INCORPORATING TARGET MENSURATION SYSTEM FOR TARGET MOTION ESTIMATION ALONG A ROAD USING ASYNCHRONOUS FILTER

by

Kwee Chye Yap

December 2006

Thesis Advisor: Isaac I. Kaminer
Second Reader: Vladimir N. Dobrokhodov

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1. AGENCY USE ONLY (Leave blank)  
2. REPORT DATE  
   December 2006  
3. REPORT TYPE AND DATES COVERED  
   Master’s Thesis  
5. FUNDING NUMBERS  

4. TITLE AND SUBTITLE:  
   Incorporating Target Mensuration System for Target Motion Estimation Along a Road Using Asynchronous Filter  

6. AUTHOR(S):  
   Kwee Chye Yap  

7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)  
   Naval Postgraduate School  
   Monterey, CA  93943-5000  

8. PERFORMING ORGANIZATION REPORT NUMBER  

9. SPONSORING /MONITORING AGENCY NAME(S) AND ADDRESS(ES)  
   SOCOM  

10. SPONSORING/MONITORING AGENCY REPORT NUMBER  

11. SUPPLEMENTARY NOTES  
   The views expressed in this thesis are those of the author and do not reflect the official policy or position of the Department of Defense or the U.S. Government.  

12a. DISTRIBUTION / AVAILABILITY STATEMENT  
   Approved for public release; distribution is unlimited  

12b. DISTRIBUTION CODE  

13. ABSTRACT (maximum 200 words)  
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14. SUBJECT TERMS  
   Small Unmanned Air Vehicle, Asynchronous filter, Perspective View Nascent Technologies, Target motion estimation  

15. NUMBER OF PAGES  
   59  

16. PRICE CODE  
   UL  

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INCORPORATING TARGET MENSURATION SYSTEM FOR TARGET MOTION ESTIMATION ALONG A ROAD USING ASYNCHRONOUS FILTER

Kwee Chye Yap
Lieutenant Colonel, Republic of Singapore Air Force
B.Eng., University of Manchester, Institute of Science and Technology, 1990

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN ENGINEERING SCIENCE
(MECHANICAL ENGINEERING)

from the

NAVAL POSTGRADUATE SCHOOL
December 2006

Author: Kwee Chye Yap

Approved by: Isaac I. Kaminer
Thesis Advisor

Vladimir N. Dobrokhodov
Second Reader

Anthony J. Healey
Chairman, Department of Mechanical and Astronautical Engineering
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In support of TNT experiments, the NPS UAV laboratory has developed a Vision-Based Target Tracking (VBTT) system for a Small Unmanned Aerial Vehicle (SUAV). This system provides an autonomous target tracking capability, while simultaneously estimating the target’s velocity and position. The accuracy of the existing system can be improved by providing external corrections to the target position estimation from the georectification system (GIS). This thesis addresses the implementation of an asynchronous correction scheme into the target position estimation filter. The current autonomous position estimation algorithm provides 20-30 meters accuracy. The external correction system (Perspective View Nascent Technologies (PVNT)) is expected to provide target position accuracy of 1-2 m. However, a delay of up to 10 seconds is expected. Therefore, in order to improve the accuracy of current estimation of target motion, a new asynchronous correction technique that incorporates the more accurate PVNT data is proposed. To further improve the target motion estimation, it was also proposed to incorporate a known road model into the filter and compare its performance with the original filter.
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ACKNOWLEDGMENTS

The author would like to thank Professor Isaac I. Kaminer for his continuous effort in explaining the concepts and requirements of designing the new filter for the thesis. His dedicated effort made the learning process enjoyable. He would also like to thank Dr. Vladimir N. Dobrokhodov for his invaluable advices and explanations throughout the thesis process. This thesis has enriched the author’s understanding in both the academic and technical areas of Unmanned Aerial Vehicle’s tracking of targets and will provide the necessary expertise in his future endeavors.

The author would like to express his gratitude to his wife, Gelin, who has supported him throughout the year when he was doing his course in NPS. Her continuous support and encouragement have made the thesis process painless.
I. INTRODUCTION

A. OVERVIEW

The main goal of this thesis was to design a new filter that is able to provide a better estimation of target motion. This new filter would complement the current non-linear target motion estimation filter mounted on a Small Unmanned Aerial Vehicle (SUAV). Naval Postgraduate School (NPS) is a participant in the Tactical Network Topology (TNT) field experimentation program, which includes United States Special Operations Command (USSOCOM), its component commands and several government laboratories. The field experimentations are part of the Surveillance and Target Acquisition (STAN) program. Quarterly field experiments are conducted at the Center for Inter-disciplinary Remotely-Piloted Aircraft Studies (CIRPAS) facility located at McMillan Field in Camp Roberts, California. These experiments aim to explore and demonstrate new technologies that are applicable to the military, with special focus on sensor and wireless network, autonomous vehicle and target tracking/identification.

B. MOTIVATION

The NPS SUAV is designed with Commercial Off-the-Shelf sensors that reduced the cost of operating the SUAV. The main role of the SUAV is in the surveillance and reconnaissance arena.

The utilization of Vision-Based Target Tracking (VBTT) allows a passive mode of target tracking and reduces the risk of exposure of the UAV when it conducts its surveillance. This would enhance the security of the SUAV operation.

Currently, the VBTT system utilizes a filter to estimate the position of the target. A coordinated control strategy is employed that estimates the position of the target using the turn rate of the Line-of-Sight (LOS) between the UAV and the target.

The accuracy of the estimated target motion can be improved if an external correction is made to the estimated target position obtained from the current filter. One of the possible correction methods can be obtained from the Perspective View Nascent Technologies (PVNT). This technology will be described in more details in Chapter 2. The PVNT software is able to provide a correction to the estimated target position up to 1
meter accuracy. However, this updated target position would only be made available about 1 to 10 seconds later. Thus, there is a need to develop an asynchronous filter to incorporate this updated position.

To further improve the performance of the new asynchronous filter, it is also proposed that a known road model be incorporated into the filter. The performance of this road-following asynchronous filter will be compared to the original filter to determine the anticipated improvement that may be achieved.
II. BACKGROUND

A. PERSPECTIVE VIEW NASCENT TECHNOLOGIES (PVNT)

The PVNT system was developed by Dr. Wolfgang Baer, a professor at the Naval Postgraduate School (NPS) in Monterey, California. The initial PVNT software was designed for tactical weapon testing. The software provided a 3D battlefield simulation and allowed the UAV to carry out target locating functions. The use of low-cost PC-based software helped to reduce the overall cost of the system. Currently, the PVNT software is capable of generating 1-meter-resolution terrain data for large area tactical battlefield simulations and uses it to create perspective views. These perspective views are employed to perform both line-of-sight (LOS) and weapon effectiveness analysis. At present, PVNT databases cover locations such as Fort Hunter Liggett, California and Camp Roberts, California.

One of the more unique features of the PVNT program is the use of raster formats (pixel) as storage for terrain surface, as opposed to polygon database that is used by most scene-visualization programs on the market. This makes PVNT more suitable for handling data that is gathered by remote sensors, and ideal for integration with tactical battlefield sensor systems.

Various experiments had previously been conducted at Camp Roberts incorporating flight test set-up with PVNT work stations. The flight test set-up utilized the vision-based target tracking and estimation system for both stationary and moving targets. A generic set up is shown in Figure 1 below.
During flight tests, images captured by the onboard camera mounted on the SUAV were broadcast and processed by OTS PerceptiVU image processing software [Ref 2]. Non-linear filtering algorithms (Figure 2) developed at NPS estimated the target geo-location’s accuracy to about 10-20 m with 10-20 seconds of tracking. Working in parallel, the images captured from the SUAV and the estimated position of the target obtained from the filtering are shared over the network and fed to the PVNT vision-based target tracking system.

The PVNT software compared the images received from the SUAV, together with GPS and camera angle coordinates, with the database information. The accuracy of the target position is determined almost solely by the accuracy of the database (currently at 1 m resolution). Thus, using the PVNT-image mensuration system would yield the target position estimates to within 1-2 m. However, due to the processing time required in comparing the target images with the PVNT database, there would be a time lapse (currently about 1 to 10 seconds) between the time the image of the target is fed to the PVNT system and the updated position of the target obtained from the PVNT system.

B. GENERIC ASYCHRONOUS KALMAN FILTER

In motion tracking, the standard Kalman filter has been extensively employed. However, such a filter requires synchronous and equi-distant measurement updates to ensure robust and accurate prediction. In many applications, such updates may not be
practical or even possible. Many enhancements to the standard Kalman filters were made [Ref 5, 6] to accept out-of-sequence, sporadic or infrequent updates to the filter. Such filters are typically known as asynchronous filters.

Asynchronous Kalman filters have been used in various applications. One of the more common applications is in sensor fusion. In sensor fusion applications, standard and extended Kalman filters are popular due to the ease of blending the various sensors’ data to provide an optimal estimate. Sensors measuring target’s velocity and/or accelerations can be blended with sensors measuring its direct position to give an optimal estimate of the target. However, Kalman filters require specific and consistent information for their current iteration in providing accurate prediction of the future states. Any interruption in any sensors update rate would degrade the effectiveness of a simple Kalman filter. Thus, asynchronous filters are designed to ensure that the effectiveness of the Kalman filters is not degraded with asynchronous updates from the sensors.

The implementation of the asynchronous Kalman filter can also take various forms. In the paper “Adaptable Sensor Fusion Using Multiple Kalman Filters” [Ref 7], the authors proposed the use of multiple Kalman filters to allow asynchronous inputs from sensors. The central idea of the paper is the use of a bank of Kalman filters to represent the various combinations of sensors. As the data acquisition rate differs on the various sensors, a sensor fusion algorithm allows the selection of the appropriate model to account for the new data that is available at each iteration. Such switching alleviates the need to receive information from all sensors at every iteration.

In this thesis, an asynchronous filter is developed to incorporate the delayed but more accurate target position estimates from PVNT.
III. PROBLEM DEFINITION

A. CURRENT ARCHITECTURE

Figure 2. Current architecture

Figure 2 depicts the current architecture for target tracking using SUAV in NPS. A system to track a target and estimate both its velocity and position has been in development over the years in NPS. Constant improvements have been made to the initial concept of target tracking. The current control system uses a nonlinear filter for target estimation [Ref 8]. This filter has shown stability in motion target estimation and graceful degradation of performance during target loss events. The filter has been flight tested using a moving target and is capable of estimating target position to an accuracy of 20 meters. Both the target’s velocity and position estimations are available in real time.

In parallel, the target image captured by the onboard camera of the small UAV is sent to the PVNT system as described in Chapter II. From PVNT, the target position estimation is expected to be 1-2 meters but with a delay of up to 10 seconds.
**B. PROBLEM DEFINITION**

In the diagram above, a target is traveling along a simulated road. At time $\tau$, the captured image of the target is sent to PVNT for processing. At the same time, the nonlinear filter onboard the UAV is processing the target image and estimating the position of the target. At time $t$ ($t > \tau$), when the target has traveled a finite distance along the road, an updated target position for time $\tau$ arrived from PVNT. The present filter would not be able to use this information to provide a better estimation of the target’s position and velocity.

**C. OBJECTIVES**

To provide a better target motion estimation using the more accurate but delayed PVNT position update, a new filter would be designed. This filter would be able to use the PVNT position and provide a more accurate velocity and position update at time $t$. To further enhance the filter, this thesis would also examine the performance of the filter that incorporates the road profile that the target is traveling on.
IV. FILTER DEVELOPMENT

A. GENERAL ASYNCHRONOUS FILTER

The following diagram shows the design of the new general asynchronous filter that was developed to estimate target motion (both velocity and position) using delayed PVNT target position estimation.

1. True Target Vehicle Model

A true target vehicle model was created in Simulink. It served two purposes. The first purpose was to generate the target’s velocity and position vectors in Local Tangent Plane. Generated positions of the target were fed to the PVNT model to provide delayed position of the target. The second purpose was to compare the target’s actual velocity and position with the filter’s estimates. The Simulink model of the true vehicle model is shown below.
2. **PVNT Model**

The purpose of the PVNT model was to simulate the delayed data received from the PVNT software. In Simulink, the PVNT model received position data from the true vehicle model, and using a Matlab script file generated delayed target position based on the delay timing specified by the user. PVNT noise can also be added to the generated target position. A Simulink diagram of the PVNT model is shown below.

3. **Data Storage**

In the model, a data storage model is generated to store the target’s velocity and position data. Both the true and estimated velocity and position are stored. This data is marked with a time stamp that allows it to be retrieved based on the time lapse between
the current time and the delayed time of the PVNT update. The filter has been designed to cater for varying delay times.

4. Filter

The Simulink model of the filter that was designed is shown below.

![Simulink model of filter in general asynchronous filter](image)

Figure 7. Simulink model of filter in general asynchronous filter

This filter uses dead-reckoning when there is no PVNT update. It is initiated based on the initial estimate of the target’s velocity and position. The gains (K1 and K2) are fixed. When the delayed PVNT update arrives (at time t for data at time $\tau$), the filter integrates backward and forward in time (from time $\tau$ to t) using PVNT delayed data. The output from the filter is an updated target velocity and position at time t. Both the velocity and position data at time t are used to re-initialize the open-looped filter to provide the target’s velocity and position from time t.

B. ROAD FOLLOWING ASYNCHRONOUS FILTER

The road following asynchronous filter was developed from the general asynchronous filter with some modifications. The diagram shows the Simulink representation of the road following asynchronous filter. The main difference for the road following asynchronous filter is the use of a parameter, $\rho$ (path length of the road), to characterize the road that the target vehicle is moving on. This parameter is chosen because its derivative, $\dot{\rho}$, is the speed of the vehicle at any point on the road. The
differences in the various models within the general asynchronous filter and the road following asynchronous filter are highlighted in the next few paragraphs.

1. True Target Vehicle Model with Road Following Characteristics

The following diagram is the modified true target vehicle model.

The main difference with the true vehicle model in the road following asynchronous filter is the use of the path length parameter to characterize the road. The values of the generated true path length as well as the speed of the vehicle are stored to be used when the PVNT position update arrives.
2. **PVNT Model**

The PVNT model for the road following asynchronous filter is the same as the one used for general asynchronous filter.

3. **Filter**

The asynchronous filter used in this section is shown in Figure 10. Both the inputs and outputs of this filter (shown below) are scalar (path length and speed).

![Simulink model of filter in road following asynchronous filter](image)

Figure 10. Simulink model of filter in road following asynchronous filter

4. **Optimization**

An optimization routine is implemented with the road following asynchronous filter to determine the path length parameter, $\rho$. The minimization equation is as shown.

$$
\min_{\rho} \left[ (x(\rho) - x_{PVNT})^2 + (y(\rho) - y_{PVNT})^2 + (z(\rho) - z_{PVNT})^2 \right]
$$

(1)
V. SIMULATION

A. FRAME REFERENCE
The frame reference used during the simulation is the Local Tangent Plane (LTP).

B. DURATION
The simulation duration is set at 180 seconds.

C. SAMPLE TIME
The sample timing used during the simulation is fixed at 0.1 second rate. For a simulation of 180 seconds, this equates to 1800 data points.

D. ROAD MODEL
In the simulation, the following equations are used to model the road.

\[
P_{\text{road}} = \begin{bmatrix} x(\rho) \\ y(\rho) \\ z(\rho) \end{bmatrix} = \begin{bmatrix} \rho \\ 0.0000192\rho^3 - 0.025\rho^2 + 9.74\rho \\ 0 \end{bmatrix}
\] (2)

A cubic representation of the road was chosen for the simulation to ensure that the profile chosen would not be a monotonically increasing function of the path length. The road profile in x-y representation is \( y = 0.0000192x^3 - 0.025x^2 + 9.74x \) and a visual representation of this road profile is shown in Figure 11.

E. MEASURE OF PERFORMANCE (MOP)

Since the main purpose of both filters is estimation of the motion of the target vehicle, the MOP chosen was the root-mean-square (rms) errors between the true motion and estimated motion.

\[
\text{rms error}_{\text{velocity}} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left[ (v_{true,x} - \hat{v}_x)^2 + (v_{true,y} - \hat{v}_y)^2 + (v_{true,z} - \hat{v}_z)^2 \right]} \\
\text{rms error}_{\text{position}} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left[ (p_{true,x} - \hat{p}_x)^2 + (p_{true,y} - \hat{p}_y)^2 + (p_{true,z} - \hat{p}_z)^2 \right]}
\]

(3)  

(4)

F. FILTER COMPARISON

The performance of the general asynchronous filter and the road following asynchronous filter were compared by varying some of the filter parameters. The variables include:

1. K1 and K2 Gains

The fixed gains within the filter are varied from a value of 10 down to 0.1. The rms errors in both velocity and position were compared.
2. PVNT Delay

The expected delay from PVNT was randomized with increasing magnitude (from 1 to 10 seconds). The rms errors in both velocity and position were again compared.

3. PVNT Noise

Lastly, the PVNT noise (errors that can be expected from the PVNT software) is also varied within each filter. The noise added to the PVNT position ranged from +/- 1 meter to 5 meters. Similarly, the rms errors in both velocity and position were compared.
VI. RESULTS AND ANALYSIS

A. FILTER PERFORMANCE WITH K1 AND K2 VALUES

To examine the filter performance based on variation of K1 and K2 values, the other two parameters were fixed. The PVNT delay is random but does not exceed 1 second while the PVNT noise is set at +/- 0 meter (i.e. no noise). The K1 and K2 gains are fixed at the following values shown in the table below.

Table 1. Variation of K1 and K2

<table>
<thead>
<tr>
<th>Runs conducted</th>
<th>K1</th>
<th>K2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Run 1</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>Run 2</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Run 3</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Run 4</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>Run 5</td>
<td>0.1</td>
<td>0.1</td>
</tr>
</tbody>
</table>

1. Results

The following four plots show the results obtained for both the general and road following asynchronous filters for the rms errors obtained for the target’s velocity and position.

Figure 12. Target velocity rms errors vs K1/K2 values (general asynchronous filter)
Figure 13. Target position rms errors vs K1/K2 values (general asynchronous filter)

Figure 14. Target velocity rms errors vs K1/K2 values (road following asynchronous filter)
2. Analysis

For both filters, decreasing the gains from 10 to 0.1 resulted in a decrease in the rms errors for both velocity and position estimations. In both filters, the gains K1 and K2 were activated only when there was a PVNT update. For the simulation, this equates to about 10% (180 PVNT updates over 1800 data points) of the simulation time. As such, although a smaller gain is desired, the rms errors resulting from the different gains did not differ significantly.

B. FILTER PERFORMANCE WITH PVNT DELAY

To examine the filter performance based on PVNT delays, the other two parameters were fixed. The K1 and K2 values are fixed at 0.5 while the PVNT noise was set at +/- 0 meter (i.e. no noise). The PVNT delays are random, but cannot exceed the values shown in Table 2.
Table 2. Variation of PVNT delays

<table>
<thead>
<tr>
<th>Runs conducted</th>
<th>PVNT delays (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Run 1</td>
<td>1</td>
</tr>
<tr>
<td>Run 2</td>
<td>2</td>
</tr>
<tr>
<td>Run 3</td>
<td>3</td>
</tr>
<tr>
<td>Run 4</td>
<td>5</td>
</tr>
<tr>
<td>Run 5</td>
<td>10</td>
</tr>
</tbody>
</table>

1. Results

The following four plots show the results obtained for both the general and road following asynchronous filters for the rms errors obtained for the target’s velocity and positions.

Figure 16. Target velocity rms errors vs PVNT delay (general asynchronous filter)
Figure 17. Target position rms errors vs PVNT delay (general asynchronous filter)

Figure 18. Target velocity rms errors vs PVNT delay (road following asynchronous filter)
Figure 19. Target position rms errors vs PVNT delay (road following asynchronous filter)

2. **Analysis**

From the plots above, the rms error for both the velocity and position increased significantly as the PVNT delay time rose. For the general asynchronous filter, the rms error for the estimation of target position rose from 10.7722 m (random delay up to 1 second) to 71.9274 m (random delay up to 10 seconds). This was almost a seven-fold increase. The number of PVNT updates for random delay up to 10 seconds is expected to be lower than the number of PVNT updates for random delay up to 1 second. As such, the general asynchronous filter would rely more on dead reckoning for random delay up to 10 seconds, which resulted in the significant increase in errors both in the position and velocity estimation. Even for the road following asynchronous filter, both the velocity and position estimation showed an increasing trend. The optimization routine, though able to reduce the magnitude of the velocity and position’s rms error significantly as compared to the general asynchronous filter, was unable to prevent the increased in rms error from increasing as the PVNT delay increased.
C. FILTER PERFORMANCE WITH PVNT NOISE

To examine the filter performance based on PVNT noise, the other two parameters were fixed. The K1 and K2 values were fixed at 0.5 while the PVNT delay was random but did not exceed 1 meter. The PVNT noise was fixed at the following values shown in the table below.

Table 3. Variation of PVNT noise

<table>
<thead>
<tr>
<th>Runs conducted</th>
<th>PVNT noise (meter)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Run 1</td>
<td>± 0</td>
</tr>
<tr>
<td>Run 2</td>
<td>± 1</td>
</tr>
<tr>
<td>Run 3</td>
<td>± 2</td>
</tr>
<tr>
<td>Run 4</td>
<td>± 3</td>
</tr>
<tr>
<td>Run 5</td>
<td>± 5</td>
</tr>
</tbody>
</table>

1. Results

The following four plots show results obtained for both the general and road following asynchronous filters for the rms errors obtained for the target’s velocity and positions.

Figure 20. Target velocity rms errors vs PVNT noise (general asynchronous filter)
Figure 21. Target position rms errors vs PVNT noise (general asynchronous filter)

Figure 22. Target velocity rms errors vs PVNT noise (road following asynchronous filter)
2. Analysis

For the general asynchronous filter, the increase in PVNT noise value caused an increase in the rms error for both the velocity and position estimation. However, the magnitude of increase was not significant. The trend for the road following asynchronous filter was similar and the increase was smaller than the general asynchronous filter. The accuracy of the PVNT position update (within +/- 1 to 5 m) was much smaller than the variation in the x and y distance traveled by the target on the simulated road during simulation. As such, the filter was able to re-initialize itself to a fairly accurate position provided by PVNT. The road following asynchronous filter was able to provide a more accurate prediction of the position of the target and used it to re-initialize the filter. Thus, its rms error for both velocity and position were almost constant for PVNT noise up to 3 meters.

D. GENERAL ASYNCHRONOUS FILTER PERFORMANCE

The general asynchronous filter was run with the following parameters: K1 = K2 = 0.5, PVNT delay = random up to 1 second, PVNT noise = +/- 3 meters. The plots for
the true and estimated velocity and position were plotted below. The rms errors were also plotted.

Figure 24. Actual vs Estimated target position (general asynchronous filter)

Figure 25. Errors in x-direction position (general asynchronous filter)
From the position plots above, it can be seen that the main errors occurred at the beginning of the road and toward the end of the road. In these two sections of the road, the change in gradients was the greatest. The general asynchronous filter, without the knowledge of the road profile, could only rely on the last PVNT position update to estimate the future target’s position. As such, with the steeper change in road gradient, the performance of the filter would not be as good as it was when the change in gradient of the road was more gradual (toward the center part of the road).
Figure 27. Velocity profile in the x-direction (general asynchronous filter)

Figure 28. Error in the x-direction velocity (general asynchronous filter)
Figure 29.  Velocity profile in the y-direction (general asynchronous filter)

Figure 30.  Error in the y-direction velocity (general asynchronous filter)
From the velocity plots above, the major velocity errors occurred when the change in gradient was the highest. The prediction of the target’s velocity was similar to its position estimation and the errors generated were also similar when there was a large change in gradient of the profiles.

E. ROAD FOLLOWING ASYNCHRONOUS FILTER PERFORMANCE

The road following asynchronous filter was run with the following parameters: \( K1 = K2 = 0.5 \), PVNT delay = random up to 1 second, PVNT noise = +/- 3 meters. The plots for the true and estimated velocity and position were plotted below. The rms errors were also plotted.

![Plot of actual vs estimated target position (road following)](image)

Figure 31. Actual vs Estimated target position (road following asynchronous filter)
Figure 32. Errors in x-direction position (road following asynchronous filter)

![Plot of errors in target position (x position)](image)

Figure 33. Expanded plot for errors in x-direction position (road following asynchronous filter)

![Expanded view of plot](image)
Figure 34. Errors in y-direction position (road following asynchronous filter)

Figure 35. Expended plot for errors in y-direction position (road following asynchronous filter)
Based on the parameters specified for the simulation, the road following asynchronous filter was able to provide very accurate position estimation. Both the x and y direction errors were close to zero. This road following asynchronous filter showed a vast improvement as compared to the general asynchronous filter. The knowledge of the road profile allowed the optimization routine to further reduce the error that the PVNT position estimate provided. The filter was able to integrate along the road provided and gave very accurate target position estimation.

Figure 36. Velocity profile in the x-direction (road following asynchronous filter)
Figure 37. Error in the x-direction velocity (road following asynchronous filter)

Figure 38. Velocity profile in the y-direction (road following asynchronous filter)
Figure 39.  Error in the y-direction velocity (road following asynchronous filter)

The target’s velocity estimation was very accurate using the road following asynchronous filter. The filter was able to use the derivative of the path length (i.e., speed) to estimate the target’s velocity. Due to the accuracy provided by the minimization routine in obtaining the path length, its derivative yields accurate velocity estimation.
VII. CONCLUSION AND RECOMMENDATION

A. CONCLUSION

The task of designing an asynchronous filter was achieved in this thesis. The asynchronous filter was able to use the delayed PVNT target position updates that arrived about 1 to 10 seconds later to refine the target’s motion estimation. This simple filter has shown its capability to estimate target motion in simulation. Furthermore, the general asynchronous filter was modified to allow the incorporation of a road model. This allowed a better prediction of target motion as the target’s motion is expected to be along the road that it is traveling on. In simulation, it was shown that this modified filter could estimate the target’s velocity and position very accurately.

B. RECOMMENDATION

The new asynchronous filter worked well in simulation. In the future, this filter could be incorporated in the hardware and be bench-tested. Further test in actual SUAV flight could be conducted once bench testing has shown promising results.

The asynchronous filter could also be combined with the current non-linear filter so that the two complement each other during target motion estimation. The advantage of the asynchronous filter is in its ability to use the delayed but more accurate PVNT update to provide a better target velocity and position estimation at current time. This information could be used to re-initialize the nonlinear filter to enhance its performance such that the current 10 – 20 m accuracy could be reduced.
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