### Title and Subtitle

A Novel Approach to Turbulence Stimulation for Ship-Model Testing

### Abstract

The goal of this project was to develop an approach for creating a boundary layer on a ship-model that more closely represents the actual boundary layer on a full-size ship. Analytical predictions and experimental data were used to work towards developing a set of guidelines to provide a more rational approach to replicating a ship's boundary layer through the use of turbulence stimulation. During the course of this project, the primary focus was on factors that affect boundary layer flow and transition and how these factors can be used for determining the optimum location of turbulence stimulation. A series of tests was performed first on a flat plate and then on a 2-D model. The tests consisted of using hot film sensors to measure the time fraction of turbulent flow within the model's boundary layer. These data were then analyzed to determine the most effective means to create a turbulent model boundary layer. The results obtained were able to shed light on the issues of sizing and placement of turbulence stimulation devices and provide guidance for future research in the field.
Abstract

Ship-model testing is vital component of naval architecture, allowing testing and evaluation on a small scale. The goal of this project was to develop an approach for creating a boundary layer on a ship-model that more closely represents the actual boundary layer on the ship. Flow within a ship’s boundary layer is turbulent for nearly the entire length of the ship. However, in the boundary layer on a model, the flow can range from completely laminar, to intermittently laminar or turbulent, or fully turbulent. In order for model tests to provide accurate predictions of ship drag and powering, the boundary layer of the ship and the model must be “similar.” Currently, the solution to creating similar boundary layers is empirically based and is guided largely by the individual naval architect’s experience and intuition. This project used analytical predictions and experimental data to work towards developing a set of guidelines to provide a more rational approach to replicating a ship’s boundary layer through the use of turbulence stimulation. During the course of this project, the primary focus was on factors that affect boundary layer flow and transition and how these factors can be used for determining the optimum location of turbulence stimulation. A series of tests was performed first on a flat plate and then on a 2-D model. The tests consisted of using hot film sensors to measure the time fraction of turbulent flow within the model’s boundary layer. These data were then analyzed to determine the most effective means to create a turbulent model boundary layer. The results obtained were able to shed light on the issues of sizing and placement of turbulence stimulation devices and provide guidance for future research in the field.
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1.1 Background

Since the days of Leonardo Da Vinci, model testing has been an integral part of naval architecture. Today, nearly all vessel designs, from yachts and pleasure craft to merchant oil tankers and U.S. Navy ships, have been validated through model testing. A large component of ship-model testing is gathering and analyzing resistance, or drag, data for a given hull form. As van Manen and van Oossanen note, ship resistance is related to “the proportions and shape… of the hull, the size and type of propulsion plant to provide motive power, and the device or system to transform the power into effective thrust” (van Manen and van Oossanen, 1988). Ship-model testing is essential, then, to ensure that ship effectiveness is maximized while key factors such as power consumption and fuel costs are minimized.

Even while model testing plays such a prominent role in the ship design process, there are those who would question why more technologically advanced methods of design are not used. The use of computational fluid dynamics (CFD) and computer simulation for modeling has been embraced by numerous disciplines, such as civil and aeronautical engineering. However, within naval architecture, the ability to use computer simulation is hindered by the complicated nature of ship resistance. The ability to predict drag and power requirements accurately is illusive computationally. A ship is constantly subjected to unique and unpredictable forces. For instance, a ship experiences bow slap as it drives through waves. This occurrence, in which the bow of the ship emerges from the water at the crest of wave and then experiences a strong force as the bow slaps down back into the water is extremely unpredictable and is a function of numerous variables including speed, and wave height. A ship, then, must be physically modeled and tested in numerous environments to determine the design’s ability to deal with the inhospitable conditions of the sea.
2.1 Similitude

In order to successfully test a ship design using models, a model and a ship must be in a condition of similitude. Similitude is defined as being able to utilize “measurements made in the laboratory [to predict] the behavior of other similar systems” (Moran et al, 2003). In the context of naval architecture and model testing, similitude is taking the results determined from a model that is “similar” to a ship and scaling these results to predict how a ship will actually operate in the marine environment.

There are three conditions that must be met for a ship and a model to be considered in a state of similitude. The first of these is the condition of geometric similitude. Geometric similitude requires that all length ratios be the same. If the length of a ship is 100 feet long and the length of a model is 10 feet long, in order for the condition of geometric similitude to be satisfied, all ratios of length from ship to model must be 10 to 1. The second condition is that of kinematic similitude. Kinematic similitude requires that the flow fields around the model and ship have scaled magnitudes and identical directions. If water flows across the ship from bow to stern, the flow must be the same for the model. Both geometric and kinematic similitude are easily achieved as compared to the final condition that must be satisfied, that of dynamic similitude.

Dynamic similitude requires that the forces associated with the fluid motion around both the model and ship have scaled magnitudes and identical directions. The forces of fluid motion are those that are associated with the drag experienced by the model or ship. Dynamic similitude is achieved when both the ship and the model experience comparable frictional and residuary resistance. Frictional and residuary resistances are functions of the Froude (Fn) and Reynolds (Rn) numbers respectively. These two dimensionless quantities are key components of
determining a ship’s coefficient of total resistance and are used to assure that a given model and ship reach complete dynamic similitude.

2.2 Ship Resistance

The resistance a ship or a model experiences, as mentioned above, is composed of two components, frictional and residuary resistance. Frictional resistance is the effect of the shear force water imparts on the hull of a ship or model. Residuary resistance is an overarching term which encompasses all resistances that are not associated with frictional forces acting on a ship. The prime source of residuary resistance is wave-making resistance. The summation of a ship or model’s frictional and residuary resistance is equal to that ship or model’s total resistance. Figure 1 below demonstrates this relationship.

Figure 1: Ship Resistance Components (Gillmer and Johnson, 1982)
The above figure plots the resistance a ship or model experiences versus a generic speed scale. The lower dashed line represents the frictional resistance experienced by the ship or model, while the top line is the sum of frictional and residuary resistance or the total resistance. The trend of the figure shows that at higher speeds, residuary resistance, especially wave-making resistance is dominant, whereas at lower speeds the effect of friction is greater. Thus when testing models at slow speeds, frictional resistance is the primary form of resistance measured whereas the total resistance of a ship running at high speed is primarily residuary resistance.

A ship or model’s resistance can be expressed in terms of various dimensionless coefficients. The equation for the coefficient of total resistance is as follows:

\[ C_T = \frac{R_T}{\frac{1}{2} \rho U^2 S} \]  

(1)

Where

\( C_T \) = coefficient of total resistance  
\( R_T \) = total resistance  
\( \rho \) = density of water  
\( U \) = model or ship’s velocity  
\( S \) = wetted surface area of ship or model

Just as the resistive force experienced by a ship or model is made up of two components, the coefficient of total resistance is comprised also of two parts, the coefficient of frictional resistance and the coefficient of residuary resistance. These coefficients are summed according to the following relationship:

\[ C_T = C_R (Fn) + C_F (Rn) \]  

(2)

Where

\( C_T \) = coefficient of total resistance  
\( C_R \) = coefficient of residuary resistance  
\( C_F \) = coefficient of residuary resistance
The above relationship indicates that the two critical numbers, the Froude and Reynolds numbers, each play a major role in the overall coefficient of resistance for a ship or model.

2.3 Residuary Resistance and Froude Number

The first component of total resistance discussed above is residuary resistance. Residuary resistance is a term used to characterize all resistive forces that are not caused by friction. Examples of residuary resistance are form drag, which is the change in pressure caused by hull geometry, and wave-making resistance, the primary source of residuary resistance. The coefficient of residuary resistance is a function of one of the two dimensionless numbers mentioned previously, the Froude number, named for William Froude. The Froude number represents the ratio between the inertia of an object and the gravitational forces that object experiences. The number is used as relationship between speed of the ship or model and its length. The Froude number is used to scale the speed of a model to match the scaling of its length as compared to the ship. The formula for the Froude number is

\[ F_n = \frac{U}{\sqrt{gL}} \]  

(3)

Where

- \( F_n \) = Froude number
- \( U \) = ship or model velocity
- \( g \) = acceleration due to gravity
- \( L \) = length of ship or model

This relationship is used to determine the coefficient of residuary resistance, one portion of the total coefficient of resistance for the ship or model.

2.4 Frictional Resistance and Reynolds Number

The remaining portion of the total resistance experienced by a ship or model is frictional resistance. Frictional resistance is caused by the shear force imparted on a ship or model by
water flowing over the hull. The amount of frictional resistance is directly related to the characteristics of flow within a ship or model’s boundary layer. The boundary layer is a “relatively thin layer next to [a] surface…in which the velocity of the fluid changes from 0 on the surface to $U$ at some distance away from the surface” (Moran et al, 2003). The variable $u$ represents the mean velocity of the water relative to the hull, which is 0 at the surface because of the no-slip condition. The no-slip condition states that a water particle encountering a surface will not continue around the object, it will “stick” in place on the surface and have zero velocity. At the same point on the surface, if one moves further away from that surface, the velocity of the fluid increases from 0 at the surface until it reaches the free-stream velocity $U$ at some distance $\delta$, termed the boundary layer thickness. Moving down the surface of a body in the direction of flow, $\delta$ increases. Figure 2 below is a diagram of a boundary layer formed by a flat plate or wall.

![Figure 2: Diagram of Flat Plate Boundary Layer](image)

The overall layer that is formed between the body and where flow reaches its free-stream velocity is considered the boundary layer. Within this boundary layer the flow is considered to be either turbulent or laminar. Laminar flow is marked by smooth, uninterrupted flow whereas turbulent flow is rough and fluctuating.

The coefficient of frictional resistance is a function of the second critical quantity discussed above, the Reynolds number, $Rn$. Because Osborne Reynolds experimented with the frictional resistance coupled with laminar and turbulent flow, the number is named for him. The
Reynolds number is a measure of the relative importance of inertial and viscous effects on the flow. That is to say, the Reynolds number relates the viscosity, or a fluid’s resistance to shear, the speed of water and the length of a ship. The formula for the Reynolds number is

\[ Rn = \frac{UL}{\nu} \]  

(4)

Where

- \( Rn \) = Reynolds number
- \( U \) = ship or model velocity
- \( L \) = length of ship or model
- \( \nu \) = kinematic viscosity of testing fluid

The Reynolds number identifies whether flow is laminar or turbulent. If a ship or model has a Reynolds number greater than 3 million, the flow around that ship or model is considered turbulent. The significance of this difference is the effect the flow has on the ship. If a ship or model experiences laminar flow, the frictional drag will be lower than if the flow were turbulent. Turbulent flow, however, results in much higher frictional drag force; that is, the effect of the water moving over the hull causes added friction and serves to impede the ship’s forward motion. On all ships the flow passing around the hull is virtually all turbulent, meaning that there is a large amount of frictional drag that must be accounted for when conducting model testing.

2.5 Ship-Model Tester’s Dilemma

In order to be in a state of dynamic similitude, a ship-model tester must ensure that a model for a given ship design will experience similar frictional and residuary resistance meaning both ship and model have the same Froude number and Reynolds number. However, here the tester encounters what is known as the Ship-Model Tester’s Dilemma, which van Manen and van Oossanen define as “the conditions of mechanical similitude for both friction and wave-making [residuary resistance] cannot be satisfied in a single test” (van Manen and van Oossanen, 1988).
It is impossible to run a test on a model and keep the Froude number and the Reynolds number the same as experienced by the ship. The problem stems from the location of the length within the equations for the two critical numbers. The Froude number, equation (1), has the square root of length in the denominator while the variable for speed is in the numerator. Therefore, if a model has a scale factor of 100 (i.e. the length of the ship over the length of the model is equal to 100), the model would have to be run at a speed 10 times slower than that of the ship. These kinds of speeds for model-testing can be easily attained. The Reynolds number, equation (2), however, has both length and speed in the numerator. Therefore, assuming the kinematic viscosity remains fairly constant, a model 100 times shorter than the ship design would need to be tested at speeds 100 times greater than that expected for the ship. It would be very difficult to run a model at such high speeds, making it almost impossible to achieve the same Reynolds number for a model and ship. Thus, the model ship tester must run tests with a Froude number equal to that of the full-scale ship while developing a system to account for the difference in Reynolds numbers and the subsequent difference in frictional drag experienced by the model and ship.

The current solution to the model ship tester’s dilemma, first discussed by Froude in 1877, is to extrapolate data to achieve acceptable results. As seen in equation (3), the total resistance experienced by a ship is the sum of the residuary resistance and frictional resistance, which are assumed to be functions of the Froude number and the Reynolds number respectively. The total resistance of a model can be measured and recorded, while the coefficient of frictional resistance is calculated using the smaller model’s Reynolds number and the International Towing Tank Conference’s (ITTC) 1957 formula
\[ C_F = \frac{0.075}{(\log_{10} Rn - 2)^2} \quad (5) \]

Where

\[ C_F = \text{coefficient of frictional resistance} \]
\[ Rn = \text{Reynolds number} \]

The ITTC formula is an empirically derived relation between Reynolds number and the coefficient of residuary resistance that is based off flat plate testing conducted by Hughes and Allan in 1951. By subtracting the calculated frictional resistance coefficient, \( C_F \), from the measured total resistance, one obtains the model’s coefficient of residuary resistance. If the Froude numbers are the same for both the ship and the model, then coefficient of residuary resistance for the ship will be the same as that obtained from the model. Using the ITTC formula again, the full-scale ship’s coefficient of frictional resistance can be calculated and added to the coefficient of residuary resistance to give the ship’s coefficient of total resistance.

While this process of extrapolation is acceptable in many cases, various problems still arise. As stated above, turbulent flow creates more frictional resistance than laminar flow. By using a low Reynolds number on the model, one may be extrapolating inaccurate results for frictional resistance that can drastically affect final values. Figure 3 below illustrates this problem.
The ITTC formula used for calculating the coefficient of frictional resistance assumes that the flow is turbulent over the entire length of a model or a ship. Figure 3 shows, however, that for a model this is not the case. There are regions of laminar and transitional flow that are not accounted for by the ITTC formula. In order to achieve the best results from model testing, then, the laminar and transitional regions must be moved as far forward as possible to imitate the regions experienced within a ship’s boundary layer.

2.6 Turbulence Stimulation

As mentioned previously, a ship experiences turbulent flow over a vast majority of the hull as it moves through water, whereas ship-models may experience laminar flow over all or most of the hull. In order to achieve dynamic similitude between a ship and a model, the flow
within a model’s boundary layer must mimic the flow in a ship’s boundary layer. The flow within a model’s boundary layer is often times laminar or transitional (i.e. partially turbulent). Consequently, to make a model’s boundary layer more representative of a ship, the boundary layer flow must be made turbulent. The primary method to make the flow within a model’s boundary more turbulent is turbulence stimulation. Turbulence stimulation consists of “tripping,” or causing the laminar flow to transition into turbulent flow. In order to “trip” the flow, foreign objects are generally placed on the forward portion of the model’s hull. These objects include sand grains, small pins, Hama strips, and trip wires. Figure 4 shows some examples of turbulence stimulators.

Figure 4: Turbulence Stimulator Examples (Top Left, Small Pins; Top Right, Sand Grains; Bottom Left, Hama Strips; Bottom Right, Trip Wire)

Turbulence stimulators introduce instability to the flow around a model. This instability disrupts the flow and causes it to be turbulent. So, while the flow that would normally be associated with
the model should be laminar, the turbulent stimulator causes the flow to become turbulent. This
turbulent flow more closely represents the flow experienced within the boundary layer of a ship
and increases the frictional drag experienced by the model, more closely aligning the model’s
frictional drag with that of the full-size ship. All these items are featured on models in the
Hydromechanics Lab and are designed to disrupt the smooth, constant shape of the hull design
and thus prevent the water flowing around the model from remaining laminar. An effective
turbulence stimulation method will allow reliable frictional and residuary resistance data to be
obtained.

It would appear that, through the use of turbulence stimulation, the problem of similitude
between model and ship has essentially been resolved. However, a new problem has emerged
with turbulence stimulation. There is no set methodology for determining the location, type, or
amount of turbulence stimulation. There are limited guidelines, primarily of empirical nature, to
answer questions about what type of stimulators should be used and/or where a given type of
stimulator should be placed on a model. Currently, the answers to the above questions are
different for each ship-model testing facility and ship-model tester. There is no consistent
method, based on flow physics, that can be used for a given ship type or model size between the
various tow tanks around the world. It is left for each person to discover his or her own method
based on trial and error and the constant tweaking of results to achieve the desirable outcome.

2.7 Previous Research

There has been previous work done in the area of turbulence stimulation for ship-model
testing, especially within the past 50 years or so. In 1951, Hughes concluded that the best results
for turbulence stimulation were “obtained by a relatively small number of moderate size pins
rather than by a large number of very small pins” (Hughes, 1951). However, Hughes makes no
definite statement about the steps necessary to successfully use turbulence stimulation on a given model. He even states that “it is hoped that the data given in the paper will assist other tanks to decide the best method of turbulence stimulation for their particular conditions”(Hughes, 1951).

Hughes presents valid data but acknowledges that there has been no attempt to set a definite system for use at all tow tanks and testing facilities.

In 1957, Hama investigated the problem of turbulence stimulation and outlined his experiment and solution. Hama prefaces his detailed explanation of his experiment and technique by stating that “The experiments presented are intentionally limited to qualitative observations. It is hoped that the present investigations will supplement more quantitative wind-tunnel investigations and provide a guide to further theoretical analysis which, in turn, may help further refinement in experimentation”(Hama, 1957). Hama’s experiment was meant to observe the vortices created when flow encounters turbulence stimulation on a flat plate and determine how these vortices transition into turbulent flow. Hama concluded that he had successfully been able to observe flow transition from laminar to turbulent and that the problem that lay ahead was finding the mechanism that ultimately triggered turbulent flow.

Studies in turbulence stimulation have also been conducted in the fields of aerodynamics and aeronautical engineering. Air flow over an airfoil or wing behaves in a similar fashion to water flowing over a hull form. Turbulence stimulation is thus utilized when turbulent flow is to be studied over a wing or airfoil. In 1986, J.C. Gibbings, discussed in his three-part paper what effect trips have on the transition of flow from laminar to turbulent over an airfoil. Gibbings examined both wire trips and what he termed “spherical trips,” which are comparable to the small pins pictured in Figure 2. Gibbings concluded that a single spherical trip is effective in tripping the flow but the size of such a trip generates unwanted effects in downstream regions of
the boundary layer (Gibbings, pt 2, 1986). He also concluded that using a “row of spherical roughness elements is effective for tripping transition [from laminar to turbulent flow]” (Gibbings, pt 3, 1986). Gibbings’ work with air flow is similar to the experimentation that will be done in this study with flow over a ship-model hull.

S.P. Schneider, a professor of aeronautical engineering at Purdue University, discussed methods for measuring the transition region within a boundary, that is, the region in which the flow transitions from laminar to turbulent flow. Schneider presents a method of using a probability density function (PDF) of collected data to determine the peaks of turbulent and laminar data (Schneider, 1995). While Schneider’s method is different from that done in this project, he acknowledges the importance of being able to replicate results for other conditions and produce a general case that can be used for various fluids and objects. Thus, the work done with turbulence stimulation in aerodynamics has provided the motivation for the relationship between momentum thickness Reynolds number and pressure gradient that will be explored in this project.

Most recently, MIDN Rebecca Islin conducted an independent research project in 2007 that investigated various turbulence stimulation devices. She wrote a paper entitled “Turbulent Flow Stimulation on a Thickened Panel.” Within the paper she discussed how her intended goal was to “bridge the gap between flat plates and ship-models” (Islin, 2007). Islin’s work in turbulence stimulation was intended to determine the best method of stimulation for a flat plate and see if that method could be adjusted and revamped to be successful in ship-model testing. While Islin’s experimental set up is the basis for this project, her data was collected and studied, but no real conclusions came from her work. The hypothesis for my study is that one can analytically determine the point along the hull of the model where turbulence stimulation will be
most effective. Thus, the project in a way picks up roughly where Islin left off in 2007. The goal was to test and verify the use of two computer programs in finding the ideal location of stimulators.
3.1 Momentum Thickness Reynolds Number

The analytical tools used were two computational fluid dynamics codes, developed by William J. Devenport and Joseph Schetz of Virginia Tech’s Department of Aerospace and Ocean Engineering. These codes are available for use from the Virginia Tech Department of Aerospace and Ocean Engineering website, <http://www.engapplets.vt.edu/>. The codes give us results that allow the computation of two key parameters, the momentum thickness Reynolds number, $Rn_\theta$, and the pressure gradient factor, $K$. The goal was to study these two parameters and determine the effect each has on the flow within the boundary layer and the impact on the effectiveness of turbulence stimulation.

As stated above, the most common form of Reynolds number, detailed in Equation (4), is calculated based off the overall length, $L$, of an object. However, since the Reynolds number is a dimensionless quantity, other variables may be used in place of the overall length. For instance, the local Reynolds number at a specific point along a body, in this case the hull of a ship, can be expressed as

$$Rn_x = \frac{U_x}{\nu}$$  \hspace{1cm} (6)

Where

- $Rn_x$ = Reynolds number based off longitudinal location
- $U$ = free stream velocity
- $x$ = longitudinal location of point of interest
- $\nu$ = kinematic viscosity of water

As one moves aft, the local Reynolds number increases until the greatest Reynolds number is achieved at the stern, where $x$ is equal to $L$. Thus, as the Reynolds number changes with relationship to hull location, one can pinpoint key spots that mark the possible transition from laminar to turbulent flow.
However, another form of the Reynolds number can be computed based on the momentum thickness of the boundary layer. Due to momentum losses to the frictional forces at the wall, a reduction in momentum flux occurs in the boundary layer as one moves downstream. Momentum flux is related to how much viscosity affects the flow in the boundary layer. Momentum thickness, \( \theta \), is a means to quantify this momentum flux reduction in terms of a length scale (Munson et al, 2006). Momentum thickness is obtained by comparing the momentum of a fluid at some point along the hull to the momentum an inviscid fluid would have at the same point. The momentum thickness at that point is the distance the flow of the inviscid fluid would have to be shifted in order to have the same momentum flux as the actual fluid. The equation for momentum thickness at a given point is as follows

\[
\theta = \int_{0}^{\delta} \frac{u}{U} \left( 1 - \frac{u}{U} \right) dy
\]  

(7)

Where

\[
\theta = \text{momentum thickness}
\]
\[
U = \text{free-stream velocity}
\]
\[
u = \text{velocity of the flow at a given distance normal to the wall}
\]
\[
\delta = \text{boundary layer thickness}
\]

The Reynolds number, as stated above, can also be expressed in terms of the momentum thickness. The equation for the momentum thickness Reynolds number thus becomes

\[
Rn_{\theta} = \frac{\theta U}{\nu}
\]  

(8)

Where

\[
Rn_{\theta} = \text{momentum thickness Reynolds number}
\]
\[
\theta = \text{momentum thickness}
\]
\[
U = \text{free-stream velocity}
\]
\[
\nu = \text{kinematic viscosity of water}
\]
If a ship or model has values of the momentum thickness Reynolds number around 800, the flow has the potential to become turbulent without stimulation at that point (Ridgely-Nevitt, 1967). The fluid codes used provided an analytical prediction of the values needed to calculate the momentum thickness Reynolds number for the models tested. These values were studied to determine a correlation between momentum thickness and turbulence stimulation.

### 3.2 Pressure Gradient Factor

The second parameter of interest in this study was the pressure gradient factor, $K$. The pressure gradient is directly related to the shape of the object, in this case the shape of the ship hull that moves through a fluid. The pressure gradient plays a large role in defining the characteristics of the flow over a surface. As Munson observes, the “variation in the free-stream velocity, is the cause of the pressure gradient in the boundary layer” (Munson et al, 2006). The pressure gradient is defined by another dimensionless quantity, the pressure gradient parameter, represented by the variable $K$. The equation for the pressure gradient factor is

$$K = \frac{\nu \cdot dU}{U^2 \cdot dx}$$  \hspace{1cm} (9)

Where

- $K$ = pressure gradient factor
- $U$ = free-stream velocity
- $\nu$ = kinematic viscosity of water
- $dU/dx$ = the rate of change of the free-stream velocity with respect to distance along the surface of an object

If $K$ for an object drops below $3.0 \times 10^{-6}$, the flow over the object at the point has the potential to be naturally tripped to turn turbulent without relaminarization. Relaminarization is a condition that occurs when a turbulent boundary layer returns to laminar flow due to a strong pressure gradient (Schetz, 1993).
3.3 Vortex Panel

As stated previously, the two codes from Virginia Tech provided analytical outputs that were used to calculate the values of momentum thickness Reynolds number and the pressure gradient factor. These two codes, the Vortex Panel and the Thwaites-Walz integral methods, are directly related, for the outputs of the Vortex Panel method are used as the inputs for the Thwaites-Walz method. The Vortex Panel method uses vortex sheets to model the flow around a model. The vortex sheets are shaped to match a hull form inputs based on a model’s half-breadths. It should be noted that the half-breadths of the model must be scaled so that the length of the inputted shape is normalized to one. Figure 5 below is a shot of the Vortex Panel output screen.

![Figure 5: Vortex Panel Applet Outputs](image-url)
The outputs are the pressure coefficient $C_p$, which is plotted versus the length of the model in the upper right-hand corner of the screen, and the tangential velocity of flow along a given waterline.

3.4 Thwaites-Walz Integral Method

The values for the pressure coefficient and the tangential velocity are then used as the inputs for the Thwaites-Walz integral method. The Thwaites-Walz method was formulated by A. Walz in 1941 and was expanded on by B. Thwaites in 1949. The method refines a method for relating momentum thickness and pressure gradient developed by K. Pohlhausen in 1921 (Schetz, 37-40). According to Joseph A. Schetz, one of the developers of the applet used, the Thwaites-Walz method has a “range of inaccuracy [that] is generally less that 10% for favorable pressure gradients” (Schetz, 40). The Thwaites-Walz method takes the tangential velocities and applies these velocities to a flat plate. Thus any model analyzed with any curvature must be normalized to represent a flat plate that has a length equivalent to the distance from stem to stern along the surface of the model. Figure 6 below is a screen shot of the Walz method window.
Figure 6: Walz Boundary Applet

The topmost plot on the above screen should have a similar shape to that of $C_p$ vs. x plot from the Vortex Panel screen. In the lower left-hand box, the parameters need to be adjusted to the appropriate velocity being analyzed as well as the proper kinematic viscosity of water. The applet calculates boundary layer thickness and pressure distribution for a given free-stream velocity. It should be noted that all the inputs for the Walz applet are in metric units and thus must be converted from standard units before analysis. The Walz applet provides six outputs which are then used to calculate $Rn_\theta$ and $K$. The outputs generated are
\( x/L \) = percent length along the chord the data pertains too

\( U_e/U \) = ratio of velocity at the edge of the boundary layer to free-stream velocity

\( \delta \) = boundary layer thickness

\( \delta^* \) = displacement thickness

\( \theta \) = momentum thickness

\( C_f \) = coefficient of friction

The outputs used for calculations were \( x/L, U_e/U, \) and \( \theta \). Equations 8 and 9 above and the following relationships were used to determine \( Rn_{\theta} \) and \( K \).

\[
U_e = \frac{U_e}{U} \tag{10}
\]

\[
\frac{dU_e}{dx} = \frac{U_{e2} - U_{e1}}{(x/L_2 - x/L_1)L_m} \tag{11}
\]

The values for \( Rn_{\theta} \) and \( K \) were calculated for a single velocity at various points along the length of a model. The applets were run multiple times to obtain results over a range of different velocities. Figure 7 below is a graphical representation of the computed results for \( Rn_{\theta} \) and \( K \) over the length of a model.
3.5 Blasius Flat Plate Theory

The first step towards experimentation was to ensure that the codes used provided valid results. To do this the codes were compared against the Blasius flat plate theory. The Blasius theory is the standard in fluid dynamics for theoretical prediction of laminar flow across a flat plate. Taking a single velocity, in this case 10 m/s, the theoretical boundary layer thickness and momentum thickness Reynolds number values were calculated. The boundary layer thickness was calculated using the following.

\[ \delta = \frac{5x}{\sqrt{Rn_x}} \]  

Where
\[ \delta = \text{boundary layer thickness} \]
\[ x = \text{length} \]
\[ Rn_x = \text{Reynolds number based off longitudinal location (equation 6)} \]
The momentum thickness Reynolds number was calculated using equation 8 but the momentum thickness was calculated using equation 13 below rather than the integral in equation 7.

\[
\theta = \frac{0.664x}{\sqrt{Rn_x}}
\]  

(13)

Where

\[
\theta = \text{momentum thickness}
\]

\[
x = \text{length}
\]

\[
Rn_x = \text{Reynolds number based off longitudinal location (equation 6)}
\]

Once these values were determined, the applets were used to calculate the same values for a virtual flat plate, that is, one with zero thickness (a thickness of 0.001 meters was inputted into the code). The results for both momentum thickness Reynolds number and boundary layer thickness from theory and code could then be plotted versus percent length to compare. The plotted results can be found in Figure 8 and Figure 9 below.

Figure 8: \(Rn_\theta\) comparison between theory and applets
The dashed line in each plot represents the theoretical values for $R_{n\theta}$ and $\delta$ while the blue diamonds represent the data determined from the applets. As can be seen in the plots, there is only minor variation between the theoretical results and the analytical results. The conclusion from this comparison was that the results obtained from the applets could be considered reasonable.
4.1 Hot-Film Anemometers

The experimental portion of this project was done as a means to collect data from models in support of the applets discussed above. The experimentation process consisted of using anemometers to analyze the flow around various models. These anemometers are probes manufactured by Dantec Dynamics. Figure 10 below is a schematic of the sensors used for the project.

![Figure 10: Schematic of Dantec Hot-Film Sensor](image)

The probes are single-sensor flush-mounted film probes meant to be used in either air or water (Dantec Dynamics). An anemometer works by having a voltage supplied through a bridge to a wire within the anemometer, which is kept at a constant temperature (Lee and Basu, 1999). The voltage adjusts rapidly to ensure that a constant temperature is maintained. Turbulent flow transfers heat out of a system much more effectively than laminar flow. Because of this the voltage to the anemometer must increase to compensate for the heat loss. Plotting the voltage vs. time, the transition from laminar to turbulent flow can easily be seen as a jump in voltage and an increase in the frequency of voltage fluctuations. However, further analysis of the voltage can be done to define more exactly when and where flow is laminar, transitional, or turbulent. Initially there were three probes available for data collection, but due to the condition of the probes, human error, and other factors, this number was reduced to one. However, two more probes were purchased and utilized for the first portion of data collection, with one probe being deemed inoperable in the middle of experimentation.
4.2 ThermalPro Software

As discussed above, in 2007 Midshipmen Rebecca Islin conducted tests on a flat plate using the TSI IFA 300 anemometer system. The IFA 300 utilizes a single processor, or cabinet, into which all Dantec probes are connected. The cabinet is used to turn on each probe and supply the voltage necessary to maintain the constant temperature of the probe. The probes and the computer system itself were inherited for use in this project. However, it was with the IFA 300 system that the first and possibly largest obstacle was encountered. The IFA 300 system uses a standard personal computer unit (PCU) to run its testing software, ThermalPro. Despite the fact that the system had been used previously, the software turned out to be incredibly unfriendly for the user and provided a real challenge when beginning the process of data collection. The first several weeks of research were devoted to attempting to learn and master the ThermalPro software. Once mastered, the steps for how to use the program were documented and can be found below in Appendix A.

The ThermalPro software is designed to be able to supply voltage to up to eight probes, collect data from these probes, and then analyze the data based on inputs from the operator. For the purposes of this research, the software was intended to merely serve as an on/off switch for the probes. The actual data collection was done with a different computer and software. Still the issue that arose was how to turn on the probes, that is to begin supplying power, by using the software. The initial attempts to turn on the probes led to having the ability to supply voltage to one of the probes at a time. Even though all probes were connected to the system, if one was turned on and another probe was selected, the first probe would shut down, leaving only the new probe engaged. During this process of attempting to employ all probes, various inputs for the gain of each probe were used as a means to try and clarify any signal ambiguity. The initial trials
with the probes were done in air rather than water, and as the gain was increased, the probes heated to very high temperatures, at times glowing red due to the current through the film. Had the probes been in water, the water would have served as a heat sink to prevent such drastic heating, but due to initial trials in air, two probes were burned out due to too large of a gain value being input.

It was determined that the initial route taken within the software to engage the probes was incorrect. The probes had to be treated as a group, rather than individuals. The program contains a data table in which probes can be input. Here, however, another problem surfaced: it was not possible to simply generate a new file for a probe. The software contains a small database of generic probe configurations, but any attempt to add a new probe was not recognized by the program. After much trial and error and thanks to the assistance of Professor Ralph Volino, the software’s preloaded probes could be modified to represent the actual probes connected to the system. This modification, however, was limited by the fact that the largest configuration contained only three probes. While this was the maximum number of probes used for the purposes of this project, any future attempt to use four or more probes would encounter the same problem of uploading new probes.

After all the issues discussed above were sorted out, a set of instructions for the usage of the IFA300 were written. These steps appear in Appendix A.
5.1 Model Design and Features

After successfully mastering the ThermalPro software and ensuring all the probes could be turned on, the researcher could start the first part of the project’s experimental portion. The focus in the first part of data collection was to develop a more in-depth understanding of the effect of $Rn_\theta$ on the turbulence in the boundary layer. The hypothesis for this effect, as stated above, is that there is a certain $Rn_\theta$ value that, when surpassed, the flow will naturally transition from laminar to turbulent. The first goal, then, for testing was to determine at approximately what value of $Rn_\theta$ the flow naturally transitions.

For this first set of data runs, a thickened panel was mounted with the anemometers and then run at a range of speeds in the 380’ tow tank at the Hydromechanics Laboratory. The thickened panel used was the same one built and used by MIDN Rebecca Islin in 2007 for her study of turbulence stimulation. Figure 11 and Figure 12 below show the dimensions and design of the thickened panel.
Figure 11: Schematic of Flat Plate Design (Islin, 2007)

Figure 12: Picture of Thickened Panel Design (Islin, 2007)
The panel is specifically designed to “ensure attached laminar flow, while the trailing edge was tapered to reduce flow separation downstream” (Islin, 2007). The curve used at the bow and stern of the plate is pictured below (Figure 13).

Figure 13: Bow of Thickened Panel (Islin, 2007)

The probes are mounted from the inside of the model. The port side of the model is able to be removed and the probes can be placed in the appropriate positions. The flat plate is equipped to mount four probes at once. However, in this project only the forward three mount locations were used. The probes were mounted using a simple locking device constructed out of PVC. One side of the clamp was glued to the model and the other was free. When the screw was tightened, the free end clinched down on the glued side, preventing rotation or the translation of the probe. It is critical to ensure the probes are oriented properly with the actual film perpendicular to the flow before the probes are clamped in position. Any rotation will reduce the effectiveness of the probes to detect turbulence.

Because the flat plate model had not been used since 2007, it was not in the optimal condition for running tests in the tow tank. Thus, one of the first tasks to ensure the model was ready was to determine whether or not the probes still fit in the drilled holes and could be made flush with the surface of the model. Ensuring the probes are flush is a key step prior to testing because, if the probes are not flush, the results may be erroneous. As discussed above, the way the probes are mounted allows for transverse movement prior to locking the probe in place.
Placing a solid object such as foam or PVC against the outside allows the probe to be pushed forward until it is flush with the surface.

As well as ensuring the probes were flush with the surface of the model, the model had to be prepped to an acceptable smoothness before testing. Since the main object of focus for this entire project was stimulating turbulence, each model needed to be free of any ridge, bump, hollow, or foreign object that might incidentally trip the flow. The first step, then, in fairing the surface of the model was to fill in any holes on the surface. These holes were either part of the manufacturing of the plate or unused holes drilled for probes. To fill these holes, an epoxy-based mixture was used, which was applied over a hole and the surrounding surfaces. Once the epoxy had cured, the model was wet sanded with several different grits of sanding, ending with a very fine 400 grit paper that achieved the desired smoothness. After sanding the model several times, the researcher deemed it ready for testing.

5.2 Plate Mounting

The flat plate was mounted to the towing carriage used in the 380-foot towing tank found in the Hydromechanics Laboratory here at the United States Naval Academy. The tank is capable of towing a model at speeds exceeding 30 feet per second. The plate was mounted with a single post centered transversely and longitudinally on the model. The mounted rig is pictured below in Figure 14.
The blue block seen at the base of the post in Figure 14 above is a force block oriented to read forces acting transversely along the model. These side force measurements were necessary to ensure that the model had zero angle of attack as it moved down the tank. Any significant positive or negative force indicated that either the model was yawed to starboard or port respectively. There are two reasons for maintaining a zero-angle of attack. The first is safety; a significant angle of attack could cause enough lift force to pull the model off the rig, damaging not only the model and carriage but the operator as well. The second reason is that an angle of attack would impact the flow around the model, which would cause for erroneous results to be recorded that would affect conclusions drawn from the experimentation. Ultimately, the goal was to maintain zero angle of attack for each run with minimal variation.
5.3 Analytical Analysis

To reiterate the material mentioned at the beginning of the paper, the primary focus of this project was to establish if one could determine the ideal thickness and location of turbulence stimulation devices for a given ship model. The hypothesis put forward was that when the $Rn_\theta$ value was above a threshold value and the pressure gradient parameter, $K$, was below a threshold value, that location would be best for placing stimulation. The experimentation was then structured to study first one of these factors, $Rn_\theta$, and then once conclusions were drawn about $Rn_\theta$, further testing would be done that introduced $K$ as a parameter of study. The thickened panel was meant to be studied as a flat plate; therefore, the pressure gradient parameter was considered negligible. Thus, beginning with the flat plate, all testing was focused solely on exploring $Rn_\theta$.

$Rn_\theta$ was meant to indicate the likelihood that the flow would transition from laminar to turbulent flow. As shown in the plot found in Figure 7, the $Rn_\theta$ values can be plotted over the length of a model. The values for $Rn_\theta$ along the length increase as the velocity of the model increases. Thus, the value of $Rn_\theta$ at a given point can be ascertained at any given velocity. The velocities at which data was collected for this project were from 1.0 to 5.0 fps at $\frac{1}{4}$ fps increments and 0.5 fps as well. This was the first step in beginning experimentation on the thickened panel model. The panel was analyzed using the applets available from Virginia Tech. The $Rn_\theta$ values were plotted vs. model length for each of these velocities.

The focus for all the testing and experimentation in this project was on small models run at slow speeds. Based on previous experience with testing ship-models, it was decided that above 5.0 fps the flow would naturally transition to turbulent before any sensing could be done. Figure 15 below is an example of what the $Rn_\theta$ vs. length output looked like for the thickened panel.
Figure 15: $R_{n\theta}$ vs. % Length for the Thickened Panel
From the plot in Figure 15, one can determine the value of $R_n\theta$ at the location of each probe for a given speed. These $R_n\theta$ values were tabulated for further use in analyzing the outcomes of the various tests conducted. The three probes were located at 17 inches aft of the bow, 24 inches aft of the bow, and 31.5 inches aft of the bow. In terms of percent length, these values were 28%, 40%, and 53% aft of the bow respectively. The red lines on the plot above represent where the $R_n\theta$ value for each probe was drawn from the plot. The values for $R_n\theta$ for the flat plate across the entire range of speeds is tabulated in

**Table 1** below.

<table>
<thead>
<tr>
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<th>Probe 1</th>
<th>Probe 2</th>
<th>Probe 3</th>
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</table>

5.4 Experimental Analysis

The next step in the testing process was to run the thickened panel at all the velocities of interest discussed above. The order of velocities at which the model was run was kept constant.
throughout the course of the project. The panel was towed first at 0.5 fps increments from 0.5 to 5.0 fps. Following the completion of these tests, the panel was then towed at 0.5 fps increments from 1.25 to 4.75 fps. The sampling rate for the system was 1000 Hz, and the length of each data run was 30 seconds, giving 30,000 data points for each run. At the slower velocities, multiple speeds were tested in one run so as to optimize testing time in the tank. When the towing carriage returned to its home position, the system was re-zeroed after a 30-second pause. This time was maintained for all testing performed.

After successfully running the panel at all desired velocities, one of the first conclusions was able to be drawn: the probes are sensitive enough to detect and output the transition from laminar to turbulent form. Figure 16 on the next page is a plot of raw output from the same probe taken at three different speeds.

Visually, it can be seen that there is marked difference between the signals produced by the same probe at different velocities. Turbulent flow is represented by a spike in the average voltage as well as an increase in the oscillations from a lower to higher voltage. The three different signals represent the various stages the flow around the model could be classified as: laminar (the orange signal taken at 0.5 fps), early transitional (the pink signal taken at 2.0 fps), and late transitional (the blue signal taken at 5.0 fps). The early transitional signal had more of a laminar characteristic while the late transitional signal was nearly fully turbulent. Although one could visually identify a difference in the signal output, it is not possible to visually approximate just how turbulent or laminar a given signal is. Therefore, the results from each data run were exported to MATLAB and analyzed using a code written specifically for this project.
Figure 16: Raw Probe Voltage Signal
The code was written in MATLAB primarily with the assistance of Professor Michael Schultz. The code took the voltage outputted by the probes and performed two separate time derivatives of the signal (Volino, 2003). In order for these derivatives to display proper results, the signal had to be passed through a series of high and low pass filters. The complete code is included in Appendix B. When a data file is loaded into the code, any part of the signal that satisfies the thresholds set for each of the two derivatives is assigned a value of 1. If a part of the signal does not satisfy the threshold requirements, it is assigned a value of 0. Thus, each signal is converted into a simple square wave. Figure 17 on the next page shows a raw signal clip along with the square wave generated in MATLAB.

The MATLAB code then generates an associated ratio of how often the square wave has a value of 1 compared to the total time analyzed. This ratio can be seen in equation 14 below.

\[
\frac{\text{Time\_Turbulent}}{\text{Total\_Time}}
\]

From this point forward this ratio will be referred to as intermittency. A fully turbulent signal will have an intermittency of 1, while a laminar signal will have an intermittency of 0. Values in between indicate transitional flow that are either closer to returning to laminar or about to become fully turbulent. The signal in Figure 17 has an intermittency value of 0.72. The thresholds for determining the intermittency of a given signal needed to be adjusted for each individual run. Therefore it was not possible to merely run a series of data files in bulk. Time and care had to be taken to ensure that each signal’s corresponding square wave made sense with what could be visually seen in the raw signal.
Figure 17: Raw Signal and Associated Square Wave
Once all the signals for the initial test case of thickened panel with no stimulation had been analyzed, all the values of % intermittency were compiled for all the probes at all speeds. These results for the initial testing on the thickened panel are tabulated below in Table 2.

<table>
<thead>
<tr>
<th>Run Velocity (fps)</th>
<th>Intermittency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Probe 1</td>
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<tr>
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</table>

It was determined that probe 2 was not functioning properly for this condition, thus the results were not included in Table 2. The next step was to achieve a graphical representation of the entire transition process. This was accomplished by plotting intermittency vs. the $Rn_\theta$ values tabulated earlier in Table 1. This plot can be found below in Figure 18.
Figure 18: Intermittency vs. $Rn_\theta$ Thickened Panel No Stimulation
The results seen above in Figure 18 are what would be expected for the probe locations and the speeds at which the panel was tested. Some of the variation may be explained by problems with the probes that will be discussed later in this paper. However, it makes sense that the first probe, the most forward of the three never detected any transition from laminar to turbulent. The shape of the plot for probe 3 was about the ideal form that one would expect. There is a region of transition beginning at a $Rn_\theta$ value of about 400 and then achieving full turbulence around a $Rn_\theta$ value of 580. The goal from this point was to determine what thickness of stimulation caused the same transition to occur at lower value of $Rn_\theta$. It should be noted here that the value of $Rn_\theta$ at which the flow transitioned around the panel was less than the value of 800 which was hypothesized as the threshold value for $Rn_\theta$. Possible reasons for this and further discussion is contained in section 7.1 below.

As mentioned above, the stimulators used for this project were Hama strips. Hama strips are created using electrical tape cut with pinking shears so that the edge facing the bow of a model has a series of wedges that serve as vortex generators. The thickness of the strip is varied by placing several layers of tape together and then cutting the strips to the desired length. The first two thicknesses used were 1 strip and 2 strips, having a thickness of 0.006 and 0.01 inches respectfully. The trips were placed 22” aft of the bow or about 1 inch in front of the second probe. (It had been determined at this point that the first probe was no longer functioning properly.)

The panel was then run with the two different strip thickness again in the same fashion as it was with no stimulation. The intermittency values for the two probes can be found below in Table 3 and Table 4.
Table 3: Intermittency Thickened Plate 1 layer Hama strip

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<td>4.25</td>
<td>0.00</td>
<td>0.92</td>
</tr>
<tr>
<td>4.5</td>
<td>0.00</td>
<td>0.81</td>
</tr>
<tr>
<td>4.75</td>
<td>1.00</td>
<td>0.45</td>
</tr>
<tr>
<td>5</td>
<td>0.02</td>
<td>0.80</td>
</tr>
</tbody>
</table>

Table 4: Intermittency Thickened Plate 2 layer Hama Strip

<table>
<thead>
<tr>
<th>Run Velocity (fps)</th>
<th>Intermittency</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>1</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>1.5</td>
<td>0.00</td>
<td>0.02</td>
</tr>
<tr>
<td>2</td>
<td>1.00</td>
<td>0.06</td>
</tr>
<tr>
<td>2.5</td>
<td>0.54</td>
<td>0.96</td>
</tr>
<tr>
<td>3</td>
<td>0.50</td>
<td>1.00</td>
</tr>
<tr>
<td>3.5</td>
<td>0.84</td>
<td>1.00</td>
</tr>
<tr>
<td>4</td>
<td>0.00</td>
<td>1.00</td>
</tr>
<tr>
<td>4.5</td>
<td>1.00</td>
<td>0.86</td>
</tr>
<tr>
<td>5</td>
<td>0.10</td>
<td>0.93</td>
</tr>
</tbody>
</table>
Once the intermittencies were determined for the 1-layer and 2-layer conditions, these results could again be plotted vs. $Rn_\theta$ in order to determine if the trip had caused transition to occur at a lower $Rn_\theta$ value. The plots for probe 3 can be found on the next page in Figure 19.

It is evident from the plots in Figure 19, that there is no significant change in when the transition from laminar to turbulent flow occurs along the model. The conclusion to be drawn from this is that a 1-layer or 2-layer Hama strip does not provide enough of a trip to the flow to cause it to transition earlier.

Evidently more of a trip was required to trip the flow along the thickened plate. The next step in the process was to determine how Hama strips are normally sized in the USNA Hydromechanics Laboratory. The lab uses a spreadsheet based on results from wind tunnel testing (Barlow, Rae, and Pope, 309-310). The spreadsheet takes data inputs such as velocity and length to approximate the thickness of Hama strips. Table 5 seen below is an example of that spreadsheet.

<table>
<thead>
<tr>
<th>Hama Strip Sizing</th>
<th>Reference - Low Speed Wind Tunnel Testing by Barlow, Rae and Pope, pgs. 309-310, John Wiley and Sons Inc, 1999</th>
</tr>
</thead>
<tbody>
<tr>
<td>V</td>
<td>3.65 fps</td>
</tr>
<tr>
<td>L</td>
<td>5.07 ft</td>
</tr>
<tr>
<td>Viscosity</td>
<td>1.30E-05</td>
</tr>
<tr>
<td>Trip Location</td>
<td>10.0 (%chord)</td>
</tr>
<tr>
<td>Rn</td>
<td>1.42E+06</td>
</tr>
<tr>
<td>Rn/ft</td>
<td>2.81E+05</td>
</tr>
<tr>
<td>Rn at Trip</td>
<td>1.42E+05</td>
</tr>
<tr>
<td>Height of Hama Strip</td>
<td>0.026 inches</td>
</tr>
<tr>
<td>Location of Hama Strip</td>
<td>6.084 inches aft LE</td>
</tr>
</tbody>
</table>
Figure 19: Initial Thickened Panel Stimulation Comparison
The sizing tool estimated that the thickened panel needed a minimum of 0.041 inches of thickness, or about 7-layers of tape. The appropriate sized strip was assembled and placed on the model. The model was then rerun over the same range of speeds. The intermittency for the two probes is tabulated below in Table 6.

<table>
<thead>
<tr>
<th>Run Velocity (fps)</th>
<th>Intermittency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Probe 2</td>
</tr>
<tr>
<td>0.5</td>
<td>0.00</td>
</tr>
<tr>
<td>1</td>
<td>0.00</td>
</tr>
<tr>
<td>1.25</td>
<td>0.00</td>
</tr>
<tr>
<td>1.5</td>
<td>0.00</td>
</tr>
<tr>
<td>1.75</td>
<td>0.00</td>
</tr>
<tr>
<td>2</td>
<td>0.00</td>
</tr>
<tr>
<td>2.25</td>
<td>0.05</td>
</tr>
<tr>
<td>2.5</td>
<td>0.89</td>
</tr>
<tr>
<td>2.75</td>
<td>0.96</td>
</tr>
<tr>
<td>3</td>
<td>1.00</td>
</tr>
<tr>
<td>3.25</td>
<td>1.00</td>
</tr>
<tr>
<td>3.5</td>
<td>1.00</td>
</tr>
<tr>
<td>3.75</td>
<td>1.00</td>
</tr>
<tr>
<td>4</td>
<td>1.00</td>
</tr>
<tr>
<td>4.25</td>
<td>1.00</td>
</tr>
<tr>
<td>4.5</td>
<td>1.00</td>
</tr>
<tr>
<td>4.75</td>
<td>1.00</td>
</tr>
<tr>
<td>5</td>
<td>1.00</td>
</tr>
</tbody>
</table>

The results for the 7-layer Hama strip were then also plotted on the same chart as the results for no stimulation. The plot is featured below in Figure 20.
Figure 20: Intermittency vs. $R_n\theta$ Thickened Panel w/ 7-layer Hama Strip
Here, the results clearly show that the 7-layer Hama strip (the pink line) transitions at a lower $Rn_\theta$ value than the no-stimulation case (blue line). The effective difference in $Rn_\theta$ is approximately 100. Clearly the guidance based on empirical evidence is sound for providing a stimulation thickness that effectively trips the flow.

The next step in the testing process was to see if a thicker Hama strip caused more of a difference for the values of $Rn_\theta$ where the flow transitioned. A 10-layer Hama strip was cut and placed on the model, and the model was retested and reanalyzed. The intermittency results for the 10 layer are listed in Table 7.

<table>
<thead>
<tr>
<th>Run Velocity (fps)</th>
<th>Intermittency</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Probe 2</td>
<td>Probe 3</td>
</tr>
<tr>
<td>0.5</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>1</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>1.25</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>1.5</td>
<td>0.00</td>
<td>0.32</td>
</tr>
<tr>
<td>1.75</td>
<td>0.02</td>
<td>0.79</td>
</tr>
<tr>
<td>2</td>
<td>0.08</td>
<td>0.96</td>
</tr>
<tr>
<td>2.25</td>
<td>0.42</td>
<td>0.99</td>
</tr>
<tr>
<td>2.5</td>
<td>0.99</td>
<td>1.00</td>
</tr>
<tr>
<td>2.75</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>3</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>3.25</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>3.5</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>3.75</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>4</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>4.25</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>4.5</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>4.75</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>5</td>
<td>1.00</td>
<td>1.00</td>
</tr>
</tbody>
</table>

The results for the 10-layer Hama strip were then plotted along with the 7-layer strip. Figure 21 below is the plot comparing 10-layer to 7-layer. The goal was to determine if the larger trip would cause a greater shift in the value of $Rn_\theta$ at which the flow transitioned.
Figure 21: Intermittency vs $Rn_\theta$ Thickened Plate (7 and 10 layer)
Figure 21 demonstrates that having a thicker Hama strip does not cause there to be a more significant difference in what value of $Rn_\theta$ the flow transitions at. It can therefore be concluded, based on the data collected from the thickened panel, that there is a certain optimal thickness that at a minimum needs to be present in order to cause flow to transition from laminar to turbulent at a lower value of $Rn_\theta$. It is not necessary to exceed this desired thickness as the increased thickness has no positive affect on the lower $Rn_\theta$ value. The greater thickness is actually undesirable due to the increase in parasitic drag accompanying the thicker Hama strip.
6.1 Model Design and Mounting

The next stage of the project was to run tests and analyze the results of a “2-D” model. The model is considered 2-D because it only has planar curvature; that is, the flow only changes in the x and y directions. The 2-D model utilized for this project was designed and created based on the Defense Advanced Research Projects Agency (DARPA) Suboff model. The Suboff model is a generic submarine form developed by using two separate parabolic formulae for the bow and stern sections (Stettler, 2009). The 2-D model created for this project took the bow and stern formulae from the Suboff model and only applied it to the x and y plane. That is to say, looking at the design from the waterplane view, straight down the z-axis, the model looks like the shape outlined in Figure 22.

![Figure 22: Suboff Model Design](image-url)
Other than the curvature in the x-y plane, the model is wall sided, having a straight, vertical hull with a depth of 30 inches.

The 2-D model was constructed with large contributions from the Naval Academy Machine and Wood Shop specifically from Mr. Tom Price. The model was created in two halves using a female mold built by bending plywood over a skeleton shaped to create the contour of the model. Woven fiberglass sheets were then epoxied together into the shape of the mold. Once each side was completed, they were bolted together, and a base was added. The top of the gunwales was reinforced with a wood lip, and the model was stiffened by a single longitudinal beam. Figure 23 below is a picture of the completed model attached to the towing rig.

![Figure 23: 2-D Model Attached to Towing Rig](image)

Due to the size of the model and the amount of water displaced as it is towed, the model was secured using two posts in the bow and the stern. This prevented the model from experiencing a large moment around a single point.

The reason for have such a large, bulky hull shape was to achieve a strong pressure gradient. The size of the gradient, indicated by the value of its parameter $K$, is indicative of extreme classes of ships that are often the most difficult to stimulate for realistic model testing.
The extreme pressure gradient developed by the model can be seen visually at higher velocity runs. Figure 24 below is a picture of the model being run at 4.5 fps.

![2-D Model Visual Pressure Gradient](image)

Figure 24: 2-D Model Visual Pressure Gradient

One can see that there is a distinct point at which the water goes from following the contours of the model cleanly to becoming random and extremely chaotic. This point is at the thickest point of the model and is where the pressure gradient transitions from positive to negative.

6.2 Analytical Analysis

It was established from testing the thickened panel model that a thick enough Hama strip placed in the flow around a model would cause the water to behave as though it was moving over the model at a higher velocity. The goal with the 2-D model was to confirm the results of the thickened panel and then to determine if the pressure gradient had suppressed the flow and forced the flow to relaminarize. If this was the case, the next step would be to determine at what location fore to aft the effect of the trip was not influenced by the pressure gradient. The hypothesis made at the beginning of the project was the optimal point to place a trip would be when the pressure gradient parameter $K$ was below a certain value. Figure 25 below represents where that location may be on the applet outputs for the 2-D model.
Figure 25: 2-D Model Applet Output, K (2.5 fps)
The red arrow points to approximately where the pressure gradient, while still positive, was no longer as extreme and therefore would allow for flow transitions without relaminarization. The goal, then, in testing was to see if indeed such an optimal location could be found.

The first step in beginning testing on the 2-D model was the same as that for the thickened panel. The hull form was entered into the programs available from Virginia Tech and analyzed at the same range of velocities used for the thickened panel testing. The results for $Rn_{\theta}$ for each of the probe locations were recorded and are tabulated in below in Table 8.

<table>
<thead>
<tr>
<th>Velocity (fps)</th>
<th>Probe 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>138</td>
</tr>
<tr>
<td>1</td>
<td>195</td>
</tr>
<tr>
<td>1.25</td>
<td>218</td>
</tr>
<tr>
<td>1.5</td>
<td>239</td>
</tr>
<tr>
<td>1.75</td>
<td>258</td>
</tr>
<tr>
<td>2</td>
<td>276</td>
</tr>
<tr>
<td>2.25</td>
<td>293</td>
</tr>
<tr>
<td>2.5</td>
<td>308</td>
</tr>
<tr>
<td>2.75</td>
<td>324</td>
</tr>
<tr>
<td>3</td>
<td>338</td>
</tr>
<tr>
<td>3.25</td>
<td>352</td>
</tr>
<tr>
<td>3.5</td>
<td>365</td>
</tr>
<tr>
<td>3.75</td>
<td>378</td>
</tr>
<tr>
<td>4</td>
<td>390</td>
</tr>
<tr>
<td>4.25</td>
<td>402</td>
</tr>
<tr>
<td>4.5</td>
<td>414</td>
</tr>
<tr>
<td>4.75</td>
<td>425</td>
</tr>
<tr>
<td>5</td>
<td>434</td>
</tr>
</tbody>
</table>

It should be noted that as testing on the 2-D model began, it became apparent that the third probe used for the thickened panel was no longer operating properly and was not considered in any conclusions drawn from the 2-D model. Therefore, only one operational probe was available for use during this phase of testing.
6.3 Experimental Analysis

The 2-D model was tested for five different conditions. The first of these was no stimulation; this data set just as with the thickened panel would serve as the basis for interpretation. The model was also tested with four different stimulation conditions. The first of these conditions was to place a 7-layer Hama strip 1 inch in front of the probe (11 inches aft of the bow or 18.3% of the length). The same sizing spreadsheet used on the thickened panel was employed to approximate the thickness of the Hama strip for the 2-D model. Since the primary focus of this second portion of testing was on $K$ and strip location, 7 layers of tape were the constant thickness for all stimulation placed on the 2-D model. For each data file collected from tests done on the 2-D model, the same MATLAB code written for the thickened panel was utilized to analyze the results. The results are listed below in Table 9.

<table>
<thead>
<tr>
<th>Velocity (fps)</th>
<th>Intermittency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No Trip</td>
</tr>
<tr>
<td>0.5</td>
<td>0.00</td>
</tr>
<tr>
<td>1</td>
<td>0.00</td>
</tr>
<tr>
<td>1.25</td>
<td>0.02</td>
</tr>
<tr>
<td>1.5</td>
<td>0.00</td>
</tr>
<tr>
<td>1.75</td>
<td>0.00</td>
</tr>
<tr>
<td>2</td>
<td>0.00</td>
</tr>
<tr>
<td>2.25</td>
<td>0.00</td>
</tr>
<tr>
<td>2.5</td>
<td>0.02</td>
</tr>
<tr>
<td>2.75</td>
<td>0.00</td>
</tr>
<tr>
<td>3</td>
<td>0.02</td>
</tr>
<tr>
<td>3.25</td>
<td>0.04</td>
</tr>
<tr>
<td>3.5</td>
<td>1.00</td>
</tr>
<tr>
<td>3.75</td>
<td>1.00</td>
</tr>
<tr>
<td>4</td>
<td>1.00</td>
</tr>
<tr>
<td>4.25</td>
<td>1.00</td>
</tr>
<tr>
<td>4.5</td>
<td>1.00</td>
</tr>
<tr>
<td>4.75</td>
<td>1.00</td>
</tr>
<tr>
<td>5</td>
<td>1.00</td>
</tr>
</tbody>
</table>
Once again intermittency was plotted vs. $Rn_\theta$. Figure 26 on the next page is a plot of the results obtained from the no stimulation condition and with the trip 1 inch forward of the probe.

It is evident from the results plotted again that the 7-layer strip is effective in reducing the $Rn_\theta$ value at which the flow transitions for the 2-D model. This confirms the conclusion drawn from the thickened panel. From here the next step was to determine how far forward stimulation could be placed to still achieve turbulent flow.
Figure 26: 2-D Comparison between Stimulation and No Stimulation
The next phase of testing began by placing a 7-layer Hama strip at a distance of 10% of the model length aft of the bow (6 in aft). 10% is considered to be the fall-back position for placing stimulation on ship-models. After the model was tested with stimulation at 6 inches aft of the bow, it was also tested at 4 inches aft and 8 inches aft of the bow. The data collected was all analyzed, and the results for the last three conditions are tabulated below in Table 10.

<table>
<thead>
<tr>
<th>Intermittency</th>
<th>Velocity (fps)</th>
<th>6 in aft</th>
<th>4 in aft</th>
<th>8 aft</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.0261</td>
</tr>
<tr>
<td>1</td>
<td>0.0291</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>1.25</td>
<td>0.1925</td>
<td>0.01</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>1.5</td>
<td>0.7916</td>
<td>0.0496</td>
<td>0.7358</td>
<td></td>
</tr>
<tr>
<td>1.75</td>
<td>0.973</td>
<td>0.8803</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2.25</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>2.5</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2.75</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>3.25</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>3.5</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>3.75</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>4.25</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>4.5</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>4.75</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td></td>
</tr>
</tbody>
</table>

Once all the data was compiled, more plots were made and conclusions were drawn from these plots. The plot for all the 2-D model stimulation conditions is below in Figure 27.
Figure 27: Intermittency vs. $Rn_\theta$ for all 2-D Stimulated Conditions
The striking result that can be seen from the plot in Figure 27 is that there was no significant difference in the effect of the trip based on the longitudinal position of the Hama strip. The significance of this is more aptly put in terms of the pressure gradient parameter $K$.

Table 11 below is a listing of the $K$ values at all the stimulation locations at 2.5 fps.

<table>
<thead>
<tr>
<th>Point aft (in)</th>
<th>K</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>0.000158</td>
</tr>
<tr>
<td>6</td>
<td>9.89E-05</td>
</tr>
<tr>
<td>8</td>
<td>6.42E-05</td>
</tr>
<tr>
<td>11</td>
<td>3.05E-05</td>
</tr>
</tbody>
</table>

*Table 11: $K$ Values for Tripped Conditions*

The values of $K$ at which each Hama strip was placed is greater than the value at which it was hypothesized that stimulation would have to be placed in order to overcome the effect of the pressure gradient on the flow. It also should be noted that again the $Rn_\theta$ values at which the flow transitioned were much lower than the hypothesized value. Indeed, the values for the 2-D were less than those for the thickened panel, which is not what would be expected. Based on the results from the 2-D model, one could conclude that the location of the strip is not a large factor in tripping the flow; however, this conclusion does not align with previous testing results. Further discussion of why this conclusion holds true for this project is found in section 7.1.

Unfortunately, during the testing of the 2-D model the last probe that was available for use on the project stopped functioning, meaning further testing and comparisons were not possible. The probes used posed numerous problems over the course of the project. Three of the original probes that were inherited from previous projects were never able to provide reliable data, and the three other probes that were acquired over the course of the project all failed either due to human error (stripping of wires, e.g.) or due to the testing environment. While the sensors are meant to be used in air or water, it could have been that the condition of the water in the towing tank and the process of taking the probes in and out of the water may have contributed to
the short lifetime of some of the sensors. That, however, in and of itself is a lesson learned from this experiment. Using a hot-film anemometer system is a means to determine whether or not flow is laminar, transitional, or turbulent. However, due to the sensitivity of the probes, the high cost of the probes, and the difficulty in achieving replicable results, another avenue of research and testing may need to be considered in the future.
7. Conclusions and Recommendations for Future Work

The extent and depth of this project must be considered in order to fully comprehend the results and conclusions given. 342 data files were collected over the course of this project, totaling about 250 total runs in the towing tank, or about 23 total miles of model towing. From all these runs and data files, several significant conclusions were drawn and are discussed below:

- Flow transition can be characterized by $Rn_\theta$ and $K$. The majority of work and research done with these parameters up to this point has been focused on testing in a wind tunnel. It was a novel approach to apply these parameters to testing done in a towing tank, and the work done in this project confirms that these values do characterize the flow around a model. All the tests run on the thickened panel and the 2-D panel show that the flow can be accurately described using $Rn_\theta$ and $K$.

- Differentiation between laminar and turbulent flow. As mentioned in Section 2.7, MIDN Islin laid out some of the groundwork for this project with her own research performed in 2007. However, at the onset of this project the value of her data collection methods was unknown. After major analysis of the data collected from this project, it was found that using the hot film probes proved very valuable. The analysis of each signal proved time consuming as well. The code discussed above in Section 5.3 was able to be used for all data files collected; however, these files could not be analyzed in bulk. Each signal had to be analyzed and then visually checked to ensure that the result made sense. It was necessary to scrutinize each output before plotting results and drawing conclusions. However, this level of scrutiny proved that not only can one differentiate whether the flow is laminar or turbulent but one can tell exactly how far between laminar and turbulent the flow is when transitioning. The intermittency of each signal can be
measured to tell whether the flow is early in the transition phase or further along. These results can be extrapolated to determine the earliest velocity at which transition occurs.

- Measuring the effect of a stimulator on the flow. As mentioned above, the purpose of a turbulence stimulator, such as the Hama strips used in this project, is to induce a momentum jump in the flow. This jump is characterized by the flow beginning to transition at a lower $Rn_\theta$ value. The results from the thickened panel and the 2-D model indicate that the momentum jump induced by a 7-layer Hama strip is about 100. The goal is to find the smallest amount of stimulation that will produce the largest momentum jump. The steps and application of the methods used in this project allow for the measurement of the momentum jump for various types and sizes of turbulence stimulators.

- Optimizing location of turbulence stimulator. Based on the results of the effectiveness of a given stimulator, one can use the Applets and the discussions above to see where the trip can be placed in order to cause the flow to transition. Viewing the results of natural transition for a given ship-model and coupling those results with the measure of effectiveness for a given trip, one can determine the farthest location forward along the hull where the trip can be placed to cause the earliest transition.

- Determining untrippable velocities. Based on the results of both the thickened panel and the 2-D model testing, it is evident that there is an optimal size for a turbulence stimulator that will cause the flow to transition at a lower $Rn_\theta$ value. It is also evident that there are certain speeds at which no size stimulator will cause the flow to transition. The presence of the stimulators causes the flow to trip at an $Rn_\theta$ value about 100 times less than the value required for no stimulation. However, there is still a minimum value that must be
achieved before transition occurs. For the 2-D model this minimum value was 250. Thus, one can take any hull form, analyze the shape using the applets discussed above, and, if the $Rn_\theta$ value in addition to the jump of 100 provided by a trip is less than 250, the flow will not transition. The significance of this is that a naval architect can tell if testing a given velocity on a certain model will be productive or not. For instance, the USS Constitution model was tested at speeds often as low as 0.5 fps. The use of the applets would tell researchers the feasibility of tripping the flow at that velocity. The results indicate that while further research and testing is necessary to optimize turbulence stimulation, the testing limitations and constraints for a given model can be more clearly defined.

Future research and work will only further expound on the conclusions discussed above. There are several areas of interest that still need to be concentrated on in order to further the results featured here. As mentioned above in sections 5.4 and 6.3, the values of $Rn_\theta$ for both the thickened panel and 2-D model at which the flow transitioned were much lower than the hypothesized threshold of 800. There are multiple possible reasons why this may be the case for each model. One explanation could be the difference in facilities where testing was occurring. The threshold value of 800 was primarily based on information and data collected from work done in a wind tunnel. The fact that all these tests were done in a towing tank may have contributed to the difference. The turbulence of the water in the tank prior to each test most likely had a large impact on the results. After a test run, the water on the surface settles relatively quickly. However, the amount of sub-surface turbulence remains for a sustained period after a single run. In a wind tunnel, the air is passed through a series of flow management devices in
order to produce an “ideal” medium for each test. Ship-model testers do not have such a luxury. A model tester will generally use the level of turbulence on the surface as the gauge for when to begin the next run. One could wait between runs for the water in a tow tank to completely settle, but this process could take hours. It is not economically feasible to conduct tests in this way; runs must be made when the water is still disturbed. Thus, while the results seem to not follow the initial assumptions made, they may more closely represent what one should expect when conducting ship-model testing.

In similar fashion, one would have expected the values of $Rn_\theta$ at which the 2-D model transitioned to be greater than those for the thickened panel. However, as the results indicated above, the values for the 2-D model were in fact less. A possible explanation for this occurrence would be the size difference between the two models. Because the 2-D model displaced so much more water than the thickened panel, the amount of disturbance caused in the tow tank may be that much greater as well. Since the same interval of 30 seconds was kept between runs for both models, the water may have been more chaotic for each 2-D run and thus more prone to tripping. The sensors on the model are located with 2 feet of the surface, thus another possibility is that the effects on the surface caused by the large model may be detected by the sensors. These occurrences should be explored in depth prior to conducting any furthering testing.

Significant strides were made for future research and work. This project began with the overall goal of exploring a “novel” approach to turbulence stimulation. The novelty of the approach was to use analytical means to determine the ideal size and location of a stimulation device. The ultimate output from this project and future research will be to have a universal analytical tool that can take inputs from a given model and optimize turbulence stimulation for that model. As mentioned above, to achieve this end state, further testing and analysis must be
done on the models used in this project and on actual ship-models.

Ultimately, the biggest step forward is to begin conducting similar testing on an actual ship-model. It had been discussed in the proposal for this project that testing would be done on the model of the *USS Constitution*. The reasoning for this was that the *Constitution’s* hull form is challenging due to its bulk similar to that of the 2-D model. However, at this stage testing on any ship-model will lead to more positive results and more definite conclusions. The way ahead is promising, large strides have been taken in right direction, and the positive results of this project are sure to be followed by more.
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Appendix A – Steps For Using ThermalPro Software

The steps for using the IFA300 ThermalPro software are as follows:

1. System start-up
   a. Ensure the IFA300 unit is turned on, the on/off switch is located in the back left corner of the unit.
   b. Connect probes to the appropriate IFA300 channels using BNC cables.
      i. There are eight possible connection ports, so ensure you begin in numerical order, probe 1 connects to channel 1, etc.
   c. Ensure the attached PCU is turned on and logged into. The automatic login screen that comes up can be utilized by pushing enter at start-up. Once the computer is up and running, the ThermalPro software must be opened.
      i. There are two versions of ThermalPro on the computer; one is an outdated version. However, the outdated version cannot be uninstalled without affecting the newer version. To open the newest version, pull up the start menu, select the Programs tab, and then ThermalPro. The program labeled ThermalPro v. 4.6 is the older version. It should also be noted that the ThermalPro shortcut on the desktop is for the older version and cannot be modified to open the new version.

2. Probe inputs
   a. To begin, one must access the probe table, which can be found under the acquisition tab as indicated in Figure 28 below.
b. Press the blue Get File icon on the right side of the window to bring up a list of probes already inputted into the system. Select the option labeled sfilm3.R0001. This will open a table of three film sensors as seen below in Figure 29.
c. Each preloaded probe must be modified to represent the actual sensor that is being plugged into the system.
   
   i. Double click on each probe to adjust the input options under the Sensor Setup box.

   1. The IFA channel number must first correspond to the terminal that the probe is plugged into in the rear of the system.
   2. The cable resistance should either by 0.33 Ω or 0.3 Ω depending on the length of the cable connected to the probe. A longer cable requires the higher resistance.
3. The probe resistance is read by the system and cannot be changed or modified.

4. The Opr Resistance or operational resistance is the resistance required for the probe to function. This value is provided with each probe, but the actual resistance may need to be adjusted throughout test runs as it fluctuates to accommodate for changes to the sensor through overuse, time, or other external factors.

5. The offset is adjusted to have the probe read 0 volts when stationary with no flow over its surface. Attach the output from the IFA system directly to a voltmeter and then adjust the offset up or down until the voltmeter is reading approximately 0.

6. The gain serves to amplify the signal put out by each probe. The goal is to have a high enough gain to be able to visually read each signal.

ii. Table 12 below contains all the values that were inputted for the probes utilized in this project.

<table>
<thead>
<tr>
<th>Probe 1</th>
<th>Probe 2</th>
<th>Probe 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cable Res. = 0.33 Ω</td>
<td>Cable Res. = 0.3 Ω</td>
<td>Cable Res. = 0.3 Ω</td>
</tr>
<tr>
<td>Opr Res. = 20 Ω</td>
<td>Opr Res. = 15 Ω</td>
<td>Opr Res. = 17 Ω</td>
</tr>
<tr>
<td>Offset = 0.78 V</td>
<td>Offset = 1.1 V</td>
<td>Offset = 1.75 V</td>
</tr>
<tr>
<td>Gain = 10</td>
<td>Gain = 5</td>
<td>Gain = 5</td>
</tr>
</tbody>
</table>
iii. After each probe has all values inputted, selecting the save line button will lock the values in for that probe.

3. Engaging Probes and Saving the Probe Table

a. Select the green Next Screen button in the lower right corner of the screen seen in Figure 29.

i. Probes will engage and the acquisition screen seen below in Figure 30 will pop up.

![Figure 30: ThermalPro Acquisition Screen](image)

ii. From this point forward the probes will remained turned on until the screen is closed and/or the system is shut down. It should be noted that
one must turn off the probes before removing from the water in order to prevent overheating.

b. Select the green Next Screen button to bring up the screen seen below in Figure 31.

c. Select the green Trigger button in the bottom right corner of the screen.
i. Selecting this will cause the computer to “run” the probes for a brief amount of time and then bring up the small window seen below in Figure 32.

Figure 32: ThermalPro Final Save Screen

d. Select Ok and the system will return to the screen pictured in Figure 30.

i. The probes will still be turned on and the data inputted into the probe table will be saved.
Appendix B – MATLAB Code for Analyzing Data

clear all
load file339.txt
data=file339;
t=data(5001:30000,1);
tau1=data(5001:30000,4);
tau2=data(5001:30000,5);
tau3=data(5001:30000,6);
n=length(t);
[B,A] = butter(9,10/500,'high');
tau1_filt=filtfilt(B, A, tau1);
tau2_filt=filtfilt(B, A, tau2);
tau3_filt=filtfilt(B, A, tau3);
tau1floor=ceil(floor(abs(tau1_filt)/0.12)/1000);
tau2floor=ceil(floor(abs(tau2_filt)/0.05)/1000);
tau3floor=ceil(floor(abs(tau3_filt)/0.08)/1000);
figure
plot(t,tau2_filt)
figure
plot(t,tau3_filt)
figure
plot(t,tau2floor)
figure
plot(t,tau3floor)
figure
tau1new=ceil(abs(tau1floor.*tau1_filt));
tau2new=ceil(abs(tau2floor.*tau2_filt));
tau3new=ceil(abs(tau3floor.*tau3_filt));
tau1new_prime=gradient(tau1new,t);
tau2new_prime=gradient(tau2new,t);
tau3new_prime=gradient(tau3new,t);
index1=find(tau1new_prime~=0);
index2=find(tau2new_prime~=0);
index3=find(tau3new_prime~=0);
dindex1=diff(index1);
dindex2=diff(index2);
dindex3=diff(index3);
lamindex1=find(dindex1>250);
lamindex2=find(dindex2>250);
lamindex3=find(dindex3>250);
lamindex1=lamindex1+1;
lamindex2=lamindex2+1;
lamindex3=lamindex3+1;
if isempty(index1)==1
\texttt{int1(1:n)=0;}
\texttt{else}
\texttt{\hspace{1em}int1(1:index1(1)-1)=0;}
\texttt{end}

\texttt{if isempty(index2)==1}
\texttt{\hspace{1em}int2(1:n)=0;}
\texttt{else}
\texttt{\hspace{2em}int2(1:index2(1)-1)=0;}
\texttt{end}

\texttt{if isempty(index3)==1}
\texttt{\hspace{1em}int3(1:n)=0;}
\texttt{else}
\texttt{\hspace{2em}int3(1:index3(1)-1)=0;}
\texttt{end}

\texttt{if isempty(index1)==1}
\texttt{\hspace{1em}int1(1:n)=0;}
\texttt{elseif isempty(lamindex1)==1}
\texttt{\hspace{2em}int1(1:n)=1;}
\texttt{else}
\texttt{\hspace{3em}int1(index1(1):index1(lamindex1(1)-1))=1;}
\texttt{end}

\texttt{if isempty(index2)==1}
\texttt{\hspace{1em}int2(1:n)=0;}
\texttt{elseif isempty(lamindex2)==1}
\texttt{\hspace{2em}int2(1:n)=1;}
\texttt{else}
\texttt{\hspace{3em}int2(index2(1):index2(lamindex2(1)-1))=1;}
\texttt{end}

\texttt{if isempty(index3)==1}
\texttt{\hspace{1em}int3(1:n)=0;}
\texttt{elseif isempty(lamindex3)==1}
\texttt{\hspace{2em}int3(1:n)=1;}
\texttt{else}
\texttt{\hspace{3em}int3(index3(1):index3(lamindex3(1)-1))=1;}
\texttt{end}

\texttt{if isempty(index1)==1}
\texttt{\hspace{1em}int1(1:n)=0;}
\texttt{elseif isempty(lamindex1)==1}
\texttt{\hspace{2em}int1(1:n)=1;}
\texttt{else}
\texttt{\hspace{3em}int1(index1(1):index1(lamindex1(1)-1))=1;}
\texttt{end}
for i=1:length(lamindex1)-1
    int1(index1(lamindex1(i)-1):index1(lamindex1(i))-1)=0;
    int1(index1(lamindex1(i)):index1(lamindex1(i+1)-1))=1;
end
end

if isempty(index2)==1
    int2(1:n)=0;
elseif isempty(lamindex2)==1
    int2(1:n)=1;
else
    for i=1:length(lamindex2)-1
        int2(index2(lamindex2(i)-1):index2(lamindex2(i))-1)=0;
        int2(index2(lamindex2(i)):index2(lamindex2(i+1)-1))=1;
    end
end

if isempty(index3)==1
    int3(1:n)=0;
elseif isempty(lamindex3)==1
    int3(1:n)=1;
else
    for i=1:length(lamindex3)-1
        int3(index3(lamindex3(i)-1):index3(lamindex3(i))-1)=0;
        int3(index3(lamindex3(i)):index3(lamindex3(i+1)-1))=1;
    end
end

if isempty(index1)==1
    int1(1:n)=0;
elseif isempty(lamindex1)==1
    int1(1:n)=1;
else
    int1(index1(lamindex1(length(lamindex1))):index1(length(index1)))=1;
    int1(index1(length(index1))+1:n)=0;
end

if isempty(index2)==1
    int2(1:n)=0;
elseif isempty(lamindex2)==1
    int2(1:n)=1;
else
    int2(index2(lamindex2(length(lamindex2))):index2(length(index2)))=1;
    int2(index2(length(index2))+1:n)=0;
end
if isempty(index3)==1
    int3(1:n)=0;
elseif isempty(lamindex3)==1
    int3(1:n)=1;
else
    int3(index3(lamindex3(length(lamindex3))):index3(length(index3)))=1;
    int3(index3(length(index3))+1:n)=0;
end

plot(t,tau1)
hold on
plot(t,int1,'r')
figure
plot(t,tau2)
hold on
plot(t,int2,'r')
figure
plot(t,tau3)
hold on
plot(t,int3,'r')

interfrac1=length(find(int1==1))/n
interfrac2=length(find(int2==1))/n
interfrac3=length(find(int3==1))/n