Predicting the effect of defect distributions in the bulk and on surfaces of ceramic materials

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This report results from a contract tasking Imperial College, London as follows: The contractor will investigate and ultimately develop ways to select optimum compositions for materials using atomic scale computer simulation. The particular material systems to be studied are: pyrochlores and fluorites (important in fuel cell and oxygen generator applications and as thermal barrier coatings on turbine blades in jet engines), and the perovskites, important electronic ceramics that also act as catalysts. The work proposed here falls into two categories: those associated with the behavior of defects within the bulk or interior, and those associated with surface structures. The contractor shall: Investigate solution of aloivalent dopant ions in pyrochlore oxides. Predict the extent of disorder in pyrochlore oxides. -Identify compositions that exhibit complex defect behavior in perovskite oxides. Predict surface hydroxylation of yttria stabilized ZrO2. Investigate how surface tension is changed by hydroxylation of ZrO2 surfaces.

EOARD, Materials, Ceramics, Computational Materials, fuel cell, coating

a. REPORT UNCLAS  
b. ABSTRACT UNCLAS  
c. THIS PAGE UNCLAS
Predicting the effect of defect distributions in the bulk
and on surfaces of ceramic materials

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Contract No. : F61775-01-WE064
Date - From : 1st April 2003
            : Until 31st October 2003

Executive Summary
Following on from the work on the pyrochlore materials (A$_2$B$_2$O$_7$), we have extended the contour map approach by application to a wider range of perovskite related materials with the general formula ABO$_3$. Intrinsic defect processes were compared within this extensive range of A$^{3+}$/B$^{3+}$O$_3$ compounds with A cation radii varying from Sc$^{3+}$ to La$^{3+}$ and B cation radii from Al$^{3+}$ to In$^{3+}$. A change in preference between cation antisite, Schottky and oxygen Frenkel disorder are predicted as a function of cation radius and trends have been explained in terms of variations in lattice energy and changes in crystal structure. Of particular interest was the unexpected result that some defect processes mirror changes in crystal structure while others change smoothly across crystal boundaries.

This work fulfils a commitment in the original contract to “Identify compositions that exhibit complex defect behaviour in perovskite oxides.”
Introduction

Due to their many actual and potential technological applications, perovskite materials have been investigated extensively [1-6]. Initially much of this prior work considered 2:4 perovskites, for example the original perovskite compositions Ca$^{2+}$Ti$^{4+}$O$_3$ and the ferroelectric phase Ba$^{2+}$Ti$^{4+}$O$_3$ [7, 8]. Nevertheless ABO$_3$ compositions in which both the A and B cations assume 3+ formal charge states are also of considerable importance with applications as microwave dielectrics [9], sensors [10, 11] and solid oxide fuel cells (SOFC’s) [1]. In all cases the application is facilitated by inducing defects (in some cases via dopanting) within the perovskite lattice.

Here our interest is focused on intrinsically pure materials as a first step towards a broader understanding of defects generally. For example, when the lattice is disordered, defects on the cation sublattice will remain due to their mobility being much lower than those generated on the oxygen sublattice (which are known to be mobile since these materials are used as anodes in SOFC’s due to their high oxygen ion conductivities). One of the more common defect processes on the cation sublattice is the antisite reaction, where the A and B cations are swapped. For materials such as (Ca,Sr)TiO$_3$, where the charges on the A and B cations are not equivalent, a considerable charge redistribution will be introduced into the lattice with intense associated strains. An additional factor contributing to the lattice strain is the significant size difference between the A and B cations.

Here we extend the studies of disorder processes in pyrochlores to the perovskites by considering ABO$_3$ materials in which the A and B cations both assume formal 3+ valence states. One of the primary motivations for studying these 3:3 compounds is
that cation disorder does not lead to a charge imbalance. It may be that the equivalence of the charge states leads to lower disorder energies; however, for many perovskites we are still faced with a significant cation size difference.

We will consider an exceptionally broad range of ABO$_3$ compositions with the A cation ranging from Sc$^{3+}$ (1.05Å) to La$^{3+}$ (1.34Å) and the B cation ranging from Al$^{3+}$ (0.535Å) to In$^{3+}$ (0.8Å). Consequently, at one extreme of the compositional range the A and B cations are of very similar size. Such A$^{3+}$B$^{3+}$O$_3$ compositions no longer exhibit a perovskite like structure, but take on the cubic bixbyite structure.

In this study, atomic scale computer simulation techniques are used to predict the structures and energies associated with defect formation in these 3:3 compounds. Those structures which exhibit larger energies for disorder processes will assume a greater residual or retained energy upon disorder and on this basis are assumed less tolerant of such defects [12]. Such an approach has proved successful in earlier work at predicting the relative structure boundary between pyrochlore (in which the cations are ordered) and fluorite (in which the cations are disordered) [12]. The approach was also successful in predicting the order / disorder transformation in A$_2$H$_2$O$_7$ compositions [13] and nonstoichiometry across the entire A$_2$B$_2$O$_7$ compositional range [14].
**Methodology**

The calculations presented here are based upon a classical Born-like description of an ionic crystal lattice [15]. The interatomic forces acting between ions are resolved into two terms: long-range Coulombic, which were summed via the Ewald method [16], and short-range pair terms, which were modelled using parameterised Buckingham pair potentials [17]. The perfect lattice is defined by tessellating the unit cell throughout space using periodic boundary conditions as defined by the crystallographic lattice vectors. The lattice energy ($E_L$) can then be expressed as follows:

$$U_L = \frac{1}{4\pi\varepsilon_0} \sum_{i \neq j} \frac{q_i q_j}{r_{ij}} + Ae^{-\frac{r}{\rho_i}} - \frac{C}{r_y^6}$$

**Equation 1**

where $A_{ij}$, $\rho_{ij}$ and $C_{ij}$ are the adjustable parameters, $r_{ij}$ are the interionic separation and $q_i$, $q_j$ are the charges on ions $i$ and $j$ respectively. The parameters of the short-range potential were derived using a multi-structure-fitting procedure, described elsewhere [18, 19], and are reported in Table 1.
Table 1. Potential parameters used[19, 20].

<table>
<thead>
<tr>
<th>Species</th>
<th>A (eV)</th>
<th>ρ (Å)</th>
<th>C (eVÅ^6)</th>
</tr>
</thead>
<tbody>
<tr>
<td>O^{2-} - O^{2-}</td>
<td>9547.96</td>
<td>0.2192</td>
<td>32</td>
</tr>
<tr>
<td>Al^{3+} - O^{2-}</td>
<td>1365.79</td>
<td>0.30096</td>
<td>2.538</td>
</tr>
<tr>
<td>Cr^{3+} - O^{2-}</td>
<td>1452.28</td>
<td>0.30918</td>
<td>4.472</td>
</tr>
<tr>
<td>Ga^{3+} - O^{2-}</td>
<td>1456.72</td>
<td>0.30988</td>
<td>4.616</td>
</tr>
<tr>
<td>Fe^{3+} - O^{2-}</td>
<td>1478.98</td>
<td>0.31306</td>
<td>6.960</td>
</tr>
<tr>
<td>Sc^{3+} - O^{2-}</td>
<td>1587.95</td>
<td>0.32190</td>
<td>8.143</td>
</tr>
<tr>
<td>In^{3+} - O^{2-}</td>
<td>1595.65</td>
<td>0.32960</td>
<td>7.402</td>
</tr>
<tr>
<td>Lu^{3+} - O^{2-}</td>
<td>1561.36</td>
<td>0.33854</td>
<td>10.01</td>
</tr>
<tr>
<td>Yb^{3+} - O^{2-}</td>
<td>1616.68</td>
<td>0.33798</td>
<td>13.34</td>
</tr>
<tr>
<td>Er^{3+} - O^{2-}</td>
<td>1678.21</td>
<td>0.33781</td>
<td>10.34</td>
</tr>
<tr>
<td>Y^{3+} - O^{2-}</td>
<td>1721.23</td>
<td>0.33821</td>
<td>10.29</td>
</tr>
<tr>
<td>Gd^{3+} - O^{2-}</td>
<td>1868.75</td>
<td>0.33880</td>
<td>11.62</td>
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<td>Eu^{3+} - O^{2-}</td>
<td>1886.71</td>
<td>0.33975</td>
<td>11.997</td>
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<td>Sm^{3+} - O^{2-}</td>
<td>1944.44</td>
<td>0.34080</td>
<td>12.49</td>
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<td>Nd^{3+} - O^{2-}</td>
<td>1979.11</td>
<td>0.34148</td>
<td>13.07</td>
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<td>Pr^{3+} - O^{2-}</td>
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<td>13.83</td>
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<td>Ce^{3+} - O^{2-}</td>
<td>2034.18</td>
<td>0.34380</td>
<td>15.86</td>
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<td>Tb^{3+} - O^{2-}</td>
<td>1818.00</td>
<td>0.33845</td>
<td>14.33</td>
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<tr>
<td>Dy^{3+} - O^{2-}</td>
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<td>0.33770</td>
<td>10.94</td>
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<tr>
<td>Ho^{3+} - O^{2-}</td>
<td>1726.29</td>
<td>0.33776</td>
<td>10.72</td>
</tr>
<tr>
<td>La^{3+} - O^{2-}</td>
<td>2051.32</td>
<td>0.34585</td>
<td>15.51</td>
</tr>
<tr>
<td>Pu^{3+} - O^{2-}</td>
<td>1152.00</td>
<td>0.37480</td>
<td>12.10</td>
</tr>
</tbody>
</table>

Table 2. Shell Parameter for O^{2-}[19, 20].

<table>
<thead>
<tr>
<th>Species</th>
<th>Y (e)</th>
<th>k (eVÅ^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>O^{2-}</td>
<td>-2.04</td>
<td>6.3</td>
</tr>
</tbody>
</table>
In order to investigate the radiation tolerance of the perovskite materials, lattice defects must be considered, and their relative energies assessed. However, defect energies involve a contribution due to lattice relaxation. This relaxation is greatest close to the defect. Therefore, the lattice is partitioned into spherical, concentric regions [21]. The defect is placed at the centre of Region I and the ions are relaxed explicitly using a Newton-Raphson procedure. Region IIa is an interfacial region in which the forces between ions are determined via the Mott-Littleton approximation [21, 22] and all ions are relaxed in a single step, whilst the interaction energies between the ions in region IIa and region I are calculated explicitly. Finally, the outer region IIb is effectively a point charge array that provides the Madelung field of the remaining crystal. The relaxation energy of region IIb is approximated via the Mott-Littleton approximation [23]. In these calculations, the radius of Region I is 10 Å and that of Region IIa is 31 Å. All calculations were carried out using the GULP code [24, 25].

The electronic polarisability of oxygen ions is accounted for via the shell model [26]. For the purposes of this study we have used a massless shell with charge $Y = -2.04\, |e|$ is coupled to a core of charge $X = +0.04\, |e|$, via an isotropic harmonic spring with force constant, $k = 6.3\, eVÅ^{-2}$. 
Results and Discussion

Crystallography

Our traditional view of the perovskite lattice is that it consists of small B cations within oxygen octahedra, and larger A cations which are XII fold coordinated by oxygen. This structural family is named after the mineral CaTiO₃ which exhibits an orthorhombic structure with space group Pnma [7]. For the $A^{3+}B^{3+}O_3$ perovskites the most symmetric structure observed is rhombohedral $R\overline{3}c$ (e.g. LaAlO₃) which involves a rotation of the BO₆ octahedra with respect to the cubic structure. However, this distortion from the perfect cubic symmetry is slight [27].

One measure of the propensity for a composition to adopt a high symmetry structure is the classical tolerance factor, $t$. This is defined in equation 2 where $R_A$, $R_B$, and $R_O$ are the relative ionic radii of the A site cations, B site cations, and oxygen ions respectively [28].

$$t = \frac{R_A + R_O}{\sqrt{2(R_B + R_O)}}$$

Equation 2

The tolerance factor will be equal to 1 if the A and B cations fit exactly into a perfect cubic packing of oxygen octahedra. It is therefore not surprising that LaAlO₃ adopts the highly symmetric $R\overline{3}c$ structure since its tolerance factor is 1.00, based on the appropriate VI and XII coordinate radii of Shannon [29]. As the A cation radius decreases and/or B cation radius increases, the tolerance factor decreases. In the perovskite structure, this is associated with the octahedral tilting to yield lower symmetry arrangements which, in the first instance, gives rise to an orthorhombic
structure with space group Pnma. Even greater deviations lead to a structure with hexagonal P63cm crystallography [30]. In this final so-called perovskite variant, the distortions are so great that the A cations are now essentially VII coordinate and the B cations are V coordinate. As such it is not clear that this so-called perovskite is very perovskite like!

Beyond this hexagonal regime, all resemblance to the perovskite structure is lost and a cubic bixbyite is formed with Ia3 symmetry. Here the A and B cation radii are very similar, both cation sites are VI coordinated by oxygen. Although dissimilar to perovskite, it is possible to consider bixbyite in terms of a defective fluorite structure [31].

In order to elucidate trends, we must compare all compositions in a single figure. This can be achieved if the A cations are ordered by size (assuming the XII coordinate radii values throughout) along an x-axis and the B cations (using the VI coordinate values) along a y-axis, thereby forming a 2D grid of compounds. Such a plot is shown in figure 1 for all 96 compounds for which calculations were performed. Of course, for the P63cm and Ia3 structures, the cations are not XII and VI coordinated, however to allow for comparison the XII and VI coordinate radii are used throughout. In this case therefore, the radii simply represent an order parameter.

The lattice energy for each compound was calculated according to equation 1, assuming each of 17 possible crystal structures reported in the literature for materials with the BO3 stoichiometry (including the four mentioned above). From these data the lowest lattice energy is identified for each compound so that an energy value is
assigned to each composition. Each composition is also identified in figure 1 by a symbol which indicates its lowest energy structure (e.g. a square for bixbyite etc.). Lattice energy contours were then generated using software [32], which connects equal energy values over the cation radii surface. Such maps facilitate comparisons and allow identification of compositional ranges that are of particular significance. In this case it is at once clear that the compounds fall into four groups: rhombohedral R̅3c, orthorhombic Pnma, hexagonal P63cm, and bixbyite Ia3. In this regard it is important to note that although 17 different crystal structures have been reported for ABO3 compounds in general, some have only been reported for A2+ B4+O3 materials and others represent only slight distortions from those already mentioned.

Our predictions of structural types are in overall agreement with experimental data and are consistent with changes in the tolerance factor (see figure 2). In particular, where we predict an orthorhombic structure, experimental structures are known to be orthorhombic in most cases. The same holds true for the hexagonal and rhombohedral structures. However, within the orthorhombic and hexagonal regimes, certain compounds are reported experimentally to exhibit slight variations from Pnma and P63cm respectively. Furthermore, a few compositions in the centre of the map, such as YFeO3, do not form an ABO3 material, but disproportionate into garnet structures.

Disorder Processes
Once the lowest energy lattice structure has been identified, the individual component defect energies were calculated. Then each compound can be assigned Schottky, oxygen Frenkel or antisite defect process energies by following the total defect processes described in equations 3, 4 and 5 below.
\[ "null" \rightarrow V_A^\text{III} + V_B^\text{III} + 3V_O^\text{**} \quad \text{Equation 3} \]

\[ O_O^X \rightarrow O_i^{\prime} + V_O^{**} \quad \text{Equation 4} \]

\[ A_A^X \rightarrow A_i^{***} + V_A^{\text{III}} \quad \text{Equation 5} \]

The calculated values for A and B cation Frenkel energies are far higher than those for Schottky, oxygen Frenkel and antisite reactions, and as such will not be considered further. In a similar manner as described for perfect lattice energies, defect process energies can be represented over the full compositional range on an energy contour map (see figures 3, 4 and 5 which use the same energy contour interval). Low energy regions identify compounds for which the defect process is more favourable. In order to allow for comparison between the different defect reactions, the energies presented are normalised per defect, as dictated by a mass action analysis [33], i.e. the Schottky process has a normalisation factor of 5, whilst the antisite and oxygen Frenkel processes have normalisation factors of 2.

Returning to the Schottky, oxygen Frenkel and antisite reactions, comparing figures 3, 4 and 5, it is at once apparent that the Schottky and oxygen Frenkel disorder processes show less variation in energy as a function of cation radii than the antisite process. Although the tolerance factor was originally derived to predict the distortion of a perovskite lattice from an idealised cubic structure, we can also use it to understand the variation exhibited by the antisite energy. This is because the tolerance factor is actually a relative measure of the difference in size of the A and B cations and by inference how much distortion would be necessary to accommodate an A cation at a B
site and vice-versa (i.e. as in the antisite reaction). In this regard, we find it convenient to quantify this for the perovskite compositions alone, such that low t values (i.e. less than 0.8) indicate that the cations fit fairly well in each others sites, while high t values (i.e. greater than 0.8) suggest that they fit rather less well. Thus the value for a perfect cubic perovskite (i.e. 1) would imply a high antisite energy. By comparing figures 2 and 5, it is clear that there is an excellent correlation between our calculated antisite energy and the tolerance factor.

The smaller predicted variation in Schottky energy as a function of cation radius is a consequence of competing factors. In the Schottky reaction (equation 3) the displaced ions form new lattice and as such, the lattice energy and hence its variation with component cation radii is an important factor. This was shown in figure 1 and clearly the lattice energy gain is greatest for compositions in the bottom left hand corner. The second term concerns the energy to form vacancies. Higher energies (less favourable) will result in materials with higher Madelung or electrostatic energies. Although these vary somewhat between structure types, values principally increase as the interatomic separation decreases. As such we expect higher energies in the bottom left hand corner, i.e. the opposite variation observed with the lattice energy (see figure 1). These electrostatic terms are therefore working in opposition, and the net effect is a smaller variation in Schottky energy as a function of cation radii. Contributions from the short range pair energies now become important. Consequently structure type boundaries where there is a change in ion coordination should show up in the Schottky energy map. In figure 3, we show evidence of such a change between Pnma (VI, XII) and P63cm (V, VII) but not R 3c (VI, XII) to Pnma (VI, XII).
By comparing the results in figures 3 and 5 it is at once evident that there is a change in lowest disorder process energy from Schottky to antisite as a function of the cation radii. If we express this in terms of the tolerance factor, the swap-over occurs at a t value between 0.99 and 0.98 with the antisite reaction dominant for all lower values. Thus, only in a small portion of the cation radii space (i.e. at the bottom right) does Schottky disorder dominate over antisite. Furthermore, in this region, the difference in process energies is not great, and thus materials such as LaAlO$_3$ should exhibit complex defect equilibria. We can also compare the oxygen Frenkel and antisite energies. The oxygen Frenkel energy decreases somewhat as the A cation radius increases and the B cation radius decreases, in a similar manner to the antisite process energies. The oxygen Frenkel energy decreases somewhat as the A cation radius decreases and the B cation radius increases, in a manner similar to the antisite process. Although it does drop to a value considerably below the Schottky for a majority of the compositional range, the oxygen Frenkel energy does not decrease to the same extent as the antisite and is never the dominant defect process. Again we see some evidence of the Pnma to P6$_3$cm structure change.

Comparison to Pyrochlore/Fluorite

The perovskite defect process energies can now be compared to the equivalent lowest energy defect process energies in other materials. Here we can make that comparison to the fluorite and pyrochlore oxides investigated previously [12, 19]. In this case, the antisite energies of the perovskites are well above those for the zirconium containing pyrochlore/fluorite materials (e.g. Er$_2$Zr$_2$O$_7$ (0.6 eV) and Gd$_2$Zr$_2$O$_7$ (1.8 eV) [12]). As such, only selected P6$_3$cm perovskites will exhibit defect concentrations as high as the zirconate pyrochlores. On the other hand, the titanate pyrochlores exhibit antisite
defect energies of typically 2.9 eV which is equivalent to the lowest energy for the Pnma perovskites.

The oxygen Frenkel defect energies for the perovskites (figure 4) are again higher than those for the pyrochlores. For example, the zirconate pyrochlores Er₂Zr₂O₇, Gd₂Zr₂O₇ exhibit oxygen Frenkel energies of 2.5 eV and 2.0 eV respectively [19], both being lower than any of the perovskite materials. However, the titanate pyrochlores have values that are similar to the Pnma perovskites, for example, Gd₂Ti₂O₇ has an oxygen Frenkel energy of 5.6 eV [19]. Consequently, values for the bixbyites, which are as low as 3 eV, compare favorably to the titanate pyrochlores and are not significantly higher than the zirconates.

Up to this point we have suggested a model that considered only isolated defects. However, the stability of such defects depend not only on their individual energies, but also on the interactions between them. This is characterised by the reduction in formation energy when the defects are associated (known as the binding energy). The work on pyrochlores considered the representative defect cluster \( \{A^+_b : B^+_A : V^+_o : O^-\}^x \), a combination of antisite and oxygen Frenkel reactions where the defects are in their nearest neighbour positions [19]. Interestingly, when different geometries of this cluster are investigated for pyrochlore, the oxygen Frenkel component sometimes self annihilates around the cation antisite pair. Such behaviour was not observed in equivalent perovskite clusters. This may in itself be a significant difference between pyrochlores and perovskites in regard to their ability to accommodate large defect populations. Nevertheless, in order to compare equivalent defect clusters, here we simply compare energies for adjacent antisite pairs.
\( \{A_b^X : B_a^X\}^X \) (see table 3 for examples). Critically, for perovskites the value when the defects are associated (i.e. clustered) are only modestly less than when the defects are isolated).

**Table 3. Comparison of the total defect energies for isolated defects and clusters for different compositions of perovskite and pyrochlore oxides. N.B. the energies in this table have not been normalised to facilitate comparisons.**

<table>
<thead>
<tr>
<th>Total Defect Energy (eV)</th>
<th>( {A_b^X : B_a^X}^X )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isolated</td>
<td>Clustered</td>
</tr>
<tr>
<td>Perovskite</td>
<td></td>
</tr>
<tr>
<td>GdAlO(_3)</td>
<td>8.20</td>
</tr>
<tr>
<td>LaAlO(_3)</td>
<td>11.98</td>
</tr>
<tr>
<td>GdFeO(_3)</td>
<td>4.24</td>
</tr>
<tr>
<td>LaFeO(_3)</td>
<td>7.44</td>
</tr>
<tr>
<td>Pyrochlore [2]</td>
<td></td>
</tr>
<tr>
<td>Gd(_2)Ti(_3)O(_7)</td>
<td>6.09</td>
</tr>
<tr>
<td>La(_2)Ti(_3)O(_7)</td>
<td>5.94</td>
</tr>
<tr>
<td>Gd(_2)Zr(_2)O(_7)</td>
<td>3.68</td>
</tr>
<tr>
<td>La(_2)Zr(_2)O(_7)</td>
<td>4.52</td>
</tr>
</tbody>
</table>

Conversely, in pyrochlore materials, cluster formation values are considerably less than for isolated defects (again see table 3). The larger binding energy for pyrochlorites now means that we see a significant difference between the antisite energy for GdFeO\(_3\) compared to lower zirconate pyrochlore values. The other perovskites maintain their higher defect process energies.

Clearly, for the pyrochlore materials, these antisite defects are more strongly bound than for the perovskite materials. This may well imply that in perovskites, as the defect concentrations increase, the retained energy increases more quickly. On this basis, all the perovskites should accommodate lower defect concentrations than pyrochlorites. However, to be definitive would require better analysis probably using a molecular dynamics approach (because of the great number of cluster configurations).
Conclusion

As a consequence of the broad compositional range of ABO$_3$ materials considered, the assumed crystal structures of individual compositions varies considerably from rhombohedral R$\overline{3}$c when the A and B cation radii are most different, to orthorhombic Pnma, to hexagonal P6$_3$cm, and finally to the cubic bixbyite Ia3 as the constituent cation radii converge. Despite this drastic change in the crystallography of the system, a smooth transition in the lattice energy across these structural boundaries is predicted (see figure 1).

As a first approximation to understanding the variation in crystal structure, the classical tolerance factor provides an important benchmark. The tolerance factor follows the changes remarkably well and infers that the atomistic simulation results are in agreement with classical perovskite theory (see figure 2).

The structural changes also manifest themselves in the defect chemistry of these ABO$_3$ materials. The defect process energies of the Schottky and oxygen Frenkel reactions show abrupt changes in compositional regions (i.e. cation radii space) associated with changes in crystal structure (see figures 3 and 4). Conversely in the antisite reaction energy decreases smoothly and rapidly as a function of the component cation radii across crystal structure boundaries (see figure 5).

For compounds with large A cation radii and small B cation radii (i.e. the lower right hand corner of the maps) the Schottky defect reaction is the dominant (lowest energy) process, whereas for the rest of the compositional range the antisite process dominates. However, if one considers defect processes on just the oxygen sublattice,
there is also a change over in the dominant reaction from Schottky to oxygen Frenkel that occurs close to the orthorhombic Pnma to hexagonal P6\textsubscript{3}cm crystal structure boundary. Such process mechanisms are important because such defect reactions on the oxygen sublattice control the equilibria which provide the defects that mediate transport mechanisms of oxygen through the lattice.

In an attempt to understand the interplay between defects on the cation and anion sublattices, defect clusters have been considered that combine a cation antisite defect pair with an oxygen Frenkel pair. The clusters in perovskite have been compared to equivalent clusters investigated previously in the pyrochlore materials. One of the startling differences between the two structures is that within the pyrochlore materials, different geometries of the cluster lead to the annihilation of the oxygen Frenkel pair vastly reducing the energy of the cluster. Such mechanisms were not seen in the perovskite materials. Partly as a consequence, a different cluster formed from an adjacent antisite defect pair was considered to allow for comparison between the perovskite and pyrochlore. Here, the energies for clustered defects in the perovskites are only modestly lower than when the defects are isolated, conversely, the equivalent cluster within the pyrochlore materials is much lower in energy than the isolated defects. As such the antisite defects are more strongly bound together in the pyrochlore material than the perovskite. This implies that as the defect concentrations increase within perovskites, the retained energy increases rapidly and as such the perovskites should not be able to accommodate such large defect concentrations as the pyrochlore material.
References


Figure 1. Lattice energy (eV) contour map.
Figure 2. Classical Tolerance Factor variations as a function of cation radii.

Figure 3. Schottky reaction energy Contour map.
Figure 4. Oxygen Frenkel reaction energy contour map.

Figure 5. Antisite reaction energy contour map.
(1) In accordance with Defense Federal Acquisition Regulation 252.227-7036, Declaration of Technical Data Conformity (Jan 1997),

"The Contractor, Imperial College, hereby declares that, to the best of its knowledge and belief, the technical data delivered herewith under Contract No. F61775-01-WE064 is complete, accurate, and complies with all requirements of the contract.

DATE: 29th Sept 2003
Name and Title of Authorized Official: [Signature]

(2) In accordance with the requirements in Federal Acquisition Regulation 52.227-13, Patent Rights—Acquisition by the U.S. Government (Jun 1989),

(A) "Disclosures of all subject inventions as defined in FAR 52.227-13 have been reported in accordance with this clause."
Or,
(B) "I certify that there were no subject inventions to declare as defined in FAR 52.227-13, during the performance of this contract."

DATE: 29th Sept 2003
Name and Title of Authorized Official: Prof. ROBIN W. GRIMES [Signature]