RUNNING PERFORMANCE AS AN INDICATOR OF VO$_{2\text{max}}$: DISTANCE EFFECTS

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Running Performance as an Indicator of VO$_{2\text{max}}$: Distance Effects

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This research has been conducted in compliance with all applicable Federal Regulations governing the protection of human subjects. No human subjects were directly involved in this review.

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EXECUTIVE SUMMARY

Background

Running performance often is used to evaluate aerobic capacity. Run tests are a useful alternative to laboratory measures of oxygen uptake because running performance is related to those measures. Run tests provide less precise estimates of aerobic capacity than laboratory measurement, but are much easier to conduct. The use of run tests, therefore, is a tradeoff between precision of estimation and simplicity of administration. Run tests must meet some minimum standard of estimation precision to justify their use.

Objective

This report reviews the literature relating aerobic capacity to running performance. The goal was to construct a model to predict run test estimation precision based on the distance or duration of the test. The model could answer questions such as "How long must a run be to provide a valid indication of aerobic capacity?" and "How much will precision increase if a 3-mile run is used instead of a 1.5-mile run?"

Approach

The published literature was searched to identify studies of maximal oxygen uptake (VO$_{2\text{max}}$) and running performance. A meta-analysis was conducted on reported correlations between VO$_{2\text{max}}$ and performance extracted from 122 studies.

Results

The correlation between VO$_{2\text{max}}$ and performance increased with distance, but only up to a point. For fixed-distance runs, the size of the correlation increased up to 2 km, then remained constant. For fixed-time runs, the correlation appeared to be constant for runs of 12 min or longer. Above these cutoffs, the fixed-time correlation ($r = .797$) was slightly higher than the fixed-distance ($r = .718$) correlation. These figures indicate a standard error between -3.7 and -4 ml•kg$^{-1}$•min$^{-1}$ compared to a range of -2.5 to -3 ml•kg$^{-1}$•min$^{-1}$ for laboratory tests.

Conclusions

Run tests should be at least 2 km in distance or 12 min in duration to maximize validity as indicators of aerobic capacity. Increasing distance or time beyond these minimum values does not improve run test validity as an indicator of VO$_{2\text{max}}$. Other things equal, fixed-time tests are preferable to fixed-distance tests. These tests estimate aerobic capacity with reasonable precision.
Introduction

Maximum oxygen uptake (VO$_{2\text{max}}$) is an important indicator of cardiopulmonary function (McArdle, Katch, & Katch, 1996). Laboratory tests that measure oxygen uptake during treadmill runs or cycle ergometry are the gold standard for assessing this capacity. These tests require special equipment and significant time investments to assess a single subject. The resource intensive character of the tests makes simpler alternatives attractive in many situations.

Run tests are a popular alternative means of estimating VO$_{2\text{max}}$. For example, run tests are common in fitness assessments of school children and military personnel. There is strong empirical justification for the use of run tests as a less technology intensive, cost-effective substitute for laboratory measures of VO$_{2\text{max}}$. Prior reviews of VO$_{2\text{max}}$ and running performance (Baumgartner & Jackson, 1982; Knapił, 1989; Safrit, Hooper, Ehler, Costa, & Patterson, 1988) identify numerous studies that reported VO$_{2\text{max}}$-running performance correlations that typically are between $r = .50$ and $r = .80$. Safrit et al. (1988) computed an average of $r = .741$, after correcting for measurement error, for runs covering 1 mile or more or lasting 9 minutes or longer.¹

Previous reviews clearly demonstrate that run tests can be valid indicators of aerobic capacity, but an important question has not been examined in detail: “Do longer runs provide better estimates of aerobic capacity?” If so, the longest distance that the test population can complete should be used to estimate aerobic capacity. Also, some populations (e.g., children, elderly) may not be able to complete a long enough run to obtain acceptable VO$_{2\text{max}}$ estimates. If so, some other method must be used to assess aerobic capacity. An examination of the relationship between run distance and validity will answer important questions such as “What is the shortest run that will meet a specified validity criterion (e.g., $r = .65$)?” and “How much would be gained if the current test were lengthened by 500 meters?” The answers to these questions have important implications for the effective use of run tests, particularly in applied settings.

Run test validity as an indicator of aerobic capacity² should increase with distance. Aerobic processes provide an increasing proportion of the total energy for performance as run distance increases (Spencer & Gastin, 2001. Increased dependence on aerobic energy should make the rate at which aerobic energy can be generated increasingly important for performance. Individual differences in that rate (i.e., differences in aerobic capacity) should be more strongly related to performance for longer runs. It follows that VO$_{2\text{max}}$, an indicator of aerobic capacity, should be more strongly related to performance for longer runs.
Two lines of evidence support the above arguments. First, studies that assessed performance for several distances have found stronger correlations for longer runs (Burke, 1976; Farrell, Wilmore, Coyle, Billing, & Costill, 1979; Shaver, 1975; Weyand, Cureton, Conley, Sloniger, & Liu, 1994). Second, mathematical models based on world records predict that a 1% difference in aerobic capacity yields a 0.3% performance difference at 400 m, but a 0.997% difference at 10 km (Ward-Smith, 1999). The close correspondence between aerobic capacity differences and performance differences at longer distances should translate into a stronger association between the two at longer distances.

The only quantitative review of the VO$_{2\text{max}}$-running performance literature contradicted the prediction that validity increases with run distance. Safrit et al. (1988) found no difference between shorter and longer runs in their analysis. However, their review only included runs $\geq$ 1 mile or $\geq$ 9 minutes. Most of the increase in the proportion of energy derived from aerobic processes occurs for shorter runs (Ward-Smith, 1999). The proportion increases from $\sim$7% at 100 m to $\sim$74% at 1500 m, then to $\sim$97% at 10 km. If validity parallels dependence on aerobic energy, about 75% of the expected increase in validity coefficients was not covered in Safrit et al.'s (1988) review.

This review extends the quantitative analysis of run test validity initiated by Safrit et al. (1988). Meta-analysis (Hedges & Olkin, 1985; Hunter & Schmidt, 1990) is used to evaluate quantitative models relating distance/duration to run test validity. The review covers runs from 10-m sprints to 84.4-km ultramarathons.

**Methods**

**Literature Search**

The literature search was conducted in a series of steps designed to ensure broad coverage of published and unpublished research:

1. Articles cited by Safrit et al. (1988), Baumgartner and Jackson (1982), and Knapik (1989) formed the initial list of studies.
2. The Medline, PsychLit, and Discus databases were searched to identify additional studies using "maximal oxygen uptake" with "Arun time" or "Arunning" as the primary keywords. Additional searches were performed with "maximum oxygen uptake," "maximal oxygen capacity," "aerobic capacity," and "AVO$_{2\text{max}}$" as variations on maximal oxygen uptake. "Performance" was used as an alternative to run time.
3. The articles identified in steps 1 and 2 were examined. Those articles that reported at least 1 relevant correlation were retained.

4. An ancestry search (Rosenthal, 1984; White, 1994) was conducted by examining the reference lists in the articles retained in step 3.

5. Year-by-year searches were conducted in Journal of Sports Medicine and Physical Fitness, Medicine and Science in Sports and Exercise, European Journal of Applied Physiology, and Research Quarterly for Sports and Exercise. Each journal contributed multiple articles in steps 1 through 4. All volumes of the first two journals were reviewed; the latter two journals were reviewed from 1975 to present.

6. The Naval Health Research Center and San Diego State University library catalogues were searched to identify unpublished studies (e.g., Master's theses, Doctoral dissertations).

7. The PubMed database was searched to identify any additional publications appearing during the time that references were being collected. The Related articles option of the program was examined for each new article found. This step updated the ancestry search.

The search produced 130 relevant studies, but only 122 were used in the analyses. Six studies (Butts, Henry, & McLean, 1991; Kohrt, Morgan, Bates & Skinner, 1987; Kohrt, O'Connor & Skinner, 1988; Krahenbuhl, Wells, Brown, & Ward, 1979; Schabort, Killian, St Clair Gibson, Hawley, & Noakes, 2000; Zhou, Robson, King, & Davis, 1997) were dropped because the run was one of several physically demanding activities performed in sequence. Fatigue from the other activities might affect the validity coefficients. The study by Cureton, Sloniger, O'Bannon, Black, and McCormack (1995) was dropped because it pooled data from several investigations. Other reports based on parts of the data included more detail on procedures and participant characteristics. The additional detail was useful for analyzing sources of variation in run test validity. The study by Doolittle and Bigbee (1968) was dropped because it reported a rank-order correlation rather than a Pearson product-moment correlation.

The remaining 122 studies reported results for 156 distinct samples. Because participants in some studies ran more than one distance, a total of 273 correlations were available based on VO\textsubscript{2max} data from 6,140 individuals paired with 10,173 run performances.

Data Extraction

The information extracted from each report consisted of the sample size, the type of run test (fixed-distance or fixed-time), the distance run, the average run time, and the VO\textsubscript{2max}-running
performance correlation. Performance was recorded a number of different ways in different studies. Performance on fixed-distance tests was usually recorded as a run time, but sometimes was represented by average running velocity. Performance on fixed-time tests typically was recorded as distance, but sometimes was reported as a predicted VO$_{2\text{max}}$. VO$_{2\text{max}}$ predictions usually were computed using equations that involved only run distance. However, in some cases the predictions were based on multivariate equations with other predictors such as weight or gender.

Two steps were taken to make sure that correlations were comparable across studies. All of the correlations that used run time as the performance criterion were reversed. For each of the other criteria, higher values indicated better performance. The correlations, therefore, were nearly all positive. When run time was the criterion, lower scores indicated better performance and nearly all correlations were negative. Reversing the sign for these correlations meant that the results from all studies were expressed using coefficients that indicated how strongly VO$_{2\text{max}}$ was related to good performance.

The second step taken to ensure that correlations were comparable restricted the set of results for the estimated VO$_{2\text{max}}$ criterion. Correlations between measured and estimated VO$_{2\text{max}}$ were included in the review only if the prediction equation was a linear function of distance with no other predictors. When these conditions are met, the prediction is merely a linear transformation of distance. Linear transformations of variables produce correlations that are identical to those for the variable itself (Hays, 1963), so the correlation between VO$_{2\text{max}}$ and predicted VO$_{2\text{max}}$ would be identical to the correlation between VO$_{2\text{max}}$ and distance. This identity did not apply in studies where other predictors (e.g., weight, gender) or higher powers of distance (e.g., distance squared) were included in the predictive equation.

A separate record was constructed for each run test in a study. Thus, if a study included 1500-m, 5-km, and 10-km runs, a separate record was constructed for each distance. Sample attributes were duplicated on each record. Each record was treated as a separate case in the analysis. This decision meant that the cases analyzed were not entirely independent, thereby introducing statistical complexities for significance testing (Becker & Schram, 1994). The common meta-analytic practice of averaging effect sizes to produce a single value for each sample was not suitable for the present purposes. Averaging would have prevented meaningful analysis of the relationship between validity and test length.
Data Analysis

Rosenthal and DiMatteo (2001) capture the intended spirit of the present data analysis with two observations: "Meta-analysis is not inherently different from primary data analysis; it requires the same basic tools, thought processes, and cautions" (Rosenthal & DiMatteo, 2001, p. 78). "The best quality scientific exploration is often one that poses unadorned, straightforward questions and uses simple statistical techniques for analysis" (Rosenthal & DiMatteo, 2001, p. 68). A meta-analysis can appear complex because it involves a number of decision points (Wanous, Sullivan, & Malinak, 1989) and because effect sizes are analyzed rather than raw data. However, the essential computational procedures are analogous to familiar procedures for computing descriptive statistics, analysis of variance (ANOVA), and regression. The central components of the procedures in this paper were:

A. Olkin and Pratt's (1958) correction for sample bias in the estimated correlations was applied. Hedges and Olkin (1985) note that this correction is most important when 0.4 # r # 0.6 and sample size is small (e.g., n < 15). The average correlation reported by Safrin et al. (1988) was just above the upper end of this range, and many of the correlations reviewed (66 of 273, 24.2%) were from samples with n # 15. These figures suggested that the unbiased correlations should be used to protect against underestimating the true population correlation.

B. Fisher's r-to-z transformation was applied to normalize the distribution of correlations. The data points analyzed and predicted, therefore, are labeled $z_{Uf(i)}$ as a reminder that they are unbiased, Fisher-transformed estimates of the population correlations for a given sample, denoted by the "i" in the subscript.

C. Each reported correlation was compared to a predicted value (i.e., $z_{Uf(i)} - z_{Uf'}$). The predicted values were familiar elements of standard analysis procedures. For example, the predicted values in one analysis of variance model were the means for all tests of specific distances (e.g., 800 m, 1500 m). The predicted values in another analysis were determined from the regression of $z_{Uf(i)}$ on the logarithm of distance.

D. The difference between the observed and predicted values was standardized. This was accomplished by dividing $z_{Uf(i)} - z_{Uf'}$ by the standard deviation for the transformed correlation (i.e., \(1/(N_i - 3)\)).

E. The standardized value for the difference was squared to produce a $\Pi^2$ with 1 degree of freedom (Hays, 1963).

F. The $\Pi^2$ values for all correlations in the analysis were summed to produce an overall $\Pi^2$ that was the summary fit statistic for the model.
The $\Pi^2$ values for competing models were compared to determine which model best accounted for the observed variation in the correlations. This summary shows that the computations involve differences between observed and predicted values. The differences are directly comparable to the deviations and/or residuals computed for descriptive statistics, ANOVA, or regression analyses of raw data. The statistical comparisons between models are comparable to using incremental variance explained to select a model in primary data analyses.

Meta-analysts must choose between fixed-effects and random-effects models (Hedges & Olkin, 1985; Hedges & Vevea, 1998; Raudenbush, 1994). Fixed-effects models were the starting point for the analyses, but a random-effects model was the end point. Fixed-effects models have smaller error variances than random-effects models (Becker & Schram, 1994; Erez, Bloom & Wells, 1996; Hedges & Vevea, 1998). Smaller error variance means larger standardized differences for fixed-effects analyses than for random-effects analyses. The overall model $\Pi^2$ is the sum of the squared standardized values (Hays, 1963), so underestimating error variance increases $\Pi^2$. This fact makes fixed-effects analyses lenient relative to random-effects models. However, fixed-effects models are a necessary first step in the iterative computation of the random-effects variance estimate in any case. Hedges and Vevea's (1998) procedures were used to compute a random-effects model after using fixed-effects analyses to choose between models. This decision made it possible to compare the models directly because each model was being used to account for the same $\Pi^2$. Hedges and Vevea's (1998) Equation 10 was used to compute the random-effects component of variance following the initial fixed-effects analysis.

Analyses were conducted with the general linear model (GLM) and linear regression procedures in SPSS-PC (SPSS, Inc., 1998a,b). The weighted least squares option in each procedure was used to apply the (n - 3) weight. Using this weighting option, the sums of squares reported in the analysis results are $\Pi^2$ values equal to Hedges' $Q$ (cf., Hedges & Olkin, 1985, pp. 235-241). The GLM procedure was used for analyses involving discrete groups (e.g., males and females) and for multivariate models. Linear regression was used for analyses of nominally continuous variables (e.g., age). Nominally continuous variables were covariates in the multivariate models.

Model Comparison and Selection

Statistical significance tests are an imperfect guide to model selection (Morrison & Henkel, 1970; Harlow, Mulaik, & Steiger, 1997). Even very small effects are statistically
significant when examined in large samples (Rosenthal & Rosnow, 1984). Including weak effects in a model increases parametric complexity with little gain in predictive accuracy. Thus, the question of whether the increase in explanatory power justifies the increased complexity of the model. Identification of a parsimonious model, therefore, involves a tradeoff between explanatory power and complexity (Popper, 1959; Mulaik et al., 1989).

Two steps were taken to foster parsimony. Hoelter’s (1983) critical N, the smallest sample size for which an observed difference would be statistically significant, was applied. If critical N is large, the effect arguably is too small to be important. Hoelter’s (1983) rule of thumb that critical N should be > 200 was adopted to identify effect sizes too small to be practically or theoretically important.

The second protection against unnecessarily complex models was based on goodness of fit statistics for the model (cf., Arbuckle & Wothke, 1999; Bentler & Bonnet, 1980, Bollen, 1989, for discussions of goodness of fit). The Tucker-Lewis index (TLI, Tucker & Lewis, 1973) was adopted as a goodness-of-fit indicator:

$$\text{TLI} = \frac{(\Pi_N^2/df_N - \Pi_M^2/df_M)}{(\Pi_N^2/df_N - 1)}$$

where N indicates the null model and M indicates the alternative model. The expected value of $\Pi$ is 1.00 when chance is the only source of variation, so TLI was the proportion of the greater than chance variation in the observed correlations accounted for by a model. James, Mulaik, and Brett’s (1982) parsimony adjustment then was applied:

$$\text{PTLI} = \text{TLI} \times (df_M/df_N)$$

Basically, PTLI increases when the proportional gain in explanatory power exceeds the proportional decrease in degrees of freedom. Mulaik et al. (1989) explain the rationale for this adjustment in detail.

**Results**

Fixed-distance and fixed-time tests were considered separately. This approach avoided confounding cases in which distance or time was an experimental design variable defining the run test with cases where the same variables were performance indices.

**Fixed-distance Tests**
General Pattern. The LOESS curve (cf., Cleveland, 1979) in Figure 1 (see p. 7) shows the basic pattern of data relating validity to run distance.

![Graph showing relationship between unbiased Fisher-transformed correlation and logarithm of distance.](image)

**Figure 1**

*Validity Coefficients as a Function of Distance*

**Group Classification Models.** Fixed-distance tests were grouped several ways to generate group-based models. These models shared the common characteristic that the grouping procedure would explain the observed variation in validity coefficients only if the runs within a group shared a common value. Fixed-distance tests were classified as short- (<1500 m), middle- (1500-1850 m), or long-distance (>2000 m) runs. One model (S/M/L) treated each category separately. Two other models, (S/M/L and S/ML) explored the effect of treating middle-distance runs as short runs or long runs, respectively.

The most extensive group model consisted of 24 groups. Twenty-two (22) groups were specific run distances (e.g., 400 m, 800 m, 5 km). A separate group was included for any run that had been studied in 3 or more samples. The other two groups in this model consisted of all short (<1500 m, n = 9) and long (>1600 m, n = 9) runs that had been studied in only 1 or 2 samples. This model was labeled the "test-by-test" (TxT) model to emphasize
that individual run tests were treated separately when there was enough data to provide a reasonably stable estimate of the VO$_{2\text{max}}$-running performance correlation.

Table 1. Comparison of Group-based Models

<table>
<thead>
<tr>
<th>Model</th>
<th>df</th>
<th>$\tau^2$</th>
<th>TLI</th>
<th>PTLI</th>
</tr>
</thead>
<tbody>
<tr>
<td>S/ML</td>
<td>1</td>
<td>203.310</td>
<td>.292</td>
<td>.291</td>
</tr>
<tr>
<td>SM/L</td>
<td>1</td>
<td>189.051</td>
<td>.271</td>
<td>.270</td>
</tr>
<tr>
<td>S/M/L</td>
<td>2</td>
<td>229.561</td>
<td>.325</td>
<td>.322</td>
</tr>
<tr>
<td>TxT</td>
<td>23</td>
<td>355.827</td>
<td>.425</td>
<td>.382</td>
</tr>
</tbody>
</table>

Note. S = Short, M = Medium, and L = Long. See text for group definitions. "df" is "degrees of freedom." "TLI" and "PTLI" are the Tucker-Lewis index and the parsimony-adjusted Tucker-Lewis index, respectively. The tabled $\tau^2$s indicate the variation in correlations accounted for by the model. The overall $\tau^2$ was 911.725 with 225 df.

The TxT model clearly was the best group alternative (Table 1). This model was a significant improvement on the next best alternative, the S/M/L model ($\tau^2 = 126.27$, 21 df, $p < .001$). Even allowing for differences in parsimony, the goodness of fit of the TxT model (PTLI = .382) was better than the S/M/L model fit (PTLI = .322). The S/M/L model was significantly better than either dichotomous model ($\tau^2 > 26.25$, 1 df, $p < .001$).

Models with Distance as a Continuous Variable. A second set of models used distance as a continuous variable. These models included simple regression and analysis of covariance (ANCOVA) models. The ANCOVA models tested the hypothesis that variations in the size of the correlations within the 2- and 3-group models could be accounted for by distance. If so, it would be unreasonable to treat the tests within a group as equivalent. Preliminary analyses showed that a logarithmic transformation of distance increased the predictive power of the analyses, so this transformation was used in constructing these models.

The analyses led to a mixed model that regressed validity on distance for shorter runs, but treated longer runs as a single group with a common validity (Table 2). A significant amount of variation in the validity coefficients could be accounted for by regressing $z_{of'}$ on distance (LogDist model; $\tau^2 > 226.80$, PTLI = .324). However, both ANCOVA models improved on this basic regression model ($\tau^2 > 17.25$, 2 df, $p < .001$). The SM/L model was the better alternative between the two ANCOVA models (SM/L PTLI = .359; S/ML PTLI = .338).

The final mixed model was developed because the regression lines were not parallel for the two SM/L groups ($\tau^2 = 15.65$, 1 df, $p < .001$; cf., Walker & Lev, 1953, pp. 390-393, for the
statistical test). The logarithm of distance predicted $z_{UF}$ in the SM group ($\Pi^2 = 69.724$, 1 df, $p < .001$), but not the L group ($\Pi^2 = 0.08$, 1 df, $p > .777$).

Table 2. Models with Distance as a Continuous Variable.

<table>
<thead>
<tr>
<th>Model</th>
<th>Df</th>
<th>$\Pi^2$</th>
<th>TLI</th>
<th>PTLI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log$_{10}$ Distance</td>
<td>1</td>
<td>226.800</td>
<td>.326</td>
<td>.324</td>
</tr>
<tr>
<td>S/ML ANCOVA</td>
<td>3</td>
<td>244.05</td>
<td>.342</td>
<td>.338</td>
</tr>
<tr>
<td>SM/L ANCOVA</td>
<td>3</td>
<td>258.85</td>
<td>.364</td>
<td>.359</td>
</tr>
<tr>
<td>PW</td>
<td>2</td>
<td>258.77</td>
<td>.368</td>
<td>.363</td>
</tr>
</tbody>
</table>

Note. See text for description of models. The within and between values for the PW model indicate the contribution of each model element on total $\Pi^2$ for the SM/L ANCOVA.

The mixed model then was constructed based on the ANCOVA results and Figure 1. The model was:

If distance < 2000 m, $z_{UF}' = (0.225\times LogD) - 0.0036$

If distance $\geq 2000$ m, $z_{UF}' = 0.9026$

where "LogD" was the logarithm of test distance. This mixed model was labeled the "piecewise" (PW) model because it had distinct prediction components for different ranges of distance. The PW model fit the data almost as well as the full SM/L ANCOVA ($\Pi^2 = 258.85$ versus $\Pi^2 = 258.77$). The PW PTLI was higher (.359 versus .363).

Comparing the Best Models

The next analysis compared the TxT and PW models as the best alternatives within the two general categories of model. The TxT model fit the data better ($\Pi^2 > 98.06$, 21 df, $p < .001$), but much of the difference was attributable to the greater parametric complexity of the TxT model. The PTLI values were similar (TxT PTLI = .382; PW PTLI = .363). The sampling variability of PTLI is not known and the specific method of quantifying the parsimony adjustment is only a rule of thumb. Under these conditions, a PTLI difference of .019 was close enough to compare the models further.

Figure 2 compares the model predictions for the 22 run distances that had been studied in 3 or more samples. Differences in the predictions from the two models generally were small. Figure 3 illustrates this fact by expressing the differences as $\Pi^2$s. Because the TxT prediction minimizes the weighted squared error for each run distance, Figure 3 also illustrates the loss in predictive accuracy by replacing the TxT model with the PW model.
The effect of a given run test on the overall $\Pi^2$ difference between the TsT model and PW models depends on the size of the difference and the sample size for the test (Rosenthal & Rosnow,
Figure 2

Piecewise and Test x Test Predictions

Figure 3

Differences Between Model Predictions

Note: Distance is not to scale. Test x Test groups equally spaced.
1984). Figure 3 plots the differences between predictions after translating each into a z-score, then squaring that score. These computations express each difference as a $\Pi'$ with 1 degree of freedom (Hays, 1963). Stavig and Acock's (1976) procedure was used to determine which $\Pi'$s were greater than expected by chance.

Only 14% (3 of 22) of the differences were greater than expected by chance. One significant difference was of limited practical importance because it was the product of a small effect size combined with a large ($N = 650$) sample size. Substantial differences between the models were limited to 2 of 22 run distances. The data for these 2 run distances consisted of 7 correlations involving 225 performance scores. For practical purposes, the two models provided effectively equivalent predictions for $\sim 97\%$ of the data ($3.4\%$ of 208 correlations; $2.7\%$ of 8,505 performance scores) reviewed. Notice also that both runs for which the showed large significant errors in prediction were $\leq 1$ km in length. Thus, neither substantial error was for a run that would be classified as an endurance test in the FW model.

Within-Study Evaluation

The stability of the $\text{VO}_{\text{max}}$-running performance correlation from 2 km on was surprising in light of bioenergetic models. However, the proportion of energy derived from aerobic processes increases relatively slowly for longer runs (Capelli, 1999; di Prampero, et al., 1993; Ward-Smith, 1999). The underlying logic of using bioenergetic models to predict validity trends, therefore, implies that validity will increase slowly for longer runs. If the true validity differences are small, sampling variation and methodological differences between studies could mask the upward trend.

Within-study analyses were conducted to increase the sensitivity of the analyses. Those samples in the data set that performed two or more runs were identified. The $\text{VO}_{\text{max}}$-performance correlations were compared for all pairwise combinations of tests in each sample. Because the people and methods are the same for each correlation in a pair, sampling effects and methods variance are constant. If there is no effect of distance, the comparisons should show that the longer run produced the larger correlation 50% of the time. If the bioenergetic predictions are correct, the longer run should produce the larger correlation more than 50% of the time.

The within-study comparisons were consistent with Figure 1 and the FW model. The correlation for the longer run was larger in 86% (134 of 156) of the pairwise comparisons when at least one run was $< 2$ km. The longer run produced the larger correlation only 54% (22 of 41) of the time when both runs were $\geq 2$ km. The frequency of a larger correlation for the longer run was greater.
than chance for short runs \((z = 8.97, p < .001)\) but not long runs \((z = 0.47, p > .319)\).

**Random Effects Model.** The preceding analyses favored the PW model. Therefore, a random-effects version of that model was computed using Hedges and Vevea’s (1998) procedures:

\[
\begin{align*}
\text{If distance } &< 2000 \text{ m, } z_{\text{r}} = (0.259 \times \log D) - 0.108 \\
\text{If distance } &\geq 2000 \text{ m, } z_{\text{r}} = 0.9518
\end{align*}
\]

The random-effects model produced smaller \(\tau^2\) values than the fixed-effects model. This trend was expected given the larger variance used to standardize differences. The shift to a random-effects model did not change the inferences about the model components. The regression of \(z_{\text{r}}\) on the logarithm of distance still was significant for the shorter runs \((\tau^2 = 27.423, 1 \text{ df, } p < .001)\), but not the longer runs \((\tau^2 = 0.258, 1 \text{ df, } p > .611)\).

The difference between the average value for the shorter and longer runs remained significant \((\tau^2 = 69.776, 1 \text{ df, } p < .001)\). The overall model, therefore, was significant \((\tau^2 = 97.199, 2 \text{ df, } p < .001)\).

**Fixed-time Tests**

A total of 47 fixed-time tests were included in the review. This set included 4 5-min tests, 4 6-min tests, 3 9-min tests, 1 10-min test, 30 12-min tests, and 5 15-min tests. The average validity for the 47 fixed-time tests was \(r = .752\).

Test time, the fixed-time equivalent of test distance for fixed-distance runs, was positively related to correlation magnitude \((\tau^2 = 61.710, 5 \text{ df, } p < .001)\). The average correlations suggested three sets of comparable tests: Set A = (6-min, \(r = .485\)); Set B = (5-min = .659; 9-min, \(r = .645, 10\)-min, \(r = .629\)); Set C = (12-min, \(r = .791; 15\)-min, \(r = .835\)).

A trend toward higher correlations for longer tests was evident. The trend was most evident as a contrast between tests 312 min and tests #10 min. Based on this observation, a model that treated each of the 5 tests as separate groups was compared to two alternatives:

**A. Regression:** The linear regression of \(z_{\text{r}}\) on time was significant \((r = .473, \tau^2 = 51.586, y' = .00137 \times \text{Seconds} + .07905)\).

**B. Dichotomous:** Short (# 10 min; \(k = 12\)) tests were compared to long (\(\geq 12\) min; \(k = 35\)) tests. Differences among short tests were nonsignificant \((\tau^2 = 6.30, 3 \text{ df, } p > .097)\).

Differences among long tests were nonsignificant \((\tau^2 = 2.173, 1 \text{ df, } p > .140)\). The difference between short and
long tests was highly significant ($\chi^2 = 53.232, 1$ df, $p < .001$).

The 5-group model predicted better than the time regression model ($\chi^2 = 10.124, 4$ df, $p < .039$), but did not improve significantly on the dichotomous model ($\chi^2 = 8.478, 4$ df, $p > .075$). Goodness of fit favored the dichotomous model (PTLI = .258) over the regression model (PTLI = .249) and the 5-group model (PTLI = .198).

Boundary Case Analysis for an Endurance Criterion

The PW model and the analyses of fixed-time tests suggested an empirical definition of the term “endurance test.” Setting the criterion of ≥2 km or ≥12 minutes provided a reasonable working definition of an endurance test. The definition treats all tests above the distance/time cutoff as equally valid. All tests below the cutoff have lower validity.

The appropriateness of the proposed boundary criteria was evaluated. Two predictions were made for 4 boundary cases, the 1500-meter, 1-mile, 2-kilometer, and 1.5-mile runs. One prediction was based on the validity-distance regression for runs <1500 m ($z_{UF} = .195\cdot \log_{10}D + .0380$). The second prediction was the average correlation for tests >1.5 miles ($z_{UF} = .8678$). Hoelter’s (1983) critical N was used to evaluate the differences ($z_{UF} - z_{UF}'$). Disch, Frankiewicz and Jackson’s (1975) names for their two running performance factors were adopted to label the two predictions “speed” and “distance,” respectively.

Table 3. Goodness of Fit for Boundary Tests

<table>
<thead>
<tr>
<th>Test</th>
<th>Average $z_{UF}$</th>
<th>Critical N if Classified as:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Speed</td>
</tr>
<tr>
<td>1500m</td>
<td>.7442</td>
<td>512</td>
</tr>
<tr>
<td>1609m</td>
<td>.7317</td>
<td>825</td>
</tr>
<tr>
<td>2000m</td>
<td>1.0167</td>
<td>38</td>
</tr>
<tr>
<td>2414m</td>
<td>1.0754</td>
<td>30</td>
</tr>
</tbody>
</table>

Note. See text for definition of speed and endurance tests.

The evaluations supported the proposed criteria. The critical N for each proposed classification was 2 to 4 times larger than that for the alternative classification. Larger critical Ns indicate better prediction, so the proposed criteria assigned each boundary test to the portion of the model that provided better predictive accuracy. The critical Ns for the 2-km and 1.5-mi tests were low, but larger for their proposed assignment than for the alternative. In these cases, the fit of the model was not as good as one would like, but the initial classification was the lesser of two evils.
Discussion

This review tested the hypothesis that the validity of run tests as indicators of \( VO_{2\text{max}} \) increases continuously with distance. The hypothesis was not supported. Validity increased up to 2 km, then remained stable. For fixed-time tests, validity was stable for runs \( \geq 12 \) minutes. The average validity for longer duration runs was comparable to that for longer distance runs. Given this similarity, an endurance run can be defined as any run \( \geq 2 \) km in distance or \( \geq 12 \) minutes in duration. This definition identifies a set of run tests that all possess the same optimal validity as indicators of aerobic capacity.

The recommended definition of endurance runs involves longer runs than some common testing practices (cf., Baumgartner & Jackson, 1982). However, the definition is consistent with Disch et al.'s (1975) factor analysis of performance for run tests ranging from 50 yards to 2 miles. Two factors, "speed" and "distance," were identified. The authors originally classified a 1-mile run as a distance test, but noted that "... shorter distance tests of 1 mi or less tended to ... [load] on both factors, whereas, the distances longer than 1 mi tended to be unidimensional and loaded almost exclusively on the distance run factor" (Disch et al., 1975; p. 169). The shortest distance exceeding 1 mile in their study was 2.01 km (1.25 miles). Thus, proposed criteria are consistent with at least one prior study.

The proposed time criterion for an endurance test is approximate. The 12-minute run is an endurance test. The 9-minute run is not. The optimum criterion might fall between these two values. However, there is too little data on fixed-time runs between 9 and 12 minutes to set the duration criterion with greater precision. Clarification of this issue could be important because, not distance, is probably the key factor affecting run test validity. For example, Sidney and Shephard's (1977) elderly men and women produced representative validity coefficients for a 12-minute run despite average distances substantially less than 2 km for both groups.

Endurance runs are more valid indicators of aerobic capacity than prior reviews suggest. With the exception of Safran et al.'s (1988) work, the prior reviews suggest validities in the range of \( 0.60 < r < 0.65 \) (Baumgartner & Jackson, 1982; Katch & Henry, 1972; Knapik, 1989). Safran et al. (1988) reported a higher value after correcting for measurement error, but their raw correlations were in the range noted in other reviews. In contrast, this review estimates the validity of endurance run tests at \( r = 0.74 \). The inclusion of shorter runs in the prior reviews is part of the reason for the difference. The analysis of boundary cases showed that even a slight lowering of the criteria
adds run tests with substantially lower correlations, thereby lowering the average.

The proposed endurance criteria do not mean that shorter runs are invalid. The random-effects PW model estimates of validity for shorter runs commonly used to assess aerobic capacity ranged from $r = .543$ for a 600-yard run to $r = .618$ for a 1-mile run. Clearly, these tests are not invalid as the correlations are substantially greater than zero. Shorter tests will be useful for estimating aerobic capacity when validities in this range are acceptable and there is some reason to avoid having the study population run the additional distance required to meet the minimum endurance criterion. However, using a shorter run does imply a substantial drop in validity relative to endurance runs. Also, factor loadings from Disch et al.‘s (1975) analysis suggest that the estimates of aerobic capacity will be moderately contaminated by differences in anaerobic power.

The endurance criteria are linked to the adoption of the PW model as the best model of the run distance and validity. That decision was supported by the parsimony of the PW model. Adopting the TtT model would increase complexity 1150% (from 2 to 23 parameters) to improve predictions for 9% (2 of 22) of the run tests representing ~3% of the total data. The PW model also has clear connections to current theoretical models of running performance. The increasing validity up to 2 km can be explained by bioenergetics. Critical power, anaerobic threshold, and related physiological concepts (Vandewalle, Vautier, Kachouri, LeChevalier, & Monod, 1997; Walsh, 2000) can account for the range of stable correlations. These concepts predict that there is critical velocity that can be maintained for extended periods of time. Optimal running strategy is to maintain a constant pace that is slightly faster so that anaerobic resources are consumed evenly over the course of the run (Fukuba & Whipp, 1999). Thus, each individual should have an approximately constant pace for longer runs that is determined by aerobic capacity and influenced only slightly by other energetic sources. The implication is that all longer runs are primarily manifestations of a single underlying physiological attribute. From statistical perspective, the tests are congeneric (Lord & Novick, 1968) and should have an approximately constant correlation to the criterion.

The TtT model predictions would be hard to explain physiologically. Mechanisms would have to be identified that could account for an up-and-down pattern of validity coefficients. The pattern might be viewed as a combination of a general upward trend with cyclical variation about that trend that damped to very small fluctuations for longer runs. It is not obvious what physiological constructs could be invoked to explain this pattern.
Noting some limitations of this review puts the results in proper perspective. The conclusions apply with greatest certainty to people between 10 and 50 years of age. Only 4 samples in this review fell outside this range. The risks in generalizing beyond this range may be slight; the 3 samples of older individuals (Sidney & Shephard, 1977; Tanaka, Takeshima, Kato, Nihata, & Ueda, 1990) produced correlations comparable to those for younger people. The statistical significance estimates must be interpreted cautiously. Each correlation was treated as an independent observation even though some were not. More complex computations allowing for the dependencies would yield more precise significance estimates (Becker & Schram, 1994; Steiger, 1978). This limitation is mitigated by the fact that model selection ultimately focused on explanatory precision, not statistical significance. Also, the within-study analysis of correlations provided a qualitative test of the model that allowed for dependencies.

The most important limitation of this review is that validity generalization has not been addressed. Validity was stable for longer runs on the average, but there was substantial variation around that average. The variation may indicate that validity is lower for some test populations than for others. Generalizability is critical in the applied use of run tests (Baumgartner & Jackson, 1982; Knapik, 1989; Safrity et al., 1988). This review provides empirical endurance criteria that define a population of run tests that share a common \( \dot{V}O_{\text{max}} \)-running performance correlation. The null hypothesis in generalizability analyses is that different populations of people share a common population correlation. This hypothesis is plausible if run tests are sampled from the population of tests defined by the endurance criteria developed here. The present findings, therefore, provide a starting point for proper selection of correlations suitable for testing generalizability hypotheses. The present findings also identify test type as one factor that affects validity. The average validity of fixed-time endurance tests (\( r = .797 \)) was significantly higher than that of fixed-distance tests (\( r = .718, \chi^2 = 30.65, 1 \text{ df}, p < .001 \)). A companion review (Vickers, in preparation) will use the present findings as a point of departure for a detailed exploration of generalizability issues.

The applied uses of the findings can be illustrated by answering the two questions raised in the introduction. "How long does a run have to be to be valid?" If \( r = .70 \) were the minimum acceptable validity coefficient, the minimum distance would be 2 km. Reducing the distance by as little as 0.4 km (i.e., to 1 mile) would incur a significant loss of validity (\( r = .63 \)). Regarding the second question, "If the current test is 2 km in length, how much will be gained by increasing the distance?", the evidence indicates nothing will be gained. However, they may be some benefit to switching from a fixed-distance test to a fixed-time test. The data also suggest an answer to a third important
applied question, "What is the highest validity that can be achieved with run tests?" The best answer from this review is $r = .80$. If this validity is not acceptable, some other method of estimating aerobic capacity must be used.

Safrit et al. (1988) concluded that their review of the $\text{VO}_{2\max}$-running performance literature provided a framework for future studies. This review has elaborated on the line of study initiated in that paper by developing a quantitative model of the effect of run distance on validity. The model has two important consequences. First, it provides an empirical definition of endurance runs. Second, the model indicates that the validity of run tests as indicators of aerobic capacity is higher than suggested in previous reviews. The empirical definition of an endurance test is a necessary starting point for validity generalization analyses that are the subject of a companion review (Vickers, in preparation). The immediate payoffs from the model developed here include the possibility of making explicit tradeoffs between distance and validity when appropriate. Overall, the PW model should promote better understanding and more effective use of run tests as aerobic capacity indicators.
Footnotes

1Safrit et al. (1988) reported two values, \( r = .771 \) in the text and \( r = .741 \) in Table 1. Whichever value is correct, the analysis procedures corrected for measurement error. The weighted average of the reliability data reported in the paper was \( r_{xx} = .892 \) for run tests and \( r_{yy} = .753 \) for \( \text{VO}_{2\text{max}} \) measurements. Inserting these values into standard equations to correct for measurement error (Hunter, Schmidt, & Jackson, 1982, p. 54-59), the correction procedure can be reversed to yield the uncorrected correlations:

\[
\begin{align*}
I_{xy} &= \Delta_{xy} \cdot \text{SQRT}(r_{xx} \cdot r_{yy}) \\
&= .771 \cdot \text{SQRT}(.892 \cdot .753) \\
&= .771 \cdot .820 \\
&= .632
\end{align*}
\]

or

\[
= .608 \text{ (if } \Delta_{xy} = .741).\]

2The referent for "validity" has been specified because test validity is the appropriateness of the interpretation of test scores (American Psychological Association, 1985). Most tests have more than one interpretation and, therefore, more than one validity. For example, a run test could be interpreted as performance indicator rather than an estimate of aerobic capacity. This review examines run tests as estimates of aerobic capacity or cardiorespiratory fitness. Unless otherwise indicated, that reference is the sole meaning of validity when the term is used in this paper.

3The 2000 meter split point for the group classification may appear too low when examining Figure 1. The graph flattens at a point closer to 2400 meters. This appearance is misleading. LOESS procedures compute the \( y \) value for an \( (x,y) \) pair by taking a weighted average of observed \( y \) values over a range of \( x \) values. The weights are larger for data points near the \( x \) value than for more distant data points (Cleveland, 1979). The procedure is designed to yield a smoother, robust representation of the data. The resulting graph will be misleading if there are real discontinuities in the data such as that embodied in the \( Fw \) model. The LOESS approach will yield an artifactual smooth increase in the curve near the transition point. The curve will be smooth and increasing in the transition region because it averages increasing points below the transition with constant points above. As the weights assigned to points in each domain shift, the curve will increase smoothly. The stable value above the transition point will be reached only when the weights assigned to shorter distances all are near zero. This condition will be satisfied only after the \( x \) value is well above the actual transition point. Thus, a smooth curve from approximately 2.4 kilometers onward indicates a transition point somewhere below
this value. Other aspects of the analysis indicate that 2
kilometers is reasonable from this perspective.

An apparent conflict between the time and distance definitions
of endurance runs should be noted. The average distance covered
in a 12-minute run test is 2.5 km, well above the 2.0-km
criterion. Regressing average time on average distance for fixed-
distance tests, the predicted average time for 2 km is 8:44. This
prediction is well below the 12-minute endurance. Note, however,
that both predicted criteria refer to average values. The more
appropriate reference point might be the time or distance
required for the 95th percentile individual. That reference point
would be more appropriate given that all individuals have to
complete the time or distance in the standard version of the
tests. That reference point would be expected to yield closer
correspondence between the criteria.
References

*Study contributed 1 or more correlations to the meta-analysis.


Distance runs often are used to estimate aerobic capacity. This meta-analysis of 226 correlations from 122 studies involving for fixed-distance run tests produced a quantitative model of run test validity as a function of distance. Validity, the correlation between maximum oxygen uptake (VO$_{2}$max) and running performance, increased with logarithm of distance up to 2 km. Validity was stable at $r = .718$ for runs $\geq$ 2 km. Based on these results, 2 km is an empirical minimum distance criterion for classifying a run as an endurance test. Analysis of a smaller set of 47 correlations for fixed-time run tests indicated that runs $\geq$ 12 minutes had a similar correlation ($r = .797$) and should be considered endurance runs. Runs that meet or exceed these minimum distance and time criteria provide interchangeable estimates of aerobic capacity.