

FUZZY LOGIC BASED UAV ALLOCATION AND COORDINATION

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Abstract A fuzzy logic resource allocation algorithm that enables a collection of unmanned aerial vehicles (UAVs) to automatically cooperate will be discussed. The goal of the UAVs' coordinated effort is to measure the atmospheric index of refraction. Once in flight no human intervention is required. A fuzzy logic based planning algorithm determines the optimal trajectory and points each UAV will sample, while taking into account the UAVs' risk, risk tolerance, reliability, and mission priority for sampling in certain regions. It also considers fuel limitations, mission cost, and related uncertainties. The real-time fuzzy control algorithm running on each UAV renders the UAVs autonomous allowing them to change course immediately without consulting with any commander, requests other UAVs to help, and change the points that will be sampled when observing interesting phenomena. Simulations show the ability of the control algorithm to allow UAVs to effectively cooperate to increase the UAV team's likelihood of success.

1 INTRODUCTION

Knowledge of meteorological properties is fundamental to many decision processes. Due to personnel limitations and risks, it is useful if related measurement processes can be conducted in a fully automated fashion. Recently developed fuzzy logic based algorithms that allow a collection of unmanned aerial vehicles (UAVs) and an interferometer platform (IP) (Smith 2005) to automatically collaborate will be discussed. The UAVs measure the index of refraction in real-time to help determine the position of an electromagnetic source (EMS). The IP is actually an airplane with an interferometer onboard that measures emissions from the electromagnetic source whose position is to be estimated. Each UAV has onboard its own fuzzy logic based real-time control algorithm. The control algorithm renders each UAV fully autonomous; no human intervention is necessary. The control algorithm aboard each UAV will allow it to determine its own course, change course to avoid danger, sample phenomena of interest that were not preplanned, and cooperate with other UAVs.

Section 2 provides an overview of the meteorological sampling problem and a high level description of the planning and control algorithms that render the UAV team fully autonomous. Section 3 discusses the electromagnetic measurement space, UAV risk, and the planning algorithm. Section 3 also discusses the UAV path construction algorithm that determines the minimum number of UAVs required to complete the task, a fuzzy logic based approach for assigning paths to UAVs and which UAVs should be assigned to the overall mission. Section 4 describes the control algorithm that renders the UAVs autonomous. Section 4 also describes the priority for helping (PH) algorithm, a part of the control algorithm based on fuzzy logic that determines which UAV should help another UAV requesting help. The three subclasses of help requests are also discussed in this section. Section 5 discusses experimental results including UAV path determination, UAV path assignment, determination of which UAVs should fly the mission and the result of a request for help during the mission. Finally, section 6 provides a summary.

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2 METEOROLOGICAL SAMPLING AND COOPERATIVE AUTONOMOUS PLATFORMS

For many applications it is useful to be able to make meteorological measurements in real-time. Examples include determining the index of refraction of the atmosphere to facilitate geolocation (Smith 2005); determination of the presence and extent of such phenomena as radio holes and ducts, which may interfere with communications; tracking atmospheric contaminants (Spears 2005); and sand suspended in the atmosphere that can interfere with sensors.

The fuzzy logic based planning and control algorithms that have been developed allow a collection of UAVs making up the UAV team to engage in cooperative sampling of the atmosphere in real-time without human intervention. Each UAV will have its own control algorithm allowing it to determine new optimal trajectories in real-time subject to changing conditions. Also, the control algorithm on the UAVs will allow them to cooperate to increase the probability of mission success. There will be two different types of cooperation allowed by the control algorithm and three classes of help requests which are discussed in section 4.

3 PLANNING AND RISK

The measurement space consists of the electromagnetic propagation environment where UAVs and the IP make their measurements. This environment includes sample points and the desirable neighborhoods that surround them. The sample points or the desirable neighborhoods are where the UAVs will make measurements. The method of determining the sample points and desirable neighborhoods is described below.

The measurement space also includes taboo points and the undesirable neighborhoods that surround them. The taboo points are points of turbulence and other phenomena that could threaten the UAVs. The undesirable neighborhoods surrounding them also represent various degrees of risk. The method of specifying taboo points and quantifying the degree of risk associated with their undesirable neighborhoods employs fuzzy logic and is discussed in this section.

The planning algorithm allows the determination of the minimum number of UAVs needed for the

mission subject to fuel constraints, risk, UAV cost, and importance of various points for sampling. Risk refers to turbulent regions or regions undesirable for other reasons, e.g., the presence of enemy observers or physical obstructions. The planning algorithm automatically establishes the order in which to send the UAVs taking into account the UAV's value; onboard sensor payload; onboard resources such as fuel, computer CPU and memory; etc. The priority of sample points and their desirable neighborhoods are taken into account. The planning algorithm also calculates the optimal path around undesirable regions routing the UAVs to or at least near the points to be sampled.

In the planning phase, the location of the EMS is unknown. Some positions are more likely than others for the EMS's location. When establishing likely positions for the EMS, human experts are consulted. The experts provide subjective probabilities of the EMS being located at a number of positions. These likely EMS locations are referred to as *hypothesis positions*. Ray-theoretic electromagnetic propagation (Blake 1986) is conducted from each hypothesis position to each interferometer element on the IP. The points on the sampling grid nearest the points of each ray's passage are the sample points. The priority of a sample point is related to the subjective probability of the hypothesis position from which the associated ray emerges. Sample points arising from the highest probability hypothesis positions have priority one; sample points associated with lower probability hypothesis positions, priority two; etc.

Each sample point is surrounded by what are referred to as *desirable neighborhoods*. Depending on local weather, topography, etc., the desirable neighborhoods are generally concentric closed balls with a degree of desirability assigned to each ball. The degree of desirability characterizes the anticipated variation in the index of refraction.

A point may be labeled taboo for a variety of reasons. A taboo point and the undesirable neighborhoods containing the point generally represent a threat to the UAV. The threat may take the form of high winds, turbulence, icing conditions, mountains, etc. The undesirable neighborhoods around the taboo point relate to how spatially extensive the threat is.

When determining the optimal path for the UAVs to follow both the planning algorithm and the control algorithm running on each UAV take into account taboo points and the undesirable neighborhood around each taboo point. The path planning algorithm and control algorithm will not

allow a UAV to pass through a taboo point. Both the concepts of risk and risk tolerance are based on human expertise and employ rules each of which carry a degree of uncertainty. This uncertainty is born of linguistic imprecision (Tsoukalas 1997), the inability of human experts to specify a crisp assignment for risk.

Risk is represented as a fuzzy decision tree (Blackman 1999; Smith 2002a, 2002b, 2003, 2004a, 2004b). The risk subtree defined below is a subtree of the larger risk tree that was actually used. The risk tree is used to define taboo points and the undesirable neighborhoods surrounding the taboo points.

The root concepts on the risk tree use the membership function defined in (1-3),

$$\mu_{\alpha}(\bar{q}_{taboo}, \bar{x}) = \begin{cases} 1, & \text{if } r = 0 \\ 3/4, & \text{if } 0 < r \leq 1 \cdot \Delta l \\ 1/2, & \text{if } 1 \cdot \Delta l < r \leq \sqrt{2} \cdot \Delta l \\ 1/4, & \text{if } \sqrt{2} \cdot \Delta l < r \leq \sqrt{3} \cdot \Delta l \\ 0, & \text{if } r > \sqrt{3} \cdot \Delta l \end{cases} \quad (1)$$

$$r = \|\bar{x} - \bar{q}_{taboo}\|, \quad (2)$$

$$\bar{q}_{taboo} = \text{position of taboo point.} \quad (3)$$

where the ‘‘taboo point,’’ \bar{q}_{taboo} is the point at which the risk phenomenon has been observed. The root concepts used on the risk subtree are given in (4), and the subscript α is an element of the root concept set, RC , i.e.,

$$\alpha \in RC = \{Mountains, High Tension Wires, Buildings, Trees, Smoke Plumes, Suspended Sand, Birds/Insects, Other UAVs, Air Pollution, Civilian, Own Military, Allied Military, Neutral Military, Cold, Heat, Icing, Rain, Fog, Sleet, Snow, Hail, Air Pocket, Wind, Wind Shear, Hostile Action/Observation\} \quad (4)$$

The norm in equation (2) is typically taken as an Euclidean distance. The values taken by the quantity Δl will be discussed in a future publication.

The fuzzy membership function for the composite concept ‘‘risk’’ is defined as

$$\mu_{risk}(\bar{q}_{taboo}, \bar{x}) = \max_{\alpha \in RC} \mu_{\alpha}(\bar{q}_{taboo}, \bar{x}). \quad (5)$$

The best path algorithm is actually an optimization algorithm that attempts to minimize a

cost function to determine the optimal trajectory for each UAV to follow, given a priori knowledge. The cost function for the optimization algorithm takes into account various factors associated with the UAV’s properties, mission and measurement space. Two significant quantities that contribute to the cost are the effective distance between the initial and final proposed positions of the UAV and the risk associated with travel.

For purposes of determining the optimal path, the UAV is assumed to follow a rectilinear path consisting of connected lines segments, where the beginning and ending points of each line segment reside on the UAV’s sampling lattice. Let A and B be two grid points on the UAV’s sampling grid with corresponding position vectors, \bar{r}_A and \bar{r}_B , respectively. Denote the Euclidean distance between A and B as $d(\bar{r}_A, \bar{r}_B)$. Let $v(\bar{r}_A, \bar{r}_B)$ be the speed at which the UAV travels in going from \bar{r}_A to \bar{r}_B . If both \bar{r}_A and \bar{r}_B are sample points then the UAV travels at sampling velocity, otherwise it travels at non-sampling velocity. The path cost is given by

$$path_cost(\bar{r}_A, \bar{r}_B) = \frac{d(\bar{r}_A, \bar{r}_B) + \beta \cdot \sum_{i=1}^{n_{taboo}} \mu_{risk}(\bar{t}_i, \bar{r}_B)}{v(\bar{r}_A, \bar{r}_B)} \quad (6)$$

where n_{taboo} is the number of taboo points, i.e., columns in the taboo point matrix

$$Taboo \equiv [\bar{t}_1, \bar{t}_2, \dots, \bar{t}_{n_{taboo}}] \quad (7)$$

and $\bar{t}_i, i = 1, 2, \dots, n_{taboo}$ are the taboo points determined to exist in the measurement space when $path_cost(\bar{r}_A, \bar{r}_B)$ is calculated. The quantity, β , is an expert assigned parameter. Note that $path_cost(\bar{r}_A, \bar{r}_B)$ is an effective time. When risk is not present, i.e., $\beta \cdot \sum_{i=1}^{n_{taboo}} \mu_{risk}(\bar{t}_i, \bar{r}_B)$ is zero, then

$path_cost(\bar{r}_A, \bar{r}_B)$ is the actual travel time. When risk is present then the travel time is increased. The time increase will be significant if the risk is high.

If the candidate path for the mission consists of the following points on the UAV lattice given by the path matrix in (8),

$$Path_i = [\bar{r}_1, \bar{r}_2, \dots, \bar{r}_n], \quad (8)$$

then the total path cost is defined to be

$$total_cost(Path_i) \equiv \sum_{j=1}^{n-1} path_cost(\bar{r}_j, \bar{r}_{j+1}). \quad (9)$$

Determining the optimal path for the i^{th} UAV consists of minimizing the total path cost given by (9) such that there is enough fuel left to complete the path.

The planning algorithm determines the path each UAV will pursue, which points will be sampled, the minimum number of UAVs required for sampling the points and makes assignments of UAVs for measurements at particular points. UAVs are assigned as a function of their abilities to sample high priority points first. The planning algorithm determines flight paths by assigning as many high priority points to a path as possible taking into account relative distances including sampling and non-sampling velocity, risk from taboo points, and UAV fuel limitations. Once flight paths are determined, the planning algorithm assigns the best UAV to each path using the fuzzy logic decision rule for path assignment described in this section.

The planning algorithm must assign UAVs to the flight paths determined by the optimization procedure described below in this section. This is referred to as the UAV path assignment problem (UPAP). The planning algorithm makes this assignment using the following fuzzy logic based procedure. To describe the decision rule it is necessary to develop some preliminary concepts and notation.

Each UAV will fly from lattice point to lattice point, i.e., grid point to grid point, let one such route be given by the matrix of points,

$$Path = [\bar{P}_1, \bar{P}_2, \dots, \bar{P}_{n_{path}}, \bar{P}_1] \quad (10)$$

where the ordering of points gives the direction of the route, i.e., starting at \bar{P}_1 and ending at \bar{P}_1 . Let the taboo points be those given in (7). Let the degree of undesirability of the neighborhood associated with taboo points, $\bar{t}_i, i = 1, 2, \dots, n_{taboo}$ be denoted $\mu_{risk}(\bar{t}_i, \bar{P}_j)$ for the route points $\bar{P}_j, j = 1, 2, \dots, n_{path}$. The definition of the mission risk is

$$mission_risk(Path) \equiv \sum_{i=1}^{n_{taboo}} \sum_{j=1}^{n_{path}} \mu_{risk}(\bar{t}_i, \bar{P}_j) \quad (11)$$

Within the path specified by (10), let there be the following sample points to be measured, $\bar{S}_j, j = 1, 2, \dots, n_{sp}$. Let the function $prio$ assign priorities to the sample points, i.e., $prio(\bar{S}_j)$ is the priority of the j^{th} sample point. The values that $prio(\bar{S}_j)$ can take are positive integers with one representing the highest priority, two the next highest priority, etc. The mission priority for $Path$ is defined to be

$$mission_prio(Path) \equiv \sum_{i=1}^{n_{sp}} \frac{1}{prio(\bar{S}_i)}. \quad (12)$$

Furthermore, let the $T(UAV(i), Path)$ be the amount of time it will take UAV(i) to fly and make measurements along $Path$.

The fuzzy degree of reliability experts assign to the sensors of UAV(i) is denoted as $\mu_{sr}(UAV(i))$. This is a real number between zero and one with one implying the sensors are very reliable and zero that they are totally unreliable. Likewise, $\mu_{nsr}(UAV(i))$ is the fuzzy degree of reliability of other non-sensor systems onboard the UAV(i). This fuzzy concept relates to any non-sensor system, e.g., propulsion, computers, hard disk, deicing systems, etc. The value of UAV(i) in units of \$1000.00 is denoted as $V(UAV(i))$. The amount of fuel that UAV(i) has at time t is denoted $fuel(UAV(i), t)$. All the UAVs participating in a mission are assumed to leave base at time, $t = t_o$.

Let UAV(i)'s fuzzy grade of membership in the fuzzy concept "risk tolerance" be denoted as $\mu_{risk-tol}(UAV(i))$. The quantity, $\mu_{risk-tol}(UAV(i))$, is a number between zero and one and will be simply referred to as UAV(i)'s risk-tolerance. If the risk tolerance is near zero then the UAV should not be sent on very risky missions. If the UAV's risk tolerance is near one then it can be sent on very risky missions. It seems natural to compare risk-tolerance to value. So the comparison can be carried out on the same footing, a fuzzy concept of value should be defined.

The fuzzy grade of membership in the fuzzy concept "Value" of each UAV that can be assigned to the mission is defined as

$$\mu_V(UAV(i)) \equiv \frac{Value(UAV(i))}{\max_j \{Value(UAV(j))\}}. \quad (13)$$

The “max” operation in (13) is taken over the set of all possible UAVs that can be assigned to the mission.

The advantage of the concept of “risk-tolerance” is that it gives the user an extra concept to exploit. If the UAV is not of great relative value, but it still might be needed for a crucial mission after the current one, it might be useful to give it a low risk tolerance so that it is not lost on the current mission. This may allow it to be used on the following mission.

The final concept and related fuzzy membership function that must be defined is “slow”. A UAV is said to be slow if it takes a long time to travel a particular path. The fuzzy membership function for the concept “slow” is defined as follows:

$$\mu_{slow}(UAV(i), Path) \equiv \frac{T(UAV(i), Path)}{\max_j \{T(UAV(j), Path)\}}. \quad (14)$$

A “slow” UAV experiences a higher relative mission risk since it is in the field longer and may be exposed to risk longer.

To construct the fuzzy membership function for the fuzzy concept “assign UAV to Path” (AUP) make the following definitions:

$$f_1(UAV(i), Path) \equiv \chi(fuel(UAV(i), t_o) + \varepsilon_{fuel} - T(UAV(i), Path)) \quad (15)$$

$$f_2(UAV(i), Path) \equiv \frac{mission_prio}{denom(UAV(i), Path)} \min[\mu_{sr}(UAV(i)), \mu_{nsr}(UAV(i))] \quad (16)$$

$$denom(UAV(i), Path) \equiv 1 + \min[1 - \mu_{risk-tol}(UAV(i)), \mu_V(UAV(i))] \mu_{slow}(UAV(i), Path) \cdot mission_risk(Path) \quad (17)$$

$$num(UAV(i), Path) \equiv f_1(UAV(i), Path) f_2(UAV(i), Path) \quad (18)$$

The Heaviside step function denoted as χ in (15) takes the value one when its argument is greater than or equal to zero and is zero otherwise. The quantity ε_{fuel} is added to the fuel term to make sure the UAV selected has more than enough fuel. Given the definition of $num(UAV(i), Path)$ the fuzzy membership function that gives the grade of membership of UAV(i) in the fuzzy concept “assign UAV to Path” is defined as

$$\mu_{AUP}(UAV(i), Path) \equiv \frac{num(UAV(i), Path)}{\max_j num(UAV(j), Path)}, \quad (19)$$

where the “max” operation in the denominator of (19) is taken over the set of all UAVs that can be assigned to the path.

4 CONTROL ALGORITHM

Each UAV has a real-time algorithm onboard it that allows recalculation of paths during flight due to changes in environmental conditions or mission priorities. These changes typically become apparent after the planning algorithm has run during the pre-flight stage. As in the case of the planning algorithm the control algorithm uses an A-star algorithm (Russel 2002) to do the best path calculation, employs fuzzy logic and solves a constrained optimization problem. Although this can require a number of minutes of computation on a two to three gigahertz computer, this is considered adequate given the required UAV flight time between points.

The control algorithms’ recalculation of flight paths can be triggered by a number of events such as weather broadcasts that indicate new taboo regions or changes of priority of sample points. For those changes that do not require UAVs supporting each other, the control algorithm does not differ from the planning algorithm. The control algorithm is faster by virtue that it only need process those parts of the measurement space where there have been changes relative to sample or taboo points.

A UAV may requests help if it discovers a potential elevated system like a radio hole, malfunctions or suspected malfunctions. All of these conditions can result in help messages being transmitted between the UAVs. These help

messages can result in interactions between the UAVs based on transmission of the results of priority calculations for rendering support to the requesting UAVs.

Currently in the control stage, when a UAV discovers an interesting physical phenomenon, is malfunctioning, or suspects due to internal readings that it is malfunctioning, it sends out a request for help. Each UAV receiving this message calculates its priorities for providing assistance to the UAV in need. This priority calculation gives rise to a number between zero and one, inclusive, which is subsequently transmitted to the original UAV desiring support. The requesting UAV sends out an omni-directional message with the ID of the UAV with highest priority for contributing support. The high priority UAV then flies into the necessary neighborhood of the requesting UAV to provide help.

There are three classes of help request. The first occurs when a UAV, the requester, determines it may have discovered an interesting physical phenomenon. This phenomenon may be an elevated duct, radio hole, rain system or some other type of system with physical extent. The requester desires to determine if the phenomenon has significant extent. It will request that a helping UAV or UAVs sample likely distant points within this phenomenon.

The second class of help request relates to a UAV that according to internal diagnostics may be experiencing a sensor malfunction. This UAV will request that another UAV or UAVs measure some of the points that the requesting UAV measured. This will help determine if the UAV is actually malfunctioning. If the requesting UAV is determined to be malfunctioning, then it will fly back to base, if it is capable. The determination of whether it is actually malfunctioning requires some consideration. Since the second UAV will probably be measuring a distant point at a time different than the original requesting UAV made its measurements, potential variation in the index of refraction over time must be taken into account.

When a UAV sends out an omni-directional request for help, those UAVs receiving the message will calculate their fuzzy priority for helping, denoted as "PH." The UAV that will ultimately help the requester is the one with the highest fuzzy priority for helping. The fuzzy priority for helping takes into account a variety of properties of the potential helper. The set of UAVs that receive the request for help from UAV(i) at time t is denoted as $help(i,t)$. If UAV(i) request help at time t and UAV(j) receives the message then UAV(j) will take

into account the amount of time, denoted, $help_time(UAV(j))$, it will take it to fly from the point where it received the request to the point where it would provide support. It also takes into account the amount of fuel UAV(j) has left at the time of the request, denoted $fuel(UAV(j),t)$; UAV(j)'s fuzzy concept of price denoted as "price", and UAV(j)'s fuzzy concept of "mission priority" at time, t . Let the set of relevant UAV properties be denoted as UAV_prop and be defined as

$$UAV_prop = \{help_time, fuel, mission_prio, price\} \quad (20)$$

The fuzzy priority for helping denoted as μ_{PH} takes the form

$$\mu_{PH}(UAV(i), UAV(j)) = \sum_{\alpha \in UAV_prop} w_{\alpha} \cdot \mu_{\alpha}(UAV(j)) \quad (21)$$

The quantities w_{α} and μ_{α} for $\alpha \in UAV_prop$ are expert defined weights and fuzzy membership functions, respectively. The fuzzy membership functions are defined in (22-25) and given below,

$$\mu_{help_time}(UAV(i), UAV(j)) = \left[\frac{help_time(UAV(j))}{\max_{k \in help(i,t)} \{help_time(UAV(k))\}} + 1 \right]^{-1} \quad (22)$$

$$\mu_{fuel}(UAV(i), UAV(j)) = \frac{fuel(UAV(j))}{\max_{k \in help(i,t)} \{fuel(UAV(k))\}} \quad (23)$$

$$\mu_{mission_prio}(UAV(i), UAV(j)) = \left[\frac{mission_prio(UAV(j))}{\max_{k \in help(i,t)} \{mission_prio(UAV(k))\}} + 1 \right]^{-1} \quad (24)$$

$$\mu_{price}(UAV(i),UAV(j))= \left[\frac{Value(UAV(j))}{\max_{k \in help(i,t)} \{Value(UAV(k))\}} + 1 \right]^{-1} \quad (25)$$

It is assumed that all evaluations are processed at time, t , so time dependence is suppressed in (21-25) for notational convenience. A more sophisticated version of the control logic that takes path risk, changes in risk, UAV reliability, UAV risk-tolerance and missed sample points into account will be the subject of a future publication.

5 COMPUTATIONAL EXPERIMENTS

The planning and control algorithms described in the previous sections have been the subject of a large number of experiments. This section provides a description of a small subset of these experiments. They serve to illustrate how the algorithms were tested. Due to space limitations only experiments involving up to three UAVs are discussed.

UAV experiments using only one UAV demonstrate how the planning and control algorithm will determine the route the UAV flies so that it is successful in making measurements at sample points in space, while the UAV avoids taboo points, that is points in space that could damage or destroy the UAV. Experiments using two UAVs illustrate how the control algorithm allows the UAVs to automatically support each other to increase the probability their joint mission is successful.

Figures 1-4 use the same labeling conventions. Sample points are labeled by concentric circular regions colored in different shades of gray. The lighter the shade of gray used to color a point, the lower the point's grade of membership in the fuzzy concept "desirable neighborhood." The legend provides numerical values for the fuzzy grade of membership in the fuzzy concept "desirable neighborhoods". If the fuzzy degree of desirability is high then the index of refraction is considered to be close to the index of refraction of the sample point at the center of the desirable neighborhood. This allows the UAV to make significant measurements while avoiding undesirable neighborhoods.

Each sample point is labeled with an ordered pair. The first member of the ordered pair provides the index of the sample point. The second member

of the ordered pair provides the point's priority. For example, if there are n_{sp} sample points and the q^{th} sample point is of priority p , then that point will be labeled with the ordered pair (q,p) .

Points surrounded by star-shaped neighborhoods varying from dark grey to white in color are taboo points. As with the sample points, neighborhoods with darker shades of gray have a higher grade of membership in the fuzzy concept "undesirable neighborhood." The legend provides numerical values for the fuzzy grade of membership in the fuzzy concept "undesirable neighborhood." UAVs with high risk tolerance may fly through darker grey regions than those with low risk tolerance. When comparing planning and associated control pictures, if a point ceases to be taboo, the neighborhood where it resides is marked by a very dim gray star as well as being labeled by a dialog box as being an "old taboo point." New taboo points and their associated undesirable neighborhoods are labeled with dialog boxes indicating that they are "new."

UAVs start their mission at the UAV base which is labeled with a diamond-shaped marker. They fly in the direction of the arrows labeling the various curves in Figures 1-4.

Figure 1 provides the sample points, taboo points and sample path for one UAV as determined by the planning algorithm. It is important to notice that the UAV's path passes directly through each sample point, i.e., through the center of the concentric circular regions representing the fuzzy degree of desirability of neighborhoods. Fortunately, the taboo points and their neighborhoods are so positioned that they do not interfere with the UAV's measurement process or its return to base.

Figure 2 depicts the actual path the UAV flies as determined by the UAV's real-time control algorithm. The path determined by the control algorithm differs from the one created by the planning algorithm due to real-time changes in taboo points. After leaving the UAV base new weather data was acquired informing the UAVs that the exact position of the third sample point, i.e., the one labeled (3,1) actually resides within an undesirable neighborhood. Due to the high priority of the sample point and the UAV's risk-tolerance, the UAV flies into the taboo points' undesirable neighborhood as indicated in Figure 2.

In both the planning and control algorithms the UAV measures sample points of two different priorities, with the direction of the flight path selected so that the higher priority points are measured first. By measuring high priority points

first, the likelihood of an important measurement not being made is diminished, if the UAV can not complete its mission due to a malfunction, change in weather, etc.

Also, due to movement of old taboo points or the emergence of new taboo points which are marked "New," the path determined for the UAV using the control algorithm is significantly different than the one created by the planning algorithm. The path change represents the control algorithm's ability to reduce UAV risk.

Figure 3 depicts the sampling path determined by the planning algorithm for an experiment involving two UAVs. The first, UAV(1) follows the dashed curve; the second, UAV(2), the solid curve. The UAVs were assigned to the different paths by the fuzzy path assignment decision rule described in section 3. UAV(1) is assigned to sample all the highest priority points, i.e., the priority one points. UAV(2) samples the lower priority points, i.e.; those with priority two. Due to the greedy nature of the point-path assignment algorithm, the highest priority points are assigned for sampling first.

Figure 4 depicts the actual flight path the UAVs take during real-time. Initially, UAV(1) is successful in measuring sample points one and two as assigned it by the planning algorithm. Just beyond sample point two, UAV(1) experiences a malfunction. UAV(1)'s real-time control algorithm

subsequently sends out a help request informing the only other UAV in the field, UAV(2) of the malfunction. UAV(2)'s control algorithm determines a new path for UAV(2) to fly so that the priority one points, labeled (3,1) and (4,1), that UAV(1) was not able to sample are subsequently measured. After UAV(2) measures sample point five, its new flight path allows it to measure sample points three and four. UAV(2)'s control algorithm determined it was very important that these priority one points be measured. Unfortunately, due to the extra fuel expended in reassigning sample points three and four to UAV(2), UAV(2) did not have enough fuel to measure sample points seven and eight which were of priority two. UAV(2)'s real-time control algorithm determined the best possible solution in the face of changing circumstances and limited resources.

It is important to note that the control algorithms running on UAV(1) and UAV(2) direct both UAVs to alter their return paths to the base due to the emergence of new taboo points making the planning algorithm determined flight paths too dangerous. The control algorithm uses each UAV's fuzzy risk-tolerance to determine how near each UAV may approach a taboo point.

Table 1: Details of three UAV mission depicted in Figure 5.

UAV 1 MISSION			UAV 2 MISSION			UAV 3 MISSION		
Locations	Fly Mode	Fuel Time Remain (minutes)	Locations	Fly Mode	Fuel Time Remain (minutes)	Locations	Fly Mode	Fuel Time Remain (minutes)
Base		90.0	Base		85.0	Base		85.0
(1,1)	NS	76.5088	(6,1)	NS	67.9691	(11,3)	NS	64.2839
(2,1)	S	61.5088	(7,2)	S	55.2412	(12,3)	S	51.0412
(3,1)	S	54.2662	(8,2)	S	47.9986	(13,3)	S	39.5559
(4,1)	S	42.7809	(9,2)	S	39.5133	(14,3)	S	31.0706
(5,1)	S	28.2956	(10,2)	S	22.028	Base	NS	6.2574
Base	NS	6.7113	Base	NS	11.7854			

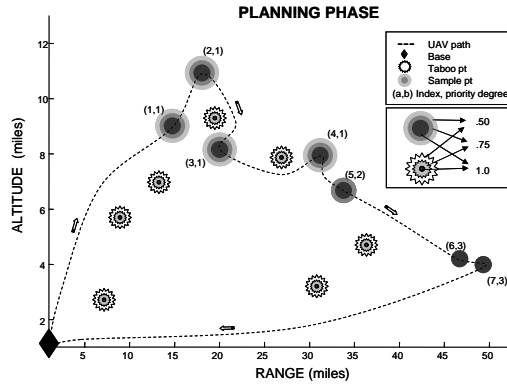


Figure 1: One UAV trajectory as determined by the planning algorithm.

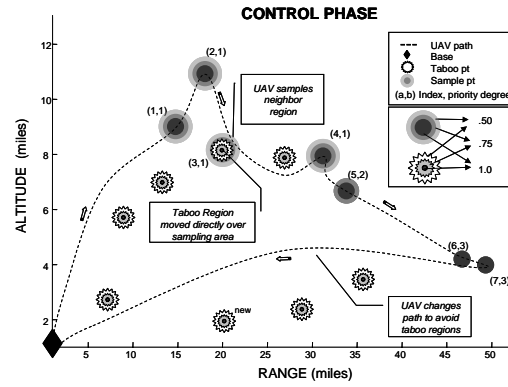


Figure 2: One UAV trajectory as determined by the real-time control algorithm.

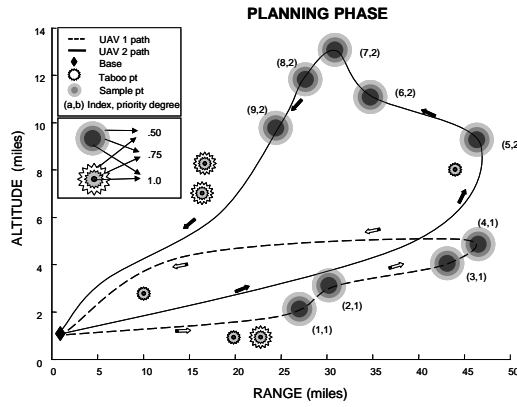


Figure 3: Trajectory of two UAVs as determined by the planning algorithm.

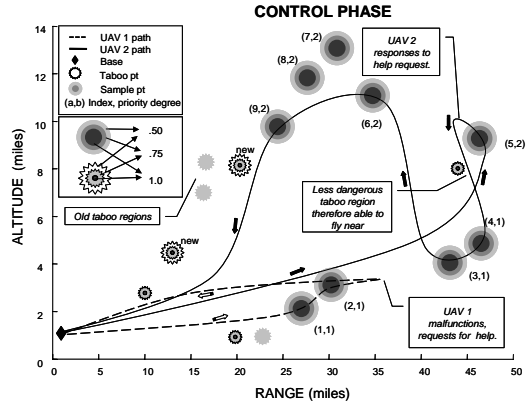


Figure 4: During flight, updates about environmental changes cause the real-time control algorithms on the two UAVs to change their trajectories.

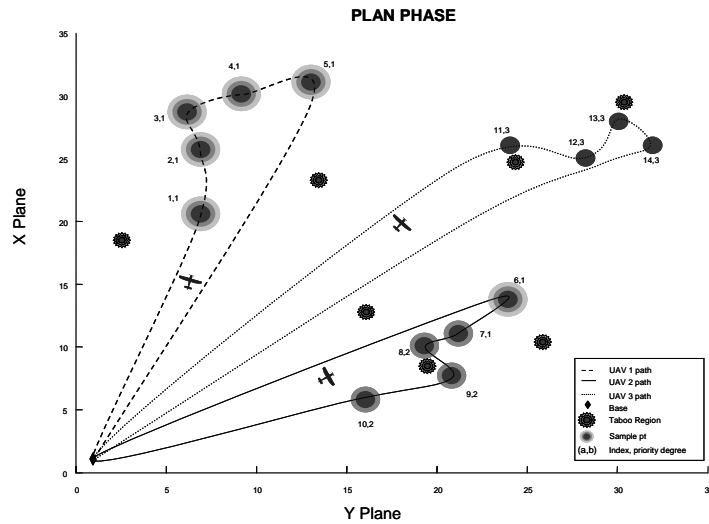


Figure 5: Three UAV mission described in Table 1, an example of the AUP decision tree's assignments.

Figure 5 provides an example of the AUP decision tree's assignment of three UAVs to three paths. The highest priority locations are assigned to UAV(1) as it has the greatest fuel capacity, i.e., 90 minutes. UAV(1) however does not have enough fuel to handle the high priority points located at positions six and seven and therefore UAV(2) is assigned these points along with the second degree high priority locations.

Table 1 provides numerical details of the tasks depicted in Figure 5. The column labels have the following interpretation: "Location," the UAV coordinates on the map; "Fly mode," whether the UAV sampled from its previous location to its current position. If the UAV sampled then a "S" was entered. "NS" was entered if sampling did not occur. "Fuel Time" refers to how much fuel remained by the time the UAV reached the associated location.

6 SUMMARY

Fuzzy logic based planning and control algorithms that allow a team of cooperating unmanned aerial vehicles (UAVs) to make meteorological measurements have been developed. The planning algorithm including the fuzzy logic based optimization algorithm for flight path determination and the UAV path assignment algorithm are discussed. The control algorithm also uses these fuzzy logic algorithms, but also allows three types of automatic cooperation between UAVs. The fuzzy logic algorithm for automatic cooperation is examined in detail. Methods of incorporating environmental risk measures as well as expert measures of UAV reliability are discussed as they relate to both the planning and control algorithms. Experimental results are provided. The experiments show the algorithms' effectiveness.

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