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### Corneal Damage from Infrared Radiation

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This report summarizes our research during the past year on the interaction of 80 ns pulses of infrared radiation produced by a CO₂-TEA laser with the cornea. Epithelial damage thresholds were determined for sequences of 1, 2, 8, 32, 128, and 1024 pulses at 10 Hz and for sequences of 1, 2, 8, 32, 128, and 1024 pulses at 16 Hz. Threshold damage is correlated by a power law of the form \( E_{Dk} = CN^{-\alpha} \) in which \( E_{Dk} \) is the threshold energy density and \( N \) is the number of pulses in the sequence. Temperature calculations reveal that the maximum temperature increase on the beam axis 10 μm beneath the anterior tear surface resulting from the different threshold exposures is essentially constant. This result is consistent with a critical peak temperature damage model and suggests that, at least for the multiple-pulse exposures, the damage mechanism may be predominaely thermal. Damage threshold measurements on corneas maintained at 21°C indicated that the damage mechanism is indeed predominaely thermal.

**Subject Terms:**
Cornea, infrared radiation, damage, multiple pulses
FOREWORD

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[Signatures and dates]

Principal Investigator's Signature

Date

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Introduction

The military employs a broad range of laser radiation in training devices, rangefinders, target designators, communications devices and other instruments. This equipment emits either single pulses or sequences of pulses in beams of various diameters. The research performed under this contract directly supports the U. S. Army Medical Research and Materiel Command (USAMRMC) mission to assess the health effects and hazards of nonionizing electromagnetic radiation from such laser systems. The data obtained will support evaluation of current permissible exposure limits and will aid health policy makers, both within and outside the DoD, in developing injury prevention criteria. The general approach is to make direct determinations of damage threshold levels for non-ionizing radiation for specific exposure conditions (e.g., wavelengths, pulse durations, etc.) and to develop models of the damage mechanism that enable the extension of the results to other exposure conditions.

Under past support from the Army Medical Research and Development Command we determined corneal damage thresholds for CO₂ lasers that emit single and sequences of pulses having durations of 1 ms and longer and developed thermal damage models for predicting this type of damage. We also determined corneal damage thresholds for single 80 ns pulses of CO₂ laser radiation and for three multiple-pulse (2 pulses at 1 Hz.; and 2 and 8 pulses at 10 Hz.) In the case of these very short pulses, damage mechanisms other than thermal (e.g., acoustical pressure pulses) could also play a role. Light and electron microscopy revealed unusual disruptions of the anterior epithelial surface for the threshold single-pulse exposure. The characteristics of these disruptions differed from those observed with simple thermal damage at longer pulse durations and appeared to be consistent with a mechanical (e.g., acoustic) damage mechanism. However, the calculated temperature increase produced by the threshold exposure was only slightly lower than that calculated for threshold exposures having durations of 1 ms and longer. Thus we could not exclude a thermal damage mechanism, with the sharp temperature gradients leading to marked differences in the character of the damage as compared to damage from longer duration exposures.

This study aims to expand the database of thresholds for sequences of 80 ns of CO₂ laser pulses to include larger numbers of pulses and other pulse repetition frequencies. In addition it will attempt to clarify the damage mechanism(s) for these types of pulses and ultimately will begin to address damage from mid-infrared wavelengths where the radiation is more penetrating.

Methods

Short-pulse exposures are made with a Boston Laser (Model 220S) CO₂-TEA laser operated in the TEM₀₀ mode. This laser delivers 80 ns pulses at pulse repetition frequencies up to 16 Hz. Mode quality is verified and the beam diameter is measured at the beginning, middle and end of each experimental session using a Spiricon linear pyroelectric array. The detector has 64 elements on 200 μm centers. It is mounted on a vertical micropositioner and is read out with a LeCroy 9354M digital oscilloscope. Pulse energy is measured with a Scientech detector immediately before and immediately after each exposure.

New Zealand white rabbits of either sex weighing 4 - 5 pounds are used for the experiments. The rabbits are treated in accordance with the Guide for the Care and Use of Laboratory Animals (DHEW Publication No. (NIH) 85-23, Revised Edition, 1985 and with the Association for Research in Vision and Ophthalmology Resolution on the Use of Animals in Research. Prior to exposure the rabbits are anesthetized with an intramuscular injection of xylazine and ketamine hydrochloride (Rompun-Ketaset) in the proportions: 60% of 20 mg/ml Rompun to 40% of 100 mg/ml Ketaset by volume. In addition, a topical anesthesia (proparacaine
hydrochloride 1/2%) is applied to each eye before exposure and a drop of homatropine bromide 5% is instilled to dilate the pupil. This facilitates examination of the exposed corneas for minimal lesions. The anesthetized animals are placed in a conventional holder for exposure. A speculum is inserted in the eye about one minute before exposure and the eye irrigated with BSS solution (Alcon Surgical) which is at room temperature; however, in order to create a reproducible “tear film,” the irrigation is stopped 20 sec before the exposure and excess fluid is blotted at the limbus. The cornea surface is assumed to have returned to its normal temperature after this time. One exposure is made to each eye. One-half hour after exposure the rabbits, still under anesthesia, are sacrificed with Beuthanasia-D administered in an ear vein. The eyes are enucleated and examined for damage using a Nikon FS-3 photo slit-lamp. In selected cases the globes are placed in gluteraldehyde/formaldehyde fixative and are delivered to Prof. W. R. Green’s laboratory at the Wilmer Ophthalmological Institute where they are processed for microscopy and the micrographs evaluated by Dr. Green.

In a few experiments we exposed enucleated eyes which were at room temperature to test the damage mechanism. We have shown previously that reliable damage thresholds can be determined in freshly enucleated eyes. For these experiments the rabbits were anesthetized and given a topical anesthesia and the pupils dilated exactly as was done for the in vivo exposures. The rabbits were then sacrificed and their eyes enucleated. The enucleated eyes were placed in room temperature (usually ~20 °C) BSS and allowed to equilibrate for at least 5 min. They were then exposed using the same protocol as for the in vivo exposures. After exposure the eyes were placed back in the BSS solution for 1/2 hr before examining them for damage.

The criterion that we use for minimal epithelial damage is that due to Brownell and Stuck, namely the presence of a superficial gray-white spot that develops within 1/2 hr after exposure. We have found that the damage threshold is sharply defined; i.e., only rarely is there overlap between exposures that produce minimal lesions and those that do not. Therefore we do not use statistical procedures such as probit analysis in order to determine the threshold, as these would require the use of more animals than we deem necessary. We make one exposure per eye, brackets exposures above and below threshold. The bracket is narrowed until there is only about a 10% difference in energy between an exposure that produces a minimal lesion and one that does not. The threshold exposure is taken to be at the center of the bracket.

Temperature calculations are based on a Green’s function solution to the heat conduction equation for an incident beam with a Gaussian irradiance profile that is absorbed according to Beer’s law. The beam is assumed to impinge on a semi-infinite slab and to have a constant peak irradiance for the duration of the exposure. We also assume that conduction is the only mode of heat transfer and that no heat is lost to the air at the epithelial interface. The absorption coefficient and thermal properties are assumed to be those of water. The solution $T(r,z,t)$, where $r$ is the radial distance from the beam axis, $z$ is the depth into the cornea, and $t$ is time, has the form of a definite integral that can be evaluated numerically. Since our last Annual report we have made additional modifications to this program to facilitate the calculations for multiple-pulse exposures using very short pulses. The modifications are discussed below and a copy of the new program is listed in Appendix 2.
Results and Discussion

We noted in the first Annual Report covering the period 1 Nov. 1995-31 October 1996 that the experimental apparatus, which had not been in use since our previous contact expired in 1989 and which had been disassembled, was operational and that its operation had been verified on a few test exposures. As a result, most of the objectives in the original Statement of Work for the first year were shifted to this year. These objectives were:

1. The data base of threshold conditions for 80 ns pulses from CO₂-TEA lasers will be extended by measuring the threshold energy densities for sequences of 32, 128 and 1024 pulses at 10 Hz and sequences of 2, 8, 32 and 128 pulses at 20 Hz. The existing thresholds for 2 and 8 pulses at 10 Hz will be refined.

2. An understanding of the damage mechanism for such pulses will be pursued by:
   a) determining how lowering the temperature of the epithelium affects the threshold,
   b) obtaining light and electron micrographs of the damage,
   c) using high-speed photography to investigate ablation of material from the corneal surface, and
   d) measuring pressure transients in model systems.

3. The required characteristics of potential near-infrared laser source(s) for damage studies will be identified by performing detailed temperature calculations in the 1.3 to 2.5 μm wavelength region.

This year we have made significant progress toward achieving these objectives in spite of having had to move and re-establish our laboratory during the third quarter. The move to improved space was necessary because of a reorganization at the Applied Physics Laboratory.

We repeated and refined the determination of the damage threshold for 2 pulses at 10 Hz. The new threshold of 235 mJ/cm²/pulse is slightly higher than the value of 200 mJ/cm²/pulse that we had determined in preliminary experiments. We then confirmed our earlier value for the threshold for 8 pulses at 10 Hz. After these experiments we determined epithelial damage thresholds for sequences of 32, 128, and 1024 pulses at a pulse repetition frequency of 10 Hz. In order to perform the experiments with 32 or more pulses it was necessary to put a partially reflecting attenuator in the laser beam because the required pulse energies were below the lasing threshold. We found that the beam diameter measured with the partial reflector in place tended to be smaller than when it was removed. This led us to question the previously reported single-pulse threshold, because at the time it was determined our practice was to attenuate the beam so that the Spiracron detector used to measure beam diameter would not be saturated. We noted that if the unattenuated beam used in determining the threshold actually had a larger diameter, then the correct value of EDₙ would be lower. Consequently we repeated the single-pulse threshold measurement without using the reflector. In these new experiments the beam intensity was reduced by decreasing the laser power. The newly determined threshold is 307 mJ/cm² compared to the value 360 mJ/cm² found previously. The final 10 Hz damage thresholds are listed in Table I together with the calculated peak temperature increases. The temperature calculations and their implications are discussed below. These threshold results were presented at the 1997 International Laser Safety
Conference\textsuperscript{11} and at the annual meeting of the Association for Research in Vision and Ophthalmology.\textsuperscript{12}

In the original Statement of Work we also were to determine epithelial damage thresholds at a pulse repetition frequency of 20 Hz. However, we discovered that output of the Boston Laser (Model 220S) was unstable at pulse frequencies above 16 Hz (although the specifications claimed 20 Hz). Boston Laser is no longer in business, consequently technical support for the laser is not available. We discussed this problem with our Contracting Officer’s Representative, Mr. Bruce Stuck, and it was agreed that we would make the determinations at 16 Hz. The final results are listed in Table I (note that we made an additional threshold determination at 1024 pulses which was not included in the original Statement of Work).

**Table 1: Threshold Energy Densities and Calculated Maximum Temperature Rises for Sequences of 80 ns Pulses.**

<table>
<thead>
<tr>
<th>Number of Pulses</th>
<th>Pulse Repetition Frequency (Hz)</th>
<th>$E_d$ (mJ/cm$^2$/pulse)</th>
<th>$d_{\text{rms}}$ (mm)</th>
<th>$\Delta T_{\text{max}}$ (C) $^\circ$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$-$</td>
<td>307</td>
<td>3.72</td>
<td>30.25</td>
</tr>
<tr>
<td>2</td>
<td>10</td>
<td>235</td>
<td>3.48</td>
<td>25.68</td>
</tr>
<tr>
<td>8</td>
<td>10</td>
<td>228</td>
<td>3.80</td>
<td>32.00</td>
</tr>
<tr>
<td>32</td>
<td>10</td>
<td>154</td>
<td>3.78</td>
<td>29.15</td>
</tr>
<tr>
<td>128</td>
<td>10</td>
<td>136</td>
<td>3.41</td>
<td>32.45</td>
</tr>
<tr>
<td>1024</td>
<td>10</td>
<td>95</td>
<td>3.21</td>
<td>26.60</td>
</tr>
<tr>
<td>2</td>
<td>16</td>
<td>265</td>
<td>3.62</td>
<td>29.73</td>
</tr>
<tr>
<td>8</td>
<td>16</td>
<td>205</td>
<td>3.75</td>
<td>31.26</td>
</tr>
<tr>
<td>32</td>
<td>16</td>
<td>150</td>
<td>3.73</td>
<td>32.90</td>
</tr>
<tr>
<td>128</td>
<td>16</td>
<td>105</td>
<td>3.82</td>
<td>32.80</td>
</tr>
<tr>
<td>1024</td>
<td>16</td>
<td>85</td>
<td>3.58</td>
<td>35.06</td>
</tr>
</tbody>
</table>

*$^\circ$Calculated on the beam axis 10 $\mu$m beneath the anterior tear surface.

The epithelial damage thresholds listed in Table I are plotted in Figure 1. The least squares fits to these data show that the thresholds at 10 Hz and 16 Hz are correlated by an empirical power law of the form

$$E_{d_{\text{th}}} = CN^{-\alpha},$$

in which $N$ is the number of pulses in the sequence. The coefficient $C$ and exponent $\alpha$ appear to differ slightly for the two cases; however it is not possible to discern if the difference is real. For the 10 Hz threshold, $C = 291$ mJ/cm$^2$/pulse and $\alpha = 0.162$ (R = 0.976), and for the 16 Hz threshold, $C = 300$ mJ/cm$^2$/pulse and $\alpha = 0.194$ (R = 0.997). The least squares fits fall within the
±10 percent accuracy estimated from the bracketing procedure used in determining the thresholds. If both sets of data are assumed to be part of the same population we find $C = 295.5 \text{ mJ/cm}^2/$pulse and $\alpha = 0.178$ (R = 0.984). The power law is of the same form that we found previously for sequences of pulses having individual pulse durations between 0.001 and 1 sec and pulse repetition frequencies between 1 and 100 Hz, except that, for these longer pulses, the exponent $\alpha = 0.25$ and the coefficient depended on the duration of the individual pulses.\textsuperscript{5} Coincidentally, retinal damage thresholds for sequences of pulses are also described by a power law of this same form with $\alpha = 0.25$.\textsuperscript{13}

In order to calculate the temperature histories for these pulse sequences it was necessary to make minor modifications to our thermal program in order to obtain sufficient time resolution after the 80 ns pulses to capture the maximum temperature increase and yet not have too many points for a practical calculation. Thus the modification allowed for calculating temperatures at a number of

![Graph](image)

**Figure 1.** The dependence of the threshold energy density per pulse on the number of pulses at pulse frequencies of 10 and 16 Hz. The lines are least squares fits to a power law of the form $ED_n = CN^{-\alpha}$. The corresponding values of $C$ and $\alpha$ are given in the text. The error bars are ±10 percent of the values and represent the estimated accuracy of the bracketing procedure used in determining the thresholds.

Equally spaced points during each pulse and at a number of points with a wider interval between them after each pulse. The numbers of points during and after each pulse and the time interval after each pulse for which temperatures are calculated are inputs into the revised program. A listing of the revised program is given in Appendix 2.

We have completed the temperature calculations at the damage threshold for all of the 10 Hz and 16 Hz exposures. Figure 2 shows typical temperature histories at the damage threshold for
sequences of 32 and 128 pulses at a pulse repetition frequency of 16 Hz. The calculations are for the temperature history at a position on the beam axis, 10 µm beneath the surface of the tear layer;

![Graph](image)

**Figure 2.** Calculated temperature histories on the beam axis 10 µm beneath the tear surface at the threshold exposure for sequences of 32 pulses, and (b) 128 pulses at 16 Hz.
thus, assuming a tear layer thickness of about 7 μm, the temperature history is that just inside the anterior-most epithelial cells.\textsuperscript{5,7} Using the modified program we showed that the maximum temperature increase occurred ~164 μsec after the final pulse. The maximum temperature increases for all of the damage thresholds are listed in Table 1.

The damage condition is described by an essentially constant maximum temperature rise and is consistent with a critical peak temperature damage model. For the exposures at 10 Hz, damage occurs at $\Delta T_{\text{max}} = 29.4 \pm 2.8$ C (mean±SD), and for the exposures at 16 Hz, it occurs at $\Delta T_{\text{max}} = 32.0 \pm 2.0$ C. The maximum temperature rises for the two exposure conditions are shown graphically in Figure 3.

![Figure 3. The calculated maximum temperature rises on the beam axis 10 μm beneath the tear surface for the damage threshold exposure. The lines show the mean values of $\Delta T_{\text{max}}$ for the two exposure conditions.](image)

In the Introduction we noted that light and electron micrographs of corneas exposed to a single 80 ns pulse just above the damage threshold show features consistent with both thermal and mechanical (e.g., acoustic) damage.\textsuperscript{6, 7} However, the fact that the calculated maximum temperature rises listed in Table 1 and plotted in Figure 3 are essentially constant for all of damage thresholds suggests that, at least for the multiple-pulse exposures, the damage mechanism may be predominately thermal.

In order to test this suggestion, we performed a series of damage experiments on enucleated eyes cooled to room temperature (average 21 C) as described in Methods. The underlying hypothesis for this test is that if the critical temperature model is valid, then damage should occur for exposures that result in the same final critical temperature (not temperature increase). Thus in a cornea initially at room temperature, sufficient additional energy would have to be supplied first to raise the temperature to the \textit{in vivo} temperature and then to the final damage temperature. In a preliminary experiment using 8 pulses at 16 Hz we showed that corneas in the
cooled enucleated eyes did not incur damage at the same (slightly above threshold) exposure that produced a lesion in the in vivo cornea. This finding suggested that the damage mechanism was at least partially thermal. We then proceeded to determine damage thresholds in cooled corneas for sequences of 8 and 32 pulses at 16 Hz. The threshold energy densities and the calculated maximum temperature rises for these experiments are listed in Table 2. Assuming that the temperature of the anterior surface of an in vivo cornea is 35 C, the “damage temperatures” from Table 1 for the 8 and 32 pulse 16 Hz thresholds are respectively 339.5 K and 341.1 K; whereas they are respectively 354 K and 345.8 K in the corneas cooled to 21 C before exposure. The additional energy required to produce a minimal lesion in the cooled cornea is therefore sufficient to raise the cornea temperature to a level slightly higher than that associated with damage in vivo. These results are highly suggestive that the multiple pulse damage is indeed predominately thermal. We speculate that the increased “damage temperatures” in the enucleated eye experiments may be due a slowing down of the processes leading to the observed damage endpoint as a result of the lower ambient temperature. (Recall that we determine damage 1/2 hour after exposure and the enucleated eye is maintained in BSS at 21 C during this time.)

Table 2: Threshold Energy Densities and Calculated Maximum Temperature Rises for Enucleated Eyes at 21 C.

<table>
<thead>
<tr>
<th>Number of Pulsed</th>
<th>Pulse Repetition Frequency (Hz)</th>
<th>E_{th} (mJ/cm²/pulse)</th>
<th>d_{th} (mm)</th>
<th>ΔT_{max} (C)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>16</td>
<td>393</td>
<td>3.58</td>
<td>59.8</td>
</tr>
<tr>
<td>32</td>
<td>16</td>
<td>236</td>
<td>3.58</td>
<td>51.6</td>
</tr>
</tbody>
</table>

*Calculated on the beam axis 10 μm beneath the anterior tear surface.

We have submitted corneas with lesions to Dr. W. R. Green at the Wilmer Institute for histology. Corneas exposed slightly above the damage threshold for 8 pulses and 1024 pulses at 16 Hz were submitted prior to the end of this reporting period; however no results were available. We plan to submit additional tissue exposed just above the damage threshold for 8 pulses, 128 pulses, and 1024 pulses at 10 Hz and 128 pulses at 16 Hz.

Conclusions

Threshold damage to the corneal epithelium resulting from exposure to sequences of 80 ns pulses of CO₂ laser radiation is correlated by a power law of the form \( E_{th} = CN^{-\alpha} \) in which \( E_{th} \) is the threshold energy density and \( N \) is the number of pulses in the sequence. The constant \( C \) and exponent \( \alpha \) appear to differ slightly depending on the pulse repetition frequency. For sequences of pulses at 10 Hz, \( C = 291 \) mJ/cm²/pulse and \( \alpha = 0.162 \) and for sequences at 16 Hz, \( C = 300 \) mJ/cm²/pulse and \( \alpha = 0.194 \). Temperature calculations reveal that the maximum temperature increase on the beam axis 10 μm beneath the anterior tear surface resulting from the different threshold exposures is essentially constant. For the exposures at 10 Hz, damage occurs at \( \Delta T_{max} = 29.4 \pm 2.8 \) C (mean±SD), and for the exposures at 16 Hz, it occurs at \( \Delta T_{max} = 32.0 \pm 2.0 \) C. This result is consistent with a critical peak temperature damage model and suggests that, at least for the multiple-pulse exposures, the damage mechanism may be predominately thermal. Damage threshold measurements on corneas maintained at 21 C indicated that the damage mechanism is indeed predominately thermal.
References


Appendix 1

Personnel Paid by Contract DAMD17-96-C-6005:

R. L. McCally, Ph. D.  Principal Investigator
C. B. Barger, Ph. D.  co-Principal Investigator
C. D. Carter  Group Secretary
APPENDIX 2

Modified program for calculating temperature histories for sequences of very short pulses. Program allows for variable resolution following pulses.

PROGRAM CALCULATES TEMPERATURE-TIME HISTORIES FOR RADIATION INCIDENT ON A SEMI-INFINITE ABSORBING SLAB
RADIATION CAN BE EITHER CW OR SEQUENCES OF PULSES RADIATION AND CONVECTIVE HEAT TRANSFER ARE IGNORED
PROGRAM ADAPTED BY R. MCCALLY SEPTEMBER 25, 1997 FROM PROGRAM TCALF TO PROVIDE INCREASED TIME RESOLUTION AFTER PULSES

S0 = IRRADIANCE (W/(CM*CM))
KAPPA = THERMAL CONDUCTIVITY (CAL/(CM*DEGC))
R = RADIAL DIST FROM BEAM AXIS (CM)
Z = DEPTH (CM)
RE = 1/E BEAM RADIUS (CM)
TAU = PULSE DURATION (SEC)
TAFFT = INCREASED RESOLUTION INTERVAL AFTER PULSES
C = HEAT CAPACITY (CAL/(GM*DEGC))
GAM = INVERSE ABSORPTION LENGTH (1/CM)
DELT = 1/PRF (SEC) --- DELT MUST BE >= TAU
NP = NUMBER OF PULSES
ND = NUMBER OF INTERVALS CALCULATED DURING EACH PULSE
NDAP = NUMBER OF POINTS IN THE INTERVAL TAFFT AFTER EACH PULSE
NPTS = NUMBER OF CALCULATED POINTS = NP*(ND+NDAP) + 1 (CALC IN PGM)
NRRUNS = NUMBER OF SETS OF INPUT DATA
IRULE - CHOICE OF QUADRATURE RULE IN DQDAG. (INPUT)
A GAUSS-KRONROD RULE IS USED WITH
7 - 15 POINTS IF IRULE = 1
10 - 21 POINTS IF IRULE = 2
15 - 31 POINTS IF IRULE = 3
20 - 41 POINTS IF IRULE = 4
25 - 51 POINTS IF IRULE = 5
30 - 61 POINTS IF IRULE = 6
IRULE = 2 IS RECOMMENDED FOR MOST FUNCTIONS.
IF THE FUNCTION HAS A PEAK SINGULARITY USE IRULE = 1.
IF THE FUNCTION IS OSCILLATORY USE IRULE = 6.

PROGRAM IRTEMP

IMPLICIT REAL*8(A-H,O-Z)
REAL*8 KAPPA
COMMON/BLOCKA/ ZO,ONE,TWO,TEN,HUN,SPI,W,ZA,GTA,AZ,E2,R2, XO,
TEGR, G2FA
DIMENSION TIME(0:62000), T1(0:62000), TEMP(0:62000), TEMPN(0:62000)
C T1 ARE TIME POINTS DURING AND AFTER A SINGLE PULSE
CHARACTER*1 TAB
EXTERNAL FF
C
INN = 7       ! DEFINES INPUT LOGICAL UNIT
IOUT = 8      ! DEFINES OUTPUT LOGICAL UNIT FOR FINAL DATA FILE
ISCREEN = 6    ! DEFINES LOGICAL UNIT FOR OUTPUT TO SCREEN
ICOUNT = 0    ! INITIALIZE COUNTER FOR TIMES INPUT FILE IS ACCESSED
C
DEFINE CONSTANTS
ZO = 0.0D0
ONE = 1.0D0
TWO = 2.0D0
TEN = 10.0D0
HUN = 100.0D0
PI = 4.0D0 * DATAN( ONE )
SPI = DSQRT( PI )
TAB = CHAR(9)  ! TAB IS ASC 9
C
OPEN I/O FILES
OPEN (UNIT=INN, FILE = 'IRINHRES', STATUS='OLD', ACCESS='SEQUENTIAL', BLANK='NULL')
OPEN (UNIT=IOUT, FILE = 'IROUT.HIRES', STATUS='UNKNOWN', ACCESS='SEQUENTIAL')
C
1000 CONTINUE
C
GET INPUT DATA
CALL
INPUT(S0,KAPPA,R,Z,RE,TAU,TAFFT,C,GAM,DELT,NP,ND,NDAP,RHO,NRUNS,I
COUNT,
INN,IOUT,ISCREEN,AERR,RERR,IRULE)
C
NT = ND+NDAP
NPTS = NP*(NT+1)
WRITE(ISCREEN,3)NPTS
WRITE(IOUT,3)NPTS
C
A2 = RHO*C/(4.0D0*KAPPA)
TSIG = RE*RE
R2 = R*R
FRONT = S0*GAM/(8.36D0*RHO*C)
ZA = Z**2 * A2
AZ = DSQRT(ZA )
TA = TWO * DSQRT( A2 )
GTA = GAM/TA
XO = TWO*A2*Z/GAM
TEGZ = TWO * DEXP(-GAM*Z)
G2FA = GAM**2 / (4.0D0*A2)
W = A2 * TSIG
C
C CALCULATE TIME POINTS
DO 30 I=0,ND
T1(I) = I*TAU/ND
30 CONTINUE
C
ND1 = ND + 1
C
DO 31 I=ND1,NT
   T1(I) = TAU + (I-ND)*TAAFT/NDAP
31 CONTINUE
C
IF (NP,EQ.1) GO TO 38
C
DO 36 J=1,NP
   JNT = (J-1)*(NT+1)
   DO 32 I=JNT,JNT+ND
      K = I - JNT
      TIME(I) = T1(K) + (J-1)*DELT
32 CONTINUE
   DO 33 I=JNT+ND1,JNT+NT
      K = I - JNT
      TIME(I) = T1(K) + (J-1)*DELT
33 CONTINUE
36 CONTINUE
C
GO TO 40
C
38 DO 39 I=0,NT
   TIME(I) = T1(I)
39 CONTINUE
C
40 TIME(NPTS) = NP*DELT
C
BEGIN TEMPERATURE CALCULATION
TEMP(0) = Z0
C
WRITE(ISCREEN,4)
C
WRITE(IOUT,5)TAB,TAB,TAB,TAB
C
DO 100 I=1,NPTS
   TL = TIME(I)
   IF(TIME(I)-TAU .GT. TL) TL=TIME(I)-TAU
   TU = TIME(I)
   CALL DQDAG (FF, TL, TU, AERR, RERR, IRULE, PSI, ERREST)
C
DQDAG IS AN IMSL ROUTINE FOR EVALUATING THE INTEGRAL. IT IS A
C
GLOBALLY ADAPTIVE SCHEME THAT IS BASED ON GAUSS-KONRAD
C
RULES
   TEMP(I) = FRONT * PSI
C
WRITE(ISCREEN,6) I,PSI,TIME(I),TEMP(I),ERREST
C
WRITE(IOUT,7) I,TAB,PSI,TAB,TIME(I),TAB,TEMP(I),TAB,ERREST
100 CONTINUE
C
DO 150 I=0,NPTS
   TEMPN(I) = TEMP(I)
150 CONTINUE
C
IF (NP,EQ.1) GO TO 375
C HANDLE MULTIPLE PULSES
C
DO 300 J=2,NP
   JNT = (J-1)*(NT+1)
   DO 200 I=0,NPTS
      IF (I.LT.JNT) THEN
         TEMPN(I) = TEMPN(I)
      ELSE
         TEMPN(I) = TEMPN(I) + TEMP(I-JNT)
      END IF
200 CONTINUE
300 CONTINUE

C WRITE TO FINAL DATA FILE
375 WRITE(IOUT,380)TAB,TAB      ! WRITE HEADER FOR RESULTS
   DO 400 I=0,NPTS
      WRITE(IOUT,390) I,TAB,TIME(I),TAB,TEMPN(I)
400 CONTINUE
   IF (ICOUNT .LT. NRUNS) GO TO 1000
99 STOP

3 FORMAT( ' NPTS = ',I5, ' TOTAL POINTS ' )
4 FORMAT(T3,T,T11,'PSI',T25,'TIME',T36,'TEMPERATURE',T52,'ERROR')
5 FORMAT(T,A1,'PSI',A1,'TIME',A1,'TEMPERATURE',A1,'ERROR')
6 FORMAT(I5,1PG14.6,1PG14.6,1PG14.6,1PG14.6)
380 FORMAT(T,A1,'TIME',A1,'TEMPERATURE')
390 FORMAT(I5,A1,1PE14.8,A1,1PE14.8)
END

C
C FUNCTION FF ( X )
C THIS DESCRIBES THE INTEGRAND
IMPLICIT REAL*8(A-Z)
COMMON/BLOCKA/ ZO,ONE, TWO, TEN, HUN, SPL, W, ZA, GTA, AZ, E2, R2, XO,
   1TEGZ, G2FA
C
IF(X .EQ. ZO) GO TO 50
C
X2 = DSQRT( X )
XW = ONE + X/W
EE = -R2/XW
E1 = ZO
IF(DABS(EE) .LE. HUN) E1 = DEXP( EE )
C
E2 = -ZA/X
C
C1 = GTA * X2
C2 = AZ/X2
ARG1 = C1 + C2
ARG2 = C1 - C2
H1 = HFUN( ARG1 )
H2 = HFUN( ARG2 )
C
IF(X.GT.XO) GO TO 10
C... FOR X LESS THEN XO AND NOT ZERO 6/2/80 THE REVISION
   FO = E1/XW
   G1 = TEGZ * DEXP(G2FA*X)
   G2=Z0
   IF(DABS(E2).GT. HUN) GO TO 30
      H1 = HFUN(DABS(ARG1))
      H2 = HFUN(DABS(ARG2))
   G2 = (H1-H2)
C
   30 FF = FO*(G1 + G2)
   RETURN
C
   10 CONTINUE
      FF = E1 * (H1 + H2) / XW
   RETURN
C... FOR X= 0 ONLY
   50 CONTINUE
      FF = TEGZ * DEXP(-R2)
   RETURN
END
C
C
FUNCTION HFUN ( ARG )
IMPLICIT REAL*8(A-Z)
COMMON/BLOCKA/ ZO,ONE,TWO, TEN, HUN, SPI, W, ZA, GTA, AZ, E2, R2, XO,
ITEGZ, G2FA
DATA HALF, ONE / 0.5D0, 1.50D0/
C
   Y = DABS( ARG )
   Y2 = Y*Y
   HFUN = ZO
   BB = Y2 + E2
   IF(ARG .GE. -13.0D0) GO TO 10
      B1=ZO
   IF(DABS(BB) .LE. 174.0D0) B1 = TWO * DEXP(BB)
      B2 = ZO
   IF(DABS(E2) .LT. 174.0D0) B2 = DEXP(E2) /
      * (SPI*(Y+HALF(Y+ONE/(Y+ONEH/(Y+TWO/Y))))
         HFUN = B1 - B2
   RETURN
10 CONTINUE
   IF(ARG .GE. ZO) GO TO 20
   IF(DABS(BB) .LT. 174.0D0) HFUN = DEXP(BB)*(TWO-DERFC(Y))
   RETURN
20 CONTINUE
   IF(ARG .GT. 13.0) GO TO 30
   IF(DABS(BB) .LT. 174.0D0) HFUN = DEXP(BB)*DERFC(ARG)
   RETURN
30 CONTINUE
   IF(DABS(E2) .GT. 174.0D0) GO TO 40
   Z = ARG
   HFUN = SPI*(Z+HALF/(Z+ONE/(Z+ONEH/(Z+TWO/Z))))
   IF(HFUN .NE. ZO) HFUN = DEXP(E2)/HFUN
40 RETURN
END

C
C FUNCTION DERFC(X)
C RETURNS THE COMPLEMENTARY ERROR FUNCTION
C CHECKS WITH MATHEMATICA TO 15 SIGNIFICANT FIGURES
C IN RANGE (.001 <= X <= 4.0) (MAXIMUM PRINTOUT FROM MATHEMATICA
C AND MAXIMUM RANGE CHECKED 3/18/96 RLM)
C
IMPLICIT REAL*8 (A-H,O-Z)
DATA Z0,HALF,ONE/0.0D0,0.5D0,1.0D0/
IF(X.LT.Z0)THEN
   DERFC=ONE+GAMMP(HALF,X**2)
ELSE
   DERFC=GAMMQ(HALF,X**2)
ENDIF
RETURN
END

C
FUNCTION GAMMP(A,X)
IMPLICIT REAL*8 (A-H,O-Z)
DATA Z0,HALF,ONE/0.0D0,0.5D0,1.0D0/
IF(X.LT.Z0.0D0)PAUSE
IF(X.LT.Z0.OR.A.LE.Z0)PAUSE
CALL GSER(GAMSER,A,X,GLN)
GAMMP=GAMSER
ELSE
   CALL GCF(GAMMCF,A,X,GLN)
   GAMMP=ONE-GAMMCF
ENDIF
RETURN
END

C
FUNCTION GAMMQ(A,X)
IMPLICIT REAL*8 (A-H,O-Z)
DATA Z0,HALF,ONE/0.0D0,0.5D0,1.0D0/
IF(X.LT.Z0.0D0)PAUSE
IF(X.LT.Z0.OR.A.LE.Z0)PAUSE
CALL GSER(GAMSER,A,X,GLN)
GAMMQ=ONE-GAMSER
ELSE
   CALL GCF(GAMMCF,A,X,GLN)
   GAMMQ=GAMMCF
ENDIF
RETURN
END

C
SUBROUTINE GSER(GAMSER,A,X,GLN)
IMPLICIT REAL*8 (A-H,O-Z)
DATA Z0,HALF,ONE/0.0D0,0.5D0,1.0D0/
PARAMETER (ITMAX=400, EPS=10D-17)
GLN = 0.5723649429247001D0 ! LN(SQRT(PI)) = GAMMA(1/2)
IF(X .LE. Z0) THEN
  IF(X .LT. Z0) PAUSE
  GAMSER = Z0
  RETURN
END IF
AP = A
SUM = ONE/A
DEL = SUM
DO 11 N = 1, ITMAX
  AP = AP + ONE
  DEL = DEL * X/AP
  SUM = SUM + DEL
  IF(DABS(DEL).LT.DABS(SUM)*EPS) GO TO 1
11 CONTINUE
PAUSE 'A TOO LARGE, ITMAX TOO SMALL'
1 GAMSER = SUM*DEXP(-X*A*DLOG(X)-GLN)
RETURN
END

C
SUBROUTINE GCF(GAMMCF, A, X, GLN)
IMPLICIT REAL*8 (A-H, O-Z)
DATA Z0, HALF, ONE/0.0D0, 0.5D0, 1.0D0/
PARAMETER (ITMAX=400, EPS=10D-17)
GLN = 0.5723649429247001D0 ! LN(SQRT(PI)) = GAMMA(1/2)
GOLD = Z0
A0 = ONE
A1 = X
B0 = Z0
B1 = ONE
FAC = ONE
DO 11 N = 1, ITMAX
  AN = DFLOAT(N)
  ANA = AN/A
  A0 = (A1 + A0*ANA)*FAC
  B0 = (B1 + B0*ANA)*FAC
  ANF = AN*FAC
  A1 = X*A0 + ANF*A1
  B1 = X*B0 + ANF*B1
  IF(A1 .NE. Z0) THEN
    FAC = ONE/A1
    G = B1*FAC
    IF(DABS((G-GOLD)/G).LT.EPS) GO TO 1
    GOLD = G
  ENDIF
11 CONTINUE
PAUSE 'A TOO LARGE, ITMAX TOO SMALL'
1 GAMMCF = DEXP(-X*A*DLOG(X)-GLN)*G
RETURN
END

C

SUBROUTINE INPUT(S0, KAPPA, R, Z, RE, TAU, TAAFT, C, GAM, DELT, NP, ND,
INDAP, RHO, NRUNS, ICOUNT, INN, IOUT, ISCREEN, AERR, ERR, IRULE

C-----------------------------------------------------------------------------------

IMPLICIT REAL*8(A-H,O-Z)
REAL*8 KAPPA
C   INTEGER*4 NPTS, NP, ND, NDAP, NRUNS, ICOUNT, INN, IOUT, ISCREEN, IRULE, I
CHARACTER*9 DAY
CHARACTER*11 AD1
CHARACTER*30 AIN2

C PURPOSE: READ INPUT FILE IRINPUT AND WRITE PARAMETERS.
C
C INPUT: INN, IOUT, ISCREEN
C
C
C OUTPUT: S0, KAPPA, R, Z, RE, TAU, TAAFT, C, GAM, DELT, NP, ND, NDAP,
C   RHO, NRUNS, ICOUNT, AERR, ERR, IRULE.
C
ICOUNT=ICOUNT+1 ! INCREMENT FILE ACCESS COUNTER
C READ FILE INN.
C
READ(INN,'(A30)',END=99,IOSTAT=I) AIN2 ! READ HEADER
READ(INN,'(A30)',END=99,IOSTAT=I) AIN2 ! READ ----
READ(INN,'(A11)',END=99,IOSTAT=I) AD1 ! READ 123 ETC
READ(INN,'(A11,15)',END=99,IOSTAT=I) AD1, NRUNS
READ(INN,'(A11,1PG14.6)',END=99,IOSTAT=I) AD1, S0
READ(INN,'(A11,1PG14.6)',END=99,IOSTAT=I) AD1, TAU
READ(INN,'(A11,1PG14.6)',END=99,IOSTAT=I) AD1, TAAFT
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, RE
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, Z
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, R
READ(INN,'(A11,15)',END=99,IOSTAT=I) AD1, NP
READ(INN,'(A11,1PG14.6)',END=99,IOSTAT=I) AD1, DELT
READ(INN,'(A11,15)',END=99,IOSTAT=I) AD1, ND
READ(INN,'(A11,15)',END=99,IOSTAT=I) AD1, NDAP
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, GAM
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, C
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, KAPPA
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, RHO
C......INTEGRATION PARAMETERS:
READ(INN,'(A11,F14.9)',END=99,IOSTAT=I) AD1, AERR
READ(INN,'(A11,1PD14.9)',END=99,IOSTAT=I) AD1, ERR
READ(INN,'(A11,15)',END=99,IOSTAT=I) AD1, IRULE
C
C WRITE INPUT TO FILE IRROUT (DISK DATA FILE)
C
WRITE(IOUT,100)
WRITE(IOUT,105)
CALL DATE(DAY)
WRITE(IOUT,110) DAY
AIN2 = * 'INPUT PARAMETERS'
WRITE(IOUT,110) AIN2
WRITE(IOUT,150) NRUNS
WRITE(IOUT,151) S0
WRITE(IOUT,152) TAU
WRITE(IOUT,167)TAAFFT
WRITE(IOUT,153)RE
WRITE(IOUT,154)Z
WRITE(IOUT,166)R
WRITE(IOUT,155)NP
WRITE(IOUT,156)DELT
WRITE(IOUT,157)ND
WRITE(IOUT,158)NDAP
WRITE(IOUT,159)GAM
WRITE(IOUT,160)C
WRITE(IOUT,161)KAPPA
WRITE(IOUT,162)RHO
AIN2 = 'INTEGRATION PARAMETERS: '
WRITE(IOUT,110)AIN2
WRITE(IOUT,163)IRULE
WRITE(IOUT,164)AERR
WRITE(IOUT,165)RERR
C
C WRITE INPUT TO SCREEN
C
WRITE(ISCREEN,100)
WRITE(ISCREEN,110)DAY
AIN2 = 'INPUT PARAMETERS'
WRITE(ISCREEN,110)AIN2
WRITE(ISCREEN,150)NRUNS
WRITE(ISCREEN,151)S0
WRITE(ISCREEN,152)TAU
WRITE(ISCREEN,167)TAAFFT
WRITE(ISCREEN,153)RE
WRITE(ISCREEN,154)Z
WRITE(ISCREEN,166)R
WRITE(ISCREEN,155)NP
WRITE(ISCREEN,156)DELT
WRITE(ISCREEN,157)ND
WRITE(ISCREEN,158)NDAP
WRITE(ISCREEN,159)GAM
WRITE(ISCREEN,160)C
WRITE(ISCREEN,161)KAPPA
WRITE(ISCREEN,162)RHO
AIN2 = 'INTEGRATION PARAMETER: '
WRITE(ISCREEN,110)AIN2
WRITE(ISCREEN,163)IRULE
WRITE(ISCREEN,164)AERR
WRITE(ISCREEN,165)RERR
99 CONTINUE
C
C FINAL WRITE STATEMENTS
C
WRITE(IOUT,120)
WRITE(ISCREEN,120)
RETURN
C
100 FORMAT('/ ---WE ARE IN IRINHRES---/')
105 FORMAT('/ ---FILE IROUT.HIRES---/')
110 FORMAT(A35)
120 FORMAT('  ---LEAVING IRINHRES--- ')  
130 FORMAT( '...')
150 FORMAT( 'NRUNS = ', I5)
151 FORMAT( ' SO = ', PG14.5,' WATTS/CM**2')
152 FORMAT( ' TAU = ', PG14.5,' SEC')
153 FORMAT( ' RE = ', F14.5,' CM')
154 FORMAT( ' Z = ', F14.5,' CM')
155 FORMAT( ' NP = ', I5,' PULSES')
156 FORMAT( ' DELT = ', PG14.5,' SEC')
157 FORMAT( ' ND = ', I5,' POINTS/PULSE')
158 FORMAT( ' NDAP = ', I5,' POINTS AFTER PULSE')
159 FORMAT( ' GAM = ', F14.5,' 1/CM')
160 FORMAT( ' C = ', F14.5,' CAL/(GM*DEGC)')
161 FORMAT( ' KAPPA = ', F14.5,' CAL/(CM**2*DEGC)')
162 FORMAT( ' RHO = ', F14.5,' GM/CM**2')
163 FORMAT( ' IRULE = ', I5)
164 FORMAT( ' AERR = ', F14.5)
165 FORMAT( ' RERR = ', PD14.5)
166 FORMAT( ' R = ', F14.5,' CM')
167 FORMAT( ' TAAFT = ', PG14.5,' SEC')

END