UNSTEADY FLOW DISTORTION PAST BLADES:
SOURCES OF NOISE GENERATION IN ROTATING FLOWS

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UNSTEADY FLOW DISTORTION PAST BLADES

- OBJECTIVES
- RESEARCH PLAN
- PRINCIPAL PHYSICAL AND THEORETICAL CONCEPTS
- EXPERIMENTAL TECHNIQUES
- GENERIC CLASSES OF EDGE/SURFACE INTERACTION
  ✓ LEADING-EDGE
  ✓ TRAILING-EDGE
  ✓ LEADING-/TRAILING-EDGE
- EXPERIMENTAL SYSTEMS
  ✓ GENERIC SYSTEMS FOR LEADING- AND TRAILING-EDGE INTERACTIONS
  ✓ ACTIVELY-CONTROLLED PUMPING SYSTEM
- FLOW STRUCTURE IN ACTIVELY-CONTROLLED RADIAL-FLOW MACHINE
  ✓ OVERALL SYSTEM RESPONSE
  ✓ FLOW STRUCTURE AND PRESSURE SOURCES IN VANELESS DIFFUSER
  ✓ FLOW STRUCTURE AND PRESSURE SOURCES ALONG DIFFUSER BLADE OR CUTTOFF
  ✓ FLOW STRUCTURE AND PRESSURE SOURCES AT TRAILING-EDGE OF IMPELLER BLADE
  ✓ THREE-DIMENSIONAL NATURE OF FLOW STRUCTURE
UNSTEADY FLOW DISTORTION PAST BLADES: OBJECTIVES

GENERAL

- DETERMINE FLOW STRUCTURE AT LEADING- AND TRAILING-EDGES OF BLADING IN TERMS OF VELOCITY GRADIENTS REPRESENTING PRESSURE SOURCES.
- EMPLOY ACTIVE AND PASSIVE CONTROL TECHNIQUES TO MANIPULATE CRUCIAL PHASE SHIFTS OF VORTICITY FIELDS PAST BLADING.

DESIGN AND IMPLEMENTATION OF EXPERIMENTAL SYSTEMS

- GENERIC, CONTROLLED SYSTEMS FOR STUDY OF BASIC CLASSES OF LEADING- AND TRAILING-EDGE INTERACTIONS.
- UNIQUE RADIAL FLOW MACHINE FOR SIMULTANEOUS ACTIVE CONTROL AND FLOW VISUALIZATION.

DEVELOPMENT OF EXPERIMENTAL TECHNIQUES

- TECHNIQUES FOR QUANTITATIVE BUBBLE AND PARTICLE TRACKING VIA LASER DIAGNOSTICS.
- METHODS OF EVALUATION OF IMAGES VIA LASER INTERROGATION.
- APPROACHES TO TWO- AND THREE-DIMENSIONAL IMAGE CONSTRUCTION.
UNSTEADY FLOW DISTORTION PAST BLADES: RESEARCH PLAN

PHASE I

- DESIGN, CONSTRUCTION AND DEVELOPMENT OF:
  √ UNIQUE ROTATING MACHINE FOR VISUAL ACCESS AND ACTIVE CONTROL
  √ CONTROLLER SYSTEMS FOR ROTATING MACHINE
  √ LASER DIAGNOSTIC TECHNIQUES FOR QUANTITATIVE FLOW VISUALIZATION AND INTERPRETATION

- EXPERIMENTAL STUDY OF GENERIC CLASSES OF LEADING-/TRAILING-EDGE INTERACTIONS

PHASE II

- PRELIMINARY STUDIES OF FLOW STRUCTURE IN ROTATING MACHINE VIA LASER DIAGNOSTICS

- ACTIVE/PASSIVE CONTROL CONCEPTS OF GENERIC EDGE INTERACTIONS

PHASE III

- ACTIVE CONTROL STUDIES OF FLOW IN ROTATING MACHINE

- CONTROL OF GENERIC EDGE INTERACTIONS

JUNE 89  JUNE 90  JUNE 91  JUNE 92  JUNE 93

PHASE I  ...........................................

PHASE II  ∙ ...................... ∙

PHASE III  ∙ ............ ∙
The principal features of this research program involve identification of the elements of unsteady flow structure and their active control by applying disturbances of desired frequency and phase. Proper phase shift $\phi$ between dynamic events may allow attenuation of unsteady mechanisms of noise generation.
PRINCIPAL MECHANISMS OF FLOW DISTORTION RELATED TO NOISE GENERATION: CONCEPTS

I. INTERPRETATIONS OF PRESSURE SOURCE TERMS

\[ \nabla^2 p = 2\rho \left\{ \frac{\partial u}{\partial x} \frac{\partial v}{\partial y} - \frac{\partial u}{\partial y} \frac{\partial v}{\partial x} \right\} \]

\[ = -\rho \left\{ \nabla \cdot (\omega \wedge \mathbf{V}) + \nabla^2 \left( \frac{1}{2} \mathbf{V}^2 \right) \right\} \]

\[ = -\rho \left\{ \frac{\partial^2 v_i v_j}{\partial x_i \partial x_j} \right\} \quad T_{ij} \approx \rho_{o} v_i v_j \]

II. FAR-FIELD ACOUSTIC PRESSURE DUE TO FLOW DISTORTION IN FREE SPACE

Expressions of (I) serve as source terms in inhomogeneous wave equations. Solve for far-field density or pressure.

III. FAR-FIELD ACOUSTIC PRESSURE DUE TO FLOW DISTORTION ADJACENT TO SURFACE/BODY

(a) \( p(x,t) \) via Lighthill’s \( T_{ij} \) using deductive theory of surface effects.

(b) \( p(x,t) = \frac{-x_i}{4\pi c|x|^2} \frac{\partial}{\partial t} F_i \) (Curle, 1955)

\[ F_i = \int \rho_o \nabla X_i(y) \cdot (\omega \wedge \mathbf{V})(y, t - \frac{|x|}{c}) \, d^3y \quad \text{(Howe, 1989)} \]

\[ F = -\sigma \rho_o \frac{\partial}{\partial t} \int (x \wedge \omega) \, d^3x \quad \text{(Lighthill, 1986)} \]
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  ✓ THREE-DIMENSIONAL NATURE OF FLOW STRUCTURE
PARTICLE IMAGE VELOCIMETRY (PIV)
VIA LASER DIAGNOSTIC METHODS

GOALS

- Instantaneous velocity field across plane of flow at arbitrary phase of rotating blade system.

- High resolution measurements via small particle displacements ($\sim 10^2 \mu m$) and minimal interpolation.

- Characterization of velocity gradients required for calculation of vorticity and pressure sources.

SYSTEM DEVELOPMENT

- Minimization of particle size and optimization of image focusing via proper combination of laser source, camera, lens system.

- Image shifting via oscillating bias mirror
  √ Preclude directional ambiguity
  √ Optimize particle displacement and fringe spacing

- Generation of high-intensity pulsed- and scanned-laser sheets
  √ Dual-pulsed YAG system with beam combiner optics
  √ Single CW scanned argon-ion systems (acousto-optic and mirror scanner)

- Optical systems for translation and rotation of laser sheets

- Integrated computer control of
  √ Laser firing
  √ Image shifting
  √ Pump impeller rotation
  √ Camera triggering
  √ Pump inlet flow
  √ External shutters

- Hardware interfacing and software development related to foregoing
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GENERIC EDGE/SURFACE INTERACTIONS

TRAILING-EDGE INTERACTIONS

WAKE FROM TRAILING-EDGE UNDERGOING SINUSOIDAL PERTURBATIONS

WAKE FROM STATIONARY TRAILING-EDGE WITH BOUNDARY-LAYER SUCTION

WAKE FROM D-CYLINDER UNDERGOING DUAL MODE EXCITATION

WAKE FROM MILDLY NONUNIFORM CYLINDER PERTURBED SINUSOIDALLY

WAKE FROM CYLINDER UNDERGOING AMPLITUDE- AND FREQUENCY-MODULATED EXCITATION

WAKE FROM STATIONARY TRAILING-EDGE WITH BASE BLOWING
GENERIC EDGE/SURFACE INTERACTIONS

TRAILING-EDGE INTERACTIONS
GENERIC EDGE/SURFACE INTERACTIONS

LEADING-EDGE INTERACTIONS

WAKE ASYMMETRICALLY INCIDENT UPON LEADING-EDGE

WAKE FROM GENERATOR PAST LEADING-EDGE

WAKE-GAP INTERACTIONS IN SYSTEM OF OSCILLATING CYLINDERS
SIMULATED BLADE-BLADE INTERACTION:
DEVELOPMENT OF VORTEX AND PRESSURE FIELDS

$V/U = 1.43$

Regime III

0.94

Regime II

0.57

0.38

Regime I

0.19

CYLINDER TO FREE-STREAM VELOCITY RATIO $V/U$ DETERMINES RATE OF DEVELOPMENT OF LARGE-SCALE STRUCTURES IN GAP BETWEEN CYLINDER AND ELLIPTICAL LEADING-EDGE.

RELATIVE AMPLITUDES OF $P_I$ (INVISCID) AND $P_V$ (VORTICITY) PRESSURE PEAKS AND PHASE OF OCCURRENCE OF PEAKS (AT $T_a$ AND $T_b$) ARE FUNCTIONS OF VELOCITY RATIO $V/U$ AND DISTANCE ALONG LEADING-EDGE.
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CONTROLLED PUMP: RADIAL FLOW IMPELLER-DIFFUSER SYSTEM

Unsteady inflow generator

CONTROLLED WAKE-BLADE INTERACTION SYSTEM (PROJECTED)

CONTROLLED AXIAL FLOW PROPELLER SYSTEM (PROJECTED)
ACTIVELY-CONTROLLED
PUMPING SYSTEM

PISTON COMPUMOTOR
COUPLING
BEARING
TABLE
RAIL BEARING
PISTON SHAFT
LEAD SCREW

GUIDE RAILS
PISTON
O - RINGS
INLET DUCT

CONTRACTION

IMPELLER DRIVE
IMPELLER INLET DUCT
IMPELLER
EXPERIMENTAL SYSTEMS

PLAN VIEW OF
IMPELLER-VANELESS
DIFFUSER SYSTEM

0 20 mm
EXPERIMENTAL SYSTEMS

PLAN VIEW OF IMPPELLER-DIFFUSER BLADE SYSTEM
INLET FLOW Q AND IMPELLER ROTATION N HAVE ARBITRARY FUNCTIONAL FORMS AND PHASE SHIFTS.

CENTRAL COMPUTER CONTROLS FLOW Q, ROTATION, AND MULTIPLE FIRING OF YAG LASER SYSTEM AND CAMERA SYSTEM.

CAMERA-IMAGE INTERROGATION SYSTEM GIVES INSTANTANEOUS VELOCITY AND VORTICITY FIELDS.
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OVERALL RESPONSE TO CONTROLLED EXCITATION:
GENERATION OF MODULATED SPECTRAL COMPONENTS AND FLOW STRUCTURE—HYPOTHESIZED MECHANISMS

(a) In absence of inflow pulsations at \( f_p \), flow structure tends to repeat with period \( 1/f_{bp} \).

(b) In presence of inflow pulsations at \( f_p \), flow structure tends to repeat at difference frequency \( f_p - f_{bp} \) and its nonlinear harmonics.

(c) Reinforcement of these components and generation of additional discrete components can arise from nonlinear interaction between \( f_p \) and \( f_{bp} \) in boundary layer or separating shear layer to give \( nf_p \pm mf_{bp} \).

(d) If inflow forcing has amplitude- or frequency-modulated form, then large number of sum and difference components is expected due to multiple sideband interactions.

(e) Foregoing processes can influence rate at which spectral broadening occurs.

(f) Spectral broadening should be enhanced by existence of adverse pressure gradient (vaneless diffuser) or separation zones (diffuser or cutoff blades).
OVERALL RESPONSE TO CONTROLLED EXCITATION: GENERATION OF NONLINEAR INTERACTION COMPONENTS

The power spectral density of the velocity fluctuation $V^*$ is measured at the indicated (+) location at the exit of the impeller. At a relatively low value of the inflow perturbation frequency $f_F$, relative to the blade passing frequency $f_{BP}$, i.e. $f_F/f_{BP} = 0.196$, only the first harmonic $2f_F$ as well as nonlinear interaction components with $2f_{BP}$ are present. Increasing the dimensionless inflow perturbation frequency to $f_F/f_{BP} = 0.39$ produces pronounced sum and difference components between $f_F$ and $f_{BP}$.
OVERALL RESPONSE TO CONTROLLED EXCITATION: ATTENUATION OF FORCING COMPONENT AND GENERATION OF NONLINEAR INTERACTIONS

The power spectral density $V^*$ of the velocity component measured at the indicated (*) location at the impeller discharge exhibits a large number of nonlinear interaction components between the inflow forcing frequency $f_F$ and the blade passing frequency $f_{BP}$. However, at these relatively high values of dimensionless forcing frequency $f_F/f_{BP} = 0.78$ and $0.88$, the spectral peak at the inflow forcing frequency $f_F$ is completely attenuated.
The power spectral density of the velocity fluctuation $V^*$ is measured at the discharge of the impeller. The amplitude of the component at the inflow forcing frequency $f_F$, as well as the amplitude of higher order spectral components, is strongly dependent upon the amplitude of the tangential velocity fluctuation $V_i$ of the impeller relative to its mean tangential velocity $\bar{V}_i$. In the top plot, only the inflow is perturbed at a dimensionless frequency $f_f/f_{BP} = 0.39$. In the middle plot, the inflow is perturbed with the same condition, but accompanied by in-phase perturbations of the tangential velocity of the impeller at an amplitude of $\bar{V}_i/\bar{V}_i = 0.1$; the amplitude of the component at forcing frequency $f_F$ is nearly attenuated. In the bottom plot, the same excitation conditions hold as for the middle plot, except the dimensionless amplitude is increased to a value of $\bar{V}_i/\bar{V}_i = 0.3$; the amplitude of the component $f_F$ is actually amplified relative to that in the top plot. Consideration of a range of excitation conditions shows that the amplitude of the spectral component $f_F$ is highly sensitive to the amplitude of the impeller perturbation $\bar{V}_i/\bar{V}_i$; extremes of either complete attenuation or substantial amplification are attainable.
The power spectral density $V^*$ of the velocity fluctuation is measured at the indicated (*) location at the impeller discharge. Excitation of the inflow only at a dimensionless frequency $f_F/f_{BP} = 0.39$, where $f_F$ is the forcing frequency and $f_{BP}$ is the blade passing frequency, is represented by the top plot. In the middle and bottom plots, there is simultaneous excitation of the inflow velocity and the impeller tangential velocity, with the phase angle $\psi_{ip}$ between them.
OVERALL RESPONSE TO CONTROLLED EXCITATION: ALTERATION OF FORCING COMPONENT

The power spectral density $V^*$ of the velocity fluctuation is measured at the indicated (*) location at the impeller discharge. Excitation of the inflow only at a dimensionless frequency $f_F/f_{BP} = 0.39$ is shown in the top plot. In the middle and bottom plots, there is simultaneous excitation of the inflow velocity and the impeller tangential velocity, with the phase angle $\psi_{ip}$ between them. The amplitudes of the spectral peaks in the lower frequency range are strongly influenced by the value of $\psi_{ip}$.
The power spectral density $V^*$ of the velocity component is measured at the indicated (*) location within the vaneless diffuser. Excitation of the inflow is at a dimensionless frequency $f_p/f_{BP} = 0.39$. As the distance $e$, relative to the radius $r_1$ of the impeller, increases, the amplitudes of the discrete spectral components are altered. At large distances, the discrete spectral components are immersed in the broadband level.
OVERALL RESPONSE TO CONTROLLED EXCITATION: DECAY OF DISCRETE SPECTRAL COMPONENTS IN VANELESS DIFFUSER

\[ \frac{f_F}{f_{BP}} = 0.39 \]

\[ e/r_i = 0.19 \]

\[ \frac{f_F}{f_{BP}} = 0.39 \]

\[ e/r_i = 0.44 \]
The amplitude of the power spectral density $V^*$ of the velocity fluctuation is measured at indicated (*) location between discharge of impeller and leading-edge of stationary diffuser blade. In the top plot, no external forcing is imposed. In the middle plot, there is forcing only of the inlet flow at an excitation frequency $f_F$, relative to the blade passing frequency $f_{BP}$, i.e. $f_F/f_{BP} = 0.39$ and at an amplitude of the inflow velocity $V_p$ relative to the mean inflow velocity $V$, $V_p/V = 0.1$. Finally, in the bottom plot, the same excitation conditions were applied for the inflow, but in presence of a perturbation of the tangential velocity of the impeller at a phase angle $\psi_{ip} = \pi$ relative to the inflow perturbation. Very substantial manipulation of the discrete spectral components is attainable, especially in the presence of simultaneous inflow and impeller perturbations.
The amplitude of the power spectral density $V^*$ of velocity fluctuation is measured at the indicated (+) location between the discharge of the impeller and the leading-edge of the stationary diffuser blade. In the top plot, no external forcing is imposed. In the middle plot, there is forcing only of the inlet flow at an excitation frequency $f_F$ relative to the blade passing frequency $f_{BP}$, i.e. $f_F/f_{BP} = 0.39$ and at an amplitude of the inflow velocity $V_p$ relative to the mean inflow velocity $V_p$, $V_p/V_p = 0.3$. Finally, in the bottom plot, the same excitation conditions were applied for the inflow, but in presence of a perturbation of the tangential velocity of the impeller at a phase angle $\psi_{ip} = \pi$ relative to the inflow perturbation. Very substantial manipulation of the discrete spectral components is attainable, especially in the presence of simultaneous inflow and impeller perturbations.
The power spectral density $V^*$ of the velocity fluctuation is measured in the gap between the discharge of the impeller and the leading-edge of the diffuser blade. In the top plot, only the inflow is perturbed at a relatively low forcing frequency $f_F$ relative to the blade passing frequency $f_{BP}$, i.e. $f_F/f_{BP} = 0.1$. In the middle plot, both the inflow and impeller are perturbed with zero phase angle between them, and in the bottom plot both the inflow and impeller are perturbed with a phase shift $\psi_{ip} = \pi$ between them. These results show that at this relatively low value of excitation frequency $f_F/f_{BP} = 0.1$, it is necessary to perturb both the inflow and impeller in order to generate a large number of nonlinear interaction components.
The power spectral density $V^*$ of the velocity fluctuation is measured at the indicated (*) location between the discharge of the impeller and the leading-edge of the diffuser blade for an off-design flow coefficient $\Phi = 0.188$. In the top plot, no perturbations are applied. In the middle plot, there is excitation only of the inflow at frequency $f_F$ relative to the blade passing frequency $f_{BP}$ of $f_F/f_{BP} = 0.67$. In the bottom plot, there is simultaneous excitation of the inflow velocity and the tangential velocity of the impeller at a dimensionless frequency $f_F/f_{BP} = 0.67$, and with the phase angle between the perturbations of the $\psi_{ip} = \pi$. 
The power spectral density $V^*$ of the velocity fluctuation is measured at the indicated (*) location between the discharge of the impeller and the leading-edge of the diffuser blade for an off-design flow coefficient $\Phi = 0.071$. In the top plot, no perturbations are applied. In the middle plot, there is excitation only of the inflow at frequency $f_F$ relative to the blade passing frequency $f_{BP}$ of $f_F/f_{BP} = 0.25$. In the bottom plot, there is simultaneous excitation of the inflow velocity and tangential velocity of the impeller at a dimensionless frequency $f_F/f_{BP} = 0.67$, with a phase angle between the perturbations of $\psi_{ip} = \pi$. 
The power spectral density $V^*$ of velocity fluctuation is measured at the exit of the diffuser in presence of a stationary diffuser blade. In the top plot, perturbations of the inflow at frequency $f_F$ relative to the blade passing frequency $f_{BP}$ of $f_F/f_{BP} = 0.39$ are applied. In the bottom plot, the same excitation condition holds for both the inflow and tangential velocity of the impeller, with the phase angle $\psi_{ip} = \pi$ between them. Note the large amplitude of the low frequency fluctuations generated in both cases. Different discrete components are evident at this location, depending upon the condition of excitation with or without perturbation of the impeller.
OVERALL RESPONSE TO CONTROLLED EXCITATION: SUMMARY

I. POSSIBLE TYPES OF RESPONSE DUE TO OSCILLATIONS OF INFLOW AT FREQUENCY $f_F$
   - GENERATION OF LARGE NUMBER OF DISCRETE COMPONENTS AT $n f_F \pm m f_{BP}$
   - ATTENUATION OF DISCRETE COMPONENTS AT $f_F$ AND $f_{BP}$
   - ALTERATION OF LOW FREQUENCY, BROADBAND CONTRIBUTIONS

II. POSSIBLE TYPES OF RESPONSE DUE TO SIMULTANEOUS OSCILLATIONS OF INFLOW AND IMPELLER AT FREQUENCY $f_F$
   - GENERATION OF LARGE NUMBER OF DISCRETE COMPONENTS AT $n f_F \pm m f_{BP}$ EVEN AT LOW $f_F$
   - ENHANCEMENT OR ATTENUATION OF COMPONENT $f_F$; ATTENUATION OF COMPONENT AT $f_{BP}$

III. POSSIBLE IMPLICATIONS OF FOREGOING DISCRETE RESPONSE FOR LOW FREQUENCY, BROADBAND RESPONSE
   - LOCAL ALTERATIONS OF LOW FREQUENCY BROADBAND RESPONSE
   - INITIAL CONDITIONS FOR SPATIAL DELAY OF DISCRETE COMPONENTS TO BROADBAND FLUCTUATIONS IN VANELESS DIFFUSER
   - INITIAL CONDITIONS FOR LOW FREQUENCY STALL FLUCTUATIONS ALONG DIFFUSER BLADE
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FLOW STRUCTURE AND PRESSURE SOURCES IN VANELESS DIFFUSER

VELOCITY FIELD IN LABORATORY REFERENCE FRAME

VELOCITY FIELD IN BIASED FRAME

STREAMLINE PATTERN IN LABORATORY FRAME

STREAMLINE PATTERN IN BIASED FRAME
FLOW STRUCTURE AND PRESSURE SOURCES
IN VANELESS DIFFUSER

INSTANTANEOUS VORTICITY \( \frac{\partial \omega}{\partial x} \)

INSTANTANEOUS PRESSURE SOURCE TERM \( \frac{\partial \rho}{\partial x} \)
FLOW STRUCTURE AND PRESSURE SOURCES IN VANELESS DIFFUSER

TOTAL INSTANTANEOUS SOURCE

VORTICITY-RELATED SOURCE

RATE-OF-STRAIN-RELATED SOURCE
FLOW STRUCTURE AND PRESSURE SOURCES
IN VANELESS DIFFUSER

INSTANTANEOUS (POSITIVE) VORTICITY:
REALIZATION #1

INSTANTANEOUS (POSITIVE) VORTICITY:
REALIZATION #2

INSTANTANEOUS (POSITIVE) VORTICITY:
REALIZATION #3

AVG ARE OF THREE REALIZATIONS OF
INSTANTANEOUS (POSITIVE) VORTICITY
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FLOW STRUCTURE AND PRESSURE SOURCES ALONG A DIFFUSER BLADE

STREAMLINES IN LABORATORY REFERENCE FRAME

\[ \frac{V_p}{V_p} = 0 \]

\[ \frac{f_p}{f_{bp}} = 0.67 \]

\[ \phi = 60^\circ \]

\[ \phi = -60^\circ \]

\[ \frac{V_p}{V_p} \]

\[ \frac{f_p}{f_{bp}} = 0.67 \]

FLOW COEFFICIENT \( \phi = 0.188 \)
FLOW STRUCTURE AND PRESSURE SOURCES ALONG A DIFFUSER BLADE

VORTICITY \((\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y})\)

IB = VORTICITY FROM IMPELLER BLADE

DB = VORTICITY FROM DIFFUSER BLADE

\(t_p/t_{bp} = 0\)

\(\phi = 60^\circ\)

\(t_p/t_{bp} = 0.67\)

FLOW COEFFICIENT \(\phi = 0.118\)
FLOW STRUCTURE AND PRESSURE SOURCES ALONG A DIFFUSER BLADE

VORTICITY

\[ f_p/f_{bp} = 0 \]

FLOW COEFFICIENT
\[ \phi = 0.183 \]
FLOW STRUCTURE AND PRESSURE SOURCES
ALONG A DIFFUSER BLADE

VORTICITY

$f_p/f_b = 0.67$

FLOW COEFFICIENT
$\phi = 0.188$

$\phi = 59^\circ$
FLOW STRUCTURE AND PRESSURE SOURCES
ALONG A DIFFUSER BLADE

VORTICITY

\[ \frac{f_p}{f_{bp}} = 0.67 \]

FLOW COEFFICIENT
\[ \Phi = 0.18 \]

\[ \Phi = -50^\circ \]
FLOW STRUCTURE AND PRESSURE SOURCES
ALONG A DIFFUSER BLADE

INSTANTANEOUS VORTICITY \( \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} \)

INSTANTANEOUS PRESSURE SOURCE \( \frac{\partial p}{\partial x} - \frac{\partial f_p}{\partial y} \)

\[ \phi = 50^\circ \]

\[ f_p/f_{bp} = 0.67 \]
FLOW STRUCTURE AND PRESSURE SOURCES
ALONG A DIFFUSER BLADE

\[ \nabla^2 \phi = \frac{1}{
\]
UNSTEADY FLOW DISTORTION PAST BLADES

- OBJECTIVES
- RESEARCH PLAN
- PRINCIPAL PHYSICAL AND THEORETICAL CONCEPTS
- EXPERIMENTAL TECHNIQUES
- GENERIC CLASSES OF EDGE/SURFACE INTERACTION
  - ✓ LEADING-EDGE
  - ✓ TRAILING-EDGE
  - ✓ LEADING-/TRAILING-EDGE
- EXPERIMENTAL SYSTEMS
  - ✓ GENERIC SYSTEMS FOR LEADING- AND TRAILING-EDGE INTERACTIONS
  - ✓ ACTIVELY-CONTROLLED PUMPING SYSTEM
- FLOW STRUCTURE IN ACTIVELY-CONTROLLED RADIAL-FLOW MACHINE
  - ✓ OVERALL SYSTEM RESPONSE
  - ✓ FLOW STRUCTURE AND PRESSURE SOURCES IN VANELESS DIFFUSER
  - ✓ FLOW STRUCTURE AND PRESSURE SOURCES ALONG DIFFUSER BLADE OR CUTOFF
  - ✓ FLOW STRUCTURE AND PRESSURE SOURCES AT TRAILING-EDGE OF IMPELLER BLADE
  - ✓ THREE-DIMENSIONAL NATURE OF FLOW STRUCTURE
UNSTEADY FLOW DISTORTION PAST BLADES

- OBJECTIVES
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  - THREE-DIMENSIONAL NATURE OF FLOW STRUCTURE
FLOW THROUGH IMPELLER DIFFUSER SYSTEM:
INSTANTANEOUS STRUCTURE IN CROSSFLOW PLANE

SHROUD SIDE

HUB SIDE

t = 0

INSTANTANEOUS VELOCITY IN LABORATORY FRAME

$\mathbf{\vec{v}_p} + \mathbf{\ddot{v}_p}$

$\frac{f_p}{f_{bp}} = 1$

FIELD OF VIEW AT INLET OF VANELESS DIFFUSER

$\frac{t}{2/f_{bp}}$
FLOW THROUGH IMPELLER DIFFUSER SYSTEM:
INSTANTANEOUS STRUCTURE IN CROSSFLOW PLANE

INSTANTANEOUS STREAMLINES
IN LABORATORY FRAME

$\text{t} = 0$

$\text{t} = 2/\tau_{bp}$

FIELD OF VIEW AT INLET
OF VANELESS DIFFUSER

INSTANTANEOUS DISTRIBUTIONS OF
STREAMWISE VORTICITY INCLUDING
ENTIRE RANGE OF POSITIVE AND
NEGATIVE CONTRIBUTIONS
FLOW THROUGH IMPELLER DIFFUSER SYSTEM:
INSTANTANEOUS STRUCTURE IN CROSSFLOW PLANE

FIELD OF VIEW AT INLET OF VANELESS DIFFUSER

INSTANTANEOUS STREAMLINES IN LABORATORY FRAME

INFINITE DISTRIBUTIONS OF STREAMWISE VORTICITY INCLUDING ENTIRE RANGE OF POSITIVE AND NEGATIVE CONTRIBUTIONS

INSTANTANEOUS NEGATIVE STREAMWISE VORTICITY

INSTANTANEOUS POSITIVE STREAMWISE VORTICITY