TRANSOM: A MULTI-METHOD REYNOLDS-AVERAGED NAVIER-STOKES SOLVER: OVERALL DESIGN

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Abstract

TRANSOM is a multi-block, multi-method Reynolds-Averaged Navier Stokes solver being developed at DREA to address problems associated with the flow around ships and submarines. It is multi-block because the flow is divided into several distinct regions. It is multi-method because a different solution method may be used on each of the flow regions. At present two different methods of solution can be chosen: a finite-volume solver based on the pseudo-compressibility method; and a finite element solver which uses the penalty function method to determine the pressure.

TRANSOM is written in C++ following principles of Object Oriented Programming. This document describes the overall design of TRANSOM with emphasis on the class hierarchies used to represent different types of blocks and flow solvers. The algorithms used to implement the pseudo-compressibility and finite element methods are not discussed here; two companion reports describe these sub-solvers in detail.

Résumé

TRANSOM est un résolveur Navier-Stokes pondéré Reynolds, multiméthode, multibloc, que le CRDA est en train de développer pour résoudre des problèmes concernant l'écoulement autour des navires et des sous-marins. Il est multibloc parce que l'écoulement se divise en plusieurs régions distinctes. Il est multiméthode parce qu'il permet d'utiliser une technique de solution différente pour chacun des régions de l'écoulement. A l'heure actuelle on peut choisir entre deux méthodes de solution: un résolveur à volumes finis basé sur la méthode de pseudo-compressibilité et un résolveur par éléments finis qui utilise la méthode de la fonction de pénalité pour déterminer la pression.

TRANSOM a été écrit en C++ en suivant les principes de la programmation orientée objet. Ce document décrit la conception générale de TRANSOM et met l'accent sur les hiérarchies de classe utilisées pour représenter différents types de blocs et de résolveurs d'écoulement. Les algorithmes utilisés pour mettre en oeuvre les méthodes de pseudo-compressibilité et par éléments finis ne sont pas traités ici. Deux rapports d'accompagnement décrivent ces sous-résolveurs en détail.
Executive Summary

Background

The numerical prediction of marine propeller performance and cavitation requires an accurate prediction of the nominal wake: that is, the flow into the propeller plane without the influence of the propeller itself. At DREA, the nominal wake is currently calculated with the HLLFLO programs which use a panel method to predict the potential flow and a boundary layer method to predict the viscous flow.

The HLLFLO programs have the advantage that they are very fast. They yield fairly good predictions for unappended destroyer hulls; however, there are several areas in which the predictions can be improved.

1. As is typical of boundary layer methods, the wake deficit is over-predicted near the stern. This is especially noticeable at model-scale Reynolds numbers.
2. HLLFLO is incapable of handling the flow past appendages. The wakes shed from the propeller shafts and shaft brackets can cause significant spatially concentrated wake defects which, in turn, affect higher harmonics of the radiated propeller noise and the speed at which cavitation first occurs.
3. HLLFLO does not account for the influence of the boundary layer on the potential flow.

These effects are especially important for smaller vessels with low length/beam ratios. Moreover, HLLFLO is incapable of handling the complex geometries of submarines or advanced marine vehicles such as small water area twin hull (SWATH) ships.

Principal Results

The program TRANSOM has been developed address these deficiencies. TRANSOM is a multi-block, multi-method Reynolds-Averaged Navier Stokes solver; multi-block because the flow is divided into several distinct regions called blocks; multi-method because a different solution method may be used on each of the blocks.

The current version of TRANSOM includes two different solution
methods which can be used on the blocks. The first is a pseudo-compressibility method based on the work of Rogers and Kwak; it is suitable for use on structured blocks. The second uses the finite element method and is based on the program MEF developed at Université Laval; it is suitable for use on unstructured blocks. Turbulence may be modelled using variants of the k-ε model or by the Baldwin-Lomax model. Currently only two-dimensional flow can be modelled.

TRANSOM is written in C++ following principles of Object Oriented Programming. This document describes the overall design of TRANSOM and, in particular, the class hierarchies used to represent different types of blocks and flow solvers. The algorithms used to implement the pseudo-compressibility and finite element methods are not discussed here; two companion reports describe these sub-solvers in detail.

Significance of Results

When TRANSOM is fully developed it will provide accurate numerical predictions of the flow into the propeller plane. It will also be applicable to many other flow problems related to ships: for example, flow around submarines, vortex generation from propellers and control surfaces, bilge vortex generation, prediction of roll damping coefficients, and prediction of the lift and drag characteristics of lifting surfaces such as submarine control planes, rudders, and fin stabilizers.

Future Work

TRANSOM is still under development; the current version will only solve two-dimensional flows and requires upgrading in many areas, in particular the ways in which different solution methods interact at their common block boundaries. Further development will be done at DREA and under contract.
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1 Introduction

At high speeds the noise radiated by a warship is primarily due to cavitation on its propellers. Naval propellers are designed so that cavitation inception is delayed to as high a speed as possible, but the design method requires an accurate prediction of the flow into the propeller plane. Over the past decade computer programs have been developed at DREA to predict the flow into the propeller plane. Known collectively as HLLFLO[1], these programs use a low-order panel method to predict the potential flow and a boundary layer method to calculate the viscous flow.

The HLLFLO programs have the advantage that they are very fast. They yield fairly good predictions for unappended destroyer hulls[2]; however, there are several areas in which the predictions can be improved.

1. As is typical of boundary layer methods, the wake deficit is over-predicted near the stern. This is especially noticeable at model-scale Reynolds numbers.

2. HLLFLO is incapable of handling the flow past appendages. The wakes shed from the propeller shafts and shaft brackets can cause significant spatially concentrated wake defects which, in turn, affect higher harmonics of the radiated propeller noise and the speed at which cavitation first occurs.

3. HLLFLO does not account for the influence of the boundary layer on the potential flow.

These effects will be exacerbated by the current trend toward smaller vessels with smaller length/beam ratios. Moreover, HLLFLO is incapable of handling the complex geometries of submarines or advanced marine vehicles such as SWATHs.

The program TRANSOM is intended to address these deficiencies. TRANSOM is a Reynolds-Averaged Navier-Stokes (RANS) solver: in conjunction with a turbulence model, it solves the Navier-Stokes equations on a grid of points which cover the regions of flow.

The chief practical problem in developing a Navier-Stokes solver for the flow past a ship is that the Reynolds Number is so high: for a destroyer moving at 20 knots the Reynolds number is about \(10^9\). The higher the Reynolds number, the more grid points are necessary to resolve the severe velocity gradients near solid surfaces. For this reason, issues of computer storage are of extreme importance.

Because of the complex geometries of appended surface ships or submarines, the type of grid used in the calculations is also important because it affects the amount of computer storage required. Methods which allow the use of unstructured grids (e.g. finite element solvers) typically require far greater computer storage than methods which require structured grids. Thus, there is a trade-off between the ease generating the grid, and the storage requirements. To address this problem, TRANSOM has been designed as a
multi-block multi-method solver. The numerical grid may consist of several blocks, some of which are structured, some unstructured. On each block a solver appropriate to the block structure is used. Since the areas of complex geometry are usually small in comparison with the whole ship, it should be possible to reduce the computer storage requirements significantly.

The current version of TRANSOM includes two different solution methods which can be used on the blocks. The first is based on the program NSI2D developed for DREA under contract to the University of Toronto[3,4,5]; it is suitable for use on a single structured block. The algorithm is a variant of the pseudo-compressibility method developed by Rogers and Kwak[6]. Currently only two-dimensional flow can be modelled; NSI2D was extended to three-dimensional flow in 1996 but the changes have not yet been incorporated into TRANSOM. Turbulence may be modelled either by the Baldwin-Lomax model[7] or by the Chen-Patel variant of the k-ε model[8]. Implementation of the Baldwin-Barth model[9] is currently underway.

The second solution is based on the finite element program MEF developed at Université Laval[10]; it is suitable for use on unstructured blocks. MEF was modified at DREA to model turbulence using a variant of the k-ε model[11]. However, the turbulence modelling has not yet been incorporated into TRANSOM; the finite element solver is currently restricted to two-dimensional laminar flow.

The name TRANSOM stands for The Reynolds-Averaged Navier-Stokes Omnigenic Method, a rather strained attempt to generate an acronym that is both easy to remember and has a connection with the ship-based flows for which TRANSOM is to be used.

TRANSOM is written in C++ following principles of Object Oriented Programming. This document describes the overall design of TRANSOM and, in particular, the class hierarchies used to represent different types of blocks and flow solvers. The algorithms used to implement the pseudo-compressibility and finite element methods are not discussed here; two companion reports[12,13] describe these sub-solvers in detail.

TRANSOM is still under development; the current version will only solve two-dimensional flows and requires upgrading in many areas, in particular the ways in which different solution methods interact at their common block boundaries. Further development will be done both at DREA and under contract.

When TRANSOM is fully developed it will provide accurate numerical predictions of the flow into the propeller plane. It will also be applicable to many other flow problems related to ships: for example, flow around submarines, vortex generation from propellers and control surfaces, bilge vortex generation, prediction of roll damping coefficients, and prediction of the lift and drag characteristics of lifting surfaces such as submarine control planes, rudders, and fin stabilizers.
TRANSOM is primarily concerned with three main types of object: collections of points such as grids, structured blocks, and unstructured blocks; collections of variables at the points of the grid; and solvers. Class hierarchies for each of these objects are described in Sections 2 to 4. Section 5 describes the TRANSOM main program. A user's guide for the program is also provided in Reference [14].

TRANSOM input and output files use the OFFSRF format described in Reference 15. Reference 16 describes C++ classes which implement specialized input and output streams for OFFSRF files and a base class which is inherited by all classes which read from or write to OFFSRF files; it should be read prior to this document for a proper understanding of TRANSOM input and output.

2 Grids, Blocks and Point Collections

In TRANSOM, the flow is approximated by specifying flow parameters (velocity, pressure, turbulence model variables, etc.) at each point of a grid. Borrowing from finite element jargon, we will call each point in a grid a node.

Collections of nodes may be ordered in many different ways. For example, a grid is simply a collection of sub-grids or blocks. A block may be structured, i.e. it can be ordered into a rectangular array of points, or unstructured, like the grids used in calculations using the finite element method. In TRANSOM, the organization of a collection of points is recognized as an important abstraction independent of the points themselves; it is represented by the class NodeOrg described in Section 2.3.

There are several classes for representing different types of collections of points, each of which is derived from the base class PointColl. Figure 1 shows the class hierarchy for the most important of these classes. In this section the PointColl and Grid classes are described. The class SBlock and its specializations S2dBlock and S3dBlock represent structured blocks; they are described in Reference 12. The class FEBlock represents an unstructured block organized into elements suitable for finite element calculations; it is described in Reference 13.

2.1 Nodes

The Node class is used as an index to the nodes in a grid. In TRANSOM the Node class is implemented as an integer: the number of the node.

Since a Node is simply an index, its value depends on a numbering system for the collection of nodes. In different contexts the same nodes may be numbered in different ways. For example, consider a grid of 300 nodes which are separated into three blocks of 100 nodes each. In a function which uses the whole grid, the nodes of the third block are numbered from 200 to

3
299. However, in a function which uses only one block at a time, it may be more convenient to number the 100 nodes of the third block from 0 to 99. In both cases the Node class is used to store the number of the nodes.

The allocation of a numbering system to a collection of nodes is the job of node organizers, discussed in the Section 2.3.

2.2 Node Iterators

An iterator is a class which returns, in some well-defined sequence, each object in a collection of objects. A NodeIter is an iterator over a collection of nodes. Suppose that iter is a NodeIter. Then the iteration can be performed as follows:

```cpp
ter.reset();
while(iter.in_range())
{
    Node n = (Node)iter;
    // Do something with n
    iter.next();
}
```

At any time during the iteration the current node may be obtained by casting the iterator to a Node; in the above code this is done on the first line in the while loop. This syntax is very convenient when the node is to be used as an argument to a function; then the conversion will take place automatically if the iterator is used as the argument. TRANSOM uses a similar syntax for all its iterator classes.

The member function reset() resets the iterator to the first node in the collection. The member function next() advances the iterator to the next node; most iterators also have a prev() function which backs the iteration up to the previous node. The member function in_range() returns true if the current node belongs to the collection, false if it does not (i.e. if the iteration has finished).
For maximum efficiency, the member functions of a Node is not virtual functions; however, there are many cases in which it is necessary that they be so. For this reason a second class, AllNode is also provided. It is identical to Node, but its member functions are declared virtual. The name AllNode arises from the main use of the base class, namely to iterate over all the nodes in a collection (see the next section).

2.3 Node Organizers

Algorithms for solving the Navier-Stokes equations are almost always highly dependent on the way in which the nodes are organized. Finite difference and finite volume methods usually require structured grids: i.e. grids which are organized into rectangular arrays of nodes. For finite element methods the grids need not be structured but they must be sub-divided into elements of different kinds; each element is itself a collection of nodes. Multigrid methods can require a hierarchy of grids: each grid in the hierarchy is a subset of its parent so that a sparser covering of the fluid domain is provided. Other subsets of a grid, such as its boundaries, are also commonly considered as separate collections of nodes.

In TRANSOM the structure of collections of nodes is described by classes called node organizers. Implicit in each node organizer is a numbering scheme for the nodes. The full range of node numbers used by the numbering scheme is from zero to \( N - 1 \), where \( N \) is called the "maximal number of nodes". However, since the node organizer may only describe a subset of the full range of nodes, \( N \) is not necessarily the same as the number of nodes governed by the node organizer.

For example, consider a collection of eleven nodes numbered \( 0, \ldots, 10 \). A node organizer, norg, is used to represent the odd numbered nodes. Then the maximal number of nodes for norg is 11, while the number of nodes governed by norg is only 5.

Most member functions of node organizers do one of four things.

1. They return the size of the collection of nodes. All node organizers will return the total number of nodes. Node organizers for structured grids also return the dimensions of the rectangular node array. Node organizers for finite element blocks return the number of elements of which the block is comprised.

2. They return node iterators which navigate through the nodes in various ways. All node organizers return a iterator which iterates over all the nodes in the collection. Node organizers for structured blocks return iterators over a single row or column of the block.

3. They return node organizers which describe a subset of the node collection. For example, node organizers for finite element blocks will return node organizers for any of the elements which they contain.

4. They alter the node organizer so that it describes a subset (or superset) of
Figure 2: Class hierarchy for the NodeOrg Class and its specializations

the original collection of nodes. This type of member function is particularly useful in multigrid solvers; the member function is called to restrict the node organizer to the nodes in the next level of the hierarchy.

It is important to recognize that node organizers contain no information on the location of a node in space; that is contained in the PointColl class and its specializations, described in the next section.

The base class for node organizers is NodeOrg. It has only two member functions:

- `unsigned num_nodes() const;` Returns the number of nodes organized by this NodeOrg.

- `virtual AllNodeIter* get_all_node_iter() const;` Returns a pointer to an AllNodeIter which iterates over the all the nodes in the current NodeOrg. Memory for the iterator is allocated from the heap and it is the responsibility of the calling function to delete the node iterator when it is finished using it.

Figure 2 shows the class hierarchy for the most important node organizers used in TRANSOM. The RNodeOrg class defines a restriction to a subset of the nodes in a collection; it is most useful for defining the rows or columns of structured block; it is described in Reference 12. The classes Base2dNodeOrg and S2dNodeOrg are used to organize structured two-dimensional blocks; they are described in Reference 12. The FENodeOrg class organizes nodes into a collection of elements for use in finite element calculations; it is described in Reference 13. The class ElementNodeOrg is used to organize the nodes in a single finite element and its specialization RefElement provides a description of a generic reference element; both classes are described in Reference 12.

2.4 Collections of Points

The coordinate values of a collection of nodes are represented by the PointColl class which is capable of describing points in one, two, or three dimensions. It is the base of a hierarchy of classes which describe collections of points with different structures; the most important classes in the
hierarchy are shown in Figure 1.

Each PointColl contains a NodeOrg which imparts the structure to the collection of points. The prototypes for the PointColl constructors are:

PointColl(unsigned ndim, const NodeOrg &norg, double *d = 0);
Makes a PointColl whose points are of dimension ndim (one, two, or three) and are organized by norg. If d is null, the default, new memory will be allocated from the heap to store the coordinate values; this memory is freed by the PointColl destructor. Otherwise the values will be stored in the memory beginning at d; in this case the memory is not freed by the PointColl destructor. Enough memory to store ndim* N doubles is required, where N is the maximal number of nodes of the node organizer.

PointColl(const PointColl &pc);
A copy constructor; new memory is allocated and the values in pc are copied to the new PointColl.

Each PointColl also has a name by which it can be referred. For example, when reading an input file, TRANSOM uses the name to allow two different solvers to share the same block. The block is defined independently of the solvers. The solvers specify the name of the block which they will use. The block is then found and passed to the solvers for use in calculating the flow.

Values for the name and for the coordinates may be read from an OFFSRF file using an extractor overloaded for the PointColl and OFFSRF_ifstream classes (see Reference 16 for a description of OFFSRF files and the class OFFSRF_ifstream). If p is a PointColl and in_stream is an OFFSRF_ifstream, then the code

    in_stream >> p;

will read the name and the coordinate values from the OFFSRF file associated with in_stream. The coordinates must be in the following format.

    {NAME: name }
    {COORDINATES
      x_1  y_1  z_1
      x_2  y_2  z_2
      :   :   :
      x_n  y_n  z_n
    }COORDINATES

For one-dimensional point collections the y and z values are missing from the COORDINATES record. For two-dimensional point collections only the z values are missing.

All point collections have the following member functions.

    unsigned num_nodes() const;
    Returns the number of nodes in the point collection.

    unsigned dim() const;
    Returns the dimension (one, two, or three) of the points.
const Str& get_name() const;
    Returns the name of the point collection (Str is a class representing
character strings).

NodeOrg *get_node_org() const;
    Returns a pointer to the node organizer which gives the point
    collection its structure.

double* operator[] (Node);
    Returns a pointer to the values of the coordinates. Thus, if p is a
    PointColl, then p[n][0] is the x-value of the coordinates at node n, p[n][1]
    is the y-value, and p[n][2] is the z-value.

2.5 Grids

A grid is a collection of points organized into blocks. It is represented by
the class Grid, a specialization of the class PointColl (see Figure 1). Each of the
blocks is also represented as a PointColl. Notice that, since a Grid is a type of
PointColl, this means that a grid can serve as the block of a different grid.

The coordinates of the points in the grid are shared with each of the
blocks. For example, suppose that g is a Grid which contains 100 points
shared among three blocks. The first block uses the first 30 of these points:
zero through 29. The second block uses the 50 points 30 through 79. The
third block uses the 30 points 70 through 99. Notice that the ten points 70
through 79 are used by two of the blocks.

The member function get_block returns a pointer to the block specified by
the argument name; its full prototype is

    PointColl* get_block(const Str &name) const;

All the PointColl member functions described in Section 2.4 are also inherited
by the Grid class.

The name, coordinate values, and the blocks of a grid are specified by a
GRID record in an OFFSRF input file. The GRID record has the following
format.

{GRID: ndim npts
 {NAME: name  }
 {COORDINATES
     x_1  y_1  z_1
     x_2  y_2  z_2
     \vdots \vdots \vdots
     x_n  y_n  z_n
 }COORDINATES
 {FIRST NODE: node block-name }
 Records to specify the blocks
 }GRID

where ndim is the dimension of the coordinates (one, two, or three), and npts
is the number of points in the grid. For one-dimensional point collections
the y and z values are missing from the COORDINATES record. For two-dimensional point collections only the z values are missing.

Currently three different types of blocks may be specified; each has an associated class (derived from PointColl) and OFFSRF record.

1. The record FE BLOCK causes an FEBlock to be created and added to the grid. These blocks are used in finite element solvers. The FEBlock class is described in detail in Reference 13. The FE BLOCK record contains data which define the FEBlock.

2. The record STRUCTURED BLOCK causes an S2dBlock to be created and added to the grid. This class describes structured blocks which may be used in finite difference or finite volume solvers. The S2dBlock class is described in detail in Reference 12. The STRUCTURED BLOCK record contains data which define the S2dBlock.

3. A nested GRID record causes a new Grid to be created and added as a block to the current grid.

The FIRST NODE record is used to specify which node in the grid is used for the first node in a block: node is the number of the node to be used as the first node in the block with name block_name. If no first node is specified for a given block, then the first unused node in the grid will be used. For example, consider a GRID record which specifies that a grid has three blocks each containing 30 points, but which has no FIRST NODE record. The first block will then use the grid points 0 through 29, the second will use the grid points 30 through 59, and the third the points 60 through 89.

An extractor is overloaded for the Grid and OFFSRF_ifstream classes. If g is a Grid and in_stream is an OFFSRF_ifstream, then the code

```cpp
in_stream >> g;
```

will read the records NAME, COORDINATES, FE BLOCK, STRUCTURED BLOCK, FIRST NODE, and GRID and use them to update g.

The classes Grid, FEBlock, and S2dBlock are all able to read coordinate values from a COORDINATES record. This means that one may choose where to define the coordinate values in the input file. They can all be specified in the GRID record, as shown above. Alternatively, the points for each block may be specified within the records defining the blocks as in the following example.

```plaintext
{GRID: 2 90
 {STRUCTURED BLOCK: 2 5 10
 {NAME: Block #1 }
 {COORDINATES
  x0   y0
  :    :
  x49  y49
 }COORDINATES
 }STRUCTURED BLOCK
 {STRUCTURED BLOCK: 2 8 5
 {NAME: Block #2 }
```

9
If coordinate values are specified in both the grid and its blocks, the values read last (i.e. those appearing last in the file) will override the values read in earlier.

3 Flow Representation

In TRANSOM, the flow is approximated by specifying flow parameters (velocity, pressure, turbulence model variables, etc.) at each point of the grid. A hierarchy of classes is defined which allows variables of different types to be associated with nodes. A diagram of the main classes in the hierarchy is shown in Figure 3.

![Class hierarchy diagram](image)

**Figure 3:** Class hierarchy for classes describing flow variables

3.1 The NodeVar class

The NodeVar class is a template used to create collections of variables each having a value at every node of a collection of points. Every instance of a NodeVar is associated with a NodeOrg; the dimensions of the NodeVar are derived from the NodeOrg and iterators returned by the NodeOrg may be used to navigate through the elements of the NodeVar.

The prototypes for the constructors of a NodeVar which stores objects of class `T` are:

```cpp
NodeVar(const NodeOrg &norg, T *v = 0);
```

Creates a `NodeVar` which stores an object of class `T` at every node.
governed by `norg`. If `v` is null, the default, new memory will be allocated from the heap to store the values; this memory is freed by the `NodeVar` destructor. Otherwise the values will be stored in the memory beginning at `v`; in this case the memory is not freed by the destructor. The memory required is `sizeof(T)*N` bytes, where `N` is the maximal number of nodes of the node organizer.

```
NodeVar(const NodeVar &nv):
    A copy constructor; new memory is allocated to store the objects and their values are obtained by copying the objects in `nv`.
```

The first constructor allows values of a `NodeVar` to be shared with an existing `NodeVar`. Shared values make sub-arrays possible so that, for example, a `NodeVar` containing the coordinates for a block could share these coordinates with a `NodeVar` containing the coordinates for a whole grid.

The following member functions are defined for the `NodeVar` class.

```
unsigned num_nodes() const;
    Returns the number of nodes governed by the `NodeVar` node organizer.

T& operator[][(Node);
const T& operator[][(Node) const;
    The square bracket operator with `Node` arguments allows access to the stored values. Thus if `x` is a `NodeVar<int>`, then `x[n]` is the integer associated with node `n`.
```

### 3.2 The `NumNodeVar` Class

The class `NumNodeVar` is a specialization of the class `NodeVar<double>`; it associates a single floating point value with every node governed by a node organizer. Its constructors are the same as the constructors for `NodeVar<double>`. The `NodeVar` member functions described in Section 3.1 are also inherited by the `NumNodeVar` class.

The floating point values may be obtained using the square bracket operator with a `Node` argument. Thus, the following code creates a `NumNodeVar` containing 100 nodes, then assigns the value 1.5 at every node. Recall that the `NodeIter` `n` will automatically be converted to a `Node` when used as an argument to `operator[][(Node)`.

```
NodeOrg norg(100);
NumNodeVar nv(norg);
AllNodeIter *n = norg.get_all_node_iter();
while (n->in_range())
{
    nv[n] = 1.5;
    n.next();
}
delete n;
```

The class `NumNodeVar` has been given several arithmetic operators to facilitate computations which are applied to floating point values at every
node. The following member operators have been defined.

```cpp
NumNodeVar& operator=(const NumNodeVar &v);
    Copies the values in v.
NumNodeVar& operator-();
    Negates all values.
NumNodeVar& operator+=(const NumNodeVar &v);
    Increments the values by the values in v.
NumNodeVar& operator-=(const NumNodeVar &v);
    Decrements the values by the values in v.
NumNodeVar& operator*=(double d);
    Multiplies all values by d.
NumNodeVar& operator/=(double d);
    Divides all values by d.
NumNodeVar& zero();
    Sets all values to zero.
```

The following operators and functions are also defined.

```cpp
int operator==(const NumNodeVar &vc1, const NumNodeVar &vc2);
    Returns true if vc1 and vc2 are governed by the same node organizer
    and, for every node, the value in vc1 is the same as the value in vc2.
int operator!=(const NumNodeVar &vc1, const NumNodeVar &vc2);
    Returns 1 if vc1 == vc2.

double abs(const NumNodeVar &vc);
    Returns the square root of the sum of the squares of the values at all
    nodes.

double min(const NumNodeVar &vc);
    Returns the minimum value stored at all nodes of vc.

double max(const NumNodeVar &vc);
    Returns the maximum value stored at all nodes of vc.

double min_abs(const NumNodeVar &vc);
    Returns the value stored in vc whose absolute value is smallest.
double max_abs(const NumNodeVar &vc);
    Returns the value stored in vc whose absolute value is largest.
```

### 3.3 The MultiNumVar Class

The class `MultiNumVar` is similar to the `NumNodeVar` class: it associates several floating point values with every node. The `MultiNumVar` class has three constructors with the following prototypes.

```cpp
MultiNumVar(unsigned nd, const NodeOrg &norg, double *d = 0);
    Constructs a MultiNumVar governed by the NodeOrg norg. At each
    node, nd doubles are stored. The doubles are stored starting at
    memory location d. If d is null, new memory will be allocated for the
    stored values.
```
MultiNumVar(const NodeOrg &norg, const MultiNumVar &iv, const Node &n);
    Shared Copy constructor: constructs an MultiNumVar governed by norg and with the same number of doubles as iv. The values in iv starting at node n are shared.

MultiNumVar(const MultiNumVar &iv);
    A copy constructor: new memory is allocated for the stored values.

The following member functions are also defined.

unsigned num_nodes() const;
    Returns the number of nodes at which the values are stored.

unsigned dim() const;
    Returns the number of values stored at each node.

Given a Node argument, the square bracket operator returns a pointer to the doubles associated with the node. Thus, the following code creates a MultiNumVar with 100 nodes and associates 10 doubles with each node. At each node the values of the doubles are set to 1.0 to 10.0.

NodeOrg norg(100);
MultiNumVar nv(10,&norg);
AllNodeIter *n = norg.get_all_node_iter();
while (n->in_range())
{
    for (unsigned i = 0; i < nv.dim(); i++)
        nv[n][i] = i + 1;
    n.next();
}
delte n;

The MultiNumVar class has the same arithmetic operators as the class NumNodeVar, but they operate on all the doubles stored at each node.

3.4 The IOVar Class

The IOVar class is a specialization of the MultiNumVar class which is used to represent global variables in TRANSOM. It provides a means of organizing the floating point values at each node so that they can be associated more easily with independent variables. A subset of the floating point values can be identified and the arithmetic operators restricted so that they act upon that subset only. Input and output functions are also defined so that the values can be read from or written into an OFFSRF file.

The organization of the floating point values is specified using successive calls to the IOVar member function add_to_structure whose full prototype is

void add_to_structure(const Str &s, unsigned n, unsigned off);

A call to add_to_structure assigns the name s to the n floating point values beginning at the offset off. For example, suppose the IOVar pv is intended to store the values of pressure and velocity in a two-dimensional flow. Three floating point values are required at each node and it is decided that the first should be pressure followed by the two velocity components. The IOVar can
be set up in this manner using the following code.

```c
IOVar pv[3,norg]; // norg is a pointer to a NodeOrg
pv.add_to_structure("Pressure", 1, 0);
pv.add_to_structure("Velocity", 2, 1);
```

The value of the pressure at node n may then be obtained by `pv[n][0]` and the two velocity components by `pv[n][1]` and `pv[n][2]`.

The member functions `clear_active` and `activate_only` may also be used to change the organization of the variables. Their full prototypes are

```c
void clear_active();
void activate_only(const Array<Str> &fields);
```

The former removes all organization of the variables; a new organization may be defined using successive calls to `add_to_structure`.

The member function `activate_only` is used to restrict the organization of an `IOVar` to certain variables. The argument `fields` is a list of names of the variables which are to remain active. If a variable name is not in the list, it will no longer be active. If `fields` contains a name which is not already part of the `IOVar` organization, a fatal error will result.

The values for any of the named variables may be read from an OFFSRF file using an extractor overloaded for the `IOVar` and `OFFSRF_ifstream` classes (see Reference 16 for a description of OFFSRF files and the class `OFFSRF_ifstream`). If `pv` is the `IOVar` defined above and `in_stream` is an `OFFSRF_ifstream`, then the code

```c
in_stream >> pv;
```

will read the values for the pressure and velocity at each node from the OFFSRF file associated with `in_stream`. The OFFSRF records should be named "Pressure" and "Velocity", the same names used when defining the structure of the floating point values with the calls to `add_to_structure`.

```c
{Pressure
  p_1  p_2  …  p_n
)Pressure
{Velocity
  v_{x0}  v_{y0}
  v_{x1}  v_{y1}
  …
  v_{xn}  v_{yn}
)Velocity
```

If one of the records is missing, the values for that variable will remain undefined.

Similarly, an inserter is overloaded for the `IOVar` and `OFFSRF_ofstream` classes. If `pv` is the `IOVar` defined above and `out_stream` is an `OFFSRF_ofstream`, then the code

```c
out_stream << pv;
```

will write "Pressure" and "Velocity" records in the OFFSRF file associated with `in_stream`.

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The IOVar constructors are similar to those of the MultiNumVar class. Their prototypes are:

```cpp
IOVar(unsigned nd, const NodeOrg &norg, double *d = 0);
IOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
IOVar(const IOVar &iv);
```

An important function of the IOVar class is to restrict a set of global variables to a subset of independent variables used by a solver. For example, consider a solver, S, which solves the laminar Navier Stokes equations on a single block. The solver is split into two sub-solvers, S1 and S2, which are solved in sequence: S1 first determines the values of the pressure and velocity, then S2 determines the streamfunction. A member of the main solver is an IOVar, vars, which contains the fields "Pressure", "Velocity", and "Streamfunction"; it is passed to both S1 and S2. Within S1 the streamfunction is not used. Therefore, a new IOVar, pv, is constructed from vars; it shares the values in vars but restricts the active fields to "Pressure" and "Velocity". This is done as follows (a simpler method using the specialized class PVIOVar is described in Section 3.5.2).

```cpp
IOVar pv(*vars->get_node_org().vars,0);
Array<Str> fields(2);
fields[0] = "Pressure";
fields[1] = "Velocity";
pv.activate_only(fields);
```

Similarly, in S2, an IOVar restricted only to the "Streamfunction" field is used. Notice that, since the values of the restricted IOVar are shared with vars, the main solver, S, has access to all the variables and can be used to handle all the input and output in a consistent way.

### 3.5 Flow Representation Classes

The classes PVIOVar, VellIOVar, SfncIOVar, TurbiOVar, and KEIOVar are specializations of the IOVar class designed specifically for representing flow variables.

#### 3.5.1 The VellIOVar Class

A VellIOVar is an IOVar containing a single active field named "Velocity". It has three constructors which correspond closely with the IOVar constructors.

```cpp
VellIOVar(unsigned nd, const NodeOrg &norg, double *d = 0);
  Creates a VellIOVar for velocity variables of dimension nd. If d is non-
  null, the velocity values will be stored starting at memory location d;
  otherwise new memory will be allocated (and destroyed when the
  VellIOVar is destroyed).
VellIOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
  Creates a VellIOVar which shares the velocity values with the IOVar iv
  starting at node n. If iv does not contain a field named "Velocity"
  whose length is nd, a fatal error will result.
```
VellOVar(const VellOVar &iv);
A copy constructor; new memory is allocated for the velocity values
and all values are copied to the newly constructed VellOVar.

The member function vel allows easy access to the velocity values; given a
Node argument, it returns a pointer to the velocity values at that node. Thus,
if v is a VellOVar, then v.vel(n)[0] is the x-component of the velocity at node n.

3.5.2 The PVIOVar Class
A PVIOVar is an IOVar containing two active fields named "Pressure" and
"Velocity". It has the following three constructors.

PVIOVar(unsigned nv, const NodeOrg &norg, double *d = 0);
Creates a PVIOVar with velocity variables of dimension nd. If d is non-
null, the pressure and velocity values will be stored starting at
memory location d; otherwise new memory will be allocated (and
destroyed when the PVIOVar is destroyed).

PVIOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
Creates a PVIOVar which shares its values with the IOVar iv starting at
node n. If iv does not contain a field named "Pressure" and a field
named "Velocity" whose length is nd, a fatal error will result.

PVIOVar(const PVIOVar &iv);
A copy constructor; new memory is allocated for the velocity values
and all values are copied to the newly constructed PVIOVar.

The member functions p and vel allow easy access to the velocity values.
The latter is the same as the vel function of the VellOVar class. Given a Node
argument, the member function p returns the pressure value at that node.
Thus, if pv is a PVIOVar, then pv.p(n) is the pressure at node n.

3.5.3 The SfncIOVar Class
A SfncIOVar is an IOVar containing a single active field named
"Streamfunction". It has the following three constructors.

SfncIOVar(const NodeOrg &norg, double *d = 0);
Creates a SfncIOVar which stores only the value of the streamfunction
at each node. If d is non-null, the streamfunction values will be
stored starting at memory location d; otherwise new memory will be
allocated (and destroyed when the SfncIOVar is destroyed).

SfncIOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
Creates a SfncIOVar which shares its values with the IOVar iv starting at
node n. If iv does not contain a field named "Streamfunction", a fatal
error will result.

SfncIOVar(const SfncIOVar &iv);
A copy constructor; new memory is allocated for the velocity values
and all values are copied to the newly constructed SfncIOVar.

The member function sfnc allows easy access to the streamfunction val-
ues; given a Node argument, it returns the value of the streamfunction at that node. Thus, if s is a SfnclOVar, then s.sfcn(n) is the streamfunction at node n.

### 3.5.4 The TurbIOVar Class

A TurbIOVar is an IOVar containing a single active field named "Turbulent Viscosity". It has three constructors which are similar in function to those of the SfnclOVar class.

```cpp
TurbIOVar(const NodeOrg &norg, double *d = 0);
TurbIOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
TurbIOVar(const TurbIOVar &iv);
```

The member function visc allows easy access to the values of turbulent viscosity.

### 3.4.5 The KEIOVar Class

A KEIOVar is an IOVar containing two active fields named "k" and "Epsilon"; it stores value of k and ε used by the k-ε turbulence model and its many variants. It has three constructors which are similar in function to those of the SfnclOVar class.

```cpp
KEIOVar(const NodeOrg &norg, double *d = 0);
KEIOVar(const NodeOrg &norg, const IOVar &iv, const Node &n);
KEIOVar(const PVIIOVar &iv);
```

The member functions k and eps allows easy access to the values of k and ε respectively.

### 4 Solvers

A solver is an abstraction of iterative methods used to determine a solution to some problem. Let x be the state vector for the problem. The solution is found by postulating an initial state, x₀, then determining successive values of the state by applying a function, F, which will be called the sweep.

\[ x_{n+1} = F(x_n) \]

The iteration must be stopped at some point. For this purpose a stopping test is defined (we avoid the term convergence criterion because, in many cases, it will be desirable to stop the iteration before convergence is attained); it is a Boolean-valued function of the state vector, C(x). The solver algorithm is then:

\[ S(x) = \{ x \leftarrow x_0 \]
\[ \text{while not } C(x) : \{ x \leftarrow F(x) \} \]  \hspace{1cm} (1)  \]

Sometimes it will be useful to define new sweeps using existing sweeps as building blocks: for example, the sweep for a multigrid solver is defined as a sequence of sweeps on each of the grids. Since this implies that a sweep
might be used in more than one solver, it is best to define the solver and the sweep as separate classes. Similarly, it may be useful to define different stopping tests for a solver; moreover, the stopping test for a sweep may be different depending upon its use within different solvers. Hence, the stopping test should not be implemented as a member function of either the solver class or the sweep class; it is implemented as a separate class.

Since, in general, both the sweep and the stopping test will need to use the state vector, it must be defined separately and shared.

4.1 The Sweep class

The Sweep class is defined to have three member functions:

\begin{verbatim}
virtual void initialize():
    Initializes the state vector to \( x_0 \) and performs any other initialization
    necessary for the efficient execution of the iteration function \( F(x) \).

virtual void sweep():
    Implements the iteration function \( F(x) \) by altering the state vector
    from the value \( x_n \) to \( x_{n+1} \).

virtual void finalize():
    Performs any tasks necessary after the iteration has been stopped: for
    example, freeing of memory allocated by initialize(). Often finalize() does
    nothing.
\end{verbatim}

The Sweep class is derived from the class OFFSRF described in Reference 16. Hence, every specialization of Sweep has an inserter and extractor defined for the OFFSRF streams OFFSRFofstream and OFFSRFifstream. The inserter and extractor for the class Sweep itself do nothing.

The most important specializations of the Sweep class are shown in the class hierarchy of Figure 4. The ResidualSweep class is described in Section 4.6. Its specializations, SPC2dPVSSweep and SPC2dKESweep, along with SPC2dBLSweep are used to implement a two-dimensional pseudo-compressibility solution of the Navier-Stokes equations on a structured grid. An SPC2dPVSSweep calculates pressure and velocity in the flow, an SPC2dKESweep calculates the turbulence variables using the k-\( \varepsilon \) turbulence model, and SPC2dBLSweep calculates the turbulent viscosity using the Baldwin-Lomax turbulence model. The class SPCMtxSweep solves the linear system which arises in the pseudo-compressibility sweeps; a line relaxation method is used. These classes are described in detail in Reference 12. The SeqSweep and ConcSweep classes are described in Section 4.4. The FESweep class is a generic finite element sweep; it assembles a linear system of equations and solves it. Its specialization FE2dNSSweep is used to solve the two-dimensional Navier-Stokes equations. The FESfncSweep calculates the streamfunction for an incompressible velocity field. The classes FESweep, FE2dNSSweep and FESfncSweep are all described in Reference 13.
4.2 The StopTest class

The StopTest class has two member functions:

virtual void initialize();
Perform any initialization necessary for the proper functioning of
the stop test.

virtual int stop();
Returns true if the sweeps should be stopped; false if they should
continue. Thus, stop() implements the function \( C(x) \). Note that, as
described above, the state vector \( x \) is shared data of both the StopTest
class and the Sweep class; hence, it is not provided as an argument to
stop(). Of course, this also circumvents the problem that the type of
data is not yet specified so that, for a strongly typed language like C++,
the type of the argument would not be known.

There are several simple but important specializations of stop tests. The
TrueStopTest always returns true; the FalseStopTest always returns false. The
OrStopTest combines two stop tests, \( C_1 \) and \( C_2 \), to obtain \( C = C_1 \lor C_2 \). An
AndStopTest is similar but is defined by \( C = C_1 \land C_2 \).

Figure 5 shows the hierarchy of classes derived from StopTest. A
ReportStopTest is a stop test which reports on its state whenever is stop() function is executed; it is described in Section 4.2.1. An NTimesStopTest allows
the sweep to be performed \( n \) times; it is described in Section 4.2.2. A
CompDataStopTest returns true when successive values of the state vector
have changed by less than some pre-defined small amount; it is described in
Section 4.2.3. A ResidualStopTest is a stop test suitable for a residual solver; it is
described in Section 4.6.1. The SeqStopTest and ConcStopTest classes represent
stop tests suitable for solvers which use more than one sweep; they are
described in Sections 4.4.1 to 4.4.3.
4.2.1 The ReportStopTest Class

A ReportStopTest is a StopTest with the ability to report on its state whenever the stop function is called. The virtual function report is used to write the report. A character string may be prepended to the report; normally this is used to identify the solver to which the stop test applies.

Each ReportStopTest can be set so that the report is written before the stop test is executed, after the stop test is executed, or not at all. The member function set_report() is used for this purpose. Its argument should be one of the following:

- ReportStopTest::before
  Write the report before the stop test is executed.

- ReportStopTest::after
  Write the report after the stop test is executed, but only if the stop test returned true.

- ReportStopTest::after_always
  Write the report after the stop test is executed, irrespective of the result of the stop test.

- ReportStopTest::none
  Do not write the report.

For example, if rst is a ReportStopTest, then

```cpp
rst.set_report(ReportStopTest::before);
```

sets the stop test so that the report will be written before the stop test is executed. By default, a ReportStopTest is set so that no report is written.
The ReportStopTest class does not define the \initialize\ virtual function inherited from StopTest. It must be defined by specializations of the class.

The constructors and member functions are:

\begin{verbatim}
ReportStopTest();
    Creates a new ReportStopTest. By default no report will be written.

void report(ostream&);
    Writes a report on the state of the stop test to the output stream.

virtual void report_no_prepend(ostream& r) = 0;
    Writes the report with no prepended string. This function must be
    defined by specializations of the class.

virtual int stop();
    Calls the function stop_no_report() to execute the stop test. The report
    is written before or after this call as specified by the most recent call to
    set_report().

virtual int stop_no_report() = 0;
    Executes the stop test with no reporting. This function must be
    defined by specializations of the class.

void set_report_string(const Str &s)
    Sets the character string which is prepended to the report.
\end{verbatim}

4.2.2 The NTimesStopTest class

An NTimesStopTest allows the sweep to be performed \( n \) times; its \( \text{stop()} \) function returns true the \((n+1)^{st}\) time it is called. It is a specialization of the ReportStopTest class. Its constructor has the following prototype:

\begin{verbatim}
NTimesStopTest(unsigned m);
\end{verbatim}

where \( m \) is the number of times the sweep is to be executed before the stop test returns true. The \initialize\ function resets the iteration count so that the stop test will be executed \( m \) more times. The number of times to execute the iteration may be changed using the following member function.

\begin{verbatim}
void set_number(unsigned m);
\end{verbatim}

The NTimesStopTest inherits the member functions \text{set_report()}, \text{report()} and \text{set_report_string()}, from ReportStopTest. The report from the NTimesStopTest simply prints the current iteration count followed by an end-of-line character. Thus, the code

\begin{verbatim}
NTimesStopTest nst(3);
nst.set_report(ReportStopTest::before);
nst.set_report_string("Iteration ");
while (nst.stop());
\end{verbatim}

will cause the following to be written to cout:

\begin{verbatim}
Iteration 0
Iteration 1
Iteration 2
\end{verbatim}
If ReportStopTest::after_always had been used, then the result would have been

Iteration 1
Iteration 2
Iteration 3

since in this case the iteration count is incremented prior to the report.

4.2.3 The CompDataStopTest class

Another important type of stop test checks convergence by comparing successive values of the state vector; if it has not changed much, then the solver has converged. The CompDataStopTest is used to implement this condition. In a CompDataStopTest the state vector is represented by an IOVar. When the CompDataStopTest is constructed, a copy of the state vector is made; it is used to store the state vector from the previous iteration. The stop test always returns false the first time it is called after initialization. Otherwise it compares the current state vector with the state vector from the previous iteration and returns true if one of two conditions is satisfied.

1. The absolute value of the largest difference in the state vectors is less than the small pre-defined value \( \varepsilon_{\text{acc}} \). This condition stops the solver when the solution has converged.

2. The absolute value of the largest difference in the state vectors is greater than the large pre-defined value \( \varepsilon_{\text{div}} \). This condition stops the solver when the solution has diverged.

The CompDataStopTest constructors and member functions are:

\[ \text{CompDataStopTest(IOVar} \,*d, \text{ double } a, \text{ double } maxa) ; \]

\[ \text{Makes a CompDataStopTest with state vector obtained from } d, \text{ with } \varepsilon_{\text{acc}} \text{ set to } a, \text{ and with } \varepsilon_{\text{div}} \text{ set to } maxa. \]

\[ \text{virtual void initialize();} \]

\[ \text{Initializes the stop test. The next call to stop()} \text{ will return false.} \]

\[ \text{virtual int stop();} \]

\[ \text{Executes the stop test.} \]

\[ \text{void set_max_residual(double maxa);} \]

\[ \text{Sets the value of } \varepsilon_{\text{div}} \text{ to } maxa. \]

\[ \text{void set_acc(double } a); \]

\[ \text{Sets the value of } \varepsilon_{\text{acc}} \text{ to } a. \]

The CompDataStopTest class is a specialization of the ReportStopTest class. The member functions set_report(), report(), and set_report_string() are inherited from ReportStopTest. The report from the CompDataStopTest prints the maximum difference found for each of the active variables in the IOVar \( d \). The default string prepended to the report is “Max.Acc. = “, but it can be changed using set_report_string(). Thus, if cdst is a CompDataStopTest constructed using a PVIOVar (three active variables: pressure and two velocity components), then the report is similar to the following.
Max.Acc. = 0.123456 -0.0256543 0.0365476

The first number is the maximum difference in the pressure values, and the latter two numbers are the maximum differences in each of the velocity components.

4.3 The Solver class

The Solver class is an implementation of the abstract solver defined above. It has a shared Sweep, sw, and a shared StopTest, st, as data and the following member functions.

- `virtual void initialize();` 
  Initializes the sweep sw and the stop test st.

- `virtual void solve();` 
  Implements the solution algorithm of equation (1).

- `virtual void finalize();` 
  Finalizes the sweep sw and the stop test st.

The Solver class has two constructors.

- `Solver(Sweep *s, StopTest *t);` 
  Makes a Solver with sweep sw and stopping test st.

- `Solver(const Solver&);` 
  Copy constructor.

The Solver class is derived from the class OFFSRF described in Reference 16. Hence, every specialization of Solver has an inserter and extractor defined for the OFFSRF streams OFFSRF_ofstream and OFFSRF_ifstream. The Solver inserter simply calls the inserter for its sweep. Similarly, its extractor calls the extractor for its sweep.

The most important specializations of the Solver class are shown in the class hierarchy of Figure 6. The ResidualSolver class is described in Section 4.6. The ConnectedSolver class is described in Section 4.4.3.2. The FE2dNSSolver class solves the laminar two-dimensional Navier-Stokes equations using the finite element method; it is described in Reference 13. The SeqSolver and ConcSolver classes are used to combine several different solvers so that they may be executed as a single solver; they are described in Section 4.4. The SeqFlowSolver and ConcFlowSolver classes are specializations of SeqSolver and ConcSolver which are specifically designed for use by flow solvers; they are described in Section 4.5. An SPC2dSolver solves the two-dimensional Navier-Stokes equations using a pseudo-compressibility method; it is described in Reference 12. Finally, an SPC2dTurbSolver solves the two-dimensional turbulent transport equations on a structured grid; it is used in conjunction with the SPC2dSolver; it is described in Reference 12.
4.4 Multiple Sweep Solvers

An important specialization of a solver is one which consists of a collection of sub-solvers each applied to a subset of the state vector. For $n=1,\ldots,N$, let $S_n(x_n)$ be the collection of sub-solvers each with its sweep, $F_n$, and stop test $C_n$. Each of these solvers can be run independently to achieve a solution over its sub-state-vector, $x_n$. However, in general, the sub-state-vectors will not be disjoint so that, when the solvers are run sequentially, they interact, the solution algorithm of one solver affecting the solution of another.

Moreover, the sub-state-vectors may be implemented in such a way that a single parameter has copies in more than one sub-state-vector. In this case whenever the parameter is changed in one sub-state-vector, its value must also be altered in all the others in which it appears. Often, but not always, such redundancy will be avoided by sharing state variables among the solvers.

It is probably clear that, in presenting the multiple sweep solver, we have in mind a multi-block Navier-Stokes solver. On each block a solution method is defined. Boundaries may be shared by two blocks and each of the block solvers may store copies of the independent variables on the boundaries.

There are two main types of multiple sweep solvers; they are described in the following two sections.

4.4.1 Concurrent Solvers

A concurrent solver is a multiple sweep solver which finds a solution to all the sub-solvers concurrently. Each of the sweeps is executed in turn.
(perhaps more than once), the cycle of sweeps continuing until the stop tests of all sub-solvers return true. More precisely:

1. The stop test for the solver is the union of all the sub-stop-tests: i.e. the stop test returns true when all of the sub-stop-tests return true.
   \[ C(x_1, \ldots, x_N) = C_1(x_1) \lor \ldots \lor C_N(x_N) \]

2. The solver is initialized by initializing all sub-sweeps and sub-stop-tests.
   \[
   \text{for } n = 1 \text{ to } N \{ \text{initialize } C_n(x_n) \text{ and } F_n(x_n) \} 
   \]

3. The algorithm for the sweep for the concurrent solver is:
   \[
   \text{for } n = 1 \text{ to } N \\
   \{ \text{initialize } C'_n(x_n) \\
   \text{while } C'_n(x_n) : x_n \leftarrow F_n(x_n) \\
   \text{for } m = 1 \text{ to } N \& m \neq n : \\
   \{ \text{if } (x_n \text{ and } x_m \text{ are redundant) } T_{nm}(S_n(x_n), S_m(x_m)) \} \\
   \}
   \]

   where the \( C'_n \) are a new stop tests and \( T_{nm} \) is a function which maintains the consistency of the sub-state-vectors \( x_n \) and \( x_m \) by changing the values of \( x_m \) according to the values of \( x_n \).

4. The solver is finalized by finalizing all sub-sweeps.
   \[
   \text{for } n = 1 \text{ to } N \{ \text{finalize } F_n(x_n) \} 
   \]

Notice that the arguments of \( T_{nm} \) are not the state vectors \( x_n \) and \( x_m \), but the solvers \( S_n(x_n) \) and \( S_m(x_m) \). This is because the algorithm to update the state vectors will usually depend on the types of solvers used and not only on the data itself.

The sweep algorithm can be made more efficient if it is assumed that the redundancy of all pairs \((x_n, x_m)\) is known \textit{a priori}. In that case the loop over \( m \) can be restricted to the sub-state-vectors which are known to be redundant with \( x_n \). In many cases there will be no redundant state vector pairs.

### 4.4.2 Sequential Solvers

A sequential solver consists of a sequence of solvers; when the stop test of one solver is satisfied, the next solver in the sequence is started. As with concurrent solvers, the sub-solvers may share portions of the state vector; hence, after each sub-solver has been solved, update functions \( T_{nm} \) must be called to preserve the consistency of the state vectors.

A solver which finds a solution to all the sub-solvers in sequence may be defined as follows. For \( n = 1, \ldots, N \), let \( S_n(x_n) \) be the collection of sub-solvers each with its sweep, \( F_n \), and stop test \( C_n \). At any time only one of the solvers,
the $n^{th}$, is active.

1. The stop test tests the stop test of the current solver. If it is true, the current solver is finalized, its connections updated, then the next solver in the sequence is activated and initialized. The stop test returns true when the stop test of the last solver in the sequence returns true.

   \[
   C(x_1, \ldots, x_N) =
   \begin{cases}
   \text{while } C_n(x_n) \& n < N \\
   \text{initialize } S_{n+1}(x_{n+1}) \\
   \text{for } m = 1 \text{ to } N \& m \neq n : \\
   \text{if } (x_n \text{ and } x_m \text{ are redundant}) \ T_{nm}(S_n(x_n), S_m(x_m)) \}
   \end{cases}
   \]

   \[\text{finalize } S_n(x_n)
   \]

   \[n \leftarrow n + 1
   \]

   return \( C_n(x_n) \)

2. The solver is initialized by resetting \( n \) to 1 and initializing \( S_i(x_i) \).
3. The sweep simply executes the sweep of the current solver:

   \[F(x_1, \ldots, x_N) = F_n(x_n)\]

4. The solver finalize function does nothing, since all the sub-solvers are finalized during the execution of the stop test.

4.4.3 Implementation of Multiple Sweep Solvers

In TRANSOM, both concurrent and sequential solvers are implemented with the help of several special classes.

4.4.3.1 The SweepConnection Class

The SweepConnection class represents the connection function \( T(S_1, S_2) \) between two solvers having redundant state vectors. It has two member functions:

   virtual void initialize():
   
   Performs initializations required for the efficient execution of \( T(S_1, S_2) \)

   virtual void update():
   
   Implement the function \( T(S_1, S_2) \). The solver arguments \( S_1 \) and \( S_2 \) will normally be specified as arguments to the constructor when an instance of SweepConnection is created.

4.4.3.2 The ConnectedSolver Class

To implement the sweep algorithms of the multiple sweep solvers the class ConnectedSolver is defined. A ConnectedSolver, \( S \), consists of a solver and a list of connection functions, \( T(S, S_i) \).
It is important that it be possible to promote any Solver to a ConnectedSolver; hence it should have a constructor with the following prototype.

ConnectedSolver(Solver &s);

When this constructor is used, the ConnectedSolver should behave exactly as did the original solver, s, except that the ability to add and to execute connection functions is provided. A natural way to implement this constructor would be to copy the sweep and stop test from s; however, in that case, any overloaded member functions of s would be lost. Instead the ConnectedSolver class stores a pointer, slv, to the original solver; the Solver member functions are then overloaded so that they execute the corresponding member function of slv.

Notice that in this implementation a ConnectedSolver stores two sweeps, Solver::sw and slv->sw, and two stop tests, Solver::st and slv->st. The duplication of sweeps has no utility; Solver::sw is always ignored. However, the second stop test can be used to store the stop test, C_n', required by the concurrent solver. Accordingly, constructors are supplied to allow Solver::st and slv->st to be defined independently.

When a connection between two solvers is defined in an input file, there must be some means of identifying the solvers which are to be connected. To make this easier, a connected solver also has a name. ConnectedSolver overloads the Solver extractor so that it may read the name from a NAME record having the following format.

{NAME: name }

where name is any character string. When comparing the name with other names, leading and trailing whitespace is ignored but the comparison is case sensitive. Other input records are read by calling slv->read_record (see Reference 16).

Following are prototypes for the ConnectedSolver constructors and member functions.

ConnectedSolver(Solver &s);
    Creates a ConnectedSolver from the solver s. The pointer slv is set to &s. The list of connection functions is empty; they must be added using the member function insert.

ConnectedSolver(const ConnectedSolver &cs, StopTest *t = 0);
    Copies cs including its list of connection functions. If t is non-null, the stop test pointer Solver::st will be set to t; otherwise it will be set to slv->st.

void insert(SweepConnection *sc);
    Adds a connection function to the list

void initialize();
    Initializes the ConnectedSolver prior to its solution. Initializes the solver slv, the stop test Solver::st, and all of the connection functions.
virtual void finalize();
    Finalizes the ConnectedSolver after its solution; equivalent to
    slv->finalize().

virtual void update_connections();
    Calls update() for every connection function in the list.

Solver* get_solver() const;
    Returns slv.

StopTest* get_original_stop_test() const;
    Returns a pointer to the stop test used by slv; i.e. returns slv->st.

const std::string get_name() const;
    Returns the solver name.

4.4.3.3 The ConcSolver Class

Concurrent solvers are represented by the class ConcSolver; the sub-solvers
are represented by a list of ConnectedSolvers. For each sub-solver, S_s, the stop
test C_s is represented by the stop test slv->st in the ConnectedSolver; the stop test
C^* is represented by Solver::st. The stop test for the ConcSolver is a
ConcStopTest; its stop() function implements algorithm described in
Section 4.4.1.

The ConcSolver class has the following constructors and member
functions.

ConcSolver():
    Creates a new ConcSolver with an empty list of sub-solvers. Sub-
solvers must be added using one of the insert functions defined below.
    During the sweep, the sub-solvers will be executed in the order in
which they are added to the list.

void insert(ConnectedSolver* s, StopTest* t = 0);
    Adds a new connected solver to the list of sub-solvers. If t is non-
    null, the stop test cs->st is replaced by t; i.e. when the sweep is
    performed, the stop test C^* will be evaluated using t.

void insert(Solver* s, StopTest* t);
    Add a new solver to the list of sub-solvers by first converting it to a
    ConnectedSolver with an empty list of connection functions. The stop
test C^* is represented by s->st and the stop test C^* by t.

int is_empty() const;
    Returns true if there are no sub-solvers.

virtual void initialize();
    Initializes all the sub-solvers prior to execution of the sweeps.

virtual void sweep();
    Executes the sweeps as described in Section 4.4.1.

virtual void finalize();
    Finalizes all sub-solvers after execution of the sweeps.
4.4.3.4 The SeqSolver Class

Sequential solvers are represented by the class SeqSolver; the sub-solvers are represented by a list of ConnectedSolvers. Since only one stop test is required for each sub-solver, in the ConnectedSolvers the stop tests siv->st and Solver::st are always the same. The stop test for the SeqSolver is a SeqStopTest; its stop() function implements algorithm (3).

The SeqSolver class has the following constructors and member functions.

SeqSolver();
Makes a SeqSolver with an empty list of sub-solvers. The sub-solvers must be added using the insert function.

void insert(ConnectedSolver *s);
Adds a new connected solver to the list of sub-solvers.

void insert(Solver *s);
Adds a new solver to the list of sub-solvers by first converting it to a ConnectedSolver with an empty list of connection functions.

virtual void initialize();
Initializes the first sub-solver prior to execution of the sweeps.

virtual void sweep();
Executes the sweep algorithm described in Section 4.4.2.

virtual void finalize();
Does nothing, since all sub-solvers are finalized during execution of the stop tests.

4.5 Flow Solvers

The FlowSolver class is an abstract base class for solvers used to calculate fluid flow. Its state consists of a Grid, an IOVar used to represent flow variables having values at all nodes, and a single double used to store the Reynolds number. The prototypes for the FlowSolver constructors are:

FlowSolver(Grid *g = 0, double r = -1.0, IOVar *v = 0);
Creates a FlowSolver using the grid g, the flow variables v, and the Reynolds number r. If the grid is null, it must be defined by reading it from an input file using the extractor described below. A negative Reynolds number is used as a flag that the Reynolds number has not been defined.

FlowSolver(const FlowSolver&);
A copy constructor.

The FlowSolver class has two specializations: SeqFlowSolver and ConcFlowSolver. Each adds a list of sub-solvers to the FlowSolver: SeqFlowSolver solves the sub-solvers in sequence, ConcFlowSolver concurrently. This is implemented by deriving the former from the SeqSolver class as well as FlowSolver, the latter from the ConcFlowSolver class as well as FlowSolver. This multiple inheritance hierarchy is illustrated in Figure 7.
Instances of both SeqSolver and ConcFlowSolver can be defined by reading records from an OFFSRF input file. Extractors are overloaded for the SeqFlowSolver and OFFSRF ifstream classes, and for the ConcFlowSolver and OFFSRF ifstream classes. Thus, if s is a SeqFlowSolver or a ConcFlowSolver and in_stream is an OFFSRF ifstream, then the code

    in_stream >> s;

will define s by reading the OFFSRF file associated with the stream in_stream. The extractor reads the following OFFSRF records.

1. A GRID record in the format described in Section 2.5.
2. A GLOBAL VARIABLES record which defines the organization of the independent variables. The format of this record is described below.
3. A REYNOLDS NUMBER record with format
   
   {REYNOLDS NUMBER: number }  

   where number is the value of the Reynolds number.
4. Any number of records describing the sub-solvers. In the current version of TRANSOM the following OFFSRF records are recognized for defining the sub-solvers.

   SPC 2D SOLVER: Creates a solver which uses the pseudo-compressibility method to solve the Navier-Stokes equations on a structured grid. The format of this record is described in Reference 12.

   STRUCTURED STREAMFUNCTION SOLVER: Creates a solver which calculates a streamfunction for a two-dimensional flow field on a structured grid. Typically this solver is used in sequence with an SPC 2D SOLVER.

   FE 2D NS SOLVER: Creates a solver which solves the two-dimensional Navier-Stokes equations using the finite element method. The format of this record is described in Reference 13.

   FE STREAMFUNCTION SOLVER: Creates a solver which uses the finite element method to calculate a streamfunction for a two-dimensional
flow field. Typically this solver is used in sequence with an FE NS SOLVER.

FE LAPLACE SOLVER: Creates a solver which uses the finite element method to solve Laplace's equation.

SEQUENTIAL SOLVER: Creates a new instance of a SeqFlowSolver. This record should have a format similar to that of the TRANSOM input file except that it may not include a GRID record. If independent variables have been inherited from the parent solver, then it also must not contain a GLOBAL VARIABLES record.

CONCURRENT SOLVER: Creates a new instance of a ConcFlowSolver. The format of this record is exactly the same as for the SEQUENTIAL SOLVER record.

The format of the GLOBAL VARIABLES record is as follows:

{GLOBAL VARIABLES
 name-1 length-1
 name-2 length-2
 ... ...
 name-n length-n
}GLOBAL VARIABLES

where name-1 to name-n are the names of the variables and length-1 to length-n are the number of doubles required per node for the corresponding variable. If the variable names contain spaces, they must be enclosed in double quotes. For example, the following record defines three global variables: Pressure, two-dimensional Velocity, and Turbulent Viscosity.

{GLOBAL VARIABLES
 Pressure 1
 Velocity 2
 "Turbulent Viscosity" 1
}GLOBAL VARIABLES

The variables can also be initialized from within the GLOBAL VARIABLES record; simply include a record whose name is the name of the variable, followed by the values of that variable at all the nodes (note that this is the format required by the IOVar extractor as described in Section 3.2). Thus, the following record defines Pressure and two-dimensional Velocity and initializes the values of Pressure.

{GLOBAL VARIABLES
 Pressure 1
 Velocity 2
 {Pressure
 p_1 p_2 \ldots p_n
 }Pressure
}GLOBAL VARIABLES

To implement the extractors, a mechanism must be provided for defining the sequence of sub-solvers by reading OFFSRF records. Moreover, it should be possible for the sub-solvers themselves to be instances of the SeqFlowSolver.
and ConcFlowSolver. To avoid duplication of code between the two solvers, the task of reading the input records is relegated to the base class FlowSolver. The FlowSolver virtual member function insert(ConnectedSolver*) is used to insert the sub-solver into the list of sub-solvers; for the class SeqFlowSolver this function is simply redefined as SeqSolver::insert(ConnectedSolver*), while for the ConcFlowSolver it is redefined as ConcSolver::insert(ConnectedSolver*).

Whenever a sub-solver is created by a FlowSolver, the grid (or perhaps an appropriate block of the grid) and the independent variables of the FlowSolver are passed to the sub-solver via its constructor. All the sub-solvers then share the grid and the variables of their parent. If a sub-solver requires an independent variable which is not defined by the parent (e.g. if the solver requires turbulent viscosity but the parent defines only pressure and velocity), then a local copy of that variable will normally be generated.

4.6 Residual Solvers

Residual solvers are an important abstraction of solvers used to solve systems of equations. Consider the system of equations

\[ f(x) = 0 \]

where \( x \) is a state vector and \( f \) is a vector of functions. In a residual solver, one evaluates \( r = f(x) \) for the current approximation to the state vector \( x \), then determines a correction to \( x \) which will reduce the magnitude of the vector \( r \). The elements of \( r \) are called the residuals of the system of equations. The solution algorithm can be written as follows.

\[
S(x) = \{ \begin{array}{l}
x \leftarrow x_0 \\
\text{repeat} \\
\quad \{ \begin{array}{l}
r \leftarrow f(x) \\
x \leftarrow x + g(x,r) \\
\text{while not } C(r) \\
\end{array} \}
\end{array} \}
\]  

(4)

where \( x_0 \) is the initial state vector, \( g(x,r) \) is the correction to \( x \), and \( C(r) \) is a stop test which returns true when the residuals are sufficiently small. To conform to the solution algorithm (1) in Section 4, the post-tested loop must be converted to a pre-tested loop. This is done simply by requiring that the stop test always return false the first time it is called after initialization. Algorithm (1) may then be used with the sweep function defined by

\[
F(x) = \{ \begin{array}{l}
r \leftarrow f(x) \\
x \leftarrow x + g(x,r) \\
\end{array} \}
\]  

(5)

In TRANSOM, residual solvers are implemented using the three classes
ResidualSolver, ResidualStopTest, and ResidualSweep. In these classes the residuals are represented as a Vec: an array of floating point values for which many arithmetic operators have been defined. The full definition of the Vec class may be found in the source files Mtx.h and Mtx.c. The state vector is represented as an IOVar.

4.6.1 The ResidualStopTest Class

The ResidualStopTest class represents a stop test suitable for use in a residual solver. The stop test always returns false the first time it is called after initialization. Otherwise it returns true if one of two conditions is satisfied.

1. The largest absolute value of all the residuals is less than the small predefined value $\varepsilon_{\text{acc}}$. This condition stops the solver when the solution has converged.

2. The largest absolute value of all the residuals is greater than the large predefined value $\varepsilon_{\text{div}}$. This condition stops the solver when the solution has diverged.

The ResidualStopTest constructors and member functions are:

```cpp
ResidualStopTest(Vec *r, double a, double maxa);
    Makes a ResidualStopTest with residuals obtained from r, with $\varepsilon_{\text{acc}}$ set to a, and with $\varepsilon_{\text{div}}$ set to maxa.
```

```cpp
virtual void initialize();
    Initializes the stop test. The next call to stop() will return false.
```

```cpp
virtual int stop();
    Executes the stop test.
```

```cpp
void set_max_residual(double maxa);
    Sets the value of $\varepsilon_{\text{div}}$ to maxa.
```

```cpp
void set_acc(double a);
    Sets the value of $\varepsilon_{\text{acc}}$ to a.
```

The ResidualStopTest class is a specialization of the ReportStopTest class. The member functions set_report(), report(), and set_report_string() are inherited from ReportStopTest. The report from the ResidualStopTest prints the maximum and the root mean square residual. The default string prepended to the report is "Accuracy = ", but it can be changed using set_report_string(). Thus, if rst is a ResidualStopTest, then the report is similar to the following.

```
Accuracy = -0.123456 0.0256543
```

The first number is the residual with the largest absolute value and the second is the root mean square residual.

4.6.2 The ResidualSweep Class

The ResidualSweep class is used to implement the sweep algorithm (5). Its data includes a Vec to represent the residuals, and an IOVar, data, to represent
the state vector. It has the following constructors and member functions.

ResidualSweep(IOVar *d, unsigned nr = 0);
    Makes a ResidualSweep with state vector d. The length of the residual
    vector is given by nr. If nr is zero, then the length of the residual
    vector is set to the number of doubles in d.

virtual void calc_residual() = 0;
    Calculates the residuals. This is a pure virtual function which must
    be defined by the specializations of the ResidualSweep class.

virtual MultiNumVar& correct() = 0;
    Returns the correction to the state vector g(x,r). This is a pure
    virtual function which must be defined by the specializations of the
    ResidualSweep class.

virtual void sweep();
    Executes the sweep algorithm (5) by calling calc_residual() and then
    incrementing the state vector by the returned value of correct().

An extractor is overloaded for the ResidualSweep and OFFSRF_ifstream
classes. It reads in values of the state vector, data. Thus, if rsw is a
ResidualSweep and in_stream is an OFFSRF_ifstream, then the code

in_stream >> rsw;

will define data by reading the OFFSRF file associated with the stream
in_stream. This code is identical in function to

in_stream >> rsw->data;

The format for the records to define an IOVar is described in Section 3.4.

4.6.3 The ResidualSolver Class

Residual solvers are represented by the ResidualSolver class. The sweep of a
ResidualSolver is a specialization of a ResidualSweep. Its stop test is an OrStopTest
which combines an NTimesStopTest and a ResidualStopTest. Thus, the solver
will stop either when the residuals are sufficiently small (or too large) or
when a fixed number of sweeps have been performed. The ResidualSolver
ensures that its sweep and the ResidualStopTest share the same residuals. The
constructor and member functions of the ResidualSolver class are:

ResidualSolver(ResidualSweep *s, unsigned mxniter = 1000, double acc = 1.0e-04,
        double maxacc = 1.0e+04);
    Makes a ResidualSolver having sweep s. A maximum of mxniter sweeps
    will be performed. The solver stops executing sweeps when the
    maximum residual is smaller than acc or if it is greater than maxacc.

void set_max_residual(double maxacc)
    Sets the value of ε_{div} for the ResidualStopTest to maxacc.

void set_acc(double acc);
    Sets the value of ε_{acc} for the ResidualStopTest to acc.
void set_max_number_sweeps(unsigned mnxiter);
Sets the maximum number of sweeps to mnxiter.

The values of $\varepsilon_{\text{acc}}$ and $\varepsilon_{\text{div}}$ can be defined by reading records from an OFFSRF input file. An extractor is overloaded for the ResidualSolver and OFFSRF_ifstream classes. Thus, if $\text{rslv}$ is a ResidualStopTest and $\text{in\_stream}$ is an OFFSRF_ifstream, then the code

\begin{verbatim}
  in\_stream >> rslv;
\end{verbatim}

will define $\text{s}$ by reading the OFFSRF file associated with the stream $\text{in\_stream}$. The records should have the following format (all records are optional).

\begin{verbatim}
{RESIDUAL ACCURACY: \text{eps\_acc}}
{MAXIMUM RESIDUAL: \text{eps\_div}}
{MAXIMUM NUMBER ITERATIONS: \text{num}}
\end{verbatim}

where $\text{eps\_acc}$ is the value of $\varepsilon_{\text{max}}$, $\text{eps\_div}$ is the value of $\varepsilon_{\text{div}}$ and $\text{num}$ is the maximum number of iterations allowed. Any other records will be passed to the sweep for interpretation.

5 The Main Program

The TRANSOM main program is very simple. It consists of four phases.

1. First a ConcFlowSolver, $\text{ms}$, is created.
2. Then an OFFSRF file is opened (its name is supplied as a command line argument when TRANSOM is executed from the shell) and the ConcFlowSolver extractor is used to define $\text{ms}$ according to the contents of the file. As described in Section 4.5, this will define the grid, any global variables to be shared among sub-solvers, and all the sub-solvers to be executed.
3. Next $\text{ms.solve()}$ is called to generate a solution to the problem.
4. Finally an OFFSRF output file is opened (its name is supplied as a command line argument when TRANSOM is executed from the shell) and the solution is written to it using the ConcFlowSolver inserter.

6 Concluding Remarks

TRANSOM is a complex program which is still in the early stage of development. There is little doubt that some of the structure defined in this memorandum will be changed as that development continues. Nevertheless, in the two flow solvers which have been implemented so far, the current class hierarchies have proved their worth.

At present TRANSOM works well when either the pseudo-compressibility solver or the finite element solver is used on a single block. Experimentation with a single solution method on multiple blocks has also shown that acceptable levels of convergence can be achieved. Some flows have also been solved in which both the pseudo-compressibility method and
the finite element method have been used on neighbouring blocks[17], although convergence is at best slow and at worst not attained. Work in this area will continue over the coming year; it will likely lead to significant changes in the ConnectedSolver and SweepConnection classes currently used to implement the transfer of information between solvers on neighbouring blocks.

Further development will also continue on each of the solvers implemented so far. Details of their shortcomings and the modifications proposed are described in References 12 and 13.
References


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TRANSOM is a multi-block, multi-method Reynolds-Averaged Navier Stokes solver being developed at DREA to address problems associated with the flow around ships and submarines. It is multi-block because the flow is divided into several distinct regions. It is multi-method because a different solution method may be used on each of the flow regions. At present two different methods of solution can be chosen: a finite-volume solver based on the pseudo-compressibility method; and a finite element solver which uses the penalty function method to determine the pressure.

TRANSOM is written in C++ following principles of Object Oriented Programming. This document describes the overall design of TRANSOM with emphasis on the class hierarchies used to represent different types of blocks and flow solvers. The algorithms used to implement the pseudo-compressibility and finite element methods are not discussed here; two companion reports describe these sub-solvers in detail.

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