NAVAL POSTGRADUATE SCHOOL
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THESIS

OPTIMIZING UNMANNED AIRCRAFT SYSTEM SCHEDULING

by

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June 2008

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Unmanned Aircraft Systems (UASs) are critical for future combat effectiveness. Military planners from all branches of the Department of Defense now recognize the value that real time intelligence and surveillance from UAs provides the battlefield commander. The Operations Analysis Division of the Marine Corps Combat Development Command is currently conducting an Overarching Unmanned Aircraft Systems study to determine future force requirements. Current analysis is conducted through the use of the Assignment Scheduling Capability for Unmanned Air Vehicles (ASC-U) and several specially designed heuristics. The Unmanned Aircraft System Scheduling Tool (UAS-ST) combines these capabilities into one model and addresses several issues associated with ASC-U. UAS-ST allows the user to control all aspects of the UAS, define a scenario, and then generates a flight schedule over a known time horizon based on those inputs. All missions are assigned a user defined value and the total schedule value is reported. The user can then quickly change a parameter of the UAS, re-solve the model, and see the impact their proposed change has on the overall value of the schedule attained. Therefore, UAS-ST is a tool for analyzing the value of future changes in UAS structure.
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OPTIMIZING UNMANNED AIRCRAFT SYSTEM SCHEDULING

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ABSTRACT

Unmanned Aircraft Systems (UASs) are critical for future combat effectiveness. Military planners from all branches of the Department of Defense now recognize the value that real time intelligence and surveillance from UASs provides the battlefield commander. The Operations Analysis Division of the Marine Corps Combat Development Command is currently conducting an Overarching Unmanned Aircraft Systems study to determine future force requirements. Current analysis is conducted through the use of the Assignment Scheduling Capability for Unmanned Air Vehicles (ASC-U) and several specially designed heuristics. The Unmanned Aircraft System Scheduling Tool (UAS-ST) combines these capabilities into one model and addresses several issues associated with ASC-U. UAS-ST allows the user to control all aspects of the UAS, define a scenario, and then generates a flight schedule over a known time horizon based on those inputs. All missions are assigned a user defined value and the total schedule value is reported. The user can then quickly change a parameter of the UAS, re-solve the model, and see the impact their proposed change has on the overall value of the schedule attained. Therefore, UAS-ST is a tool for analyzing the value of future changes in UAS structure.
THESIS DISCLAIMER

The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.
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EXECUTIVE SUMMARY

Unmanned Aircraft Systems (UASs) procurement is vital to the United States Marine Corps' (USMC) combat effectiveness in the near future. UASs are used for collecting intelligence, surveillance, and targeting information. They accomplish these missions at a much lower overall risk than conventional, manned aircraft. Military planners from all branches of the Department of Defense (DoD) recognize the value that real time intelligence and surveillance from UASs provides the battlefield commander. In an ongoing operation, mission requests from units in theater typically far exceed the capacity of available UAS assets. Demand for UAS missions is increasing as the capability of these platforms expands. Individual branches of DoD are scrambling to acquire the UASs needed to support the requirements of currently deployed units in combat operations. As a result, interoperability and compatibility is a major concern with today’s current family of UASs.

Due to operational requirements in Iraq and Afghanistan, DoD is focusing procurement strategy away from force transformation and future generation weapons to more immediate concerns. Acquisition of UASs needed to meet operational requirements is the agency’s highest priority. As a result, large procurement budgets exist to fill the supply shortage and meet future operational requirements. Currently DoD is evaluating a large number of alternative UAS programs. This selection process requires an objective analysis of each alternative. The model in this thesis allows the USMC to accomplish their analysis by clearly depicting the impact of changes in system capabilities on a daily flight schedule. Application of the model is not limited to UASs. The model is capable of analyzing any asset which must be scheduled in response to user demands. Therefore, this model has future application in a multitude of other programs.

The current model in use for the Marine Corps Combat Development Command (MCCDC) Overarching Unmanned Aircraft Systems (OUAS) study is the Assignment Scheduling Capability for UAVs (ASC-U) model. The design agency for ASC-U is the U.S. Army Training and Doctrine Command Analysis Center (TRAC). ASC-U is
designed to support the development of an effective UAS force structure. It is a spreadsheet-based decision support tool primarily for allocation and scheduling of assets. ASC-U addresses complexities in military operations and scheduling of multiple moving platforms. ASC-U accepts user parameters that define a scenario then seeks to provide a feasible schedule for available UASs. ASC-U is the first model that enables analysts to address this scheduling problem effectively. ASC-U combines both optimization and simulation to produce a tool with unique capabilities.

This thesis develops an integer linear programming model, UAS-ST, for scheduling UASs. UAS-ST allows the user to define all elements, both operational and performance, of the UAS via an Excel spreadsheet. A schedule generator written in visual basic for this application then takes these elements and generates a user-defined number of individual schedules. This schedule generation is done for every UAV (UAV) that is included in the scenario. Once the predefined number of schedules is generated, UAS-ST creates data files for a General Algebraic Modeling System (GAMS) model. GAMS, through the use of CPLEX, finds a near optimal combination of individual schedules to produce a complete schedule for a user designated time period.

The initial test scenario replicates a generic scenario given in the OUAS study. This replication provides the simplest and most direct comparison of results with ASC-U. The scenario time period is twenty four hours divided into ninety six intervals of fifteen minutes each. This scenario does not refer to a specific country, but is designed solely to provide the framework for determining the value of changes in UAS structure on a given set of mission requests. UAS force structure for the initial scenario represents a small but realistic composition of systems. Tier I is comprised of three separate units with four UAVs and one Ground Control Station (GCS) per unit. Tier II is comprised of three separate units with one UAV and one GCS per unit. Tier III is comprised of a single unit with two UAVs and two GCSs.

UAS-ST is significantly different from ASC-U. ASC-U utilizes an Excel spreadsheet and pulls the data into an Access database. UAS-ST applies an Excel spreadsheet, which then uses Visual Basic to transfer the data to GAMS. GAMS then applies the CPLEX solver to quickly optimize the schedule for all mission requests.
Features that require supplemental heuristics in ASC-U are incorporated directly into UAS-ST, eliminating the need for further processing. This produces a much quicker and efficient analysis of alternatives. CPLEX is highly efficient in preprocessing feasible solutions and reduces the run time to a matter of minutes. Overall, UAS-ST provides an efficient update to the model presented in ASC-U.

UASs are critical to our nation’s and the USMC's future military combat effectiveness. All branches of DoD recognize the need to develop an integrated network of UASs. To answer this need, the Marine Corps is developing the concept of the UAS Family of Systems (FoS). The FoS calls for a three tier structure of UASs with overlapping capabilities. Currently, the MCCDC Operation Analysis Division is conducting an OUAS study. This thesis is a direct contribution to that study, and UAS-ST, provides a planning tool for development of future UAS structure. UAS-ST allows the user to control all aspects of the UAS, define a scenario, and then generates a flight schedule over a known time horizon based on those inputs. All missions are assigned a user-defined value and the total schedule value is reported. The user can then quickly change an operational or performance parameter of the UAS, re-solve the model, and see the impact on the overall value of the schedule. UAS-ST is a tool for analyzing the value of future changes in UAS structure.
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I. INTRODUCTION

A. PURPOSE AND OVERVIEW

Unmanned Aircraft System (UAS) procurement is vital to the United States Marine Corp's (USMC) combat effectiveness in the near future. UASs are used for collection of intelligence, surveillance, and targeting information. They accomplish these missions at a much lower risk than conventional, manned aircraft. Military planners from all branches of the Department of Defense (DoD) recognize the value that real time intelligence and surveillance from UASs provides the battlefield commander. In an ongoing operation, mission requests from units in theater typically far exceed the capacity of available UAS assets. Future demand for UAS missions will increase as the capability of these versatile platforms expands. Individual branches of DoD are scrambling to acquire the UASs needed to support the requirements of currently deployed units in combat operations. [IHT, 2008] As a result, interoperability and compatibility is a major concern with today’s current family of UASs.

To address these issues in future systems, the USMC is developing the UAS Family of Systems (FoS). Each system consists of an Unmanned Air Vehicle (UAV), Ground Control Station (GCS), Launch and Recovery Station (LRS) and a combination of various sensors and payload components. The components of the FoS have several complementary capabilities which overlap in certain mission areas. The intent is to create a mix of several UASs able to support various units of different sizes and levels of operation.

To assess the effectiveness of a combination of UASs, quantitative models must be applied to provide a reasonably accurate measurement of capability and some guidance for efficient employment. To this end, this thesis develops a UAS planning and decision support tool that takes as input a planning horizon, a fleet of UAVs and their individual operating limits, a list of available payloads and a list of mission requests. The model then provides as output an operational schedule for each individual vehicle indicating the missions to be accomplished in a specified time horizon and the payloads
required. This schedule provides analysts the ability to quickly determine the impact of changes in any system parameter on the overall value of missions accomplished.

B. BACKGROUND

1. Problem Statement

Due to operational requirements in Iraq and Afghanistan, DoD is focusing procurement strategy away from force transformation and future generation weapons to more immediate concerns. Acquisition of the UASs needed to meet operational requirements is the agency’s highest priority. [IHT, 2008] As a result, large procurement budgets exist to fill the supply shortage and meet future operational requirements. Currently DoD is evaluating a large number of alternative UAS programs. The selection process requires an objective analysis of each alternative. This thesis develops a model to help the USMC with this analysis. The model in this thesis allows the USMC to accomplish their analysis by clearly depicting the impact of changes in system capabilities on a daily flight schedule. Application of the model is not limited to UASs. The model is capable of analyzing any asset which must be scheduled in response to user demands. Therefore, this model has future application in a multitude of other programs.

In recent comments, Defense Secretary Robert Gates, addresses wasteful or inefficient UAS procurement programs in a speech given at the Air Force’s Air University at Maxwell Air Force Base:

Because people were stuck in old ways of doing business, it's been like pulling teeth. While we've doubled this capability in recent months, it is still not good enough. [IHT, 2008]

The fact that the Defense Secretary is unusually blunt in his criticism of current program development, should serve as proof of the pressure to field future UASs.
2. The Marine Corps Three Tier UAS Family of Systems

The FoS divides the various UASs into three separate tiers. The tier assignments provide each level of the Marine Air Ground Task Force (MAGTF) an organic, interoperable, integrated and tailored capability that raises the situational awareness of the combat unit commander through a common communication network. The current operational conditions in Operation Enduring Freedom and Operation Iraqi Freedom demonstrate the importance of UAS operations and the need for commanders at all levels to maintain control of their respective battle space. Therefore, tiers are defined by the area of interest and operational level of the supporting unit, such as a company, battalion, or regiment. There is some operational overlap in tier capabilities; this is intentional and should be considered beneficial to mission accomplishment.
The three tiers are described in [MCCDC, 2005] as follows:

- **Tier I – Short Range UAS**
  - Operationally Supports Battalion, Company, and Platoon
  - Performs Reconnaissance and Surveillance Missions
  - Current System: Dragon Eye, Future: Raven-B
  - Endurance of 1.5 hours, Combat Radius of 5 miles
  - Speed: Less than 20 knots
  - Capacity for Single Payload

- **Tier II – Division or Regimental UAS**
  - Operationally Supports Division, Marine Expeditionary Unit (MEU), Regiment and Battalion
  - Air vehicle: Persistent, low cost, durable, low observable, easily transported, shipboard compatible, target acquisition capable, heavy fuel engine
  - Current: Scan Eagle Contract
  - Endurance of 15 hrs, Combat Radius of 50 miles
  - Speed: 60 knots
  - Capacity for Two Payloads

- **Tier III – UAS**
  - Operationally supports Marine Expeditionary Force, Marine Expeditionary Brigade, MEU, Division and Regiment
  - Reconnaissance Surveillance and Target Acquisition, Electro-Optical /Infrared Imagery (EO/IR)
  - Current System: Pioneer, Future Concept - Vertical Takeoff UAV
  - Air vehicle (Proposed; expeditionary, sea based, Vertical Takeoff, large sensor payload, multi-mission capable, weaponization)
  - Sensor payload (Proposed: EO/IR/laser designation, communication relay, Signals Intelligence, Electronic Warfare)
  - Endurance of 8 hours, Combat Radius of 300 miles
  - Speed: 200 knots
  - Capacity for three payloads
3. Current UAS Structure

There are several specialized terms associated with a UAS that this thesis uses repeatedly. To avoid any confusion, the following definitions apply:

- **UAV (Unmanned Aerial Vehicle):** A UAV is an unpiloted aircraft. UAVs can be remote controlled or fly an automated route based on pre-programmed information.

- **UAS (Unmanned Aircraft System):** UAS is the current term introduced by DoD and accepted by the Federal Aviation Administration to replace the term UAV. A UAS consists of not only the unmanned aircraft, but also the data link system, the launch and recovery station, and all maintenance and support equipment.

- **GCS (Ground Control Station):** A GCS is a land or sea-based system that allows an operator to control an unmanned aircraft. A GCS may control both "active" and "passive" missions. An active mission requires the operator to monitor the UAV, while a passive mission requires no interaction from the operator.
• **LRS (Launch and Recovery Site):** Used to control an unmanned aircraft during the initial and terminal phases of flight. The LRS can also function as a GCS when not recovering UAVs.

• **Payload:** Future system requirements call for a system of “payloads,” each of which provides a custom capability. These payloads will be uniform in size and connectivity to allow for rapid configuration of mission specific profiles.

• **Mission Package:** Consists of the combination of payloads loaded on an individual UAV which determines the mission capability of the UAV. Required payload capacity is a key element of the current study.

4. **Current UAS Missions Types**

Following is a table of terms associated with current UAS missions. These missions represent general categories and are derived from the Overarching Unmanned Aircraft System (OUAS) study [OUAS, 2007].

<table>
<thead>
<tr>
<th>Missions</th>
<th>Abbreviation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reconnaissance, Surveillance, Target Acquisition (RSTA) (EO/IR)</td>
<td>RSTA-EO/IR</td>
<td>ISR asset for routine day and night time operations</td>
</tr>
<tr>
<td>Reconnaissance, Surveillance, Target Acquisition (Synthetic aperture radar)</td>
<td>RSTA-SAR</td>
<td>ISR asset for dense vegetation and poor weather conditions</td>
</tr>
<tr>
<td>Signals Intelligence</td>
<td>SIGINT</td>
<td>Sensor(s) designed for passive collection of signals</td>
</tr>
<tr>
<td>Air Vehicle Communications Link Relay</td>
<td>AV_CLR</td>
<td>Relays information and instructions through one UAV to another</td>
</tr>
<tr>
<td>Communications Relay</td>
<td>CR</td>
<td>Relays voice and data between ground points</td>
</tr>
<tr>
<td>Strike</td>
<td>STK</td>
<td>Weapons enabled kinetic destruction of a time sensitive target</td>
</tr>
<tr>
<td>Electronic Warfare</td>
<td>EW</td>
<td>Active denial of radio frequency</td>
</tr>
</tbody>
</table>

Table 1. General Description of Mission Types
C. SCOPE AND LIMITATIONS

The intent of this thesis is to provide a model for use as an analytical tool in determining the future force structure for UASs. The model allows the user to quickly change both operational and performance parameters for each UAS tier. Once parameters are set, the model quickly generates a near-optimal schedule. This rapid schedule generation allows an analyst to see the impact of changing UAS capabilities on a given daily schedule.

D. THESIS ORGANIZATION

Chapter II provides a discussion of the Assignment Scheduling Capability for UAVs (ASC-U) the current UAS evaluation tool in use by the Operation Analysis Division (OAD), MCCDC. Chapter III describes the optimization model and the stack based enumeration heuristic used to solve it. Chapter IV provides a detailed analysis of the ASC-U results and compares it to the current model. Chapter V is devoted to conclusions and recommendations for future research.
II. ASSIGNMENT SCHEDULING CAPABILITY FOR UAS

A. INTRODUCTION

The current model in use for the OUAS study is the ASC-U model. The agency responsible for the design of ASC-U is the U.S. Army Training and Doctrine Command Analysis Center (TRAC). ASC-U is designed to support the development of an effective UAS force structure. This chapter describes the basic structure of the ASC-U model. It begins with a description of the inputs accepted by the model then describes its implementation in the study. The chapter then discusses limitations of ASC-U which are addressed by this thesis. The majority of the information given here is summarized from the OUAS report [OUAS, 2007]. This chapter also includes a review of current literature.

B. BASICS OF ASC-U

1. Model Description

ASC-U supports the development of an effective UAS force structure. It is a spreadsheet-based decision support tool used primarily for allocation and scheduling. ASC-U addresses the complexities in military operations and scheduling of multiple moving platforms. ASC-U accepts user parameters that define a scenario and then seeks to provide a feasible schedule for available UASs. As stated in the ASC-U Analyst Manual:

ASC-U provides a solution to the following problem: Given a scenario that specifies the number of each type of UAV, initial UAV locations, and UAV performance characteristics, determine the number of missions that can successfully be completed and the schedule for each UAV. The solution must consider GCS locations and capacities, remote viewing terminal requirements, and communication platform footprint and capacities. [Ahner, 2006]
ASC-U is the first model that enables analysts to address this scheduling problem effectively. It combines both optimization and simulation to produce a tool with unique capabilities.

2. ASC-U Implementation

The ASC-U model works by allowing the user to design a scenario which consists of a set of mission requests. A mission request consists of a specific, required UAS capability at a specific geographic location, for a set amount of time. The location of the mission remains fixed once it is assigned. The allocation tool uses the UAS capability data and mission data it is given to create a feasible schedule which will accomplish as many mission requests as possible. ASC-U is deterministic. For a given input, it will always produce the same schedule with the same measures of performance. Specifically, ASC-U uses a deterministic algorithm to optimize over a given finite time horizon to obtain near-optimal UAS mission area assignments.

ASC-U allows the user to define several different input parameters. Mission requirements are the most important parameter. Mission requirements consist of a coordinate location, payload requirement, length of mission and mission priority. Mission priority functions as a selection criterion. A user may establish mission precedence by assigning a higher value to a specific mission type. UAS parameters that may be entered by the user are payload details, GCS attributes, and UAV attributes. GCS attributes consist of coordinate location, control limits, and unit assignment. UAV attributes include speed, operating time, combat radius, launch site, and total time available.

3. Model Capabilities and Limitations

ASC-U is the first attempt to create a specific tool that involves all aspects of the UAS family of systems. As part of its support program, TRAC-Monterey publishes an ASC-U user’s manual. For its use in the OUAS study, some settings are different than the manual’s recommended settings. Different settings are required due to the small size of the original test scenario chosen. ASC-U is designed to model several thousands of
missions over a long time period. The scenarios used in the OUAS study are much shorter in duration and involve only a few hundred missions.

The mission requirements are the most important input data because they have the most direct effect on the schedule generated. ASC-U attempts to complete as many mission hours as possible. The objective function has a significant drawback. It leads to preferential assignment of missions that are close to the launch and recovery site because they allow for more follow-on missions to be accomplished. The model schedules as many close-in missions as possible and foregoes farther outlying missions. Therefore, mission priority, a specific input, allows the user to set a precedence level. However, in some instances the user is forced to artificially inflate the value of a mission to ensure it is scheduled.

All inputs are usually entered in Excel spreadsheets, and then read into Access. ASC-U can take input from either Excel or Access. The Excel inputs are placed in an Access database as the model begins its run. The output is also stored in an Access database. Several tables are produced in the output. The most important table for the OUAS study is mission coverage. Mission coverage is broken down into requesting unit, mission type and UAV type. In ASC-U every possible payload combination is enumerated as a mission package. Mission packages are then assigned to UAVs. Mission package usage is recorded; therefore individual payload usage is not available.

The objective of the first OUAS study is to provide as many hours of UAS support as possible. For ASC-U, the two key factors are the optimization interval and the time horizon for scheduling the UAV. The optimization interval controls how often ASC-U runs its routine to assign missions. The time horizon controls how far forward in time ASC-U will look to assign the UAV to a mission. The optimization interval is crucial because if the interval is set too long then the UAS will remain idle instead of performing another mission. If the interval is set too low the model has difficulties and exhibits odd behavior. An interval of 12 minutes is best for the scenarios used in the OUAS study [OUAS, 2007]. Time horizon is critical because ASC-U will only schedule a UAV once during the given time period. Therefore, if the horizon is set too long, ASC-U can see a high value mission at the end of the period and keep a UAV idle the entire
period waiting for that mission. A UAV can complete another mission and still complete its priority mission. On the other hand, if the time horizon is set too low then ASC-U misses high priority missions because it cannot see far enough out. The final horizon for the OUAS study is 6 hours for Tier II and 4 hours for Tier III.

Because of these shortcomings, several workarounds and new heuristics are used to enable ASC-U to find schedules that exhibit required behaviors. The SUPER MISSION ability allows a UAV to fulfill multiple missions if they are within its operating range. Three optional heuristics are also used in the OUAS study. They are implemented in this order:

**EARLY RETURN** (Go Home vs. Stay) - When a UAV completes an assigned mission, a value of $\text{TRUE}$ allows the UAV to return to base if it can do so and still make it back on station in time for its next mission. A value of $\text{FALSE}$ forces the UAV to fly until its operating limit is met. For the OUAS study, this is set to $\text{FALSE}$.

**SECONDARY AREAS** (Go Get More Value From Another Mission) - If a UAV is scheduled for more than one mission in the same location with a time gap in between them, a value of $\text{TRUE}$ allows the UAV to perform another mission in between as long as it is available at the start of its previously scheduled mission. A value of $\text{FALSE}$ will force it to remain on station until the start of its next mission. For the OUAS study, this was set to $\text{TRUE}$.

**APPENDED AREAS** (Done, Is There Another Mission?) - If a UAV has completed its assigned missions, a value of $\text{TRUE}$ allows it to use its remaining time to find another mission. A value of $\text{FALSE}$ will not allow additional missions. For the OUAS study, this was set to $\text{TRUE}$.

C. LITERATURE REVIEW

Many recent studies attempt to shape some aspect of the future design of UAS force structure. An unintended consequence is that most of these studies focus only on some specific technical portion of the overall problem. The Deputy Commandant, Aviation and the Deputy Commandant Combat Development and Integration are
sponsoring the OUAS study. Their intent is to analyze the future USMC UAS force structure to determine how to best meet the needs of the MAGTF. The initial phase of OUAS is being conducted by OAD MCCDC. The model given in this thesis is intended for use in the follow on analysis of OUAS. Therefore, the initial report by OAD is critical to this thesis, as it largely determined the requirements for the model.

Tutton [2003] deals with the optimal placement of a unit’s sensing assets. He presents a methodology for finding the most beneficial mix and allocation strategy for an individual unit’s sensors for a given threat scenario. Doll [2004] takes the model developed by Tutton [2003] and translates it into a programming language for easier simulation. She refines many of the constraints in the original model to make for a much more realistic simulation. Finally, Zacherl [2006] deals specifically with reactive aircraft scheduling. The thesis develops a model which reviews a current air tasking order and then rapidly reassigns aircraft to new targets as they become available.

Finally a large number of commercial information sources address current topics in UAS development and model optimization. When possible, these sources are used for the sake of currency or accuracy.
III. OPTIMIZATION MODEL FOR THE SCHEDULING OF UNMANNED AIRCRAFT SYSTEMS

A. INTRODUCTION

This chapter develops the mathematical programming model, Unmanned Aircraft System Scheduling Tool (UAS-ST). UAS-ST applies an optimization based approach to analyze the best mix of future UAS mission capabilities. The main goal of this thesis is to provide a model, which will be applied to the current OUAS study.

The model allows the user to define all elements of the UAS via Excel spreadsheet. The schedule generator then takes these elements and generates a user defined number of individual schedules for every UAV included in the scenario. This schedule generation is done via Excel and Visual Basic. Once the predefined number of schedules is generated, the data is read into a General Algebraic Modeling System (GAMS) program to find a near optimal combination of individual schedules.

B. AN INTEGER PROGRAM TO OPTIMIZE UAS SCHEDULING

The following integer linear program (ILP), UAS-ST, attempts to find the consolidated UAS schedule with the highest overall total value. First the model is presented, then the detailed input required to optimize the objective function is discussed. Once this is complete, instances of UAS-ST are generated to demonstrate its function.

1. Indices

\( v \in V \) Tier levels [3]

\( h \in H \) Mission types [2] (H= \{'passive, active'}

\( g \in G \) Ground Control Station (GCS) [~10]

\( l \in L \) Launch and Recovery Site (LRS) [~6]

\( m \in M \) Missions [~150] (alias \( m' \))
\[ p \in P \quad \text{Payload module types [~10]} \]

\[ t \in T \quad \text{Time periods [96]} \]

\[ s \in S \quad \text{UAV employment schedules} \]

\[ m' \in P_m \quad \text{Mission prerequisites: mission } m \text{ cannot be covered in any time period } t \text{ unless at least one mission } m' \text{ in } P_m \text{ is also covered in time period } t \]

\[ (m,m') \in E \quad \text{Pairwise exclusive missions: mission } m \text{ cannot be covered in any time period that mission } m' \text{ is covered. } E \subseteq M \times M \]

\[ (s,m,t) \in A \quad \text{schedule } s \text{ covers mission } m \text{ in time period } t \]

\[ (s,v,t) \in B \quad \text{schedule } s \text{ uses UAV in tier level } v \text{ in time period } t \]

\[ (s,l,t) \in K \quad \text{schedule } s \text{ uses LRS } l \text{ in time period } t \]

\[ (s,c,t) \in Q \quad \text{schedule } s \text{ carries payload of class } c \text{ in time period } t \]

\[ (s,l) \in SL \quad \text{schedule } s \text{ uses LRS } l \]

\[ (m,g) \in MG \quad \text{mission } m \text{ can be covered by GCS } g \]

\[ (m,h) \in MH \quad \text{mission } m \text{ is of mission type } h \]

\[ (g,v) \in GV \quad \text{GCS } g \text{ can support a UAS in tier } v \]

2. **Given Data [units]**

\[ \text{val}_m \quad \text{Value per time period of mission } m \text{ (=total value of } m \text{ divided by length of } m) \]

\[ r_m \quad \text{Number of time periods of required coverage for mission } m \]

\[ \text{num_uavs}_{v,t} \quad \text{Number of UAVs in tier level } v \text{ available in time period } t \]

\[ \text{num_pay}_{c,t} \quad \text{Number of payloads of class } c \text{ available in time period } t \]
$gcs\_cap_{g,t}^h$ Capacity (in UAVs) of GCS $g$ in time period $t$ for missions of type $h$

$lrs\_cap_{l,t}$ Capacity (in UAVs) of LRS $l$ in time period $t$

$length_m$ Maximum number of periods mission $m$ can be covered

$k_{l,s,t}$ =1 if schedule $s$ uses LRS $l$ in time period $t$

3. Decision Variables

$X_s$ =1 if schedule $s$ flown by some UAS [binary]

$Y_{m,v,t}$ =1 if mission $m$ covered by a tier $v$ UAS in period $t$

$W_{m,v,g,t}$ =1 if mission $m$ supported by GCS $g$ for a tier $v$ UAS in time period $t$ [binary]

$D_m$ Total dwell time on mission $m$ [time periods]

$LOAD_{c,v,l}$ Payloads of class $c$ for tier $v$ sited at LRS $l$ [cardinality]
4. Formulation

\[
\begin{align*}
\text{max} & \quad \sum_m val_m D_m & (R0) \\
\text{s.t.} & \quad \sum_{x(s,v,t) \in B} X_s \leq \text{num\_uavs}_{l,v,t} & \forall l,v,t & (R1) \\
& \quad \sum_{x(s,v,t) \in B} X_s \leq \text{LOAD}_{c,v,l} & \forall c,v,l,t & (R2a) \\
& \quad \sum_l \text{LOAD}_{c,v,l} \leq \text{num\_pay}_{c,v} & \forall c,v & (R2b) \\
& \quad \sum_{m,v,g,t \in MG, (m,h) \in MH, (g,v) \in GV} W_{m,v,g,t} \leq \text{gcs\_cap}_{g,t}^h & \forall g,t,h & (R3) \\
& \quad \sum_{x(s,l,t) \in K} X_s \leq \text{hrs\_cap}_{l,t} & \forall l,t & (R4) \\
& \quad Y_{m,v,t} \leq \sum_{x(s,m,t) \in A, (s,v,t) \in B} X_s & \forall m,v,t & (R5) \\
& \quad D_m \leq \sum_{v,t} Y_{m,v,t} & \forall m & (R6) \\
& \quad D_m \leq \sum_{m',v,t} Y_{m',v,t} & \forall m : P_m \neq \emptyset, \forall v, \forall t & (R7a) \\
& \quad Y_{m,v,t} \leq \sum_{g(m,g) \in MG, (g,v) \in GV} W_{m,v,g,t} & \forall m : P_m = \emptyset, \forall v, \forall t & (R7b) \\
& \quad \sum_v Y_{m,v,t} + \sum_{m'} Y_{m',v,t} \leq 1 & \forall (m,m') \in E, \forall t & (R8) \\
& \quad D_m \geq r_m & \forall m & (R9) \\
& \quad 0 \leq D_m \leq \text{length}_m & \forall m & (R10) \\
& \quad X_s \in \{0,1\} & \forall s & (R11) \\
& \quad Y_{m,v,t} \in \{0,1\} & \forall m,v,t & (R12) \\
& \quad W_{m,v,g,t} \in \{0,1\} & \forall m,v,g,t & (R13)
\end{align*}
\]
5. Discussion

The objective function (R0) calculates the value of all mission time periods covered. Constraints (R1) limit the number of active UAVs in each tier, in each time period, based at each LRS, by the number of UAVS available. Constraints (R2a) limit the number of a specific payload class an tier flown from an LRS in each period to the number of payloads of that class and tier assigned to that LRS, and constraints (R2b) limit the total number of payloads of each class and each tier assigned over all LRSs by the total number available in that class. Constraints (R3) limit the number of missions, by type supported by a GCS in each time period. Constraints (R4) limit the total number of UAVs launching or recovering at a LRS by the capacity of the LRS in a given time period. Constraints (R5) controls whether or not a mission is accomplished in any time period. Constraints (R6) limit the total time spent on a mission to the number of time periods covered. Constraints (R7a) address prerequisite missions such as AV_CLR required for long range Tier III missions, and (R7b) address line-of-sight issues from each GCS for missions that do not have other prerequisites. Constraints (R8) prevent scheduling of mutually exclusive missions by UAS of any tier. Constraints (R9) force “required” missions to be covered for the number of time periods required. Constraints (R10) limit the total dwell time on a mission to between zero and the total amount of time requested for the mission. Constraints (R11-R13) restrict schedule assignment, mission coverage, and GCS assignment to be binary decisions.

6. Route Enumeration and Data Development

UAS-ST requires a significant amount of data processing to produce an optimal schedule; most of this effort is performed by a stack-based enumeration routine that generates all feasible schedules for each tier and LRS in the given scenario. The schedule generator, or simply generator, requires two primary data structures for computation of feasible schedules: a stack, PATH(), containing a current feasible list of missions to be accomplished, and an array, ON_STACK(), that indicates whether each mission is currently on the stack of missions. Various data tables are pre-computed to aid in
determining feasibility, such as flight times between airfields and missions, and between pairs of missions, payload requirements by mission, etc.

For each tier, $v$, and LRS, $l$, such that there is at least one UAS of tier $v$ located at $l$, the generator starts with an empty mission list PATH(), (representing the trivial action of launching, and then immediately recovering, a UAS of tier $v$ from $l$), and builds feasible mission lists exhaustively by adding one mission at a time to the end of the current mission list represented in PATH(). A mission is only added to the end of PATH() if it is within range of a GCS capable of controlling the appropriate tier, if the first period of the mission that can be accomplished (based on the current mission list) allows the UAS to return back to its LRS before running out of operational time available, and if the required list of payloads to accomplish all the missions in PATH() can fit on one UAS of tier $v$. If a mission does not meet these requirements, it is discarded and the next mission from the overall mission list is considered. Other rules for calculating feasible extensions to a current feasible PATH() can be incorporated easily, but these three capture the primary constraints on feasibility. For example, we also check to see if a mission is already on the stack PATH(), and discard those to prevent missions being revisited. However, if the capability to revisit missions in the same schedule is required, this test can be removed. Of course, more feasible schedules will be generated if this is done.

Once a mission is added to PATH(), all missions are considered again for the next empty slot at the end of PATH(). In this manner the generator provides a depth-first exploration of all feasible mission lists. If all missions have been ruled out for a slot, the stack is “popped,” the previous slot is then considered again, and the next mission in the list takes the current mission’s place; this replacement is repeated until a feasible mission for that slot is found. If no more feasible missions are found for that slot, we “pop” the stack again. When the first slot is finished, we have enumerated all missions from $l$ using tier $v$ assets.

Every feasible set of missions in PATH() is recorded by incrementing the number of feasible paths found, $s$, and then adding the appropriate elements to the sets
\((s, m, t) \in A, \ (s, v, t) \in B, \ (s, c, t) \in Q, \ \text{and} \ (s, l) \in SL\) to define schedule \(s\). See Appendix B for the details of the algorithm.

We set an upper bound on the total number of schedules that can be generated, so as not to create unsolvable ILPs. We also provide a limit on the number of missions enumerated per schedule, and the generator implicitly calculates a limit on the number of schedules to generate for each tier-LRS pair, to allow for the generation of a nonempty list for each such pair regardless of the order in which schedules are generated for those pairs. So, for example, we might set a limit of 120,000 total schedules, and four missions per schedule. The generator calculates how many tier-LRS pairs are feasible, and if, say, there are six such pairs in the scenario, then the generator will generate no more than 20,000 schedules for each pair considered, calculated cumulatively. (Specifically, in this example if the first pair does not generate all 20,000 of its allotted schedules, then the generator can generate up to 40,000 total schedules for the first two pairs combined.) When these enumeration limits are reached for a tier-LRS pair, the stack is cleared out and the generator moves to the next tier-LRS pair.

This procedure can generate tens- or hundreds-of-thousands of feasible schedules. Each such schedule is associated with a decision variable, \(X_s\), in the ILP. The limits on enumeration therefore restrict the schedules available, and, consequently, the resulting ILP will be a restriction of the model that considers every feasible schedule. The more schedules that are generated (through increasing the limit on missions per schedule, or the total schedules generated, etc.) the better the final schedule found by the integer program.
IV. COMPUTATIONAL RESULTS

The OUAS study generic unclassified scenario is replicated with the intent to test the results provided by UAS-ST [OUAS, 2007]. All computations are performed on a Pentium 4 desktop computer at the Naval Postgraduate School with the use of the GAMS solver CPLEX [2008].

A. INITIAL TEST SCENARIO

The initial test scenario replicates a generic scenario given in the OUAS study [OUAS, 2007]. This replication provides the simplest and most direct comparison of results with ASC-U. The scenario time period is twenty four hours divided into ninety six intervals of fifteen minutes each. This scenario does not refer to a specific country, but is designed solely to provide the framework for determining the value of changes in UAS structure on a given set of mission requests. UAS force structure for the initial scenario represents a small but realistic composition of systems. Tier I is comprised of three separate units with four UAVs and one Ground Control Station (GCS) per unit. Tier II is comprised of three separate units with one UAV and one GCS per unit. Tier III is comprised of a single unit with two UAVs and two GCSs.

Table 2 provides a summary of the given UAS force structure for the generic scenario.

<table>
<thead>
<tr>
<th>Number of:</th>
<th>Tier I</th>
<th>Tier II</th>
<th>Tier III</th>
</tr>
</thead>
<tbody>
<tr>
<td>Systems</td>
<td>12</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>UAVs per system</td>
<td>3</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>GCSs per system</td>
<td>1</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>UAVs controlled by GCS</td>
<td>1</td>
<td>2</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 2. Number of UAS Assets Available in Generic Scenario

The initial test scenario consists of placing units from different UAS Tiers at specific ranges to test the scheduling constraints of the model. The tier III squadron is centered at an airfield in support of a regiment. The squadron consists of two UAVs and
two GCSs at this location. These are the only tier III assets available for our test scenario. The mission areas for the tier III UAS are obtained by plotting points in the cardinal directions at or beyond one hundred and fifty nautical miles, (beyond tier II range).

The three tier II units are deployed in a triangular pattern around the tier III location in direct support of individual battalions. The tier II units are separated from each other by a distance of at least 20 nautical miles. As before, specific mission areas are chosen for each tier II unit.

Tier I units are collocated in the same manner as tier II, but are in direct support at the company level. Each tier I unit consists of four UAVs and a single GCS. Mission areas are selected with a special emphasis on their range. Once the areas are designated, they are used repetitively to generate multiple missions. The use of repetitive mission areas makes it much simpler to detect mission assignments beyond the range of a specific tier. Tier I and II missions are within range of tier III assets.

Figure 3. Plot of OUAS Scenario Taken from OUAS
B. UAS-ST INITIAL RESULTS AND ANALYSIS

Data for the initial scenario is entered via a mission request worksheet in Excel. The user enters mission requests for UAS coverage in the following manner:

<table>
<thead>
<tr>
<th>Mission ID</th>
<th>Location</th>
<th>Mission Class</th>
<th>Start Time</th>
<th>End Time</th>
<th>Total Time Requested</th>
<th>Start Period</th>
<th>Finish Period</th>
<th>Time Periods Requested</th>
<th>Value Per Time Period</th>
</tr>
</thead>
<tbody>
<tr>
<td>m1</td>
<td>N323934W1144850</td>
<td>AV_CLR</td>
<td>0:00</td>
<td>8:00</td>
<td>8:00</td>
<td>1</td>
<td>32</td>
<td>32</td>
<td>5</td>
</tr>
<tr>
<td>m2</td>
<td>N322947W1144606</td>
<td>ISR</td>
<td>0:30</td>
<td>2:30</td>
<td>2:00</td>
<td>3</td>
<td>10</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>m3</td>
<td>N322825W1144547</td>
<td>ISR</td>
<td>1:00</td>
<td>4:00</td>
<td>3:00</td>
<td>5</td>
<td>16</td>
<td>12</td>
<td>10</td>
</tr>
<tr>
<td>m4</td>
<td>N322648W1144730</td>
<td>ISR</td>
<td>1:30</td>
<td>2:30</td>
<td>1:00</td>
<td>7</td>
<td>10</td>
<td>4</td>
<td>10</td>
</tr>
<tr>
<td>m5</td>
<td>N322549W1144914</td>
<td>ISR</td>
<td>2:00</td>
<td>4:00</td>
<td>2:00</td>
<td>9</td>
<td>16</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>m6</td>
<td>N324012W1142426</td>
<td>ISR</td>
<td>2:30</td>
<td>5:30</td>
<td>3:00</td>
<td>11</td>
<td>22</td>
<td>12</td>
<td>10</td>
</tr>
<tr>
<td>m7</td>
<td>N324021W1142011</td>
<td>ISR</td>
<td>3:00</td>
<td>4:00</td>
<td>1:00</td>
<td>13</td>
<td>16</td>
<td>4</td>
<td>10</td>
</tr>
<tr>
<td>m8</td>
<td>N324055W1142318</td>
<td>ISR</td>
<td>3:30</td>
<td>5:30</td>
<td>2:00</td>
<td>15</td>
<td>22</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>m9</td>
<td>N323922W1142442</td>
<td>ISR</td>
<td>4:00</td>
<td>7:00</td>
<td>3:00</td>
<td>17</td>
<td>28</td>
<td>12</td>
<td>10</td>
</tr>
<tr>
<td>m10</td>
<td>N323848W1142056</td>
<td>ISR</td>
<td>4:30</td>
<td>5:30</td>
<td>1:00</td>
<td>19</td>
<td>22</td>
<td>4</td>
<td>10</td>
</tr>
</tbody>
</table>

Table 3. Input Worksheet for Mission Requests

Waypoints for the mission areas are placed at specific ranges to test the scheduling constraints of the model. These waypoints are then used to generate a table of one hundred and fifty mission requests. The requests are broken down by mission areas. Mission requests one through forty focus on the tier I mission areas. Requests forty one through one hundred and three focuses on tier II and the remaining requests are tier III mission areas. See Appendix A for the complete scenario worksheet used in analysis of UAS-ST. The model constraints allow a higher tier vehicle to perform a lower tier mission if that is the highest value mission available at the time and the vehicle is within range. However, the longer range of each subsequent tier’s mission area make it infeasible to schedule a lower tier UAS. The sequential mission numbers enable the user to quickly identify any infeasible mission assignments.

Mission classes are defined according to the mission categories given in the OUAS study. Values for the individual missions are chosen arbitrarily. Selection of the assigned mission values is critical because they have the ability to skew the results by inflating the value of a specific category. In the scenario, active missions are given greater priority than passive. Of the active subset, missions which are unique to a
specific tier are given the highest priority. Missions which are redundant to all tiers are given the lowest priority. Table 4 outlines the missions which each tier can perform and their associated value in the scenario.

<table>
<thead>
<tr>
<th>Mission</th>
<th>Tier I</th>
<th>Tier II</th>
<th>Tier III</th>
</tr>
</thead>
<tbody>
<tr>
<td>ISR</td>
<td>10</td>
<td>15</td>
<td>20</td>
</tr>
<tr>
<td>AV_CLR</td>
<td>5</td>
<td>10</td>
<td>5</td>
</tr>
<tr>
<td>CR</td>
<td>10</td>
<td>10</td>
<td>5</td>
</tr>
<tr>
<td>LSR_P</td>
<td>30</td>
<td>30</td>
<td></td>
</tr>
<tr>
<td>SIGINT</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>EW</td>
<td></td>
<td></td>
<td>40</td>
</tr>
<tr>
<td>STK</td>
<td></td>
<td></td>
<td>60</td>
</tr>
<tr>
<td>LSR_D</td>
<td></td>
<td></td>
<td>40</td>
</tr>
</tbody>
</table>

Table 4. Assigned Mission Values by Tier

The requested mission time is defined through the start and end times, which are entered by the user. UAS-ST then converts that time into the appropriate number of fifteen minute time periods. Once a UAS is assigned in a given time period it may not be reassigned until the next time period. Times are started at the beginning of the first time period and continue to the end of the final period.

Another element which greatly affects the optimal value achieved is the number of mission payloads available. See Figure 4 for a sample of the payload worksheet. By manipulating the number of payloads of a given type available to a UAS tier, it is possible to test the scheduling constraints and see very quickly if payload availability was a limiting factor. This is highly beneficial in determining future requirements for UAS structure.
### Example of Payload Worksheet

<table>
<thead>
<tr>
<th>Payload ID</th>
<th>Payload Type</th>
<th>Mission Class</th>
<th>Quantity Available</th>
<th>UAS Tier</th>
</tr>
</thead>
<tbody>
<tr>
<td>p1</td>
<td>EO/IR</td>
<td>ISR</td>
<td>9</td>
<td>T1</td>
</tr>
<tr>
<td>p2</td>
<td>EO/IR-targeting</td>
<td>ISR_T</td>
<td>3</td>
<td>T2</td>
</tr>
<tr>
<td>p3</td>
<td>EO/IR-targeting</td>
<td>ISR_T</td>
<td>2</td>
<td>T3</td>
</tr>
<tr>
<td>p4</td>
<td>SAR w/MTI</td>
<td>ISR_SAR</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p5</td>
<td>SIGINT</td>
<td>SIGINT</td>
<td>1</td>
<td>T2</td>
</tr>
<tr>
<td>p6</td>
<td>SIGINT</td>
<td>SIGINT</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p7</td>
<td>Mine Detection</td>
<td>ISR_MD</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p8</td>
<td>Pointer</td>
<td>LSR_P</td>
<td>1</td>
<td>T2</td>
</tr>
<tr>
<td>p9</td>
<td>Pointer</td>
<td>LSR_P</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p10</td>
<td>Rangefinder</td>
<td>LSR_RF</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p11</td>
<td>Designator</td>
<td>LSR_D</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p12</td>
<td>AV_CLR</td>
<td>AV_CLR</td>
<td>9</td>
<td>T1</td>
</tr>
<tr>
<td>p13</td>
<td>AV_CLR</td>
<td>AV_CLR</td>
<td>3</td>
<td>T2</td>
</tr>
<tr>
<td>p14</td>
<td>AV_CLR</td>
<td>AV_CLR</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p15</td>
<td>CR</td>
<td>CR</td>
<td>1</td>
<td>T2</td>
</tr>
<tr>
<td>p16</td>
<td>CR</td>
<td>CR</td>
<td>1</td>
<td>T3</td>
</tr>
<tr>
<td>p17</td>
<td>Strike</td>
<td>STK</td>
<td>2</td>
<td>T3</td>
</tr>
<tr>
<td>p18</td>
<td>EW</td>
<td>EW</td>
<td>2</td>
<td>T3</td>
</tr>
</tbody>
</table>

Figure 4. Example of Payload Worksheet

System capabilities and limitations are drawn directly from the OUAS study. The study seeks to define UAS tier requirements. Therefore, those assumptions are critical to any analysis that is conducted. The tier parameters as given in Figure 5 are used in all testing. Operational time limit and maintenance time are not known at this time. Those columns are for future expansion when the data becomes available.

<table>
<thead>
<tr>
<th>UAS Tier</th>
<th>Max Endurance (hrs)</th>
<th>Cruise Speed (knots)</th>
<th>Operational Radius (nm)</th>
<th>Payload Capacity</th>
<th>Operational Time Limit (hrs)</th>
<th>Maintenance Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1</td>
<td>1.5</td>
<td>17</td>
<td>5</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>T2</td>
<td>15</td>
<td>60</td>
<td>50</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>T3</td>
<td>8</td>
<td>200</td>
<td>300</td>
<td>3</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* All Values Taken from Table ES-2 of Overarching UAS Study 21Nov2007

Figure 5. OUAS Study Future Tier Performance Parameters

Once all data for the scenario is entered via Excel spreadsheet, UAS-ST is run from the graphical interface given in Figure 6. The interface, known as the dashboard,
allows the user to specify several key parameters. First the user specifies the start time, the time periods in horizon, and the number of periods per hour. For the mission generation portion, a user specifies the maximum number of schedules that UAS-ST can generate and the maximum number of missions per schedule that a single UAV can perform. These two parameters greatly affect the outcome of the model.

As the number of maximum missions per schedule increases, the number of possible schedules rapidly increases as well. Setting the number of maximum schedules too low prevents a full enumeration of all possible schedules and is a constraint on the model. Setting the number of maximum schedules too high allows a full enumeration of all possible schedules and results in a longer processing time. See Figure 6 for an example. All tested combinations satisfy the requirement for a quick total solution time. Once all parameters are set, selecting the BUILD function initiates VBA to build the designated number of flight schedules. After the build is complete, selecting SOLVE initiates GAMS to read in the data, apply the selected solver, and generate a near optimal solution. When GAMS reaches a solution, selection of RESULTS displays the solution in the format seen in Figure 7.

<table>
<thead>
<tr>
<th>UAS Planner v 1.01 2-Jun-08</th>
<th>Build</th>
<th>Solve</th>
<th>Results</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Start Time</strong></td>
<td>0:00</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Time Periods in Horizon</strong></td>
<td>96</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>First Planning Period</strong></td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Last Planning Period</strong></td>
<td>96</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Periods per hour</strong></td>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Max Schedules</strong></td>
<td>75000</td>
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**Figure 6. Sample of User Interface (Dashboard)**
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<th>Total Value Achieved</th>
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Figure 7. Partial Display of Optimal UAS-ST Schedule

Figure 7 demonstrates the format in which the solution given by UAS-ST is displayed. All missions are sorted sequentially by their assigned mission number. The total value achieved for each mission is given in the right column. The total value obtained by the entire schedule is given in the top right corner. This format enables the easiest comparison between runs because it quickly lets the user see which missions are scheduled and for what portion of the requested time. If certain missions are not being scheduled, the trend is easy to detect.

C. COMPARING UAS-ST TO ASC-U

ASC-U is the model originally used in the OUAS study. It is highly useful in the analysis of UAS future requirements with several strong attributes. However, there are some areas which require modification to meet the needs of the OUAS study. The intent of this thesis is to develop a user friendly model that addresses those shortcomings and meets the requirements of OAD.
For ease-of-use the individual elements of the UAS are separated into different worksheets. A separate spreadsheet for the UAS tier-specific performance requirements is also included. This spreadsheet allows the user to verify the basic parameters of all UAS tiers in one chart. The user can easily modify a parameter and re-run the model to analyze the effect. The model applies these values to the system constraints when optimizing the schedule.

UAS-ST takes a different approach from ASC-U when addressing the optimization of payloads. In ASC-U all possible combination of payloads are enumerated and then designated as mission packages. UAS-ST treats the payloads as individual units, which allows for tracking of specific payload utilization. OAD indicated this was necessary for determining future requirements. The payload data is further separated by creating a mission class worksheet and a payload worksheet. The mission class worksheet defines all current missions for the UAS. It allows the user to designate a mission as either active or passive and which tier is capable of covering that mission. The payload worksheet allows the user to designate the quantity available.

A major difference between the two models is in the handling of the mission data. In UAS-ST all information is consolidated, both input and output, in the same worksheet. The user builds the missions page in the same manner as a flight schedule and assigns a specific number to an individual mission. UAS-ST sorts all output based on mission number, which makes for easy tracking of a specific mission. ASC-U uses either the mission number or the coordinates of the mission location to sort output. This makes analysis of results extremely time consuming and requires additional sorting. ASC-U requires the use of a heuristic, SUPER MISSIONS, to designate a mission as mandatory by assigning it extra value. UAS-ST addresses this in the mission input page by allowing the user to designate any portion of a mission request as required. Setting this requirement serves as an additional constraint on the optimization model.

ASC-U utilizes an Excel spreadsheet and pulls the data into an Access database. UAS-ST applies an Excel spreadsheet, which uses Visual Basic to transfer the data to GAMS. GAMS then applies the CPLEX solver to quickly optimize the schedule for the mission requests it is given. The required features addressed by the supplemental
heuristics in ASC-U are incorporated directly into UAS-ST to eliminate the need for further processing. This allows for a much quicker and efficient analysis of alternatives. CPLEX is highly efficient in preprocessing the feasible solutions and reduces the run time to a matter of minutes. Overall, UAS-ST provides an efficient update to ASC-U.
V. CONCLUSIONS AND NEW OPPORTUNITIES

A. SUMMARY

This thesis develops a scheduling tool, UAS-ST as a replacement for ASC-U. UAS-ST addresses several areas which require additional processing in ASC-U. UAS-ST allows a user to generate a daily flight based on a given set of operational and performance parameters. The true strength of UAS-ST is that a user can change a single parameter or some combination of parameters and quickly rerun the model to see the effect on a flight schedule. UASs are critical to our nation’s future combat effectiveness. As a result, all branches of DoD recognize the need to develop an integrated network of UASs. MCCDC OAD is currently conducting an OUAS study with the goal of defining future UAS requirements. This thesis is a direct contribution to that study, and the model developed herein, provides a planning tool for the development of future UAS structure.

B. OPERATIONAL INTRODUCTION

UAS-ST is currently intended for use in the second phase of the OUAS study. It will replace ASC-U and provide another tool for quantitative analysis. UAS-ST provides new capabilities which ASC-U was unable to perform. With the use of the CPLEX solver in GAMS, UAS-ST is able to quickly analyze tens of thousands of schedules for individual UAVs and then choose a near-optimal subset to provide a complete schedule. The user is able to modify all aspects of the UAS structure through a simple spreadsheet interface. Output is provided in the same format, which makes understanding the results and error tracking much simpler. ASC-U requires the use of several heuristics to meet the needs of OUAS. UAS-ST directly addresses these issues without the need for additional heuristics. UAS-ST provides a rapid analysis tool and should be implemented immediately in the ongoing OUAS study.
C. FUTURE DEVELOPMENT

UAS development is expanding rapidly with several new technologies becoming available. Therefore, modeling requirements are expected to change rapidly as well. A possible issue with UAS-ST is the requirement for the GAMS CPLEX solver to produce a quick solution. Due to portability issues, the future development of a non-proprietary heuristic is a valuable topic for future analysis. To improve on UAS-ST, the heuristic needs to modify the enumeration routine used in the model. Rather than a total enumeration of all possible schedules, a new heuristic should initially select higher value routes and not consider low value routes beneath a designated limit. One possible method is a greedy heuristic which selects the highest value subset of individual schedules and eliminate all others from consideration. By initially eliminating low value routes, the overall processing time is greatly reduced. In the long term, analysts in theater may run UAS-ST on their laptops as they plan for actual UAS employment. The ultimate goal is to find a near-optimal solution without the need for specialty software applications.


APPENDIX A TEST SCENARIO

Tier I  Mission Areas (m1-m40)
Tier II Mission Areas (m41-m103)
Tier III Mission Areas (m104-150)

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APPENDIX B VBA CODE

Sub SolveUAS()
    Dim bSolveResult As Boolean
    bSolveResult = SolveProblem(True)
End Sub

Sub BuildData()
    Dim uasDataFN As Integer
    Dim uasSetsFN As Integer
    Dim uasDynSetsFN As Integer
    Dim logFN As Integer
    Dim rTiers As Range
    Dim rGCSs As Range
    Dim rLRSs As Range
    Dim rUAVs As Range
    Dim rMissions As Range
    Dim rPayloads As Range
    Dim rSchedules As Range
    Dim rClasses As Range
    Dim lNumTiers As Long, lNumGCSs As Long, lNumLRSs As Long, lNumUAVs As Long
    Dim lNumMissions As Long, lNumPayloads As Long, lNumClasses As Long
    Dim lNumSchedules As Long
    Dim lNumLRSSchedules As Long
    Dim bNextRoute As Boolean

    Dim rValues As Range
    Dim lNumValues As Long
    Dim rDependencies As Range
    Dim lPlanPeriods As Long
    Dim lFirstPeriod As Long
    Dim lLastPeriod As Long
    Dim lPeriodsPerHour As Long

    Dim lCount As Long
    Dim currCell As Range
    Dim iRow As Integer, iCol As Integer
    Dim lMission As Long, lMission2 As Long, lUAV As Long
Dim lPeriod As Long, lPeriod1 As Long, lPeriod2 As Long
Dim lTier As Long, lPayload As Long, lGCS As Long, lLRS As Long
Dim lClass As Long

Dim tierNames As StringDictionaryClass
Dim uavNames As StringDictionaryClass
Dim gcsNames As StringDictionaryClass
Dim lrsNames As StringDictionaryClass
Dim missionNames As StringDictionaryClass
Dim payloadNames As StringDictionaryClass
Dim classNames As StringDictionaryClass
Dim periodNames As StringDictionaryClass
Dim tValues As TupleDictionaryClass

uasDataFN = FreeFile()
Open ThisWorkbook.path & "\uasData.gms" For Output As uasDataFN
uasSetsFN = FreeFile()
Open ThisWorkbook.path & "\uasSets.gms" For Output As uasSetsFN
logFN = FreeFile()
Open ThisWorkbook.path & "\uasXL.log" For Output As logFN

' {STATIC, GROUNDED} SETS
'   v             Tier levels
'   h             mission types {active, passive}
'   g             Ground control stations
'   l             Launch and recovery sites
'   m             Missions {missions that ships can be assigned}
'   t             Time periods
'   p             Payload module types
'   s             UAV employment schedules
'

Print #logFN, "Starting output"
Print #uasSetsFN, " OPTIONS"
Print #uasSetsFN, " MIP = " & wsDashboard.Range("SOLVER")
Print #uasSetsFN, " OPTCR = " & wsDashboard.Range("OPTCR")
Print #uasSetsFN, " RESLIM = " & wsDashboard.Range("RESLIM")
Print #uasSetsFN, " ;"
Print #uasSetsFN, " SETS"
Set rTiers = wsTiers.Range("A4", wsTiers.Range("A4").End(xlDown))
call GAMSWriteSetDef(rTiers, "v", uasSetsFN, "Tier levels")
Set rUAVs = wsUAV.Range("A4", wsUAV.Range("A4").End(xlDown))
Print #uasSetsFN, "   h /
Print #uasSetsFN, "     h_active"
Print #uasSetsFN, "     h_passive"
Print #uasSetsFN, "/"
Set rGCSs = wsGCS.Range("A4", wsGCS.Range("A4").End(xlDown))
call GAMSWriteSetDef(rGCSs, "g", uasSetsFN, "Ground control stations")
Set rLRSs = wsLRS.Range("A4", wsLRS.Range("A4").End(xlDown))
call GAMSWriteSetDef(rLRSs, "l", uasSetsFN, "Launch and recovery sites")
Set rMissions = wsMissions.Range("A4", wsMissions.Range("A4").End(xlDown))
call GAMSWriteSetDef(rMissions, "m", uasSetsFN, "Missions")
Set rPayloads = wsPayloads.Range("A4", wsPayloads.Range("A4").End(xlDown))
call GAMSWriteSetDef(rPayloads, "p", uasSetsFN, "Payloads")
Set rClasses = wsMClasses.Range("A4", wsMClasses.Range("A4").End(xlDown))
call GAMSWriteSetDef(rClasses, "c", uasSetsFN, "Payload Classes")
lPeriodsPerHour = CLng(wsDashboard.Range("PERIODS_PER_HOUR"))
lPlanPeriods = CLng(wsDashboard.Range("HORIZON"))
lFirstPeriod = CLng(wsDashboard.Range("FIRST_PERIOD"))
lLastPeriod = CLng(wsDashboard.Range("LAST_PERIOD"))
If lLastPeriod > lPlanPeriods Then
    MsgBox "Last Period comes after maximum planning horizon: truncating."
    lLastPeriod = lPlanPeriods
End If
If lFirstPeriod > lLastPeriod Then
    MsgBox "Empty planning horizon: first Period occurs after last Period. Aborting."
    GoTo subExit
End If
Print #logFN, "Periods " & lPlanPeriods & " First: " & lFirstPeriod & 
" Last: " & lLastPeriod
Print #uasSetsFN, "   t Time Periods /t_" & Format(lFirstPeriod) & 
"*t_" & Format(lLastPeriod) & "/"
Set tierNames = New StringDictionaryClass
If DefineGroundedSet(rTiers, tierNames) = False Then
    Print #logFN, "Duplicate element in grounded set (tiers). User chose to cancel: no further output."
    GoTo subExit
End If
lNumTiers = tierNames.Count

For lCount = 1 To lNumTiers
    Print #logFN, Format(lCount) & " : " & tierNames.Item(lCount)
Next lCount

Set uavNames = New StringDictionaryClass
If DefineGroundedSet(rUAVs, uavNames) = False Then
    Print #logFN, "Duplicate element in grounded set (uavs). User chose to cancel: no further output."
    GoTo subExit
End If
lNumUAVs = uavNames.Count

For lCount = 1 To lNumUAVs
    Print #logFN, Format(lCount) & " : " & uavNames.Item(lCount)
Next lCount

Set missionNames = New StringDictionaryClass
If DefineGroundedSet(rMissions, missionNames) = False Then
    Print #logFN, "Duplicate element in grounded set (missions). User chose to cancel: no further output."
    GoTo subExit
End If
lNumMissions = missionNames.Count

For lCount = 1 To lNumMissions
    Print #logFN, Format(lCount) & " : " & missionNames.Item(lCount)
Next lCount

Set payloadNames = New StringDictionaryClass
If DefineGroundedSet(rPayloads, payloadNames) = False Then
    Print #logFN, "Duplicate element in grounded set (payloads). User chose to cancel: no further output."
End If
GoTo subExit
End If
lNumPayloads = payloadNames.Count

For lCount = 1 To lNumPayloads
  Print #logFN, Format(lCount) & ": " & payloadNames.Item(lCount)
Next lCount

Set classNames = New StringDictionaryClass
If DefineGroundedSet(rClasses, classNames) = False Then
  Print #logFN, "Duplicate element in grounded set (classes). User chose to cancel: no further output."
  GoTo subExit
End If
lNumClasses = classNames.Count

For lCount = 1 To lNumPayloads
  Print #logFN, Format(lCount) & ": " & payloadNames.Item(lCount)
Next lCount

Set gcsNames = New StringDictionaryClass
If DefineGroundedSet(rGCSs, gcsNames) = False Then
  Print #logFN, "Duplicate element in grounded set (GCS). User chose to cancel: no further output."
  GoTo subExit
End If
lNumGCSs = gcsNames.Count

For lCount = 1 To lNumGCSs
  Print #logFN, Format(lCount) & " : " & gcsNames.Item(lCount)
Next lCount

Set lrsNames = New StringDictionaryClass
If DefineGroundedSet(rLRSs, lrsNames) = False Then
  Print #logFN, "Duplicate element in grounded set (LRS). User chose to cancel: no further output."
  GoTo subExit
End If
lNumLRSs = lrsNames.Count
For lCount = 1 To lNumLRSs
    Print #logFN, Format(lCount) & " : " & lrsNames.Item(lCount)
Next lCount

Set periodNames = New StringDictionaryClass
periodNames.Size = 3 * lPlanPeriods
For lCount = 1 To lPlanPeriods
    periodNames.Add "t" & Format(lCount)
Next lCount

For lCount = lFirstPeriod To lLastPeriod
    Print #logFN, Format(lCount) & " : " & periodNames.Item(lCount)
Next lCount

' {GIVEN} PARAMETERS
'   num_uavs(l,v,t) number of uavs available at lrs l in tier v in period t
'   num_mods(p,t)   number of payload modules available of ID p in period t
'   gcs_cap(g,t,h)  max num UAVs on gcs g in period t on mission type h
'   lrs_cap(l,t)    max num UAVs at LRS l in period t
'   length(m)       maximum periods of coverage of mission m
'   val(m)          value of mission m
'   k(l,s,t)        indicator if lrs l used by schedule s in period t
';

Print #uasDataFN, " PARAMETERS"
'   num_uavs(l,v,t) number of uavs available at lrs l in tier v in period t
Print #uasDataFN, "   num_uavs(l,v,t) /
ReDim lNumUAVinPeriod(1 To lrsNames.Count, 1 To tierNames.Count, lFirstPeriod To lLastPeriod) As Long
For lPeriod = lFirstPeriod To lLastPeriod
    For lLRS = 1 To lrsNames.Count
        For lTier = 1 To tierNames.Count
            lNumUAVinPeriod(lLRS, lTier, lPeriod) = 0
        Next lTier
    Next lLRS
    For iRow = 1 To rUAVs.Rows.Count
        If rUAVs(iRow, COL_UAV_FIRST_AVAIL) <= lPeriod And rUAVs(iRow, COL_UAV_LAST_AVAIL) >= lPeriod Then
lLRS = lrsNames.Lookup(rUAVs(iRow, COL_UAV_LRS))
lTier = tierNames.Lookup(rUAVs(iRow, COL_UAV_TIER))
If lLRS = 0 Then
    MsgBox "Error: invalid LRS name in UAV list"
    wsUAV.Activate
    rUAVs(iRow, COL_UAV_LRS).Select
    GoTo subExit
ElseIf lTier = 0 Then
    MsgBox "Error: invalid tier name in UAV list"
    wsUAV.Activate
    rUAVs(iRow, COL_UAV_TIER).Select
    GoTo subExit
Else
    lNumUAVinPeriod(lLRS, lTier, lPeriod) = lNumUAVinPeriod(lLRS, lTier, lPeriod) + 1
End If
End If
Next iRow
Next lPeriod

For lLRS = 1 To lrsNames.Count
    For lTier = 1 To lNumTiers
        For lPeriod = lFirstPeriod To lLastPeriod
            If lNumUAVinPeriod(lLRS, lTier, lPeriod) >= 1 Then
                Print #uasDataFN, "     l_{" & lrsNames.Item(lLRS) & ".v_" &
                        tierNames.Item(lTier) & ".t_" & lPeriod & "}" & _
                lNumUAVinPeriod(lLRS, lTier, lPeriod)
            End If
        Next lPeriod
    Next lTier
Next lLRS
Print #uasDataFN, "   /"

ReDim numMods(classNames.Count, tierNames.Count) As Long
For lPayload = 1 To rPayloads.Rows.Count
    iRow = classNames.Lookup(rPayloads(lPayload, COL_PAYLOAD_CLASS))
    iCol = tierNames.Lookup(rPayloads(lPayload, COL_PAYLOAD_TIER))
    numMods(iRow, iCol) = numMods(iRow, iCol) + rPayloads(lPayload, COL_PAYLOAD_QUANTITY)
Next lPayload
num_mods(c,v) number of payload modules available of class c for
tier v

Print #uasDataFN, " num_mods(c,v) /

For lClass = 1 To classNames.Count
    For lTier = 1 To tierNames.Count
        Print #uasDataFN, "c_" & classNames.Item(lClass) & ".v_" &
tierNames.Item(lTier) & " " & numMods(lClass, lTier)
    Next lTier
Next lClass
Print #uasDataFN, " /"

gcs_cap(g,t,h) max num UAVs on gcs g in period t on mission type h

Print #uasDataFN, " gcs_cap(g,t,h) /

For lGCS = 1 To lNumGCSs
    For lPeriod = lFirstPeriod To lLastPeriod
        Print #uasDataFN, " g_" & gcsNames.Item(lGCS) & ".t_" & lPeriod & ".h_active " & rGCSs(lGCS, COL_GCS_ACTIVE)
        Print #uasDataFN, " g_" & gcsNames.Item(lGCS) & ".t_" & lPeriod & ".h_passive " & rGCSs(lGCS, COL_GCS_PASSIVE)
    Next lPeriod
Next lGCS
Print #uasDataFN, " /"

lrs_cap(l,t) max num UAVs at LRS l in period t

Print #uasDataFN, " lrs_cap(l,t) /

For lLRS = 1 To lNumLRSSs
    For lPeriod = lFirstPeriod To lLastPeriod
        Print #uasDataFN, " l_" & lrsNames.Item(lLRS) & ".t_" & lPeriod & ".lrs_active " & rLRSSs(lLRS, COL_LRS_ACTIVE)
    Next lPeriod
Next lLRS
Print #uasDataFN, " /

length(m) maximum periods of coverage of mission m

Print #uasDataFN, " length(m) /

For lMission = 1 To lNumMissions
    Print #uasDataFN, " m_" & missionNames.Item(lMission) & " " & rMissions(lMission, COL_MISSION_PERIODS)
Next lMission
Print #uasDataFN, " /"
' val(m)          value of mission m
Print #uasDataFN, "   val(m) /"
For lMission = 1 To lNumMissions
    Print #uasDataFN, "     m_ & missionNames.Item(lMission) & " & rMissions(lMission, COL_MISSION_VALUE)
Next lMission
Print #uasDataFN, " /"

' Calculate distances between GCS-Mission pairs, LRS-mission pairs, and mission-mission pairs
ReDim dDistGM(lNumGCSs, lNumMissions) As Double
ReDim dDistLM(lNumLRSs, lNumMissions) As Double
ReDim dDistMM(lNumMissions, lNumMissions) As Double
Dim i As Long, j As Long

For lGCS = 1 To rGCSs.Rows.Count
    i = gcsNames.Lookup(rGCSs(lGCS, COL_GCS_NAME))
    For lMission = 1 To rMissions.Rows.Count
        j = missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))
        dDistGM(i, j) = SphericalDistance(rGCSs(lGCS, COL_GCS_LAT),
                                           rGCSs(lGCS, COL_GCS_LON),
                                           rMissions(lMission, COL_MISSION_LAT), rMissions(lMission, COL_MISSION_LON))
    Next lMission
Next lGCS

For lLRS = 1 To rLRSs.Rows.Count
    i = lrsNames.Lookup(rLRSs(lLRS, COL_LRS_NAME))
    For lMission = 1 To rMissions.Rows.Count
        j = missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))
        dDistLM(i, j) = SphericalDistance(rLRSs(lLRS, COL_LRS_LAT),
                                           rLRSs(lLRS, COL_LRS_LON),
                                           rMissions(lMission, COL_MISSION_LAT), rMissions(lMission, COL_MISSION_LON))
    Next lMission
Next lLRS

For lMission = 1 To rMissions.Rows.Count
    i = missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))
    For lMission2 = 1 To rMissions.Rows.Count
\[
j = \text{missionNames.Lookup(rMissions(lMission2, COL\_MISSION\_NAME))}
\]
\[
dDistMM(i, j) = \text{SphericalDistance(rMissions(lMission, COL\_MISSION\_LAT), rMissions(lMission, COL\_MISSION\_LON),}
\]
\[
rMissions(lMission2, COL\_MISSION\_LAT), rMissions(lMission2, COL\_MISSION\_LON))
\]
\[
\text{Next lMission2}
\]
\[
\text{Next lMission}
\]

'Find GCSs within range of each mission. If none, require one of the AV\_CLR missions

Dim pFN As Integer, hpFN As Integer
Dim numPreq As Long
numPreq = 0
pFN = FreeFile()
Open "p.gms" For Output As pFN
hpFN = FreeFile()
Open "hp.gms" For Output As hpFN
Print #pFN, " SET P(m,mp) /
Print #hpFN, " SET HP(m) /
For lMission = 1 To missionNames.Count
    For lGCS = 1 To gcsNames.Count
        If dDistGM(lGCS, lMission) <= rGCSs(lGCS, COL\_GCS\_LOS) Then GoTo nextMissionGCS
    Next lGCS
    numPreq = numPreq + 1
    For lMission2 = 1 To rMissions.Rows.Count
        If rMissions(lMission2, COL\_MISSION\_CLASS) = wsGCS.Range("LINK").Value Then
            Print #pFN, " m_" & missionNames.Item(lMission) & ".m_" & rMissions(lMission2, COL\_MISSION\_NAME)
        End If
    Next lMission2
nextMissionGCS:
    Next lMission
    If numPreq = 0 Then
        Print #pFN, " m_ " & missionNames.Item(1) & ".m_ " & missionNames.Item(1)
        Print #hpFN, " m_ " & missionNames.Item(1)
    End If
Print #pFN, " /"
Print #pFN, ";"
Close pFN
Print #hpFN, " /"
Print #hpFN, " ;"
Close hpFN

Dim mgFN As Integer
mgFN = FreeFile()
Open "mg.gms" For Output As mgFN
Print #mgFN, " SET mg(m,g) /
For lMission = 1 To missionNames.Count
For iRow = 1 To rGCSs.Rows.Count
lGCS = gcsNames.Lookup(rGCSs(iRow, COL_GCS_NAME))
If dDistGM(lGCS, lMission) <= rGCSs(iRow, COL_GCS_LOS) Then
Print #mgFN, " m_" & missionNames.Item(lMission) & ".g_" & gcsNames.Item(lGCS)
End If
Next iRow
Next lMission
Print #mgFN, " /;"
Close mgFN

Dim mhFN As Integer
mhFN = FreeFile()
Open "mh.gms" For Output As mgFN
ReDim bClassActive(classNames.Count) As Boolean
For iRow = 1 To rClasses.Rows.Count
lClass = classNames.Lookup(rClasses(iRow, COL_MCLASS_NAME))
If CLng(rClasses(iRow, COL_MCLASS_ACTIVE)) = 1 Then
bClassActive(lClass) = True
Else
bClassActive(lClass) = False
End If
Next iRow
Print #mhFN, " SET mh(m,h) /
For iRow = 1 To rMissions.Rows.Count
lClass = classNames.Lookup(rMissions(iRow, COL_MISSION_CLASS))
If bClassActive(lClass) Then
Print #mhFN, "   m_" & rMissions(iRow, COL_MISSION_NAME) & ".h_active"
Else
Print #mhFN, "   m_" & rMissions(iRow, COL_MISSION_NAME) & ".h_passive"
End If
Next iRow
Print #mhFN, "/;"
Close mhFN

Dim gvFN As Integer
gvFN = FreeFile()
Open "gv.gms" For Output As mgFN
Print #gvFN, " SET GV(g,v) /"
For iRow = 1 To rGCSs.Rows.Count
lGCS = gcsNames.Lookup(rGCSs(iRow, COL_GCS_NAME))
lTier = tierNames.Lookup(rGCSs(iRow, COL_GCS_TIER))
Print #gvFN, "   g_" & gcsNames.Item(lGCS) & ".v_" & tierNames.Item(lTier)
Next iRow
Print #gvFN, "/;"
Close gvFN

Print #uasDataFN, " r(m) /
For iRow = 1 To rMissions.Rows.Count
lMission = missionNames.Lookup(rMissions(iRow, COL_MISSION_NAME))
If Trim(CStr(rMissions(iRow, COL_MISSION_REQUIRED))) <> "" Then
If CLng(rMissions(iRow, COL_MISSION_REQUIRED)) > CLng(rMissions(iRow, COL_MISSION_PERIODS)) Then
If MsgBox("Required coverage exceeds total mission time", vbOKCancel) = vbCancel Then
wsMissions.Activate
rMissions(iRow, COL_MISSION_REQUIRED).Select
Exit Sub
Else
Print #uasDataFN, "   m_" & missionNames.Item(lMission) & " " & CLng(rMissions(iRow, COL_MISSION_REQUIRED))
End If
Else
Print #uasDataFN, "   m_" & missionNames.Item(lMission) & " " & CLng(rMissions(iRow, COL_MISSION_PERIODS))
End If
End If
Else
    Print #uasDataFN, "   m_" & missionNames.Item(lMission) & "   0"
End If
Next iRow
Print #uasDataFN, " /"

' Count number of UAVs in each tier at each LRS
ReDim tierAtLRS(tierNames.Count, lrsNames.Count) As Long
For lLRS = 1 To lrsNames.Count
    For lTier = 1 To tierNames.Count
        tierAtLRS(lTier, lLRS) = 0
    Next lTier
Next lLRS

For lUAV = 1 To rUAVs.Rows.Count
    i = tierNames.Lookup(rUAVs(lUAV, COL_UAV_TIER))
    j = lrsNames.Lookup(rUAVs(lUAV, COL_UAV_LRS))
    tierAtLRS(i, j) = tierAtLRS(i, j) + 1
Next lUAV

' a(m,s,t)  indicator if mission m covered by schedule s in period t
' b(v,s,t)  indicator if UAV in Tier v required by schedule s in period t
' f(g,s,t,h) indicator if gcs g used by schedule s in period t for mission type h
' k(l,s,t)  indicator if lrs l used by schedule s in period t
' q(p,s,t)  indicator if payload p used by schedule s in period t

Dim lMaxRoutes As Long
lMaxRoutes = CLng(wsDashboard.Range("MAX_ROUTES"))

Dim lMaxMissions As Long
lMaxMissions = CLng(wsDashboard.Range("MAX_MISSIONS")) + 1

ReDim a(lMaxRoutes, wsDashboard.Range("LAST_PERIOD")) As Long
ReDim b(lMaxRoutes) As Long
ReDim f_act(lMaxRoutes, wsDashboard.Range("LAST_PERIOD")) As Long
ReDim f_pas(lMaxRoutes, wsDashboard.Range("LAST_PERIOD")) As Long
ReDim k(lMaxRoutes, wsDashboard.Range("LAST_PERIOD")) As Long
ReDim q(lMaxRoutes, wsDashboard.Range("LAST_PERIOD")) As Long
ReDim q(lMaxRoutes, classNames.Count) As Long

ReDim stack(lMaxMissions + 1) As Long
ReDim onStack(lNumMissions) As Long
ReDim dwell(lMaxMissions + 1) As Long

For lMission = 1 To lNumMissions
    onStack(lMission) = 0
Next lMission

Dim top As Long
    top = 0

lNumSchedules = 0
lNumLRSschedules = 0
bNextRoute = True
lLRS = 1
Dim s As Long, t As Long
Dim lNextMission As Long, lCurrMission As Long
ReDim lNextStack(lMaxMissions + 1) As Long
Dim dRemTime As Double
Dim lRemPeriods As Long
Dim dTransitTime As Double
Dim lTransitPeriods As Long
Dim lcurrNumClasses As Long
Dim dTierSpeed As Double
Dim lThisLaunchPeriod As Long
Dim lThisRecoverPeriod As Long
Dim lMaxClasses As Long
ReDim lTransitPeriod(lMaxMissions + 1) As Long
ReDim lIdlePeriod(lMaxMissions + 1) As Long
ReDim lMissionPeriod(lMaxMissions + 1) As Long
ReDim lStartPeriod(lNumMissions) As Long
ReDim lFinishPeriod(lNumMissions) As Long
For lMission = 1 To rMissions.Rows.Count
    lStartPeriod(missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))) = CLng(rMissions(lMission, COL_MISSION_START_PERIOD))
    lFinishPeriod(missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))) = CLng(rMissions(lMission, COL_MISSION_FINISH_PERIOD))
Next lMission
ReDim dMissionValue(missionNames.Count) As Double
For lMission = 1 To rMissions.Rows.Count
  dMissionValue(missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))) = CDbl(rMissions(lMission, COL_MISSION_VALUE))
Next lMission
ReDim lHasClass(lNumClasses) As Long
For lClass = 1 To lNumClasses
  lHasClass(lClass) = 0
Next lClass
lcurrNumClasses = 0
ReDim reqClass(lNumMissions)
For lMission = 1 To rMissions.Rows.Count
  reqClass(missionNames.Lookup(rMissions(lMission, COL_MISSION_NAME))) = 
    classNames.Lookup(rMissions(lMission, COL_MISSION_CLASS))
Next lMission
ReDim lClassTierAvail(classNames.Count, tierNames.Count) As Long
For lClass = 1 To classNames.Count
  For lTier = 1 To tierNames.Count
    lClassTierAvail(lClass, lTier) = 0
  Next lTier
Next lClass
For lPayload = 1 To rPayloads.Rows.Count
  lClass = classNames.Lookup(rPayloads(lPayload, COL_PAYLOAD_CLASS))
  lTier = tierNames.Lookup(rPayloads(lPayload, COL_PAYLOAD_TIER))
  lClassTierAvail(lClass, lTier) = CLng(rPayloads(lPayload, COL_PAYLOAD_QUANTITY))
Next lPayload
Dim aFN As Integer, bFN As Integer, fFN As Integer, kFN As Integer, qFN As Integer
aFN = FreeFile()
Open ThisWorkbook.path & "\a.gms" For Output As aFN
bFN = FreeFile()
Open ThisWorkbook.path & "\b.gms" For Output As bFN
kFN = FreeFile()
Open ThisWorkbook.path & "\k.gms" For Output As kFN
qFN = FreeFile()
Open ThisWorkbook.path & "\q.gms" For Output As qFN
s = 0
Print #aFN, "  SET A(s,m,t) /"
Print #bFN, " SET B(s,v,t) /
Print #qFN, " SET Q(s,c,t) /

Dim tierLRScombos As Long
tierLRScombos = 0
For lTier = 1 To tierNames.Count    
   For lLRS = 1 To lrsNames.Count
      If tierAtLRS(lTier, lLRS) Then
         tierLRScombos = tierLRScombos + 1
      End If
   Next lLRS
Next lTier
Dim currCombo As Long
currCombo = 1
For lLRS = 1 To rLRSs.Rows.Count
   Print #logFN, "LRS " & rLRSs(lLRS, COL_LRS_NAME) & ":" & lrsNames.Lookup(rLRSs(lLRS, COL_LRS_NAME))
   For lTier = 1 To rTiers.Rows.Count
      Print #logFN, " tier " & rTiers(lTier, COL_TIER_NAME) & ":" & tierNames.Lookup(rTiers(lTier, COL_TIER_NAME))
      If tierAtLRS(tierNames.Lookup(rTiers(lTier, COL_TIER_NAME)), lrsNames.Lookup(rLRSs(lLRS, COL_LRS_NAME))) > 0 Then
         dTierSpeed = rTiers(lTier, COL_TIER_SPEED)
         dRemTime = rTiers(lTier, COL_TIER_ENDURANCE) ' * rTiers(lTier, COL_TIER_SPEED)
         lRemPeriods = Ceiling(dRemTime * lPeriodsPerHour)
         lMaxClasses = rTiers(lTier, COL_TIER_CAPACITY)
         Print #logFN, " tierAtLRS? yes lMaxClasses=" & lMaxClasses
         For lClass = 1 To lNumClasses
            lHasClass(lClass) = 0
         Next lClass
         lcurrNumClasses = 0
         top = 1
         stack(top) = EVENT_LR 'L/R event at lLRS
         lNextStack(top) = 1
         Do
            lCurrMission = stack(top)
            lNextMission = lNextStack(top)
            'Find next mission to put on the stack
            If lNextMission < lNumClasses Then
               stack(top) = lNextMission
            Else
               lNextMission = 1
               top = top + 1
               stack(top) = lNextMission
            End If
         Loop While lNextMission < lNumClasses
      End If
   Next lTier
Next lLRS
lcurrNumClasses = 0
Do While lNextMission <= lNumMissions
    If onStack(lNextMission) > 0 Then
        'Print #logFN, " onstack"
        GoTo skipMission
    End If
    If dDistLM(lLRS, lNextMission) > rTiers(lTier, COL_TIER_RADIUS) Then
        'Print #logFN, "Out of range"
        GoTo skipMission
    End If
    If lClassTierAvail(reqClass(lNextMission), lTier) = 0 Then
        'Print #logFN, "No Payloads available for this Tier"
        GoTo skipMission
    End If
    If lCurrMission = EVENT_LR Then
        dTransitTime = dDistLM(lLRS, lNextMission) / dTierSpeed
    Else
        dTransitTime = dDistMM(lCurrMission, lNextMission) / dTierSpeed
    End If
    lTransitPeriods = Ceiling(dTransitTime * lPeriodsPerHour)
    If lCurrMission <= 0 Then
        If lFinishPeriod(lNextMission) <= lStartPeriod(lCurrMission) + lTransitPeriods Then
            'Print #logFN, " time warp"
            GoTo skipMission
        End If
    ElseIf dMissionValue(lNextMission) <= dMissionValue(lCurrMission) Then
        If lFinishPeriod(lNextMission) <= lFinishPeriod(lCurrMission) + lTransitPeriods Then
            'Print #logFN, " time warp"
            GoTo skipMission
        End If
    Else
        If lStartPeriod(lNextMission) <= lStartPeriod(lCurrMission) + lTransitPeriods Then
            'Print #logFN, " time-value warp"
            GoTo skipMission
        End If
    End If
End If
If lTransitPeriods + Ceiling(lPeriodsPerHour * (dDistLM(lLRS, lNextMission) / rTiers(lTier, COL_TIER_SPEED))) > lRemPeriods Then
  'Print #logFN, " out of time"
  GoTo skipMission
End If
If (lcurrNumClasses = lMaxClasses And lHasClass(reqClass(lNextMission)) = 0) Then
  'Print #logFN, " no payload space left"
  GoTo skipMission
End If
GoTo foundMission
skipMission:
lNextMission = lNextMission + 1
Loop
foundMission:
If lNextMission > lNumMissions Or top >= lMaxMissions Then 'out of missions: pop stack
  If lCurrMission > 0 Then
    lHasClass(reqClass(lCurrMission)) = lHasClass(reqClass(lCurrMission)) - 1
    If lHasClass(reqClass(lCurrMission)) = 0 Then
      lcurrNumClasses = lcurrNumClasses - 1
    End If
    onStack(lCurrMission) = 0
  End If
  top = top - 1
  GoTo nextMission
End If
If lCurrMission = EVENT_LR Then
  lTransitPeriod(top) = lTransitPeriods
  lThisLaunchPeriod = lStartPeriod(lNextMission) - lTransitPeriod(top) - 1
  If lThisLaunchPeriod < 1 Then
    lThisLaunchPeriod = 1
  End If
  lRemPeriods = Ceiling(dRemTime * lPeriodsPerHour) + lThisLaunchPeriod - 1
  lTransitPeriod(top) = lThisLaunchPeriod + lTransitPeriods
  lIdlePeriod(top) = lThisLaunchPeriod - 1
Else
  lMissionPeriod(top) = lFinishPeriod(lCurrMission)
If \( dMissionValue(l\text{CurrMission}) < dMissionValue(l\text{NextMission}) \) And \\
\( lStartPeriod(l\text{NextMission}) - lTransitPeriods - 1 < lFinishPeriod(l\text{CurrMission}) \) Then \\
lMissionPeriod(top) = lStartPeriod(l\text{NextMission}) - lTransitPeriods - 1 \\
End If \\
End If \\
lNextStack(top) = lNextMission + 1 \\
top = top + 1 \\
stack(top) = lNextMission \\
onStack(l\text{NextMission}) = top \\
lMissionPeriod(top) = lFinishPeriod(l\text{NextMission}) \\
lTransitPeriod(top) = lFinishPeriod(top) + Ceiling((dDistLM(lLRS, l\text{NextMission}) / rTiers(l\text{Tier}, COL\_TIER\_SPEED}) * lPeriodsPerHour) \\
lNextStack(top) = 1 \\
If lHasClass(reqClass(l\text{NextMission})) = 0 Then \\
lcurrNumClasses = lcurrNumClasses + 1 \\
End If \\
lHasClass(reqClass(l\text{NextMission})) = lHasClass(reqClass(l\text{NextMission})) + 1 \\

'New feasible schedule: now copy stack info into appropriate arrays \\
s = s + 1 \\
t = 1 \\
'calculate start period of mission sequence: find start time of first mission \\
' in stack(2), figure out latest departure period to arrive at first mission (if \\
' earlier than period 1, then l/r in period 1, transit, and do as much of mission \\
' as possible \\
Print \#logFN, "dTransitTime " & dTransitTime & " & lTransitPeriods " & lTransitPeriods \\
Print \#logFN, "s:" & CStr(s) & " "; \\
For iRow = 1 To top \\
    Print \#logFN, stack(iRow) & ","; \\
Next iRow \\
Print \#logFN, "0"
Print #logFN, "m:" & CStr(s) & " ";
For iRow = 1 To top
    Print #logFN, lMissionPeriod(iRow) & ",";
Next iRow
Print #logFN, "0"
Print #logFN, "t:" & CStr(s) & ";
For iRow = 1 To top
    Print #logFN, lTransitPeriod(iRow) & ",";
Next iRow
Print #logFN, "0"
Print #logFN, "i:" & CStr(s) & ";
For iRow = 1 To top
    Print #logFN, lIdlePeriod(iRow) & ",";
Next iRow
Print #logFN, "0"

Do While t < lThisLaunchPeriod And t <= lLastPeriod
    a(s, t) = EVENT_IDLE
    t = t + 1
Loop
a(s, t) = EVENT_LR
f_act(s, t) = 1
k(s, t) = 1LRS
    t = t + 1
Do While t <= lTransitPeriod(1) And t <= lLastPeriod
    a(s, t) = EVENT_TRANSIT
    f_pas(s, t) = 1
    t = t + 1
Loop
For iRow = 2 To top
    lCurrMission = stack(iRow)
    If iRow < top Then
        lNextMission = stack(iRow + 1)
    Else
        lNextMission = EVENT_LR 'L/R event
    End If
    ' XXX Need upper bounds: time horizon, flight time, etc...
    Do While t <= lMissionPeriod(iRow) And t <= lLastPeriod
        'fill in arrays
\(a(s, t) = l\text{CurrMission}\)
\(f_{\text{act}}(s, t) = 1\)
\(t = t + 1\)

Loop
Do While \(t \leq l\text{TransitPeriod}(iRow)\) And \(t \leq l\text{LastPeriod}\)
\(a(s, t) = \text{EVENT_TRANSIT}\)
\(f_{\text{pas}}(s, t) = 1\)
\(t = t + 1\)

Loop
Do While \(t \leq l\text{IdlePeriod}(iRow)\) And \(t \leq l\text{LastPeriod}\)
\(a(s, t) = \text{EVENT_IDLE}\)
\(f_{\text{pas}}(s, t) = 1\)
\(t = t + 1\)

Loop
Next iRow

If \(t \leq l\text{LastPeriod}\) Then
\(a(s, t) = \text{EVENT_LR}\)
\(l\text{ThisRecoverPeriod} = t\)
\(f_{\text{act}}(s, t) = 1\)
\(k(s, t) = l\text{LRS}\)
\(b(s) = l\text{Tier}\)

End If

For iRow = 1 To lLastPeriod
    Print \#logFN, ":" & a(s, iRow);
Next iRow

Print \#logFN, ""

For iRow = 2 To top
    For lPeriod = 1 To lLastPeriod
        If a(s, lPeriod) = stack(iRow) Then
            Print \#aFN, " s_" & CStr(s) & ".m_" & missionNames.Item(stack(iRow)) & ".t_" & CStr(lPeriod)
        End If
    Next lPeriod
    Next iRow

For lPeriod = 1 To lLastPeriod
    If lPeriod >= lThisLaunchPeriod And lPeriod <= lThisRecoverPeriod Then
        Print \#bFN, " s_" & CStr(s) & ".v_" & Trim(rTiers(lTier, COL_TIER_NAME)) & ".t_" & CStr(lPeriod)
    End If
Next lPeriod
Next iRow

End If
Next lPeriod
Print #kFN, " k('s" & CStr(s) & ",l_" & Trim(rLRSs(lLRS, COL_LRS_NAME)) & ",t_" & CStr(lThisLaunchPeriod) & ")=1;"
Print #kFN, " k('s" & CStr(s) & ",l_" & Trim(rLRSs(lLRS, COL_LRS_NAME)) & ",t_" & CStr(lThisRecoverPeriod) & ")=1;"
For lClass = 1 To classNames.Count
  If lHasClass(lClass) > 0 Then
    q(s, lClass) = 1
  For lPeriod = 1 To lLastPeriod
    If lPeriod >= lThisLaunchPeriod And lPeriod <= lThisRecoverPeriod Then
      Print #qFN, " s_" & CStr(s) & ".c_" & classNames.Item(lClass) & ".t_" & CStr(lPeriod)
    End If
  Next lPeriod
  End If
Next lClass
End If
Next lPeriod
Next lClass
If s >= lMaxRoutes Then GoTo doneMissions
If s Mod 1000 = 0 Then wsDashboard.Range("ROUTESCELL") = s
If s >= (currCombo - 1) * lMaxRoutes / (tierLRScombos) Then
  GoTo nextTier
nextMission:
  Loop While top > 0
End If
nextTier:
  currCombo = currCombo + 1
Next lTier
Next lLRS
doneMissions:
wsDashboard.Range("ROUTESCELL") = s
Print #uasSetsFN, " s /s_1*s_" & CStr(s) & "/"
Print #uasSetsFN, ";"
Print #uasDataFN, ";"
Print #aFN, ";"
Print #aFN, "/"
Print #bFN, ";"
Print #bFN, "/"
Print #qFN, ";"
Print #qFN, "/"
subExit:
  Print #logFN, "Ending output"
Close uasSetsFN
Close uasDataFN
Close aFN
Close bFN
Close kFN
Close qFN
Close logFN
End Sub
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APPENDIX C GAMS CODE

$TITLE UAS Planner 08.06.02

$context
MCCDC/OAD UAS Mission Planner
Assigns a fleet of UAVs to a list of missions with various requirements and time windows over a fixed time horizon of many time periods.
Solved using explicit column generation, one column per UAS schedule.
$offtext
$inlinecom { }
FILE UASP_log/UASP.log/ ;
PUT UASP_log ;
PUT 'UASP - MCCDC/OAD UAS Planner 08.06.02' // ;
PUTCLOSE UASP_log ;

FILE UASP_sta/UASP.sta/ ;
PUT UASP_sta ;
PUT 'ERROR - Did not solve' // ;
PUTCLOSE UASP_sta ;

FILE VALUE_CSV/VALUE.csv/ ;
PUT VALUE_CSV ;
PUT '' / ; { scratch legacy file contents }
PUTCLOSE VALUE_CSV ;

FILE MISSIONS_CSV/MISSIONS.csv/ ;
PUT MISSIONS_CSV ;
PUT '' / ; { scratch legacy file contents }
PUTCLOSE MISSIONS_CSV ;

65
FILE SCHEDULES_CSV/SCHEDULES.csv/ ;
PUT SCHEDULES_CSV ;
PUT '' / ; { scratch legacy file contents }
PUTCLOSE SCHEDULES_CSV

FILE DUALS_CSV/DUALS.csv/ ;
PUT DUALS_CSV ;
PUT '' / ; { scratch legacy file contents }
PUTCLOSE DUALS_CSV

PUT UASP_log ;
UASP_log.ap=1 ; { re-open log file, appending to prior contents }

OPTIONS
  optcr = 0.1
  limrow = 0
  limcol = 0
  SEED  = 1234
  ITERLIM = 10000000
  LP     = CPLEX
  RMIP   = CPLEX
  MIP    = CPLEX
;
$ONTEXT
{STATIC, GROUNDED} SETS
  v Tier levels
  h mission types {active, passive}
  g Ground control stations
  l Launch and recovery sites
  m Missions {missions that ships can be assigned}
  c Payload classes

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t  Time periods
s  UAV emplyment schedules
;
$OFFTEXT
$INCLUDE uasSets.gms

alias(m,mp);
$ONTEXT
{GIVEN} PARAMETERS
num_uavs(l,v,t)  number of uavs available in tier v in period t
num_mods(c,t)    number of payload modules available of class c in period t
gcs_cap(g,t,h)    max num UAVs on gcs g in period t on mission type h
lrs_cap(l,t)      max num UAVs at LRS l in period t
length(m)        maximum periods of coverage of mission m
val(m)           value of mission m
r(m)             required periods of coverage for mission m
k(s,l,t)         indicator if lrs l used by schedule s in period t
;

$OFFTEXT
$OFFLISTING
$INCLUDE uasData.gms

PARAMETER
k(s,l,t)
;
$INCLUDE k.gms

$ONTEXT
{DYNAMIC} SETS
A(s,m,t)    schedule s covers mission m in period t
B(s,v,t)    schedule s uses tier v UAV in period t
Q(s,c,t)    schedule s requires payload class c in period t

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P(m,mp)  mission prerequisite fixed mission m requires at least one
mission mp in same period
E(m,mp)  exclusive missions m and mp cannot be accomplished in same
period

;  
{Notional data: will be replaced with INCLUDE statements and accompanying
data files}

$OFFTEXT
alias(m,mp);
alias(v,vp);
alias(t,tp);
$INCLUDE a.gms
$INCLUDE b.gms
$INCLUDE q.gms
$INCLUDE hp.gms
$INCLUDE p.gms
$INCLUDE mg.gms
$INCLUDE mh.gms
$INCLUDE gv.gms
$ONLISTING

SET sl(s,l);
LOOP((s,l)$(SUM(t,k(s,l,t))>eps),
   sl(s,l) = yes;
);

SCALARS errors,warnings ;

errors=0 ;
warnings=0;
{Loops for data checking go here}
IF(errors>0,
   PUT / 'inconsistencies found in active and value data: ',errors:10:0 / ;
PUT 'should I have shut you down here?' ;

VARIABLE
  OBJECTIVE
  ;

BINARY VARIABLES
  X(s) Schedule s flown by some UAV
  Y(m,v,t) Mission m covered in period t
  W(m,v,g,t) Mission m handled by GCS g in period t
  ;

INTEGER VARIABLES
  D(m) Total number of dwell periods on mission m
  MODS(c,v,l)
  ;

EQUATIONS
  eqnObj {R0} Objective function measures total value of mission accomplishment
  UAVLimit(l,v,t) {R1} limit on UAVs flying by tier and period
  ModuleLimit(c,v,l,t) {R2} limit on payload modules flying by payload and period
  TotalMods(c,v) {R2.5}
  GCSLimit(g,t,h) {R3} limit on GCS use by gcs period and type
  LRSLimit(l,t) {R4} limit on LRS use by LRS and period
  CoverageLimit(m,v,t) {R5} mission and period coverage control
  DwellLimit(m) {R6} limit on total dwell time by mission
  Prerequisite(m,v,t) {R7} prerequisite controls by period
  Mission_Control(m,v,t)
  * Exclusive(m,mp,t) {R8} mutually exclusive missions by period
  RequiredDwell(m) {R9} required missions must be completely covered
  ;
eqnObj.. {R0}
  OBJECTIVE =e= sum(m, val(m)*D(m))
;
UAVLimit(l,v,t).. {R1}
  SUM(s$(B(s,v,t) and sl(s,l)), X(s)) =l= num_uavs(l,v,t)
;
ModuleLimit(c,v,l,t).. {R2}
  SUM(s$(sl(s,l) and B(s,v,t) and Q(s,c,t)), X(s)) =l= MODS(c,v,l)
;
TotalMods(c,v)..
  SUM(l, MODS(c,v,l)) =l= num_mods(c,v)
;
GCSLimit(g,t,h).. {R3}
  SUM((m,v)$(MG(m,g) and MH(m,h) and GV(g,v)), W(m,v,g,t)) =l=
    gcs_cap(g,t,h)
;
LRSLimit(l,t).. {R4}
  SUM(s$(k(s,l,t)>eps), X(s)) =l= lrs_cap(l,t)
;
CoverageLimit(m,v,t).. {R5}
  Y(m,v,t) =l= SUM(s$(A(s,m,t) and B(s,v,t)), X(s))
;
DwellLimit(m)..
  D(m) =l= SUM((v,t), Y(m,v,t))
;
Prerequisite(m,v,t)$HP(m)..
  Y(m,v,t) =l= SUM((mp,vp)$P(m,mp), Y(mp,vp,t))
;
Mission_Control(m,v,t)$(not HP(m))..
  Y(m,v,t) =l= SUM(g$(MG(m,g) and GV(g,v)), W(m,v,g,t))
;
* Exclusive(m,mp,t)$E(m,mp)..

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* Y(m,t) + Y(mp,t) =l= 1
*
RequiredDwell(m)$(r(m)>eps).. {R9}
D(m) =g= r(m)
;
LOOP(m,
        D.up(m) = length(m); {R10}
);

MODEL UAS_PLANNER /
eqnObj  
UAVLimit  
ModuleLimit  
TotalMods  
GCSLimit  
LRSLimit  
CoverageLimit  
DwellLimit  
Prerequisite   
* Exclusive  
Mission_Control  
RequiredDwell  / 
;

IF(errors=0,
    PUT 'solve UAS_PLANNER' / ;
* UAS_PLANNER.reslim=60. ;  
* UAS_PLANNER.optcr=0.05 ;
    PUT ' reslim=',UAS_PLANNER.reslim:5:0,' seconds,  
    optcr=',UAS_PLANNER.optcr:5:2 ;
    PUT ' optfile=',UAS_PLANNER.optfile:2:0 / ;
SOLVE UAS_PLANNER USING MIP MAXIMIZING OBJECTIVE;

PUT 'PLANNER solver and model status', UAS_PLANNER.solvestat:4:0, UAS_PLANNER.modelstat:4:0 /;

IF( UAS_PLANNER.modelstat<>1 and UAS_PLANNER.modelstat<>8,
   errors=1;
ELSE
   PUT / 'Objective: ', OBJECTIVE.l:10:4 /;
   PUT / 'Module Deployment' /;
   LOOP((c,v,l)$(MODS.L(c,v,l)>eps),
      PUT ' ',c.tl:10,' ',v.tl:8,' ',l.tl:10,': ',MODS.L(c,v,l):4:0 /;
   );
   PUT / 'UAV flight schedules..' //;
   LOOP(s$(X.l(s)>eps),
      PUT ' ',s.tl:10,' ';
      LOOP(v$SUM(t$B(s,v,t),1),
         PUT ' ',v.tl:8;
      );
      PUT ' ',X.l(s):4:1 /;
   LOOP(m$(SUM(t$A(s,m,t),1)>0),
      PUT ' ',m.tl:10;
      LOOP(t$A(s,m,t),
         PUT ' ',t.tl:5;
      );
      PUT /;
   );
);

PUT / 'GCS Usage' /;
LOOP(g$(SUM((m,v,t)$(MG(m,g) and GV(g,v)), W.l(m,v,g,t))>eps),
   PUT ' ',g.tl:8 /;
   LOOP((m,v)$(MG(m,g) and GV(g,v) and (SUM(t,W.l(m,v,g,t))>eps)),
      PUT ' ',m.tl:8, ' ',(SUM(t,W.l(m,v,g,t))) ;
   LOOP(t$(W.l(m,v,g,t)>eps),
   );
```plaintext
PUT ",.tl:8;
);
PUT /;
);
);
PUT /'MISSION COVERAGE'/;
PUT 'Mission  Dwell Time'/;
LOOP(m$(D.l(m)>0),
  PUT ',m.tl:8, ',D.l(m):5:1 /
  LOOP(t$(SUM(v,Y.l(m,v,t))>eps),
    PUT ',t.tl:4, ',(SUM(v,Y.l(m,v,t))):4:1 /
  );
); PUTCLOSE UASP_LOG;

PUT MISSIONS_CSV;
PUT ',,,Total,Total,Value,Total'/;
PUT 'Start,End,Time Periods,Time Periods,Per Time,Value'/;
PUT 'Mission,Time,Time,Requested,Assigned,Period,Achieved,OBJECTIVE.L'/;
LOOP(m,
  PUT m.tl,','D.l(m),','val(m),','(D.l(m)*val(m)) /
); PUTCLOSE MISSIONS_CSV;
{Rest of report writer goes here}
);
);

IF(errors>0,
  PUT '<*** errors aborting this run:',errors:10:0 /
); IF(warnings>0,
```
PUT / ' <+++ warnings generated by this run: ',warnings:10:0 / ;
PUT ' please find out what these indicate' / ;
);
PUTCLOSE UASP_log ;

IF(errors=0,

{Build CSV Output Files}

PUT UASP_STA;
PUT 'Optimal solution found. Successful completion.' /;
PUTCLOSE UASP_STA;
);
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