STUDIES OF REGIONAL PHASE PROPAGATION IN EURASIA

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This technical report has been reviewed and is approved for publication.

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We investigated various issues related to the propagation of seismic waves in Eurasia during the period 16 Aug 1990 - 15 Dec 1992. This final report covers the research accomplished under the 2 tasks that have not been reported previously in the first annual report PL-TR-92-2042.

Section I describes briefly how we derived a spherically symmetric velocity structure for the Garm region in Central Asia with travel-time residuals of regional phases recorded at the IRIS station GAR and the CDSN station WMQ. In Section II, we conducted a tomographic inversion to determine the regional Lg Q structure in the Iranian Plateau. Although the whole of Iran can be regarded as a region of very low Q, applying a simple averaged attenuation coefficient (Q) for the whole plateau would be inappropriate for the Lg magnitude determination. The regional variation of the anelastic attenuation parameter is significant enough that it must be taken into account in calibrating each monitoring station for a reliable magnitude scale in monitoring possible clandestine tests from a vast area. Section III of this report gives a perspective overview of the whole project.
SUMMARY

As part of Phillips Laboratory's Eurasian Seismology Program, we have been investigating the path effects on seismic waves under Contract F19628-90-C-0158 during the period 16 Aug 1990 - 15 Dec 1992. Both theoretical and observational studies were conducted at different phases of this project to explore a wide spectrum of topics that are directly related to the monitoring of compliance of the Threshold Test Ban Treaty and the Non-Proliferation Treaty:

[1] Quantifying the path effects on body-wave amplitudes of Novaya Zemlya explosions.

The first two sections of this final report cover the research performed under Tasks 3 and 4, respectively. We present a perspective overview of the whole project in the third section, which also summarizes the work done under Tasks 5 and 6. The results obtained under Tasks 1 and 2 have been reported previously in our first annual report PL-TR-92-2042.

The objective of Task 3 is to obtain the velocity structure of the Garm region of Central Asia. Travel-time residuals of regional phases recorded at the IRIS station GAR and the CDSN station WMQ were used to derive a spherically symmetric structure for the crust and upper mantle in this region.

Under Task 4 we examined a general procedure which incorporates the independently derived information of localized path effects into the magnitude determination. The goal of this exercise is to quantify the bias in the seismic magnitude (such as mb(Lg)) that would be inherent in a scheme without fully coupling the regional propagational characteristics into the magnitude determination procedure. Iran was chosen as a test case in this study because of the growing nuclear proliferation concern in the Middle East. A tentative zoning partitioning the Iranian Plateau into six regions has been used in our block inversion to reveal the spatial pattern of the Lg attenuation parameter, Q. Although the whole Iranian Plateau can be briefly described as a region of very low Q, applying a simple averaged attenuation coefficient (Q) for the whole plateau would be inappropriate for mb(Lg) calculation. The regional variation of the anelastic attenuation parameter is significant enough that it must be taken into account in calibrating each monitoring station for a reliable magnitude scale for monitoring possible clandestine tests from a vast area.
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SECTION I
TRAVEL TIME INVERSION IN THE GARM REGION

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1. INTRODUCTION

The propagation of regional phases is still problematic: amplitudes and even the observability of phases can be highly variable. This has important implications for the application and efficacy of earthquake/explosion discriminants and event size estimation. At least some of this variation is likely due to the effects of lateral heterogeneity, particularly in the waveguides and near the boundaries along which regional phases such as $P_g$, $P_n$, $S_n$, and $L_g$ propagate. The effects of lateral heterogeneity on regional phase propagation can be modeled using finite-difference methods. To employ these methods, however, a realistic velocity model is required. Block inversion of travel times is a well-established technique for deriving laterally heterogeneous velocity structures. In order to simplify the problem and improve ray coverage, a two-dimensional geometry is sought: the high seismicity rate in the vicinity of the IRIS station GAR provides such an opportunity. The first step in this process is the derivation of a spherically symmetric structure for the crust and upper mantle in this region. This model can then serve as the starting model for a two-dimensional velocity inversion in the vertical plane.

2. METHODOLOGY

The inversion method used herein is based on the joint inversion of hypocenters and velocity structure outlined by Crosson (1976). Beginning with a starting model, perturbations ($\Delta m$) to the previous model $m$ are sought to minimize the travel time residual vector $d = T_{pred} - T_{obs}$. The model perturbations include both hypocentral parameters and velocity structure.

The above method requires computations of theoretical travel times, ray parameter and partials for all source-station pairs in an arbitrary velocity structure. As the solution of the two-
point problem can be lengthy and unstable in the presence of low-velocity zones or strong gradients, we use Vidale's (1988) finite-difference technique to compute the travel times throughout a two-dimensional grid for a source at the surface. The various hypocentral partial derivatives are computed numerically, interpolating from the grid points at the corresponding focal depth and epicentral distance. Rays are also traced by following the travel time gradient back to the source at the surface in order to compute the velocity structure derivatives.

A joint hypocenter-structure inversion algorithm has been developed based on that described by Crosson (1976). Beginning with a starting model, perturbations ($\Delta m_i$) to the previous model $m_i$ are sought to minimize the travel time residual vector $d_i = T_i^{\text{pred}} - T_i^{\text{obs}}$. The normal equations to be solved are $A_{ij} \Delta m_i = d_i$. For the hypocentral model parameters, the components of $A$ are the partial derivatives of the predicted travel time for that event, assuming a flat earth:

$$T_x = \rho \cos(\phi)$$
$$T_y = \rho \sin(\phi)$$
$$T_z = \frac{\pm 1}{\rho s \sqrt{1 - (\rho v_s)^2}}$$
$$T_4 = 1$$

where $\rho$ is the ray parameter for a given source-station pair, $\phi$ is the source-station azimuth, and $v_s$ is the velocity at the source. The earth structure parameters, which are defined in terms of slowness are simply given by:

$$\frac{\partial T_i}{\partial s_i} = \frac{h_i}{\sqrt{1 - \rho^2 s_i^{-2}}}$$

where $s_i$ is the slowness ($v^{-1}$) in layer $i$, and $h_i$ is the thickness of layer $i$ traversed by the ray. Similar equations can be obtained for a spherical earth.

The resulting matrix $A$ for inverting $p$ events and $k$ layers is:

$$A = \begin{bmatrix}
    H_1 & 0 & \ldots & 0 & s_1 \\
    0 & H_2 & \ldots & 0 & s_2 \\
    \vdots & \vdots & \ddots & \vdots & \vdots \\
    0 & 0 & \ldots & H_p & s_p
\end{bmatrix}$$
where \( H_i \) is the hypocentral sub-matrix and \( S_i \) is the velocity structure sub-matrix for event \( i \):

\[
H_i = \begin{pmatrix}
T_{x,1} & T_{y,1} & T_{z,1} & T_{t,1} \\
T_{x,2} & T_{y,2} & T_{z,2} & T_{t,2} \\
\vdots & \vdots & \vdots & \vdots \\
T_{x,N_i} & T_{y,N_i} & T_{z,N_i} & T_{t,N_i}
\end{pmatrix}
\]

\[
S_i = \begin{pmatrix}
T_{s_{1,1}} & T_{s_{1,2}} & \ldots & T_{s_{1,N_i}} \\
T_{s_{2,1}} & T_{s_{2,2}} & \ldots & T_{s_{2,N_i}} \\
\vdots & \vdots & \ddots & \vdots \\
T_{s_{N_i,1}} & T_{s_{N_i,2}} & \ldots & T_{s_{N_i,N_i}}
\end{pmatrix}
\]

\( N_i \) is the number of observations for event \( i \).

In reality, each row of \( A \) and \( d \) is weighted according to the precision and quality (impulsive or emergent) of the arrival time report contributing to \( d \).

The equation \( A\Delta m = d \) is then solved for \( \Delta m \) by multiplying both sides by \( A^T \):

\[
A^T A \Delta m = A^T d
\]

\[
(A^T A)^{-1} A^T A \Delta m = (A^T A)^{-1} A^T d
\]

The matrix \( A^T A \) is a sparse matrix of doubly-bordered block-diagonal form. The inversion thus lends itself well to conjugate gradient techniques, such as that described by Press et al. (1986). Unfortunately, the matrix \( A^T A \) is often close to being singular, particularly since there are strong tradeoffs between the velocity in the source layer and the partial derivative with respect to depth. The near-singularity renders the matrix inversion unstable. To get around this problem, we decided to adopt the Sherman-Morrison inversion procedure (Press et al., 1986), in which the matrix inverse is found for the purely block-diagonal matrix, and then successively modified for each row and column making up the borders. Increasing the number of events thus results in an increase of only order \( N^2 \) for the inversion of the normal equations.

In the actual joint inversion algorithm, the model perturbations are computed from inversion using a starting model, and are then added to the starting model. The procedure continues until model perturbations are sufficiently small for a given iteration, or the improvement of the travel time residual vector is sufficiently small. At each iteration, both the travel time and ray parameter must be recomputed for all source-station pairs for the current structure. In order to solve the two-point problem for a large number of pairs, we use Vidale’s (1988)
algorithm for computing travel times everywhere within a grid using finite-difference. At each
iteration, this grid need be computed only once for a source at the surface; travel times and
ray parameters are then obtained from the grid point at the appropriate hypocentral depth and
epicentral distance.

The implementation of the algorithm comprises three programs:

hvnormeqn:
constructs the normal equations.
hvinvert:
invets for the solution, i.e., the model perturbations.
hvadjust:
adds the model perturbations to the previous model.

This separation of the inversion program from the others allows us to vary parameters
with each iteration, such as the damping added to the matrix $A^T A$, as well as to recover easily
from inversion failures due to non-convergence of the conjugate gradient method. The joint
inversion algorithm has been tested on synthetic cases and is now being applied to the ISC
arrivals.

3. DATA AND RESULTS

Hypocenters and arrivals have been obtained from International Seismological Center
(ISC) tapes for the years 1971-1982. They have been dearchived and reformatted for use by
software for earth-structure inversion. The travel time data actually used in this study consist
of those recorded at stations less than 1000 km (9°) away. The ISC locations (Figure 1) are
used as the initial guesses for hypocentral parameters. Events were selected carefully to
include close stations so that the tradeoff between depth, origin time and source layer velocity
could be resolved.

Several studies (e.g., Carter et al., 1991) indicate the crust to be very thick in this
region. Figure 2 shows reduced travel time residuals for events with ISC depths of 10-15 km.
The travel time curve for the Soviet GAR model (which has a mantle velocity of about 8.22
km/s) is superimposed. The match is fairly good at this depth, with the thick crust confirmed
by the large crustal-mantle phase crossover distance. Figure 3 shows the residuals for
events with ISC depths between 40 and 45 km. The deterioration at depth may indicate that
ISC depths are systematically overestimated due to the velocity model.
A starting model similar to the GAR model was used in the inversion. The mantle velocity was fixed at 8.2 km/s in order to stabilize the layer directly above. However, this velocity appears to be well constrained by the travel time slope from 400-1000 km (Figures 2-3). The crustal depth was fixed at 65 km. Figure 4 shows the results of the joint inversion. The resulting model is similar to the GAR model. The velocity gradient is slightly steeper in the upper crust. Below this is a 35-km thick lower crust of about 7 km/s, slightly lower than the GAR model velocity. The relocated depths are plotted against the ISC depths in Figure 5. As indicated in Figure 3, the relocated depths are generally less than the ISC depths.

4. CONCLUSIONS

A joint inversion algorithm for hypocenters and velocity structure has been developed based on the algorithm of Crosson (1976). Vidale's (1988) finite-difference travel time algorithm and the Sherman-Morrison inversion of sparse matrices have been used to speed execution for large numbers of events. A joint inversion for hypocenters and velocity structure in Central Asia yields a 1-dimensional model with a thick crust consisting a 30-km crust with a steep gradient and a roughly homogeneous 35-km lower crust of about 7 km/s. Focal depths appear to be systematically overestimated by the ISC. This model can be used as the starting model for a 2-dimensional tomographic inversion of a profile in central Asia.

5. ACKNOWLEDGES

This study was supported under Phillips Laboratory contracts F19628-90-C-0158. The views and conclusions contained in this paper are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of Hughes STX, Teledyne Inc., the U.S. Air Force or the U.S. Government.
6. REFERENCES


Figure 1. Index map showing the events used in the inversion, and station GAR.
Figure 2. Reduced travel times for events 10-15 km in the shaded region of Figure 1 with ISC depths of 10-15 km. (The inversion events in this depth range are a subset of this set). The predicted travel time curve for the Soviet GAR model reported by Carter et al. (1991) is superimposed.
Figure 3. Same as Figure 2 for a depth range of 40-45 km. The small reduced travel times for close stations suggests the ISC depths are systematically overestimated.
Figure 4. The final velocity model from the joint inversion is shown as the thick line. The Soviet model for station GAR (Carter et al., 1991) and K8 model (Given and Helmberger, 1980) for NW Eurasia are shown for comparison.
Figure 5. Hypocentral depths obtained from joint inversion plotted vs. those from the ISC. The inversion yields systematically shallower depths.
Section II

REGIONAL $L_g$ Q VARIATION IN IRANIAN PLATEAU AND ITS IMPLICATION FOR $m_b(L_g)$ DETERMINATION

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1. INTRODUCTION

An accurate characterization of the propagation of regional phases due to explosion sources in regions of high proliferation concern (such as Iran) requires fairly accurate crustal models. Iran lies on the Alpine-Himalayan seismo-tectonic belt, within a wide band of seismic activity connecting the Hindu Kush and eastern Mediterranean highly seismic regions. The Zagros Main Thrust Fault constitutes the boundary between the Iranian and Arabian Plates. Central Iran, northwest Iran, and the south Caspian areas have low levels of seismicity compared to those of the narrow belts surrounding them (McEvilly and Razani, 1971; Nowroozi, 1971, 1972, 1976; McKenzie, 1972; Dewey and Grantz, 1973; Hedayati et al., 1976; Chandra et al., 1979; Quintinmeyer and Jacob, 1979; Rowshandel et al., 1981; Ambrasseys and Melville, 1982; Jackson and McKenzie, 1984, 1988; and many others). This is regarded as a highly heterogeneous and complicated geological environment (Leith, 1992).

The seismic structure of the Iranian Plateau has been discussed in several studies. For instance, using travel time residuals derived from data recorded at WWSSN stations in Iran (MSH, SHI, TAB), Chen et al. (1980) inferred an uppermost mantle $P$-wave velocity of $8.0\pm0.1$ km/s for Iran. They also suggested that the crust dips toward the south-southeast at about $1^\circ$. Thus if the crustal thickness were 34 km in the north, it would reach about 49 km in the south. Kadinsky-Cade et al. (1981) also derived the average upper-mantle velocity beneath Iran with the same single-station method. Asudeh (1982) applied the two-station method to earthquakes along the interstation line, and he derived a $P$-wave velocity of $7.70\pm0.05$ km/s with a crust 43 km thick between southern Iran and the SRO station MAIO. This profile crosses the Tabas area. Asudeh (1982) also derived simple velocity profiles for several other regions with MAIO and ILPA (Iranian Long Period Array) data. Asudeh (1982) suggests that the crust to the north, east, and central parts of the Iranian Plateau is approximately 10 km thicker than at its western extreme. Roughly, the crust thickens from SSW to
NNE across the Zagros Main Thrust Fault, contrary to the assertion made by Chen et al. (1980). Wallace's (1991) over-simplified two-block model of Iran seems to support Asudeh's (1982) interpretation. A point that should be made here is that, although a few crustal models have been proposed during the past three decades, the requirement to identify small seismic events has raised a need to refine the available crustal models for more detailed and more accurate regionalized profiles based on newly available data sources and methodologies.

This study covers two topics. In the first part, we establish a regionalized $L_g Q$ map for Iranian Plateau with a 7-zone tomographic inversion. In the second part, we illustrate the importance of applying the 2-dimensional $L_g Q$ map to $m_b(L_g)$ calculation. The bias in $m_b(L_g)$ due to erroneous constant $Q$ model is quantified. Due to the preliminary nature of the result, however, it is not our intention to explain the cause of the regional variation of $L_g Q$ in Iranian Plateau. Mitchell and Hwang (1987) find that the variation of $L_g Q$ values between Appalachian and Rocky Mountains can easily be produced by accumulations of sandstone and shale of Mesozoic age and younger. By contrast, throughout most of the Western United States, neither the low $L_g Q$ values which have been observed nor the regional variation of those values can be explained by accumulation of low-$Q$ sediments. Mitchell and Hwang (1987) suggest that the explanation requires low and laterally varying values of $Q$ in the crystalline crust for Western United States. To explore the cause of the regional variation of $L_g Q$ in Iranian Plateau would require more data and further investigation.
2. NUTTLI’S Lg ATTENUATION MEASUREMENTS

Nuttli (1980) selected 99 Iranian earthquakes which occurred during 1972-1974. For these earthquakes, the body-wave magnitude, \( m_b \), varied from 3.7 to 6.0, with a median of 4.8, and the focal depth varied from 0 to 94 km, with a median of 43 km. Nuttli measured the \( \gamma \) of 109 paths recorded at three WWSSN [World Wide Standard Seismograph Network] stations in Iran: Mashad (MSH), Tabriz (TAB), and Shiraz (SHI). However, Nuttli (1980) did not tabulate the events he used. Instead of cross referencing the epicentral coordinates published in the *Bulletin of the International Seismological Centre*, we digitized Nuttli’s hand-drawn maps to retrieve his epicenters. Figure 1 shows the re-constructed 109 \( L_g \) paths.

Nuttli (1980) measured the “sustained maximum motion”, namely the amplitude equaled or exceeded by the three largest amplitude waves, of the vertical-component \( L_g \) waves with period around 1 second. A “normalized” amplitude, \( A' \), is defined as follows: the amplitude readings, \( A(\Delta) \) (in \( \mu m \)), are first corrected for the effects of geometrical spreading and dispersion with the formula appropriate for an Airy phase (cf. Ewing et al., 1957); then they are normalized according to Nuttli’s empirical scaling that an Iranian event with ISC \( m_b \) 5.0 would have a hypothetical \( L_g \) amplitude of 270 \( \mu m \) at 10-km distance. All events are thus “equalized” to magnitude 5.0:

\[
A'(\Delta) = A(\Delta) \cdot \Delta^{0.373} \cdot [\sin(\Delta/111.1)]^{0.5} \cdot 10^{3.6372 - \gamma ISC},
\]

If there is no anelastic attenuation or other scattering mechanism, the normalized amplitude, \( A'(\Delta) \), should be 1 at any distance, \( \Delta \). Otherwise, \( A'(\Delta) \) would be smaller than 1, and it is defined as \( \exp[-\gamma(\Delta-10)] \), where \( \gamma \) is the anelastic absorption coefficient. When the normalized amplitudes \( A'(\Delta) \) are plotted as a function of \( \Delta \) on a semi-logarithmic scale, the slope of the straight line connecting [10km, 0] and [\( \Delta \), \( \ln(A'(\Delta)) \)] would be exactly \(-\gamma\). Nuttli used this time-domain approach to determine the attenuation coefficient, \( \gamma \), of 109 paths in his study (cf. Figure 3 of Nuttli, 1980). The average \( \gamma \) of these 109 paths is 0.00442 \( \text{km}^{-1} \), very close to that of 0.0048 for coastal California derived by Herrmann (1980). Solid and dashed lines in Figure 1 represent those paths with \( \gamma \) smaller and larger, respectively, than the average.
Figure 1. 109 $L_g$ paths recorded at 3 WWSSN stations in Iran (MSH, TAB, and SHI) during 1972-1976 for which the attenuation parameter, $\gamma$, was readily measured by Nuttli (1980). Solid and dashed lines represent those with $\gamma$ value smaller and larger than the average (0.0044 km$^{-1}$), respectively.
3. TOMOGRAPHIC IMAGING METHOD

The datum for seismic tomographic imaging is the integral of some physical parameter along a specified path through the medium. For example, the travel time accumulated along a ray path between a source and a receiver can be expressed as the integrated slowness; the amplitude decay can be expressed as the integrated attenuation. The application of tomographic imaging to construct the 2-dimensional map of lateral heterogeneity in the crust is essentially the same as the method that has been widely used for decades in X-ray tomography or radioastronomy.

Suppose there are M seismic sources recorded at some or all of N stations, and suppose that these events and stations are spread over K seismotectonic regions. For coding and computational simplicity, the region boundaries were chosen on a $0.333^\circ$ by $0.333^\circ$ grid. Thus each "seismotectonic province" is composed of many square cells of size $0.333^\circ$ by $0.333^\circ$. We assume that the attenuation, $\gamma_k$, varies from one province (region) to another. The total path attenuation can be decomposed as the sum of the attenuation incurred in each region that the ray has traversed. That is,

$$\sum_{k=1}^{K} \gamma_k \Delta_k(i,j) = \gamma(i,j) \Delta(i,j), \text{ for } i=1,...,M; j=1,...,N$$

where $\gamma(i,j)$ is the path attenuation that Nuttli (1980) already measured, and $\Delta(i,j)$ is that epicentral distance from the $i$'th event to the $j$'th station. On the left-hand side, $\gamma_k$ is the (unknown) attenuation coefficient in the $k$'th region and $\Delta_k(i,j)$ is the distance traversed in the $k$'th region along the path from the $i$'th event to the $j$'th station. $\Delta_k(i,j)$ is computed as the sum of all segments of the great-circle path of the $(i,j)$'th ray that fall in a square cell comprising the $k$'th region. Thus $\Delta_k(i,j)$ would be 0 if the $(i,j)$'th ray does not cross any square cell of the $k$'th region. The determination of $\Delta_k(i,j)$ for $i=1,...,M; j=1,...,N$, is the crucial step of this linear tomographic imaging problem. Once the elements of matrix $[\Delta_k(i,j)]_{M \times N}$ are known, it is straightforward to solve for the unknown vector, $[\gamma_1, \gamma_2, ..., \gamma_K]$, with the standard least-squares techniques.
4. REGIONAL VARIATION OF Q IN IRANIAN PLATEAU

There have been different opinions regarding how Iranian Plateau should be partitioned in terms of the seismotectonic properties. Nowroozi (1976) presented 23 seismotectonic provinces for Iran based on 638 relocated earthquakes as well as 24 instrumentally located epicenters given by others. Berberian (1979) largely disagreed with the boundaries Nowroozi (1976) proposed, and he suggested that the only justifiable partitioning of the Iranian Plateau should be: [1] two Marginal Fold Belts of Zagros (in southwestern Iran) and Kopeh Dagh (in northeastern Iran) resting on the Arabian and Turan platforms, respectively; [2] the Central Iranian ranges and basins between them; and finally, [3] the post-colored melange-orhiolitic flysch belt of east and southeast Iran. Berberian's (1979) characterization of Iranian Plateau implies that some seismotectonic provinces in Nowroozi's (1976) map need to be merged.

If the ray paths sample each portion of the region of interest fairly well, then the tomographic imaging can be utilized to reveal the regional characteristics without the need to impose any specific a priori zoning. Thus the tomographic inversion technique can be used to test various hypotheses regarding the partitioning of Iran, whenever the data resolution permits. If, however, the data coverage is poor in a certain portion, as in the case of Nuttli's (1980) data set, then applying some regionalization based on the seismotectonic information is necessary and reasonable. Figure 2 shows a tentative regionalization which partitions Iran into 6 regions: Zagros Range, Lut Block, East Iran Range, Central Iran Range, Elburz/Caspian region, and Great Kavir/Esfahan/Rezaiyeh.

The tomographic imaging result with this partitioning is listed in Table 1. East Iran Range and western Afghanistan have the poorest ray coverage in Nuttli's data set, and hence the uncertainty in the associated Q estimate is high. For other regions, the standard error in the Q value is around 10%. Both the Zagros Range and the Lut Block show a large γ of 0.005 km⁻¹, roughly corresponding to a Q of 181±12 and 183±18, respectively. The Kopet Dagh, Shahrud Doruneh, and the Qom region also seem to have a Q slightly smaller than the average. On the other hand, the Elburz Province and central Iran have a Q of about 250 for 1 Hz Lg waves, which may be the highest Q value in Iran. Despite the large uncertainty in the Q value for the western Afghanistan area, the estimated Q of 201 is in agreement with Nuttli's (1981) earlier work in which he pointed out that Afghanistan, northern Pakistan, and northern India have crustal Q values comparable to those of Iran and the western United States.
Figure 2. A preliminary regionalization which partitions Iran into 6 seismotectonic regions: Zagros Range, Lut Block, Eastern Iran Range, Central Iran Range, Elburz/Caspian region, and Great Kävir/Esfahan/Rezaiyeh. Block inversion indicates that both the Zagros Range and the Lut Block show a large gy of 0.005 km⁻¹, roughly corresponding to a Q of 181+12 and 183+18, respectively. The Kopet Dagh, Shahrud Doruneh, and the Qom region also seem to have a Q slightly smaller than the average. The Elburz Province and central Iran have a Q of about 250 for 1 Hz tg waves, which may be the highest Q value in Iran.
Table 1. Regional γ and Q of 1 Hz $L_g$ in Iran

<table>
<thead>
<tr>
<th>Region</th>
<th>$\gamma$ (1/Km)</th>
<th>$Q_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Central Iran Plateau</td>
<td>0.0037±0.0006</td>
<td>246±38</td>
</tr>
<tr>
<td>Elburz + Caspian</td>
<td>0.0035±0.0004</td>
<td>257±26</td>
</tr>
<tr>
<td>East Iran Range</td>
<td>0.0038±0.0013</td>
<td>248±91</td>
</tr>
<tr>
<td>Western Afghanistan</td>
<td>0.0045±0.0025</td>
<td>201±112</td>
</tr>
<tr>
<td>Great Kavir + Esfahan + Rezaiyeh</td>
<td>0.0043±0.0003</td>
<td>209±6</td>
</tr>
<tr>
<td>Zagros Range</td>
<td>0.0049±0.0003</td>
<td>181±12</td>
</tr>
<tr>
<td>Lut Block</td>
<td>0.0049±0.0005</td>
<td>183±18</td>
</tr>
</tbody>
</table>

Table 2. Crustal Q Results of Various Regions*

<table>
<thead>
<tr>
<th>Author</th>
<th>$Q_0$ $f^*$</th>
<th>Geometrical Spreading + Dispersion</th>
<th>$f$ (Hz)</th>
<th>Region</th>
<th>Method and Distance Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nuttli (1973)</td>
<td>1500</td>
<td>$\Delta^{-5/6}$</td>
<td>1</td>
<td>ENA</td>
<td>time domain amplitudes</td>
</tr>
<tr>
<td>Street (1976)</td>
<td>900</td>
<td>$\Delta^{-5/6}$</td>
<td>1</td>
<td>US &amp; Canada E of Rockies</td>
<td>time domain amplitudes $\Delta = 200-4500$ km</td>
</tr>
<tr>
<td>Horner et al. (1978)</td>
<td>1500</td>
<td>$\Delta^{-5/6}$</td>
<td>1</td>
<td>Canadian shield</td>
<td>time domain amplitudes $\Delta = 300-7000$ km</td>
</tr>
<tr>
<td>Herrmann (1980)</td>
<td>229</td>
<td></td>
<td>1</td>
<td>Berkeley, CA</td>
<td></td>
</tr>
<tr>
<td>Mechler et al. (1980)</td>
<td>400 $f^{0.44}$</td>
<td>$\Delta^{-5/6}$</td>
<td>0.5-8</td>
<td>France $\Delta = 350-1100$ km</td>
<td>time domain max amps bandpass filtered data,</td>
</tr>
<tr>
<td>Mitchell (1981)</td>
<td>-900 $f^{0.2}$</td>
<td></td>
<td>0.25-1</td>
<td>ENA $\Delta = 500-2000$ km</td>
<td>theoretical modeling of spectral shape</td>
</tr>
<tr>
<td>Nuttli (1981)</td>
<td>800 $f^{0.5}$</td>
<td></td>
<td>-1-5</td>
<td>ENA CUS</td>
<td>$\Delta \leq 1000$ km</td>
</tr>
<tr>
<td>1500 $f^{0.2}$</td>
<td>-1-5</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nuttli (1981)</td>
<td>200 $f^{0.7}$</td>
<td></td>
<td>-1-5</td>
<td>S. Calif.</td>
<td>Lg coda, $\Delta \leq 1000$ km</td>
</tr>
<tr>
<td>Dwyer et al. (1983)</td>
<td>1230 $f^{0.4}$</td>
<td>$\Delta^{-5/6}$</td>
<td>1-10</td>
<td>Central US</td>
<td>time domain max amps from bandpass filtered data, $\Delta = 200-2000$ km</td>
</tr>
</tbody>
</table>

* Partially adapted from Goncz et al. (1987).
Table 2. Crustal Q Results of Various Regions* (Continued)

<table>
<thead>
<tr>
<th>Author</th>
<th>$Q_0$</th>
<th>$\kappa$</th>
<th>Geometrical Spreading + Dispersion</th>
<th>$f$ (Hz)</th>
<th>Region</th>
<th>Method and Distance Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Singh &amp; Herrmann (1983)</td>
<td>900 f 0.35</td>
<td>&quot;</td>
<td>$\Delta^{-5/6}$</td>
<td>0.5-3.5</td>
<td>NENA</td>
<td>Lg coda, 300-800 km</td>
</tr>
<tr>
<td></td>
<td>1000 f 0.1</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
</tr>
<tr>
<td></td>
<td>1200 f 0.2</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
</tr>
<tr>
<td></td>
<td>900 f 0.25</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
</tr>
<tr>
<td>Pulli (1984)</td>
<td>660 f 0.4</td>
<td>&quot;</td>
<td>0.75-10</td>
<td></td>
<td>NENA</td>
<td>coda amps, ~ 50-600 km</td>
</tr>
<tr>
<td>Chen et al. (1984)</td>
<td>(400–500) f 0.0</td>
<td>(120–200) f 0.2</td>
<td>&quot;</td>
<td>−1</td>
<td>Beijing area</td>
<td>coda amps,</td>
</tr>
<tr>
<td>Raoof &amp; Nuttli (1985)</td>
<td>(130–350) f (0.4–0.7)</td>
<td>(420–580) f (0.2–0.3)</td>
<td>&quot;</td>
<td>0.4-1.4</td>
<td>Andes</td>
<td>coda amps,</td>
</tr>
<tr>
<td>&quot;</td>
<td>(580–980) f (0.0–0.2)</td>
<td>&quot;</td>
<td>&quot;</td>
<td>&quot;</td>
<td>Patagonian</td>
<td>&quot;</td>
</tr>
<tr>
<td>Hasegawa (1985)</td>
<td>900 f 0.2</td>
<td>&quot;</td>
<td>$\Delta^{-1/2}$</td>
<td>0.6-20</td>
<td>Canadian shield</td>
<td>spectra of ground accel, $\Delta = 70-900$ km</td>
</tr>
<tr>
<td>Shin (1985)</td>
<td>(500±50) f (0.6–0.7)</td>
<td>(500±50) f (0.6–0.7)</td>
<td>$\Delta^{-5/6}$</td>
<td>1-10</td>
<td>Eastern Canada</td>
<td>time domain max amps freq domain amp spectra $\Delta = 100-1000$ km</td>
</tr>
<tr>
<td>Campillo et al. (1985)</td>
<td>290 f 0.52</td>
<td>&quot;</td>
<td>$\Delta^{-5/6}$</td>
<td>0.5-10</td>
<td>France</td>
<td>time domain max amps &amp; theoretical modeling</td>
</tr>
<tr>
<td>Chavez &amp; Priestley (1986)</td>
<td>206 f 0.68</td>
<td>&quot;</td>
<td>$\Delta^{-1/2}$</td>
<td>0.3-10</td>
<td>US Great Basin explosions</td>
<td>frequency domain amps $\Delta = 200-500$ km</td>
</tr>
<tr>
<td>&quot;</td>
<td>214(±50) f 0.54±0.09</td>
<td>&quot;</td>
<td>&quot;</td>
<td>0.3-5</td>
<td>US Great Basin earthquakes</td>
<td>&quot;</td>
</tr>
<tr>
<td>Gupta &amp; McLaughlin (1987)</td>
<td>800 f 0.32</td>
<td>400 at 1 Hz</td>
<td>$\Delta^{-5/6}$</td>
<td>0.5-7</td>
<td>EUS</td>
<td>amplitudes from PSRV $\Delta &lt; 1100$ km</td>
</tr>
<tr>
<td>&quot;</td>
<td>1100 at 1 Hz</td>
<td>1400 at 1 Hz</td>
<td>&quot;</td>
<td>1</td>
<td>CUS</td>
<td>&quot;</td>
</tr>
<tr>
<td>Goncz et al. (1987)</td>
<td>1000 f 0.35</td>
<td>&quot;</td>
<td>$\Delta^{-5/6}$</td>
<td>0.5-13</td>
<td>Central &amp; ENA</td>
<td>time domain max amps $\Delta = 500-3000$ km</td>
</tr>
<tr>
<td>Chun et al. (1987)</td>
<td>1100 f 0.19</td>
<td>&quot;</td>
<td>$\Delta^{-1/2}$</td>
<td>0.6-10</td>
<td>Eastern Canada</td>
<td>spectral ratios $\Delta = 53-210$ km</td>
</tr>
<tr>
<td>Xie &amp; Mitchell (1990)</td>
<td>low</td>
<td>&quot;</td>
<td>$\Delta^{-5/6}$</td>
<td></td>
<td>E. Africa Rift</td>
<td></td>
</tr>
<tr>
<td>Chun et al. (1992)</td>
<td>564(±53) f 0.49±0.06</td>
<td>283(±15) f 0.72±0.02</td>
<td>$\Delta^{-5/6}$</td>
<td>0.1-1.0</td>
<td>Asia</td>
<td>CDSN + IRIS $\Delta \leq 1000$ km</td>
</tr>
</tbody>
</table>

*) Partially adapted from Goncz et al. (1987).
5. IMPLICATION FOR SEISMIC MONITORING

Attenuation of short-period $L_g$-wave motions is of concern for a number of seismological problems. For engineering purposes, $L_g$ is often the wave group responsible for the largest and most prolonged ground motion observed on accelerograms, and hence it determines the "design motion" at a site. For seismicity studies, $L_g$ amplitudes can be used to estimate 1-Hz $m_b$ values for small earthquakes for which the $P$ wave cannot be seen at teleseismic distances (Nuttli, 1973). For discrimination between earthquakes and explosions at regional distances, the ratio of $L_g$ to $P$ amplitudes has been investigated in many studies (e.g., Blandford, 1981; Lynnes et al., 1990; Lynnes and Baumstark, 1991).

For the purpose of calculating $m_b(L_g)$ in Iran, Nuttli’s original $L_g$ formula can be rewritten in an equivalent form:

$$m_b(L_g) = 3.6372 + \log A(\Delta) + \frac{1}{3} \log(\Delta) + \frac{1}{2} \log \left[ \sin \left( \frac{\Delta(km)}{111.1(km/deg)} \right) \right] + \frac{\gamma}{\ln(10)} \left( \frac{\Delta-10(km)}{10} \right),$$  \[3\]

where $\gamma = \frac{\pi}{Q \cdot U \cdot T}$, $Q(f) = Q_0 \cdot f^k$.

$\Delta$ is the epicentral distance in km, $A(\Delta)$ is the observed $L_g$ amplitude measured in the time domain in $\mu$m [microns] at the epicentral distance of $\Delta$ km. For instance, a seismic source in Iran with 1-sec $L_g$ amplitude of 270 $\mu$m at 10 km epicentral distance would correspond to a $m_b(L_g)$ of $3.6372 + 2.4314 + 0.3333 - 1.4019 + 0.0000 = 5.000$, same as what Nuttli’s (1986) formula would give. Nuttli’s (1986) later study of $L_g$ suggested that a different constant of 4.0272 is required for Eastern North America and Central Asia regions (Jih, 1992). The bias of 0.39 m.u. could reflect the difference in $L_g$ excitation relative to $m_b$ (ISC) between Eastern U.S. (or Central Asia) and Iran. Alternatively, it could reflect the $m_b$ bias between these two areas. This issue will be discussed later.

Once the regionalized $\gamma$ map is available, an individual path $\gamma$ for an arbitrary source-station pair can simply be computed as the weighted sum of the $\gamma_k$'s of the subregions that the ray path traverses:

$$\gamma = \sum_{k=1}^{K} \gamma_k \cdot \frac{A_k}{A},$$  \[4\]

It is clear from [3] that an erroneous path $\gamma$ would yield a $m_b(L_g)$ bias which increases with the distance. Furthermore, this error is independent of the actual source size or the quality of the amplitude measured at the recording station. It is the bias solely due to inaccurate calibration of the propagation effect.
Figure 3 shows the spatial pattern of apparent $m_b(L_Q)$ corrections that would be needed at WWSSN station SHI and IRIS station ASH (Ashkhabad), respectively, if a constant $\gamma$ of 0.0044 km$^{-1}$ (viz., the average $\gamma$ across Iran) was assumed in computing $m_b(L_Q)$ at these two stations. For each hypothetical epicenter, the $m_b(L_Q)$ correction required is independent of the amplitude actually observed (cf. Equation [3]).

Partitioning Iran into 21 regions as proposed by Nowroozi (1976) (Figure 4) in our block inversion would yield more prominent spatial variations in the resulting $Q$ map (Figure 5), and hence a stronger variation in $m_b(L_g)$ residual as well. The regional variation of the anelastic attenuation parameter in Figure 5 is significant enough that it needs to be taken into account in calibrating each monitoring station for a reliable magnitude scale in monitoring possible clandestine tests from a vast area. Unless this has been done, adding more stations/arrays to the monitoring network may not provide substantial improvement in reducing the error in the network-averaged magnitude based on regional phases. In fact, since the bias increases with distance, the bias in $m_b(L_g)$ would be much smaller if the magnitude were based on the nearest station alone (as compared to using a network of sparse stations for simple averaging). Figure 6 shows the spatial pattern of apparent $m_b(L_g)$ corrections as a function of hypothetical hypocenters that would be needed for a network of 3 stations (SHI, TAB, and MSH) if a constant $\gamma$ of 0.0044 km$^{-1}$ were assumed in computing $m_b(L_g)$ at these three stations. The residuals are determined with respect to 7- (top) and 21-zone (bottom) tomographic inversions, respectively. Note that magnitudes based on the network average is not necessarily better than those based on the nearest station alone, if the path attenuation is not carefully accounted for. This should be obvious by comparing Figures 3 and 6.
Figure 3. The spatial pattern of apparent $m_b(L_g)$ corrections as a function of hypothetical hypocenters that would be needed at WWSSN station SHI (top) and IRIS station ASH (bottom) if a constant $y$ of 0.0044 km$^{-1}$ (viz, the average $y$ across Iran) were assumed in computing $m_b(L_g)$ at these two stations.
Figure 4. A more detailed partitioning of Iran as proposed by Nowrooz (1976) which partitions Iran into 21 regions.
Partitioning Iran into 21 regions as proposed by Nowroozi (1976) in our block inversion would yield more prominent spatial variations in the resulting $O$ map as well as a more complicated pattern of $m_b(L_3)$ residual.
Figure 6. The spatial pattern of apparent $m_b(L_g)$ corrections as a function of hypothetical hypocenters that would be needed for a network of 3 stations (SHI, TAB, and MSH) if a constant $\gamma$ of 0.0044 km$^{-1}$ were assumed in computing $m_b(L_g)$ at these three stations. Top and bottom show the results of 7- and 21-zone tomographic inversion, respectively. Magnitude based on the network average is not necessarily better than that based on the nearest station alone, if the path attenuation is not carefully accounted for.
Figure 7. The seismicity map of Iranian Plateau showing all events with $m_b > 4$. 
6. CONCLUSION

Although the whole Iranian Plateau can be briefly described as a region of very low $Q$, applying a simple averaged attenuation coefficient ($Q$) for the whole plateau would be inappropriate for measuring $m_b(L_g)$. The regional variation of the anelastic attenuation parameter is significant enough that it needs to be taken into account in calibrating each monitoring station for a reliable magnitude scale in monitoring possible clandestine tests from a vast area. Unless this has been done, adding more stations/arrays to the monitoring network may not provide substantial improvement in reducing the error in the network-averaged magnitude based on regional phases. In fact, since the bias increases with distance, the bias in $m_b(L_g)$ would be much smaller if the magnitude were based on the nearest station alone (as compared to using a network of sparse stations for simple averaging). This situation may be very different from that of monitoring a specific nuclear test site for which the empirical site-dependent correction can be applied afterwards to the station magnitudes even when the path $Q$s are not fully known beforehand. For instance, Jih (1992) recently demonstrated a joint inversion procedure which can determine the $L_g$-based explosion size estimate as well as the path attenuation coefficient simultaneously. Such a technique would be most useful for calibrating the regions where underground nuclear tests or other man-made seismic events frequently take place. For regions like Iran where relatively very little is known about what the explosion signature should look like, however, a regionalized $\gamma$ map (e.g., Singh and Herrmann, 1983, for North America; and that in Kadinsky-Cade et al., 1982, for $S_n$) for each crustal phase of interest should be established and applied to the routine magnitude computation procedure.

7. RECOMMENDATIONS

Nuttli (1980) suggested that a seismic source in Iran with the ISC bulletin $m_b$ 5.0 should excite $L_g$ amplitude of 270 microns at a 10-km extrapolated distance, whereas the seismic sources in Central Asia and eastern North America with comparable ISC bulletin $m_b$ would excite a $L_g$ amplitude of 110–150 microns (Nuttli, 1986). Possible explanations for this apparent bias of 0.26–0.39 m.u. include [1] uncertainty in the ISC bulletin $m_b$ values (Nuttli, 1981), [2] differences in $L_g$ excitation relative to $m_b$, or [3] differences in the upper mantle property which could cause a bias in $m_b$. Many $L_g$ studies have used the ISC $m_b$ for “normalizing” their $L_g$ magnitude scale (e.g., page 2146 of Nuttli, 1986a; page 128 of Israelson, 1992). Without careful re-processing, the ISC bulletin $m_b$ values typically would be associated with large uncertainty. Therefore, it is very important to adopt a better $m_b$ in calibrating
the crustal phases in Iran (or any other area of proliferation concern) in the first place. Magnitudes based on the short-period teleseismic recordings corrected for the station amplifications as well as the path effects (due to the focusing/defocusing near the source region etc.) such as those in Jih and Wagner (1992ab) may better serve such a purpose.

Wallace (1991) reports that the central Iran region has more efficient $L_g$ propagation than the surrounding area, qualitatively in agreement with our result in Table 1. Many previous studies (e.g., Ruzaikan et al., 1977; Kadinsky-Cade et al., 1981; Ni and Barazangi, 1982; Pomeroy et al., 1982; Wallace, 1991) have pointed out that $L_g$, $S_n$, and $P_n$ do not necessarily have the same propagation characteristics. For instance, the inefficient $S_n$ propagation beneath the northern Iranian Plateau identified by Kadinsky-Cade et al. (1981) seems to permit efficient $L_g$ propagation (Figure 6). The spectral and phase discrimination methodologies should take this into account. A regionalized $\gamma$ map (e.g., Figure 5 for $L_g$ in Iran; the map derived by Singh and Herrmann, 1983, for North America; and that in Kadinsky-Cade et al., 1982, for $S_n$) for each crustal phase of interest should be established and applied to the routine magnitude computation procedure such as the one in the knowledge-based automatic processing system (Bratt et al., 1991).

Fault-plane solutions for many suitably located earthquakes in the Middle East have been determined by McKenzie (1972) and Jackson and McKenzie (1984). We recommend assembling events recorded at regional as well as at teleseismic distances according to the clustering of earthquakes with similar focal mechanism. Preferably for each crustal phase at least 10 events in each clustered area (cf. Figure 7) should be measured. The redundancy of data in each group will provide better constraints for inferring the empirical station and region-specific path corrections (Jih and Wagner, 1992ab; Jih, 1992), and it will thereby result in more precise magnitude scales for both regional and teleseismic phases. The determination of seismic magnitudes for events occurring in isolated suspected spots will also benefit from this exercise significantly, since more accurate station corrections will be available. Although several crustal models of the Middle East have been suggested during the past three decades, the task of identifying small seismic events requires a refinement of the available models for more detailed and more accurate regionalized profiles. Consequently, more tomographic inversions of the Middle East would be very useful.

To be more specific, we recommend first to assemble broadband digital data of recent seismic events of Iran (and Iraq) recorded at IRIS stations/arrays (ASH, KIV, and GNI) and then to complement this data set with digital data of MAIO (SRO) and analog recordings of historical events recorded at WWSSN and other former Soviet stations nearby. We suggest
that phase parameters of $L_g$, Rayleigh waves, and other regional phases be measured, and then inverted for the regionalized anelastic attenuation coefficients as well as for the crustal structures of Iran (and Iraq). Our preliminary result along these lines as presented in this study can be improved further by using an enlarged data set along with a more carefully defined seismotectonic map. We recommend that the $m_b$ (of relatively larger events) and $m_b(L_g)$ be determined with two simultaneous inversion procedures which have been tested with Soviet events (Jih and Wagner, 1992ab; Jih, 1992). The resulting refined $m_b$ values should then be applied to normalize the regional and local magnitudes of Iranian events. More detailed phase discrimination studies, such as those in Lynnes and Baumstark (1991) and Lynnes et al. (1990), should be conducted for the Iranian region with the improved phase parameters to be obtained in the manner we suggest.

8. ACKNOWLEDGEMENTS

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SECTION III

PROJECT OVERVIEW

STUDIES OF SEISMIC WAVE PROPAGATION IN EURASIA

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2. MOST IMPORTANT SCIENTIFIC RESULTS

Under this Air Force-funded contract, we have been conducting both theoretical and observational studies covering a wide spectrum of topics directly related to monitoring the compliance of both the Threshold Test Ban Treaty [TTBT] and the Non-Proliferation Treaty [NPT]. Each of the following paragraphs summarizes a paper that has been or will be presented/published. The investigator who performed the specific task is also identified.

2.1 ISC Travel Time Inversion in the Garm Region, Central Asia¹ (Lynnes)

The propagation of regional phases is still problematic: amplitudes and even the observability of phases can be highly variable. This has important implications for the application and efficacy of earthquake/explosion discriminants and event size estimation. At least some of this variation is likely due to the effects of lateral heterogeneity, particularly in the waveguides and near the boundaries along which regional phases such as \( P_g \), \( P_n \), \( S_n \), and \( L_g \) propagate. The effects of lateral heterogeneity on regional phase propagation can be modeled using finite-difference methods.

In order to employ these methods, a realistic velocity model is required. Block inversion of travel times is a well-established technique for deriving laterally heterogeneous velocity structures. In order to simplify the problem and improve ray coverage, a two-dimensional geometry is sought: the high seismicity rate along the great circle arc between the IRIS station GAR and and the CDSN station WMQ provides such an opportunity. Travel times for regional phases are used to derive a spherically symmetric structure for the crust and upper mantle in this region. This model is then starting model for a two-dimensional velocity inversion in the vertical plane.

¹Reported in Semi-annual R&D Status Reports #1 and #2 dated 14 February and 19 August, 1991, respectively. See also Section I of this report.
2.2 Path Effects on Body-wave Amplitudes of Novaya Zemlya Explosions\(^2\) (Jih)

The standard procedure used in estimating the source size of underground nuclear explosions using \(m_b\) measurements has been to separate the station terms from the network-averaged source terms. The station terms thus derived actually reflect the combination of the path effect and the station effect, when only those events in a close proximity are utilized. If worldwide explosions are used in the inversion, then the path effect tends to be averaged out at each station. In either case, the effect due to the propagation path alone would not be obvious.

The major research goal of this contract is to improve our fundamental understanding of the seismic wave propagation in Eurasia. To achieve this goal, we further decompose the station amplification effect with a joint inversion scheme that simultaneously determines the seismic source size, the path terms, and the receiver terms. Short-period \(P\)-wave amplitudes of 217 worldwide underground nuclear explosions, including 28 blasts from Novaya Zemlya, recorded at 118 WWSSN stations have been used in one single inversion to isolate the propagation complexities affecting the \(P\)-wave amplitudes. For all 28 Novaya Zemlya events in our WWSSN database, the new \(m_b\) factoring procedure provides more stable \(m_b\) measurements across the whole recording network with a reduction in the fluctuational variation by a factor of up to 3. A typical reduction factor in the variation is about 2.0, and the the worst case is 1.4.

The inferred path terms are then compared against the travel-time residuals to characterize the propagation paths. Our result indicates that paths from the northern test site in Novaya Zemlya to stations in North America have systematically faster arrivals and smaller amplitudes, suggesting a profound defocusing effect on the first arrivals; while stations in Ireland, Scotland, Spain, Bangladesh, northern India, Pakistan, Korea, and Kenya report slow arrivals and large amplitudes, suggesting a focusing effect. Amplitudes for paths to Greenland, Iceland, Alaska, Turkey, Germany, Luzon, Zimbabwe, Italy, Puerto Rico, Ethiopia, and Hawaii, however, seem to be controlled by the anelastic attenuation with slow rays also associated with small amplitudes, and fast rays associated with large amplitudes. A strong correlation between \(P\)-wave amplitude and \(L_2\) detection at teleseismic distance is also observed.

2.3 Yield Estimates of Novaya Zemlya Explosions: Preliminary Result\(^3\) (Jih)

As a byproduct of the study described in Section 2.2, we have derived the yield estimates of Novaya Zemlya explosions based on the path-corrected \(m_b\) values. Assuming the basic coupling and the mantle condition at Novaya Zemlya are comparable to those at Eastern Kazakhstan, the \(m_b\) bias relative to NTS at 50 KT level using the path-corrected \(m_b(P_{\text{max}})\) values is inferred as 0.25 and 0.36 magnitude unit for Novaya Zemlya and Semipalatinsk, respectively. The \(m_b(P_{\text{max}})\) bias of 0.11 between Semipalatinsk and Novaya Zemlya could be largely due to the difference in \(pP\) interference between these two test sites (rather than the seismic coupling). The relative source size determined by Burger et al. (1986) and the theoretical \(\log(T-\text{yield})\) scaling are combined to extrapolate our \(m_b\) scaling to the higher end. The resulting yield estimates of Novaya Zemlya explosions range from 2 to 2100 KT, with peak values at 550 KT and 65 KT for events before and after 1976, respectively, which are in reasonable agreement with those in previous studies.

Also included in the Annual Scientific Report No. 1 is a complete listing of path-corrected \(m_b\) values and yield estimates of Semipalatinsk explosions which are used as our baseline in calibrating Novaya Zemlya explosions. First motion of the initial short-period \(P\) waves appears to be a very favorable source measure for explosions fired in hard rock sites underlain by the stable mantle (such as Semipalatinsk).

2.4 Regional \(Lg\) Q Variation In the Iranian Plateau Revisited\(^4\) (Jih)

We examined a general procedure which incorporates the independently-derived information of localized path effects into the magnitude determination. The goal of this exercise is to quantify the bias in the seismic magnitude (such as \(m_b(L_g)\)) that would be inherent in a scheme without fully coupling the regional propagational characteristics into the magnitude determination procedure. Iran was chosen as a test case in this study because of the growing nuclear proliferation concern in the Middle East.

A tentative zoning partitioning Iranian Plateau into six regions (viz., the Zagros Range, the Lut Block, East Iran Range, Central Iran Range, the Elburz/Caspian area, and the Great Kavir/Esfahan/Rezaiyeh region) has been used in our block inversion to reveal the spatial pattern of the \(L_g\) attenuation parameter, \(Q\). We used 109 observations recorded at 3 WWSSN stations in Iran (MSH, TAB, and SHI) for which the \(\gamma\) was readily measured by Nuttli

\(^3\)Reported in Semi annual R&D Status Report #3 dated 16 February, 1992, and Scientific Report #1, PL-TR-92 2042
\(^4\)Reported in Semi annual R&D Status Report #4 dated 14 August, 1992. See also Section II of this report.
(1980). The weighted average \( \gamma \) of these paths is 0.0044 km\(^{-1}\), very close to the 0.0048 for coastal California derived by Herrmann (1980). It is also in agreement with the \( L_g \) coda \( Q \) map recently compiled by Xie and Mitchell (1992) for Eurasia. In our inversion with a more detailed regionalization, both the Zagros Range and the Lut Block show a large \( \gamma \) of 0.005 km\(^{-1}\), roughly corresponding to a \( Q \) of 181±12 and 183±18, respectively. The Kopet Dagh, Shahrud Doruneh, and the Qom region also seem to have a \( Q \) slightly smaller than the average. On the other hand, the Elburz Province and central Iran have a \( Q \) of about 250 for 1 Hz \( L_g \) waves, which could be the highest \( Q \) value in Iran.

Although the whole Iranian Plateau can be briefly described as a region of very low \( Q \), applying a simple averaged attenuation coefficient \( (Q) \) for the whole plateau would be inappropriate. The regional variation of the anelastic attenuation parameter is significant enough that it must be taken into account in calibrating each monitoring station for a reliable magnitude scale in monitoring possible clandestine tests from a vast area. Unless this has been done, adding more stations/arrays to the monitoring network may not provide substantial improvement in reducing the error in the network-averaged magnitude based on regional phases. In fact, the bias in \( m_b(L_g) \) would be much smaller if the magnitude was solely based on the nearest station alone (as compared to using a network of sparse stations for simple averaging). This situation is very different from that of monitoring a specific nuclear test site for which the empirical site-dependent correction term can be applied afterwards to the station magnitudes even when the path \( Qs \) are not fully known in advance.

2.5 Theoretical Investigation of Ripple-fired Explosions\(^{5}\) (Jih)

A major issue for the Non-Proliferation Treaty is the discrimination of large chemical explosions from possible clandestine or small nuclear tests. Unless discrimination is possible, the numerous mining blasts could give ample opportunity for concealing clandestine tests. Rippled-fired explosions are commonly used for fragmenting rocks during quarry and open-pit mining. The periodicity inherent in the ripple firing could produce a seismic reinforcement at the frequency of the delay between shots or rows. Since ripple firing is essentially a sequence of single explosions arranged and fired using a series of time-delayed detonations between adjacent shot holes or rows of shot holes, it has been suggested that the convolution of a single explosion with a comb function of variable spacing and variable amplitude can be used to study the distinctive signature of ripple firing (Stump, 1988; Smith, 1989). Baumgardt and Ziegler (1988) delicately demonstrated that the incoherent array-stack spectra can be

\(^{5}\)Reported in Semi annual R&D Status Report #4 dated 14 August 1992
used to identify some multiple shots recorded at NORSAR. By superpositioning the waveform due to a single shot with proper time delay, they were able to model the source multiplicity under the assumption that the spatial spreading of the shots are negligible with respect to the traveling distance.

There are, however, wave excitation characteristics of ripple-fired explosions which are not predicted by such spectral or waveform superposition approaches. Figure 1 of our 4th semi-annual R&D status report shows the vertical component of the displacement wave field of 7 ripple-fired explosions detonated with a *rupture velocity* of 2.5 km/s in a granitic half space. Neithe $R_g$ nor the $S^*$ was emitted in the single explosion case using the same shot depth. However, a very clear $R_g$ is excited in the forward direction for the ripple firing. In fact, one of the standard industrial practices in reducing potential damage caused by ground vibration is to detonate ripple shots in a direction away from the buildings (Dick *et al.*, 1983). An immediate implication of this exercise on the discrimination problem is that the lack of $R_g$ is not necessarily indicative of deep sources. Furthermore, although path effects such as anelastic attenuation and scattering by shallow heterogeneity and topography in the upper crust can reduce $R_g$ significantly as demonstrated by Jih *et al.* (1988) and McLaughlin and Jih (1986, 1987), the reported lack of $R_g$ in many seismograms from known quarry blasts could also be due to the intrinsic source effect (such as the shooting pattern) rather than the path effects.

Several previous theoretical studies with spectral superposition approach (*e.g.*, Smith, 1989; Greenhalgh, 1980) suggest that for ripple firings with simple configurations, the spectrum will be reinforced at every $1/\Delta t$ Hz, where the $\Delta t$ is the delay time between the shots. However, our numerical experiments indicate that even with a very simple linearly distributed shot array in the half space, the frequencies at which the amplitude reinforcement could occur also depend on the relative azimuth angle and take-off angle with respect to the rupture direction. Figure 2 of our 4th semi-annual R&D status report gives the spectral ratios of $P$-wave synthetics to that due to a single explosion. It is clear that reinforcement does occur at exactly every 50 Hz along the orthogonal direction, consistent with Smith’s prediction (1987, 1989). For other directions, however, the frequency at which the enhancement would occur is clearly off due to the *Doppler Effect*. This phenomenon suggests that the shift of the spectral reinforcement, whenever observable, could be used as a simple discriminant between multiple explosions and a single shot. It could also provide an alternative explanation of why the spectral reinforcement was not observed at the expected frequency at RSON for the mining blast C detonated at Mesabi Range, August 6 1986 (Smith, 1989). Kim *et al.* (1991) report that
seismograms from the same quarry recorded at the same station could have distinct spectral characteristics. They attribute this phenomenon to the considerable fluctuation in delay times and sub-charge sizes. The numerical modeling study we conducted provides another possible explanation, however.

2.6 Lop Nor Explosion of 21 May 1992 as Observed at ANP (Anpu, WWSSN), Taiwan (Jih)

The "megaton"-level explosion detonated on 21 May 1992 at the test site between Lop Nor and Bosten Lake, Xinjiang, is believed to be the largest Chinese underground nuclear test conducted so far. The raw body-wave magnitudes (viz., log(A/T) + B(A)) measured at WWSSN station ANP (Anpu, 121.517°E, 25.183°N, Δ=3523km) are 5.72, 6.17, and 6.43, based on the first motion (zero-to-peak or \( P_a \)), the "b" phase (first peak-to-first trough or \( P_b \)), and the largest peak-to-peak (\( P_{\text{max}} \)) amplitudes, respectively. Applying the empirical station correction of 0.143 magnitude unit [m.u.] along with the path correction of -0.045 m.u. derived by Jih and Wagner (1992a) to bring the station recordings at ANP in alignment with the optimal worldwide network average, the final station \( m_b \) values at ANP are set at 5.82 (\( P_a \)), 6.27 (\( P_b \)), and 6.52 (\( P_{\text{max}} \)), respectively. Since there is no evidence of a low velocity zone [LVZ] in the area of eastern Tien Shan Mountains or the test site (Matzko, 1992), it would seem reasonable that the upper-mantle conditions at Lop Nor test site are very similar to those at Eastern Kazakh where the major nuclear test sites of the former Soviet Union are located. As a result, the magnitude-yield calibration curve derived from the \( P_a \) phases of Eastern Kazakh explosions (cf. Jih and Wagner, 1992a,b) could be adequate for Lop Nor explosions as well. The calibration curves for \( P_b \) and \( P_{\text{max}} \) phases can then be inferred from the empirical \( P_b \cdot P_a \) and \( P_{\text{max}} \cdot P_a \) regressions, respectively. Under the assumption that the source coupling as well as the anelastic attenuation at Lop Nor test site are comparable to those at Eastern Kazakh, and further that the corner-frequency effect is negligible, the yield of 21 May 1992 explosion is estimated as 350 KT based on the \( m_b \) values measured at ANP alone. If we assume that Lop Nor area has a \( t^* \) intermediate between those at Nevada test site (U.S.A.) and Eastern Kazakh, then our yield estimate would become 550 KT instead. This seems, however, very unlikely as the alternative assumption lacks geophysical support. The news media report that the nuclear device was emplaced in a shaft somewhat over 900 meters deep which, if correct, would suggest a yield most likely in the range of 400-480 KT and no more than 550 KT. Thus 350 KT and 550 KT can be regarded as the lower and upper bounds, respectively, of our preliminary yield estimate.
3. REPORTS AND PRESENTATIONS DELIVERED


(1992) Simultaneous inversion of explosion size and path attenuation coefficient with crustal phases (submitted for publication).6


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