Applications of motion estimation in image processing
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This report presents examples of image sequence processing using motion estimation. We present results of noise reduction by motion compensated temporal filtering in a noisy image sequence and we give examples of the detection of moving targets in an air-to-ground IR image sequence.
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SAMENVATTING (ONGERUBRICERD)

In dit rapport worden voorbeelden gegeven van beeldbewerking op beeldreksen waarbij gebruik wordt gemaakt van bewegingsschatting. Er worden resultaten getoond van ruisreductie door bewegingsgecompenseerde temporele filtering en van de detectie van bewegende doelen in een air-to-ground IR beeldreks.
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INTRODUCTION

Motion perception is an important source of information for the human visual system. The determination of our motion relative to the environment as well as the determination of the three-dimensional structure of the environment largely depend on the interpretation of visual motion. The human visual system is capable of extracting information from a sequence of images that is hard to extract from the individual images. An example is the interpretation of a very noisy image sequence. By using spatial and temporal correlation we are able to "see through the noise." Sometimes, visual detection of an object fully depends on the perception of motion. This is illustrated by the ease with which we see an otherwise successfully camouflaged object as soon as it moves.

The apparent motion of brightness patterns observed when a camera is moving relative to the objects being imaged is called optical flow. Optical flow can be represented by a two-dimensional vector field. Loosely speaking, the optical flow field links a pixel at the position \((x, y)\) to the corresponding pixel at position \((x + u(x, y), y + v(x, y))\) in the next image. Ideally, both pixels correspond to the same physical object point in the scene. In practice, this is hard to achieve because there is an infinite number of vector fields that is consistent with the data. Possible approaches to the problem of estimating the optical flow field are described in a separate report [2]. This report also describes the particular approach to the motion estimation problem we have taken. See also [1].

The goal of this report is to give examples of image sequence processing using motion estimation. All examples were obtained by simple and straightforward methods. The examples show what kind of improvements or detection results can be expected, rather than being optimal results in some sense.

Chapter 2 of this report is concerned with noise reduction in a noisy image sequence. It presents some results on IR image sequences.

Chapter 3 deals with the detection of moving objects in image sequences. Typically, these sequences are recorded from a moving platform. The aim is to detect objects moving relative to the moving background.

There are numerous other applications of image motion estimation. These include image sequence coding, satellite image processing, medical image processing, robot vision, obstacle avoidance, image sequence stabilization etc.
2 NOISE REDUCTION IN IMAGE SEQUENCES

This chapter is concerned with noise reduction in image sequences by motion compensated temporal filtering. We present some preliminary results obtained with straightforward methods.

2.1 Filtering along motion trajectories

By \( I(x, t) \) we denote the image brightness function, where vector \( x \) denotes the spatial coordinates and \( t \) denotes time. Let \( v(x, t) \) be the displacement of the image point at \( (x, t) \) between time \( t - \Delta t \) and \( t \), where \( \Delta t \) denotes the temporal sampling interval. Assuming that image brightness for an object point is conserved over time, we can write

\[
I(x, t) = I(x - v(x, t), t - \Delta t)
\]  

(2.1)

Obviously, \( v \) is undefined when an object is occluded or when it is newly exposed. In general \( v \) will be a slowly varying function of the spatial coordinates with discontinuities at the edges of moving objects. A spatiotemporal volume can be formed by stacking the consecutive frames of the sequence. A physical point in the scene traces out a trajectory in this spatiotemporal volume during the time it is visible in the sequence. The brightness value along this trajectory forms a one dimensional signal. This signal is assumed to consist of a deterministic image component and an additive noise component. Variation of the image component is due to change in the luminance of the object. This variation is assumed to be relatively slow, so that the image component is a low bandwidth signal. The additive noise is assumed to be uncorrelated with the image signal. Lowpass filtering along the motion trajectory can significantly reduce the noise component. The filter operation along the motion trajectory can be either linear or non-linear. When the image noise is additive Gaussian noise, independent in each pixel and of fixed variance along a motion trajectory, then it can be shown that the sample mean along a motion trajectory is the maximum likelihood estimator for the grey value of the pixel. In this case, the linear estimator will yield the best signal to noise ratio in the result. On the other hand, a non-linear filter may be more robust to errors in the displacement estimate and the non-validity of the noise model e.g. in the case of dead pixels in the images. In addition, a non-linear filter might be able to deal with occlusion and exposure effects more adequately. The choice of filter will generally depend on the ease of implementation and the particular distortions in the image sequence. The number of frame stores can be reduced if the used filter is recursive [5].
With regard to exposure and occlusion effects, it would be of interest to know exactly the lifetime of a motion trajectory. Unfortunately this is a hard problem. It requires the identification of image areas that are newly exposed and image areas that are just occluded in each frame of the image sequence. Most current motion estimators are not able to solve this problem reliably.

2.2 Examples

This section presents examples from a IR image sequence. Figure 2.1 shows the reference image from this sequence. All computations are performed relative to this image. Figure 2.1 shows the average of six motion compensated images, 3 forward in time and 3 backward in time, and the reference image. This result is an example of a linear filtering operation along the motion trajectories. Figure 2.2 shows the median of six motion compensated images and the reference image. This result is an example of a non-linear filtering operation along the motion trajectories. It is clear from both the linear and the non-linear results that the noise is significantly reduced without affecting the sharpness. In this case, the linear filter yields a visually more pleasing result. In both results details become visible that are hard to infer from a single noise corrupted image. Figure 2.2 shows the result of running the contrast enhancement algorithm of [4] on the image of figure 2.1. This algorithm locally adjusts the contrast. Without the noise reduction furnished by the motion compensated filtering, local contrast enhancement merely amplifies the noise and other image distortions.
Figure 2.1: (Top) Original reference image from an IR image sequence. (Bottom) Mean along motion trajectories of six motion compensated images and the reference image.
Figure 2.2: (Top) Median along motion trajectories of six motion compensated images and the reference image. (Bottom) Contrast enhanced version of bottom image of figure 2.1
DETECTION OF MOVING TARGETS

This chapter is concerned with the detection of moving targets from an image sequence produced by a moving camera. The proposed approach is particularly well suited for air-to-ground applications. In principle, it is possible to detect camouflaged targets moving relative to a textured background.

3.1 Principle of detection

Algorithms for the detection of dim, low contrast targets usually consist of two stages. Firstly, the algorithm selects a number of potential targets, for example bright spots. Due to clutter\(^1\) this usually results in a large number of false alarms. The second stage therefore has to reject the falsely selected objects. This can be done by combining information over frames, or by use of contextual information.

In this report, we choose to detect targets on basis of their motion. Our approach consists of essentially two stages:

1. motion estimation,
2. target detection in the motion compensated image sequence.

We assume we have to deal with an essentially stationary scene that is being imaged from a moving platform (e.g. helicopter). If we are able to estimate a sufficiently accurate 2-D vector field that maps one frame in the sequence to the next, we can in principle predict one frame from the previous one. The principle to detect moving targets is particularly simple and amounts to analyzing the image sequence on the occurrence of unexpected events. In this context, unexpected events are temporal variations of the image brightness function that are impossible to predict and that can not be accounted for by noise. Thus, targets are detected by analyzing the difference between the predicted and the actual image.

As a simple example of this detection principle, consider a stationary camera imaging a stationary scene. From one or a collection of images (frames) it is possible to predict the next frame to be acquired by the camera. The prediction is simply the previous frame or an estimate based on a collection of previous frames, such as the pixel-wise mean. The only difference between the predicted

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\(^1\)In this report, clutter is loosely defined as the amount of target-like objects in a scene.
frame and the actually acquired frame will be due to noise that is introduced somewhere in the imaging process. When an object in the scene moves, it is generally impossible to predict the next frame from a limited history of past frames. This is due to the fact that the object uncovers background that is not visible in previous frames and hence hard to predict. Even when motion estimation is used, and the moving part of the scene is warped\(^2\), it is impossible to predict the background that is uncovered by the moving object. Subtracting the predicted frame from the actual frame will generally produce large differences at image locations corresponding to covered and uncovered background. Automatic detection based on this principle is feasible by comparing the differences with the noise statistics of the difference image.

A similar detection principle can be used when a scene is imaged from a moving platform. In this case we have to perform image registration prior to subtraction. Image registration is done by estimating the image motion field and warping the first frame to the next accordingly. The image motion is estimated using the method described in [1, 2]. Image warping generally involves interpolation. In the examples shown in this chapter we used bi-linear interpolation.

In evaluating the difference images thus obtained, we have to distinguish several possibilities.

1. When the image motion estimate is perfect, the scene has no appreciable depth discontinuities, and there are no moving objects in the scene, we expect the difference image to be a sample from a 2-D random noise process. The noise is a mixture of image noise and noise due to the interpolation process.

2. When the motion estimate is accurate, there are no moving objects, but there is considerable depth variation in the scene, we expect uncovered background adjacent to physical edges of foreground objects. This is the parallax effect. Generally, this will result in large amplitudes in the difference image at locations corresponding to covered and uncovered background, while the rest of the difference image is characterized by random noise. In air-to-ground imagery the large response areas will usually be chain-like, for example the outline of a hill. Although the large response areas will generally not correspond to moving targets, they are nonetheless of interest because they often correspond to previously unexposed parts of the scene. In some applications it may be of interest to perform extra processing on parts of the scene that are newly exposed.

3. When there are moving objects in the scene and the motion estimate is such that this object motion is correctly captured, the difference image will show large amplitudes at locations of

\(^2\)In this context, warping is the process in which one image is registered with another and re-sampled (interpolated) at the grid positions of the reference image.
covered and un-covered background if the background is sufficiently textured. This enables us to detect camouflaged objects.

4. When there are small, moving objects we may be unable to capture object motion correctly. This behaviour may be forced by only using large scale image structure in the motion estimate. In this case the difference image will generally display a small area with a large positive response adjacent to a small area with a large negative response. This case is of practical interest in target acquisition applications at long stand off ranges.

To automate the detection process, we have to make a number of assumptions about the image noise statistics. In the examples shown in this report, the noise was assumed to be additive zero-mean Gaussian noise, independent in each pixel. The noise statistics are obtained from a fit of a Gaussian to the sample histogram of the difference image. This is more robust than calculating the usual sample statistics because the influence of the outliers (targets!) is reduced. From the standard deviation thus obtained, a statistically meaningful threshold may be obtained.

The confidence in the presence of potential targets may be increased by correlating the detection results over time. This may involve more or less sophisticated techniques such as [3].

The overall procedure for detection of moving targets can be summarized by the scheme of figure 3.1
Figure 3.1: Block diagram for the detection of moving targets in an image sequence obtained by a moving camera.
3.2 Example of target detection using target motion

The example shown in figure 3.4 is an example of case 4 in the enumeration of pages 11 and 12. The upper photograph of figure 3.4 shows a frame from an air-to-ground IR image sequence. In this sequence there are several moving targets, cars on the roads. Notice that in this sequence the contrast is inverted, i.e. hot areas appear dark. For the present algorithm, this makes no difference.

For the target detection we used three frames $f(t)$ at times $t_0$, $t_0$ and $t_0$. The image motion between $f(t_0)$ and $f(t_0)$ and between $f(t_0)$ and $f(t_0)$ was estimated using the phase based estimator described in [1, 2]. Because this image sequence is contaminated by a fair amount of noise and sensor artefacts, and because this image sequence lacks small scale image structure in certain parts of the scene, we used a planar patch model to improve the estimated image motion.

It can be shown [6] that the planar patch model is described by the mapping:

\[
X' = \frac{A_{11}X + A_{12}Y + A_{13}}{A_{01}X + A_{02}Y + 1},
\]

\[
Y' = \frac{A_{21}X + A_{22}Y + A_{23}}{A_{01}X + A_{02}Y + 1}.
\]

Equations (3.1) and (3.2) define a mapping from the two-dimensional image-space $(X, Y)$ at time $t = t_0$ onto the image-space $(X', Y')$ at $t = t_0$, see figure 3.2. The eight non-trivial parameters $A_{ij}$ are the so called pure parameters $(A_{ii} = 1)$. They are uniquely determined for a given motion and planar patch. The pure parameters are estimated from the image motion vectors produced by the phase based motion estimator. Both $f(t_0)$ and $f(t_0)$ were warped according to the estimated model (3.1) and (3.2) to obtain estimates valid at $t = t_0$. These warped images are denoted by $f(t_0)$ and $f(t_0)$.

First, we form the difference images $d_0 = f(t_0) - f(t_0)$ and $d_0 = f(t_0) - f(t_0)$. Figure 3.3 shows a histogram of $d_0$. From figure 3.3 it is clear that this distribution is very well approximated by a Gaussian distribution, as shown by the dashed line. The parameters of this Gaussian were determined using a non-linear least squares fit to the histogram.

Next, we apply a thresholding procedure to the difference images $d_0$ and $d_0$. A threshold factor $\theta$ is selected. Let $p(x, y)$ be the pixel value at location $(x, y)$ in either $d_0$ or $d_0$, and let $\mu$ and $\sigma$ be the corresponding mean and standard deviation, respectively, as determined by the histogram fit. We define $s$ by

\[
s(x, y) = \frac{p(x, y) - \mu}{\sigma}.
\]
Figure 3.2: Basic geometry for three-dimensional motion estimation. Lower case letters refer to 3-D scene coordinates, whereas the image coordinates are denoted by capitals. $F$ is the focal length of the camera. $(x, y, z)$ denote the coordinates of an object at $t = t_1$, $(x', y', z')$ give the coordinates of the same object at $t = t_1$.

The result of thresholding procedure is determined by:

$$
o(x, y) = \begin{cases} 
0 & \text{if } |s(x, y)| < \theta/2 \\
\frac{2s(x, y)}{\theta} - \text{sign}(s(x, y)) & \text{if } \theta/2 < |s(x, y)| < \theta \\
\text{sign}(s(x, y)) & \text{if } |s(x, y)| > \theta
\end{cases}
$$

where $\text{sign}(\xi)$ is defined by

$$
\text{sign}(\xi) = \begin{cases} 
-1 & \text{if } \xi < 0 \\
0 & \text{if } \xi = 0 \\
1 & \text{if } \xi > 0
\end{cases}
$$

This yields two frames of which almost all pixels are zero except for a number of positive and negative 'blobs' with values between 0 and 1 and -1 and 0, respectively. This thresholding procedure has the advantage that it retains target responses that are not very strong. Of course, these 'weak' target responses have to be confirmed later on. Next, we discard all non-zero pixels in both frames that have opposite signs at corresponding positions. These 'cleaned' images are referred to as $c_-$ and $c_+$. 
Figure 3.3: Histogram of the difference image $d_+$, obtained by subtracting the motion compensated image $f(t_+)$ from the reference image $f(t_0)$. The dashed line represents the fitted Gaussian.

In the next step, we combine the images $c_-$ and $c_+$ by pixel-wise multiplication. The positive blobs in this image, denoted by $T_0$, correspond to potential targets.

The detection result shown in figure 3.4 was obtained by requiring that each target in $T_0$ corresponds to an object in image $f(t_0)$ that significantly differs in greyvalue from its neighborhood as determined by an inverse median filter. Inverse median filtering amounts to forming the difference between the original image and a median filtered version of it.
Figure 3.4: (Top) One image from an air-to-ground IR image sequence. (Bottom) Four consecutive frames with the detected moving targets in red. There are a few false alarms in individual frames. However, only the true targets are consistently detected. The false alarms could be eliminated by requiring consistency over time.
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Automatic, adaptive, brightness independent contrast enhancement.  

Noise reduction in image sequences using motion compensated temporal filtering.  

Estimating three-dimensional motion parameters of a rigid planar patch.  

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    THIS REPORT PRESENTS EXAMPLES OF IMAGE SEQUENCE PROCESSING USING MOTION ESTIMATION. WE PRESENT RESULTS OF NOISE REDUCTION BY MOTION COMPENSATED TEMPORAL FILTERING IN A NOISY IMAGE SEQUENCE AND WE GIVE EXAMPLES OF THE DETECTION OF MOVING TARGETS IN AN AIR-TO-GROUND IR IMAGE SEQUENCE

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