Advanced Relay Design and Technology for Energy-Efficient Electronics

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As the era of traditional Complementary-Metal-Oxide-Semiconductor (CMOS) technology scaling is coming to an end, continual improvements in integrated-circuit (IC) performance and cost per function are becoming difficult to achieve without increasing power density. This necessitates the investigation of alternate device technologies that surmount the fundamental CMOS energy-efficiency limit and hence enable ultra-low-power ICs. To that end, a nanoelectro-mechanical (NEM) relay technology is promising, because of its immeasurably low offstate leakage current and abrupt turn-on behavior, which provide for zero static power consumption and potentially very low dynamic power consumption. In this dissertation, relay design and process technology improvements, which led to the successful demonstration of relay-based digital IC building blocks, are discussed from both device- and circuit-level perspectives. A non-volatile (NV) memory relay design that can enable embedding of NV memory with relay-based logic circuits is also discussed. In addition, multielectrode relays that can lead to smarter design and compact implementation of zero-leakage digital integrated circuits are discussed.
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Advanced Relay Design and Technology for Energy-Efficient Electronics

By

Jaeseok Jeon

A dissertation submitted in partial satisfaction of the

requirements for the degree of

Doctor of Philosophy

in

Engineering – Electrical Engineering and Computer Sciences

in the

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of the

University of California, Berkeley

Committee in charge:

Professor Tsu-Jae King Liu, Chair

Professor Elad Alon

Professor Liwei Lin

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by

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Abstract

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Doctor of Philosophy in Engineering - Electrical Engineering and Computer Sciences
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Professor Tsu-Jae King Liu, Chair

As the era of traditional Complementary-Metal-Oxide-Semiconductor (CMOS) technology scaling is coming to an end, continual improvements in integrated-circuit (IC) performance and cost per function are becoming difficult to achieve without increasing power density. This necessitates the investigation of alternate device technologies that surmount the fundamental CMOS energy-efficiency limit and hence enable ultra-low-power ICs. To that end, a nano-electro-mechanical (NEM) relay technology is promising, because of its immeasurably low off-state leakage current and abrupt turn-on behavior, which provide for zero static power consumption and potentially very low dynamic power consumption.

In this dissertation, relay design and process technology improvements, which led to the successful demonstration of relay-based digital IC building blocks, are discussed from both device- and circuit-level perspectives. A non-volatile (NV) memory relay design that can enable embedding of NV memory with relay-based logic circuits is also discussed. In addition, multi-electrode relays that can lead to smarter design and compact implementation of zero-leakage digital integrated circuits are discussed.
Dedicated to my family
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Chapter 1

Introduction

Over the last 50 years, the evolution of information-processing technology has transformed every aspect of our lives -- the way we think, work, communicate, commute, and entertain ourselves. We use smart phones to communicate, computers at work, and digital cameras to keep alive our special memories. However, as electronic products have become a pervasive part of our daily lives, available any place at any time, reducing their energy consumption has become a major challenge. Take the data center, for example: in the year of 2000, the total electricity consumed for all data centers around the world (including that used for the cooling and auxiliary equipment) was 0.5% of total electricity consumption in the world. The percentage was doubled to 1% in the year of 2005, as shown in Figure 1.1(a), [1] and roughly octupled to 3.7% (~195 TWh) in the year of 2008 [2]. This represents a significant increase over the past decade, considering the fact that it is now comparable to the total electricity consumption of Australia (~220 TWh), as shown in Figure 1.1(b) [2].

Since the integrated circuit (IC) was invented, continual improvements in IC performance and cost per function have enabled more capable and affordable electronic products. However, they are no longer achievable today without increasing power density (Figure 1.2), as traditional Complementary-Metal-Oxide-Semiconductor (CMOS) technology scaling has essentially ended.

![Figure 1.1: (a) Adapted from [1]: Total electricity usage of all data centers in the world in 2000 vs. 2005 (the electricity used for cooling and auxiliary equipment is included). Note that total electricity consumption in the world was increased from 13,238 TWh in 2000 to 15,747 TWh in 2005.](image)
At the 130 nm CMOS technology node and beyond, the power-supply voltage ($V_{DD}$) at which the CMOS chip operates has not been reduced as aggressively as the device pitch (Figure 1.3(a)), e.g. $V_{DD} = 1.3 \text{ V}$ [5] vs. 1 V [6] for the 130 and 32 nm nodes, respectively. This is because the threshold ($V_{TH}$) of a CMOS transistor (i.e. the voltage at which the transistor turns on and off) cannot be scaled down any lower, without incurring significant increase in transistor off-state leakage and hence increase in static power dissipation (Figure 1.3(b)).

As power consumption (and resulting heat generation) becomes more exacerbated with newer generations of the CMOS chip, parallel-computing has become widely-employed in microprocessors [8]. For example, a dual-core microprocessor has two parallel processing units, each of which is designed to run at a slower clock speed, in order to reduce its energy per operation; the overall system performance can be recovered by operating both of the processors in parallel (Figure 1.4).
The paradigm shift to multi-core computing, however, inherently has a fundamental problem at the device-level. Take the CMOS transistor, for instance. As $V_{DD}$ of a transistor is reduced, the active energy consumed to switch capacitors ($E_{ACTIVE}$) decreases at the expense of a longer time to perform logical operations ($t_{DELAY}$):

$$E_{ACTIVE} = \alpha f L_D C V_{DD}^2,$$

$$t_{DELAY} = \frac{f L_D C V_{DD}^2}{2 I_{ON}},$$

where $\alpha$ is the activity factor, $f$ is the fan-out, $L_D$ is the logic depth, $C$ is the capacitance per stage, and $I_{ON}$ is the on-state current. The $V_{DD}$ reduction, however, forces the transistor to dissipate even higher passive energy ($E_{PASSIVE}$) due to increasing off-state leakage ($I_{OFF}$):

$$E_{PASSIVE} = f L_D I_{OFF} V_{DD} t_{DELAY}.$$
As a result, the minimum point where $E_{\text{ACTIVE}}$ and $E_{\text{PASSIVE}}$ balance each other out yields the fundamental energy-efficiency limit, as shown in Figure 1.5(a). The parallel computing methodology would eventually become ineffective, because addition of a processor core (that operates albeit at lower throughput) would not lead to any lower energy consumption per logic operation, as Figure 1.5(b) shows. This will necessitate alternate device technologies that surmount the fundamental CMOS energy-efficiency limit and hence enable emerging, ultra-low-power IC applications. To that end, a nano-electro-mechanical (NEM) relay technology is the closest to ideal, because of its immeasurably low off-state leakage and abrupt turn-on behavior, which provide for zero static power consumption and potentially very low dynamic power consumption. A scaled relay, in principle, can be implemented to switch on or off at very low voltages (< 100 mV) and hence to have a higher energy-efficiency ($\approx 10^\times$ or more) than a similarly-sized CMOS transistor [9].

Figure 1.6(a) shows a simplified diagram of a mechanical relay: In the off-state, no current can flow because of the air gap that separates the source electrode from the drain electrode, as

![Figure 1.6: (a) Diagram of a three-terminal mechanical relay. The air gap between the source and drain electrodes is what leads to zero off-state leakage. The electrical contact between the source and drain is made by the electrostatic force induced between the gate and source electrodes. (b) Measured $I_{DS}-V_{GS}$ characteristic of a relay fabricated in the Berkeley Microfabrication Laboratory. The relay turns on or off abruptly with a small change in the gate voltage.](image)
confirmed by measured $I_{DS}-V_G$ characteristic in Figure 1.6(b). The relay turns on abruptly (less than 0.1 mV/decade) when the electrostatic force induced between the gate and source electrodes brings the source into contact with the drain.

This Ph.D. dissertation aims to address challenges for achieving a NEM relay technology that can provide a potential pathway for achieving truly “greener” computing via reducing carbon footprint of information-processing systems. In particular, relay design and process technology improvements, which led to the successful demonstration of relay-based digital IC building blocks, are discussed from both device- and circuit-level perspectives. In addition, multi-electrode relays that can lead to more efficient design and implementation of ultra-low-power digital electronics are discussed.

In Chapter 2, improvements to the prototype four-terminal (4-T) relay design are investigated to resolve the parasitic issues inherent in the original design, namely a relatively weak body bias effect, undesirable influence of source/drain bias voltages on the gate switching voltages, and parasitic actuation by channel-to-body potential.

In Chapter 3, an electrostatically actuated 4-T relay is demonstrated to function as a memory cell. This indicates promise for embedding non-volatile memory with relay-based logic circuits, without incurring additional fabrication cost.

In Chapter 4, a see-saw relay design is proposed and demonstrated to provide for perfectly complementary switching behavior that is symmetric about $V_{DD}/2$. Also, the experimental results demonstrate that the complementary see-saw relay design is versatile for mechanically implementing various logic functions and a latch function with a single structure.

In Chapter 5, multi-gate, multi-source/drain relays are proposed and demonstrated, in order to provide an evolutionary pathway for compact implementation of ultra-low-power digital electronics (e.g. table-top supercomputer).

In Chapter 6, the key results and contributions of this work are summarized, and future research directions are briefly suggested.
References


Chapter 2

Four-Terminal Relay Design Improvements

Abstract: The first prototype electrostatically actuated four-terminal (4-T) relays suffer from a relatively weak body bias effect, undesirable influence of source/drain bias voltages on the gate switching voltages, and parasitic actuation by channel-to-body potential. In this chapter, improvements to the 4-T relay design are investigated to resolve these issues.

2.1. Introduction

Transistor off-state leakage limits the degree to which the energy per operation can be lowered in Complementary-Metal-Oxide-Semiconductor (CMOS) digital integrated circuits (ICs) [1]. For this reason, nano-electro-mechanical (NEM) relays, which have zero off-state leakage, have been proposed for ultra-low-power digital IC applications [2]. Because a relay has abrupt switching characteristics (less than 0.1 mV/decade [3]), in principle it can be made to operate with lower supply voltage ($V_{DD}$) than CMOS transistors, for lower dynamic power consumption as well as zero static power consumption. Recently, a reliable micro-relay technology has been demonstrated [4], and a four-terminal (4-T) relay design has been introduced for digital logic applications [3]. The purpose of the fourth (“body”) terminal is to provide a means to tune the gate switching voltages of the relay for low-voltage operation [3]. Basic digital building-block ICs, such as carry-generation circuit, oscillator, and adder, have been demonstrated with 4-T relays and passive circuit elements [5], [6], [7]. A scaled 4-T relay technology shows promise for breaking the lower energy limit for CMOS technology – by more than one order of magnitude – at throughputs up to 100 MOPS and comparable layout area [8].

2.2. 4-T Relay Design

The first prototype 4-T relay design reported in [3] (replicated in Figure 2.1) suffers from a relatively weak body bias effect and undesirable influence of source/drain bias voltages on the gate switching voltages, due to significant overlap between the actuated gate electrode and source/drain electrodes resulting in unwanted parasitic actuation effects. An improved 4-T relay design shown in Figure 2.2 is demonstrated to resolve these issues.
The device operating principle is the same as for the first prototype 4-T relay design described in [3]: As the voltage difference between the movable p+ polycrystalline-Si$_{0.4}$Ge$_{0.6}$ electrode and the underlying Tungsten (W) actuation electrode is increased above the turn-on threshold voltage, the electrostatic force becomes sufficiently large to bring the W channel layer into contact with the W source and drain electrodes (which are coplanar with the actuation electrode) so that current can flow between these two electrodes; the gate voltage corresponding to the turn-on threshold voltage is called the “pull-in” voltage, $V_{\text{PI}}$.

Figure 2.1: Isometric view of the prototype 4-T relay structure and schematic cross-sections in the off- and on-states [3]. In the off-state, no Direct-Current (DC) current can flow between the source and drain electrodes, because an air gap separates the channel from the source/drain electrodes. In the on-state, electrostatic force between the movable gate electrode and the underlying body electrode brings the channel into contact with the source and drain electrodes.

The device operating principle is the same as for the first prototype 4-T relay design described in [3]: As the voltage difference between the movable p+ polycrystalline-Si$_{0.4}$Ge$_{0.6}$ electrode and the underlying Tungsten (W) actuation electrode is increased above the turn-on threshold voltage, the electrostatic force becomes sufficiently large to bring the W channel layer into contact with the W source and drain electrodes (which are coplanar with the actuation electrode) so that current can flow between these two electrodes; the gate voltage corresponding to the turn-on threshold voltage is called the “pull-in” voltage, $V_{\text{PI}}$.

Figure 2.2: (a) Isometric view of the improved 4-T relay structure and schematic cross-sections of the channel region in the off- and on-states, showing the various relay design parameters. The W channel layer is attached underneath the poly-Si$_{0.4}$Ge$_{0.6}$ only in the “hammerhead” portion (7.5 μm by 2 μm). In the off-state, the channel layer is separated from the source/drain electrodes by an air gap, so that no current can flow between the source and drain electrodes. In the on-state, the moveable structure is actuated downward (by electrostatic force between the movable SiGe electrode and the underlying W actuation electrode) so that the channel contacts the source and drain electrodes.
As the voltage difference between the poly-Si$_{0.4}$Ge$_{0.6}$ electrode and the underlying actuation electrode is decreased back down to be below the turn-off threshold voltage, the spring restoring force of the poly-Si$_{0.4}$Ge$_{0.6}$ folded-flexures becomes sufficiently large to break the contact between the channel and source/drain electrodes so that no current can flow; the gate voltage corresponding to the turn-off threshold voltage is called the “release” voltage, $V_{RL}$. Note that a gate-insulating layer (40 nm of Al$_2$O$_3$) electrically isolates the poly-Si$_{0.4}$Ge$_{0.6}$ electrode from the channel to prevent DC current flow between the poly-Si$_{0.4}$Ge$_{0.6}$ and the source/drain electrodes when the relay is in the on-state.

### 2.2.1. Relay Fabrication Process

Improved 4-T relays were fabricated in the Berkeley Microfabrication Laboratory using the four-mask process illustrated in Figure 2.3. Note that all photolithography steps were performed using a 5X Chrome reticle (6" X 6" X 0.25") with an anti-reflective coating in an ASML Deep-Ultra-Violet (DUV) 5500/90 stepper that can resolve 250 nm features.
A 200-nm-thick substrate-insulating layer of Silicon Dioxide (SiO$_2$) was thermally grown at 1000 ºC in steam ambient on 150-mm-diameter Boron-doped p-type (1-0-0) low-resistivity (about 20 Ω·cm) Silicon wafers. An Aluminum Oxide (Al$_2$O$_3$) layer deposited using an atomic layer deposition (ALD) reactor (Picosun SUNALE™ R-150) was used for the substrate-coating (100 nm) and gate-dielectric (40 nm) layers. The ALD processing temperature of 300 °C used to yield relatively low tensile stress (about 200 MPa) within the deposited film leads to a growth rate of approximately 0.9 nm per cycle [11], [12] and film thickness uniformity less than ± 1 % across the wafer and wafer-to-wafer. The pulsing and purging times of both Trimethylaluminum (TMA) and H$_2$O precursors were set to 0.1 and 4 seconds, respectively, in order to allow sufficient time for the self-terminating gas-solid reaction [13]. This Al$_2$O$_3$ layer can serve as an excellent substrate insulator, because it is highly resistant to HF-vapor release etching [14] and is known to provide good adhesion to W without any intermediate glue layer [15], [16]. In addition, ALD Al$_2$O$_3$ is a good gate-insulating material in that it shows reasonably low gate leakage and relatively high dielectric breakdown strength (larger than 5 MV/cm); For example, a 12-nm-thick ALD Al$_2$O$_3$ layer shows gate leakage currents less than 1 nA/cm$^2$, when an electric field of 2 MV/cm is applied [17].

**Figure 2.3:** Four-mask fabrication process for the improved 4-T relay. (a) W body, drain, and source electrodes formed on the Al$_2$O$_3$-coated substrate. (b) 1st sacrificial low-temperature oxide (LTO) layer deposition, followed by contact area definition. (c) 2nd sacrificial LTO layer deposition, followed by W channel formation. (d) Gate oxide (Al$_2$O$_3$) deposition. (e) Gate layer (p+ poly-Si$_{0.4}$Ge$_{0.6}$) deposition followed by LTO deposition and gate patterning. (f) Release etching in vapor-HF.
The W material deposited by DC magnetron sputtering (base pressure $\approx 1 \times 10^{-7}$ Torr, process pressure $\approx 10$ mTorr, and DC power = 2 kW) was used as the source, drain, body, and channel material. It has excellent resistance to physical wear due to its relatively high hardness [18]; Vickers hardness of Tungsten (approximately 3.42 GPa) is higher than that of most metals shown in the periodic table (e.g. $\approx 0.17$ GPa for Aluminum, $\approx 0.87$ GPa for Tantalum, and $\approx 0.97$ GPa for Titanium) [19], [20]. In addition, it has high resistance to vapor-phase HF release etching [21]. The SF$_6$ dry etch plasma chemistry (85 sccm of SF$_6$, chamber pressure = 10 mTorr, bias peak power = 100 W, and source peak power = 1000 W) used to pattern the W film provides an etch selectivity to the underlying Al$_2$O$_3$ substrate insulator (greater than 100:1) and to the sacrificial SiO$_2$ (about 3:1).

Undoped low-temperature-oxide (LTO deposited at 400 °C and 300 mTorr), about 200 nm thick in the actuation region and about 100 nm thick in the contact regions, was used as the sacrificial material. Note that the sacrificial oxide thickness translates to an air gap in the actuation and contact regions of the relay, upon removal of the sacrificial oxide. (This air gap formation is what leads to zero off-state leakage current.)

*In-situ* boron-doped p-type poly-Si$_{0.4}$Ge$_{0.6}$ deposited by low-pressure chemical vapor deposition (LPCVD) at 410 °C and 600 mTorr was used as the structural gate material. A thin layer (less than 5 nm) of amorphous Silicon (a-Si) was deposited in between the poly-Si$_{0.4}$Ge$_{0.6}$ and the sacrificial oxide (by flowing Disilane at 410 °C and 300 mTorr). This layer not only promotes the adhesion of the poly-Si$_{0.4}$Ge$_{0.6}$ to the underlying gate oxide, but also seeds film growth [22].

Prior to release etching, a Xenon Dichloride (XeCl$_2$) excimer laser ($\lambda = 308$ nm) pulse (400 mJ/cm$^2$, 38 ns) was applied to the poly-Si$_{0.4}$Ge$_{0.6}$ gate electrode through a 100-nm-thick SiO$_2$ hardmask layer, in order to reduce the impact of large negative stress gradient within the film.

![Figure 2.4](image)

Figure 2.4: (a) The $V_{\text{PI}}$ values (measured at room temperature under N$_2$ purge at atmospheric pressure) decrease with increasing energy density of a single laser pulse (38 ns). (b) Measured $I_{\text{DS}}-V_{\text{G}}$ characteristics of the fabricated 4-T relay with vs. without the application of the laser pulse. $V_B$, $V_D$, and $V_S$ were biased at 0.5 V, 0 V, and 0 V, respectively. Note that negative strain gradient within the poly-Si$_{0.4}$Ge$_{0.6}$ was reduced substantially, resulting in smaller $T_{\text{ACT}}$ and hence lower actuation voltages.
[23], [24] and hence achieve lower operating voltages. This negative stress gradient causes the top portion of the poly-Si$_{0.4}$Ge$_{0.6}$ film to expand more than the less-compressive (or more-tensile) bottom portion, i.e. it induces negative strain gradient through the film thickness. The movable structure is gradually buckled upward from its anchors toward its geometric center (it appears like an open umbrella), and as a result, $T_{ACT}$ is rendered non-uniform across the actuation area (being the largest at the center).

As shown in Figure. 2.4, measured $V_{PL}$ and $V_{RL}$ of the laser-annealed relays decrease with increasing energy density of the laser pulse, because of reduction in effective $T_{ACT}$. Note that the negative strain gradient effect is diminished, because compressive stress within the top portion is relieved [22], [23].

Finally, the dies were released in vapor-phase HF -- the surface temperature of the dies was kept to 50 ºC during the release etch step, so that the reaction by-product (H$_2$O) can vaporize more quickly, thereby preventing release stiction.

### 2.2.2. Dependence of Gate Switching Voltage on Body Bias

Measured $I_{DS}$-$V_G$ characteristics of a 4-T relay are shown in Figure 2.5, for operation with the poly-Si$_{0.4}$Ge$_{0.6}$ electrode as the gate and the underlying W electrode as the body. Note that $V_{PL}$ can be reduced very effectively by adjusting the body bias, in order to allow for operation with reduced gate-voltage swing.

**Figure 2.5:** Measured $I_{DS}$-$V_G$ characteristics of a fabricated 4-T relay at room temperature under N$_2$ purge at atmospheric pressure, for various body biases. Zero off-state leakage and abrupt switching behavior (less than 1 mV/decade) are observed. The on-state resistance ($R_{ON}$) values are 5.5 kΩ, 3.3 kΩ, and 9.1 kΩ at $V_{G_{SiGe}} = 1.2 \cdot V_{PL}$ for $V_{B_{W}}$ of -2.5 V, 0 V, and 2.5 V, respectively. The hysteretic switching behavior is due to pull-in mode operation (because $T_{CONTACT} > T_{ACT} / 3$) as well as surface adhesion forces which increase with decreasing $R_{ON}$. The variation in $R_{ON}$ is partly attributed to oxidation of the channel and source/drain electrode surfaces over time. The measurements were made firstly for $V_{B_{W}} = 0$ V, then for $V_{B_{W}} = -2.5$ V, finally for $V_{B_{W}} = 2.5$ V.
Ideally, a change in the $V_B$ should result in commensurate changes to the gate switching voltages $V_{PI}$ and $V_{RL}$. Also, the $V_{PI}$ and $V_{RL}$ values for operation with the poly-Si$_{0.4}$Ge$_{0.6}$ electrode as the gate (and the W electrode as the body) should be the same as for operation with the W electrode as the gate (and the poly-Si$_{0.4}$Ge$_{0.6}$ as the body), to allow for versatility in digital circuit design [3]. Neither of these was found to be the case for the first prototype 4-T relay design: a 1 V change in $V_B$ resulted in an about 0.5 V change in $V_{PI}$ [3], and $V_{PI}$ for operation with the W electrode as the gate is considerably higher (by approximately 50 %) than for operation with the poly-Si$_{0.4}$Ge$_{0.6}$ electrode as the gate (Figure 2.6), due to the relatively small percentage of the actuated region of the poly-Si$_{0.4}$Ge$_{0.6}$ electrode that overlaps with the underlying W electrode. To address these issues, the percentage overlap between the actuated region of the poly-Si$_{0.4}$Ge$_{0.6}$ electrode and the underlying W electrode is increased to be nearly 100 % in the improved 4-T relay design. Note that the area of the overlap between the poly-Si$_{0.4}$Ge$_{0.6}$ and the source/drain electrodes is reduced to 8 $\mu$m$^2$, which is much smaller than the poly-Si$_{0.4}$Ge$_{0.6}$-to-W overlap area of about 1600 $\mu$m$^2$. Since the capacitance between the poly-Si$_{0.4}$Ge$_{0.6}$ and the source/drain

![Figure 2.6: $V_{PI}$ for operation with the W electrode as the gate (15.9 V) is higher (by ~47 %) than that for operation with the poly-Si$_{0.4}$Ge$_{0.6}$ electrode as the gate (10.85 V). The data were taken at room temperature under N$_2$ purge at atmospheric pressure.](image)

<table>
<thead>
<tr>
<th>Parallel-Plate Capacitance</th>
<th>Prototype 4-T Design</th>
<th>Improved 4-T Design</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Si$<em>{0.4}$Ge$</em>{0.6}$ to W</td>
<td>Si$<em>{0.4}$Ge$</em>{0.6}$ to Source/Drain</td>
</tr>
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<td>off-state</td>
<td>19.57 fF</td>
<td>13.39 fF</td>
</tr>
<tr>
<td>on-state</td>
<td>38.45 fF</td>
<td>44.43 fF</td>
</tr>
</tbody>
</table>

Table 2.1: Calculated parallel-plate capacitance values for the first prototype and improved 4-T relay designs. In the improved design, parasitic electrostatic force in the source/drain regions is relatively small, because the on-state capacitance between the poly-Si$_{0.4}$Ge$_{0.6}$ and source/drain electrodes is much smaller than that between the poly-Si$_{0.4}$Ge$_{0.6}$ and W electrodes. Note that the ratio of the on-state to off-state capacitances is approximately 2.49 and 55.58 for the prototype and improved designs, respectively.
electrodes is much smaller than that between the poly-Si_{0.4}Ge_{0.6} and the W electrode (as shown in Table 2.1), parasitic electrostatic force in the source/drain regions is relatively small. As a result, the gate switching voltage changes directly with body bias \( (i.e. \frac{dV_{PI}}{dV_B}) \), as shown in Figure 2.7.

The \( V_{PI} \) and \( \frac{dV_{PI}}{dV_B} \) values for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate are slightly lower than for operation with the W electrode as the gate, because of a small amount of parasitic actuation between the poly-Si_{0.4}Ge_{0.6} electrode and the source/drain electrodes. Specifically, the effective actuation area for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate is slightly larger than for operation with the W electrode as the gate, so that \( V_{PI} \) is slightly lower for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate. However, this also means that the percentage overlap between the gate and body electrodes is slightly smaller for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate, so that \( \frac{dV_{PI}}{dV_B} \) is slightly smaller for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate.

2.2.3. Dependence of Gate Switching Voltage on Drain Bias

Ideally, a change in the \( V_D \) should not affect the gate switching voltages. This was not the case for the first prototype 4-T relay design [3]: a 1 V change in \( V_D \) resulted in an approximately 0.25 V change in \( V_{PI} \), due to significant overlap (roughly 37%) between the actuated region of the poly-Si_{0.4}Ge_{0.6} electrode and the source/drain electrodes. Since this overlap area is dramatically reduced (to about 0.5%) in the improved 4-T relay design, \( V_{PI} \) does not change significantly with \( V_D \), as shown in Figure 2.8. \( \frac{dV_{PI}}{dV_D} < 0 \) for operation with the W electrode as the gate, because the drain electrode is located on the same side of the actuation gap as the gate in this case, so that an increase in \( V_D \) helps to actuate the poly-Si_{0.4}Ge_{0.6} electrode downward. \( \frac{dV_{PI}}{dV_D} > 0 \) for operation with the poly-Si_{0.4}Ge_{0.6} electrode as the gate, because the drain electrode is located on
the opposite side of the actuation gap as the gate in this case, so that an increase in \( V_D \) reduces the electrostatic force exerted on the poly-Si\(_{0.4}\)Ge\(_{0.6}\) electrode.

2.2.4. Parasitic Actuation by Channel-to-Body Potential

In the prototype 4-T relay, the W channel interposed between the gate and body electrodes is unnecessarily large [3]; the area of overlap between the channel and body electrodes (170 \( \mu \text{m}^2 \)) is comparable to that between the gate and body (450 \( \mu \text{m}^2 \)). This is undesirable, because the parasitic electrostatic force is induced between the channel and body electrodes, when a voltage \( (V_{DD}) \) is applied between them. This force keeps the relay in the on-state (\( i.e. \) causing in-use stiction), even if the gate-to-body voltage is no longer applied. In the improved 4-T relay design, therefore, the W channel layer was removed from the gate-to-body overlap area to remove parasitic actuation. (as Figure 2.2(a) shows, it is attached underneath the poly-Si\(_{0.4}\)Ge\(_{0.6}\) only in the hammerhead portion.)

2.3. Revised 4-T Relay Design

Experimental measurements of the improved 4-T relays are the basis for the revised 4-T relay layout shown in Figure 2.9. In particular, the improved 4-T relay design is mechanically-refined, such that the cantilever springs are now replaced with the symmetric flexure-beam springs to relieve growth stress build-up within the poly-Si\(_{0.4}\)Ge\(_{0.6}\) microstructures [3], [4], [26]. To ensure good electrostatic integrity (\( i.e. \) symmetric actuation, no dependence of \( V_{PI} \) on source/drain bias, and a commensurate change to \( V_{PI} \) with a change in body-bias), the revised 4-T relay is designed such that the gate-to-source/drain capacitance is less than 2.5 \% of the gate-to-body capacitance. Note that the channel is still interposed between the gate and body electrodes; This is to maintain

![Figure 2.8: The measured \( V_{PI} \) values show negligible dependence on the drain. All measurements were made at room temperature under N\(_2\) purge at atmospheric pressure.](image-url)
the original device footprint that was used for the demonstration of the relay-based IC building blocks [5]. To allow only minimal parasitic actuation, therefore, the channel-to-body overlap area is minimized to 2 \( \mu \text{m}^2 \) (c.f. gate-to-body overlap area is about 750 \( \mu \text{m}^2 \)). In addition, the as-fabricated contact-gap-to-actuation-gap thickness ratio (\( T_{\text{CONTACT}} \) to \( T_{\text{ACT}} \)) was chosen to be 0.5. This ratio should be smaller than one third in order to minimize the hysteric switching behavior -- by allowing the relay to operate in non-pull-in mode. Otherwise, \( V_{\text{DD}} \) scaling is limited by the release voltage of the relay. To achieve most energy-efficient relay operation, however, the relay should operate in pull-in mode (with a \( T_{\text{CONTACT}} \)-to-\( T_{\text{ACT}} \) ratio of 0.7 to 0.8) [25].

To validate the new relay design, Finite-Element-Method (FEM) analysis was performed using a multi-physics simulation software (COVENTORWARE™ DESIGNER [27] and ANALYZER [28]). Figures 2.10(a) shows the simulated \( V_{\text{PI}} \) value of the 4-T relay for operation with the poly-Si electrode as the gate and the underlying W electrode as the body. Note that poly-Si (Young’s modulus of 158 GPa) was used to model the poly-Si_{0.4Ge0.6} layer, as the latter material is unavailable in the Material Properties Database in COVENTORWARE™. The simulated \( V_{\text{PI}} \) value of the relay for operation with the poly-Si electrode as the gate is consistent with that for operation with the underlying W electrode as the gate, as shown in Figure 2.10(b).

Figure 2.11(a) shows \( V_{\text{PI}} \) of the relay for operation with the poly-Si electrode as the gate. Figure 2.11(b) confirms minimal dependence of the gate switching voltage of the revised 4-T relay upon
drain bias \((dV_{PI} / dV_D \approx 0)\), and Figure 2.11(c) verifies effective adjustment of \(V_{PI}\) of the relay with body-bias \(i.e.\) a commensurate change to \(V_{PI}\) with a change in body-bias).

Figure 2.12(a) shows the simulated \(V_{PI}\) value of the relay for operation with the poly-Si electrode as the gate. Figure 2.12(b) confirms that the relay operation is negligibly affected by the parasitic electrostatic force induced by the channel-to-body potential.

**Figure 2.10:** \(T_{ACT} = 200\) nm, \(T_{CONTACT} = 100\) nm, \(T_{GOX} = 40\) nm, \(T_{ELECTRODE} = T_{CHANNEL} = 50\) nm, \(T_{SUB\_OX} = 80\) nm, and \(H_{POLY\_SI} = 1\) \(\mu\)m are the vertical dimensions used for this work. The W channel and Si substrate were left floating. (a) The relay is actuated downward by \(-63\) nm \((\approx T_{CONTACT} / 3)\) at \(V_{POLY\_SI} = 4.69\) V, right before it turns *on* abruptly. \(V_D, V_S,\) and \(V_{B\_W}\) were set to 0 V. (b) When \(V_{G\_W}\) is increased to about 4.75 V, the relay is on the verge of being pulled-in. \(V_D = V_S = V_{POLY\_SI} = 0\) V.

**Figure 2.11:** The vertical dimensions of the relay are \(T_{ACT} = 130\) nm and \(T_{CONTACT} = 90\) nm; the other vertical dimensions are as described in Figure 2.9. Both the W channel and the Si substrate were left floating. The source was biased at 0 V. (a) The relay pulls-in at \(V_{POLY\_SI} = \sim2.72\) V. The relay is about to turn *on* at the downward displacement of \(-34\) nm \((\approx T_{ACT} / 3)\) due to the pull-in mode operation. \(V_D = V_{B\_W} = 0\) V.
The revised 4-T relays fabricated in the Berkeley Microfabrication Laboratory have been demonstrated to have good electrostatic integrity [29]; in fact, these relays were used to demonstrate the operation of an one-bit adder (12 relays) [29] as well as a full (7:3) compressor (98 relays) [30].
2.4. Summary

Improvements in 4-T relay design to maximize the percentage overlap between the actuated region of the movable electrode and the underlying actuation electrode, and to minimize the overlap between the movable electrode and the source/drain electrodes, are demonstrated to provide for a strong body bias effect with equally effective relay switching using either the movable electrode or the underlying actuation electrode as the gate, as well as dramatically reduced drain bias effect on the gate switching voltage. Although there is still room for further improvement, for example, to increase layout compactness and to prevent pull-in of the entire actuated portion of the poly-Si$_{0.4}$Ge$_{0.6}$ electrode, this work represents a significant step forward in the development of 4-T relays for ultra-low-power digital integrated circuit applications.
2.5. References


Chapter 3
Four-Terminal Relay Design and Operation for Embedded Memory Applications

Abstract: An electrostatically actuated four-terminal (4-T) micro-relay is demonstrated to function as a memory cell. This indicates promise for embedding non-volatile memory with relay-based logic circuits, without incurring additional fabrication cost.

3.1. Introduction

Complementary-Metal-Oxide-Semiconductor (CMOS) technology scaling is challenged by power density constraints, due to a slowdown in voltage scaling and limitations in cooling technology [1]. The root cause of this CMOS power crisis is transistor off-state leakage current ($I_{\text{OFF}}$), which increases exponentially with decreasing threshold voltage. This fundamental issue can be circumvented altogether by using mechanical switches which have zero $I_{\text{OFF}}$ and abrupt on/off switching behavior [2], [3]. For efficient implementation of digital integrated circuits with nano-electro-mechanical (NEM) switches, a four-terminal (4-T) relay design is necessary [4], [5]. Recent developments to improve device yield and endurance (greater than $10^9$ on/off switching cycles) [6] enabled the demonstration of functional monolithically integrated digital building blocks (logic, dynamic memory, and clocking structures) implemented with 4-T relays [7], [8], [9]. For many applications, e.g. system on chip, the capability to implement non-volatile memory (NVM) in a logic process (i.e. without significant additional fabrication cost) is desirable. Therefore, the capability of a 4-T relay to function as a NVM cell is investigated in this chapter.

3.2. Memory Relay Design

Figure 3.1(a) is a scanning electron micrograph of a programmable 4-T relay that can be fabricated using the same process as described in Chapter 2.2.1 for 4-T logic relays. If the voltage applied between the Tungsten (W) gate electrode and movable poly-Si$_{0.4}$Ge$_{0.6}$ body ($V_{\text{GB}}$) is greater than the “pull-in” voltage ($V_{\text{PI}}$), then the channel (attached underneath the poly-Si$_{0.4}$Ge$_{0.6}$ body in the “hammerhead” region via an intermediary Al$_2$O$_3$ dielectric layer) is brought into contact with the W source and drain electrodes so that direct current can flow between these electrodes, i.e., the relay is turned on. If $V_{\text{GB}}$ is less than the “release” voltage, $V_{\text{RL}}$, then an air gap separates the channel from the source/drain electrodes so that no direct current
can flow, i.e., the relay is turned off. As illustrated in Figure 3.1(b), the as-fabricated thickness of the gap in the W source/drain contact regions, $T_{\text{CONTACT}}$, is smaller than the as-fabricated thickness of the gap in the actuation region, $T_{\text{ACT}}$. This “dimpled” contact design is beneficial to precisely define the area of the contacting regions and to reduce the turn-on delay.

The relay switching voltages, $V_{\text{PI}}$ and $V_{\text{RL}}$, can be affected by electronic charge within the dielectric layer [4]. Therefore, binary information can be stored in the form of trapped charge, similarly as in Silicon-Oxide-Nitride-Oxide-Silicon-type (SONOS-type) memory devices [10], [11]. In the HOLD state ($V_G = V_B = 0$ V), the poly-Si$_{0.4}$Ge$_{0.6}$ body electrode is suspended above the W gate, source, and drain electrodes, and stored charge is retained in the dielectric layer. To program the cell, a large positive gate voltage ($V_{\text{PROG}}$) is applied such that $V_{\text{GB}}$ is much larger than $V_{\text{PIO}}$ (where $V_{\text{PIO}}$ is the native pull-in voltage), so that the poly-Si$_{0.4}$Ge$_{0.6}$ body electrode is pulled in to the W gate electrode, and electron injection into the dielectric layer via Fowler-Nordheim (FN) tunneling can occur, as shown in Figure 3.1(c), to reduce the relay switching voltages. To read out the binary information stored in the cell, a moderate gate voltage ($V_{\text{READ}}$) is applied such that $V_{\text{GB}}$ is less than $V_{\text{PIO}}$, and then the cell current is sensed: if the cell is programmed, then the relay will be turned on so that current flows; if the cell is erased, then the relay will be turned off so that no current flows.
3.3. Testing Results

Figure 3.2 compares the measured $I_{DS}$ vs. $V_G$ characteristics for a 4-T relay before and after programming and after ultraviolet (UV) exposure. A reduction in switching voltage is clearly seen for the programmed device. Note that the zero $I_{OFF}$ provides for a very large current-sensing window. Together with the abrupt switching behavior (less than 1 mV/decade), this makes it possible to operate a relay-based memory cell with a relatively small program/erase voltage window, or as a multi-level cell. Of course, variation in the programmed-state and erased-state switching voltages must be minimized, for example, by established circuit techniques [12] to facilitate this.

UV exposure is effective for removing most of the stored charge; any remaining charge is likely trapped at the dielectric/body interface. The reduction in switching voltages increases with the duration of the programming voltage pulse (hence FN tunneling), as shown in Figure 3.3. The device also can be erased via FN tunneling by applying a large gate voltage of opposite polarity, as shown in Figure 3.4. For very long erase times, holes are injected into the dielectric layer, so that the switching voltages are increased beyond their native values.

The program/erase times used in this work are much longer than typical (10 ms) for flash memory devices [13]. This is because a single layer of dielectric material (40-nm-thick Al$_2$O$_3$) serves as both the tunneling material and charge storage material. The use of a multi-layer dielectric stack comprising at least a thin (less than 3-nm-thick [14], [15]) tunnel dielectric layer and a charge-storage layer with smaller energy band gap (to allow for direct tunneling of electrons into the conduction band) should provide for much faster program/erase operation, as well as improved retention and endurance characteristics. Note that endurance characteristics are not reported herein because the dielectric stack is sub-optimal.
Figure 3.3: (a) Measured program behavior of a 4-T relay. $V_D$, $V_S$ and $V_B$ were biased at 0 V during the program operation. The FN tunneling current is on the order of pA. (b) Measured $I_{DS}$-$V_G$ characteristics after 600 and 10,000 seconds programming voltage pulses were applied.

Figure 3.4: (a) Measured erase behavior of a 4-T relay. $V_D$, $V_S$ and $V_B$ were biased at 0 V during the erase operation. (b) Measured $I_{DS}$-$V_G$ characteristics after 1 and 1,000 seconds erasing voltage pulses were applied.

Figure 3.5: Measured hole retention behavior of an over-erased 4-T relay cell.

Figure 3.5 shows the measured hole retention behavior of an over-erased cell. A retention time of approximately 1 hour (corresponding to a minimum voltage window of 0.5 V) is seen. The use of a multi-layer dielectric stack, as shown in Figure 3.6, should provide for much longer retention time, as there would be a significant potential barrier to prevent charge loss into the body.
Storage density is a consideration for any memory device. As mentioned previously, a relay-based memory cell potentially can store more than one bit of information. To further increase storage density, the device layout area must be reduced. If the vertical dimensions, such as $T_{ACT}$, $T_{CONTACT}$, and the body electrode thickness, are scaled down in proportion with the lateral dimensions, the cell operating voltages will also scale down proportionately [3]. In order to avoid stiction issues in the contacting regions, a dry release-etch process (e.g. using a mixture of anhydrous HF and vapor-phase methanol at sub-atmospheric pressures) can be used [17], [18].

**3.4. Summary**

In this chapter, a 4-T relay is demonstrated to function as a memory cell. To achieve fast program/erase operation and long retention time, a multi-layer dielectric is necessary. Such a dielectric stack would not pose an issue for a logic relay, because it only serves to electrically isolate the channel. In other words, the same multi-layer dielectric stack can be used for logic vs. memory relays, and would not significantly affect the operation, endurance, or scalability of the logic relay. Note that for a given actuation gap ($T_{ACT}$), the relay switching voltages will increase with the equivalent air-gap thickness of the gate dielectric stack – which would be very small since the permittivities of the gate dielectric materials would be much larger than that of air. In contrast, the dielectric layer(s) in a Metal-Oxide-Semiconductor-Field-Oxide-Transistor (MOSFET) must also provide adequate capacitive coupling between the gate electrode and the channel region; therefore, the dielectric stacks for logic vs. memory devices in a CMOS technology typically are different. Thus, a 4-T relay logic technology can offer embedded memory capability without significant additional process cost.
3.5. References


Chapter 4

See-Saw Relay Technology for

Complementary Logic and Memory Circuits

Abstract: A dual-ended “see-saw” relay design is proposed and demonstrated. Fabricated see-saw relays demonstrate perfectly complementary switching behavior that is symmetric about $V_{DD}/2$, with extremely steep switching behavior (less than 1 mV/decade), very small switching asymmetry (approximately 300 mV), and low on-state resistance (less than 1 kΩ). The perfectly complementary and symmetric operation provides for zero crowbar current, as evidenced by an abrupt inverter voltage transfer characteristic. Various logic functions can be implemented by appropriately biasing a single see-saw relay. The see-saw relay also can be configured as a bi-stable latch, so that a memory cell can be implemented with one relay and one access transistor or relay. Measurements of see-saw-relay switching speed are well matched to lumped-parameter modeling results.

4.1. Introduction

Nano-electro-mechanical relays have been proposed for ultra-low-power digital integrated circuit applications [1], [2], because their ideal switching behavior (zero off-state leakage and abrupt on/off switching behavior) in principle allows the supply voltage ($V_{DD}$) to be scaled down further than for Complementary-Metal-Oxide-Semiconductor (CMOS) transistors [3]. Micrometer-scale single-ended relays have recently been demonstrated to operate reliably with more than $10^9$ on/off cycles [4] and with relatively low gate-voltage swing (less than 2 V), when a body electrode is used for threshold-voltage ($V_{TH}$) adjustment [5]. Operation of relays as “pull-up” and “pull-down” devices is desirable for implementing complementary logic and was demonstrated in [5], [6]. Various functional digital-IC building blocks, such as carry-generation circuit, oscillator, and XOR, have been demonstrated using these single-ended relays and passive circuit components [6], [7], [8], [9]. The $V_{TH}$ values should be set such that switching is symmetric about $V_{DD}/2$, in order to maximize operating voltage margin and to minimize crowbar current. This is challenging to achieve, however, with single-ended relays, due to process-induced $V_{TH}$ variations and their passive pull-out mechanism.

A single structure is also more desirable for more compact mechanical implementation of simple digital logic functions. For example, a single micro-electro-mechanical structure operated in
bending mode has been demonstrated to function as either an OR or AND gate [11]. A compound structure operated in torsional (see-saw) mode has been proposed to function as either a NAND or NOR gate [12]; however, its functionality was not verified electrically, due to very high contact resistance.

A single structure operated in see-saw mode has also been investigated for radio-frequency (RF) [13], [14] and projection display applications [15], [16]. For example, a large array of torsional structures (more than 500,000 elements) that can rotate through a large angle (± 10 degrees) has been demonstrated to operate reliably with more than $10^{12}$ cycles without mechanical failures, such as fatigue, stress rupture, and creep [17], [18]. A torsional RF micro-electro-mechanical-systems (MEMS) switch has been shown to operate with very low contact resistance less than 1 Ω (and hence low insertion loss) [19], [20].

In this chapter, a different see-saw relay design is proposed and demonstrated to achieve perfectly complementary switching behavior that is symmetric about $V_{DD}/2$ to provide for minimal switching hysteresis, maximum noise margin, and zero “crow-bar current”. This “see-saw” design inherently provides for more reliable operation, because electrostatic force as well as spring restoring force is used for off-switching as well as for on-switching, thereby overcoming surface adhesion forces in the contacting regions [19], [20]. Due to this active pull-out mechanism (rather than passive pull-out that relies solely on the spring restoring force), the see-saw relay design inherently shows minimal hysteric behavior during switching operations. Since the see-saw relay achieves the functionality of two single-ended relays with a single movable structure, it is also advantageous for compact implementation of relay-based digital logic integrated circuits; functional seesaw-relay-based logic and memory circuits are also described in this chapter.

4.2. Prototype See-Saw Relay

4.2.1. Device Design and Fabrication

Figure 4.1(a) shows the see-saw relay design that utilizes a single suspended gate electrode (the see-saw beam) anchored by two torsional beams which allow the ends of the gate to move up and down in a perfectly complementary fashion. The two Tungsten (W) channel electrodes attached via an intermediary gate-dielectric (40-nm-thick ALD Al$_2$O$_3$) layer to the underside of the p+ polycrystalline-Si$_{0.4}$Ge$_{0.6}$ gate at either end are used to connect a pair of W source and drain electrodes upon physical contact. Figure 4.1(b) illustrates how the two W body electrodes (co-planar with the source/drain electrode pairs) located underneath the gate electrode, one on either side of the torsional axis, are used to apply voltages across the actuation air gap (with as-fabricated thickness $T_{ACT}$) to electrostatically actuate the see-saw beam downward on either side to close the contact air gaps (with as-fabricated thickness $T_{CONTACT}$), turning on either only the
Figure 4.1: (a) Three-dimensional schematic of the see-saw relay structure and definition of design parameters. Parameter values used in this work are $L = 3 \ \mu m$, $W = H = 1 \ \mu m$, $L_C = 7.5 \ \mu m$, $W_C = 2 \ \mu m$, $L_A = 11 \ \mu m$, 14 $\mu m$, 30 $\mu m$, or 33 $\mu m$, $L_{A1} = 9 \ \mu m$ or 12 $\mu m$, $W_A = 20 \ \mu m$ or 40 $\mu m$, $T_{ACT} = 0.2 \ \mu m$, and $T_{CONTACT} = 0.1 \ \mu m$. (b) Schematic cross-sectional views from (a). The mechanical gate, anchored by two torsion beams, is torqued by electrostatic force induced by applying a voltage between the gate and a body electrode. The two steady states are on-off (illustrated here) and off-on, for perfectly complementary operation. (c) Scanning electron micrograph (SEM) of a fabricated see-saw relay and zoomed-in view of the right channel region.

left side or only the right side. Details of the seesaw-relay fabrication process are described in Chapter 2. Scanning electron micrographs of fabricated see-saw relays are shown in Figures 4.1(c).

4.2.2. Testing Results from Device Perspective

$I_{DS-V_G}$ and $I_{DS-V_DS}$ characteristics of see-saw relays measured in $N_2$ atmosphere are plotted in Figures 4.2(a) and 4.2(b), respectively, for right body bias $V_{BR} = V_{DD} = 10 \ \text{V}$ and left body bias $V_{BL} = 0 \ \text{V}$. As the gate voltage ($V_G$) is increased from 0 V to $V_{DD}$ (10 V), the left side turns on
abruptly, and the right side turns off abruptly at $V_{ON,L} = V_{OFF,R}$, when the see-saw beam is actuated to bring the left channel into contact with the left source/drain electrodes. The on-state resistances are approximately 926 $\Omega$ and 800 $\Omega$, when $V_G = 8$ V and 10 V, respectively. As $V_G$ is reduced back to 0 V, the left side turns off abruptly and the right side turns on abruptly at $V_{OFF,L} = V_{ON,R}$, when the see-saw beam is actuated to bring the right channel into contact with the right source/drain electrodes. Note that $V_{ON,L}$ and $V_{ON,R}$ are symmetric about $V_{DD} / 2$, and that the switching asymmetry, which can be defined by the difference in pull-in voltage that makes the right side turn on (7.16 V) and that makes the left side turn on (6.84 V = 10 V – 3.16 V), is very small (300 mV). This small difference could be caused by measurement variations. On the other hand, it might be caused by strain gradient of the p+ poly-Si$_{0.4}$Ge$_{0.6}$ layer, which was not completely removed via excimer laser annealing; As a result, $T_{ACT}$ on either side of the relay would be slightly different.

The complementary operation of the see-saw relay can be used to achieve a very steep inverter voltage transfer characteristic, as shown in Figure 4.3. The observed asymmetric shifts in $V_{ON,LEFT}$ and $V_{ON,RIGHT}$ values are caused by strain gradient of the poly-Si$_{0.4}$Ge$_{0.6}$ gate electrode, which makes $T_{ACT}$ on the left and right sides inconsistent from the as-fabricated $T_{ACT}$. On the other hand, the asymmetric changes might be caused by gate-oxide charge trapping after 400 on/off switching cycles. This reliability issue, along with the mismatch between input and output voltage swings, can be mitigated by reducing the magnitude of the gate actuation voltage, for example, by reducing $V_{DD}$ as shown in Figure 4.4 or by scaling down $T_{ACT}$ and/or $T_{CONTACT}$. In this work, the output voltage range was kept conservatively low in order to minimize the possibility of micro-welding-induced failure. If the W electrodes are coated with a ultra-thin layer of TiO$_2$, the output voltage range can be increased to approximately 4 V without reliability issues because the work of adhesion in the contacting regions can be reduced [4] and current hence Joule heating is reduced. For the formation of small gaps (below 100 nm), stiction issues

Figure 4.2: (a) Measured $I_{DS}$-$V_G$ characteristics with $V_{BR} = V_{DD} = 10$ V, $V_{BL} = 0$ V, and $V_{DS,R} = V_{DS,L} = 0.8$ V. Note that turn-on and turn-off are abrupt (< 0.1 mV/decade) and that $V_{ON,R}$ and $V_{ON,L}$ are symmetric about 5 V. $L_A = 30 \mu m$, $L_{AI} = 12 \mu m$, and $W_A = 40 \mu m$. (b) Measured $I_{DS,L}$-$V_{DS,L}$ characteristics for the relay in (a). The on-state resistances are approximately 926 $\Omega$ and 800 $\Omega$ when $V_G = 8$ V and 10 V, respectively.
Figure 4.3: Measured voltage transfer curve of the see-saw relay in Figure 4.2, after approximately 400 switching cycles. The $V_{\text{ON_L}}$ and $V_{\text{ON_R}}$ values are shifted due to the strain gradient of the poly-Si$_{0.4}$Ge$_{0.6}$ gate electrode and/or symmetric charging of the Al$_2$O$_3$ gate oxide.

Figure 4.4: Measured values of $V_{\text{ON_L}}$ and $V_{\text{ON_R}}$ vs. $V_{\text{BR}}$ for a different see-saw relay. Note the symmetry of switching about $V_{\text{BR}} = V_{\text{DD}} / 2$, and the reduction in switching voltages with decreasing $V_{\text{DD}}$.

can be avoided by using an advanced dry release etch process, for example, with a mixture of vapor-phase methanol and anhydrous HF at reduced (sub-atmospheric) pressures [21], [22].

In order to reduce the device layout area, the vertical dimensions of the see-saw relay (i.e. $T_{\text{ACT}}$, $T_{\text{CONTACT}}$, and the thickness of the gate layer) should be scaled down to allow for smaller actuation area without increased gate actuation voltage. It should be noted that the optimal circuit topology for a relay-based integrated circuit is significantly different than that for a CMOS integrated circuit, so that fewer relays can often be used to implement a digital logic function [2], [7], [9]; thus the layout area efficiency of a relay-based circuit can be comparable to or better than that of a functionally equivalent CMOS circuit.
4.2.3. Testing Results from Circuit Perspective

Digital logic functions such as BUFFER, NOT (INVERTER), AND, and OR are easily implemented using a single see-saw relay with the drain electrodes tied together to form the output node and with appropriate bias configurations as shown in Figure 4.5(a). The measured logic waveforms (timing diagrams) for single-input functions in Figure 4.5(b) and for dual-input functions in Figure 4.5(c) confirm the versatile functionality of the see-saw relay. Note that a lower ‘HI’ voltage (1 V) is used to bias the source electrodes vs. the gate electrode, in order to avoid potential reliability issues caused by micro-welding.

A single see-saw relay can also be configured as shown in Figure 4.6(a) to form a bi-stable latch. With an access transistor added, a Static-Random-Access-Memory (SRAM) cell is formed. In this work, a discrete n-channel Metal-Oxide-Semiconductor-Field-Effect-Transistor (MOSFET) is used as the access transistor to connect the data-storage node to a bit-line node. Another discrete n-channel MOSFET is used to write voltage data (generated by a function generator, Agilent 33120A 1-channel 15 MHz Function Generator) to the bit-line node. Full functionality of

![Figure 4.5:](image)

Figure 4.5: (a) Drain electrodes are connected to form the logic gate output node (left). A see-saw relay can be properly configured for implementing logic functions (right). (b) Measured BUFFER/INVERTER timing diagrams: (top) INPUT signal, (middle) BUFFER output signal, (bottom) INVERTER output signal.
Figure 4.5: (c) Measured logic gate timing diagrams: (top) **INPUT 1** signal, (middle top) **INPUT 2** signal, (middle bottom) **AND** output signal, (bottom) **OR** output signal.

The hybrid SRAM cell is demonstrated by the measured timing diagrams shown in Figure 4.6(b). Note that a 100 kΩ resistor is inserted between the gate and each drain electrode for this demonstration, in order to allow for lower $V_{DS}$ than $V_{GB}$ to avoid reliability issues caused by micro-welding.

The measurement setup, illustrated in Figure 4.7(a), is used to estimate the switching delay of a see-saw relay under $N_2$ ambient conditions. The switching delay is estimated by measuring the time difference between a change in the input signal (from a function generator, Agilent 81150A 2-channel 120 MHz Function Generator) and a change in the output signal (from the see-saw relay). The measured switching delay is observed to decrease with increasing $V_{DD}$, and is approximately within 10% of the value predicted by a lumped parameter model [23], as shown in Figure 4.7(b). In order to increase SRAM storage density and to reduce $V_{DD}$, the dimensions of a see-saw relay should be scaled down.
Figure 4.6: (a) Schematic circuit diagram of a relay one transistor (1R-1T) SRAM cell. (b) SRAM cell timing diagrams which demonstrate see-saw relay operation as a bi-stable latch: (b-a) voltage data signal $V_{\text{DATA}}$ (supplied by a function generator) used for write operations, (b-b) control signal $V_{\text{CTRL}}$ (supplied by a problematic function generator – hence the “noisy” signal for the first two pulses) used to write voltage data to the bit-line node, (b-c) word-line signal $V_{\text{WL}}$ (supplied by a function generator) used to access the storage node, and (b-d) measured bit-line voltage ($V_{\text{BL}}$) waveform. The noise in the measured bit-line voltage is due to capacitive coupling to the noisy control signal $V_{\text{CTRL}}$. 
Using a calibrated relay model [23], the switching performance of a see-saw relay for a 32-nm-equivalent technology is simulated. The simulation results indicate that sub-10-ns switching delay at $V_{DD}$ less than 1 V is achievable for $V_{DD} / V_{ON} > 1.3$, as shown in Figure 4.7(c). Note that the quality factor is assumed to be 1, which is conservative assuming vacuum packaging, for example, via microshell encapsulation, for operation in the milliTorr (mT) range [24]. To achieve a given delay performance requirement, $V_{DD}$ must be selected such that $V_{DD} / V_{ON}$ will exceed a minimum required value, accounting for variations in $V_{ON}$, due to process-induced variations in device dimensions and environmental variations.
4.3. See-Saw Relay Design Optimization

The testing results of the prototype see-saw relays indicate that there is significant room for improvement and optimization. In this section, monotonicity analysis is conducted, in order to find the optimal device dimensions that yield low operating voltages and hence improve the energy performance of the device. From this monotonicity analysis, design intuitions about the limiting set of cases are derived, as are an optimal set of device dimensions. The results of the monotonicity analysis are validated by comparing against those produced by constrained numerical optimization in MATLAB®. In addition, the accuracy of the values of the objective function obtained from these analyses is compared against the value obtained via Finite-Element-Method (FEM) simulation of the see-saw relay device.

4.3.1. Monotonicity Analysis

Monotonicity analysis is a pre-optimization tool that can be used to solve an optimization problem with a differentiable objective function while satisfying a particular set of constraints [25], [26]. This can be achieved by enumerating various cases, in which groups of constraints are identified as redundant, active, or inactive, and by systematically checking for boundedness of all variable parameters. By doing so, algebraic solutions to constraint-bound cases can be identified, and thus, numerically-based optimization is no longer needed; because a combinatorially large solution space is now simplified to a manageable size, computational loads can be reduced significantly. The formal rules of monotonicity analysis are described as follows [26]:

1. Monotonicity is defined only for differentiable functions, \( f(x) \), with respect to \( x_i \).

2. \( df(x) / dx_i > 0 \) means that \( f(x) \) is strictly monotonically increasing.

3. A variable, \( x_i \), is defined as “bounded below by a constraint,” when \( g_j(x) \leq 0 \), which is monotonic in \( x_i \), if the variable achieves its minimum value at \( g_j(x) = 0 \), e.g. \( g(x) = 1 - x \leq 0 \).

4. A variable, \( x_i \), is defined as “bounded above by a constraint,” when \( g_j(x) \leq 0 \), which is monotonic in \( x_i \), if the variable achieves its maximum value at \( g_j(x) = 0 \), e.g. \( g(x) = x - 1 \leq 0 \).

5. An inequality constraint, \( g_j(x) \), is defined as “active at \( x^* \),” if \( g_j(x^*) = 0 \).

6. An inequality constraint, \( g_j(x) \), is defined as “inactive at \( x^* \),” if \( g_j(x^*) < 0 \).

7. An equality constraint, \( h_k(x) = 0 \), is defined as “irrelevant at \( x^* \),” if the optimal solution is not affected by eliminating the constraint.

8. If the objective function, \( f(x) \), is \( \pm \) monotonic with respect to \( x_i \), then there must exist at least
one active constraint that is of opposite monotonicity in $x_i$, \textit{i.e.} all values must be bounded.

9. A variable, $x_i$, not explicitly represented in the objective function, must either be contained only in inactive constraints or be contained in two active constraints of opposite monotonicity.

10. Degenerate or unbounded problems are violations of the rules 8 and 9.

4.3.1.1. \textit{Assumptions}

Unless otherwise specified, the design optimization studies shown in this section are performed based on the following assumptions:

1. Non-linearities are ignored.

2. Infinitely stiff plates and trusses.

3. Perfectly rectangular torsional beams.

4. Mechanical deformation is elastic.

5. Purely torsional mode operation, \textit{i.e.} minimal out-of-axis motion or forces, including gravity.

6. Ideal processing conditions, \textit{i.e.} devices are fabricated as designed, with no manufacturing variations.

7. Ideal materials that are free of any mechanical reliability issues, such as stress/strain gradient, fatigue, and creep.

8. Isotropic materials are used, which have constant Young's modulus ($E$) and moment of inertia ($I$) throughout the structure.

9. The structure is well encapsulated such that the impact of temperature, humidity, and particle contamination on device performance can be ignored.
4.3.1.2. Problem Statement

To optimize the see-saw relay design, it is first necessary to state the problem in terms of an objective function and design constraints. Because one ultimate goal of the see-saw relay design is to achieve a low power operation, an intuitive objective function is the pull-in voltage ($V_{PI}$) -- the voltage at which either side of a see-saw relay unconditionally snaps closed -- which is derived by comparing the spring restoring force ($F_{SPRING}$) to the electrostatic actuation force ($F_{ELEC}$).

Specifically, $F_{ELEC}$ increases quadratically as this force makes one particular side of the movable see-saw structure move downward, whereas $F_{SPRING}$ increases linearly with increasing downward displacement. Therefore, there is a critical displacement beyond which $F_{ELEC}$ is always larger than $F_{SPRING}$, so that the contact gap will eventually close abruptly, as the applied voltage across the actuation gap increases. This phenomenon, referred to as “pull-in”, is dependent on relay design parameters and can be quantified by the voltage at which it occurs [13], [28]:

Objective: $V_{PI} = \frac{8}{27} \sqrt{\frac{k_T T_{ACT}^3}{\varepsilon_0 L_A W_A}}$, 

where $\varepsilon_0$ is the permittivity of free space, $T_{ACT}$ represents the distance between the movable gate electrode and the fixed body electrode on each side, as illustrated in Figure 4.8(a), $L_A$ and $W_A$ represent the corresponding labeled dimensions in the same figure, and $k_T$ represents the torsional spring constant that characterizes the restoring force generated in the structure’s anchors, as they rotate.

Of note is that $k_T$ can be derived, to the first degree approximation, as follows. In general, the torque, $T_{BEAM}$, applied at one end of a torsional beam with rectangular cross-section is given by [29]
\[ T_{\text{BEAM}} = k_T \cdot \phi = \beta \cdot W_S \cdot H^3 \cdot \frac{G}{L_S} \cdot \phi, \]

where \( k_T \) is the torsional spring constant in N·m/rad, \( \phi \) is the rotation angle that the beam makes, as it rotates, \( \beta \) is a dimensionless parameter that is related to the aspect ratio of the cross-section of the rectangular torsional beam, \( W_S \) and \( L_S \) are the width and length of the torsional beam, respectively, as shown in Figure 4.8(a), \( H \) is the thickness of the beam as shown in the same figure, and \( G \) is the shear modulus of the beam material.

Assuming that the torque applied to make the see-saw structure rotate (\( T_{\text{SEE-SA W}} \)) is equally distributed on both of the torsional beams, as illustrated in Figure 4.8(a),

\[ T_{\text{SEE-SA W}} = 2 \cdot T_{\text{BEAM}} = 2 \cdot \beta \cdot W_S \cdot H^3 \cdot \frac{G}{L_S} \cdot \phi. \]

Because the small angle approximation is valid (i.e. \( \phi \ll 10^\circ \); \( \phi \approx 0.14^\circ \) for the prototype see-saw design with \( L_A + L_{A1} = 40 \ \mu \text{m} \)), assuming that a concentrated load (\( F \)) is applied at the distance \( (L_L) \) from the torsional axis,

\[ T_{\text{SEE-SA W}} = F \cdot L_L = (k_T \cdot T_{\text{ACT}}) \cdot L_L = (k_T \cdot L_L \cdot \tan(\phi)) \cdot L_L = (k_T \cdot L_L \cdot \phi) \cdot L_L = k_T \cdot L_L^2 \cdot \phi, \]

where \( k_T \) is the torsional spring constant in N/m and \( L_L \) is the distance between the torsional axis and the point at which the distributed force from the electrostatic actuation is modeled by a point load.

Next, equating the two analytical equations for \( T_{\text{PLATE}} \),

\[ 2 \beta \cdot W_S \cdot H^3 \cdot \frac{G}{L_S} \cdot \phi = k_T \cdot L_L^2 \cdot \phi, \]

which in turn leads to the first equality constraint \( (h_1) \), as follows:

\[ h_1: k_T = \frac{2 \beta \cdot W_S \cdot H^3 \cdot G}{L_S \cdot L_L^2}, \]

Additionally, equating \( L_L \) in terms of the relevant design parameters yields the second equality constraint \( (h_2) \):

\[ h_2: L_L = 0.5 \cdot L_A + L_{A1}, \]

where \( L_{A1} \) is the offset between each body electrode and the torsional axis, as shown in Figure 4.8(a).
In order to ensure that the torsional mode operation of the see-saw relay dominates over the flexural mode operation while it is switching, it is necessary to include a constraint on the torsional spring constant relative to the flexural spring constant ($k_F$). Note that $k_F$ represents the restoring force of the anchors, as they deflect vertically; if the device tends to deflect too far vertically during switching operations, the entire movable structure can be stuck down onto the substrate. As assumed in Chapter 4.3.1.1, since the see-saw plate is a rigid body, $k_F$ of the two torsional beams is given by [29], [30]

$$h_3: k_F = 2E \cdot W_S \cdot \left( \frac{H}{L_S} \right)^3,$$

where $E$ is the Young’s modulus of the structural material. The spring ratio constraint ($g_1$) is expressed as a function of the constant, $R_S$:

$$g_1: \frac{k_F}{k_T} \geq R_S.$$

The other constraint that is required for proper operation as a component of a logic circuit is that the device be able to restore itself to its initial position after being actuated. To ensure this, the restoring force of the torsional spring needs to be greater than the surface adhesion force:

$$g_2: k_T \cdot T_{ACT} \geq F_{ADHESION}.$$

In addition, constraints are introduced to ensure that the see-saw relay can be fabricated in the Berkeley Microfabrication Laboratory. In particular, no device dimension is allowed to be less than a minimum feature size, $\lambda$:

$$g_3: L_A \geq \lambda,$$

$$g_4: W_A \geq \lambda,$$

$$g_5: L_S \geq \lambda,$$

$$g_6: W_S \geq \lambda,$$

and the ratio of the length and width dimensions is constrained to confine the strain gradient effect to one dimension:

$$g_7: L_A + L_{A1} \geq 2W_A.$$

In addition, practical design rules (which had been verified by the prior experiment) are introduced to address the potential problems of buckling or fracture under cycling stress. The most relevant of these concerns is a constraint on the minimum possible actuation offset:
Finally, the device needs to be confined to a finite area:

\[ g_9: L_{\text{MAX}} \geq 2L_A + 2L_{A1} + W_S, \]
\[ g_{10}: W_{\text{MAX}} \geq W_A + 2L_S, \]

where \( L_{\text{MAX}} \) and \( W_{\text{MAX}} \) are constants that specify the maximum allowable footprint of the seesaw relay.

These constraints are compiled into a form amenable to monotonicity analysis, as follows:

\[ g_1: k_T R_S - k_F \leq 0, \]
\[ g_2: F_{\text{ADHESION}} - k_T T_{\text{ACT}} \leq 0, \]
\[ g_3: \lambda - L_A \leq 0, \]
\[ g_4: \lambda - W_A \leq 0, \]
\[ g_5: \lambda - L_S \leq 0, \]
\[ g_6: \lambda - W_S \leq 0, \]
\[ g_7: 2W_A - L_A + L_{A1} \leq 0, \]
\[ g_8: 2\lambda - L_{A1} \leq 0, \]
\[ g_9: 2L_A + 2L_{A1} + W_S - L_{\text{MAX}} \leq 0, \]
\[ g_{10}: W_A + 2L_S - W_{\text{MAX}} \leq 0, \]

\[ h_1: k_T L_S L_L^2 = 2\beta W_S H^2 G, \]
\[ h_2: L_L = 0.5 L_A + L_{A1}, \]
\[ h_3: k_F L_S^3 - 2E W_S H^3 = 0, \]

and the results are compiled into an always true monotonicity table, Table 4.1.

Note that many of the line width constraints (\( g_3, g_4, \) and \( g_5 \)) are irrelevant, because other constraints already limit these dimensions. For instance, if \( g_9 \) and \( g_7 \) or \( g_{10} \) constraints are active,
the constraints \( g_3, g_4, \) and \( g_5 \) become irrelevant. The constraint, \( g_6 \), however, must be always active, because a minimized \( W_S \) reduces the objective function, but the ratio of spring constants is not negatively penalized. In the case of very strong surface adhesion, it might be necessary to increase \( W_S \) beyond this minimum feature size to generate a high enough restoring force in the structure.

In addition, there are two pairs of linked constraints: \( h_1 \) and \( h_2 \) must always be activated together, as must \( g_1 \) and \( h_3 \). This is because the values \( L_L \) and \( K_F \) appear only in these pairs, respectively, and providing a positive and negative bound on \( L_L \) and \( K_F \) requires that both of the constraints be active. For this reason, \( h_3 \) can only be activated with one set of signs, even though it is an equality constraint.

As shown in Table 4.1, the always-true table reveals a large number of possible cases and sub-cases, because almost all of the variable columns have multiple possible positive or negative bounds. This makes pure monotonicity analysis of this structure somewhat challenging. By building from simple cases to more complex ones, however, it is possible to make an understandable logic flow that addresses a set of realistic design cases. A logic flow designed for the monotonicity analysis is featured in Figure 4.9.

#### Table 4.1: Always-true monotonicity table.

<table>
<thead>
<tr>
<th>( k_T )</th>
<th>( L_A )</th>
<th>( W_A )</th>
<th>( k_F )</th>
<th>( L_S )</th>
<th>( W_S )</th>
<th>( L_L )</th>
<th>( L_{A1} )</th>
<th>Activity</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Obj.</strong> ( (8k_T\cdot T_{ACT}^3 / (27k_T\cdot L_A\cdot W_A))^{0.5} )</td>
<td>+</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Always active</td>
</tr>
<tr>
<td>( g_1 ): ( k_T\cdot R_S - k_F )</td>
<td>+</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Activated if ( h_3 ) is active</td>
</tr>
<tr>
<td>( g_2 ): ( F_{ADHESION} - k_T\cdot T_{ACT} )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>( g_3 ): ( \lambda - L_A )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Irrelevant</td>
</tr>
<tr>
<td>( g_4 ): ( \lambda - W_A )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Irrelevant</td>
</tr>
<tr>
<td>( g_5 ): ( \lambda - L_S )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Irrelevant</td>
</tr>
<tr>
<td>( g_6 ): ( \lambda - W_S )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Always active for realistic ( F_{ADHESION} )</td>
</tr>
<tr>
<td>( g_7 ): ( 2W_A - L_A - L_{A1} )</td>
<td>–</td>
<td>+</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>( g_8 ): ( 2\lambda - L_{A1} )</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>( g_9 ): ( 2L_A + 2L_{A1} + W_S - L_{MAX} )</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td></td>
</tr>
<tr>
<td>( g_{10} ): ( W_A + 2L_S - W_{MAX} )</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td></td>
</tr>
<tr>
<td>( h_1 ): ( L_S\cdot L_L^2\cdot k_T = 2\beta\cdot W_S\cdot H\cdot G )</td>
<td>–/+</td>
<td>–/+</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>Activated if ( h_2 ) is active</td>
</tr>
<tr>
<td>( h_2 ): ( L_L = 0.5\cdot L_A + L_{A1} )</td>
<td>–/+</td>
<td>–/+</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>+/–</td>
<td>Activated if ( h_1 ) is active</td>
</tr>
<tr>
<td>( h_3 ): ( k_F\cdot L_S^3 - 2E\cdot H\cdot W_S = 0 )</td>
<td>+</td>
<td>+</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Activated if ( g_1 ) is active</td>
</tr>
</tbody>
</table>
4.3.1.3. Case Study I

The first case uses the minimum number of constraints to frame the monotonicity problem, as shown in Table 4.2. The objective function activates a positive constraint on $k_T$ and negative constraints on $L_A$ and $W_A$. In this case, the $k_T$ constraint is bounded by the surface adhesion force constraint ($g_2$) to prevent the activation of the variable-rich equality constraints, $h_1$ and hence $h_2$. $L_A$ is limited by the $L_{MAX}$ constraint ($g_9$). $W_A$ is limited by the strain confinement constraint ($g_7$), which prevents the introduction of $L_S$ as a variable. Lastly, $W_S$ and $L_{A1}$ are also limited by the $L_{MAX}$ constraint ($g_9$).

A set of optimal solutions can be found from CASE I. Specifically, first consider the values that can be pinned by the active constraints, which are distinguished from the other variables with a star superscript:

$$W_S^* = \lambda,$$

$$k_T^* = \frac{F_{ADHESION}}{T_{ACT}}.$$

\[46\]
Next, the constraints \((g_7\) and \(g_9\)) that contain \(L_{A1}\) and \(L_{A}\) give rise to a master equality:

\[
L_{A} + L_{A1} = 2W_{A} = \frac{L_{\text{MAX}} - W_S}{2},
\]

which leads to an optimal design point for \(W_{A}\):

\[
W_{A}^* = \frac{L_{\text{MAX}} - \lambda}{4}.
\]

Since the offset constraint \((g_8)\) is active to minimize \(L_{A1}\), the rest of the dimensions are found to be

\[
L_{A1}^* = 2\lambda,
\]

\[
L_{A}^* = \frac{L_{\text{MAX}} - 5\lambda}{2}.
\]

In addition, even though the variable, \(L_{L}\), is inactive \(i.e.\) initially unconstrained, it can be computed from the unconstrained \(L_{L}\) constraint \((h_2)\), because \(L_{A1}^*\) and \(L_{A}^*\) are already pinned by the active constraints:

\[
L_{L} = \frac{1}{2}(L_{A} + L_{A1}) \rightarrow
\]

\[
L_{L}^* = \frac{1}{2}(L_{A}^* + L_{A1}^*) = \frac{L_{\text{MAX}} + 3\lambda}{4}.
\]

Of particular interest in **CASE I** \(\text{is the decision to minimize } L_{A1}\). This is because the objective function is not dependent on \(L_{A1}\), as long as \(g_2\) is constrained, \(i.e.\) \(k_T\) is tied to \(F_{\text{ADHESION}} / T_{\text{ACT}}\). That is to say, while \(g_2\) is active, the objective function is only affected by changes in \(L_{A}\) and \(W_{A}\). Also of note is that \(L_{S}\) can be computed from the inactive \(k_T\) constraint \((h_1)\), as follows:
\[ L_S = \frac{32\beta \cdot G \cdot H^3 \cdot T_{ACT}}{(L_{MAX} + 3\lambda)^2 \cdot F_{ADHESION}}. \]

Because this variable, \( L_S \), is not explicitly constrained by \textbf{CASE I}, it forms the basis for both of the following tests, which indicate if \textbf{CASE I} is indeed valid: a check to see if the total width constraint is obeyed and a test to confirm that the spring constant ratio (a function of \( L_S \)) is valid. These are noted in the logic flow in Figure 4.9, but are more precisely stated as follows:

\[ W_A + 2L_S = \frac{L_{MAX} - \lambda}{4} + \frac{64\beta \cdot G \cdot H^3 \cdot T_{ACT}}{(L_{MAX} + 3\lambda)^2 \cdot F_{ADHESION}} \leq W_{MAX}, \]

\[ \frac{k_F}{k_T} = \frac{2E \cdot F_{ADHESION}^2}{T_{ACT}^2 \cdot \lambda^2} \left( \frac{(L_{MAX} + 3\lambda)^2}{32\beta \cdot G \cdot H} \right)^3 \geq R_S. \]

Physically, the set of the optimal solutions (the variables with a star superscript) found in \textbf{CASE I} indicates a somewhat ideal design, where the see-saw device design is not initially constrained by \( W_{MAX} \), and where structural material properties are assumed such that, even with a minimized \( L_L \), both a smallest possible \( k_T \) and a sufficiently large \( k_F \) that obey the \( R_S \) constraint (\( g_1 \)) can be achieved. Therefore, \textbf{CASE I} represents a good alignment of the design constants to allow the highest degree of optimization.

\subsection*{4.3.1.4. Case Study II}

The next interesting case arises when the initial constraints in \textbf{CASE I} fail due to a high \( R_S \) and more limited area. These constraints result in a set of active constraints that are complementary to the active \( g_2 \) in \textbf{CASE I}; by unpinning \( k_T \) from its minimum value (\textit{i.e.} remove the \( g_2 \) constraint from the monotonicity table) and by enforcing the stiffness ratio constraint (\( g_1 \)), the opposite set of functionality constraints can be addressed. Note that \( L_{A1} \) is also unpinned from its minimum value. The new set of active constraints is summarized in Table 4.3 and gives rise to a new set of optimal solutions. Again, starting with the quantities that are directly defined by their active constraints:

\[ W_S^* = \lambda. \]

The objective function can be expressed as a function of only one variable, \( L_L \), by recognizing that

\[ W_A^* = \frac{L_{MAX} - \lambda}{4} \quad \text{(from } g_7 \text{ and } g_9 \text{),} \]
\[ L_A = L_{\text{MAX}} - \lambda - 2L_L \text{ (from } g_5 \text{ and } h_2), \]
\[ L_S^2 = \frac{E}{G} \cdot \frac{L_L^2}{\beta R_S} \text{ (from } g_1, h_1, \text{ and } h_3), \]

which leads to an objective function of the following form:

\[
V_{\text{PI}}^2 = \frac{64\beta H^3 \cdot T_{\text{ACT}}^3 \cdot \lambda \cdot \sqrt{\beta R_S G/E}}{27\varepsilon_0 (L_{\text{MAX}} - \lambda)(L_{\text{MAX}} - \lambda - 2L_L) L_L^3} \triangleq \text{Constant } \frac{(L_{\text{MAX}} - \lambda - 2L_L)^3}{(L_{\text{MAX}} - \lambda)^3}.
\]

The optimal \( L_L \) can be found by differentiating the objective function with respect to \( L_L \) and equating the resulting expression to zero:

\[ L_L^* = \frac{3}{8} (L_{\text{MAX}} - \lambda), \]

and this expression is used to solve for the other critical dimensions:

\[ L_A^* = \frac{L_{\text{MAX}} - \lambda}{4}, \]
\[ L_S^* = \frac{3}{8} \sqrt{\frac{E}{G} \cdot \frac{1}{\beta R_S} (L_{\text{MAX}} - \lambda)}. \]

In **CASE II**, since the spring restoring force constrain \((g_2)\) is not enforced, it is necessary to check the values found for \( k_T \cdot T_{\text{ACT}} \) against \( F_{\text{ADHESION}} \) to determine if **CASE II** is the valid case. In addition, the \( W_{\text{MAX}} \) constraint \((g_{10})\) is also inactive, and hence, it is necessary to check if the
device indeed fits in the appropriate footprint. These checks are summarized in Figure 4.9, but are given more specifically as follows:

$$\frac{F_{\text{ADHESION}}}{T_{\text{ACT}}} \leq k_T = \left(\frac{8}{3}\right)^3 \sqrt{\frac{G}{E}} \cdot \beta \cdot R_s \frac{2\beta \cdot H^3 \cdot G}{(L_{\text{MAX}} - \lambda)^3},$$

$$\left(\frac{1}{4} + \frac{3}{4} \sqrt{\frac{E}{G}} \cdot \frac{1}{\beta \cdot R_s}\right) \cdot (L_{\text{MAX}} - \lambda) \leq W_{\text{MAX}}.$$

**CASE II** represents one design scenario, in which the minimum torsional spring constant ($k_T$) might be unattainable, and hence makes the relay device harder to achieve lower operating voltages, if limited device footprint is given (for example, $L_{\text{MAX}}$ is required to be very small). In addition, the flexural spring constant ($k_F$) is might be on the verge of being large enough, because the stiffness ratio constraint ($g_1$) is forced to be active. Therefore, **CASE II** is in some ways the opposite of the first case, perhaps reflecting some of the worst possible design conditions.

### 4.3.1.5. Case Study III

To find the case most representative of reality, a balance between the first two cases is investigated by enforcing both the stiffness ratio ($g_1$) and the surface adhesion limit on $k_T$ ($g_2$). The constraint on the maximum allowable width ($g_{10}$) is chosen to be active, in order to limit the device width with a given footprint. This latter addition represents a departure from the assumptions in the first two cases, where both allowed an inactive $W_{\text{MAX}}$. This is a justifiable change, because it makes **CASE III** closer to the prototype see-saw relays that are the basis for this optimization. Even though it is possible to represent a version of this case where $W_\Lambda$ is limited by the $g_7$ constraint (and to represent the previous two cases with the $g_{10}$-based constraints), doing so would be repetitive because, fundamentally, only one of the $g_7$ or $g_{10}$ constraints can limit $W_\Lambda$ and changing which constraint is active only affects the device width without changing other variables. These changes are summarized in Table 4.4.

A set of optimal solutions for **CASE III** can be found in the same way as the previous two cases, noticing that a series of the active constraints reveals the design variable values as follows:

$$W_{S}^* = \lambda,$$

$$k_T^* = \frac{F_{\text{ADHESION}}}{T_{\text{ACT}}}.$$
Table 4.4: Monotonicity table for CASE III.

<table>
<thead>
<tr>
<th></th>
<th>$k_T$</th>
<th>$L_A$</th>
<th>$W_A$</th>
<th>$k_F$</th>
<th>$L_S$</th>
<th>$W_S$</th>
<th>$L_L$</th>
<th>$L_{A1}$</th>
<th>Activity</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Obj.:</strong> $(8k_T \cdot T_{ACT}^3 / (27\varepsilon_O \cdot L_A \cdot W_A))^{0.5}$</td>
<td>+</td>
<td>–</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Always active</td>
</tr>
<tr>
<td>$g_1$: $k_T \cdot R_S - K_F$</td>
<td>+</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $k_F$ in $h_3$.</td>
</tr>
<tr>
<td>$g_2$: $F_{ADHESION} - k_T \cdot T_{ACT}$</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $k_T$ in Obj.</td>
</tr>
<tr>
<td>$g_6$: $\lambda - W_S$</td>
<td></td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $W_S$ in $h_1$.</td>
</tr>
<tr>
<td>$g_9$: $2L_A + 2L_{A1} + W_S - L_{MAX}$</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $L_A$ in Obj.</td>
</tr>
<tr>
<td>$h_1$: $2\beta \cdot W_S \cdot H^3 \cdot G - L_S \cdot L_L^2 \cdot k_T = 0$</td>
<td>–</td>
<td>–</td>
<td>+</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $W_S$ in $g_6$.</td>
</tr>
<tr>
<td>$h_2$: $L_L - 0.5 \cdot L_A - L_{A1} = 0$</td>
<td>–</td>
<td></td>
<td>+</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $L_1$ in $h_1$ &amp; $L_{A1}$ in $g_9$</td>
</tr>
<tr>
<td>$h_3$: $k_F \cdot L_S^3 - 2E \cdot H^3 \cdot W_S = 0$</td>
<td>–</td>
<td>+</td>
<td>+</td>
<td>–</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Active to bound $L_S$ in $h_1$.</td>
</tr>
</tbody>
</table>

$$k_F^* = k_T^* \cdot R_S = \frac{F_{ADHESION} \cdot R_S}{T_{ACT}}$$,

$$k_F = \frac{2E \cdot W_S \cdot H^3}{L_S^3} \rightarrow L_S^* = \frac{3}{\sqrt{\frac{2E \cdot \lambda \cdot T_{ACT}}{F_{ADHESION}}}} \cdot H,$$

$$k_T = \frac{2\beta \cdot W_S \cdot H^3 \cdot G}{L_S \cdot L_L^2} \rightarrow L_L^* = \sqrt{\frac{\beta \cdot G \cdot (R_S / E)^{1/3}}{F_{ADHESION}}} \cdot \left(\frac{2\lambda \cdot T_{ACT}}{F_{ADHESION}}\right)^{2/3} \cdot H,$$

$$L_A^* = L_{MAX} - \lambda - 2 \cdot \sqrt{\frac{\beta \cdot G \cdot (R_S / E)^{1/3}}{F_{ADHESION}}} \cdot \left(\frac{2\lambda \cdot T_{ACT}}{F_{ADHESION}}\right)^{2/3} \cdot H,$$

$$L_{A1}^* = 2 \cdot \sqrt{\frac{\beta \cdot G \cdot (R_S / E)^{1/3}}{F_{ADHESION}}} \cdot \left(\frac{2\lambda \cdot T_{ACT}}{F_{ADHESION}}\right)^{2/3} \cdot H - \frac{L_{MAX} - \lambda}{2},$$

$$W_A^* = W_{MAX} - 2 \cdot \frac{3}{\sqrt{\frac{2E \cdot \lambda \cdot T_{ACT}}{R_S \cdot F_{ADHESION}}}} \cdot H.$$

To determine that CASE III is indeed a valid case, the values found for $L_A + L_{A1}$ need to be checked against $2W_A$ (note that the $g_7$ constraint was set to be inactive). This is shown in Figure 4.9, and the specific check is given as:
Because almost all of the constraints are enforced in this case, it physically represents a design where both spring constants are at their minimum possible value (while maintaining the stiffness ratio), which results in the lowest $V_{PL}$ in a given footprint.

4.3.1.6. **Fundamental Insights from the Case Studies**

In summary, two key lessons are embedded in the three case studies. First, the width of the see-saw relay ($W_A$) is set by one of the $g_7$ or $g_{10}$ constraints and has little bearing on other aspects of the design, such as $L_S$, $L_L$, and the spring constants. Second, there are three possible approaches that make the spring constants be limited: $k_T$ is at its minimum value and $k_F$ is not, $k_F$ is at its minimum value and $k_T$ is not, or both $k_T$ and $k_F$ are at their minimum values. The latter of the three cases is closest to the ideal and yields the best $V_{PL}$ performance per unit footprint. Also, in order to minimize $V_{PL}$ with the smallest possible footprint overhead, $W_{MAX}$ should be set such that $W_A$ is precisely at the limit allowed by $g_7$, which would suggest that both of the $W_A$ constraints ($g_7$ and $g_{10}$) are effectively active for the most optimally selected set of design constants.

4.3.2. **Validation of Monotonicity Analysis**

The monotonicity analysis is verified against constrained numerical optimization in MATLAB® [31] as well as FEM analysis in COVENTORWARE™ [32], [33]. Each of the methods well predicts the value of the objective function, which agrees with each other within approximately 10%.

4.3.2.1. **Monotonicity Analysis vs. Nonlinear Constrained Optimization**

The closed-form analytical solutions obtained from CASE III of the monotonicity analysis were evaluated with the constant values (summarized in Figure 4.8(b)) used in the prototype see-saw relay design. The results of the monotonicity analysis are plotted in Figure 4.10(a); the lowest $V_{PL}$ of the see-saw relay was found to be 1.29 V, when $L_S = 8.6 \, \mu m$, $W_S = 1 \, \mu m$, $L_{A1} = 36.9 \, \mu m$, $L_A = 12.6 \, \mu m$, and $W_A = 12.8 \, \mu m$. To validate the analytical results of CASE III, the Rosenbrock Test Function (“fmincon” function in MATLAB® built-in for nonlinear constrained minimization [31]) was used to find a global optimal $V_{PL}$ for the see-saw relay. All of the inequality and equality constraints were entered into MATLAB® with the same constant values.
This numerical analysis yielded the optimal $V_{PI}$ of 1.49 V, as indicated in Figure 4.10(b).

The results of both analyses match closely. This is non-trivial, especially when considering the difficulty of forcing an eight-variable constrained optimization to converge; the tolerances of the optimization were loose and account for the difference between the monotonicity and numerical optimum points. Note that convergence aids were used in finding the numerical solution, e.g., a lower bound of zero on the search space was used, instead of negative infinity, which might have resulted in slight inconsistency (the closed dot is outside the valid region in Figure 4.10(b)).

4.3.2.2. Monotonicity Analysis vs. Finite-Element-Method Analysis

FEM analysis was performed on the see-saw relay with the optimal set of the device dimensions found from the monotonicity analysis. The result of the FEM simulation is shown in Figure 4.11. The values of the objective function predicted by the analyses are summarized in Table 4.5; The close agreement of the values of the objective function between the methods verifies that the monotonicity analysis indeed produced a valid, optimal design solution.

4.3.3. Summary of Design Optimization Study

The results of the analyses lead to an insight into the proper optimizations for the see-saw relay: the torsional spring constant ($k_T$) should be minimized, as should the flexural spring constant ($k_F$),
the actuation area should have a reasonable offset from the torsional axis, and the actuation width should be maximized under the constraints of the strain gradient and footprint limitations.

Monotonicity analysis also revealed some underlying facts about the design cases. The constraint on device width has little effect on other variable parameters, and hence, the ideal footprint should be assigned to be reasonably lengthy enough (in the direction perpendicular to the torsional axis) such that the device width \( W_F \) is limited by the stress confinement constraint. In addition, there are three possible routines in monotonicity analysis that the torsional and flexural spring constants can decide device dimensions: only the \( k_T \) constraint can be active, only the \( k_F \) constraint can be active, or both spring constant constraints can be activated.

Finding these design insights with monotonicity analysis was somewhat challenging, because of multiple design constraints that affected the same variables. This suggests that the formulation of monotonicity design problems is vastly simplified by finding the dominant constraints and focusing on those, while ignoring corner cases that make the scale of the monotonicity table explode. This was accomplished by identifying the three dominant spring limitations and two dominant width limitations mentioned previously. It is also interesting to note that the monotonicity analysis revealed the tolerance and convergence limitations of numerical optimization, nevertheless, it is particularly useful in its initially proscribed role as a pre-optimization tool.
4.4. Corrugated See-Saw Relay Design

The case studies in the previous section were performed, based on the assumption that the structural material of the see-saw relay shows zero strain gradient effect, i.e. there is no out-of-plane curvature of the released structure. This is difficult to realize in practice, because intrinsic stress (and stress gradient) of a material -- which results in dimensional change and out-of-plane deflection upon removal of the sacrificial oxide underneath the pre-released structure -- depends on deposition conditions as well as film micro-grain structure. For example, undoped polycrystalline-Silicon (poly-Si) films are amorphous in nature when they are deposited at 550 ºC or below; The internal microstructure and residual stress of this material is dependent upon processing temperature and partial pressure of Silane (SiH₄), and thus, a low temperature anneal that leads to a fine-grained poly-Si is necessary to achieve low tensile stress and smooth surface texture [34].

When the gate stack of the see-saw relay (e.g. 1-μm-thick p+ poly-Si₀.₄Ge₀.₆ on top of 40-nm-thick Al₂O₃) has positive strain gradient, its bottom portion is more inclined to stretch out than its top portion upon release, because it is increasingly compressed toward its bottom. On the other hand, if the gate stack has negative strain gradient, the top portion of the gate stack tends to stretch out more than the bottom portion upon release, because the gate stack is increasingly compressed toward its top portion.

The negative strain gradient was certainly the case for the pre-laser-annealed see-saw relays, as confirmed using a white-light interferometer (Veeco Wyko NT3300 3-D Optical Profiling System) in Figure 4.12(a); Since the see-saw structure is anchored by the two torsional beams, it is increasingly buckled upward at its center line along the torsional axis as well as along the direction perpendicular to the torsional axis (i.e. it appears like an open umbrella). Figure 4.12(b) shows measured parasitic out-of-plane displacement of the see-saw relays, which increases with increasing device dimensions, because of more severe negative strain gradient.
Quantitatively, strain gradient is calculated -- to the first degree approximation -- from [35]

\[
\frac{1}{\rho} = \frac{2\Delta z}{L_A + L_{A1}},
\]

where \(\rho\) is the radius of the curvature of the see-saw structure, \(\Delta z\) is the out-of-plane deflection of the see-saw structure, \(L_A\) represents the length of the see-saw structure, and \(L_{A1}\) is the offset between each body electrode and the torsional axis, as Figure 4.8(a) shows. Using this equation, the strain gradient values of the see-saw structures were approximated, as shown in Figure 4.13. The calculated values on the order of high \(10^{-4}\) per \(\mu m\) are relatively large, considering that inertial sensor applications typically require strain gradient of \(10^{-5}\) per \(\mu m\), which translates into 1.25 \(\mu m\) tip deflection of a 500-\(\mu m\)-long cantilever beam [35].

Clearly, minimization of the strain gradient effect is desirable, to achieve low operating voltages, since these require the formation of very small actuation and contact gaps with good uniformity.
In fact, various processing techniques have been investigated, in order to control the stress (and stress gradient) by engineering the structural and morphological properties of a film. For example, intrinsic stress can be minimized by properly tuning material deposition conditions. The hinge material of the Texas Instruments Digital Mirror Display devices -- the amorphous TiAl$_3$ sputtered with 4 % Oxygen -- was found to yield the lowest stress relaxation [36].

Annealing techniques have been proven to be effective in inducing changes in film grain microstructures and hence alleviating the strain gradient effect. For instance, positive stress gradient of an as-deposited poly-SiGe film can be changed to negative stress gradient by various post-deposition processing methods, such as furnace annealing, rapid thermal annealing, or flash lamp annealing; This is possible, because voids and defects within the film are removed, as the amorphous region of the film (which is needed initially to provide crystal seeds) is crystallized while the upper crystalline portion of the film is recrystallized [35], [37], [38].

In contrast, argon implantation or excimer laser annealing with Krypton Fluoride (KrF) or Xenon Dichloride (XeCl$_2$) laser sources produces the reverse effect within the deposited film, i.e. negative stress gradient is turned into positive stress gradient because compressive stress within the portion is relieved [35], [39], [40].

These processing approaches, however, might be inadequate for high-yield fabrication of the see-saw relays, because it is difficult to precisely control the stress (and stress gradient) within the gate stack, especially in academic laboratory settings, due to process-induced run-to-run and wafer-to-wafer variations.

Therefore, of particular interest would be the approach that can reduce out-of-plane deflection of the released structure via mechanical design. Lateral poly-Si resonator designs that incorporate symmetric folded flexures have been shown to relieve residual stress within the structural microstructures; however, they are still susceptible to out-of-plane warpage, due to the intrinsic stress gradient through the thickness of the film [41], [42].

Another intriguing approach would be to take advantage of the corrugated structural design [43], [44] -- which was invented for bulk micromachined sensors [45] -- to reduce intrinsic stress within the deposited film. Corrugated single-crystal Si membranes have much lower intrinsic stress (by a factor of 1,000 to 10,000), compared to non-corrugated membranes [46]. Corrugated cantilever beams made out of Chromium (Cr) or poly-SiGe show 20 to 50 times reduction in parasitic out-of-plane deflection because of higher effective moment of inertia that enhances stiffness of the structure [47], [48].
4.4.1. Device Design and Fabrication

The corrugated see-saw relay design shown in Figure 4.14(a) uses a single moveable plate (which serves as the gate electrode) anchored by two torsional beams which allow the ends of the plate to be displaced up and down in a perfectly complementary fashion. Two W channel electrodes are attached to the p+ poly-Si$_{0.4}$Ge$_{0.6}$ gate electrode at either end via an intermediary Al$_2$O$_3$ gate-oxide film. Two W body electrodes are located underneath the gate electrode, one on either side of the torsional axis. The device operating principle is the same as for the prototype see-saw relay design described earlier in this chapter: Differential bias voltages applied to the body electrodes cause the gate electrode to be electrostatically actuated downward on one side at a time. As a result, one of the channel electrodes makes contact with a pair of W source/drain electrodes (co-planar with the body electrodes), i.e. either only the left end or only the right end of the see-saw relay is turned on at a time.

\[ I_R = \frac{W_R \cdot H^3}{12} = 0.61 \, \mu m^4 \]
\[ I_U = \frac{D \cdot W_O^3 - W_I^3 \cdot (D - H)}{12} = 5.71 \, \mu m^4 \]
Note that the corrugated see-saw structure consists of multiple U-shaped beam(s). As described earlier, this U-profile makes the structure stiffer by increasing the moment of inertia (i.e., increases the ability/capacity of the structure cross-section to resist bending). The area moment of inertia of the rectangular vs. U-shaped cross-sections of a beam are given by

\[
I_R \approx \frac{W_R \cdot H^3}{12},
\]

\[
I_U \approx \frac{D \cdot W_O^3 - W_I^3 (D - H)}{12},
\]

respectively, where \(W_R, H, D, W_O,\) and \(W_I\) are correspond to the labeled dimensions in Figure 4.14(c). The calculated values of \(I_R\) vs. \(I_U\) are summarized in Figure 4.14(c) -- The moment of inertia of the U-shaped beam is higher by approximately 9.4 times than that of the rectangular beam. Note that \(H\) is chosen to be 1 \(\mu\)m due to the limited depth of focus (~1 \(\mu\)m) of the photolithography tool that was used to fabricated the relays.

Corrugated see-saw relays were fabricated in the Berkeley Microfabrication and Marvell Nanofabrication Laboratories. The original process flow described in Chapter 2 was slightly modified. The specific changes are as follows: (1) At the beginning of the process, a 1-\(\mu\)m-thick thermal SiO\(_2\) was grown on the Si substrate. This layer was defined using the mask with various corrugation features. A 100 nm Al\(_2\)O\(_3\) was then deposited to insulate the corrugated substrate. (2) The timed-etching step used to thin down the sacrificial oxide after the W channel formation was no longer used. To remove this step, a thinner 1\(^{st}\) sacrificial oxide (100 nm instead of 200 nm) was deposited and patterned, prior to the 2\(^{nd}\) sacrificial oxide deposition.

Fabricated see-saw relays were inspected using the white-light interferometer, as shown in Figure 4.15, to observe the impact of corrugation on strain gradient. The negative strain gradient of the corrugated relay seemed to be slightly lower than that of the non-corrugated one, and yet
not sufficiently low enough to yield low operating voltages and high production yield. Therefore, to reduce the impact of negative strain gradient within the poly-Si$_{0.4}$Ge$_{0.6}$ layer, a KrF excimer laser ($\lambda = 248$ nm) pulse (200 mJ/cm$^2$, 10 ns per shot, 10 shots) was applied to the gate electrode through a SiO$_2$ hardmask layer.

4.4.2. Testing Results

Fabricated see-saw relays were tested under N$_2$ purge at room temperature and atmospheric pressure. Unless otherwise specified, the drain-to-source bias voltage ($V_{DS}$) was constrained to be no greater than 2 V, in order to avoid reliability issues due to possible micro-welding between contacting electrodes. Figure 4.16(a) represents measured $I_{DS}$-$V_{GS}$ characteristic of the corrugated see-saw relay. Note that the right and left body bias voltages were set to $V_{BL} = 0$ V and $V_{BR} = V_{DD} = 6$ V, respectively. As the gate voltage ($V_G$) is increased from 0 to $V_{DD}$, $V_G$ needed to turn on the left side ($V_{ON,L}$) turns off the right side abruptly at approximately 4.88 V. Likewise, as $V_G$ is reduced back to 0 V, the right side turns on abruptly and the left side turns off abruptly at about 1.9 V -- thus, the voltage needed to turn on the right side ($V_{ON,R}$) is $V_{DD} - V_G = 6$ V -- 1.9 V = 4.1 V. Notice that $V_{ON,R}$ and $V_{ON,L}$ are slightly asymmetric about $V_{DD} / 2$, which yields switching hysteresis (difference between $V_{ON,L}$ and $V_{ON,R}$) of about 0.78 V. This hysteresis is caused by different $T_{ACT}$ on the left and right sides of the relay. This indicates that the impact of laser-annealing was not uniform across the device. The turn-on voltages can be lowered by scaling down the as-fabricated $T_{ACT}$ and $T_{CONTACT}$ and/or by further design optimization (for example, reducing the torsional spring constant of the see-saw relay).

Figure 4.16: (a) Measured $I_{DS}$-$V_{GS}$ characteristic. $V_{BL} = 0$ V and $V_{BR} = V_{DD} = 6$ V. $V_{ON,R}$ and $V_{ON,L}$ are slightly asymmetric about $V_{DD} / 2$, due to the negative strain gradient within poly-Si$_{0.4}$Ge$_{0.6}$ that makes $T_{ACT}$ on either side different. (b) Measured $I_{DS}$-$V_{DS}$ characteristic for the relay in (a). The on-state resistance decreases with increasing gate voltage (2.2 k$\Omega$ at $V_G = 9.5$ V).
As $V_G$ is increased beyond $V_{\text{ON}_L}$ of the see-saw relay, the on-state resistance of the W to W contact decreases from ~4.0 kΩ to ~2.2 kΩ, as shown in Figure 4.16(b). This is because the effective contact area ($A_R$) increases with increasing $F_{\text{ELEC}}$. Note that $R_{\text{CONTACT}}$ at each side of the channel on either side is dependent upon the conditions under which the contact is formed as well as the properties of the contacting electrode material [9], [50]:

$$R_{\text{CONTACT}} = \frac{4 \cdot \rho \cdot \lambda}{3 A_R} = \frac{4 \cdot \rho \cdot \lambda \cdot H \cdot \xi}{3 F_{\text{ELEC}}(T_{\text{ACT}})},$$

where $\rho$ and $\lambda$ are the resistivity and the mean free path of electrons of the contacting electrode material, respectively, $A_R$ is the effective contact area, $H$ is the hardness of the contacting electrode material, and $\xi$ is the deformation constant.

Figure 4.17: Measured values of $g_m$ for the relay in Figure 4.16(a): $g_m$ increases only slightly with increasing $V_G$.

Figure 4.18: (a) Measured $V_{\text{ON}_L}$ and $V_{\text{ON}_R}$ with decreasing $V_{\text{BR}}$ for a different see-saw relay. The switching voltages are reduced with decreasing $V_{\text{BR}} = V_{\text{DD}}$. (b) Measured values of $V_{\text{ON}_L}$ and $V_{\text{ON}_R}$ with change in body-bias for the relay shown in Figure 4.16(a). For each pair of $V_{\text{ON}_L}$ and $V_{\text{ON}_R}$, $V_G$ was swept from $V_{\text{BL}}$ to $V_{\text{BR}}$. The difference between $V_{\text{BR}}$ and $V_{\text{BL}}$ was kept constant at $V_{\text{DD}} = 6$ V, e.g., $V_G$ was swept from −3 V to 3 V with $V_{\text{BL}} = −3$ V and $V_{\text{BR}} = 3$ V.
Figure 4.17 shows that measured values of $g_m$ for the corrugated see-saw relay are relatively low (less than about 0.4 mS/μm of channel width) to be used for small-signal current amplification. The values of $g_m$ for a small-signal MOSFET are typically in the range between 10 and 30 mS/μm. For the 65 nm technology node ($I_D \approx 1$ mA/μm), a $g_m$ of 11 to 32 mS/μm is achieved with the overdrive voltage in the range between 70 to 200 mV [51].

Figures 4.18(a) and 4.18(b) show that the turn-on voltages of the see-saw relay can be adjusted via body-bias. In Figure 4.18(a), both $V_{BR}$ and $V_{DD}$ were decreased while $V_{BL}$ was kept at 0 V, whereas in Figure 4.18(b), $V_{BR}$ and $V_{BL}$ were reduced by the same amount while $V_{DD}$ was kept at $V_{BR} - V_{BL} = 6$ V. The asymmetry of switching about $V_{DD} / 2$ in both figures is caused by different $T_{ACT}$ on the left and right sides of the relay (due to the effect of negative strain gradient).

Figures 4.19 shows measured VTC of a different corrugated see-saw relay. This relay shows complementary switching behavior that is almost perfectly symmetric about $V_{DD} / 2$. The slight asymmetry of switching indicates that the strain gradient effect was not completely removed.

4.5. Summary

A see-saw relay design is proposed and demonstrated to provide for perfectly complementary switching behavior that is symmetric about $V_{DD} / 2$. The main advantages of this design are that it can maximize the operating voltage margin and minimize the crowbar current and that by allowing active turn-off, it can also minimize the asymmetric switching behavior and improve the reliability of a relay-based digital logic technology. The complementary see-saw relay design is versatile for mechanically implementing various logic functions and a latch function with a single structure. It is a viable option for the implementation of compact, relay-based ultra-low-power integrated circuits in the future.
4.6. References


Chapter 5

Multi-Electrode Relays for Compact Implementation of Digital Integrated Circuits

Abstract: In this chapter, multi-gate, multi-source/drain relays are proposed and demonstrated to enable compact implementation of zero-leakage digital electronics at no incremental process cost. Basic multi-input logic functions (e.g. AND, NAND, OR, MAJORITY, and WEIGHTED) can be implemented by tuning the body bias voltage of a single multi-input relay. The gate electrodes of the multi-input relay can be properly sized to decode an analog input signal level, so that flash-type analog-to-digital converters can be achieved via multi-gate operation. Performance improvement with scaling is also discussed.

5.1. Introduction

Nano-electro-mechanical relay technology has been proposed as a potential solution to overcome the fundamental energy-efficiency limit of Complementary-Metal-Oxide-Semiconductor (CMOS) technology, because it offers the ideal characteristics of zero off-state leakage current and abrupt on/off switching behavior which provide for zero static power consumption and aggressive supply voltage ($V_{DD}$) scaling [1]. Various digital integrated-circuit (IC) building blocks (logic, memory, and clocking structures) implemented purely with micro-electro-mechanical relays have been demonstrated recently [2], [3]. New relay designs that incorporate multiple input (gate) electrodes and multiple pairs of output (source/drain) electrodes would enable more compact implementation of digital ICs (Figure 5.1) at no incremental process cost. In this chapter, the first functional prototype multi-electrode relays are presented and performance improvement with scaling is discussed.

Figure 5.1: A generic multi-input relay combinational logic circuit.
Figure 5.2: Perspective view of a 2-input, dual-source/drain relay structure; In the off-state, an air gap prevents DC current to flow between the source and drain electrodes on each side. In the on-state, electrostatic force between the gate(s) and the body brings both channels into contact with the pairs of source/drain electrodes. Both gate electrodes are equally sized (472 \( \mu \text{m}^2 \) each).

5.2. 2-Input, Dual-Source/Drain Relay

Figure 5.2 illustrates the structure and operation of a 2-input, dual-source/drain relay: In the off-state, immeasurably low leakage current flows because an air gap (of thickness \( T_{\text{CONT}} \)) separates the channels from the pairs of source/drain electrodes on each side. As voltage applied to the gate(s) increase(s) beyond a threshold “pull-in” voltage \( (V_{\text{PI}}) \), the relay turns on abruptly because the attractive electrostatic force between the gate electrode(s) and the movable body electrode brings the channels (attached underneath the body electrode via an insulating oxide layer) into contact with the source/drain electrodes. A CMOS-compatible (peak substrate temperature < 410 °C) surface-micromachining process (Figure 5.3) was used to fabricate all of the multi-gate, dual-source/drain relays in this work. Scanning electron microscopy (SEM) images of a double-gate, dual-source/drain relay are shown in Figure 5.4.

Figure 5.3: Low-thermal-budget process used to fabricate multi-input, dual-source/drain relays: (a) Tungsten (W) gate, source, and drain electrodes defined on the Al\(_2\)O\(_3\)-coated substrate. (b) 1\(^{st}\) sacrificial Low-Temperature-Oxide (LTO) layer deposition at 400 °C, followed by contact region definition. (c) 2\(^{nd}\) sacrificial LTO layer deposition, followed by W channel formation. (d) Al\(_2\)O\(_3\) insulator ALD at 300 °C. (e) p+ poly-Si\(_{0.4}\)Ge\(_{0.6}\) body layer deposition at 410 °C, followed by LTO deposition and body patterning. (f) Release etch in vapor-HF at 50 °C to form an air gap.
Figure 5.4: (a) Plan view scanning electron micrograph (SEM) of the 2-input relay. (b) Cross-sectional SEM (X-SEM) from focused ion beam (FIB) cut through A-A’ in (a).

Figure 5.5 shows measured $V_{pi}$ values for a relay with 2 equally-sized gate electrodes (472 $\mu$m$^2$). Due to body curvature resulting from undesirable strain gradient within the structural layer, the actuation gap ($T_{ACT}$) is larger at the center than at the edge of the body so that $V_{pi}$ for the center gate electrode (input combination [1, 0], where ‘1’ $\equiv V_G$) is higher than that for the edge gate electrode (input combination [0, 1]). The measured $I_{ds}-V_G$ characteristics for double-gate operation, i.e. with the 2 gates tied together (input combination [1, 1]), are shown in Figure 5.6. The gate switching voltages can be tuned by biasing the body electrode, as shown in Figure 5.7. $V_{pi}$ for single-gate operation (with the other gate grounded) is more sensitive to body bias because of the additional electrostatic force between the inactive (grounded) gate and the body.

Figure 5.5: Measured pull-in voltages ($V_{pi}$) of the 2-input relay. ‘1’ $\equiv V_G$. 
Figure 5.6: Measured $I_{DS}-V_G$ characteristic; Both gate electrodes were swept to 12.5 V.

Figure 5.7: Measured $V_{PI}$ and $V_{RL}$ with changes in body-bias voltages. (a) Both gate electrodes were swept. (b) The gate edge electrode ($V_{GE}$) was swept.

Figure 5.8 demonstrates that a single 2-input relay (with drain electrodes connected to a power supply and source electrodes connected to an oscilloscope with 1 MΩ internal resistance) can perform either the AND function or the NAND function, depending on the body bias voltage. If the input voltage level is increased sufficiently (reference Figure 5.5), a 2-input relay performs the OR function. This is demonstrated in Figure 5.9, which also shows that the output voltage range is solely determined by the drain bias voltage and hence can be different for each set of source/drain electrodes. This feature can be leveraged for voltage level conversion applications.

Figure 5.10 shows measured 2-input relay turn-on delay ($t_{DELAY}$) as a function of the driving gate voltage, for single-gate and double-gate operation. Double-gate operation is faster due to larger electrostatic force between the gates and the body. In both cases, $t_{DELAY}$ is reduced with increasing gate overdrive. A negative body bias also improves $t_{DELAY}$ because it serves to reduce $T_{ACT}$ and $T_{CONT}$, resulting in larger electrostatic force and shorter distance to switch on. Figure
Figure 5.8: Measured chronogram for 2-input AND and NAND gates illustrating full-rail swing at the output. The drain electrodes were connected to the power supply ($V_{DD} = 8$ V), and the source electrodes were tied together to form the logic gate output node. (a) INPUT 1 signal. (b) INPUT 2 signal. (c) AND output signal. $V_B = -4$ V. (d) NAND output signal. $V_B = 12$ V.

Figure 5.9: Measured chronogram for a 2-input OR gate showing voltage level conversion. The left and right drain electrodes were at 12 V and 6 V, respectively. Each source electrode serves as the logic gate output node. $V_B = 0$ V. (a) INPUT 1 signal. (b) INPUT 2 signal. (c) OR output signals at 12 V (left source) and 6 V (right source).

5.11 shows that on-state resistance ($R_{ON}$) is fairly stable, staying below 10 kΩ after $3 \times 10^7$ on/off cycles, which is adequate for digital logic applications [3].
5.3. 3-Input Relay

By partitioning the gate layer into 3 electrodes (Figure 5.12), various 3-input logic functions are realized by adjusting the input voltage level, as shown in Figure 5.13. (Again, $V_{PI}$ for each gate electrode is different due to body curvature resulting from an undesirable strain gradient within the structural layer.) Measured $I_{DS-V_{G}}$ characteristics for the outer two gates (Y and Z) tied together (input combination [0, 1, 1]) are shown in Figure 5.14. The additional input electrode increases the versatility of the relay: basic logic functions, such as AND, MAJORITY ($X \cdot Y + Y \cdot Z + X \cdot Z$), and OR, are achieved by adjusting the input voltage level, as demonstrated in Figure 5.15. Similarly as for the 2-input relay, $t_{DELAY}$ can be improved by body-biasing and/or increasing gate overdrive (Figure 5.16).
Figure 5.12: (a) Three-dimensional (3-D) schematic of a 3-input relay structure. The vertical dimensions are as shown in Figure 5.3. All gate electrodes are equally sized (288 μm² each). (b) Plan-view SEM of the 3-input relay. (c) X-SEM from FIB cut through A-A’ in (b). (d) X-SEM through B-B’ in (b).

Figure 5.13: Measured $V_{PI}$ of the 3-input relay. ‘1’ $\equiv V_G$. The logic expression for a MAJORITY gate is $X \cdot Y + Y \cdot Z + X \cdot Z$.

Figure 5.14: Measured $I_{DS}$-$V_G$ characteristic of the 3-input relay with vs. without applying a body-bias voltage.
Figure 5.15: Measured chronogram for 3-input **AND**, **MAJORITY**, and **OR** gates. The drain electrodes were connected to the power supply (6 V), and the source electrodes were tied together to form the logic gate output node tied to GND via the 1 MΩ internal resistance of the oscilloscope. (a) **INPUT X** signal (to “Gate X”). (b) **INPUT Y** signal (to “Gate Y”). (c) **INPUT Z** signal (to “Gate Z”). (d) **AND** output signal. (e) **MAJORITY** gate ($X \cdot Y \cdot Z + Y \cdot Z + X \cdot Z$) output signal. (f) **OR** output signal.
Figure 5.16: Measured turn-on delay of the 3-input relay with increasing gate overdrive.

Figure 5.17: Measured, linearly-increasing $V_{\text{PI}}$ of a 3-input relay with differently-sized gates for an analog-to-digital converter (ADC).

For use as a flash-type analog-to-digital converter (ADC), the switching voltages for single-gate (most significant bit, MSB), double-gate, and triple-gate (least significant bit, LSB) operation must decrease linearly to properly decode an analog input signal level ($v_{\text{AC}}$). This can be achieved by properly sizing the gate electrodes, as shown in Figure 5.17. As an example, if $v_{\text{AC}}$ is between 11.7 V and 13.3 V, only the LSB relay (with $v_{\text{AC}}$ driving all 3 input electrodes) turns on; the other two relays (with $v_{\text{AC}}$ driving only the 2 smallest input electrodes, or with $v_{\text{AC}}$ driving only the smallest input electrode) do not turn on, so that the thermometer code [001] is generated.
Figure 5.18: (a) 3-D view of a 4-input relay. The vertical dimensions are as shown in Figure 5.3. The “Gate Z” is weighted heavier (400 \(\mu\)m\(^2\)) than the other gate electrodes (128 \(\mu\)m\(^2\) each). (b) SEM of the relay.

Figure 5.19: (a) Measured \(V_{pi}\) of the 4-input relay at 298 \(^\circ\)K under N\(_2\) purge at 1 atm. ‘1’ \(\equiv V_G\). \(V_{DS} = 2\) V and \(V_B = 0\) V. The BOOLEAN expression for a WEIGHTED gate is \(Z \cdot (W + X + Y)\).

5.4. 4-Input Relay

Figure 5.18 shows a 4-input relay structure used to demonstrate the possibility of performing complex logic functions by adjusting the areas of the input electrodes. The area of the outermost gate electrode (Gate Z) is designed to be larger than that of the other gate electrodes (Gates W, X, and Y) to realize the function \(Z \cdot (W + X + Y)\), i.e. the relay turns on only when the input signals to the larger electrode and at least one of the other gate electrodes are “high.” Figure 5.19(a) shows the input voltage ranges required for the relay to perform the AND or WEIGHTED \((Z \cdot (W + X + Y))\) functions, and Figure 5.19(b) shows the measured \(I_{DS}-V_G\) characteristic for quadruple-gate operation, i.e. with the 4 gates tied together (input combination \([1, 1, 1, 1]\)). Note that the switching hysteresis is relatively large, which can adversely affect the relay functionality (such that it does not turn off if an input signal changes from “high” to “low”). Recent improvements to the relay fabrication process and design mitigate this issue, as demonstrated by the measured \(I_{DS}-V_G\) characteristic in Figure 5.19(c) [4]. Similarly as for a 3-input relay, the gate electrodes of the 4-input can be sized to generate each bit of a 4-bit thermometer code for flash-type ADC applications (Figure 5.20).
5.5. Multi-Electrode Relay Scaling

The dimensions of multi-gate, dual-source/drain relays must be scaled down to reduce their operating voltage for improved energy efficiency as well as improved layout area efficiency. The operation of a multi-electrode relay scaled to a 22-nm-equivalent technology node was simulated using Finite-Element-Method (FEM) software [6], [7]. The results in Figure 5.21 indicate that sub-500-mV operation is achievable (c.f. $V_{DD}$ projected for 8-nm CMOS technology is 0.6 V [8]).
Figure 5.21: A 2-input relay scaled to a 22 nm technology node.

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</tr>
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Finite-Element-Method Simulation

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<th>$V_{\text{RL}}$ [mV]</th>
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<td>290</td>
</tr>
<tr>
<td>[1, 0]</td>
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<td>290</td>
</tr>
<tr>
<td>[1, 1]</td>
<td>300</td>
<td>192</td>
</tr>
</tbody>
</table>

5.6. Summary

In this chapter, multi-gate, multi-source/drain relays are proposed and demonstrated for compact implementation of ultra-low-power digital electronics.
5.7. References


Chapter 6

Conclusions

This dissertation aimed to solve one of the important societal challenges we are facing today -- reducing greenhouse gas emissions by improving energy efficiency of future information-processing systems. To that end, a nano-electro-mechanical (NEM) relay technologies that offer zero off-state leakage current and thus allows ultimate $V_{DD}$ scaling have been investigated.

In this work, design challenges for NEM relay technology were addressed. In particular, improvements in relay design and process technology, which led to the successful demonstration of purely-mechanical digital IC building blocks, were discussed. In addition, multi-electrode relays that would enable smarter design and compact implementation of zero-static-power digital electronics were discussed.

As a final remark, the author believes that NEM relay technology will pave a revolutionary pathway to realize truly “greener,” “smarter” computing of future electronics systems (e.g. tabletop and/or portable super-computer).

6.1. Contributions of This Work

The key contributions of this work are summarized, as follows:

In Chapter 2, improvements in four-terminal (4-T) relay design were demonstrated to provide for improved electrostatic integrity, i.e. a strong body bias effect with equally effective relay switching using either the movable electrode or the underlying actuation electrode as the gate, a dramatically reduced drain bias effect on the gate switching voltage, and a minimal actuation due to the parasitic channel-to-body potential.

In Chapter 3, a 4-T relay was demonstrated to function as a memory cell. Thus, a 4-T relay logic technology (reference Chapter 2) can offer embedded memory capability at no additional process cost.

In Chapter 4, a see-saw relay design that provides for perfectly complementary switching behavior that is symmetric about $V_{DD} / 2$ was proposed and demonstrated. This design can maximize the operating voltage margin, minimize the crowbar current, and improve the
reliability (by allowing active turn-off) of a relay-based logic technology. The complementary see-saw relay design is versatile for implementing basic logic functions and a latch function with a single structure.

In Chapter 5, multi-gate, multi-source/drain relays were proposed and demonstrated to enable smarter design and compact implementation of ultra-low-power digital electronics without incurring additional process cost.

6.2. Future Directions

Source/Drain (and Channel) Engineering: The Tungsten (W) film used for the source/drain and channel electrodes tends to oxidize, once it is exposed to air. The W native oxide (typically composed of conductive WO$_2$ and W$_2$O$_5$ and insulating WO$_3$ [1]) always resides in the contacting regions (at the surface of the source/drain and channel) of a released device. This oxide formation is undesirable, in that $I_{ON}$ (and hence $R_{ON}$) of the relay can increase over the operating lifetime of the relay.

Similarly as for the switching mechanism of Resistive-Random-Access-Memory (ReRAM) [1], a relay in the on-state can show a high-resistance state when the drain-to-source bias ($V_{DS}$) is not sufficiently high -- perhaps due to the insulating WO$_3$ component. When the $V_{DS}$ is increased beyond a certain level, however, it shows a low-resistance state -- perhaps because conducting filaments are formed (WO$_2$ and/or W$_2$O$_5$) in the oxides between the source/drain and channel electrodes.

In order to ensure reliable operation of relay-based circuits, stable $I_{ON}$ (and hence $R_{ON}$) must be achieved. An alternative contact material, e.g. Ruthenium, conductive Ruthenium Oxide, or Titanium Nitride, should be adapted for the source/drain and channel electrodes.

Air-Gap Thickness Engineering: In this work, the as-fabricated, contact-gap-to-actuation-gap thickness ratio ($T_{CONTACT}$ to $T_{ACT}$) was chosen to be 0.5. This ratio needs to be smaller than one third, in order to minimize the hysteric switching behavior -- by allowing the relay to operate in non-pull-in mode. Otherwise, $V_{DD}$ scaling would be limited by the release voltage of the relay. To achieve most energy-efficient relay operation, however, the relay should operate in pull-in mode (with a $T_{CONTACT}$-to-$T_{ACT}$ ratio of 0.7 to 0.8) [2]. Therefore, energy-performance tradeoff between a relay chain operating in non-pull-in-mode vs. multi-stage CMOS inverter chain needs to be evaluated, if non-pull-in-mode operation is preferred for relay scaling.

Surface (or Contact) Engineering: A relay that operates in non-pull-in-mode would not eliminate the hysteric switching behavior, due to surface adhesion that is always present when the channel and source/drain surfaces are brought into contact. This hysteric switching behavior
is exacerbated if the relay is hermetically sealed in an inert environment, because the absence of any chemical films and absorbates at the interface usually increases surface adhesion [3]. From endurance standpoint, however, the contact surface should remain clean to ensure good $R_{ON}$ stability over a longer lifetime [4]. Therefore, a novel material, e.g. Graphene, that shows low surface energy and adhesion, high current-carrying capability, and high stability in harsh environments, might be a compelling surface-coating material to minimize hysteresis as well as to achieve stable $R_{ON}$.

**Gate Stack Engineering**: The gate stack of a relay should show low strain gradient (on the order of $10^{-5} \mu m$ or less) to achieve low operating voltages, since these require the formation of very small actuation and contact gaps with good uniformity. In addition, the gate stack material should be free of any mechanical reliability issues, such as fatigue, creep, and stress rupture, for use in digital IC products. These might be difficult to achieve with any polycrystalline film, because of columnar growth of micro-grains that cause strain gradient in film thickness and because of the micro-voids, dislocations, and defects that are inherently present along film grain boundaries. Therefore, a new material might be needed for the relay structure. For example, the hinge material of the Texas Instruments Digital Mirror Display (DMD) devices -- the amorphous TiAl$_3$ sputtered with 4% Oxygen -- was found to yield the lowest stress relaxation [5]. With this material incorporated, a large array of DMD devices (more than 500,000 elements) that can rotate through a large angle (± 10 degrees) has been demonstrated to operate reliably with more than $10^{12}$ cycles without any mechanical failures (such as fatigue, stress rupture, and creep) [6], [7].
6.3. References


