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DEPENDENCE OF SOLAR-THERMAL ROCKET PERFORMANCE ON CONCENTRATOR PERFORMANCE

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TRACT

This paper introduces some performance parameters relevant to rocket propulsion and shows how these parameters impact on a rocket thruster powered by concentrated solar energy. Solar-Thermal Propulsion is a promising concept that could double spacecraft pay-load. Thrust and specific impulse (Isp) are key performance indicators. The propellant usage efficiency, defined as the ratio of thrust to propellant flow rate, is discussed. Elementary heat transfer theory is used to analyze the upper limits in thrust and Isp that can be achieved. The configuration of a solar rocket that can perform an orbit transfer or other space missions is discussed. The basic geometry of off-axis lenticular concentrators is discussed along with their concentration performance. An example for an 25 kW off-axis concentrator is discussed.

The propellant must be heated to high temperatures to take advantage of its light weight. Thermodynamics allows temperatures approaching that of the Sun's surface (about 5800 K). This is well above the temperature achievable by practical large scale concentrators. It is also well above any material's melting or boiling point. Therefore, the propellant temperature is limited only by the performance of the concentrator system and/or the breakdown temperature of the materials making up the thruster.

The purpose of this paper is to give a feeling for the concentrator performance level needed to make this propulsion concept useful. This paper introduces some basic propulsion concepts. This basic prerequisite is necessary to show how concentrator behavior affects the performance of a solar rocket. Some concentrator basics are also included. Upper-limits are defined for performance of the solar rocket and compared with conventional rocket designs. The most popular configuration for a solar powered rocket is described and discussed. The geometry and performance of a specific type of off-axis paraboloid is discussed. Finally, recent concentrator structure development is reviewed briefly.

RODUCTION

Solar Engineering – Vol. 2
ASME 1995
BASIC PROPULSION CONCEPTS

Rocket thrusters produce thrust by throwing mass, called the propellant, out a nozzle. Newton’s second law gives the resulting thrust:

\[ F = \frac{dp}{dt} = m \frac{dv}{dt} + v \frac{dm}{dt} \]  

where \( p \) is the momentum of the propellant, \( v \) is the velocity of the propellant, and \( m \) is the mass of the propellant. Once the propellant has left the nozzle, and it is no longer accelerating, \( \frac{dv}{dt} \) is zero. Therefore, the thrust is equal to the propellant mass flow rate out the nozzle times the final velocity of the propellant.

The two most important propulsion parameters are a rocket’s thrust \( F \) and specific impulse \( I_{sp} \). Thrust is commonly referred to by the acceleration it will produce in terms of \( g \), the acceleration due to gravity at Earth’s surface. High thrust, greater than 1\( g \), is required to get a spacecraft off the Earth’s surface. A 1\( g \) thrust force is equal to the total weight of the rocket, including payload and propellant. In the weightlessness of orbit very low thrust can be used.

The specific impulse \( I_{sp} \) of a thruster is defined as the thrust divided by the mass flow rate out the nozzle and is a measure of how efficiently propellant mass is used. \( I_{sp} \) is measured in meters per second (m/s) and in seconds (s) (the latter is actually thrust divided by weight flow rate).

It is desirable to maximize the \( I_{sp} \). The payload that can be carried by a thruster can be increased by increasing the \( I_{sp} \); or, less propellant is needed to boost the same payload if the thruster’s \( I_{sp} \) is increased. This latter advantage can allow a payload to be carried on a smaller booster from the Earth’s surface, which will typically save many tens of millions of dollars. The former advantage can enable the delivery of payloads that could not otherwise be delivered on existing spacecraft.

The specific impulse is proportional to the square root of the propellant initial temperature \( T \) divided by the molecular mass \( m \) of the propellant.

\[ I_{sp} \propto \left( \frac{T}{m} \right)^{1/2} \]  

This is a simplified but still the dominating relationship for \( I_{sp} \) (Sutton, 1992). For molecular hydrogen, an \( I_{sp} \) of 9800 m/s (1000 s) roughly corresponds with temperatures of around 3500 K, 8330 m/s (850 s) with temperatures of around 2500 K. Conventional rockets have \( I_{sp} \) between 1960 and 4400 m/s, (200 and 450 s).

One other important propulsion system parameter is the total thruster mass. If the total mass of a solar thruster with concentrator is too great, then there is nothing to be gained by increasing \( I_{sp} \) since the decrease in propellant mass is offset by increased thruster mass. Concentrator support structures must be lightweight and still stiff enough to maintain high solar concentration.

BASIC SOLAR CONCENTRATION CONCEPTS

We receive about 1350 watts per square meter (W/m\(^2\)) from the sun at our position in the vicinity of Earth. From our position, the mean angular diameter of the sun is 9.3 milliradians, or about 0.53 degrees. The irradiance, or power per unit area of the solar surface is about 63 \( \times \) 10\(^6\) W/m\(^2\). This is consistent with a surface temperature of about 5780 K. By the time sunlight reaches Earth, its intensity (W/m\(^2\)) is reduced by a factor of about 46,000, which is the ratio of the irradiance at the Sun’s surface to the irradiance at Earth’s orbit, 1350 W/m\(^2\).

The function of a concentrator is to take solar radiation from the small patch of sky occupied by the sun and concentrate it into as small a spot, the focal point, as is possible. Ultimately, the maximum temperature achievable by a concentrator is the Sun’s surface temperature, or 5780 K. This is essentially a statement of the second law of thermodynamics; for two objects in thermal contact, energy always flows from the hotter object to the cooler. An ideal concentrator gives perfect thermal connection between the solar surface and the focal point.

The ideal concentrator, by reaching solar temperatures, puts the focal point at the solar surface as far as thermodynamics is concerned. An observer on either the sun or the focal point will see sunlight over 2\( \pi \) steradians (one hemisphere). Therefore, an alternate and equivalent function of a concentrator is to fill the view from the focal point with as much sunlight as is possible.

The power emitted by a surface per unit area per unit steradian is defined as the radiance \( \frac{dL}{d\Omega} \). The radiance of the sun is 63 \( \times \) 10\(^6\)/\( \pi \) or about 20,000,000 watts per square meter per steradian (W/m\(^2\)sr). From Earth the solid angle subtended by the Sun is \( \pi \sin^2 \theta_{\text{sun}} \), where \( \theta_{\text{sun}} \) is the half angle of the sun, or 9.3/2 milliradians. The power \( P \) received by an area \( A \) is:

\[ P = \Omega A \frac{dL}{d\Omega} \]  

where \( \Omega \) is the solid angle of the radiating source as viewed by the area \( A \). Therefore, a patch of area one meter square will absorb \( 20 \times 10^6 \times \pi \sin^2 \theta_{\text{sun}} \times 1 \text{m}^2 \) or about 1350 W/m\(^2\) as stated earlier. On the surface of
\( \theta_{\text{sun}} \) is \( \pi/2 \) giving \( 63 \times 10^6 \) watts on the same meter.

The radiance \( \frac{I}{d\Omega} \) of the sun (or any other uniformly emitting object) can never be increased by reflection action through an optical system (This is again its the second law of thermodynamics). Therefore, only way to increase absorbed power per unit time the focal point of a concentrator is to increase the solid angle \( \Omega \) of the sun as observed from that focal point. This is the same as filling up the sky with concentric spheres and the concentrator surface with sun. The practical result of this fact is that to achieve maximum intensities or temperatures the concentrator system must fill more of the sky, as observed from the focal point with sunlight. The other result of this a restatement of the second law of thermodynamics: maximum intensity or temperature is achieved if the hemisphere observed by the focal point is filled with incident sunlight (as might be well on the sun). A concentrator effectively puts the focal point in live equilibrium with the Sun's surface.

A solid angle of a concentrator system can be calculated by:

\[
I(\theta_{\text{rim}}) = \int_0^{2\pi} d\phi \int_0^{\theta_{\text{rim}}} d\theta \frac{dI}{d\Omega} \cos \theta \sin \theta
\]

where \( I(\theta_{\text{rim}}) \) is the intensity at the focal point from a concentrator that has a rim half angle of \( \theta_{\text{rim}} \). The radiance or power per unit area per unit solid of the sun, \( 20 \times 10^6 \) watts per meter squared per radian. Spherical coordinates are used and the concentrator rim is assumed to have rotational symmetry about the \( z \) axis. Since the intensity of the solar disk is uniform, \( \frac{dI}{d\Omega} \) is constant here:

\[
I(\theta_{\text{rim}}) = 2\pi \int_0^{\theta_{\text{rim}}} d\theta \frac{dI}{d\Omega} \cos \theta \sin \theta
\]

and

\[
I(\theta_{\text{rim}}) = \frac{dI}{d\Omega} \pi \sin^2 \theta_{\text{rim}}
\]

The limit where \( \theta_{\text{rim}} \rightarrow \pi/2, \Omega \rightarrow \pi \) steradians in the \( 2\pi \) steradians in a hemisphere. This is the surface receiving the radiation projects an \( A \cos \theta \) and for large \( \theta \) the power received per unit time is reduced by \( \cos \theta \) (as seen in Equation 4). The maximum solid angle available for radiation on a flat surface is only \( \pi \) steradians. The solid angle of the sun is \( \pi \sin^2 \theta_{\text{sun}} \) as stated earlier. Equation 6 also works he Sun when \( \theta_{\text{rim}} \rightarrow \theta_{\text{sun}} = 9.3/2 \) milliradians as previously.

The geometric concentration ratio is defined to be the shadow area of the collecting optics divided by the area of the spot of sunlight focused at the focal point \( (A_c/A_f) \). For an ideal concentrator in the vicinity of Earth, this area is 46,000 times smaller than the shadow area of the collecting optics. The geometric concentration ratio is therefore 46,000 to 1, which is the maximum allowed by the second law of thermodynamics. Unfortunately, there is no such thing as an ideal concentrator.

The most common shape for a concentrator is a paraboloid. A paraboloid is the surface of rotation that results from rotating a parabola around the line between its focus and vertex. This line of symmetry is known as the optical axis. A paraboloid has the desirable property of producing a perfect point image, at the focal point, of a point on the optical axis an infinite distance away. The distance between the vertex and the focus, or focal point, is the focal length \( f \). Extended objects are not perfectly focused, however. Astronomical telescopes use paraboloids to image extraterrestrial objects. They tend to be much longer focal length and produce much better images than systems used to collect solar energy. The short-focus, off-axis parabolic concentrators to be used for propulsion do not form good images.

Paraboloids produce at best an average geometric concentration ratio one fourth of the theoretical maximum 46,000 allowed by thermodynamics (Winston, 1991) (averaged over the focused spot area). Each mirror element of the paraboloid projects a cone of light of angular diameter \( 2\theta_{\text{sun}} \) at the focal point. This cone in turn projects an ellipse of light (a stretched image of the sun) on the focal plane. The integration over the concentrator surface of all projected ellipses onto the focal plane gives the intensity profile of sunlight on the focal point. Not all points on the paraboloid are at equal distance to the focal point so that the projected ellipses from different parts of the paraboloid do not overlap well. Therefore, the circle enclosing all the focused light has a larger area than would an ideal concentrator and so a paraboloid produces a lower geometric concentration ratio.

It is possible, however, to achieve peak intensities that approach the thermodynamic limit of 46,000 suns. The intensity profile about the focal point of a paraboloid looks somewhat like a Gaussian distribution. The geometric concentration ratio is an average intensity over this distribution divided by the intensity of 1 sun (1350 W/m²). The focal point, where the center of the Sun is perfectly imaged, receives sunlight from all regions of the paraboloid. The intensity there is the solid angle of the concentrator multiplied by the solar intensity (see Equation 6). The concentration ratio at the
focal point is;
\[ R_c = \frac{I(\theta_{rim})}{I(\theta_{sun})} = \frac{\sin^2 \theta_{rim}}{\sin^2 \theta_{sun}} = 46,000 \sin^2 \theta_{rim} \]

This is the peak concentration ratio as opposed to the geometric concentration ratio. For a concentrator that covers a 45 degree half-angle;
\[ R_c = 46,000/2 = 23,000 \]

The effect of errors in the surface shape typically increases the focused spot size and decreases intensity. The standard unit of measure for mirror surface errors in the solar concentrator business is the mean slope error. The mean slope error is the mean deviation in angle of the mirror surface from the desired surface slope. The distribution of slope errors for a concentrator can be found by measuring the slope error for every point on the mirror surface and binning the frequency of errors. This slope error distribution typically looks like a Gaussian curve and can be convoluted with the focused intensity distribution of the perfect mirror to get the actual focused intensity distribution. However, in many cases it is usually good enough to sum the squares of the error with the square of the width of the perfect image to get an estimate;
\[ \sigma_{system} = \left( \sigma_{perfect}^2 + (2\sigma_{slope})^2 \right)^{1/2} \]

where \( \sigma_{system} \) is the focal plane intensity distribution width, \( \sigma_{perfect} \) is the width of the intensity distribution for a perfect paraboloid, and \( \sigma_{slope} \) is the width of the slope error distribution. The slope error is multiplied by two because reflected light deviates by twice the slope error. This process decreases both the geometric concentration ratio and the peak intensity. A one miliradian mean slope error is considered very good for a solar concentrator system and will not overly degrade performance. For comparison, consider that the width of the Sun is much larger.

The reflectance of real mirrors is usually somewhere between 90 and 98 percent. Polished or vapor deposited aluminum has a reflectance of about 92 percent. Polished silver surfaces reflect around 98 percent but are easily corroded. Protective coatings can decrease reflectance slightly but also greatly improve lifetime for terrestrial mirrors. Reflectance losses decrease the intensity of the distribution of light in the focal plane but do not change its shape.

**SOLAR ROCKET PERFORMANCE UPPER-LIMITS**

Figure 1 is a schematic drawing of a generic solar thruster. Sunlight enters from the left and is absorbed by the absorber/heat exchanger. Propellant flows in behind the window and proceeds to the right through the nozzle. Along the way, the propellant is heated in the absorber/heat exchanger. A window may be required for some designs to contain the propellant. The window spacer spaces the window back from the primary concentrator focal point at the front of the secondary concentrator. This minimizes the thermal flux in the window. The window spacer also serves as a heat shield to external components and can provide initial heating of the propellant. A Secondary concentrator may be used to increase the solar flux through the absorber. A cavity can be used to increase the absorptivity of the absorber/heat exchanger by making it look more like a blackbody.

A propellant temperature \( T \) can only be reached if the radiation field temperature \( T_{rad} \) exceeds \( T \). \( T_{rad} \) is given by the Stefan-Boltzmann law;
\[ T_{rad}^4 = \frac{R_{\text{Earth}}}{\sigma} \]

where \( I_{\text{Earth}} \) is the 1350 W/m² received in Earth's orbit and \( R_c \) is the concentration ratio. If the propellant temperature \( T \) approaches \( T_{rad} \), then combining the relationship for specific impulse (Equation 2) with Equation 10 gives;
\[ I_{sp} \propto R_c^{1/8} \]

This is the maximum possible specific impulse for a given concentration ratio \( R_c \) and is proportional to the eighth root of concentration ratio.

The temperature reached by a particular concentration ratio \( R_c \) can also be found from;
\[ \frac{T^4}{T_{sun}^4} = \frac{RI_{\text{Earth}}}{46,000I_{\text{Earth}}} \]
\[ T = T_{sun} \left( \frac{R}{46,000} \right)^{1/4} \]

where \( T_{sun} \) is the solar surface temperature. A concentration ratio of 10,000 will produce an equilibrium temperature (allowing only radiation transfer) of 3960 K. This is well above the 3500 K or so temperature needed to achieve 9800 m/s(1000 s) \( I_{sp} \). If the concentration ratio is cut in half, then the \( I_{sp} \) goes as the eighth power of 1/2; therefore, \( R=5000 \) gives 3600 K. This is sufficient to achieve 9800 m/s(1000 s) \( I_{sp} \). However, the thruster should not be operated near radiative equilibrium since this means a large amount of incident radiation is reradiated and lost. Operating at 5000 suns to get 2500 K on the other hand, results in only 22 percent reradiation loss. It is important to remember that
The upper-limit of propellant temperature also depends upon the details of the thruster's receiver design. The maximum temperature possible is that corresponding to the average intensity $I_{avg}$:

$$ I_{avg} = \frac{1}{A} \int \int_{Aperture} I(x,y) dx dy $$

where $A$ is the aperture area. This average intensity is less than the peak intensity available. A different receiver design could use the peak of the intensity distribution to do the final propellant heating. This type of thruster could produce higher temperatures than a cavity absorber. Another alternative is to use a secondary concentrator to fold the light in the wings of the intensity distribution into the aperture of a cavity receiver. This approach squeezes all the light into a smaller aperture to increase the total intensity to a value possibly larger than the peak intensity of the original distribution. An absorber should be well matched to the distribution of focused light (i.e., a cylindrical cavity may not work well).

Thrust is given by Newton's Law, $F = \nu \frac{dm}{dt}$ (Equation 1), where $\nu$ is the propellant velocity and $\frac{dm}{dt}$ is the propellant mass flow rate. The power $P$ put into propellant flow is $\frac{1}{2} \nu^2 \frac{dm}{dt}$. $\nu^2$ is proportional to the kinetic energy imparted to the propellant. If the $I_{sp}$ is held fixed, then $\nu$ is also constant:

$$ I_{sp} \equiv F \left/ \frac{dm}{dt} \right. = \nu $$

$(\nu$ is also proportional to the square root of $T$) and thrust $F$ is proportional to $\frac{dm}{dt}$ only. $\frac{dm}{dt}$ is proportional to the thermal energy input since that determines how much propellant per unit time can be heated to the required temperature. Therefore, thrust is proportional to the area of the concentrator (for fixed $I_{sp}$).

If mass flow $\frac{dm}{dt}$ is held constant, then both thrust $F$ and $I_{sp}$ will go up with increasing temperature. If
is increased while keeping the thermal power input constant, thrust increases monotonically but the propellant temperature will drop. Simultaneously, receiver temperatures should drop, reducing reradiation and increasing thermal efficiency. Also, there are energy loss mechanisms involved with the energy states of molecular hydrogen that increase with increasing temperature. Thrust can be traded off with Isp. Figure 2 shows approximate thrust and Isp as a function of temperature. Higher Isp decreases thrust very rapidly. However, higher temperatures are always desirable if the mass flow rate can be maintained.

Figure 3 shows performance envelopes for a variety of propulsion systems. The specific impulse is plotted on the vertical axis and the thrust to vehicle weight ratio is plotted on the horizontal axis. Conventional rocket thrusters are in the oval labelled "Liquid and Solid Chemical Propellants". These typically produce thrust between 0.1 to a few hundred gs. The maximum Isp is about 4500 m/s. The region of this chart where boosting from the Earth's surface is possible is on the right side of 1g. As is well known, conventional thrusters can leave the ground. Solar-Thermal propulsion however cannot as its oval lies to the left of 0.1g. The top of the Arcjet, Solar-Thermal, Nuclear Fission, and Laser-Thermal propulsion ovals is limited to around 10,000 m/s because of the limitation in fabrication materials; no material can survive the temperatures required to reach higher Isp. Electrostatic and electromagnetic thrusters do not have this constraint because they use electromagnetic fields to contain the hot propellant (in this case a plasma).

Figure 2: TRADEOFF OF THRUST AND Isp WITH CHANGING PROPELLANT TEMPERATURE.

Solar Rocket Configuration

Operation of a Solar Rocket requires pointing the thruster force vector along the desired direction of acceleration and pointing the concentrator system at the sun at the same time. The thrust vector passes through the center-of-mass of the rocket (unless you want only to go in loops) and preferably down the centerline of the rocket body (so that propellant usage does not offset the center of mass). The rocket may be rotated around the thrust vector, which should be the body axis, without changing the direction of acceleration. Only one other degree of freedom is then required to allow the concentrator system to collect sunlight at all times. This is obtained by allowing the concentrator system to pivot on an axis perpendicular to the body axis.

The nozzle produces thrust by flowing hot propellant, such as molecular hydrogen, through its throat. The path of the hot propellant to the nozzle throat must be kept short to minimize thermal conduction losses and spacecraft weight. The absorber/heat exchanger must therefore be very close to the nozzle. Furthermore, the exhaust plume, which expands out at very high angles from the nozzle, can do serious damage to concentrator structures (Merkle and Yu, 1988). The concentrator must be removed from this hazard.

The only way to meet the above constraints is to use off-axis concentrators. Sunlight enters the concentrator system and is deflected at a large angle into the absorber/heat exchanger. The direction to the sun is somewhere close to 90 degrees from the optical axis of the concentrators. A paraboloid shape is still desirable since it focuses an on-axis point into the focal point. The focused light from the Sun comes into the thruster bound by the surface of a cone. The surface of this cone is far removed from the plume to prevent plume impingement damage to the concentrator. The centerline of this cone, which is the optical axis, is close to perpendicular to the rocket body axis to allow the concentrators to be rotated to give the second degree of freedom required. The resulting appearance of most solar powered thruster designs is similar to that of a conventional rocket but with two large opposing concentrators attached to a point near the rocket nozzle (See Figure 4).

There are other ways to build a solar rocket if one is willing to reduce some of the above constraints. One is to use a focal point far from the concentrator and transmit the solar energy to the thruster via a fiber optic
Figure 3: PERFORMANCE ENVELOPES FOR A VA-RIETY OF PROPULSION SYSTEMS.

Available (Nakamura and Irvin 1992). Another is to thrust
ly in certain orientations, thus relaxing the need for
wo degrees of freedom in concentrator orientation.

Conventional thrusters typically burn all of their pro-
ell in a few minutes. It takes just this one short
ut high acceleration boost to place the spacecraft into
transfer orbit. Once the spacecraft rises to its high-
st point, another burst of thrust puts the spacecraft into a circular orbit (if that is the desired orbit). A
lar-thermal thruster, on the other hand, does not have
ough thrust to do a large orbit transfer with one short
rst. It will take many hours typically for a solar
ruster to expel all of its propellant.

This adds further constraints on how a solar-thermal
ruster must operate. A continuous but low acceler-
thrust can be used to spiral the spacecraft to its
bit. This is not the most efficient way to perform a
bit transfer, however. A more efficient approach is
thrust only at apogee or perigee. At these points
 energy is put into maximizing the increase in linear
omentum and angular momentum. This type of orbit
ever is called a multi-burn orbit transfer. In LEO
Low Earth Orbit) these thrust periods will last around
minutes. Then the spacecraft must not thrust until
ext perigee or apogee. This slows the orbit trans-p since the majority of time is spent waiting until the
xt apogee or perigee. Most orbit transfers using solar-
thermal propulsion will require around two weeks.

THE OFF-AXIS PARABOLOID

Concentrators for most solar-thermal spacecraft con-
cepts are extreme off-axis paraboloids as compared with
typical terrestrial concentrators. While typically still
jecting a circular cone of concentrated light, the in-
tensity distribution within that cone is very nonuniform.
The geometric concentration ratio is lower than avail-
able from an on-axis paraboloid concentrator because
of the larger variation in distances from the reflective
urface to the focal point. Finally, the shape of the
concentrator itself (one that projects light within a cir-
cular cone) is elliptically shaped instead of circular.

The intersection of a circular cone and paraboloid,
with the cone apex at the focal point of the paraboloid,
is an ellipse that lies within a plane. This is convenient
as it is usually simpler to build support structures that
lie in a plane; for this reason a torus is the simplest
upport structure for inflatable and other types of solar
ulsion concentrators that require support. Rigid
elf-supporting concentrators need not be constrained
to this geometry.

Figure 5 shows the geometry and dimensions of a
genric off-axis concentrator. The Y-Z plane is viewed
in this figure and the X axis is perpendicular to the
age and pointing at the reader. The Z axis is the axis
rotation symmetry of the paraboloid. The circular
cone has a half angle of $\theta_c$ and its apex is at the focal
point. The axis of symmetry of the cone is rotated in
the Y-Z plane at an angle $\phi$ measured clockwise from
the Z axis. The projection of the ellipse, or torus, along
the axis of symmetry of the paraboloid is a circle. The
CONCENTRATION

EXAMPLE: 2 X 25 KW RIGID

For an example case, consider the design of a space.

\[ R^2 = \frac{46,000 \sin^2 \theta}{d^2} \]

Determine the cone half angle \( \theta \)

(1) Given the desired power \( P \) collected by the concentrator.

(2) The area enclosed by the locus of the rays and the parameter \( d \) is approximated by

\[ \cos \text{section} \left( \phi \sin \theta \right) \left( \cos \theta - \cos \theta_0 \right) = \frac{d}{R} \]

(3) The half angle is given by

\[ \theta = \sin^{-1} \left( \frac{d}{2R} \right) \]

(4) The length of the two strings going to the minor axis is given by

\[ f \frac{2 \sin^2 \theta}{\sin^2 \phi + \sin^2 \theta} = \frac{f}{T_{\text{mirror}}} \]

(5) The length of the major axis is given by

\[ \frac{f}{T_{\text{mirror}}} \]

(6) The string point to the power major axis intersection has

\[ \frac{f}{T_{\text{mirror}}} \]

(7) The distance of the center of the circle from the Z axis

\[ (\phi \sin \theta)/\left( \cos \theta - \cos \theta_0 \right) \]

(8) The cross-sectional profile of the concentrator is given by

\[ \frac{\left( \phi \sin \theta \right) \cos \theta \cos \theta_0}{\left( \cos \theta - \cos \theta_0 \right)} = f \]

(9) The radius \( R \) is chosen to give the desired power \( P \)
angle $\theta = 120$ degrees is chosen to minimize the long of the torus since we are assuming a very tight fit of booster fairing. The focal length can then be defined from Equation 22 to be 2.18 meters. Equation 1 gives the offset of the center of the shadow from the major axis of the torus is equal to $R$. The major a of the torus is 1.23$R$ or 3.15 meters. The total th of the major axis is $2a = 2 \times 1.23R = 6.302$ m.

The length of the major axis is almost short enough in an Atlas fairing. If a rigid reflector is used, the straining of using a torus can possibly be relaxed and concentrator could be trimmed, then added to at tegic places to produce a better fit. The calculation the elliptical concentrator would simply serve as a le in this case to determine the approximate dimen and geometry for a rigid nontoroidal concentrator sort structure.

The mass $m$ of the support structure is estimated by;

$$m = (2L_{\text{minor}} + L_{\text{major}} + p)\lambda_0 \left( \frac{R}{R_0} \right)^\mu$$

where $\lambda_0$ is a linear mass density characteristic of the tand torus material for a radius $R_0$. This is the us of the concentrator shadow, and $\mu$ is a real number between 0.0 and 1.0. As the size of a concentrator em is increased, the linear density must also increase to provide greater stiffness. $\mu = 1.0$ would give a lin-mass increase proportional to the concentrator area, which should be avoided (e.g., structural stiffness can increased by making larger diameter, hollow struts lead). $\mu = 0.0$ represents no change in strut size with rger system which seems unlikely. The baseline case here will assume that a PL(OLAC) altitude cham-deployed foam inflated strut is stiff enough. This it is three inches in diameter and weighs approximately 0.5 kg/m. Therefore, $\lambda_0R^\mu$ is set to 0.5 kg/m. It also assumed here that the torus and struts are made of the same material. The length $L_{\text{minor}} = 4.1$ me met by Equation 23. The length $L_{\text{major}} = 2.2$ meters Equation 24. The perimeter of the torus $p = 18$ met from Equation 19. Therefore, the total mass of the port structure for one concentrator side is 28.5 kg Equation 25. The mass of the concentrator is approximately the area enclosed by the torus times the thickness of the mirror times the mass density of the mirror material (this assumes the added mass due to vature is negligible). For typical inflatable film concentrators, this mass works out to be one or two kg. As alternative, consider a rigid concentrator shell 1mm thick. The area of the concentrator is 25 square meters.

If the reflector shell material density is 2g/ml, then the mass is about 50 kg.

RECENT CONCENTRATOR DEVELOPMENT EFFORTS

There have been several trade studies of concentrator structures performed. All of these studies reviewed considered either a 7 or 9 meter concentrator system, a 30 or 40 meter concentrator system, or both. This paper does not include previous studies since a review of these can be found in another paper (Aug, 1989). This set does reflect the most current information on structural issues regarding the accuracy of concentrators designed for solar-thermal propulsion. There is not yet much data on the optical performance of space-deployed concentrators.

The Gossamer Baggie Torus project, performed by Thiokol Corporation for the Phillips Laboratory (Lester and Warner, 1994), was a study of a concentrator support torus using FIR (Foam Inflated/Rigidized) structures. A proof-of-concept 8-foot diameter torus was deployed in an altitude chamber as a part of this project. Thiokol's favorite torus structure, as designed in this study, was a 7 by 9 meter elliptical truss structure.

The foam used to inflate the tubes of the FIR structure serves to expand the structure from a size that will fit into a booster fairing to the desired concentrator size. The tubes are made of E-glass cloth impregnated with ultraviolet curing resin. Ultraviolet radiation from the sun cures the tube walls after inflation. At the same time the inflation foam hardens. Stiffness is provided primarily by the rigidized tube walls. The foam increases the buckling strength by a factor of 2.3 in laboratory deployed tubes. The 8-foot diameter proof-of-concept torus began as a 2-foot diameter torus and completely deployed in about 15 seconds.

Producing an elliptical structure would require curved E-glass cloth tubes. While these are available, Thiokol considered the cost prohibitive. Instead, they choose to approach the elliptical shape with a dodecagon. This results in a mass only a few percent greater than an elliptical shape. Each side of the dodecagon consists of three parallel tubes instead of a single tube. This gives the required stiffness at minimum mass.

The total estimated mass for the Thiokol 7 by 9 meter design is 47 kg. This also includes the weight of the canisters which inject foam into the tubes during deployment. Thiokol did not calculate masses for the attachment struts from the torus to the spacecraft.

Thiokol and SRS Technologies are planning a rigidized-concentrator deployment in December 1994.
This deployment will use a FIR structure and an inflatable concentrator with two chambers. The first chamber is inflated with gas to form the appropriate shape for the concentrator reflective surface. The second chamber is foam-inflated against the pressurized back side of the reflective surface. Once the foam hardens, the front film of the front chamber can be removed and the concentrator shape is maintained by the hardened foam.

Harris (Borell, et al., 1993) has also studied concentrator support structures. They considered a 30 by 40 meter system, a 7 by 9 flight test version of the 30 by 40 meter system, and a Single Chamber Concentrator (Gierow, et al, 1992). Harris has been designing and building space deployable antennae and concentrators for the Air Force and NASA for many years. Some of their past ideas are considered in their study.

They based their torus deployment and support system on work done for NASA in the mid-1980s. A 15 meter diameter circular version of their torus (which they call a hoop) was actually fabricated for NASA-Langley. The struts that attach the concentrator to the spacecraft are graphite epoxy which telescope and latch upon deployment. The torus consists of 44 segments of 2.5 inch diameter graphite-epoxy tubes which unfold accordion-style by the action of small motors in each hinge. The number of segments was chosen to minimize stowage size.

The Harris 7 by 9 meter concentrator system will fit into a 28-inch diameter cylinder that is 28 inches high. The calculated mass of the total system is 57 kg. This mass includes everything but the turntable to rotate the concentrator about its axis. Under zero acceleration, this concentrator will generate a peak intensity of about 13,000 suns which is sufficient for most thruster designs. Under 1g of acceleration (considered for ground testing), the peak intensity remains greater than 12,000 suns. The single chamber 7 by 9 meter system weighs about 23 kg and will fit inside a GetAway Special (GAS) canister on the Space Shuttle. However, this system is not as mature as the torus structures. No estimates were made of optical performance in this report.

The Harris 30 by 40 meter concentrator system is the same basic design as for the 7 by 9 meter system except that the torus will consist of 78 segments. This system will stow to 65 inch diameter by 65 inch length. The mass is estimated to be 280 kg.

Martin Marietta has proposed using graphite/gelatin as the torus material (Draper, 1993) (preferred over kevlar/gel) for a 30 by 40 meter concentrator support system. This type of torus is inflated with gas and then rigidized to form a cylindrical shell. They also considered a rigid, folding torus similar to that proposed by Harris. This particular report also considered in some detail mission requirements and pointing and tracking issues. In addition, space environmental hazards are addressed.

Martin Marietta compared 10 variations of the two basic approaches in the previous paragraph and selected a rigid torus with four telescoping, graphite/epoxy tube struts. This system meets a ±0.5° pointing criteria under acceleration and will package into the Space Shuttle cargo bay. The mass of this system is estimated to be 430 kg. The weight can be reduced considerably using a graphite/gelatin inflatable self-rigidizing torus. This system would weigh about 260 kg. This system has a higher developmental risk and was therefore Martin Marietta’s second choice.

TRW Space and Electronics Group selected inflation/rigidized struts and torus to support an inflatable concentrator (Kovalčik, 1993). The 120-inch diameter Space Station Alpha Joint is suggested for a concentrator attachment point and to allow rotation about the axis perpendicular to the spacecraft. It has been prototyped already and appears to be suitable for a Solar-Propulsion spacecraft. There are three attachment points on the torus and three attachment points on the Alpha Joint. The Alpha Joint is connected to the concentrator by six struts arranged as three bipods. The two struts of a bipod meet only at the concentrator. The estimated total weight of one concentrator and support (minus the Alpha Joint) is 205 kg. The TRW configuration gives less than 2.2 milliradian slope error. To do this requires the strut materials have a low coefficient of thermal expansion, such as given by Kevlar.

Lockheed has studied the widest variety of strut types of all PL funded trade studies to date (Richie, 1993). These types are IRSC (Inflated, Rigidized, Space-Cured Composites) tubular, Lenticular, Inflated Pressurized tubular, Bi-STEM (Storable, Tubular, Extensible Member), Collable, FAST (Flexible Articulated Square Truss), and Telescopic. For each type of strut, mass and volume were estimated. Some of these need thermal protection to reduce thermal expansion effects. Five additional criteria were used in their selection of best strut; material shelf-life, ground test deploy simulation, deployment location accuracy, material dimensional stability in space, and damage tolerance in space. Lockheed assumes that the torus is inflated and then rigidized so this report does not discuss the torus in great detail.

Lockheed deemed four strut concepts worthy of further study; Lenticular, Collable, FAST, and Telescopic, all of which used composite materials. They considered FAST to be the most accurate during deployment, to have low developmental risk, and to be one of the light-
strut concepts. The weight of all six FAST struts both sides of a 30 by 40 meter concentrator system 6 kg. The total weight of both concentrators with port structure, including turntables, is about 450 kg. 

The Lockheed numbers are based on the assumption that thrust can be throttled up slowly so as not to excite structural vibration modes with a sharp thrust transient. Furthermore, Lockheed assumes that the thrust is throttled so that the acceleration never exceeds 0.002 g. This in fact may be a reasonable concern, since at LEO (Low Earth Orbit) the propellant tanks will be full and the acceleration will be low at thrust. Once the orbit has been raised sufficiently, propellant tanks will be lighter and thrust will need to be reduced. However, low thrust in higher orbits is not a problem: the trip time is too much because thrusters can be longer since orbit periods are longer. Furthermore, lower thrust will in general allow increased specific impulse.

Figure 6 shows a plot of mass vs. minor axis diameter for the above concentrator systems. It is seen that current estimates between different groups are within about fifty percent of each other. All of these masses are a reasonably small fraction, between 10 and 20 percent, of a typical payload. While somewhat larger than conventional thrusters, the increased Isp offers a much lower propellant mass, on the order of percent less. The net result is a nearly doubled payload. The 50 percent variation in estimated masses for concentrator systems will appear as a 5 to 10 percent variation in payload.

The two curves on Figure 6 are based on Equation with linear mass density $\lambda_0 = 1.2$ kg/m. The top curve has $\mu = 0.4$ and the bottom has $\mu = 0.1$. The line of $\lambda_0$ corresponds to the 7.5 by 9 meter concentrator and both curves are fit to the one point on Figure 6 for this size concentrator. The value of $\lambda_0$ is 2 to 3 times larger than any strut designs for this size concentrator. However, this is because the masses on Figure 6 include more than just the strut masses (e.g., foam injection cannisters, pivoting joints, etc.) fit to Equation 1. If it happens that these extra masses scale the same as the strut masses, then this equation will give a useful fit for concentrator mass estimation. As such, the value of $\mu$ for the two curves indicate that the concentrator support strut linear density is approximately proportional to the fourth root of concentrator diameter. More data points are really needed however, since there is only one point at the 7 by 9 meter size.

**CONCLUSION**

The maximum possible specific impulse $Isp$ of a solar powered rocket is proportional to the eighth root of the peak concentration ratio. The thrust is proportional to the solar power collected and the energy efficiency of the absorber and concentrator. A peak concentration ratio of 10,000 to 1 should be sufficient to produce a thruster with an $Isp$ of 9800 m/s (1000 s) and still retain reasonable thrust and efficiency. This is better than double that of conventional thrusters. To do this however, will require careful management of the asymmetric cone of focused light from an off-axis paraboloid concentrator.

Flight-weight concentrator development is ongoing as is the development of inflatable and inflatable/rigidized reflective films. Current data indicates that concentrators can be made light enough to realize the potential of Solar-Thermal Propulsion.

The Phillips Laboratory (OLAC) at Edwards Air Force Base is actively working to forward research and development in Solar-Thermal Propulsion. The concentrator support structure trade studies reviewed above were the result of PRDA Program Research and Development Announcement contracts, for example. Current funding is through SBIRs (Small Business Innovative Research), however, as money for larger contracts becomes rare. Topics such as space concentrator development, thruster development, pointing and accuracy,
etc., are of interest to the Phillips Laboratory Solar Propulsion Group.

The Phillips laboratory also has a 25 kW solar furnace on which to perform ground tests on thruster prototypes. This facility can also be used to test space based concentrator prototypes, provided they can be supported in a one gravity environment. Our goal is to achieve 8000 m/s (10000 seconds) Isp in the Phillips Laboratory Solar Lab.

References


