**Title and Subtitle**

The Interplay Between Geometric and Electronic Structure and the Magnetism of Small Pd Clusters

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**Abstract**

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THE INTERPLAY BETWEEN
GEOMETRIC AND ELECTRONIC
STRUCTURE AND THE MAGNETISM OF
SMALL Pd CLUSTERS

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- ABSTRACT -

The electronic structure and geometric characteristics of small Pd clusters (up to 13 atoms) are studied at the SCF/CI level, with major focus on the mutual dependence between these properties. To this end, Jahn-Teller effects have been considered, and the magnetic moments analyzed on the distorted, most stable, structures.

By means of calculations of the INDO type, the energies and normal modes involved in the different steps of the distortions which leads to diamagnetic Pd_{13} but paramagnetic Pd_{4} are described. Comparisons with other calculations and experimental data are included.
1- INTRODUCTION -

The potential uses of metal clusters in chemistry, physics and technology have lead to impressive effort towards a better understanding of their properties. Because their characterization represents an important link in the understanding of the fundamental mechanisms of catalysis, the basic properties (geometry, bond strength, reactivity) of small metal aggregates have become the subject of intense theoretical [1-13] and experimental study [14-21].

It is well known that the electronic properties and structural characteristics of metal aggregates are different from the bulk [20-22]. The nature of these differing electronic properties is believed to play an important role in the adsorption and reaction of small molecules, and is largely related to geometry [6,16,23,24]. Metal clusters of suitable size are able to reproduce the electronic features of crystal defects and of the small metal particles in supported structures that are responsible for catalytic reactivity. Research on the electronic structure and geometry of small metal clusters may lead to the development of more selective and efficient catalysts, and to model specific reactions through the analysis of the interactions involved in the adsorption of simple molecules.

As the simplest representation of the reactive site, often metal clusters defined by 2 to 100 atoms are studied, with particular emphasis in the change of the properties as a function of the size [3,4,6,10]. However, as has been previously described, not only the size, but also the geometric and electronic structure are important to reproduce surface defects or metal particles in supported catalysts. Besides, the experimental information available on the geometrical structure of metallic clusters of the order of 10 atoms is indirect [15,20,21] and, in most cases, not even the symmetries are known. Any calculation of the physical properties of microclusters has to start, therefore, by the prediction of the geometry by means of the minimization of the total energy. On the other hand, the most symmetrical configurations of small clusters are very often
unstable due to the Jahn-Teller effect [1,4,7,25]. The calculations that only consider highly symmetric geometries often miss the true equilibrium geometry. For a detailed understanding of the structure-reactivity relationships in clusters, and a successful correlation between chemical and physical properties, the most stable structure of the cluster must first be determined. However, because of the unquestionable coupling between electronic and geometric structure, clearly shown by the importance of the Jahn-Teller distortions [7], both are to be determined simultaneously when an interpretation of the reactivity is the goal.

This mutual dependence follows from the consideration of two coupled effects:

The non-equivalent occupation of energetically degenerate orbitals leads to a splitting of the degeneracy, by means of a distortion of the geometry to a lower symmetry one. The structure of the cluster is determined by Jahn-Teller effects.

Elemental clusters, on the other hand, have the tendency to assume highly symmetric structures, as a consequence of which degeneracy in the one-electron levels occur (effect of the geometry on the electronic structure). Only those systems with a number of electrons sufficient to completely fill or half-fill the sets of degenerate one-electron levels will not Jahn-Teller distort.

This electronic structure-geometry interplay opens a challenging field in the study of the characteristics of metal clusters, when properties relevant to catalysis (local density charges, magnetic moments) are to be analyzed.

With the aim of better understanding the coupling between the electronic configuration and the geometry of the transition metal structures, we discuss, in this paper, the electronic and geometric characteristics of Pd clusters, evaluated at the Self Consistent Field - Configuration Interaction (SCF/CI) level, in an attempt to compare them with those previously found for Rh [23-25].
Different cluster sizes can be analyzed for a given transition metal. On the basis of previous results on Rh clusters [24], we have chosen a 13 atom cluster because it is large enough to provide a good description of the behavior of the tiny particles that are present in supported catalysts and small enough, on the other hand, to allow accurate calculations. A 13 atom cluster is also compatible with the representation of structures of different possible symmetries [5,25], and 13 is one of the magic numbers of atoms frequently observed in clusters of various kinds [5,26,18,19]. In addition, going from the bulk to the smaller crystallites, the density of states of transition metal 13 atom clusters [27] has been found to be close to that of the bulk. Finally we remark that often properties that bear no resemblance to the crystalline state are more frequently found: the most attractive include the larger stability of the five fold symmetry structures and the unusual magnetic properties of these systems.

From many experimental [18,19,27,28] and theoretical [3-7,10,11] investigations, it was concluded that five fold symmetry is the natural choice of small microclusters of materials that crystallize in fcc lattices. Such structures are based on a centered 13-atom icosahedron, representing the minimum energy packing configuration in mono- and bimetallic clusters [29-33]. The planes of 13 as well as 55-atom icosahedral structures resemble close packed (111) planes, the most compact and most stable single crystal structures of fcc lattices. While there is evidence that a 55 atom icosahedron likely represents the actual particle size in supported clusters, a 13 atom icosahedron is an obvious simpler target that keeps the same local properties on the reactive centers because of the identical local environment on each of the sites. This provides an extra justification for the choice of this cluster size in our studies.

According to the previous discussion we apply, in this work, a version of the Intermediate Neglect of Differential Overlap (INDO) model [34,35] at the Self Consistent Field- Configuration Interaction (SCF-CI) level, to study the results of the geometry-electronic structure coupling on the magnetic and structural
characteristics of Pd$_{13}$ clusters. Results on Pd$_4$ and on the dimer Pd$_2$ are also reported for comparison and calibration.

2- COMPUTATIONAL DETAILS -

Because of the 4d$^{10}$ ($^{1}S_0$) ground state of the Pd atom, open- and closed-shell electronic configurations are compatible with both an odd or an even number atom cluster. The stability of the different multiplicities (M) for a given cluster size has been compared after a complete search for the structure of minimum energy on the potential energy surface, starting from different initial geometries which are associated with the different symmetries compatible with the number of atoms that define the cluster.

The calculated geometries are the result of a full optimization of the coordinates (interatomic distances and angles), without any constraint on their variation. Optimization is based on a minimization of the gradient [36,37], evaluated analytically, using the BFGS algorithm to update the inverse Hessian matrix in successive geometry cycles. Calculations have been made at the Restricted Hartree Fock (RHF) and Restricted Open-Shell Hartree Fock (ROHF) level. Dealing with structures of high symmetry and a large number of electrons, changes in the one-electron distribution during the SCF cycles may lead to a non-equivalent occupation of degenerate orbitals which, by breaking the symmetry in the electronic distribution may result in spurious Jahn Teller distortions. In order to avoid this effect, we start the calculations using Configuration-Average Hartree Fock (CAHF) theory [38], with an average M for the number of electrons considered. The final geometries depend somewhat on the number of open-shell orbitals and electrons. This number has been chosen to be compatible with the size of the open-shell for the different average M (i.e., 4 electrons in 3 orbitals for M=3, but in 6 orbitals for M=6). For each of the different geometries that result from the different definition of the open-shell, the M has been chosen after CI calculations, using the orbitals of the CAHF calculation as the reference for a Rumer CI projection over pure spin states [39]. In this way, M and geometry are
simultaneously optimized, avoiding the possibility of getting trapped in spurious local minima corresponding to a stable geometry for a given electronic configuration.

For the 13 atom Pd cluster, the stability of icosahedral ($I_h$) precrystalline structures has been compared to that of fcc ($O_h$) and hcp pieces of bulk. In order to keep the $I_h$ symmetry, it was neccessary to start with an average of 130 electrons in 78 orbitals, then decreasing the orbital space to 66 using the previous set of eigenvectors as an initial guess. These vectors then serve as starting orbitals for a calculation with 4 electrons in 3 orbitals. With a similar strategy, 130 electrons were averaged in 78 orbitals to start the SCF calculations for fcc ($O_h$) and hcp symmetries. The resulting orbitals were used for an intermediate calculation, before the final RHF, with 130 electrons in 65 orbitals.

In the case of Rh$_4$, geometry optimizations have been done for closed-shell and an average of 4 electrons in 3 orbitals, 4 electrons in 6 orbitals, and 10 electrons in 9 orbitals, corresponding, in this way, modelling possible multiplicities (M) as high as 3, 5 or 7, respectively. With this strategy, distortions in the geometry during the SCF cycles are avoided, and geometries optimized for different electronic configurations are compared after a CI that uses the resulting orbitals that maintain full symmetry.

It is clear from this work and our previous work, that correlation energy must be included in the comparison of the energies of the different geometries for a given cluster size. Final energies, as well as electronic parameters and molecular orbital interactions, are the result of multi-reference configuration interaction calculations using single excitations, MRCIS.

Two parametrizations of the INDO theory have been used in these studies: one for geometry, which utilizes two-center two-electron integrals that are calculated ab-initio; and one to calculate the electronic descriptors and compare different M at fixed geometries, that obtain these integrals empirically from atomic spectroscopy [35, 40-42]. This latter method is
parametrized directly on molecular spectroscopy at the CI singles (CIS) level, which explains our use of MRCIS for these clusters. The resonance integrals $\beta$ are chosen according to formulae that takes into account different electronegativities [23], and reproduces the available experimental geometries and spectroscopy for the dimer.

More details on the method are given elsewhere [24,41].

3- RESULTS AND DISCUSSION -

3.1- Pd$_2$ dimer -

The ground state of transition metal dimers is often controversial, because both the symmetry and the geometry are largely dependent on the level of correlation used in the calculations.

Our MRCIS-INDO calculations give a triplet ($^3\Sigma^+_g$) ground state for Pd$_2$, with a leading configuration $\sigma_g^2 \pi_u^2 \delta_g^2 \delta_u^4 \pi_g^4 \sigma_u^1 \sigma_g^1$, and an interatomic distance of 2.46 Å. The lowest exited state is a singlet ($^1\Sigma^+_g$), 0.16 eV higher in energy than the first triplet, with a Pd-Pd bond length of 2.67 Å. The next triplet, $^3\Pi_g$, lies 0.44 eV above the ground state.

The Mulliken population analysis (5s$^{0.065}$p$^{0.05}$d$^{9.89}$ in the first exited singlet, 5s$^{0.515}$p$^{0.05}$d$^{9.44}$ in the triplet ground state) indicates a larger contribution of the 5s orbital to the stabilization of the metal-metal bond in the triplet, shortening the bond length relative to the singlet. The 4d$^{10}$ Pd atoms undergo rehybridization of orbitals in order to form the 5s bonding combination $\sigma_g$ that defines the HOMO.

Our results on the spectroscopy and the geometry of the dimer are in agreement with Density Functional [43,44] and MCSCF/MRCISD calculations [45,46]. The latter has demonstrated to give results that agree well with experiment, not only for the dimer Pd$_2$ [45] but also for the dimer Pd$_3$ [46]. There is general agreement among the different authors in the well studied case of Pd$_2$, in contrast to the situation for Rh$_2$ [23]. While a mixture of configurations characterize the electronic states in Rh$_2$ [23,47,48], we have found that nearly pure configurations characterize the lowest lying states of Pd$_2$. There is also
agreement in the larger bond length in Pd₂ than in Rh₂ (2.28 Å [23]), associated with a more efficient 5s-5s bonding in the latter, where no promotion energy is needed for the 5s contribution to the σ bond.

3.2- Pd₄ structures -

Four atom clusters are most frequently studied in tetrahedral symmetry as models for a (111) structure [44]. They are usually the most stable geometries for fcc habits, with a large coordination number, compatible with the directionality of the d orbitals. We have compared tetrahedral and square planar structures, and found the former 1.77 eV more stable than the latter.

The final geometry of the tetrahedral Pd₄ is strongly dependent on the number of open-shells included in the configuration average, as shown in table 1, and this is to be expected. The more states that we include in an average involving frontier orbitals and electrons, the more likely we are to include high energy states in the average. At the SCF level, RHF calculations are based on a 4d¹⁰ configuration of the atoms and lead to longer interatomic distances than the ROHF procedure. These calculations imply, through the definition of the open-shells, that the participation of the 5s orbitals is important in the stabilization of the bond. Different M have been compared at the MRCIS level for each of the structures in table 1. Independent of the specific model and the geometry, the triplet is always the most stable state.

In table 1 the geometry of the triplet is determined from the indicated calculation using the INDO/1 model with parameters determined for geometry as described in the Computational Details section. The relative energies at fixed geometry are then determined via MRCIS INDO/S calculations. For this reason energies between rows cannot be compared.

The Mulliken populations, reported for the triplets, show the larger contribution of the s orbitals to the shorter bonds. The s participation is, in turn, dependent on the open-shell definition of the initial configuration.
Lower energies are always found for an average of 4 electrons in 3 orbitals. For this definition of the open-shell, several interatomic distances, which may either result from geometry optimizations from different initial guesses or single point calculations, have been compared. As one of the single points, the interatomic distance characteristic of the bulk (2.75 Å [49]) has been analyzed. The results for the different M are reported in table 1. These calculations indicate a very flat potential for Pd₄. Within the accuracy of our treatment, however, no change in the interatomic distance with the change in M can be assessed.

The most stable structure (ground state-GS) corresponds to a triplet ³T₂ (Fig 1), with a leading configuration 1a₁²1t₂⁶1e⁴1t₁⁶2e⁴2t₁⁶ 2t₂⁶2a₁²3t₂⁴3t₁⁰. At this geometry the singlet ¹A₁ lies 0.40 eV higher in energy and has the same electronic assignment as the GS.

The Mulliken population analysis shows a smaller population of the s orbital in the configuration that results from RHF calculations and this leads, in turn, to longer Pd-Pd interatomic distances.

Similar calculations for the square planar geometry yield a ³B₁g GS, with an interatomic distance of 2.34 Å.

This state is 0.14 eV lower in energy than the first exited state we calculate for this structure, which is of ¹A₁g symmetry.

**3.3- Pd₁₃ structures**

After a full optimization of the geometry in the way previously described, the I₄h symmetry is calculated to be most stable, table 2. The interatomic distance of 2.63 Å among the peripheral surface atoms (Fig. 2) represents a compromise between the value in the diatomics (2.46 Å [48]), and that in the bulk (2.75 Å [49]).

The results of MRCIS calculations show that the GS is a triplet, ³T₂g (Fig. 3), 0.21 eV lower in energy than the first exited singlet ¹H₉. These two states arise mostly from the configuration shown in Fig. 3. The next triplet, ³G₉, is 0.28 eV above the GS, followed by two singlets, ¹G₉ and ¹A₉, 0.08 and
0.25 eV higher in energy respectively. The singlet $^1A_g$ also arises from the configuration shown in Fig. 3. The lowest quintet $^5T_u$, lies 0.73 eV above the GS (table 2). About 38 terms lie within 1.0 eV of the lowest calculated $^3T_{2g}$.

The most stable structures in either $O_h$ or $D_{3h}$ symmetries belong to closed-shell configurations $^1A_g$ and $^1A_1''$, respectively, and are about 1.7 eV less stable than the $^3T_{2g}$ GS of $I_h$ symmetry (table 2). The triplet $^3T_{2g}$ in $O_h$ symmetry is 0.37 eV higher in energy than the singlet $^1A_g$, and the quintet of $^5T_{1u}$ symmetry is 1.15 eV higher in energy. In the hcp ($D_{3h}$) structure, the triplet $^3A_1''$ and the singlet $^1A_1''$ are almost degenerate, with the singlet 0.06 eV lower. The lowest quintet of $^5A_1$ symmetry is calculated to lie 1.036 eV above the GS.

We have checked the $^1A_g$ of $O_h$ symmetry and the $^1A_1''$ of $D_{3h}$ symmetry and both are true minimum on the potential energy surface.

The larger stability of five fold symmetries in small transition metal clusters has been both experimentally determined [15,20,21] and theoretically derived [5,7,11,24,50]. It is known from experiment that five fold symmetry characterizes small Co, Cu, Ni and Mg clusters [15,20,21]. Calculations are more frequently found for the lighter elements, although molecular dynamics and density functional theory, applied to Ni$_{13}$ and Cu$_{13}$ respectively [3,5,11], also favor the $I_h$ symmetry. In recent density functional calculations (LSD), Reddy, Khanna and Dunlap [50] find $I_h$ structures more stable than $O_h$ for Pd$_{13}$, Rh$_{13}$ and Ru$_{13}$, in agreement with our present results on Pd and those previously published for Rh [25]. However, they have not considered any decrease in the symmetry, and the large magnetic moment of the $I_h$ clusters, which results from the partial filling of the d bands in structures of high symmetry, is the main topic of their discussion.

The small transition metal clusters are models of catalytic active sites, which are usually associated with surface defects, characterized by a local electron deficiency. A Mulliken population analysis (table 2) shows a negative charge (-0.175 au) largely concentrated on the atom in the center, counterbalanced
by a small positive charge (0.015 each atom) distributed among the peripheral atoms. Previous calculations on the interaction of CO with Rh clusters [24] have demonstrated larger activity towards CO adsorption on electron deficient sites, characteristics of the surface atoms, in the precrystalline structures. The study of the electronic characteristics imply, thence, practical importance, and can only be analyzed after a complete study of the structure of minimum energy.

3.4- On the stability of the highly symmetric structures -

The electronic degeneracy in a molecule forces departures from the symmetry on which the degeneracy was evaluated [51,52]. Therefore, for non-linear molecules, a nuclear arrangement that will lead to electronic degeneracies will automatically have at least one non-totally symmetric vibrational coordinate that will split the degenerate state and destroy the symmetry. When degeneracy occurs, only those systems where the number of electrons either completely fill or half-fill sets of degenerate one-electron levels will not Jahn-Teller distort. As this is not the case of either Pd$_{13}$ or Pd$_4$ structures, the nature of the distortion should be evaluated.

The large stability of the I$_h$ and T$_d$ structures for the 13 and 4 atom clusters respectively, allowed us to obtain these structures through configuration averaging. This, of course, is an intermediate stage we examine to make comparisons with the work of others, and one which will allow us to examine the Jahn-Teller distortions in some detail. Of interest is that we were unable by any means to successfully obtain the full I$_h$ structure for Rh$_{13}$. Rather, a near C$_{5v}$ symmetry is achieved from both I$_h$ and O$_h$ starting geometries [25]. We have not been able to analyze quantitatively the steps and the normal modes involved in the distortion of the Rh$_{13}$ molecule from I$_h$ to C$_{5v}$, although we could for Rh$_{13}^+$ [25].

In order to analyze this effect for Pd, and to learn about distortions that may lower the energy through the splitting of the degenerate orbitals, different initial geometries have been
compared, which are related through a normal mode to the higher symmetry ones.

**a- Icosahedral Pd\(_{13}\) clusters.**

According to the electronic distribution depicted in Fig 3, the Jahn-Teller theorem requires a splitting of the \((t_{2g})^4 = 3T_{2g} + 1H_g + 1A_g\) degeneracy, leading to orbitals of \(e_{2g}\) and \(a_{2g}\) symmetry in D\(_{5d}\). Correspondingly, the \(3T_{2g}\) state reduces to \(3E_{2g}\) and \(3A_{2g}\), the \(1H_g\) state to states of \(1A_{1g}\), \(1E_{1g}\) and \(1E_{2g}\) symmetry and \(1A_g\) becomes \(1A_{1g}\), see Fig. 4. The relative positions of the \(e_{2g}\) and \(a_{2g}\) orbitals in energy depend on the final geometry. The simpler distortions that can be idealized imply an axial elongation along the principal axis in D\(_{5d}\) symmetry (z axis, Fig 2) or an axial compression along the same axis, to give prolate or oblate ellipsoids respectively, from an initial spheroid \(I_h\) structure. Depending on the characteristics of the distortion, the \(e_{2g}\) orbital will be above or below the \(a_{2g}\) for the elongated or compressed geometries respectively.

In the case of Pd\(_{13}\), the prolate or oblate distorted starting structures returns to the perfect \(I_h\) after optimizing the geometry. Starting structures resulting from prolate or oblate distortions along a 3 fold axis in D\(_{3d}\) symmetry, or a 2-fold axis in D\(_{2h}\) symmetry, also lead to the perfect \(I_h\).

After several trials, a related structure was found, with lower energy than the initial \(3T_{2g}\). It is the result of an elongation of the Pd\(_{13}\) \(I_h\) molecule along the principal axis in D\(_{5d}\) symmetry, coupled to a compression along the same axis that shortens the distance between opposite pentagons (Fig. 5). This corresponds to an \(h_g\) mode in \(I_h\) symmetry.

The molecular orbital distribution in the D\(_{5d}\) structure shows the \(e_{2g}\) orbital below the \(a_{2g}\) (Fig.3). The lowest energy corresponds to a singlet \((1A_{1g})\), followed by a triplet \((3E_{2g})\), which lies 0.16 eV above. The next states are a triplet and a singlet which lie 0.31 and 0.49 eV, respectively, higher in energy than the GS, see Fig 5.

The distortion of the geometry can be described as a first order Jahn-Teller effect from the \(3T_{2g}\), in \(I_h\) symmetry, to the
$^3E_{2g}$ in $D_{5d}$, through an $h_g$ mode, with an energy decrease of 0.9 Kcal. Further decay to the singlet $^1A_{1g}$ decreases the energy through spin pairing to give a closed-shell structure (Fig. 5). The GS of the Jahn-Teller distorted structure is 4.68 Kcal below the spherical $^3T_{2g}$. An alternative conceptual description may involve the lowest singlets in $I_h$ and $D_{5d}$ symmetries. An initial activation from the triplet to the singlet implies, however, an energy barrier of 0.21 eV. We stress conceptual as the Jahn-Teller effect is a theoretical construction to describe distortions, not a physical one. One does not observe $I_h$ distorting to $D_{5d}$, one simply observes $D_{5d}$.

A Mulliken population analysis of the $D_{5d}$ GS structure shows that a negative charge (-0.154 au) is still located on the atom in the center, while the positive charge is now more concentrated on the apical atoms (+0.149 au on each). This allows one to infer a larger catalytic activity of these centers.

Although the highly symmetric structures are characterized by a non-zero magnetic moment, the stabilization through a Jahn-Teller distortion, followed by spin pairing, results in a prediction of diamagnetic $Pd_{13}$ clusters.

The consecutive geometric distortion—followed by electron pairing shows the importance of this interplay: the geometry of the final (distorted) state, which is a consequence of the electronic distribution in the higher symmetry one, leads to spin quenching.

Providing that there is not a large change in the geometry and that the molecular orbital distribution is nearly kept, the positively charged $Pd_{13}^+$ structure would give a perfect icosahedron which would not distort, due to the equivalent filling of the degenerate $t_{2g}$ HOMO orbitals. The optimization of the geometry gives a perfect icosahedron (Fig 2), with an interatomic distance of 2.63 Å and a molecular orbital distribution similar to that in the neutral but for the $t_{2g}$ - $h_g$ inversion and the larger HOMO-LUMO gap (Fig 6). The GS is a quartet $^4A_g$, followed by a doublet $^2H_g$, which is 0.22 eV higher in energy.
Pd_{13}^+ clusters would be predicted to have non-zero magnetic moments.

**b- Tetrahedral Pd$_4$ clusters.**

The tetrahedral Pd$_4$ clusters are predicted to have $^3T_2$ symmetry, and they also suffer a first order Jahn-Teller distortion.

After examining several structures, we find that the most stable structure, depicted in Fig 7, corresponds to a $^3A_2$ in $C_{2v}$ symmetry, and is the result of a Jahn-Teller distortion of the $^3T_2$ in $T_d$ symmetry through an e mode. There is no extra stabilization through spin pairing. The GS in $C_{2v}$ is a non-degenerate triplet, with the lowest singlet, $^1A_2$, 0.38 eV higher in energy. The energy associated to the distortion is 0.08 eV (1.84 Kcal).

The Pd$_4$ clusters are, thence, paramagnetic.

4- CONCLUSIONS -

In agreement with previous results on Rh$_{13}$ and Rh$_4$ clusters, we have found that Icosahedral and Tetrahedral geometries are, respectively, the most stable ones for the higher symmetric structures. Both Ih and Td structures are characterized by a large concentration of triangular faces, which are the minimum part of an fcc(111) structure, associated with the larger packing density and the lower total energy for this crystalline habit. This is accepted as a valid explanation of the larger stability of these geometries for the cluster sizes analyzed. The final geometries are, however, largely determined by Jahn-Teller distortions, that we predict lower the Ih and Td geometries to D$_{5d}$ and C$_{2v}$ structures, respectively.

A small energy difference between the symmetrical and the distorted structure may determine the spontaneous evolution to the latter. This effect, previously found in Rh$_{13}$ clusters, does not characterize either Pd$_{13}$ or Pd$_4$ clusters, and the different steps involved in the distortion can be analyzed. This analysis, discussed in this paper, shows the close relation and mutual
dependence between the electronic structure and the geometry of the small structures.

The electronic configuration of the final structure, which we found determined by a Jahn-Teller distortions in both Pd$_4$ and Pd$_{13}$ defines the magnetic moment of the tiny particles. While we calculate that paramagnetism characterizes Pd$_4$ clusters, the most stable Pd$_{13}$ structures have zero magnetic moment. Recent density functional calculations [50] have found a non-zero magnetic moment (-2$\mu_B$), based on a most stable I$_h$ symmetry. This is in agreement with our results for this structure. But our final structure is a distorted I$_h$ cluster of D$_{5d}$ geometry and has a zero magnetic moment. This agrees with the zero magnetic moment experimentally found [53].

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REFERENCES

- **FIGURE CAPTIONS** -

- **Figure 1** - The frontier molecular orbitals obtained for Pd$_4$ in T$_d$ symmetry and the distorted molecule in C$_{2v}$ symmetry. The distortion that relates both structures is indicated. Energies are in Hartrees.

- **Figure 2** - Most stable Pd$_{13}$ structure as result from a full geometry optimization procedure, starting from an Ih initial structure. The symmetry is kept when 4 electrons are averaged in 3 orbitals in the CAHF calculations. More details are given in the text.

- **Figure 3** - The frontier molecular orbitals obtained for Pd$_{13}$ in Ih symmetry and the distorted molecule in D$_{5d}$ symmetry. The distortion that relates both structures is indicated. Energies are in Hartrees.

- **Figure 4** - Electronic states associated to the Ih $\rightarrow$ D$_{5d}$ Jahn-Teller distortion of the Pd$_{13}$ structure.

- **Figure 5** - Distortion of the Pd$_{13}$ molecule, in Ih symmetry, to the most stable one in D$_{5d}$ symmetry. Geometrical parameters are indicated.

- **Figure 6** - The frontier molecular orbitals obtained for Pd$_{13}^+$ in Ih symmetry, from CAHF calculations with 3 electrons in 3 orbitals. Because of the half filling of degenerate orbitals, the molecule does not Jahn-Teller distort. The symmetry of the resulting state is $^4A_g$.

- **Figure 7** - Distortion of the Pd$_4$ molecule, in T$_d$ symmetry, to the most stable one in C$_{2v}$ symmetry. Geometric parameters are indicated.
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<td>bulk</td>
<td>-118.075 ( {^1A_1} )</td>
<td>-118.093 ( {^3T_2} )</td>
<td>-118.020 ( {^5T_1} )</td>
<td>-118.001 ( {^7T_2} )</td>
<td>2.750</td>
<td>( 5s^{0.53}5p^0. ) 144d^{9.32}</td>
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</table>

Table 1- Absolute values of the total energies [Hartrees] calculated for Pd₄ tetrahedral structures after MRCIS calculations. Electronic states are also indicated. Different M are compared for the different geometries that result from RHF (1st row) or CAHF calculations with different number of open shells included in the average. 4/3, 4/6 and 6/9 stands for 4 e⁻ in 3 orbitals, 4 e⁻ in 6 orbitals, and 6 e⁻ in 9 orbitals, respectively.

In the last row, calculations for the bulk interatomic distance are reported. The Mulliken populations (M.P.) given are for the triplet, see text.
<table>
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<th></th>
<th>Ih</th>
<th></th>
<th>Oh</th>
<th></th>
<th>D3h</th>
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<td>Energy</td>
<td>State</td>
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<td>-384.447</td>
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<td>$^3$T$_{2g}$</td>
<td>-384.435</td>
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<tr>
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<td>-384.406</td>
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<td>5p$^0.78$</td>
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<td>r[A]</td>
<td>Fig. 1</td>
<td>2.54</td>
<td></td>
<td></td>
<td>2.55</td>
<td></td>
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Table 2- The total valence energies [hartrees] calculated for Pd$_{13}$ structures after MRCIS calculations. Electronic states are also indicated. Different M are compared for the geometries associated with the Ih, Oh and D$_{3h}$ symmetries. Details on the calculations are given in the text. The Mulliken populations (M.P.) are reported for the central atom and correspond to the most stable M for each geometry.
-0.21092 — — — $T_1$

-0.35011 — $A_1$

-0.36348 — — $T_2$

-0.41225 — — — $T_2$

$Pd_4$, $Td$

$^3T_2$ $\rightarrow$ $^3A_2$

$Pd_4$, $C_{2v}$
Pd$_{13}$, I$_h$

$^3T_{2g}$, $^1H_g$  $\rightarrow$  $^3E_{2g}$, $^1A_{1g}$

Fig 3
- 0.39590  —  —  —  —  —  h_g
- 0.42708  —  —  —  —  —  a_g
- 0.43422  —  —  —  —  —  t_{1u}

- 0.53781  —  —  —  —  —  t_{2g}
- 0.54645  —  —  —  —  —  —  h_g
- 0.54698  —  —  —  —  —  —  t_{1g}

- 0.56617  —  —  —  —  —  —  —  h_u

\text{Pd}^{+}_{13}, \text{Ih}
Fig 7

$T_d \rightarrow C_{2v}$

$2.39 \rightarrow 2.43$

$2.39 \rightarrow 2.55$

$2.39 \rightarrow 2.35$