This work represents the joint work of several groups including numerical calculations and experiments. Numerical calculations were performed for the propagation of a femtosecond laser beam through an optical path and a nonlinear absorber. The results were compared with experiments performed under similar conditions. There was excellent agreement between calculations and experiments at low input energy. However, further additions must be done to the calculation of the optical path for high input energy.
15. **SUBJECT TERM**  
nonlinear absorbers, numerical simulations

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<td>c. THIS PAGE</td>
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<td>Dr. M. J. Potasek</td>
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Standard Form 298 (Rev. 8-98)  
Prescribed by ANSI Std. Z39.18
"Computational Analysis of Hybrid Two-Photon Absorbers with Excited State Absorption"

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AFOSR Contract:
FA9550-04-C-0036

Dates:
April 1, 2004 to March 31, 2007
Abstract

This work represents the joint work of several groups including numerical calculations and experiments. Numerical calculations were performed for the propagation of a femtosecond laser beam through an optical path and a nonlinear absorber. The results were compared with experiments performed under similar conditions. There was excellent agreement between calculations and experiments at low input energy. However, further additions must be done to the calculation of the optical path for high input energy.
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1. Introduction

Multiphoton absorption processes are useful in several applications. These applications include, but are not limited to, optical data storage [1]-[2], micro fabrication [3]-[7], photoconductors and photovoltaics [8], markers for genomes and proteins [9]-[10], biological and medical detectors [11]-[12], optical limiters [13]-[16], biomimetic electromagnetic devices [17], nanopatterning of inorganic/organic materials [18]-[19] and photomedicine/photodynamic therapy [20].

The wide range of applications of multiphoton absorption processes makes it particularly useful to have a detailed method for numerical investigations because some of the strongest two-photon absorbers are hybrid chromophores. These complex molecules exhibit a hybrid photo-activated energy level system in which the two-photon absorption (TPA) level is coupled to an excited state absorption (ESA) level. This hybrid arrangement creates a complex dynamical system in which the electron carrier concentration of every photo-activated energy level must be taken into account in order to determine the actual optical properties. Most traditional calculations of the laser matter interaction make simplifying assumptions about the optical field and the electron density states of the molecular system. We model propagation through two-photon materials and describe the numerical analysis of the complex interaction of the optical pulses with these hybrid systems. The numerical method calculates the spatiotemporal details of the electron population densities of each photo-activated energy level as well as the pulse shape in space and time.

The main topic of this effort was to coordinate a numerical simulation amongst a geographically and technically group of experts (See list below). The project involved a simulation of an optical path and propagation through a nonlinear absorber with experiments.
Good agreement was found between calculations and experiments at low input energy, but, at very high input energy it was determined that additional term, such as optical breakdown in air and lens, were required. This report describes the author’s section of the project involving the propagation through the nonlinear absorber. It necessitated writing additional features in the propagation code including: (1) expressing the field in real units, (2) describing the field in terms of $x,y,z,t$ and $r,z,t$ and (3) inputting the field from a digitized field file.

2. Description of the Test Case

The test case involves simulations and comparison to experiments. A schematic diagram of the experimental set up for the test case is shown below.

The nonlinear material is AF380. Test case parameters: laser pulse width 130 fs FWHM, laser wavelength 775 nm, laser energy 10 microJoule and 1 mJ, beam waist 2.5-3 mm $1/e^2$ radius, divergence $\pm 100$ microradians; sample thickness 1 mm AF380 film sandwiched between two glass slides, 1 mm each. Lens has a focal length of 1 m; lenses are either BK-7 or SF-11 Schott glass with 2.54 cm diameter. Data interchanges will be via flat ASCII files, SI units; in format $1pE14.21$; space delimited by at least one column. Data interchange grid size: 256x256 (space, Cartesian) x 256 (time) or Cylindrical (256x256 space x time). Field magnitudes will be normalized such that peak amplitude is $V/m$ to yield correct total energies.

2.1 Tasks:
### Table of tasks

<table>
<thead>
<tr>
<th>Task</th>
<th>Group</th>
<th>Activity</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Bill Dennis UGA</td>
<td>model the initial Gaussian pulse and take care of propagation through all optical windows/elements.</td>
</tr>
<tr>
<td>2</td>
<td>Vance Hedin</td>
<td>model all free-space propagation steps throughout optical path.</td>
</tr>
<tr>
<td>3</td>
<td>Mary Potasek</td>
<td>model propagation through all two-photon materials within setup</td>
</tr>
<tr>
<td>4</td>
<td>Mark Walker</td>
<td>measurements</td>
</tr>
<tr>
<td>5</td>
<td>ALL</td>
<td>Final simulation results will be passed back to Mark for comparison to experimental data</td>
</tr>
</tbody>
</table>

Initially the data was passed from one group to another by CDs. Later a server was set up at Wright-Patterson AFB for the data exchange.

### 2.2 Simulation file format.

The field file is in the standard ASCII format (1PE24.15E3) and order (r,t or x,y,t). The params file has the following form:

#### Table for simulation file format.

<table>
<thead>
<tr>
<th>Number</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>128</td>
<td>Number of space points</td>
<td>none</td>
</tr>
<tr>
<td>256</td>
<td>Number of time points.</td>
<td>none</td>
</tr>
<tr>
<td>1.00000000000000E-003</td>
<td>The width of the spatial window</td>
<td>m</td>
</tr>
<tr>
<td>1.474970454238465E-012</td>
<td>The length of the time window</td>
<td>s</td>
</tr>
<tr>
<td>7.750000000000000E-007</td>
<td>The center wavelength</td>
<td>m</td>
</tr>
</tbody>
</table>

### 3. Numerical method used for propagation through AF380

The energy level diagram for the AF380 is given below.
Schematic energy level diagram of the hybrid multiphoton absorber (AF380). The solid lines are the photo excitations, the dashed lines show the decay from the various electronic states and the dot-dashed line corresponds to the thermal excitation directly into the conduction band without any excited state absorption. The multiple horizontal lines represent the vibrational levels of the various electronic states. The parameters are $\sigma_{\text{gap}} = 8.0 \text{ e}^{-21} \text{ cm}^4 / \text{GW}$, $\sigma_{1,4} = 2.0 \text{ e}^{-17} \text{ cm}^2$, $\sigma_{3,4} = 2.0 \text{ e}^{-17} \text{ cm}^2$, $k_{10} = 0.5 \text{ e}^{-3} \text{ ps}^{-1}$, $k_{1,2} = 0.5 \text{ e}^{-2} \text{ ps}^{-1}$, $k_{2,3} = 0.29 \text{ e}^{-3} \text{ ps}^{-1}$, $k_{4,3} = 4.0 \text{ e}^{-9} \text{ ps}^{-1}$, $k_{3,0} = 0.34 \text{ e}^{-3} \text{ ps}^{-1}$, $\eta = 0.06$

These parameters are used in the rate equations to analyze all the carrier density distributions. The propagation equation is coupled to these rate equations, which is used to calculate the laser pulse intensity shape. Initially all of the carriers are assumed to be in the ground state ($N_0$) before the laser pulse enters the material. The energy levels have the following properties. $N_0$ is the ground state, $N_1$ is the first excited state reached by two-photon absorption, $N_2$ is an intermediate state between the first excited state and the fluorescing state $N_3$. The intermediate state is attributed to an intramolecular transitional state in which the two-photon excitation rearranges itself from the D-π section of the molecule towards the acceptor region. Quantum mechanical calculations of the excited state electron density and molecular motion support this interpretation. The upper level $N_4$ is assumed to be the continuum (similar to a conduction band in semiconductors) that can be populated from either $N_1$ or $N_3$. Free carrier generation was demonstrated by measurement of a nonlinear photocurrent using a thin film of the material placed between transparent conducting glasses. $N_4$ has a long lifetime.

The rate equations are given by
\[
\frac{dN_0}{dt} = -\frac{\sigma_{\text{tpa}} I(t)^2 N_0}{2\hbar \omega_0} + k_{1,0} N_1 + k_{3,0} N_3
\]
\[
\frac{dN_1}{dt} = \frac{\sigma_{\text{tpa}} I(t)^2 N_0}{2\hbar \omega_0} (1-\eta) - k_{1,0} N_1 - k_{1,2} N_1 - \frac{\sigma_{1,4} I(t) N_1}{\hbar \omega_0}
\]
\[
\frac{dN_2}{dt} = k_{1,2} N_1 - k_{2,3} N_2
\]
\[
\frac{dN_3}{dt} = k_{2,3} N_2 - k_{3,0} N_3 - \frac{\sigma_{3,4} I(t) N_3}{\hbar \omega_0} + k_{4,3} N_4
\]
\[
\frac{dN_4}{dt} = \frac{\sigma_{3,4} I(t) N_3}{\hbar \omega_0} - k_{4,3} N_4 + \frac{\sigma_{\text{tpa}} I(t)^2 N_0}{2\hbar \omega_0} + \frac{\sigma_{1,4} I(t) N_1}{\hbar \omega_0}
\]

where \( N_j \) is the electron number density of the state \( j \), \( \sigma_{j,k} \) is the absorption cross-section for electron pumping from the state \( j \) to the state \( k \), and \( k_{j,k} \) is the decay rate from the state \( j \) to the state \( k \). The fraction of the two-photon population contributing to the photo-induced current is given by the Boltzmann distribution for electron

\[
\eta = \left(1 + \frac{\Delta E}{k_B T} \right)^{-1}
\]

where \( T \) is the temperature, \( k_B \) is Boltzmann's constant and \( \Delta E \) is the energy gap between the two-photon state and the continuum level.

The rate equations are written in the following form and assumed to be in a moving coordinate system

\[
\frac{d\mathbf{N}}{dt} = \dot{M} \mathbf{N} = [\dot{G} + \frac{I}{\hbar \omega_0} \dot{H} + \frac{I^2}{2\hbar \omega_0} \dot{F}] \mathbf{N}
\]

where the matrix \( M \) is given by
The matrix $M$ is separated into three matrices for convenience. Thus $G$ multiplies the constant decay terms, $H$ multiplies terms dependent on the intensity and describes ESA, and $F$ describes TPA. These matrices are given below.

$$
M = \begin{bmatrix}
\frac{-\sigma_{pe}I(t)^2}{2\hbar\omega_0} & k_{1,0} & 0 & k_{3,0} & 0 \\
\frac{\sigma_{pe}I(t)^2(1-\tilde{\eta})}{2\hbar\omega_0} -k_{1,0} -k_{1,2} & -\frac{\sigma_{pe}I(t)}{h\omega_0} & 0 & 0 & 0 \\
0 & k_{1,2} & -k_{2,3} & 0 & 0 \\
0 & 0 & k_{2,3} & -\frac{\sigma_{pe}I(t)}{h\omega_0} & k_{4,3} \\
\frac{-\tilde{\eta}\sigma_{pe}I(t)^2}{2\hbar\omega_0} & \frac{\sigma_{pe}I(t)}{h\omega_0} & 0 & \frac{\sigma_{pe}I(t)}{h\omega_0} & -k_{4,3}
\end{bmatrix}
$$

$$
G = \begin{bmatrix}
0 & k_{1,0} & 0 & k_{3,0} & 0 \\
0 & -k_{1,0} -k_{1,2} & 0 & 0 & 0 \\
0 & k_{1,2} & -k_{2,3} & 0 & 0 \\
0 & 0 & k_{2,3} & -k_{3,0} & k_{4,3} \\
0 & 0 & 0 & 0 & -k_{4,3}
\end{bmatrix}
$$

$$
H = \begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & -\sigma_{1,4} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & -\sigma_{3,4} \\
0 & 0 & 0 & 0 & 0
\end{bmatrix}
$$

$$
F = \begin{bmatrix}
-\sigma_{pe} & 0 & 0 & 0 & 0 \\
0 & \sigma_{pe}(1-\tilde{\eta}) & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
\tilde{\eta}\sigma_{pe} & 0 & 0 & 0 & 0
\end{bmatrix}
$$

4. Results

The following section describes the numerical and experimental results. The numerical results were obtained by calculating the laser propagation through the lens, air and first section of the cuvette (Prof. Dennis group), followed by propagation through AF380 (Potasek), and then propagation through the remainder of the optical path (Prof. Dennis group). The calculations were then compared with experiments (Mark Walker group). The following figures are from Potasek, except where noted. The results are divided into two energy regions: (1) low energy-10uJ and (2) high energy-1000uJ. A brief schematic diagram of the experimental set up is given in the figure below.
4.1 Low input energy-10 uJ

The numerical calculations and comparison with experiments are described next. In this case the input energy is 10uJ. The plots below show the calculated contour plots for the pulse propagation from the input to the material and the output from the material. As can be seen there is no pulse distortion.

Calculated contour plots. Left side: z=0. Right side: z=1 mm.
The figure below shows a comparison between the numerical calculation and the experiment. As can be from the figure, there is good agreement between the calculation and the experiment.

**Mod/Sim Comparison**

*Time Integration of Input Pulse to Measured Beam Profile*

dimensions are in mm

(From Mark Walker, MLPJ)

### 4.2 High Input Energy-1000uJ

The next section compares the numerical calculations with the experiments. The numerical calculations include the calculations from both the Dennis group and Potasek. It should be noted that at high input energy there is optical breakdown in the air and cuvette, which is not taken into account by the Dennis group at this time. The plots below show the calculated pulse shapes and contour plots as a function of propagation. It can be seen from the figures that the pulse splits in the temporal domain. This feature is not seen in the low energy case.
Calculated Contour Plots for Propagation through AF380 for x vs Time as a Function of Distance (BK-7 lens) Input 1 mJ

Corresponding Pulse Shapes for x versus t as a function of propagation distance.
These temporal features are seen in the comparison between calculations and experiments below.

![Instantaneous beam profiles for x versus t. Left side: calculations. Right side: experiment (Mark Walker)](image)

However, in the xy pulse shape there is significant difference between the calculations and the experiment. The figure below shows the calculation on the left and the experiment on the right. As can be seen from the figure the experimental pulse shape is significantly larger than the calculated one.

![Comparison of beam shape at high input energy. (Mark Walker)](image)
Additionally, there is a factor of two difference between the calculated experimental transmission.

5. Conclusions

Comparison of numerical calculations and experiments agreed well in the case of low input energy. However, for high input energy the agreement is not as good. The likely cause of the difference between experiment and calculation is probably due to neglect of ionization and plasma formation in the air between the lens and the AF380. Future calculations may need to include these effects.

6. References


7. Appendix

Personnel supported

PI:
M. J. Potasek

Collaborators:
- Drs. Sean Kirkpatrick, Chris Brewer and Mark Walker, WPAFB/ML
- Prof. Dennis, Univeristy of Georgia
- Dr. Erik Zeek, Univeristy of Georgia
- Dr. Tracey Bowen, Kirtland AFB
- Dr. Vance Hedin, Comcast

Publications:
No external reviewed publications
Three internal progress reports

Interactions/Transitions:
a. Participation/presentations at meeting, conferences, etc
   • Presentation at Initial Meeting, AFOSR, Washington, DC, Jan 22, 2004
   • Presentation at Review Meeting, AT&T, Fairborn, Ohio, Dec 8, 2004
   • Presentation at Review Meeting, Kirtland AFB, N.M. Feb. 2, 2006
   • Numerous e-mail, phone discussions, and data exchange with Materials Lab, WPAFB and Bill Dennis and Erik Zeek, Univ of Georgia and others concerning the test case.
   • Numerical code and data exchange with Materials Lab, WPAFB and Bill Dennis and Erik Zeek, Univ of Georgia and others concerning the test case.

b. Consultative and advisory functions to other laboratories and agencies
   • Meeting, discussions, phone calls,
   • Drs. Sean Kirkpatrick, Chris Brewer and Mark Walker, WPAFB/ML
   • Prof. Dennis, University of Georgia
   • Dr. Erik Zeek, University of Georgia
   • Dr. Tracey Bowen, Kirtland AFB
   • Dr. Vance Hedin, Comcast

c. Transitions
   • Initial numerical code on multiphoton materials was transitioned to WPAFB.

New discoveries, inventions or patent disclosures:
None.