical codeword, and to determine whether the particular optical symbol corresponds to a first optical symbol or a second optical symbol. The optical receiver may also include a decoder to construct a codeword based on the determinations, and to decode the constructed codeword into a message using the codebook. The optical receiver may attain superadditive capacity, and, with an optimal code, may attain the Holevo limit to reliable communication data rates.

20 Claims, 15 Drawing Sheets

An optical receiver may include a unitary transformation operator to receive an n-symbol optical codeword associated with a codebook, and to perform a unitary transformation on the received optical codeword to generate a transformed optical codeword, where the unitary transformation is based on the codebook. The optical receiver may further include n optical detectors, where a particular one of the n optical detectors is to detect a particular optical symbol of the transformed optical codeword, and to determine whether the particular optical symbol corresponds to a first optical symbol or a second optical symbol. The optical receiver may also include a decoder to construct a codeword based on the determinations and to decode the constructed codeword into a message using the codebook. The optical receiver may attain superadditive capacity, and, with an optimal code, may attain the Holevo limit to reliable communication data rates.
References Cited

PUBLICATIONS


FIG. 1
FIG. 2A
FIG. 2B
FIG. 3

$W \in \{1, \ldots, 2^{nR}\}$

MESSAGE 310

ENCODER 320

MODULATOR 330

OPTICAL CODEWORD STATE 340
\{ \gamma_r^2 \ldots \gamma_1 \} \in \mathbb{M}

**FIG. 4**

- **MESSAGE 310**
- **DECODER 430**
- **DOLINAR RECEIVER 420-A**
- **DOLINAR RECEIVER 420-B**
- **DOLINAR RECEIVER 420-N**
- **UNITARY TRANSFORMATION DEVICE 410**
- **OPTICAL CODEWORD 340**

160
FIG. 5
FIG. 9

TEMPORALLY ENCODED CODEWORD

UNITARY TRANSFORMATION DEVICE

DEMULTIPLEXER BUFFERS

OPTICAL DEMULTIPLEXER BUFFERS
1110 - RECEIVE OPTICAL CODEWORD

1120 - PERFORM UNITARY TRANSFORMATION ON OPTICAL CODEWORD

1130 - DETECT INDIVIDUAL SYMBOLS OF TRANSFORMED OPTICAL CODEWORD BY INDIVIDUAL RECEIVERS

1140 - CONVERT INDIVIDUAL OPTICAL SYMBOLS INTO ELECTRICAL SIGNALS TO GENERATE ELECTRICAL CODEWORD

1150 - DECODE ELECTRICAL CODEWORD TO RETRIEVE MESSAGE

FIG. 11
FIG. 12
SELECT CODEBOOK WITH $2^nR$ CODEWORDS, EACH CODEWORD BEING A SEQUENCE OF n BPSK SYMBOLS $|+\rangle$ and $|-\rangle$

GENERATE MINIMUM PROBABILITY OF ERROR (MPE) BASIS FOR CODEBOOK

EXTEND CODEWORDS OF CODEBOOK INTO A SET OF ALL $2^n$ BINARY SEQUENCES OF $|+\rangle$ and $|-\rangle$

EXTEND MPE BASIS TO SPAN THE WHOLE SPACE OF THE $2^n$ BINARY SEQUENCES

REPRESENT SINGLE MODE MPE MEASUREMENTS ON $|+\rangle$ and $|-\rangle$ AS $|+\rangle$ and $|\rangle$

GENERATE SINGLE MODE MEASUREMENT BASIS BASED ON KRONECKER PRODUCT OF $|+\rangle$ and $|\rangle$

REPRESENT EACH CODEWORD OF CODEBOOK IN EXTENDED MPE BASIS TO GENERATE EXTENDED MPE UNITARY MATRIX

REPRESENT EACH CODEWORD OF CODEBOOK IN SINGLE MODE MEASUREMENT BASIS TO GENERATE SINGLE MODE MEASUREMENT UNITARY MATRIX

GENERATE UNITARY TRANSFORMATION OPERATOR BY MULTIPLYING INVERSE OF EXTENDED MPE BASIS UNITARY MATRIX WITH SINGLE MODE MEASUREMENT UNITARY MATRIX

FIG. 13
FIG. 14

1410 - DETERMINE UNITARY TRANSFORMATION OPERATOR FOR A PARTICULAR CODEBOOK

1420 - REPRESENT DOLINAR RECEIVER AS A CONCATENATION OF A SINGLE-MODE UNITARY OPERATOR AND A PHOTON COUNTING DETECTOR

1430 - COMBINE N SINGLE-MODE UNITARY OPERATORS WITH UNITARY TRANSFORMATION OPERATOR TO GENERATE COMBINED UNITARY TRANSFORMATION OPERATOR

1440 - GENERATING A LAYOUT FOR A PHOTONIC CIRCUIT FOR IMPLEMENTING A JOINT-DETECTION RECEIVER BASED ON COMBINED UNITARY TRANSFORMATION OPERATOR AND A SET OF N PHOTON COUNTING DETECTORS

FIG. 15

1510 - DETERMINE UNITARY TRANSFORMATION OPERATOR FOR A PARTICULAR CODEBOOK

1520 - DECOMPOSE UNITARY TRANSFORMATION OPERATOR INTO A SET OF ELEMENTARY UNITARY OPERATORS REPRESENTING A BEAM SPITTER, A PHASE SHIFTER, A SQUEEZER, AND A KERR NONLINEARITY DEVICE

1530 - GENERATE LAYOUT OF PHOTONIC CIRCUIT COMPRISING BEAM SPLITTERS, PHASE SHIFTERS, SQUEEZERS, AND KERR NONLINEARITY DEVICES
According to another aspect, a method, performed by an optical receiver, may include: receiving, by the optical receiver, an n-symbol optical codeword associated with a codebook, the optical codeword including n symbols; performing, by the optical receiver, a unitary transformation on the received optical codeword to generate a transformed optical codeword, where the unitary transformation is based on the codebook. The optical receiver may further include n optical detectors, where a particular one of the n optical detectors is to detect a particular optical symbol of the transformed optical codeword, and to determine whether the particular optical symbol corresponds to at least a first optical symbol or a second optical symbol. The optical receiver may also include a decoder to construct a codeword based on the determinations, and to decode the constructed codeword into a message using the codebook.

According to one aspect, an optical receiver may include a unitary transformation device to receive an n-symbol optical codeword associated with a codebook, and to perform an optical unitary transformation on the received optical codeword to generate a transformed optical codeword, where the unitary transformation is based on the codebook. The optical receiver may further include n optical detectors, where a particular one of the n optical detectors is to detect a particular optical symbol of the transformed optical codeword, and to determine whether the particular optical symbol corresponds to at least a first optical symbol or a second optical symbol. The optical receiver may also include a decoder to construct a codeword based on the determinations, and to decode the constructed codeword into a message using the codebook.

According to yet another aspect, a method, performed by a computer device, may include: receiving, by the computer device, a codebook; generating, by the computer device, a minimum probability of error (MPE) basis for the codebook; generating, by the computer device, a measurement unitary matrix for the codebook by expressing codewords of the codebook in the MPE basis; and generating, by the computer device, a single mode MPE basis based on representations of single mode measurements on binary symbols used to represent the codewords of the codebook; generating, by the computer device, a single mode measurement unitary matrix for the codebook by expressing the codewords of the codebook in the single mode MPE basis; and generating, by the computer device, a unitary transformation operator for the codebook by multiplying an inverse of the measurement unitary matrix with the single mode measurement unitary matrix.
DETAILED DESCRIPTION

The following detailed description of the invention refers to the accompanying drawings. The same reference numbers may be used in different drawings to identify the same or similar elements.

An implementation described herein may relate to a joint-detection optical receiver (JDR) that can achieve superadditive channel capacity. Superadditivity may refer to a channel capacity higher than a channel capacity realizable by making single symbol measurements, and may be achieved by making joint measurements over multiple symbols. A joint measurement may correspond to a measurement of a quantum state of a codeword block that includes multiple symbols. Joint measurements made over multiple quantum state symbols for a communication channel may be necessary to achieve a Holevo limit associated with the communication channel.

An implementation described herein may relate to approaching a Holevo limit by performing a projective measurement. A projective measurement may be implemented by performing a unitary transformation on a quantum codeword, which may transform quantum states associated with symbols of the quantum codeword into superpositions of quantum states, followed by separable projective measurements. A unitary transformation on an optical codeword of n symbols may correspond to a lossless transformation on the quantum state of the n symbols. In other words, a unitary transformation on an optical codeword in a vector space may correspond to a transformation that preserves an inner product.

An optical receiver described herein, which may approach the Holevo limit, may include a unitary transformation operator and one or more separate optical detectors. In one example, the separate optical detectors may include Dolinar receivers. In another example, the separate optical detectors may include a different type of optical receiver, such as Kennedy receivers, Sasaki-Hirota receivers, homodyne receivers, heterodyne receivers, or single photon detectors.

A structure of the unitary transformation operator may be based on the codebook used to encode the codewords received by the receiver. In an example where the codebook corresponds to three two-symbol binary phase shifting key (BPSK) states, the unitary transformation operator may correspond to a beam splitter that acts on the two symbols. In an example where the codebook corresponds to a BPSK Hadamard code, the unitary transformation operator may correspond to a multi-stage butterfly 50-50 asymmetric beam splitter circuit. The multi-stage butterfly 50-50 asymmetric beam splitter circuit may be implemented as an integrated photonic circuit. The multi-stage butterfly 50-50 asymmetric beam splitter circuit may be known as a Green Machine. In general, the unitary transformation operator may be determined for a particular codebook and may be decomposed into a combination of elementary optical operators corresponding to a beam splitter operator, a shifter operator, a squeezer operator, and a third-order Hamiltonian operator, such as a Kerr non-linearity operator or a photon number resolving operator. In one example, the unitary transformation operator may be implemented as an integrated photonic circuit that includes a combination of a beam splitter, shifters, squeezers, and Kerr nonlinearity devices.

In some implementations, the unitary transformation operator may be implemented using more than two-symbol (binary) states. For example, an arbitrary unitary operator on a n-symbol codeword (where each symbol is chosen from a M-ary modulation constellation, such as BPSK or QPSK) may include: (a) beamsplitters, (b) phase shifters, (c) squeezers, and (d) Kerr non-linearities (or any other device that can provide a third-order Hamiltonian interaction). Photon number resolving (PNR) detectors, for instance, may be used to provide a third-order Hamiltonian interaction, and may potentially be used in place of Kerr non-linearities.

The unitary transformation operator may be generated, for a codebook, by generating a minimum probability of error (MPE) basis for the codebook, and by representing each codeword of the codebook in terms of the MPE basis to generate a first unitary matrix. A single measurement basis may be generated based on a Kronecker product of single mode MPE measurements on the individual symbols used to generate codewords of the codebook. Each codeword of the codebook may be represented in terms of the single measurement basis to generate a second unitary matrix, and the unitary transformation operator may be generated by multiplying an inverse of the first unitary matrix with the second unitary matrix.
optical codeword, measure individual symbols of the transformed n-symbol optical codeword using n optical detectors to convert the individual symbols into n electrical symbols, decode the converted electrical symbols into an estimate of the k-bit message, and forward the decoded message to receiving device 170. FSO receiver 160 may include, among other components, a phase-locked loop, a fiber modulator, a digital oscilloscope, and/or an optical receiver telescope.

Although FIG. 1 shows example components of system 100, in other implementations, system 100 may include fewer components, different components, differently arranged components, and/or additional components than depicted in FIG. 1. Additionally or alternatively, one or more components of system 100 may perform one or more tasks described as being performed by one or more other components of system 100.

FIG. 2A is a diagram illustrating a graph 200 of photon information efficiency. As shown in FIG. 2A, graph 200 may illustrate a relationship between bits per photon and mean photon number per mode, represented as curve 210. Curve 210 may represent the information carrying capacity of photons, and may depict that no fundamental upper limit exists on the information that may be encoded in a photon. If one desires to encode more information in a photon, one may need to lower the mean photon number per mode. Point 220 may illustrate an example of the information carrying capacity of photons at 10 bits per photon. According to an implementation described herein, using FSO transmitter 120 at 1.55 micrometers (µm) and operating at a 1 gigahertz (GHz) modulation bandwidth, the laws of physics may permit reliable communication at 0.27 Gigabits per second (Gbps) using only 3.4 picowatts (pW) of average received optical power. At such low optical power levels, communications may be secure, as it may be difficult for an intercepting party to detect the signal.

FIG. 2B is a diagram illustrating a graph 250 of the relationship between a binary phase shift keying (BPSK) Holevo limit and an ultimate Holevo limit. A BPSK modulation optical communication system may encode data by sending either an optical pulse or a 180° phase reversed optical pulse over each use of a physical channel. The maximum information that may be sent over the channel using any binary modulation scheme, such as BPSK, is 1 bit per channel use, which may be achieved if the two optical states are perfectly distinguishable to the receiver. The lower a mean photon number in each of the two BPSK states, the harder it is to tell the two optical states apart. The quantum limit to the minimum probability of error (MPE) of discriminating between the two optical pulses may be expressed as

\[ P_{\text{min}} = \frac{1}{2} \left[ 1 - \sqrt{1 - e^{-2N}} \right], \]

where N corresponds to the mean photon number in each of the two BPSK states. The quantum limit of the MPE may be lower than any probability of error achievable by an optical receiver (e.g., a direct optical detector, a homodyne optical detector, or a heterodyne optical detector). The quantum limit of the MPE may be achieved using a Dolinar receiver, which uses a single photon detector coupled with near instantaneous electrical to optical feedback from the electrical output of the single photon detector to optical input of the single photon detector.

Curve 260 may illustrate a highest Shannon capacity achievable by the BPSK modulation system using a single symbol receiver, which may be attained with a Dolinar receiver. Thus, a maximum capacity reachable by a single symbol receiver may correspond to 2-ln2, or 2.89 bits per photon. Curve 270 may illustrate an ultimate Holevo limit of a joint detection receiver that performs a joint measurement over a codeword block of symbols using an optimal codebook. Curve 280 may illustrate the Holevo limit of a joint detection receiver that uses binary modulation. Thus, FIG. 2B may demonstrate that binary modulation (e.g., using BPSK) may be close to optimal to approaching the Holevo limit at low photon numbers per mode.

FIG. 3 is a diagram illustrating example components of FSO transmitter 120. As shown in FIG. 3, FSO transmitter 120 may include an encoder 320 and a modulator 330.

Sending device 110 may break up a message to be sent to receiving device 170 into k-bit messages. Encoder 320 may receive a k-bit message 310 and encode k-bit message 310 into an n-bit code word. The k-bit message may correspond to an element from the set \( \{1, \ldots, 2^n\} \), where R corresponds to the transmission rate in bits per channel use, or bits per modulation symbol, n corresponds to the size of a codeword, and k-nR corresponds to the size of message 310. Thus, message 310 may correspond to any sequence of k bits. Encoder 320 may include a 1-1 map that maps a particular sequence of k bits to a particular codeword of n bits. Thus, each member of the set \( \{1, \ldots, 2^n\} \) may be associated with a particular n-bit codeword. The set of n-bit codewords may correspond to the codebook.

Modulator 330 may receive a codeword from encoder 320 and may generate modulated light signal 150 that includes optical codeword state 340. Modulator 330 may use BPSK to convert bits of the received n-bit codeword into one of two possible light symbols |+a) and |−a). For example, |+a) may correspond to a first phase of a photon and |−a) may correspond to a second phase of a photon, where the second phase differs from the first phase by 180°. Modulator 330 may be implemented, for example, as a ferroelectric liquid crystal (FLC) array incorporated into an integrated circuit, in combination with a light source. An FLC may use birefringence to convert a voltage polarity into a rotation of the optical axis of light emitted by the light source. In another implementation, modulator 330 may be implemented using a different type of device.

Although FIG. 3 shows example components of FSO transmitter 120, in other implementations, FSO transmitter 120 may include fewer components, different components, differently arranged components, and/or additional components than depicted in FIG. 3. Additionally or alternatively, one or more components of FSO transmitter 120 may perform one or more tasks described as being performed by one or more other components of FSO transmitter 120.

FIG. 4 is a diagram illustrating example components of FSO receiver 160. As shown in FIG. 4, FSO receiver 160 may include a unitary transformation device 410, one or more Dolinar receivers 420-A to 420-N (referred to herein collectively as “Dolinar receivers 420” and individually as “Dolinar receiver 420”), and a decoder 430.

Unitary transformation device 410 may receive optical codeword 340 and may perform a unitary transformation in the optical domain on the received optical codeword 340. The unitary transformation may correspond to a joint operation performed on all the symbols of the received optical codeword 340 simultaneously. Unitary transformation device 410 may output a transformed (and possibly entangled) optical quantum state of the received optical codeword 340. While
the received optical codeword 340 may correspond to a set of pure coherent-state BPSK symbols |+a⟩ and |−a⟩ (e.g., optical states corresponding to two different phases), the transformed optical codeword may correspond to states which may not be pure BPSK symbols |+a⟩ and |−a⟩, but rather may correspond to linear combinations of |+a⟩ and |−a⟩ (e.g., superpositions of |+a⟩ and |−a⟩). Unitary transformation device 410 may forward individual symbols associated with the transformed optical codeword to particular ones of Dolinar receivers 420.

Dolinar receiver 420 may convert the received optical symbol into an electrical signal corresponding to an estimate of the local field controlled by feedback amplitude modulator 520 and feedback phase modulator 530 on the observed photon count. Feedback controller 570 may control feedback amplitude modulator 520 and feedback phase modulator 530 based on the observed photon count.

Although FIG. 5 shows example components of Dolinar receiver 420, in other implementations, Dolinar receiver 420 may include fewer components, different components, differently arranged components, and/or additional components than depicted in FIG. 5. Additionally or alternatively, one or more components of Dolinar receiver 420 may perform one or more tasks described as being performed by one or more other components of Dolinar receiver 420. In alternative implementations, a receiver other than a Dolinar receiver may be used. For example, in the context of Reed Muller codes, a Kennedy receiver may be used instead of a Dolinar receiver.

In other example implementations, FSO receiver 160 may use different type of receivers. For example, FSO receiver 160 may use Kennedy receivers. A Kennedy receiver may add a local field to a received signal field without the use of a feedback loop. Rather, in a Kennedy receiver, the amplitude and phase of the local field may be set to correspond to H0.

FIG. 6 is a diagram illustrating example components of a first example receiver 600 capable of being used by FSO receiver 160. As shown in FIG. 6, receiver 600 may include a unitary transformation operator 610 and a projective measurement receiver 620.

Unitary transformation operator 610 may correspond to a unitary transformation on a codebook that includes three codewords 601, 602, and 603. Codeword 601 may correspond to |ψ1⟩ = |+a⟩ ⊗ |a⟩, codeword 602 may correspond to |ψ2⟩ = |a⟩ ⊗ |−a⟩, and codeword 603 may correspond to |ψ3⟩ = |−a⟩ ⊗ |−a⟩. Unitary transformation operator 610 may include a beam splitter 615.

Beam splitter 615 may include a device with two input modes and two output modes and may separate an incident beam of light into a reflected beam and a transmitted beam. Beam splitter 615 may be implemented as two right-angle prisms, cemented together at their hypotenuse, with the hypotenuse surface being coated with a metallic or dielectric layer.

Beam splitter 615 may take as input two quantum symbols and may output two quantum symbols that are a superposition of the two input quantum symbols. Thus, beam splitter 615 may perform a unitary transformation on an incoming codeword to generate a transformed (and possibly entangled) codeword. For example, beam splitter 615 may transform first codeword 601 to first transformed codeword 611 corresponding to |ψ1⟩ = |+a⟩ ⊗ |0⟩, may transform second codeword 602 to second transformed codeword 612 corresponding to |ψ2⟩ = |0⟩ ⊗ |2a⟩, and may transform third codeword 603 to third transformed codeword 613 corresponding to |ψ3⟩ = |0⟩ ⊗ |−2a⟩.

Projective measurement receiver 620 may include a single photon detector 630 and a Dolinar receiver 640. Projective measurement receiver 620 may perform a measurement on a transformed codeword and may determine to which codebook the transformed codeword corresponds.
Receiver 600 may achieve superadditive capacity gain in comparison to using a single Dolinar receiver (e.g., using Dolinar receiver 640 by itself). For example, using Dolinar receiver 640 by itself may result in a maximum photon efficiency of 2.8854 bits per photon, while receiver 600 may result in a maximum photon efficiency of 2.9572 bits per photon.

Although FIG. 6 shows example components of receiver 600, in other implementations, receiver 600 may include fewer components, different components, differently arranged components, and/or additional components than depicted in FIG. 6. Additionally or alternatively, one or more components of receiver 600 may perform one or more tasks described as being performed by one or more other components of receiver 600.

FIG. 7 is a diagram illustrating example components of a second receiver 700 capable of being used by FSO receiver 160. As shown in FIG. 7, receiver 700 may include a unitary transformation operator 710 and a projective measurement receiver 730.

Unitary transformation operator 710 may perform a unitary transformation on codewords based on a Hadamard matrix 701. The top row of Hadamard matrix 701 may correspond to an ancilla mode (e.g., a locally encoded signal that may facilitate the identification of errors in a received codeword). The use of an ancilla mode as part of a transmitted codeword may prevent receiver 700 from having to perform active-phase tracking and may improve performance of receiver 700.

Unitary transformation operator 710 may include a group of beam splitters 711-722. If the input of unitary transformation operator 710 includes a codeword with n optical symbols, then unitary transformation operator 710 may include n*log2(n/2) beam splitters. Each of beam splitters 711-722 may take as input two quantum symbols of a codeword and may output two different quantum symbols.

Projective measurement receiver 730 may perform projective measurements on particular symbols of the transformed optical codeword. The projective measurements may include multiple single photon detectors. A particular single photon detector may perform photon counts for a particular output of unitary transformation operator 710.

Given Hadamard matrix 701, unitary transformation operator 710 may, in combination with projective measurement receiver 730, output pulse position modulation matrix 702. Thus, unitary transformation operator 701 may perform a unitary operation that corresponds to a Walsh transform.

As an example, using receiver 700 with a 2048 input by 2048 output that includes 11,264 beam splitters (2048*log2(2048)/2=11,264), together with 2048 single photon detectors, may attain a capacity of 10 bits per photon using BPSK modulation at a mean photon number of 2.8854 photons detected. Decoder 830 may correspond to decoder 430 of FIG. 4.

Although FIG. 8 shows example components of receiver 800, in other implementations, receiver 800 may include fewer components, different components, differently arranged components, and/or additional components than depicted in FIG. 8. Additionally or alternatively, one or more components of receiver 800 may perform one or more tasks described as being performed by one or more other components of receiver 800.

FIG. 9 is a diagram illustrating example components of a fourth receiver 900 capable of being used by FSO receiver 160. While implementations described herein correspond to receivers using spatial encoding (e.g., an n number of orthogonal spatial modes with n symbols transmitted simultaneously), receiver 900 may correspond to an implementation using temporal coding (e.g., one spatial mode with one symbol transmitted at a time). Thus, while receiver 400 (or receiver 800) may receive an n-symbol codeword in one pulse, receiver 900 may receive an n-symbol codeword in n pulses.

As shown in FIG. 9, receiver 900 may include an optical demultiplexer 910, one or more optical buffers 920-A to 920-N (referred to herein collectively as “optical buffers 920” and individually as “optical buffer 920”), a unitary transformation device 410, one or more Dolinar receivers 420-A to 420-N, and decoder 430.

Optical demultiplexer 910 may receive a temporally encoded codeword 901 at a symbol rate and may select optical buffers 920 in sequence. Thus, optical demultiplexer 910 may send a first symbol to optical buffer 920-A, a second symbol to optical buffer 920-B, and so on until optical buffer 920-N receives the n-th symbol.

Optical buffers 920 may temporarily store particular symbols of temporally encoded codeword 901. In one example, optical buffers 920 may include optical paths (e.g., optical fibers) of different lengths so that when the n-th symbol is received by optical buffer 920-N, all n symbols are forwarded to unitary transformation device 410 at substantially the same time. For example, optical buffer 920-A may include an opti-


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cal path that is longer than the optical path of optical buffer 920-B, the optical path of optical buffer 920-B may
equipped with an optical path that is longer than the optical path of optical
buffer 920-C, and so on, with optical buffer 920-N having a shortest optical path. In another example, optical buffers 920
may include slow light devices configured so that all n optical symbols exit optical buffers 920 at substantially the same
time.

Unitary transformation device 410, Dolinar receivers 420, and
decoder 430 may correspond to unitary transformation
device 410, Dolinar receivers 420, and decoder 430 of FIG. 4,
respectively.

Although FIG. 9 shows example components of receiver
900, in other implementations, receiver 900 may include
cocoder, different components, differently
arranged components, and/or additional components than
depicted in FIG. 9. Additionally or alternatively, one or more
components of receiver 900 may perform one or more tasks
described as being performed by one or more other compo-
nents of receiver 900.

FIG. 10 is a diagram illustrating example components of a
fifth receiver 1000 capable of being used by FSO receiver
160. Receiver 1000 may detect codewords encoded using a
first-order Reed-Muller code R(l,m). A Reed-Muller code
R(m,m) may correspond to a [n, k, d] linear code [0a1..m],
where n=2^m is the length of each codeword, with K=2^m
codewords in the code, and with a minimum distance, in the code
space, of d=2^m-n between any two codewords.

First order Reed-Muller code R(1,m) may be a [2^m, m+1, 2^{m-2}-1] code that corresponds to a [2^m, m, 2^{m-1}] Hadamard code,
including an ancilla, with the same codewords with flipped bits. An R(1,m) code, similar to a Hadamard code, may be
decoded in the optical domain using a joint detection receiver
with n log n/2 beamsplitters (where n=2^m), followed by an
array of n single photon detectors, followed by a single Dolinar
receiver.

As shown in FIG. 10, receiver 1000 may include a unitary
transformation operator 1010, a projective measurement receiver 1020, a switch 1030, and a Dolinar receiver 1040.
Unitary transformation operator 1010 may perform a unitary
transformation on codewords, analogous to unitary transformation
operator 710 of FIG. 7. Projective measurement receiver 1020 may include a group of single photon detectors
that perform photon counts for a particular output of unitary
transformation operator 1010, analogous to projective measure-
ment receiver 730. Dolinar receiver 1040 may include a
Dolinar receiver analogous to Dolinar receiver 640. Dolinar receiver 1040 may be switchable, via switch 1030, to any of
the single photon detectors of projective measurement receiver 1020.

When a codeword is received by receiver 1000, a particular
one of the single photon detectors, of projective measurement receiver 1020, may click (e.g., detect a photon). The particular
single photon detector that clicks may trigger Dolinar receiver 1040. If none of the single photon detectors clicks,
receiver 1000 may yield an unsatisfactory outcome, indicating that receiver 1000 was not able to determine which particular
codeword was received.

Receiver 1000, which may decode codewords based on a
first order BPSK Reed-Muller codebook, may outperform a
detector based on direct detection of on-off keying. Further-
more, receiver 1000 may exhibit superadditive capacity for a
BPSK alphabet, with a higher capacity than a codebook in the
Hadamard codebook family.

Although FIG. 10 shows example components of receiver
1000, in other implementations, receiver 1000 may include
fewer components, different components, differently
arranged components, and/or additional components than
depicted in FIG. 10. Additionally or alternatively, one or more
components of receiver 1000 may perform one or more tasks
described as being performed by one or more other compo-
nents of receiver 1000.

FIG. 11 is a flow chart of an example process for perform-
ing a superadditive measurement of a received codeword
according to an implementation described herein. In one
implementation, the process of FIG. 11 may be performed
by FSO receiver 160. In other implementations, some or all of
the process of FIG. 11 may be performed by another device or
a group of devices separate and/or possibly remote from or
including FSO receiver 160.

The process of FIG. 11 may include receiving an optical
codeword (block 1110). For example, FSO receiver 160 may
receive an optical codeword based on modulated light signal
150. The codeword may be received by unitary transformation
device 410.

A unitary transformation may be performed on the
received optical codeword (block 1120). For example, unitary
transformation device 410 may perform a unitary transformation
on the received optical codeword. Unitary transformation
device 410 may output a transformed (and possibly
entangled) optical quantum state of the received optical
codeword. While the received optical codeword may correspond
to a set of pure BPSK symbols |+a> and |-a> (e.g., photon
dstates corresponding to two different phases), the transformed
optical codeword may correspond to states which may not be
pure BPSK symbols |+a> and |-a>, but may rather corre-
spond to linear combinations of |+a> and |-a> (e.g., super-
positions of |+a> and |-a>).

Individual symbols of the transformed optical codeword
can be converted into electrical signals to generate an electrical
codeword (block 1140). For example, unitary transformation
device 410 may perform the detection of individual receivers (block 1130). For one or more unitary transformation
device 410 may perform the detection of individual receivers (block 1130). For one or more
components of Dolinar receivers 420. Each of
Dolinar receivers 420 may detect a particular transformed symbol (e.g., corresponding to a particular linear combina-
tion of |+a> and |-a>).

The individual optical symbols may be converted into elec-
trical signals to generate an electrical codeword (block 1140). For example, a Dolinar receiver 420 may convert
the detected optical symbol into an electrical signal corre-
sponding to an estimate of whether the received optical sym-
bol corresponds to a |+a> symbol or a |-a> symbol.

The electrical codeword may be decoded to retrieve a mes-
 sage (block 1150). For example, decoder 430 may receive the
electrical signals from Dolinar receivers 420 and may com-
bine the received electrical signals into an estimate of an
n-symbol particular codeword of the codebook. Decoder 430
may then use a 1-1 map to generate an estimate of a k-bit
message corresponding to the n-symbol estimated codeword.

FIG. 12 is a diagram illustrating example components of a
computer device 1200 that may be used to generate a unitary
transformation matrix corresponding to unitary transformation
device 410, that may be used to generate a combined
unitary transformation matrix corresponding to combined
unitary transformation device 810, or that may be used to
generate a layout for a photonic circuit based on a particular
unitary transformation matrix. As shown in FIG. 12, com-
puter device 1200 may include a bus 1210, a processor 1220,
a memory 1230, an input device 1240, an output device 1250,
and a communication interface 1260.
Bus 1210 may include a path that permits communication among the components of computer device 1200. Processor 1220 may include one or more processors, microprocessors, or processing logic (e.g., application specific integrated circuits (ASICs) or field programmable gate arrays (FPGAs)) that may interpret and execute instructions. Memory 1230 may include a random access memory (RAM) device or another type of dynamic storage device that may store information and instructions for execution by processor 1220, a read only memory (ROM) device or another type of static storage device that may store static information and instructions for use by processor 1220, a magnetic and/or optical recording memory device and its corresponding drive, and/or a removable form of memory, such as a flash memory.

Input device 1240 may include a mechanism that permits an operator to input information to computer device 1200, such as a keypad, a button, a pen, a touch screen, voice recognition and/or biometric mechanisms, etc. Output device 1250 may include a mechanism that outputs information to the operator, including one or more light indicators, a display, a speaker, etc.

Communication interface 1260 may include any transceiver-like mechanism that enables computer device 1200 to communicate with other devices and/or systems. For example, communication interface 1260 may include a modem, a network interface card, and/or a wireless interface card.

As described herein, computer device 1200 may perform certain operations. Computer device 1200 may perform these operations in response to processor 1220 executing software instructions contained in a computer-readable medium, such as memory 1230. A computer-readable medium may be defined as a non-transitory memory device. A memory device may contain fewer components, different components, additional components, or differently arranged components than depicted in FIG. 12. Alternatively, hardwired circuitry may be used in place of or in addition to software.

The software instructions may be read into memory 1230 from another computer-readable medium, or from another device via communication interface 1260. The software instructions contained in memory 1230 may cause processor 1220 to perform processes that will be described later. Alternatively, the processes described herein are not limited to any specific combination of hardware circuitry and software.

Although FIG. 12 shows example components of computer device 1200, in other implementations, computer device 1200 may contain fewer components, different components, additional components, or differently arranged components than depicted in FIG. 12. Additionally or alternatively, one or more components of computer device 1200 may perform more tasks described as being performed by one or more components of computer device 1200.

FIG. 13 is a flow chart of an example process for generating a unitary transformation operator for a codebook according to an implementation described herein. In one implementation, the process of FIG. 13 may be performed by computer device 1200. In other implementations, some or all of the process of FIG. 13 may be performed by another device or a group of devices separate and/or possibly remote from or computer device 1200.

The process of FIG. 13 may include selecting a codebook with $2^n$ codewords, each codeword being a sequence of $n$ BPSK symbols. Each codeword may include a particular sequence of $n$ BPSK symbols $|a_0\rangle$ and $|\bar{a}_0\rangle$, with $|a_0\rangle$ and $|\bar{a}_0\rangle$ corresponding to two different binary states. For example, $|a_0\rangle$ may correspond to a first phase of a photon and $|\bar{a}_0\rangle$ may correspond to a second phase of a photon, where the second phase differs from the first phase by 180°. The number of codewords may correspond to $K=2^n$, where $n$ corresponds to the number of symbols per codeword and where $R$ corresponds to the transmission rate in bits per BPSK symbol.

An MPE basis for the codebook can be generated (block 1320). For example, computer device 1100 may calculate an MPE measurement on codebook C in terms of a set of projection operators $W_C=\{w_1, w_2, \ldots, w_q\}$. $W_C$ may form a complete orthogonal-normal (CON) basis of a vector space spanned by the codewords in C.

The codewords of codebook C may be extended into a set of all $2^n$ binary sequences of $|a_0\rangle$ and $|\bar{a}_0\rangle$ (block 1330). For example, computer device 1200 may generate a set $C^T=\{i_1, \ldots, i_q\}$, where $q=2^n$. For example, if $n=3$, $C^T=\{1-a_0, 1-a_0, 1-a_0\}$, $\{1-a_0, 1-a_0, 1+a_0\}$, $\{1-a_0, 1+a_0, 1+a_0\}$, $\{1-a_0, 1+a_0, 1+a_0\}$, $\{1-a_0, 1-a_0, 1-a_0\}$, $\{1+a_0, 1+a_0, 1-a_0\}$, $\{1+a_0, 1+a_0, 1+a_0\}$, $\{1+a_0, 1-a_0, 1+a_0\}$.

The MPE basis may be extended to span the whole space of the $2^n$ binary sequences (block 1340). For example, computer device 1200 may extend basis $W_C$ to span the whole vector space spanned by $C^T$ using Gram-Schmidt orthonormalization. Extended basis $W_{CE}$ may be represented as basis $W=\{w_1, w_2, \ldots, w_{2^n}\}$.

Single mode MPE measurements on $|a_0\rangle$ and $|\bar{a}_0\rangle$ may be represented as $|+\rangle$ and $|-\rangle$ (block 1350). For example, computer device 1200 may represent a single mode MPE measurement on $|a_0\rangle$ and $|\bar{a}_0\rangle$, which may correspond to a detection by a Dolinar receiver or a Sasaki-Hirota receiver, in terms of two projectors on the span of the two BPSK states $|a_0\rangle$ and $|\bar{a}_0\rangle$. The two projectors, $|+\rangle$ and $|-\rangle$, may each correspond to a linear combination of the two pure states $|a_0\rangle$ and $|\bar{a}_0\rangle$. In other words, $|+\rangle=a_0|a_0\rangle+a_0|\bar{a}_0\rangle$ and $|-\rangle=b_0|a_0\rangle+b_0|\bar{a}_0\rangle$.

A single mode measurement basis may be generated based on Kronecker products of $|+\rangle$ and $|-\rangle$ (block 1360). For example, computer device 1200 may construct a complete orthonormal basis $M$ of the vector space spanned by $C^T$ using a Kronecker product of $|+\rangle$ and $|-\rangle$. In other words, $M=\{|m^1_1\rangle, |m^1_2\rangle, \ldots, |m^1_q\rangle\}$, where $|m^1_i\rangle=|+\rangle|+\rangle \ldots |+\rangle|+\rangle$, $|m^1_i\rangle=|+\rangle|+\rangle \ldots |+\rangle|-\rangle$, $|m^2_i\rangle=|+\rangle|-\rangle \ldots |+\rangle|-\rangle$, and $|m^2_i\rangle=|-\rangle|-\rangle \ldots |-\rangle|-\rangle$.

Each codeword of codebook C may be represented in the extended MPE basis to generate an extended MPE unitary matrix (block 1370). For example, each code word $i_k \in C^t$ may be expressed in basis $W$ as
may be generated based on the set of coefficients, where \( \{ w_j | c \} \) corresponds to the \((j,k)^{th}\) coefficient of \( U_{jk} \).

Each codeword of codebook \( C \) may be represented in the single mode measurement basis to generate a single measurement MPE unitary matrix (block 1380). For example, each code word \( \{ c_j \} \) in \( C^R \) may be expressed in basis \( M \) as

\[
| c_j \rangle = \sum_{j=1}^{n} \langle m_j | c_j \rangle | m_j \rangle,
\]

and the single mode measurement MPE unitary matrix \( U_{jk} \) may be generated based on the set of coefficients, where \( \langle m_j | c_j \rangle \) corresponds to the \((j,k)^{th}\) coefficient of \( U_{jk} \).

A unitary transformation operator may be generated by multiplying an inverse of the extended MPE basis unitary matrix with the single mode measurement unitary matrix (block 1290). For example, computer device 1200 may generate unitary transformation operator

\[
U = \frac{1}{\sqrt{n}} \sum_{j=1}^{n} u_{jk} | m_j \rangle | m_k \rangle,
\]

where \( u_{jk} = (U_{jk}^{-1} U_{kk})^{1/2} \) (represented in the \( M \) basis).

FIG. 14 is a flow chart of an example process for generating combined unitary transformation device 810 according to an implementation described herein. In one implementation, the process of FIG. 14 may be performed by computer device 1200. In other implementations, some or all of the process of FIG. 14 may be performed by another device or a group of devices separate and/or possibly remote from or computer device 1100.

The process of FIG. 14 may include determining a unitary transformation operator for a particular codebook (block 1410). For example, computer device 1200 may determine a unitary transformation matrix that has been generated for codebook \( C \) using the process of FIG. 13.

A Dolinar receiver may be represented as a concatenation of a single-mode unitary operator and a photon number resolving (PNR) detector (block 1420). For example, computer device 1200 may represent Dolinar receiver 420 as a single-mode unitary operator and a photon number resolving (PNR) detector. Computer device 1200 may generate a single mode measurement basis to generate a single measurement device 810 and n PNR detectors 820-A through 820-N.

FIG. 15 is a flow chart of an example process for generating an optical circuit for a unitary transformation operator according to an implementation described herein. In one implementation, the process of FIG. 15 may be performed by computer device 1200. In other implementations, some or all of the process of FIG. 15 may be performed by another device or a group of devices separate and/or possibly remote from or computer device 1200.

The process of FIG. 15 may include determining a unitary transformation operator for a particular codebook (block 1510). For example, computer device 1200 may determine a unitary transformation matrix that has been generated for codebook \( C \) using the process of FIG. 13.

The unitary transformation operator may be decomposed into a set of elementary unitary operators representing a beam splitter, a phase shifter, a squeezer, and a Kerr nonlinearity device (block 1520). Any optical unitary transformation on multiple optical modes may be accomplished using a combination of beam splitters, a phase shifter, a squeezer, and any third-order Hamiltonian operator, such as a device that includes a Kerr nonlinearity device. In another implementation, a third-order Hamiltonian operator may be implemented by a photon-number-resolving (PNR) detector.

A phase shifter may include a device, with one optical input and one optical output, which may introduce a variable phase delay into the optical input. In one implementation, a phase shifter may include one or more piezoelectric mirrors. In another implementation, a phase shifter may include a polaroptical phase shifter that is electrically tunable using a liquid crystal driver.

A squeezer may include a device with either one optical input and one optical output or two optical inputs and two optical outputs. A squeezer may reversibly transform an optical state in a manner that enables a measurement of one field quadrature of the optical output, with an accuracy higher than a vacuum noise fluctuation level, at a cost of being able to measure an orthogonal quadrature with a proportionately lower accuracy. Thus, the squeezer may squeeze a quadrature noise variance in one direction, while elongating the variance in another direction. A squeezer may be implemented using, for example, a nonlinear periodically poled lithium niobate (PPLN) or periodically poled potassium titanyl phosphate (PPKTP) crystal and a strong pump laser.

A Kerr nonlinearity device may include a device with two optical inputs and two optical outputs, which exhibits third-order nonlinear susceptibility. A Kerr nonlinearity device may be implemented using an atomic, capable of an electro-magnetically induced transparency, embedded inside a photonic crystal microcavity. The embedded atom may impart a pi-rad-peak phase shift in response to a single photon excitation. A Kerr nonlinearity device may implement an effect called a cross-Kerr effect or cross-phase modulation, and may be used for realizing an all-optical two-qubit control-NOT quantum logic gate.

Each of a beam splitter, phase shifter, squeezer, and Kerr nonlinearity device may be represented with a corresponding Hamiltonian operator. Any Hamiltonian operator may be decomposed to a linear combination of commutation opera-
An optical receiver comprising:

1. An optical receiver comprising:

a unitary transformation operator to:

receive an n-symbol optical codeword associated with a codebook,
the n-symbol optical codeword being based on a Hadamard matrix, and
perform a unitary transformation on the received optical codeword to generate a transformed optical codeword,
the unitary transformation being based on the codebook, and
the unitary transformation operator including \( n \log_2(n/2) \) beamsplitters;

2. The optical receiver of claim 1, where the particular one of the n optical detectors includes a Dolinar receiver.

3. The optical receiver of claim 2, where the Dolinar receiver includes:
a first beam splitter to split an incoming beam into a first beam and a second beam;
a second beam splitter to combine the first beam and the second beam into a combined beam;
a photon detector to perform a photon count on the combined beam;
a processor to select at least the first optical symbol or the second optical symbol based on the photon count; and
a feedback controller to control an amplitude and a phase of the second beam based on the photon count.

4. The optical receiver of claim 1, where the n-symbol optical codeword corresponds to a two symbol codeword, where the unitary transformation operator includes a beam splitter, and
where the n optical detectors include a single photon detector and a Dolinar receiver.

5. The optical receiver of claim 1, where, for an M-ary modulation alphabet, the particular optical symbol corresponds to a particular symbol selected from three or more optical signals.

6. The optical receiver of claim 1, where the n optical detectors perform n projective measurements on the transformed optical codeword.

7. An optical receiver of comprising:
a unitary transformation operator to:
receive an n-symbol optical codeword associated with a codebook, and
perform, based on the codebook, a unitary transformation on the n-symbol optical codeword to generate a transformed optical codeword;
the unitary transformation operator including a combined unitary transformation operator that performs a particular unitary transformation on the n-symbol optical codeword followed by a plurality of single mode unitary transformations on particular optical symbols of the transformed optical codeword;
n optical detectors, a particular one of the n optical detectors being to:
detect a particular optical symbol of the transformed optical codeword, and
buffers include optical paths of different lengths to cause all optical buffers include devices configured to cause all the optical buffers at substantially the same time.

symbols of the temporally encoded codeword to exit the n optical detectors, a particular one of the n optical detectors being to receive the particular optical symbol of the temporally encoded codeword; and a decoder to: construct a codeword based on whether the particular optical symbol corresponds to at least the first optical symbol or a second optical symbol; and decode the constructed codeword into a message using the codebook.

The optical receiver of claim 9, where the n optical detectors include n photon number resolving detectors.

An optical receiver comprising:
a unitary transformation operator to:
receive an n-symbol codeword associated with a codebook,
where the n-symbol optical codeword corresponds to a temporally encoded codeword, and perform, based on the codebook, a unitary transformation on the temporally encoded codeword to generate a transformed optical codeword;
n optical buffers, a particular one of the n optical buffers being to:
detect a particular optical symbol of the transformed optical codeword, and determine whether the particular optical symbol of the transformed optical codeword corresponds to at least a first optical symbol or a second optical symbol; and an optical demultiplexer to select a particular optical symbol of the temporally encoded codeword; and a decoder to:
construct a codeword based on determining whether the particular optical symbol of the transformed optical codeword corresponds to the at least the first optical symbol or the second optical symbol, and decode the constructed codeword into a message using the codebook.

The optical receiver of claim 9, where the n optical buffers include devices configured to cause all the optical symbols of the temporally encoded codeword to be forwarded to the unitary transformation operator substantially at the same time.

An optical receiver comprising:
a unitary transformation operator to:
receive an n-symbol codeword associated with a codebook,
the n-symbol codeword being encoded based on a first order Reed-Muller code, the unitary transformation operator including \( n \log_2(n/2) \) beam splitters, and perform, based on the codebook, a unitary transformation on the encoded n-symbol codeword to generate a transformed optical codeword;
n optical detectors, the n optical detectors including n single photon detectors,
the unitary transformation corresponding to a lossless transformation on a quantum state of the n symbols, and
performing the unitary transformation on the received optical codeword including:
performing a unitary transformation on the received optical codeword; and
performing a plurality of single mode unitary transformations on particular optical symbols of the transformed optical codeword;
determining, by the optical receiver and for the n transformed symbols, whether a particular one of the n transformed symbols corresponds to at least a first optical symbol or a second optical symbol; and
generating, by the optical receiver, an electrical codeword, corresponding to the optical codeword, based on determining whether the particular one of the n transformed symbols corresponds to the at least the first optical symbol or the second optical symbol.

19. The method of claim 18, where determining whether the particular one of the n transformed symbols corresponds to the at least a first optical symbol or the second optical symbol includes:
determining a quantity of photons detected for the particular one of the n transformed symbols, and
determining whether the particular one of the n transformed symbols corresponds to the at least a first optical symbol or the second optical based on the quantity of photons.

20. A method comprising:
receiving, by an optical receiver, an optical codeword associated with a codebook,
the optical codeword being encoded based on a first order Reed-Muller code, and
the optical codeword comprising n symbols;
performing, by the optical receiver, a unitary transformation on the received optical codeword to generate a transformed optical codeword comprising n transformed symbols,
the unitary transformation corresponding to a lossless transformation on a quantum state of the n symbols, and
the unitary transformation including n*\log_2(n/2) beam splitting operations, and
determining, for the n transformed symbols, whether a particular one of the n transformed symbols corresponds to at least a first optical symbol or a second optical symbol,
determining whether the particular one of the n transformed symbols corresponds to a first optical symbol or a second optical symbol is performed by n single photon detectors in combination with a Dolinar receiver or a Kennedy receiver triggered by a first one of the n single photon detectors that detects a photon; and
generating, by the optical receiver, an electrical codeword, corresponding to the optical codeword, based on the determination.

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