COMPARISON OF THE OPERATIONAL CHARACTERISTICS OF THE THEORY OF CONSTRAINTS AND JUST-IN-TIME SCHEDULING METHODOLOGIES

THESIS

Lynn A. Sines, Captain, USAF

AFIT/GSM/LSM/91S-24

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DEPARTMENT OF THE AIR FORCE
AIR UNIVERSITY
AIR FORCE INSTITUTE OF TECHNOLOGY

Wright-Patterson Air Force Base, Ohio
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COMPARISON OF THE OPERATIONAL CHARACTERISTICS OF THE THEORY
OF CONSTRAINTS AND JUST-IN-TIME SCHEDULING METHODOLOGIES

THESIS

Presented to the Faculty of the School of Systems and
Logistics of the Air Force Institute of Technology
Air University
In Partial Fulfillment of the
Requirements for the Degree of
Master of Science in System Management

Lynn A. Sines, B.S.
Captain, USAF

September 1991

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Preface

The purpose of this thesis was to investigate the operational characteristics of Drum-Buffer-Rope, a Theory of Constraints scheduling methodology. The Theory of Constraints (TOC) has not been well researched in the past and this effort is one of the first evaluations of its operational characteristics.

The results of the simulation modeling were very encouraging, but some of the problems found in JIT systems are still present in TOC. This type of work with TCC should be continued so that when an organization implements the TOC control system they can be assured of the type of results expected.

In programming of the simulation models, running the models, and writing of this thesis I have had a great deal of help from others. I wish to thank my thesis advisor, Lt Col Richard Moore, for his patience and assistance when it was needed. I also wish to thank Dr. Fraker and the Computer Services Division of the University of Dayton for allowing me access to their computer and GPSSH software. Finally, I wish to thank my wife Kathy for her understanding on those nights when nothing was going right. I especially wish to acknowledge the help of my son Wil whose smiling face made each day a little brighter.

Lynn A. Sines
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Abstract

This study compared the characteristics of scheduling using two approaches: Just-in-Time (JIT) and the Theory of Constraints (TOC). Computer simulation was used to evaluate changes in the throughput of the system due to system variability and varying work-in-process (WIP) levels. The independent variables were processing time, probability of failure, and WIP level. The literature search revealed that these variables impacted performance of JIT systems. Simulation models of three different production systems were developed to determine if the TOC scheduled system would provide greater or equivalent throughput for equivalent levels of WIP, and to determine if the system production flow path had an impact on the performance of the TOC system. The models were scheduled using both JIT and TOC methodologies. The mean throughput for each combination of independent variables was calculated along with the 95 percent confidence interval. The mean and confidence intervals were then graphed for analysis. Simulation results indicated that the TOC system outperforms the JIT system for single product systems while the results of the multiple product system were inconclusive. There was no difference between the TOC systems for process time variability, but there was a difference for process station failure.
This thesis compares the performance of production systems which utilize Just-in-Time (JIT) and Theory of Constraints (TOC) scheduling methodologies. Dr. Eliyahu Goldratt, developer of the Theory of Constraints, has defined throughput, operating expense, and inventory as the three key performance measures in any system (Goldratt and Fox, 1986:28). The definitions of these three performance measures, as commonly used in American business, are:

1. Throughput - The total volume of production through a facility (Wallace and Dougherty, 1987:32).

2. Inventory - Items which are in a stocking location or work in process and which serve to decouple successive operations in the process of manufacturing a product and distributing it to the consumer (Wallace and Dougherty, 1987:15).

3. Operating Expense - Cost incurred in the course of the day-to-day activities of the firm (Skousen and others, 1987:1026)

The definitions Goldratt (1986:59-60) assigns to the measures above are simpler than those that are commonly used.
1. Throughput - The rate at which the system generates money through sales.

2. Inventory - All the money the system invests in purchasing things the system intends to sell.

3. Operating Expense - All the money the system spends in turning inventory into throughput. (Goldratt and Fox, 1986:29)

This research compares throughput and inventory of systems scheduled using TOC with the throughput and inventory of systems scheduled using JIT. Throughput will be the dependent variable of the model system. Inventory and system variability will be the independent variables for the comparison of JIT and TOC scheduling.

General Issue

Before the development of JIT, production scheduling was accomplished using heuristics to sequence jobs (Panwalker and Iskander, 1977:46). The first major step forward in scheduling was the Japanese Just-in-time (JIT) system. JIT provides an specific methodology for the scheduling of repetitive production systems which had not been provided by past methods. JIT allowed the Japanese to capture many markets due to improvements in quality, due date performance, and flexibility (Goldratt and Fox, 1986:36-60). While JIT was a major step forward in the development of scheduling methodologies, it has limited application outside of the repetitive manufacturing environment. In addition, it experiences a decrease in system reliability in the presence of variation in system
component reliability. The decrease in total system reliability can not be adequately protected against with increases in work-in-process (WIP) inventory as had been done in traditional scheduling methodologies (Lulu, 1986:237-238). The intent behind the JIT scheduling methodology was also to minimize the WIP inventory. Thus, while increased WIP inventory is required to protect the system reliability the increased inventory is in conflict with the intent of JIT (Schonberger, 1982:31-32).

Dr. Eliyahu Goldratt has said that the system variability problems associated with JIT can be alleviated through application of TOC to production control. Production organizations that implemented TOC have been able to maintain system reliability while decreasing WIP inventory below the levels of JIT (Goldratt, 1990:109-128).

United States industries must improve faster than the Japanese even to catch up, much less compete effectively in the world market. Through the initiatives currently under way in the U.S. Air Force, many organizations will compete with industry for workload and must be able to compete against companies employing JIT or TOC scheduled production. If TOC does perform to the level that has been claimed by its advocates, then Air Force organizations which utilize the TOC philosophy should be able to outperform commercial concerns which use JIT.
Specific Problem Statement

While JIT scheduling systems have been extensively investigated, TOC remains largely unresearched in the academic world. This difference in the amount of research that has been conducted is due primarily to the competitive threat of Japanese industry. Japanese industry has utilized JIT and other management methods to compete with American industry. The companies that have implemented the TOC philosophy have been primarily American or European. Academic research has been focused on JIT since it has been the scheduling methodology that has received the bulk of the business and public press attention. The large number of research efforts that were devoted to JIT may have impacted the number of available researchers that could have been evaluating TOC. Additionally, when compared to JIT, TOC concepts are relatively new. The first published explanation of the concept of drum-buffer-rope was not published until 1986. (Goldratt and Fox, 1986)

To develop realistic schedules and effectively control production in an actual organization, the effects of the scheduling theory on the organization must be known. To determine the suitability of the scheduling methodology research must be conducted to evaluate the expected impacts of the methodology.
Research Objectives

This research will investigate whether, through the use of TOC, system throughput is greater than that achieved with JIT scheduling techniques. A system that uses TOC scheduling should not be as significantly affected by system variabilities as one which uses JIT scheduling methodologies. The specific research questions that will be addressed are:

1. Does TOC's Drum-Buffer-Rope (DBR) technique resolve the throughput problems associated with system variability in JIT scheduled systems?

2. Is the throughput achieved in TOC systems dependent on the flow path of production system under consideration?

Scope of the Research

This research will be limited to the analysis of theoretical systems in which process component reliability and process time reliability are probabilistic variables. The total possible work-in-process inventory levels will be set at a constant level through the specification of buffer sizes and will only vary between simulation trials. The dependent variable in the system will be limited to the measurement of system throughput.

Background

Since the introduction of TOC in the early 1980s there has been little academic research conducted to evaluate the system effects of the TOC. Meanwhile a great deal of research has been conducted on JIT scheduled systems. These
articles have identified many problems with JIT which, if the claims of the proponents of TOC are true, make TOC a viable replacement for JIT. The most severe anomaly that affects production systems occurs when the system experiences variation in either process time or system reliability. Since JIT greatly reduces the work-in-process inventory that allows decoupling of operations, a small variation at a process station is magnified by the system and has a major impact on the ability of the system to produce an end item (Lulu, 1986:241).
II. Production Process Scheduling

Production process scheduling or control has long been recognized as a very important component in the effective utilization of a production system. Prior to the development of the Just-in-time (JIT) scheduling methodology efforts were made either to deal with the system on a gross capacity basis or in the sequencing of parts being fabricated. Both of these views of the system failed to incorporate the effects of interdependencies and inherent variabilities of the production system. This failure made the scheduling systems which resulted from the views very unreliable and operations managers viewed the generated schedules with suspicion. (Rowe, 1960:125)

In 1929, the Taylor Society acknowledged the problem of scheduling of a manufacturing concern. Control of the manufacturing process was viewed as essential to the smooth flow of processing and to meet sales demands. It was also seen that control of production and sales were correlated, but this correlation was viewed to add so much diversity that there was no way of establishing control over the productive process. So while establishing control was viewed as essential it was also viewed as impossible to accomplish. (Lansburgh, 1929:263-265)

The JIT philosophy was the first major effort which succeeded in establishing both required and realistic control over the production process. While JIT was the
first to succeed it was by no means the first effort made in establishing control. Prior efforts include:

1. Simple priority rules related to processing time, due date, number of operations, cost rules, setup time, arrival times, and machine selection.

2. Combinations of the simple priority rules above such as first in first out (FIFO), dividing jobs into priority classes and using FIFO, queuing rules, and cost/time criteria.

3. Weighted priority indexes which select the job with the smallest value of priority index.

4. Heuristic scheduling rules which include many different kinds of rules based on the operation under consideration.

All of these efforts failed to establish firm control over the production process due primarily to the subjective nature of the rules. JIT and TOC both establish firm control since they are based on the movement of subcomponents within the production system. (Panwalker and Iskander, 1977:45-59)

**Just-in-time Scheduling Methodology**

JIT mandates that the amount of work-in-process and finished inventory contained in the system should be very strictly controlled. JIT is both a system for managing an organization and an overall approach to production and inventory management (Heiko, 1989:61).

JIT, as an approach to production and inventory management, is used by many manufacturing companies in the United States and Japan. (Walton, 1986:42). The basic idea of the production and inventory management portion of JIT is simply:
Produce and deliver finished goods just in time to be sold, subassemblies just in time to be assembled into finished goods, fabricated parts just in time to go into subassemblies, and purchased materials just in time to be transferred into fabricated parts. (Heiko, 1989:61)

Philosophy. The Japanese approach to the management philosophy of JIT is the elimination of waste or non-value-added actions. Taiichi Ohno states that JIT "is a system of production, based on the philosophy of total elimination of waste, that seeks the utmost in the way we make things" (Heiko, 1989:61).

The JIT management philosophy contains three primary guiding principles:

1. Streamline manufacturing operations. The streamlining of operations includes setting up dedicated lines and flow layout, and reducing or eliminating setup times (Heiko, 1989:62).

2. Control for total quality. Total quality control is the implementation of Dr. Edward Deming’s 14 points of quality management (Heiko, 1989:62). These points are:

   Point 1 - Create constancy of purpose toward improvement of product and service (Deming, 1982:23). The goal of the organization must be defined so that the entire organization can work toward the common goal (Walton, 1986:34).

   Point 2 - Adopt the new philosophy (Deming, 1982:23). The organization’s management and workforce must adopt the attitude that mistakes that were tolerated in the past are now unacceptable (Walton, 1986:34).

   Point 3 - Cease dependence on inspection to achieve quality (Deming, 1982:23). The organization tolerates the workers mistakes through the inspection of products. The organization, in a sense, pays for worker mistakes, then corrects the mistakes through rework. "Quality does not come from inspection but from improvement of the process" (Walton, 1986:34).

   Point 4 - End the practice of awarding business on the basis of price-tag (Deming, 1982:23). The awarding of
business to a firm based upon price alone frequently leads to supplies being of low quality. The effective manager should seek the best quality, and work to achieve even better quality through one vendor under a long-term relationship (Walton, 1986:35).

Point 5 - Improve constantly and forever the system of production and service (Deming, 1982:23). Management should always look for ways to reduce waste and improve quality. This commitment should also be passed on to workers since they are closer to the problem areas (Walton, 1986:35).

Point 6 - Institute training on the job (Deming, 1982:23). Too often the workers can not do quality work because they have not been properly trained (Walton, 1986:35).

Point 7 - Institute leadership (Deming, 1982:23). Management should help workers do a better job. Management should also evaluate workers using objective methods to determine who is in need of individual help (Walton, 1986:35).

Point 8 - Drive out fear (Deming, 1982:23). Employees should not be afraid to ask questions or to take a position. To achieve improvements in quality and productivity, the people of the organization must feel secure (Walton, 1986:35).

Point 9 - Break down barriers between departments (Deming, 1982:24). All units in the organization must work together as a team and work toward the same goal (Walton, 1986:35).

Point 10 - Eliminate slogans, exhortations, and targets for the workforce asking for zero defects and new levels of productivity (Deming, 1982:24). Slogans have never helped anyone do a better job (Walton, 1986:35).

Point 11 - Eliminate numerical quotas on the factory floor and eliminate management by objective (Deming, 1982:24). As Dr. Deming states, "Quotas take account of numbers, not quality or methods" (Walton, 1986:35).

Point 12 - Remove barriers to pride of workmanship (Deming, 1982:24). People want to do a good job, and get discouraged when the process does not allow quality. The normal barriers to quality are misguided supervisors, faulty equipment, and defective materials (Walton, 1986:36).

Point 13 - Institute a vigorous program of education and self improvement (Deming, 1982:24).
Management and workers must be trained in the new management methods such as teamwork and statistical techniques (Walton, 1986:37).

Point 14 - Put everyone in the company to work to accomplish the transformation (Deming, 1982:24). Neither the workers nor management can implement the transformation on their own. All people in the organization must work together as a team (Walton, 1986:37).

3. Leverage with worker creativity. Management must realize that the average worker is very creative and this creativity must be focused on the process. As in Deming's 14 points, the worker is closest to the process (Heiko, 1989:63).

While, the application of the JIT philosophy to the production system is extremely inexpensive, it does call for a change in the traditional culture of American business. The implementation of JIT does not require the use of computers or other capital investments, since it provides control over the inventory in the system through the use of visual indicators.

Kanban. Kanban is a Japanese word meaning "visible record" (Schonberger, 1982:86). The kanban can be anything from a golf ball to a card, but its basic function is to indicate to the receiver of the kanban that a quantity of parts is required elsewhere in the production process. The kanban functions in conjunction with the other elements of the JIT philosophy to provide production control and process improvement (Suzaki, 1987:148-149).

1. Production control - The function is to tie different processes together and deliver the required materials at the right time in the right amount (Suzaki, 1987:152).
2. Process improvement - The emphasis is on reducing the inventory levels in the system through the removal of kanbans (Suzaki, 1987:152).

The production control aspect of the use of kanbans is utilized to provide a controlled environment to the production operation. The idea of the kanban is to link adjoining operations with a "rope". The rope is the combination of the card and parts containers. For example, if there are ten containers between two production processes each with the ability to hold one component then the work-in-process inventory level between the processes has been set at ten components. As the first operation completes processing of a component it is placed in an empty container. The first operation now checks to see if there are any remaining empty containers. If empty containers remain then work begins to process another component. If there are no empty containers then no processing takes place until a container is emptied by the second operation (Ricard, 1984:7). This movement of containers takes place between each set of production stations in the production process.

As can be seen by the discussion above the primary type of production operation to which the JIT with kanbans system could be applied is a flow-shop. A flow-shop and job-shop as defined by the American Production and Inventory Control Society are:

1. Flow-shop - A manufacturing organization in which machines and operators handle a standard, usually uninterrupted material flow. The plant layout is designed
to facilitate a product "flow." Production is set at a given rate and the products are generally manufactured in bulk (Wallace and Dougherty, 1987:12).

2. **Job-shop** - A manufacturing organization in which the productive resources are arranged according to function. The jobs pass through the functional departments in lots and each lot may have a different routing (Wallace and Dougherty, 1987:15,16).

The application of this type of control system to a job-shop is very complicated due to the number of different types of components and processes which are normally involved. The application of JIT with kanbans can be used in a job-shop in the area of raw material or subcomponent control and ordering (Schonberger and Knod, 1991:369).

**The Theory of Constraints Scheduling Methodology**

The overall objective of the Theory of Constraints (TOC) is to implement a process of continuing improvement. The continuing improvement process is achieved through commitment of an organization's management to the theories and practices that comprise TOC (Goldratt and Cox, 1986:266-272).

TOC is based on the theory of Dr. Eliyahu Goldratt which builds on the principles of the Quality Management Theory developed by Dr. Edward Deming, and the Just-in-time (JIT) inventory control procedure developed by Taiichi Ohno (Goldratt, 1990a:109).

The Theory of Constraints is a methodology for analyzing a system to determine the location and type of constraints present. Prior to the constraints being
analyzed, the management of the organization must determine
the organization's goal and the measurement criteria
applicable to those goals. The goals of the organization
will drive the decisions of how to manage the constraints.
After the goals and the measurement criteria are determined,
management can begin the process of analyzing the
constraints (Goldratt, 1990a:3-4). There are five
facilitating steps of TOC:

Step 1 - Identify the system's constraints. The
constraints must be identified and then prioritized
according to their effect on the system (Goldratt, 1990a:5).
Constraints can be categorized as either physical
constraints or policy constraints (Goldratt and Fox,
1989a:2).

1. Physical constraints. Physical constraints
are those physical things in the system which limit the
production capability. They can be resources that are in
short supply, vendor limitations, the demand for the
product, or long processing time operations which affect the
flow of material internal to the system (Goldratt and Fox,
1989a:2-4).

2. Policy constraints. Policy constraints
include all rules levied on the organization by management
that limit the system (Goldratt and Fox, 1989a:5-7).

Step 2 - Decide how to exploit the system's
constraints. The system's constraints should be fully
exploited so that the maximum output is achieved from the
system. Non-productive time for the constraint is the same
as non-productive time for the entire system (Goldratt,
1990a:5). On the surface it appears that the easiest type
of constraint to exploit is a policy constraint since the
policies that govern an organization are controlled or
influenced by management, but these constraints are the
least obvious since they are imbedded in the structure of
the organization (Goldratt and Fox, 1989a:3; Goldratt and
Fox, 1989b:22-23).

Step 3 - Subordinate everything else to the above
decision. The decision of how to exploit the full potential
of the constraint will place limits on all other decisions
affecting operation of the system. The constraint is the
limiting factor in the performance of the system (Goldratt, 1990a:5).

Step 4 - Elevate the system's constraints. If we can elevate or reduce the impact of the constraints' limiting effect, the system's performance can be improved. If the constraint can be sufficiently elevated the constraint will eventually be broken (Goldratt, 1990a:5-6).

Step 5 - If in the previous steps a constraint has been broken, go back to the first step. The constraint that has been broken in the preceding steps will no longer be the limiting factor in the system, but there will be other constraints on the system (Goldratt, 1990a:6).

The preceding five steps used in analyzing and resolving constraints are all equally important but, as Dr. Goldratt warns, the effective manager must "not allow inertia to cause a system constraint" (Goldratt, 1990a:6).

Scheduling with the TOC. Several of the tenets of TOC run counter to the conventional view of a production organization. These tenets are:

1. Balance flow, not capacity. Traditional manufacturing control systems have tried to balance capacity and then maintain flow. While the theoretical "perfect system" capacity can be balanced, the inherent variability of the real environment makes this impossible (Berry, 1985:81).

2. The level of utilization of a non-constraint is not determined by its own potential but by some other constraint in the system (Berry, 1985:81). As stated in the Theory of Constraints, the constraints of the system drive the performance of all aspects of the system (Goldratt, 1990a:4).

3. Utilization and activation of a resource are not synonymous. Management should not strive to keep everyone busy all the time. The only resource that should be 100 percent utilized is the constraint of the system (Berry, 1985:81).

4. An hour lost at a constraint is an hour lost for the total system. Since the constraint controls the
system it must be active constantly for the maximum system performance to be achieved (Berry, 1985:81).

5. An hour saved at a non-constraint is a mirage. A non-constraint is defined as having excess capacity, so time saved on it is only an increase in excess capacity (Berry, 1985:81).

6. Constraints govern both throughput and inventories. The amount that the system can produce (throughput) and the amount of material contained in the system (inventory) are controlled by the constraint. Thus, the constraint is the controlling element in the system (Berry, 1985:81).

7. The transfer batch may not, and many times should not, be equal to the process batch. The transfer batch must be sized to keep the constraint fully utilized and not by the theoretical economic process quantity (Berry, 1985:81).

8. The process batch should be variable, not fixed (Berry, 1985:81). The principles of JIT should be applied to minimize the amount of inventory contained in the system (Heiko, 1989:62).

9. Schedules should be established by looking at all the constraints simultaneously. The capacity of the constraints specifies the timing of the schedules and the ability of the system to produce (Berry, 1985:81).

Under TOC there are essentially three ways to develop a realistic production schedule, Optimized Production Technology (OPT), DISASTER, and Drum-Buffer-Rope (DBR), all of which use the TOC philosophy. The first developed by Dr. Goldratt was the Optimized Production Technology (OPT) scheduling software. In the OPT software the user constructed the flow of the organization, then input the processing times, market requirements, and all other production data. The software then generated a complete schedule for the organization which could be updated in a matter of minutes as compared to the hours required to
regenerate an MRP schedule. One of the problems associated with the OPT software was that it required a mainframe computer which was available for the large corporations which initially implemented the software, but was not available to numerous small businesses. The DISASTER software provided a Personal Computer based scheduling system to the small company. DISASTER is a computer-based implementation of Drum-Buffer-Rope (DBR). DBR is a manual, philosophical-based approach to the problem of scheduling that is simple enough to implement in many cases without the need for computers. (Lundrigan, 1986:5–9; Severs, 1991:4–5)

Drum-Buffer-Rope (DBR). Just as in JIT where kanban provides the primary means of control over the production system, DBR provides the same type of control in the TOC philosophy. While being similar to kanban, DBR is much easier to implement since the control is tying the constraint of the system to the material release point for the system (Goldratt and Fox, 1986:94). The idea of DBR comes from an analogy that Dr. Goldratt developed in The Goal (Goldratt and Cox, 1986) of a Boy Scout troop marching in single file on a hike.

In the hike analogy the drum is the slowest scout since he sets the pace for the troop. The rope is tied from the slowest scout to the first scout in the line. The buffer is the amount of slack that is placed in the rope to account for variations in the speed of the scouts. The scouts in the line after the slowest are constrained to travel no
faster than the slowest scout since the scout master has specified that there will be no passing. (Goldratt and Fox, 1986:96-99)

The hike analogy can also be applied to the JIT system. In a JIT system the rope is tied between each scout in the line and the buffer between each scout is the amount of slack in the particular segment of rope. The drummer of the system is the last scout in the line or in a production system the market demand for the product produced. (Goldratt and Fox, 1986:94-95)

In a DBR controlled production system the amount of buffer required is governed by the amount of variability or unreliability in the operations preceding the system constraint. The objective of the controlling process is the maintain 100 percent utilization of the constraint. The utilization of the other processes in the system is much less important since by definition they have excess capacity. (Goldratt and Fox, 1986:100-103)

The overall point to DBR control is that material is not released to supply work to workers, but is released and processed according to the needs of the system constraint. This idea of having idle labor is a major change to the culture of most American companies where in the past the main duty of management was to keep everyone busy all the time. (Goldratt and Fox, 1986:112-115)

Advantages of the TOC. The TOC has been successfully implemented by several of the major manufacturing companies.
in the United States in the last 10 years. The initial implementation of the TOC was in producing prefabricated chicken coops in Israel. From this humble beginning, US companies such as General Motors, General Electric, AVCO, Ford, and Bendix have implemented the TOC concepts and achieved remarkable results. The results achieved include decreased inventories and lower processing times (Jayson, 1987:18).

The primary advantage of the TOC is the new way at viewing the organizational environment (Waters, 1986:107). In the past, manufacturing managers have tried to achieve local optimization by, as Dr. Goldratt states, thinking that "the only way to reach a global optimum is by insuring local optimums." The local optimization led to nothing more than clogging the constraints of the system and, as the managers tried to balance the production, the bottlenecks wandered from station to station. Thus the motto of the TOC is: "The sum of the local optimums is not equal to the global optimum" (Berry, 1985:81-82).

Another advantage of TOC and particularly the Drum-Buffer-Rope control methodology is the ease in implementing the system. While JIT is primarily constrained to the flow shop environment, DBR can be implemented in either a flow shop or job shop. Since the primary concern of the control system is to keep the constraint fully utilized and not controlling between each production station the mixture of
products going through the system can be much larger
(Goldratt, 1990b:222-228).
III. Methodology

Method of Approach

System simulation will be used in this investigation to determine the effects of system variability on JIT and TOC scheduled systems. In the JIT systems kanban control will be used, while the TOC systems will use drum-buffer-rope (DBR) control. The variability of the production systems will consist of process time variation as well as breakdowns resulting in downtime. Theoretical production systems with different flow paths will be scheduled using both the JIT and TOC scheduling methodologies to determine if the type of production system effects the selection of optimum scheduling methodology.

Background - Simulation of Production Systems

Past production system scheduling research has extensively utilized simulation to determine the effects of JIT scheduling on the system. The effects of system variability on JIT scheduled systems, particularly variability caused by process failure, has been shown to degrade the ability of the system to produce at a constant rate (Lulu, 1986:248; Lulu and Black, 1987:227-228). This type of variability will be simulated in this study to determine if these effects are also found in TOC scheduled systems.
There have been no past studies that have compared JIT and TOC. The only comparative studies that were found were between JIT and traditional scheduling methodologies (Pyke and Cohen, 1990; Spearman and Zazanis, 1988; Austin and Khoshnevis, 1986; Karmarkar, 1986). In these studies the analysis of the optimum methodology was based primarily on the qualitative assessment of system performance by the researcher. The main problem with providing a quantitative comparison between traditional and JIT comes from the inherent differences in the operating philosophies behind the methodologies. Under traditional scheduling there is no effort to limit the amount of inventory in the system. In contrast, limiting inventory is a primary factor in the JIT philosophy. The quantitative studies that have been conducted have dealt primarily with the assessment of the operational characteristics of JIT. (Manivannan and Pegden, 1990; Ketcham, 1988; Lulu and Black, 1987; Lulu, 1986; Schroer and others, 1985; Huang and others, 1983) The studies that have been conducted on various configurations of JIT systems all conclude, that without the variability reductions, inherent in the JIT philosophy, the ability of the system to produce the intended output is severely impacted.

Justification of the Approach

Due to the complexities of production environments and the costs associated with varying actual systems, simulation
is the most feasible approach for the study of these systems. Also due to the variability of the human element in actual systems precise mathematical measurements are either infeasible or costly to obtain (Malcolm, 1958:177-178).

The use of simulation to study production systems has been acknowledged to be not only the best means for researching the effects of changes to the system, but also in most cases it is the only reasonable means to study such effects. Experimentation on the actual system is disruptive to the production environment and normally not cost effective (Law, 1988:40). The results obtained from experimentation on the actual system may also yield results that are affected by extraneous variables that can not be controlled. Through the use of simulation the total environment is controllable and the effects of extraneous environmental variables can be eliminated (Dunham and Kochhar, 1983:19). In the business world today simulation is routinely used for day-to-day decision-making and long-range planning. Some of the typical applications include inventory management, scheduling, and operations planning (Russell and others, 1967:162-163).

Assumptions

The following assumptions have been made relating to the simulation of these production systems:

1. The processing time for each production station is uniformly distributed.
2. Processing time and probability of process station failure will not both vary in the same simulation run.

3. Probability of process station failure is uniformly distributed with respect to time.

4. The probability of failure of the system constraint is zero.

5. Each buffer within the particular system is of the same capacity.

6. The market for the products produced can absorb the total throughput of the system.

General Research Method

This research study will utilize three different theoretical production systems to determine if throughput variations due to variations in work-in-process inventory, probability of process station failure, and process time variation are system dependent. Each of the production systems will be scheduled using JIT (Kanban) and TOC (Drum-Buffer-Rope) scheduling techniques to determine if throughput level is affected by scheduling methodology when subjected to system variations.

Specific Methodology

Development of Theoretical Production Systems. The research study will utilize three theoretical production systems to compare the operational characteristics of the TOC with JIT under a variety of conditions. The three types of production systems that will be utilized are:

Model System 1 - Single Product Assembly Line. This system will consist of a single product manufacturing
line with no parallel actions required to complete the product (Lulu, 1986:237). The actions required to complete the product will be performed by four process stations in a serial network (Figure 3-1). This type of production system is similar to type of system that aircraft engines are repaired under at an Air Force Air Logistics Center. The four steps in the actual system could be: (1) Incoming Inspection, (2) Engine Disassembly, (3) Engine Repair, (4) Engine Reassembly.

![Figure 3-1. Single Product Assembly Line](image)

Model System 2 - Single Product Parallel Process Assembly Line. This system model will consist of a total of six process stations. The raw material required by the product will flow through either of two parallel paths, each consisting of two process. The two subassemblies are then combined and production of the finished component is completed by the two remaining processes (Figure 3-2).
The single product parallel process system is analogous to the type of systems found in defense contractor facilities. The two subcomponents that are combined into a finished product could be the F110 engine and F-16 airframe in the production of the F-16 fighter aircraft.

**Model System 3 - Multiple Product Parallel Process Assembly Line.** This system model will produce two different products with parallel processes required to complete both products. Each product will consist of two subassemblies, one of which is common to both products. Each of the three subassemblies will flow through two processes before being combined to flow through the remaining two process cells to
be completed into a finished product. The completion of the products will not require the utilization of the same production assets and material to be completed (Figure 3-3).

The system could be the production system used in the manufacture of aircraft pneumatic regulators. Two different regulators are produced from one unique component, the regulator body, and one common component, the actuating mechanism. The regulator body and actuating mechanism are then combined into the finished product. Pneumatic regulators are found on all Air Force aircraft.

![Figure 3-3. Multiple Product Parallel Process Assembly Line](image-url)
System Model Development

Simulation Language. General Purpose Simulation System (GPSS/H) (Wolverine Software Corp., 1990) will be utilized as the simulation language to develop computer models of the above three systems. This simulation language is flexible enough to model a wide range of systems, but also provides the necessary capability for this application. GPSS/H has also been shown to be very reliable in a variety of applications (Banks and others, 1989:ix). In past research GPSS has been used effectively in the study of work-in-process inventory in a production system (Bowen, 1970). The past usage of GPSS combined with the inherent speed and flexibility of the simulation language make it appropriate for this research application.

System Model Programming. The system models were developed and programmed using the simulation language. Models were developed for each system using both JIT (JIT with kanban) and TOC (Drum-Buffer-Rope) scheduling methodologies. The symbols used to describe the buffer, production station, product flow, and control signal flow in the production systems are shown in Figure 3-4. These symbols will be used to describe the general flow through the systems that the programming will follow. The models will be developed from these general flow diagrams.
The programming of System 1 - Single Product Assembly Line for the JIT with kanban model was developed with buffers located before each production station. The kanban control signal and product flow will be as illustrated in Figure 3-5. The work-in-process inventory was measured from the time the product entered Station 1 until the product completed processing on Station 4. This flow diagram illustrates a general production line controlled by the JIT methodology. The simulation program will duplicate this type of system flow pattern.
The programming of System 1 using TOC Drum-Buffer-Rope control was developed with the buffer protection immediately before the system constraint (Station 3). The control signal flowed back to the initial product release point for ease into Station 1 (Figure 3-6). The work-in-process inventory was measured, as in the prior model, from the time the product entered Station 1 until it departed Station 4. The programming of the actual model followed the general flow pattern established by this diagram. The control of the model was established through the use of a buffer counter.
The programming of System 2 using JIT with kanban followed the same buffering and kanban flow as System 1 using JIT with kanban control. The work-in-process was measured by taking the amount of product in each of the parallel operations as half of a unit. The buffers, however, considered a subcomponent as a whole unit. The flow for the programming of the model is illustrated in Figure 3-7.
The programming for System 2 - Drum-Buffer-Rope was similar to the flow that was programmed in the previous DBR model with the exception of the parallel processes. The work-in-process was calculated as in the previous JIT model and Figure 3-8 illustrates the flow of this model. The flow through the model was established by splitting the input product into two separate entities that were rejoined immediately before the constraint operation. The control released both parts of the product into the model at the same time as the buffer before the constraint requires additional inputs.
The programming for System 3 - JIT with kanban was similar to that established in the previous JIT models with the exception of the production of two products. The work-in-process considers the subcomponents in the initial processing stations, Stations 1 and 2, as half of a full unit; while the product in Stations 3 and 4 were considered as full units. The throughput data output from this model included the separate data on Product 1 and 2, as well as, the total throughput for the system. The programming followed the flow diagram of Figure 3-9.
The programming of System 3 - Drum-Buffer-Rope consisted of all requirements of the previous DBR models and the previous System 3 - JIT model. The programming was developed using the product and flow diagram illustrated in Figure 3-10.

Figure 3-9. System 3 - JIT with Kanban
Figure 3-10. System 3 - Drum-Buffer-Rope

Processing Times

System 1. The mean times for each of the process stations of System 1 are listed in Table 3-1. As can be seen from the values, Station 3 with a mean of 20 minutes is the system constraint for both models. The times
for each station will be identical for the models of both scheduling methodologies.

### TABLE 3-1

**SYSTEM 1 - MEAN PROCESSING TIMES**

<table>
<thead>
<tr>
<th>Process Station</th>
<th>Mean Time (Minutes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>7.5</td>
</tr>
<tr>
<td>2</td>
<td>12.5</td>
</tr>
<tr>
<td>3</td>
<td>20.0</td>
</tr>
<tr>
<td>4</td>
<td>5.0</td>
</tr>
</tbody>
</table>

System 2. The mean times for each of the process stations of System 2 are listed in Table 3-2. As was the case in System 1, Station 3 is still the system constraint. The addition of the processing times for Stations 1B and 2B are the only differences from the System 1 processing times.
### Table 3-2
SYSTEM 2 – MEAN PROCESSING TIMES

<table>
<thead>
<tr>
<th>Process Station</th>
<th>Mean Time (Minutes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1A</td>
<td>7.5</td>
</tr>
<tr>
<td>1B</td>
<td>5.0</td>
</tr>
<tr>
<td>2A</td>
<td>12.5</td>
</tr>
<tr>
<td>2B</td>
<td>7.5</td>
</tr>
<tr>
<td>3</td>
<td>20.0</td>
</tr>
<tr>
<td>4</td>
<td>5.0</td>
</tr>
</tbody>
</table>

System 3. The mean times for each of the process stations in System 3 are listed in Table 3-3. There are now two system constraints in the system, Process 3-1 is the constraint for Product 1 and Process 3-2 is the constraint for Product 2. The processing time for Station 1B was reduced from 5.0 minutes to 2.5 minutes to eliminate the possibility of the B parallel branch from becoming a constraint on both products.
TABLE 3-3
SYSTEM 3 - MEAN PROCESSING TIMES

<table>
<thead>
<tr>
<th>Process Station</th>
<th>Mean Time (Minutes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1A</td>
<td>7.5</td>
</tr>
<tr>
<td>1B</td>
<td>2.5</td>
</tr>
<tr>
<td>1C</td>
<td>5.0</td>
</tr>
<tr>
<td>2A</td>
<td>12.5</td>
</tr>
<tr>
<td>2B</td>
<td>7.5</td>
</tr>
<tr>
<td>2C</td>
<td>10.0</td>
</tr>
<tr>
<td>3-1</td>
<td>20.0</td>
</tr>
<tr>
<td>3-2</td>
<td>25.0</td>
</tr>
<tr>
<td>4-1</td>
<td>5.0</td>
</tr>
<tr>
<td>4-2</td>
<td>5.0</td>
</tr>
</tbody>
</table>

Independent Variables. The variables that were studied using the model systems are:

1. Type of scheduling system utilized.

2. Maximum work-in-process inventory present in the system during the simulation run. The maximum work-in-process level for the simulation run was set by designating the size of the buffers in the model. The size of the buffers in the system ranged from 1 unit to 8 units.

3. Probability of failure of process station. Nine different probability values, ranging from 0 to 0.4 in 0.05 increments, were established for the simulation testing. The probability of failure for each station in the model was the same for the simulation run with the exception of the system constraint which did not have a probability of failure.

4. Variance of processing time for process station of the system. Nine different variances, ranging
from 0 to 40 percent in 5 percent increments of the mean process time, were established for the simulation testing. The percentage variability will be plus or minus the percent variability so that a station with a mean processing time of 20-minutes varying at 40 percent encountered processing times ranging from 12-minutes to 28-minutes. All stations within the model, including the system constraint, will have the same percent variability.

**Dependent Variables.** As has been stated by Dr. Goldratt, one of the measures of a production system is throughput, so the amount of product generated in a set amount of time was the measurement variable. Throughput is also easily measured in the simulation environment.

**Data Generation.** The probability of process station failure and variation of process time were each evaluated separately using the same testing hierarchy.

**Testing Hierarchy.** Each of the model systems was scheduled using JIT and TOC methodologies. The model execution sequence consisted of a simulation run, a set-point group, an equi-inventory group, an equi-variability group, and model execution.

1. **Simulation Run** - consists of an initial 40-hour warm-up period to load all system buffers, followed by an 160-hour data gathering period. The simulation run is a single execution of the particular model and is therefore the smallest unit of the study. During the simulation run all independent variables were set at a constant value. The results of the simulation run consisted of the values of the independent variables and the number of units completed during the data gathering period, dependent variable.

2. **Set-point Group** - consists of 100 simulation runs. The set-point group is a collection of simulation runs each with the same values for the independent variables. Each of the simulation runs within this group utilized different groups of random numbers by starting the particular simulation run at a different point on the random number stream.
3. Equi-Inventory Group – consists of 9 set-point groups each having the same value of inventory, but each set-point group had different values of variability.

4. Equi-Variability Group – consists of 8 set-point groups each having the same variability value, but different inventory. The equi-variability group was either a process time equi-variability group or a station failure equi-variability group. Each of the set-point groups in the utilized the same random numbers.

5. Model Execution – consists of 72 set-point groups with all combinations of inventory and variability tested. The two types of model execution are process time variation and station failure. Both of these model executions were conducted using both JIT and TOC scheduling on all three of the production systems. There were a total of 12 model executions in this study.

Data Set. The data set for a model execution consisted of 7,200 lines of data. Each data line consists of the output data for the particular simulation run.

Data Acceptability. Even though the systems that are being simulated are purely theoretical, the model executions were evaluated to insure that they were performing as expected. To insure that the data generated by the model execution is as expected the following steps were taken.

1. To insure that each random process in the model encounters a statistically random set of random numbers each process was driven off of a different and unique random number stream. This insured that no process encountered either consistently low or high random numbers during a simulation run.

2. The results of the JIT model executions were compared against the results achieved in previous JIT performance evaluation efforts (Lulu, 1986; Lulu & Black, 1987).

Data Analysis. A point estimate for the throughput mean and standard error of the mean was calculated using the
data of each set-point group. The point estimate consists of the calculation of the average throughput for the set-point group and the sample variance of the throughput. These values were then utilized to calculate upper and lower confidence limits. Since the sample size was n=100 then, through the Central Limit Theorem, it can be assumed that the mean throughput is normally distributed (Devore, 1987:212-214). Since the mean throughput is approximately normally distributed the confidence limits were calculated using the standard normal distribution. Confidence limits were calculated around each of the estimation points. For equal levels of work-in-process, equi-inventory group data for the TOC model was compared to the JIT model for each of the systems and both types of variability using graphical comparison. The confidence limits were be graphed along with the average throughput for each level of variability to determine if the mean throughputs are statistically different. The hypothesis was that the TOC scheduled system would yield higher throughput than the JIT scheduled system. If the confidence limits for the mean values do not overlap then it can be assumed with 95 percent confidence that they are not equivalent and the scheduling methodology with the larger average throughput yielded superior performance.

The production systems were compared using only the TOC scheduling methodology to determine if the flow of the system affects the resulting throughput. System 1, System 2, and Product 1 of System 3 all utilize essentially the
same longest path processing times so comparison between these throughputs will be made. These comparisons were again made graphically using equi-inventory group data for the equivalent buffer size setting for each of the systems. The hypothesis was that there would be no difference in the throughput due to differing system flow.

Statement of Decision Rules. The Type I Error that was allowed is 0.05 level of significance. This indicates that the level of confidence is 95 percent. If the expected throughput for the JIT scheduled systems are less than this 95 percent confidence level then the hypothesis that the expected throughput of the TOC scheduled system is greater than systems scheduled with other methodologies will not be rejected.
IV. Results and Analysis

Introduction

This research effort was to investigate and compare the effects of system variability on systems scheduled using both Just-in-Time (JIT) and the Theory of Constraints (TOC). This chapter provides the results of the execution of the experimental design developed in the previous chapter. The data generated by the simulation models will be analyzed for both the JIT and TOC models, and then the results will be compared at the lower equivalent work-in-process (WIP) levels. The analysis and comparison will be conducted in accordance with the experimental design outlined in the previous chapter. The experimental design was modified slightly by additional simulation runs of System 1, both JIT and TOC models, for larger variability of processing time. The additional runs were conducted to investigate a downward trend of the JIT model that was noticed at the 40 percent variability level. The analysis will be conducted for each of the three systems separately, then the results of the TOC models for each of the systems will be compared. For each system the effects of process time variability will first be analyzed for both scheduling methodologies. Then the results for the scheduling methodologies will be compared. This sequence will then be repeated for variability of process station failure.
Findings

System 1. Internal to the system models (Appendix A and B) the buffer size was set at a value ranging between 1 and 8; this setting of the buffer size caused the maximum work-in-process (WIP) level for the JIT system to be greater than the level of the TOC system. For example, for a buffer size of 1 the JIT system would be capable of having one unit of product in each of the four process stations so the maximum WIP level is 4. The TOC system can have only 1-unit in Stations 1 and 2, 1-unit in Station 3, and 1-unit in Station 4 for a total of 3-units. So for a buffer size of 1 the JIT system will have a WIP level of 4 while the TOC system has a WIP level of 3. This difference, due to the buffering arrangement of the methodology, can be seen in Table 4-1. Table 4-1 also contains the line legend for the graphs of the System 1 and 2 results.

Process Time Variability. The process time variability value is the percent variability around the mean processing time for the station. For example, for a processing station with a mean of 20 minutes and a variability value of 0.2 or 20 percent, the actual time can range between 16 and 24 minutes. The percent variability ranged from 0 to 40 for the model executions. A baseline throughput value was generated by running a model with no variability. For both of the model executions the baseline throughput value was 480 units, which was the expected value for the system.
### TABLE 4-1

**WORK-IN-PROCESS LEVELS AND GRAPH LEGEND - SYSTEMS 1 AND 2**

<table>
<thead>
<tr>
<th>Buffer Size</th>
<th>JIT WIP Level</th>
<th>TOC WIP Level</th>
<th>Graph Line</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>6</td>
<td>4</td>
<td></td>
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<tr>
<td>3</td>
<td>8</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>10</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>12</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>14</td>
<td>8</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>16</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>18</td>
<td>10</td>
<td></td>
</tr>
</tbody>
</table>

**JIT with Kanban.** The results of this model execution were compared with the results of the 1987 study of the same type by Lulu and Black, and the results of both this and the Lulu and Black study are essentially identical. The finding of the Lulu and Black study was that a JIT system was not significantly affected by process time variability (Lulu and Black, 1987:215); this same result can be seen in Figure 4-1. The lines for the different levels
of WIP vary some around the baseline throughput value of 480 units, but there are no significant deviations from the baseline value. There is a slight drop in the throughput of the lowest WIP level, buffer size 1, in the 35 to 40 percent variability range. This drop will be investigated further in the analysis of the data. The program which generated the Figure 4-1 data is in Appendix A.

Figure 4-1. System 1 - JIT - Process Time Variability
TOC – Drum-Buffer-Rope (DBR). There are no previous published studies which evaluate DBR systems to provide a comparative baseline for the results. The only level that deviates from the results of the JIT model execution is the lowest WIP level which drops sharply below the baseline value (Figure 4-2). This result was achieved at a WIP level of 3-units, buffer size 1, and is due to the starvation of units to be processed by the constraint. The buffering of the DBR control methodology caused the initial two processing stations to, in effect, become one station equal in processing time to the constraint. The specification of a buffer size of 1-unit stipulated that only one unit could be between the material release point and the constraint. As the variability of the processing time increased the throughput of the system was disrupted since the system constraint was not fixed. The constraint could be either the normal constraint, Station 3, or the constraint created by the combination of Stations 1 and 2 depending on the actual processing times for the stations. The combination of Stations 1 and 2 into a constraint created a situation where the buffer for the normal constraint worked against achieving the baseline throughput. This situation illustrates the importance of properly sizing the system buffer and reducing the variability of the system which are both part of the TOC philosophy. The program which generated the data for Figure 4-2 is in Appendix B.
Comparison of JIT and TOC. The comparison of the two scheduling systems was conducted at the lowest two levels of work-in-process (4 and 6-units) for the JIT model. To avoid a confound, equivalent inventory levels were used for comparison. Since the philosophy of both methodologies emphasizes the minimization of WIP in the system the comparison at higher levels is not consistent with the philosophy. It can also be seen from the previous graphs (Figures 4-1 and 4-2) that for high levels of WIP, both
methodologies produce the baseline throughput for all levels of variability.

At the 4-unit level it can be seen from the graph (Figure 4-3) that, at process time variability of less than 35 percent, the two scheduling methodologies produce similar results that are not statistically different. At levels of variability greater than 35 percent the TOC system, large solid line, produces throughput that is higher than the JIT system, large dotted line, and the difference is statistically significant ($\alpha = 0.05$) since the confidence intervals do not overlap.

![Graph showing throughput vs. percent variability for TOC and JIT systems](image)

*Figure 4-3. System 1 - Comparison at WIP = 4-units - Process Time Variability*
It can also be seen that while the TOC throughput remains at essentially the baseline value at the 40 percent variability level the JIT throughput begins to diverge. These systems were run again with the WIP inventory set at 4 units and the variability ranging from 0 to 75 percent. The results of this additional equi-inventory group run can be seen in Figure 4-4.

![Figure 4-4. System 1 - WIP = 4-units - High Process Time Variability](image)

It can be seen from this graph that at very high levels of variability the TOC system significantly outperforms the JIT system. The deleterious impact of variability is
acknowledged by the variability reduction techniques which are inherent in both philosophies.

The comparison between JIT and TOC at 6 units of WIP was conducted only over the variability range from 0 to 40 percent. It can be seen from the graph (Figure 4-5) that there is no statistical difference between the two systems at this level of WIP inventory. The oscillations around the baseline level of throughput are normal experimental error as the baseline value is always within the confidence interval for both systems.

![Figure 4-5. System 1 - Comparison at WIP = 6-units - Process Time Variability](image)
Probability of Station Failure. The probability of failure value is the probability that the process station will experience a failure when a unit attempts to enter. As in the previous tests, the baseline throughput value was 480 units.

The line legend for all of the graphs of probability of station failure is in Table 4-1.

JIT with Kanban. The throughput of the JIT system was degraded as the probability of station failure increased (Figure 4-6). This is consistent with results documented by Lulu (1986:237). While the throughput did increase as the WIP level increased the level did not reach the baseline level of 480 units in any of the trials for high probability of failure values. The throughput values seem to be converging on a single value, so that as even higher levels of WIP are used the throughput curve does not change. This is the expected result since as the WIP level increases the availability of material in the system is no longer a limiting factor and the time required to return the stations to full operational capability begins to dictate the throughput of the system. This type of degradation of throughput illustrates the importance of the system reliability aspects that are inherent in the JIT philosophy. It can be seen from Figure 4-6 that as long as the probability of a station failure is small the throughput remains at the baseline value even for low WIP values.
The program which generated the data for Figure 4-6 is in Appendix A.

![Diagram showing Throughput vs Probability of Failure](image)

**Figure 4-6. System 1 - JIT - Station Failure**

**TOC - Drum-Buffer-Rope.** The results of this model execution are similar to the results achieved by the JIT model. For high probabilities of failure the throughput does not reach the baseline value even for very high levels of WIP (Figure 4-7). The values of the throughput, as in the JIT system, appear to be approaching a constant value for a particular probability of failure.
The program which generated the data for Figure 4-7 is in Appendix B.

Comparison of JIT and TOC. The comparison between the two methodologies was conducted at 4 and 6 units of WIP and results illustrated in Figures 4-8 and 4-9. The JIT throughput curve is the heavy dotted line and the TOC curve is the heavy solid line. The confidence interval lines can not be seen clearly in these graphs due to the very narrow width of the confidence interval and the large
scale required by the throughput values. The data for Figures 4-8 and 4-9 was generated by the programs in Appendices A and B.

At the 4-unit level the TOC system achieves a higher throughput than the JIT system for all probabilities of failure (Figure 4-8). The difference between the curves is statistically significant at the 95 percent confidence level ($\alpha = 0.05$).

![Figure 4-8. System 1 - Comparison at WIP = 4-units - Station Failure](image)
At the 6-unit level of WIP the TOC system again achieves a higher throughput for all probability values of station failure (Figure 4-9). The curves again drop off significantly below the baseline value as the probability of failure increases. Since the confidence intervals for the two curves do not overlap the difference between the scheduling methodologies is statistically significant ($\alpha = 0.05$).

![Throughput vs Probability of Failure](image)

**Figure 4-9. System 1 - Comparison at WIP = 6-units - Station Failure**
System 2. The results from the model executions for System 2 were essentially identical to the results obtained from the System 1 model executions. The buffer sizing and graph line legend is the same as in System 1 so it will not be repeated here. The WIP level for the JIT system again ranged from 4 units (buffer size = 1) to 18 units (buffer size = 8) in increments of 2 units; the TOC system's WIP ranged from 3 units to 10 units in increments of 1 unit.

Process Time Variability

JIT with Kanban. The results of this model execution appear in Figure 4-10. The shape of the curve and the values obtained in the point estimates are essentially the same as that of the System 1 execution. The program which generated this data is in Appendix C.

It can be seen in Figure 4-10 that the throughput is essentially constant and not dependent on process time variability. The only exception is at the WIP level of 4 units where the throughput begins to drop at very high levels of variability. This drop was investigated previously in System 1 so it will not be repeated for System 2, but the results are expected to be similar. The remaining WIP levels only vary about the baseline value and do not appear to be affected by the variability.
Figure 4-10. System 2 - JIT - Process Time Variability

TOC - Drum-Buffer-Rope. The only significant feature of the throughput graph (Figure 4-11) for this model execution is the drop in throughput for the lowest WIP level. This drop was discussed above in System 1 and there is no change for System 2. The remaining WIP levels maintain the baseline throughput for all levels of variability. The program which generated this data is in Appendix D.
Comparisons of JIT and TOC. The results of this comparison are the same as System 1 so only the 4-unit level of WIP will be analyzed. The throughput of the TOC system (solid line) maintains the baseline value for all levels of variability (Figure 4-12). The JIT system, dotted line, begins to drop from the baseline value at the 35 percent variability level and by the 40 percent level the difference between the two systems is statistically significant ($\alpha = 0.05$).
Throughput

Figure 4-12. System 2 - Comparison at WIP = 4-units -
Process Time Variability

Probability of Station Failure

JIT with Kanban. The results of this model
execution are essentially the same as was obtained in System
1. If additional information is required the model which
generated the data is in Appendix C.

None of the WIP levels provided complete protection for
throughput and so there was some degradation as the
probability of failure increased. It can be seen in Figure
4-13 that the lower the level of WIP the greater the

4-18
reduction in throughput. This degradation is very similar to that seen in the previous System 1 analysis for the same levels of failure probability. For low levels of WIP the JIT system essentially shuts down when a failure occurs and there is no product to move through the processing station to the next buffer. For high levels of WIP the repair times for the stations begin to control the amount of possible throughput.

Figure 4-13. System 2 - JIT - Station Failure
**TOC - Drum-Buffer-Rope.** The results of this model are similar to the previous process station failure models. For all levels of WIP the throughput begins to degrade as the probability of failure increases (Figure 4-14). As in the System 1 analysis, this is the expected result due to the starvation of the constraint caused by station failure in the initial processing stations and the increased flow time caused by the inclusion of station repair time.

![Figure 4-14. System 2 - TOC - Station Failure](image-url)
Comparison of JIT and TOC. The results of this comparison and the System 1 analysis are similar as can be seen by a comparison of Figures 4-8 and 4-15. Due to the similarity, this comparison will be accomplished only at the 4-units of WIP level. The results of a comparison at the 6-unit level are expected to be similar to those obtained for System 1.

At the 4-unit level of WIP the results are, as expected, closely parallel to those of System 1. The TOC scheduled system significantly outperforms the JIT system. The difference between the results is statistically significant at the \( \alpha = 0.05 \) level.

![Figure 4-15. System 2 - Comparison at WIP = 4-units - Station Failure](image-url)
System 3. The analysis of System 3 reviews not only the total throughput of the system, but also the throughput of each of the individual products. The results of the System 3 model executions is similar to those seen in the previous systems, but there are differences brought about by the interaction of the two products produced by the system. The buffer size and graph line legend is in Table 4-2 and is applicable to all System 3 figures.

TABLE 4-2
WORK-IN-PROCESS LEVELS AND GRAPH LEGEND - SYSTEM 3

<table>
<thead>
<tr>
<th>Buffer Size</th>
<th>JIT WIP Level</th>
<th>TOC WIP Level</th>
<th>Graph Line</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>7</td>
<td>6</td>
<td>-----------</td>
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<tr>
<td>2</td>
<td>10</td>
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<td>8</td>
<td>28</td>
<td>20</td>
<td>-----------</td>
</tr>
</tbody>
</table>

4-22
Process Time Variability. The effects of process time variability on this system are analyzed from the perspective of both the total throughput of the system and individual products produced by the system.

JIT with Kanban. The result of this model execution show a degradation of the total throughput of the system that was not experienced in the previous systems (Figure 4-16). For the lowest WIP level (7-units) the throughput decreased from the baseline value of 864-units to 849-units at 40 percent variability. The program which generated the data is in Appendix E.

![Graph of Throughput vs. Percent Variability](image-url)

Figure 4-16. System 3 - JIT - Total Throughput - Process Time Variability

4-23
The degradation in the total throughput of the system can be attributed to the degradation experienced by Product 1. Figure 4-17 shows that the throughput of Product 1 decreased as the amount of variability increased, while Figure 4-18 shows that there was no decrease in the throughput of Product 2. The throughput of Product 2 also does not exhibit the decrease in throughput that was experienced in the previous systems in the 35 to 40 percent variability range.

Figure 4-17. System 3 - JIT - Product 1 Throughput - Process Time Variability
Product 2 may have been able to maintain the baseline throughput value due to the lower processing times in the initial stations for the unique subcomponent in Product 2. Since the unique subcomponent finished initial processing faster than the unique subcomponent for Product 1, Product 2 was able to consume the common subcomponent before Product 1. This research effort did not investigate the cause of this finding to determine the exact cause of the irregularity since it was not pertinent to the comparative study.

![Figure 4-18. System 3 - JIT - Product 2 Throughput - Process Time Variability](image-url)
TOC - Drum-Buffer-Rope. The results of this model execution show the characteristic drop in throughput for the lowest WIP level that has been experienced with the previous models. The drop for the total throughput of the system goes 864-units down to 813-units (Figure 4-19). As in the previous JIT model this drop is caused by the drop in the Product 1 throughput and not Product 2. If further information is required on this model the program which generated the data is in Appendix F.

![Graph](image-url)

Figure 4-19. System 3 - TOC - Total Throughput - Process Time Variability
The drop in Product 1 throughput for the lowest WIP level is equal to amount of the drop in the total throughput (Figure 4-20). This drop is consistent with that experienced by the previous TOC models for Systems 1 and 2. An in-depth analysis is made later in this chapter when the performance of the TOC models of each system is compared.

The throughput of Product 2 maintained the baseline value for all levels of WIP and amount of variability (Figure 4-21). This result is very similar to that obtained
from the previous JIT model, but the cause of this anomaly can not be the same as the JIT model since the subcomponents for the TOC model are product designated at the initial release of material. The lower initial processing times for both subcomponents may account for the product maintaining the baseline throughput level.

**Figure 4-21. System 3 - TOC - Product 2 Throughput - Process Time Variability**

Comparison of JIT and TOC. The comparison of these systems is made for only the total throughput of the system. The baseline throughput for the two products under
each of the scheduling methodologies is the same and the reaction of the products is independent of the scheduling methodology selected. Therefore, the comparison of the total throughput will yield an overall trend in the performance of the methodologies.

The comparison of the results of these models at low levels of WIP for this system was complicated by the buffering systems of the methodologies. The first WIP level that is common to both models is at the 10-unit level which for the JIT model is a buffer size of 2, while for the TOC model it is a buffer size of 3. Previous comparisons at this level of WIP have yielded inconclusive results since both models maintain the baseline throughput except for the lowest level of WIP.

The initial comparison for this system is made the lowest levels for both systems. The JIT level of WIP is 7-units, while the throughput for the 6- and 8-unit levels are shown for the TOC system. Figure 4-22 shows the result of this comparison including the confidence intervals for each of the throughput curves. The result is inconclusive since a direct comparison can not be made with differing WIP levels. The throughput of the TOC and JIT models both decrease with increasing variability at the lowest WIP level for each model while for the next higher level the throughput is maintained at the baseline level.
The throughput at the 10-unit level of WIP is shown in Figure 4-23 for both models. As discussed previously both models maintain the baseline throughput and there is no statistical difference at the 95 percent confidence level (α = 0.05). This is the expected result as has been seen in the comparison of Systems 1 and 2 at levels of WIP above the very lowest levels for the particular system.
Throughput

Probability of Station Failure. The results of this portion of the analysis for System 3 are similar to those obtained from the previous systems when subjected to increasing probability of process station failure. The throughput of both the JIT and TOC models decreases with increasing probability of failure and the increasing WIP level does not fully protect the throughput.
JIT with Kanban. The equi-inventory curves for the total throughput of this model execution show a greater reaction to the increasing failure rate than those of previous systems (Figure 4-24). This drop can be attributed to the increased drop in Product 1 throughput which is not offset by the decreased drop in Product 2 throughput. If further information is required the program which generated the data for this analysis is in Appendix E.

![Figure 4-24. System 3 - JIT - Total Throughput - Station Failure](image)
The Product 1 throughput shows an increased drop for all levels of WIP as the probability of failure increases (Figure 4-25). This drop in throughput is greater than that shown by previous JIT system models. The cause of this increased throughput degradation can probably be attributed to the interaction with Product 2 that was exhibited when the model was executed under conditions of process time variability.

Figure 4-25. System 3 - JIT - Product 1 Throughput - Station Failure
As stated previously, the reaction of Product 2 to increasing probability of failure was not as severe as seen in the model executions of previous systems. Product 2 used its interaction with Product 1 to maintain the baseline throughput for all probability levels except at the lower levels of WIP. Figure 4-26 shows the reaction of Product 2 to increasing probability of failure for various levels of WIP.

Figure 4-26. System 3 - JIT - Product 2 Throughput - Station Failure
TOC - Drum-Buffer-Rope. The reaction of the TOC model to increasing probability of failure is very similar to that seen in previous TOC model executions. The total throughput of the system is degraded for all levels of WIP as the probability of failure increases (Figure 4-27). The increase in WIP can not fully protect the throughput of the system although an increase in throughput is seen as the WIP increases. The convergence of the equi-inventory curves into a single curve is also the same as that seen with previous systems.

![Figure 4-27. System 3 - TOC - Total Throughput - Station Failure](image-url)
If further information is required the program which generated the data used in this analysis is in Appendix F.

The throughput of Product 1 is similar to the general shape of the curves seen in previous TOC model executions for increasing probability of station failure. The curves again converge on a single maximum curve as WIP increases (Figure 4-28). The equi-inventory curves exhibit the same spread between each level of WIP as was seen in previous model executions.

![Throughput vs Probability of Failure](Figure 4-28. System 3 - TOC - Product 1 Throughput - Station Failure)
The throughput of Product 2 differs from that which has been characteristic of other model executions. While the throughput is degraded by increasing probability of failure, the equi-inventory curves converge on a single curve much faster than previous systems (Figure 4-29). This convergence is probably a characteristic of the relationship of the processing times of the stations in the flow of Product 2 since the subcomponents of the two products are independent in the TOC model (Appendix F).

![Figure 4-29. System 3 - TOC - Product 2 Throughput - Station Failure](image-url)
Comparison of JIT and TOC. The comparison of these scheduling methodologies will, as in the process time variability comparison, be made only for the total throughput of the system. The comparison of the throughput of the individual products is unnecessary since this research study is concerned only with the general reaction of the scheduling methodology to specific system variabilities.

The comparison at the lower levels of WIP is again complicated by the buffering of the models. The first level of WIP which is common to both systems is at the 10-unit level which is significantly above the level at which comparisons were made for previous systems. As was done in the comparison for process time variability the graph for the lowest WIP level is presented in Figure 4-30. While the analysis of this graph is inconclusive as to which methodology yields the greater throughput for the lowest level of WIP, a general knowledge can be gained from a visual comparison at these low levels. The TOC model at the 8-units of WIP level yields a greater throughput and provides nearly the baseline throughput for a greater range of failure probability values. The throughput of the TOC model at a WIP level of 8-units also provides an increase in throughput of approximately 50 units over the JIT model for only an increase of 1-unit of WIP.
The comparison at the 10-unit level of WIP is also inconclusive for this particular model as the throughput curves cross at approximately the 0.35 level of probability (Figure 4-31). This indicates that for level of failure less than 0.35 the TOC model provides increased throughput while at higher failure rates the JIT model outperforms the TOC model. This type of result was not expected from the analysis and has not been experienced in previous systems. The interaction of the two products produced by the system could account for this result, due to the differences in the internal buffering of the methodologies.
Comparison of TOC Results. The comparison of the TOC models for each of the three systems are presented to determine if there is any difference due to the structure of the system on the throughput achieved by the TOC scheduling methodology. This analysis will be conducted separately for both types of system variability to determine if the type of variability affects the throughput. The total throughput of Systems 1 and 2 will be used as the critical path through both of these systems is identical. The Product 1 throughput of System 3 will be utilized in the comparison.
since its critical path is again the same as that of the total throughput of Systems 1 and 2.

Process Time Variability. The initial comparison that is conducted is at a buffer size of one unit for each of the systems. This buffer size yields a WIP level of three units for Systems 1 and 2, and six units total for System 3. These 6 units for System 3 are divided evenly between Products 1 and 2. It can be seen in Figure 4-32 that at this level of WIP there is no difference between the systems due to differing flow patterns. This is the expected result for the analysis since there is no difference between the systems in the amount of time required to produce a product.

Figure 4-32. System Comparison - Buffer Size = 1-unit - Process Time Variability
The next comparison for process time variability will be conducted at a buffer size of two units. It can be seen in Figure 4-33 that all of the systems produce the baseline throughput for all levels of process time variability and there is no statistical difference between the systems at the 95 percent confidence level ($\alpha = 0.05$). This result is again what was expected and as could be determined from the previous presentations of the results of the model executions.

![Throughput vs. Percent Variability](image)
Probability of Station Failure. This comparison is conducted at the same buffer sizes as the previous comparison for process time variability. The results of this comparison are more interesting than that of the process time variability due to the interaction of assembling the subcomponents of the product produced by Systems 2 and 3. At the buffer size of 1-unit, Figure 4-34 shows that the throughput of System 1 is statistically greater for all failure probabilities than the throughput of Systems 2 and 3. There is no statistical difference ($\alpha = 0.05$) between the throughput curves for Systems 2 and 3.

![Figure 4-34. System Comparison - Buffer Size = 1-unit - Station Failure](image-url)
Figure 4-35 shows the comparison of the systems at a buffer size of two units. In this case Systems 1 and 2 provide the same throughput with no statistical difference while System 3 throughput is statistically lower for all probability of failure values. This situation could be caused by the interaction of Product 1 with Product 2 in obtaining access to the common processing stations. However, the difference between the throughput curves, while statistically significant at the 95 percent confidence level ($\alpha = 0.05$), is still fairly small when compared to the overall throughput of the models.
V. Conclusions and Recommendations

Introduction

The original intent of this research effort was to answer two specific research questions. The research questions which were posed in Chapter 1 are:

1. Does TOC's Drum-Buffer-Rope (DBR) technique resolve the throughput problems associated with system variability in JIT scheduled systems?

2. Is the improvement in throughput achieved in TOC systems dependent on the flow path of the production system under consideration?

The analysis conducted in the first portion of Chapter 4 where Just-in-Time (JIT) and TOC models were compared addressed the first research question. The comparison conducted between the results of the TOC models at the end of Chapter 4 addresses the second question.

Conclusions

Research Question 1. The results of the analysis conducted in the previous chapter lead to the conclusion that for Systems 1 and 2 the Theory of Constraints (TOC) provides superior stability of throughput under process time variability. When these systems were subjected to process station failure the TOC models provided superior throughput for equivalent amounts of work-in-process (WIP). The results of the System 3 models are inconclusive, but the TOC model does appear to provide equivalent throughput to the JIT model independent of the type of variability.
The analysis conducted under conditions of process time variability show that for System 1 (Figures 4-3 and 4-4) and System 2 (Figure 4-12) the TOC scheduled model provided better throughput stability than the JIT system. As the process time variability percentage increased the JIT scheduled models throughput began to drop below the baseline throughput value. The expanded analysis (Figure 4-4) done on System 1 shows that the decrease continues as the variability increased above the normal level of this study. The results of System 3 showed no differences between JIT and TOC systems. Figure 4-23 shows that at the 10-unit level of WIP both scheduling methodologies provided the baseline throughput over the entire range of variability.

The analysis conducted for process station failure is more conclusive than the process time variability analysis. For Systems 1 and 2 (Figures 4-8, 4-9, and 4-15) the TOC scheduled model outperformed the JIT model by approximately 25-units over a large range of failure probabilities. The TOC system did experience degradation of throughput due to process station failure, but it was not as significantly affected by the failure as the JIT system. The results for System 3 were more inconclusive for process station failure than for process time variability. At the 10-unit level of WIP the TOC system outperformed the JIT system marginally up to the 0.30 probability level and then the JIT system outperformed the TOC system for high probability levels (Figure 4-31). This anomaly could have been due to product 5-2
interaction differences caused by the buffering of the scheduling methodologies. In the JIT system the common subcomponent was released into the system as demanded by the first buffer in its flow path. The TOC system released the common subcomponent as required by the particular product buffer. The common subcomponent in the TOC system was designated at release as to the product requiring the subcomponent. This was not done in the JIT system due to the nature of the JIT buffering.

Research Question 2. The conclusion that can be derived from the results of the process time variability comparison is that these results are not affected by the flow path of the system. The results of the process station failure comparison lead to the conclusion that there is some dependence on the flow path of the system.

Figures 4-32 and 4-33 both show that there is no statistical difference between the throughputs achieved by any of the different systems. The throughput achieved for each of the variability percentages for buffer sizes of one and two units are statistically identical.

When the systems were compared under conditions of process station failure the results were mixed. For a buffer size of one unit System 1 outperformed the other two systems which had statistically identical throughput curves. When the buffer size was increased to two units Systems 1 and 2 had statistically identical throughput curves while System 3 provided significantly lower throughput.
Recommendations

There is significant research that needs to be conducted before the full characteristics of TOC can be verified. This is one of the first independent research efforts that has been conducted on TOC so the opportunity for future research is unlimited.

One of the anomalies that was documented by this research effort was the convergence of the equi-inventory curves on a single curve when subjected to process station failure (Figures 4-6, 4-7, 4-14, and 4-27). This convergence should be investigated further to determine the exact cause of the phenomenon.

The analysis of System 3 in this research also illustrated several product interaction effects that could have a significant impact on an actual production system. Few production systems produce a single product so the determination of the causes and effects of product interaction would significantly aid the production manager in effectively scheduling product flow.

The final area in which this research should be expanded is into an actual production system. The researcher could develop and validate a simulation model using the current production scheduling system. This model could then be used to compare the effects of JIT and TOC scheduling on an actual production system without the cost
and disruption caused by experimenting with the actual system.

This research effort is simply the starting point for many future research efforts that are needed by before any conclusive statement can be made as to the relative effectiveness of the Theory of Constraints scheduling methodology. TOC appears to have partially resolved some of the variability problems associated with JIT, but a great deal of future research is required using both theoretical and actual production systems.
Appendix A: System 1 - JIT - GPSSH Program Listing

REALLOCATE COM,150000

SIMULATE

Variable Declaration Section

******************************************************************************

Variable Definitions

******************************************************************************

&I, &J - Loop Counters
&BFSZ - Defined Buffer Size
&BUFF1 - Buffer Counter for Buffer 1
&BUFF2 - Buffer Counter for Buffer 2
&BUFF3 - Buffer Counter for Buffer 3
&POF - Defined Probability of Station Failure
&DELT - Percent Variability of Processing Time
&MN1 - Mean Processing Time for Station 1
&MN2 - Mean Processing Time for Station 2
&MN3 - Mean Processing Time for Station 3
&MN4 - Mean Processing Time for Station 4
&MMEAN1 - Calculated Actual Processing Time for Station 1
&MMEAN2 - Calculated Actual Processing Time for Station 2
&MMEAN3 - Calculated Actual Processing Time for Station 3
&MMEAN4 - Calculated Actual Processing Time for Station 4

******************************************************************************

INTEGER &I,&J
INTEGER &BFSZ,&BUFF1,&BUFF2,&BUFF3
REAL &POF,&MN1,&MN2,&MN3,&MN4
REAL &MMEAN1,&MMEAN2,&MMEAN3,&MMEAN4,&DELT

******************************************************************************

Declaration of Output File

******************************************************************************

OUTA FILEDEF 'THSJ1A1.OUT'
Variable Assignment Section

Definition of Mean Processing Times

GPSS/H Block Section

Beginning of product flow

Process 1
* Buffer 1
*
* ENTER BFFR1 Enter Buffer 1
* TEST NE &BUFF2,&BFSZ Check capacity of Buffer 2
* BLET &BUFF2=&BUFF2+1 Increment Buffer 2 counter
* TEST E F(STA2),0 Check status of Sta 2
* BLET &BUFF1=&BUFF1-1 Decrement Buffer 1 counter
* LEAVE BFFR1 Leave Buffer 1
*
* Process 2
*
* SEIZE STA2
* TEST LE FRN(4),&POF,STRT2
* FUNAVAIL PRCS2
* ADVANCE 2*&MN2
* FAVAIL PRCS2
* STRT2 SEIZE PRCS2
*
* BLET &MEAN2=&MN2+((FRN(5)-0.5)*2)*&MN2*DELT
* ADVANCE &MEAN2
* RELEASE PRCS2
* RELEASE STA2
*
* Buffer 2
*
* ENTER BFFR2
* TEST NE &BUFF3,&BFSZ
* BLET &BUFF3=&BUFF3+1
* TEST E F(STA3),0
* BLET &BUFF2=&BUFF2-1
* LEAVE BFFR2

A-3
Process 3

**SEIZE STA3**

**SEIZE PRCS3**

**BLET &MEAN3=&MN3+(((FRN(7)-0.5)*2)*&MN3*DELT)**

**ADVANCE &MEAN3**

**RELEASE PRCS3**

**RELEASE STA3**

Buffer 3

**ENTER BFFR3**

**TEST E F(STA4),0**

**BLET &BUFF3=&BUFF3-1**

**LEAVE BFFR3**

Process 4

**SEIZE STA4**

**TEST LE FRN(8),&POF,STRT4**

**FUNAVAL PRCS4**

**ADVANCE 2*&MN4**

**FAVAIL PRCS4**

**STRT4 SEIZE PRCS4**

**BLET &MEAN4=&MN4+(((FRN(9)-0.5)*2)*&MN4*DELT)**

**ADVANCE &MEAN4**

**RELEASE PRCS4**

**RELEASE STA4**

**DEPART SYSQ**

**PDCT TERMINATE 0** Terminate the XACT

A-4
* Model Timing
  * Run model for 40 hour week

  GENERATE 60.*8.*5.
  TERMINATE 1

******************************************************************************
* GPSS/H Control Statements
******************************************************************************

Process Time Variability (&DELT) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &DELT=0.0

Probability of Station Failure (&POF) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &POF=0.0

LET &BFSZ=1 Buffer size initialized
DO &J=1,8
  BFFR1 STORAGE &BFSZ
  BFFR2 STORAGE &BFSZ
  BFFR3 STORAGE &BFSZ
  DO &I=1,100 100 iterations at each set-point
    LET &BUFF1=0
    LET &BUFF2=0
    LET &BUFF3=0
  START 1,NP 40 hour warm-up period
  RESET
  START 4,NP 160 hour data gathering period

Output of data to file

PUTPIC FILE=OUTA,(&DELT,&POF,N(PDCT),QM(SYSQ))

CLEAR
ENDDO
LET &BFSZ=&BFSZ+1 Increment Buffer Size
ENDDO
END
Appendix B: System 1 - TOC - GPSSH Program Listing

REALLOCATE COH,150000

SIMULATE

Variable Declaration Section

******************************************************************************

Variable Definitions

******************************************************************************

&I, &J - Loop Counters
&BSZ - Defined Buffer Size
&BUFF - Buffer Counter for System Buffer
&POF - Defined Probability of Station Failure
&DELT - Percent Variability of Processing Time
&MN1 - Mean Processing Time for Station 1
&MN2 - Mean Processing Time for Station 2
&MN3 - Mean Processing Time for Station 3
&MN4 - Mean Processing Time for Station 4
&MEAN1 - Calculated Actual Processing Time for Station 1
&MEAN2 - Calculated Actual Processing Time for Station 2
&MEAN3 - Calculated Actual Processing Time for Station 3
&MEAN4 - Calculated Actual Processing Time for Station 4

******************************************************************************

INTEGER &I,&J
INTEGER &BSZ,&BUFF
REAL &POF,&MN1,&MN2,&MN3,&MN4
REAL &MEAN1,&MEAN2,&MEAN3,&MEAN4,&DELT

******************************************************************************

Declaration of Output File

******************************************************************************

OUTA FILEDEF 'THSC1A1.OUT'

******************************************************************************
Variable Assignment Section

Definition of Mean Processing Times

\[\begin{align*}
    \text{LET } \&M1 &= 7.5 \\
    \text{LET } \&M2 &= 12.5 \\
    \text{LET } \&M3 &= 20.0 \\
    \text{LET } \&M4 &= 5.0
\end{align*}\]

GPSS/H Block Section

\[
\begin{align*}
\text{GENERATE } 0,0 & \quad \text{Generate a XACT whenever the input buffer is empty} \\
\text{SEIZE } \text{INBUF} & \quad \text{Enter the input buffer}
\end{align*}\]

Beginning of product flow

\[
\begin{align*}
\text{TEST NE } \&BUFF,\&BFSZ & \quad \text{Test for room in Buffer} \\
\text{MLET } \&BUFF=\&BUFF+1 & \quad \text{Increment Buffer Counter} \\
\text{TEST E } F(\text{STA1}),0 & \quad \text{Test Status of Station 1} \\
\text{RELEASE } \text{INBUF} & \quad \text{Leave Input buffer}
\end{align*}\]

\[\text{QUEUE } \text{SYSQ} \quad \text{Enter System queue}\]

Process 1

\[
\begin{align*}
\text{SEIZE } \text{STA1} & \quad \text{Enter Station 1} \\
\text{TEST LE } \text{FRN}(2),\&POF,\text{STRT1} & \quad \text{Test Failure of Sta 1} \\
\text{FUNAVAIL } \text{PRCS1} & \quad \text{Make Sta 1 unavailable} \\
\text{ADVANCE } \&M1 & \quad \text{Repair Station 1} \\
\text{FAVAIL } \text{PRCS1} & \quad \text{Make Sta 1 Available} \\
\text{STRT1 SEIZE } \text{PRCS1} & \quad \text{Enter Process 1} \\
\text{BLET } \&\text{MEAN1}=\&M1+((\text{FRN}(3)-0.5)^2)*\&M1*\&DELT) & \quad \text{Advance} \\
\text{ADVANCE } \&\text{MEAN1} & \quad \text{Release PRCS1} \\
\text{RELEASE } \text{PRCS1} & \quad \text{Leave Station 1}
\end{align*}\]
Process 2

SEIZE STA2
TEST LE FRN(4),&POF,STRT2
FAVAIL PRCS2
ADVANCE 2*MN2
FAVAIL PRCS2

STRT2 SEIZE PRCS2

BLET &MEAN2=0.5+((FRN(5)-0.5)^2)*&MN2*&DELT)
ADVANCE &MEAN2
RELEASE PRCS2
RELEASE STA2

System Buffer

ENTER BFFR Enter the system buffer
TEST E F(STA3),0' Check status of Sta 3
BLET &BUFF=BUFF-1 Decrement buffer counter
LEAVE BFFR Leave the system buffer

Process 3

SEIZE STA3
SEIZE PRCS3

BLET &MEAN3=0.5+((FRN(7)-0.5)^2)*&MN3*&DELT)
ADVANCE &MEAN3
RELEASE PRCS3
RELEASE STA3
Process 4

SEIZE STA4
TEST LE FRN(8),&POF,STRT4
FNAVAIL PRCS4
ADVANCE 2*MN4
FNAVAIL PRCS4

STRT4 SEIZE PRCS4

BLET &MEAN4=MN4+((FRN(9)-0.5)*2*MN4*DEL5)
ADVANCE &MEAN4
RELEASE PRCS4
RELEASE STA4

DEPART SYSQ Depart the system queue

PDCT TERMINATE 0 Terminate the XACT

Model Timing

Run model for 40 hour week

GENERATE 60.*8.*5.
TERMINATE 1

GPSS/H Control Statements

Process Time Variability (&DEL5) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

Processing Time Variability = 0.00%

LET &DEL5=0.0

Probability of Station Failure (&POF) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &POF=0.0
LET &BFSZ=1 Buffer size initialized
DO &J=1,10

BFFR STORAGE &BFSZ Buffer storage set to &BFSZ
DO &I=1,100 100 iterations at each set-point

LET &BUFF=0
START 1,NP 40 hour warm-up period
RESET
START 4,NP 160 hour data gathering

* Output of data to file

PUTPIC FILE=OUTA,(&DELT,&POF,N(PDCT),QM("VSQ"))

CLEAR
ENDDO
LET &BFSZ=&BFSZ+1
ENDDO
END

B-5
REALLOCATE COM, 150000

SIMULATE

Variable Declaration Section

Variable Definitions

&I, &J - Loop Counters
&BFSZ - Defined Buffer Size
&BUFF1A - Buffer Counter for Buffer 1A
&BUFF1B - Buffer Counter for Buffer 1B
&BUFF2A - Buffer Counter for Buffer 2A
&BUFF2B - Buffer Counter for Buffer 2B
&BUFF3 - Buffer Counter for Buffer 3
&POF - Defined Probability of Station Failure
&D'LT - Percent Variability of Processing Time
&MN1A - Mean Processing Time for Station 1A
&MN1B - Mean Processing Time for Station 1B
&MN2A - Mean Processing Time for Station 2A
&MN2B - Mean Processing Time for Station 2B
&MN3 - Mean Processing Time for Station 3
&MN4 - Mean Processing Time for Station 4
&MEAN1A - Calculated Actual Processing Time for Station 1A
&MEAN1B - Calculated Actual Processing Time for Station 1B
&MEAN2A - Calculated Actual Processing Time for Station 2A
&MEAN2B - Calculated Actual Processing Time for Station 2B
&MEAN3 - Calculated Actual Processing Time for Station 3
&MEAN4 - Calculated Actual Processing Time for Station 4
&MWIP - Maximum Work-in-Process

INTEGER &I
INTEGER &J
INTEGER &BFSZ, &BUFF1A, &BUFF1B, &BUFF2A, &BUFF2B, &BUFF3
REAL &POF, &MN1A, &MN1B, &MN2A, &MN2B, &MN3, &MN4
REAL &MEAN1A, &MEAN1B, &MEAN2A, &MEAN2B
REAL &MEAN3, &MEAN4, &DELT
REAL &MWIP
Declaration of Output File

OUTA FILEDEF 'THSJ2A1.OUT'

Variable Assignment Section

Definition of Mean Processing Times

\[
\begin{align*}
\text{LET} & \quad & \&\text{MN}1\text{A} = 7.5 \\
\text{LET} & \quad & \&\text{MN}1\text{B} = 5.0 \\
\text{LET} & \quad & \&\text{MN}2\text{A} = 12.5 \\
\text{LET} & \quad & \&\text{MN}2\text{B} = 7.5 \\
\text{LET} & \quad & \&\text{MN}3 = 20.0 \\
\text{LET} & \quad & \&\text{MN}4 = 5.0
\end{align*}
\]

GPSS/H Block Section

Subcomponent A Assembly

Beginning of product flow

\[
\begin{align*}
\text{GENERATE} & \quad 0, 0 \quad \text{Generate a XACT whenever the input buffer A is empty} \\
\text{SEIZE} & \quad \text{INBUFA} \quad \text{Seize input buffer A}
\end{align*}
\]

\[
\begin{align*}
\text{TEST NE} & \quad & \&\text{BUFF}1\text{A}, \&\text{BUFF}1\text{A} \quad \text{Test for room in Buffer 1A} \\
\text{BLET} & \quad & \&\text{BUFF}1\text{A} = \&\text{BUFF}1\text{A} + 1 \quad \text{Increment Buffer counter} \\
\text{TEST E} & \quad & \&\text{F(STA1A)}, 0 \quad \text{Test status of Station 1A} \\
\text{RELEASE} & \quad & \text{INBUFA} \quad \text{Release input buffer A}
\end{align*}
\]

\[
\begin{align*}
\text{QUEUE} & \quad & \text{SYSQ} \quad \text{Enter the system queue} \\
\text{QUEUE} & \quad & \text{SUBAQ} \quad \text{Enter the subcomponent A queue}
\end{align*}
\]
***************

* 

** Process 1A **

******

SEIZE STA1A Seize Station 1A
TEST LE FRN(2),&POF,SRT1A Test for failure of station
FUNAVAIL PRCS1A Make process unavailable
ADVANCE 2*&MN3 Repair delay time
FAVAIL PRCS1A Make process available

SRT1A SEIZE PRCS1A Seize Process 1A

BLET &MEAN1A=((FRN(3)-0.5)*2)*&MN1A*DELT)
ADVANCE &MEAN1A
RELEASE PRCS1A
RELEASE STA1A Release Station 1A

***************

* 

** Buffer 1A **

******

ENTER BFR1A Enter the buffer
TEST NE &BUFF2A,&BFSZ Test for room in next buffer
BLET &BUFF2A=&BUFF2A+1 Increment next buffer counter
TEST E F(STA1A),0 Test status of station
BLET &BUFF1A=&BUFF1A-1 Decrement present buffer counter
LEAVE i 'RIA Leave buffer

***************

* 

** Process 2A **

******

SEIZE STA2A
TEST LE FRN(4),&POF,SRT2A
FUNAVAIL PRCS2A
ADVANCE 2*&MN3
FAVAIL PRCS2A

SRT2A SEIZE PRCS2A

BLET &MEAN2A=((FRN(5)-0.5)*2)*&MN2A*DELT)
ADVANCE &MEAN2A
RELEASE PRCS2A
RELEASE STA2A

C-3
Buffer 2A

---

ENTER BFR2A Enter the buffer
ADVANCE 0
GATE LS SUBA On "SET" go through gate
LOGIC R SUBA "RESET" gate
BLET &BUFF2A=&BUFF2A-1 Decrement Buffer counter
LEAVE BFR2A Leave buffer

DEPART SYSQ Leave System queue
DEPART SUBAQ Leave subcomponent A queue
TERMINATE 0 Terminate subcomponent A

---

Subcomponent B Assembly

---

GENERATE 0,0
SEIZE INBUF

Beginning of product flow

TEST NE &BUFF1B,&BFZ
BLET &BUFF1B=&BUFF1B+1
TEST E F(STA1B),0
RELEASE INBUF

QUEUE SYSQ
QUEUE SUBBQ
***************
*               *
*  Process 1E   *
*               *
***************
*                *
* SEIZE          *
* STA1B          *
* TEST LE        *
* FRN(6),&POF,SRT1B *
* FUNAVAL        *
* PRCS1B         *
* ADVANCE        *
* 2* &MN3        *
* FAVAIL         *
* PRCS1B         *
* SRT1B SEIZE    *
* PRCS1B         *
* BLET           *
* &MEAN1B= &MN1B+(((FRN(7)-0.5)*2)*&MN1B* &DELT) *
* ADVANCE        *
* &MEAN1B        *
* RELEASE        *
* PRCS1B         *
* RELEASE        *
* STA1B          *
***************
*                *
* Buffer 1B      *
*                *
***************
*                *
* ENTER          *
* BFR1B          *
* TEST NE        *
* &BUFF2B, &BFSZ *
* BLET           *
* &BUFF2B=&BUFF2B+1 *
* TEST E         *
* F(STA2B),0     *
* BLET           *
* &BUFF1B=&BUFF1B-1 *
* LEAVE          *
* BFR1B          *
***************
*                *
* Process 2B     *
*                *
***************
*                *
* SEIZE          *
* STA2B          *
* TEST LE        *
* FRN(8),&POF,SRT2B *
* FUNAVAL        *
* PRCS2B         *
* ADVANCE        *
* 2* &MN3        *
* FAVAIL         *
* PRCS2B         *
* SRT2B SEIZE    *
* PRCS2B         *
* BLET           *
* &MEAN2B= &MN2B+(((FRN(9)-0.5)*2)*&MN2B* &DELT) *
* ADVANCE        *
* &MEAN2B        *
* RELEASE        *
* PRCS2B         *
* RELEASE        *
* STA2B          *

C-5
**Buffer 2B**

```
ENTER BFR2B
TEST NE SE(BFR2A),1 Test for availability of subcomponent A

TEST NE &BUFF3,&BFSZ Test for room in next buffer
BLET &BUFF3=&BUFF3+1 Increment buffer 3 counter
TEST E F(STA3),0 Test status of Sta 3
BLET &BUFF2B=&BUFF2B-1 Decrement buffer counter
LOGIC S SUBA "SET" subcomponent A gate
LEAVE BFR2B

DEPART SUBBQ
```

**Joining of Subcomponents A and B**

```
QUEUE ASSEMQ Enter the assembly queue

Process 3

```

```
SEIZE STA3
SEIZE PRCS3
BLET &MEAN3=&MN3+((FRN(10)-0.5)*2)*&MN3*&DELT)
ADVANCE &MEAN3
RELEASE PRCS3
RELEASE STA3
```
******************************

* Buffer 3
*
******************************

* *
* ENTER BFFR3
* TEST E F(STA4),0
* BLET &BUFF3=&BUFF3-1
* LEAVE BFFR3
* *
*
******************************

* Process 4
*
******************************

* *
* SEIZE STA4
* TEST LE FRN(11),&POF,STR14
* FUNAVAL PRCS4
* ADVANCE 2*MN3
* FAVAIL PRCS4
* *
* STR14 SEIZE PRCS4
* *
* BLET &M4=&MN4+((FRN(12)-0.5)*2)*MN4*DELT
* ADVANCE &M4
* RELEASE PRCS4
* RELEASE STA4
* *
* DEPART SYSQ
* *
* DEPART ASSEMQ
* *
* PDCT TERMINATE 0
* *
* *
* Model Timing
* *
* Run model for 40 hour week
* *
* GENERATE 60.*8.*5.
* TERMINATE 1
* *
*
C-7
GPSS/H Control Statements

Process Time Variability (&DELT) initialized. The values in successive models ranged between 0.0 and 0.40 in increments of 0.05.

LET &DELT=0.0

Probability of Station Failure (&POF) initialized. The values in successive models ranged between 0.0 and 0.40 in increments of 0.05.

LET &POF=0.0

LET &BFSZ=1 Buffer size initialized

DO &J=1,8

BFR1A STORAGE &BFSZ
BFR1B STORAGE &BFSZ
BFR2A STORAGE &BFSZ Set all model buffers to same size
BFFR2B STORAGE &BFSZ
BFFR3 STORAGE &BFSZ

DO &I=1,100 100 iterations at each set-point

LET &BUFF1A=0
LET &BUFF1B=0 Initialize buffer counters
LET &BUFF2A=0
LET &BUFF2B=0
LET &BUFF3=0

INITIAL LR(SUBA) Initialize Subcomponent A gate

START 1,NP 40 hour warm-up

RESET

START 4,NP 160 hour data gathering

Calculate Maximum WIP in model

LET &MWIP=((0.5*QM(SUBA))+((0.5*QM(SUBB))+QM(ASSEM)))
* Output data to file

PUTPIC FILE=OUTA,(&DELT,&POF,N(PDCT),&MWIP)

CLEAR
ENDDO
LET &BFSZ=&BFSZ+1 Increment buffer size
ENDDO
END
REALLOCATE COM,150000

SIMULATE

Variable Declaration Section

*********************************************************************************

Variable Definitions

*********************************************************************************

&I, &J - Loop Counters
&BFSZ - Defined Buffer Size
&BUFF - Buffer Counter for Buffer
&POF - Defined Probability of Station Failure
&DELT - Percent Variability of Processing Time
&MN1A - Mean Processing Time for Station 1A
&MN1B - Mean Processing Time for Station 1B
&MN2A - Mean Processing Time for Station 2A
&MN2B - Mean Processing Time for Station 2B
&MN3 - Mean Processing Time for Station 3
&MN4 - Mean Processing Time for Station 4
&MEAN1A - Calculated Actual Processing Time for Station 1A
&MEAN1B - Calculated Actual Processing Time for Station 1B
&MEAN2A - Calculated Actual Processing Time for Station 2A
&MEAN2B - Calculated Actual Processing Time for Station 2B
&MEAN3 - Calculated Actual Processing Time for Station 3
&MEAN4 - Calculated Actual Processing Time for Station 4
&MWIP - Maximum Work-in-Process
&WIP - Temporary inventory counter

*********************************************************************************

Variable Declaration Section

*********************************************************************************

INTEGER &I
INTEGER &J
INTEGER &BFSZ,&BUFF,&WIP,&MWIP
REAL &POF,&MN1A,&MN1B,&MN2A,&MN2B,&MN3,&MN4
REAL &MEAN1A,&MEAN1B,&MEAN2A,&MEAN2B
REAL &MEAN3,&MEAN4,&DELT

D-1
Declaration of Output File

OUTA FILEDEF 'THSC2A1.OUT'

Variable Assignment Section

Definition of Mean Processing Times

** declaration of variable assignment section 

LET &MN1A=7.5
LET &MN1B=5.0
LET &MN2A=12.5
LET &MN2B=7.5
LET &MN3=20.0
LET &MN4=5.0
LET &MWIP=0

GPSS/H Block Section

Subcomponent A Assembly

** block section for subcomponent A assembly

GENERATE 0,,0 Generate a XACT whenever the input buffer is empty
SEIZE INBUF Seize the input buffer

TEST NE &BUFF,&BFSZ Test for room in buffer
BLET &BUFF=&BUFF+1 Increment buffer counter
RELEASE INBUF Leave the input buffer
BLET &WIP=&WIP+1 Increment the inventory counter

SPLIT 1.PRCB Split the XACT in to 2 subcomponents
TEST E F(STA1A),0 Test status of Sta 1A

D-2
Process 1A

SEIZE STA1A Enter the station
TEST LE FRN(2),&POF,SRT1A Test for failure
FUNAVAIL PRCS1A Make process unavailable
ADVANCE 2*&MN3 Delay for repair
FAVAIL PRCS1A Make process available

SRT1A SEIZE PRCS1A Enter processing

BLET &MEAN1A=&MN1A+(((FRN(3)-0.5)*2)*&MN1A*DELT)
ADVANCE &MEAN1A
RELEASE PRCS1A
RELEASE STA1A Leave the station and processing

TEST E F(STA2A),0 Test status of next station

Process 2A

SEIZE STA2A
TEST LE FRN(4),&POF,SRT2A
FUNAVAIL PRCS2A
ADVANCE 2*&MN3
FAVAIL PRCS2A

SRT2A SEIZE PRCS2A

BLET &MEAN2A=&MN2A+(((FRN(5)-0.5)*2)*&MN2A*DELT)
ADVANCE &MEAN2A
RELEASE PRCS2A
RELEASE STA2A

TRANSFER ,PDT
Subcomponent B Assembly

PRCB  ADVANCE  0
TEST E  F(STA1B),0  Test status of station

Process 1B

SEIZE  STA1B
TEST LE  FRN(6),&POF,STA1B
FUNAVAIL  PRCS1B
ADVANCE  2*&MN3
FAVAIL  PRCS1B
SRT1B SEIZE  PRCS1B

BLET  &MEAN1B=2*MN1B+((FRN(7)-0.5)*2)*&MN1B*6DELT)
ADVANCE  &MEAN1B
RELEASE  PRCS1B
RELEASE  STA1B

TEST E  F(STA2B),0

Process 2B

SEIZE  STA2B
TEST LE  FRN(8),&POF,STA2B
FUNAVAIL  PRCS2B
ADVANCE  2*&MN3
FAVAIL  PRCS2B
SRT2B SEIZE  PRCS2B

BLET  &MEAN2B=2*MN2B+((FRN(9)-0.5)*2)*&MN2B*6DELT)
ADVANCE  &MEAN2B
RELEASE  PRCS2B
RELEASE  STA2B
Joining of Subcomponents A and B

PDT ADVANCE 0
ASSEMBLE 2 Assemble the 2 subcomponents

Buffer

ENTER BFFR
TEST E F(STA3),0
BLET &BUFF=&BUFF-1
LEAVE BFFR

Process 3

SEIZE STA3
SEIZE PRCS3
BLET &MEAN3=&MN3+(((FRN(10)-0.5)*2)*&MN3*DELT)
ADVANCE &MEAN3
RELEASE PRCS3
RELEASE STA3
TEST E F(STA4),0
*** Process 4 ***

---

** SEIZE STA4 
** TEST LE FRN(11),&POF,STRT4 
** FUNAVAIL PRCS4 
** ADVANCE 2*&MN3 
** PAVAIL PRCS4 

STRT4 SEIZE PRCS4 

** BLET &MEAN4=&MN4+(((FRN(12)-0.5)*2)*&MN4*DELT) 
** ADVANCE &MEAN4 
** RELEASE PRCS4 
** RELEASE STA4 

** TEST G &WIP,&MWIP,BPSS Test to see if current inventory is greater than past 
** BLET &MWIP=&WIP 
** BPSS BLET &WIP= &WIP-1 Decrement inventory counter 

** PDCT TERMINATE 0 

---

* Model Timing 
* Run model for 40 hour week 
* GENERATE 60.*8.*5. 
* TERMINATE 1 

*** GPSS/H Control Statements ***

---

* Process Time Variability (&DELT) initialized. 
The values in successive models ranged between 0.0 and 0.40 in increments of 0.05. 
* LET &DELT=0.0 

* Probability of Station Failure (&POF) initialized. 
The values in successive models ranged between 0.0 and 0.40 in increments of 0.05. 
* LET &POF=0.0 

---

D-6
LET &BFSZ=1 Initialize buffer size
DO &J=1,8
BPFR STORAGE &BFSZ Set buffer
DO &I=1,100 100 iterations at each set-point
LET &BUF=0 Initialize buffer counter
LET &WIP=0 Initialize inventory counter
START 1,NP 40 hour warm-up
RESET
LET &MWIP=0 START 4,NP 160 hour data gathering
Output data to file
PUTPIC FILE=OUTA,(&DELT,&POF,N(PDCT),&MWIP)
CLEAR ENDDO
LET &BFSZ=&BFSZ+1 Increment buffer size
ENDDO END
Appendix E: System 3 - JIT - GPSSH Program Listing

REALLOCATE COH, 500000
*
SIMULATE
*
******************************************************************************
*
Variable Definitions
*
******************************************************************************
*
&I, &J - Loop Counters
&BFSZ - Defined Buffer Size
&BUFF1A - Buffer Counter for Buffer 1A
&BUFF1B - Buffer Counter for Buffer 1B
&BUFF1C - Buffer Counter for Buffer 1C
&BUFF2A - Buffer Counter for Buffer 2A
&BUFF2B - Buffer Counter for Buffer 2B
&BUFF2C - Buffer Counter for Buffer 2C
&BF3X1 - Buffer Counter for Buffer 3-1
&BF3X2 - Buffer Counter for Buffer 3-2
&P0F - Defined Probability of Station Failure
&DILT - Percent Variability of Processing Time
&MN1A - Mean Processing Time for Station 1A
&MN1B - Mean Processing Time for Station 1B
&MN1C - Mean Processing Time for Station 1C
&MN2A - Mean Processing Time for Station 2A
&MN2B - Mean Processing Time for Station 2B
&MN2C - Mean Processing Time for Station 2C
&MN3X1 - Mean Processing Time for Station 3-1
&MN3X2 - Mean Processing Time for Station 3-2
&MN4X1 - Mean Processing Time for Station 4-1
&MN4X2 - Mean Processing Time for Station 4-2
&MMEAN1A - Calculated Actual Processing Time for Station 1A
&MMEAN1B - Calculated Actual Processing Time for Station 1B
&MMEAN1C - Calculated Actual Processing Time for Station 1C
&MMEAN2A - Calculated Actual Processing Time for Station 2A
&MMEAN2B - Calculated Actual Processing Time for Station 2B
&MMEAN2C - Calculated Actual Processing Time for Station 2C
&MMEAN3X1 - Calculated Actual Processing Time for Station 3-1
&MMEAN3X2 - Calculated Actual Processing Time for Station 3-2
&MMEAN4X1 - Calculated Actual Processing Time for Station 4-1
&MMEAN4X2 - Calculated Actual Processing Time for Station 4-2
&MWIP - Maximum Work-in-Process
*
******************************************************************************
*
E-1
Variable Declaration Section

INTEGER &I
INTEGER &J
INTEGER &BSZ,&BUFF1A,&BUFF1B,&BUFF1C
INTEGER &BUFF2A,&BUFF2B,&BUFF2C
INTEGER &BF3X1,&BF3X2
REAL &POF,&MN1A,&MN1B,&MN1C,&MN2A,&MN2B,&MN2C
REAL &MN3X1,&MN3X2,&MN4X1,&MN4X2
REAL &MEAN1A,&MEAN1B,&MEAN1C,&MEAN2A,&MEAN2B,&MEAN2C
REAL &MEAN3X1,&MEAN3X2,&MEAN4X1,&MEAN4X2,&DELT
REAL &MNIP

******************************************************************************

Declaration of Output File

******************************************************************************

OUTA FILEDEF 'THS3A1.OUT'

******************************************************************************

Variable Assignment Section

******************************************************************************

Definition of Mean Processing Times

******************************************************************************

LET &MN1A=7.5
LET &MN1B=2.5
LET &MN1C=5.0
LET &MN2A=12.5
LET &MN2B=7.5
LET &MN2C=10.0
LET &MN3X1=20.0
LET &MN3X2=25.0
LET &MN4X1=5.0
LET &MN4X2=5.0

GPSS/H Lock Section

E-2
Subcomponent A Assembly

Generate a XACT whenever there is room in the input buffer
Enter the input buffer

Beginning of product flow

Test for room in the first buffer
Increment the buffer counter
Test status of station
Exit the input buffer

Enter the subassembly A queue

Process 1A

Enter Station 1A
Test for failure of process
Make process unavailable
Repair delay
Make process available
Begin processing
Release Station and process
_BUFFER 1A

**-------------------------------------------**
* Buffer 1A
*
**-------------------------------------------**

**-------------------------------------------**
* Enter Buffer 1A
**-------------------------------------------**

**-------------------------------------------**
* Test for room in next buffer
**-------------------------------------------**

**-------------------------------------------**
* Increment buffer counter
**-------------------------------------------**

**-------------------------------------------**
* Test status of station
**-------------------------------------------**

**-------------------------------------------**
* Decrement the buffer counter
**-------------------------------------------**

**-------------------------------------------**
* Leave the buffer
**-------------------------------------------**

**-------------------------------------------**
* Process 2A
*
**-------------------------------------------**

**-------------------------------------------**
* Seize STA2A
**-------------------------------------------**

**-------------------------------------------**
* Test for station availability
**-------------------------------------------**

**-------------------------------------------**
* Increment counter
**-------------------------------------------**

**-------------------------------------------**
* Test station status
**-------------------------------------------**

**-------------------------------------------**
* Decrement counter
**-------------------------------------------**

**-------------------------------------------**
* Logics to set gate SUBB
**-------------------------------------------**

**-------------------------------------------**
* Leave the buffer
**-------------------------------------------**

**-------------------------------------------**
* Depart the queue
**-------------------------------------------**

**-------------------------------------------**
* Transfer to Product 1 final assembly
**-------------------------------------------**

E-4
Subcomponent B Assembly

BEGINNING OF PRODUCT FLOW

TEST NE &BUFF1B,&BFSZ
BLET &BUFF1B= &BUFF1B+1
TEST E F(STA1B),0
RELEASE INBUF1B

QUEUE SUBBQ

PROCESS 1B

SEIZE STA1B
TEST LE FRN(6), &POF, SRT1B
UNAVAIL PRCS1B
ADVANCE 2*MN1B
FAVAIL PRCS1B
SRT1B SEIZE PRCS1B
BLET &MEAN1B+ &MN1B+((FRN(7)-0.5)*2)*&MN1B*Delt
ADVANCE &MEAN1B
RELEASE PRCS1B
RELEASE STA1B
**Buffer 1B**

**Process 2B**

**Buffer 2B**
Subcomponent C Assembly

BEGINNING OF PRODUCT FLOW

TEST NE &BUFF1C, &BFSZ
BLET &BUFF1C= &BUFF1C+1
TEST E F(STA1C), 0
RELEASE INBUFC

QUEUE SUBCQ

PROCESS 1C

SEIZE STA1C
TEST LE FRN(10), &POF, SRT1C
FUNAVAL PRCS1C
ADVANCE 2*MN1C
FAVAIEN PRCS1C
SRT1C SEIZE PRCS1C
BLET &MEAN1C= MN1C+(((FRN(11)-0.5)*2)*MN1C*DELT)
ADVANCE &MEAN1C
RELEASE PRCS1C
RELEASE STA1C

BUFFER 1C

ENTER BFR1C
TEST NE &BUFF2C, &BFSZ
BLET &BUFF2C= &BUFF2C+1
TEST E F(STA2C), 0
BLET &BUFF1C= &BUFF1C-1
LEAVE BFR1C

---
Process 2C

 SEIZE STA2C
 TEST LE FRN(12),&POF,SRT2C
 FUNAVAL PRCS2C
 ADVANCE 2*MN2C
 FAVAIL PRCS2C

 SRT2C SEIZE PRCS2C

 BLET &MN2C=6MN2C+((FRN(13)-0.5)*2)*MN2C*DELT
 ADVANCE &HEAN2C
 RELEASE PRCS2C
 RELEASE STA2C

 Buffer 2C

 ENTER BFR2C
 TEST NE SE(BFR2B),1
 TEST NE &BF3X2,&BF5Z
 BLET &BF3X2=EF3X2-1
 TEST E F(STA3X2),0
 BLET &BUFF2C=EFUFF2C-1
 LOGIC S SUBB
 LEAVE BFR2C

 DEPART SUBCQ

 TRANSFER ,PDT2

 Joining of Subcomponents A and B

 PDT1 QUEUE ASSEM1Q Enter the assembly queue for Product 1
************

* Process 3 Product 1 *

************

* SEIZE STA3X1*

* SEIZE PRCS3X1*

* BLET &MEAN3X1=(&(FRN(14)-0.5)*2)*&MN3X1*DELT)*

* ADVANCE &MEAN3X1*

* RELEASE PRCS3X1*

* RELEASE STA3X1*

************

* Buffer 3-1 *

************

* ENTER BFR3X1*

* TEST E F(STA4X1),0*

* BLET &BF3X1=&BF3X1-1*

* LEAVE BFR3X1*

************

* Process 4 Product 1 *

************

* SEIZE STA4X1*

* TEST LE FRN(15),&POF,SRT41*

* FUNAVAIL PRCS4X1*

* ADVANCE 2*&MN4X1*

* FAVAIL PRCS4X1*

* SRT4 :=IZE PRCS4X1*

* BLET &MEAN4X1=(&(FRN(16)-0.5)*2)*&MN4X1*DELT)*

* ADVANCE &MEAN4X1*

* RELEASE PRCS4X1*

* RELEASE STA4X1*

* DEPART ASSEM1Q*

* PDCT1 TERMINATE 0*
Joining of Subcomponents B and C

PDT2 QUEUE ASSEM2Q

Process 3 Product 2

SEIZE STA3X2
SEIZE PRCS3X2

BLET &MEAN3X2= &MN3X2+((FRN(17)−0.5)2)*&MN3X2*&DELT
ADVANCE &MEAN3X2
RELEASE PRCS3X2
RELEASE STA3X2

Buffer 3-2

ENTER BFR3X2
TEST E SRT42,0
BLET &BF3X2= &BF3X2-1
LEAVE BFR3X2

Process 4 Product 2

SEIZE STA4X2
TEST LE FRN(18), &POF, SRT42
FUNAVAL PRCS4X2
ADVANCE 2*&MN4X2
FAVAIL PRCS4X2

SRT42 SEIZE PRCS4X2
BLET &MEAN4X2= &MN4X2+((FRN(19)−0.5)2)*&MN4X2*&DELT
ADVANCE &MEAN4X2
RELEASE PRCS4X2
RELEASE STA4X2
DEPART ASSEM2Q

PDCT2 TERMINATE 0

E-10
Model Timing

Run model for 40 hour week

GENERATE 60.*8.*5.
TERMINATE 1

GPSS/H Control Statements

Process Time Variability (&DELT) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &DELT=0.0

Probability of Station Failure (&POF, initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &POF=0.0

LET &BFSZ=1 Buffer size initialized

DO &J=1,8
BFR1A STORAGE &BFSZ
BFR1B STORAGE &BFSZ
BFR1C STORAGE &BFSZ Set all model buffers
to the same size
BFR2A STORAGE &BFSZ
BFR2B STORAGE &BFSZ
BFR2C STORAGE &BFSZ
BFR3X1 STORAGE &BFSZ
BFR3X2 STORAGE &BFSZ

DO &I=1,100 100 iterations at each set-point
LET &BUFF1A=0
LET &BUFF1B=0
LET &BUFF1C=0
LET &BUFF2A=0 Initialize all buffer counters
LET &BUFF2B=0
LET &BUFF2C=0
LET &BF3X1=0
LET &BF3X2=0
INITIAL LR(SUBB) Initialize the Gate SUBB
START 1, NP  40 hour warm-up period
RESET
START 4, NP  160 hour data gathering

Calculation of Maximum Work-in-Process

LET &HWIP=((0.5*QM(SUBAQ))+(0.5*QM(SUBBQ))+(0.5*QM(SUBCQ)))+QM(ASSEM1Q)+QM(ASSEM2Q))

Output data to file

PUTPIC FILE=OUTA, (&DELT, &POF, N(PDCT1), N(PDCT2), 
N(PDCT1)+N(PDCT2), &MWIP)

CLEAR
ENDDO
LET &BFSZ=&BFSZ+1  Increment buffer size
ENDDO
END

Repeat execution
Appendix F: System 3 - TOC - GPSSH Program Listing

REALLOCATE COM, 500000
*
SIMULATE
*

********************************************************************************
*
Variable Definitions
*
********************************************************************************
*
&I, &J - Loop Counters
&BFZ2 - Defined Buffer Size
&BUFF1 - Buffer Counter for Buffer 1A
&BUFF2 - Buffer Counter for Buffer 2A
&POF - Defined Probability of Station Failure
&DELT - Percent Variability of Processing Time
&MN1A - Mean Processing Time for Station 1A
&MN1B - Mean Processing Time for Station 1B
&MN1C - Mean Processing Time for Station 1C
&MN2A - Mean Processing Time for Station 2A
&MN2B - Mean Processing Time for Station 2B
&MN2C - Mean Processing Time for Station 2C
&MN3X1 - Mean Processing Time for Station 3-1
&MN3X2 - Mean Processing Time for Station 3-2
&MN4X1 - Mean Processing Time for Station 4-1
&MN4X2 - Mean Processing Time for Station 4-2
&MEAN1A - Calculated Actual Processing Time for Station 1A
&MEAN1B - Calculated Actual Processing Time for Station 1B
&MEAN1C - Calculated Actual Processing Time for Station 1C
&MEAN2A - Calculated Actual Processing Time for Station 2A
&MEAN2B - Calculated Actual Processing Time for Station 2B
&MEAN2C - Calculated Actual Processing Time for Station 2C
&MEAN3X1 - Calculated Actual Processing Time for Station 3-1
&MEAN3X2 - Calculated Actual Processing Time for Station 3-2
&MEAN4X1 - Calculated Actual Processing Time for Station 4-1
&MEAN4X2 - Calculated Actual Processing Time for Station 4-2
&MWIP1 - Maximum Work-in-Process for Product 1
&WP1 - Interim variable for calculating &MWIP1
&MWIP2 - Maximum Work-in-Process for Product 2
&WP2 - Interim variable for calculating &MWIP2
&MWIP - Total Work-in-Process for the model

********************************************************************************
**Variable Declaration Section**

```
INTEGER &I
INTEGER &J
INTEGER &BFSZ,&BUFF1,&BUFF2
INTEGER &WIP1,&MWIP1,&WIP2,&MWIP2,&MWIP
REAL &POF,&MN1A,&MN1B,&MN1C,&MN2A,&MN2B,&MN2C
REAL &MN3X1,&MN3X2,&MN4X1,&MN4X2
REAL &MEAN1A,&MEAN1B,&MEAN1C,&MEAN2A,&MEAN2B,&MEAN2C
REAL &MEAN3X1,&MEAN3X2,&MEAN4X1,&MEAN4X2,&DELT
```

**Declaration of Output File**

```
OUTA FILEDEF 'THSC3A1.OUT'
```

**Variable Assignment Section**

```
** Definition of Mean Processing Times **
```

```
LET &MN1A=7.0
LET &MN1B=2.5
LET &MN1C=5.0
LET &MN2A=12.5
LET &MN2B=7.5
LET &MN2C=10.0
LET &MN3X1=20.0
LET &MN3X2=25.0
LET &MN4X1=5.0
LET &MN4X2=5.0
LET &MWIP1=0
LET &MWIP2=0
```

F-2
GPSS/H Block Section

Subcomponent A Assembly

GENERATE 0,0,,1PH Generate a transaction whenever the input buffer has room
SEIZE INBUF1 Enter the input buffer 1
ASSIGN PROD,1,PH Assign Product 1 code

Beginning of product flow

TEST NE &BUFF1,&BFSZ Test for room in buffer
BLET &BUFF1=&BUFF1+1 Increment buffer counter
TEST E F(STA1A),0 Test status of station
RELEASE INBUF1 Exit the input buffer

BLET &WIP1=&WIP1+1 Increment the WIP counter

SPLIT 1,PRCB Split the transaction into two subcomponents

Process 1A

SEIZE STA1A Enter Station 1A
TEST LE FRN(2),&POF,SRT1A Test for failure
FUNAVAIL PRCS1A Make process unavailable
ADVANCE 2*&MN1A Delay for repair of process
FAVAIL PRCS1A Make process available
SRT1A SEIZE PRCS1A Start processing

BLET &MEAN1A=6&MN1A+(((FRN(3)-0.5)*2)&MN1A*DELT) Advance
ADVANCE &MEAN1A Delay for repair of process
RELEASE PRCS1A Release
RELEASE STA1A Leave station and process
TEST E F(STA2A),0 Test status of station

F-3
Process 2A

SEIZE STA2A
TEST LE FRN(4),&POF,SRT2A
FAVAIL PRCS2A
ADVANCE 2*&MN2A
FAVAIL PRCS2A

SRT2A SEIZE PRCS2A

BLET &MEAN2A=&MN2A+(((FRN(5)-0.5)*2)*&MN2A*DELT)
ADVANCE &MEAN2A
RELEASE PRCS2A
RELEASE STA2A

TRANSFER ,PDT1 Transfer to Product 1 assembly

Subcomponent B Assembly

PRCB ADVANCE 0 .
Beginning of product flow
TEST E F(STA1B),0

Process 1B

SEIZE STA1B
TEST LE FRN(6),&POF,SRT1B
FAVAIL PRCS1B
ADVANCE 2*&MN1B
FAVAIL PRCS1B

SRT1B SEIZE PRCS1B

BLET &MEAN1B=&MN1B+(((FRN(7)-0.5)*2)*&MN1B*DELT)
ADVANCE &MEAN1B
RELEASE PRCS1B
RELEASE STA1B

TEST E F(STA2B),0

F-4
**************************************************************************
* *
* Process 2B
*
**************************************************************************
*
SEIZE STA2B
TEST LE FRN(8),&POF,SRT2B
FUNAVAIL PRCS2B
ADVANCE 2*&MN2B
FAVAIL PRCS2B
*
SRT2B SEIZE PRCS2B
*
BLET &MEAN2B=&MN2B+(((FRN(9)-0.5)*2)*&N2B*&DELT)
ADVANCE &MEAN2B
RELEASE PRCS2B
RELEASE STA2B
*
*
TEST E PH(PROD),1,PDT2  Test if subcomponent is for
TRANSFER ,PDT1  Product 1 or 2
*
**************************************************************************
* *
* Subcomponent C Assembly
*
**************************************************************************
*
GENERATE 0,,0,,1PH
SEIZE INBUF2
*
ASSIGN PROD,2,PH
*
Beginning of product flow
*
TEST NE &BUFF2,&BFSZ
BLET &BUFF2=&BUFF2+1
TEST E F(STA1C),0
RELEASE INBUF2
*
BLET &WIP2=&WIP2+1
*
SPLIT 1,PRCB
*
**************************************************************************
***************
* Process 1C *
***************

    SEIZE  STA1C
    TEST LE FRN(10), &POF, SRT1C
    FUNAVAIL PRCS1C
    ADVANCE 2*&MN1C
    FAVAIL  PRCS1C

    SRT1C SEIZE  PRCS1C

    BLET  &MEAN1C= &MN1C+((FRN(11)-0.5)*2* &MN1C* &DELT)
    ADVANCE &MEAN1C
    RELEASE  PRCS1C
    RELEASE  STA1C

    TEST E  F(STA2C), 0

***************
* Process 2C *
***************

    SEIZE  STA2C
    TEST LE FRN(12), &POF, SRT2C
    FUNAVAIL PRCS2C
    ADVANCE 2*&MN2C
    FAVAIL  PRCS2C

    SRT2C SEIZE  PRCS2C

    BLET  &MEAN2C= &MN2C+((FRN(13)-0.5)*2* &MN2C* &DELT)
    ADVANCE &MEAN2C
    RELEASE  PRCS2C
    RELEASE  STA2C

    TRANSFER ,PDT2

F-6
Joining of Subcomponents A and B

PDT1 ADVANCE  0
ASSEMBLE  2 Assemble the 2 subcomponents

 Buffer 1

ENTER BFFR1 Enter the constraint buffer
TEST E F(STA3X1),0 Test station status
BLET &BUFF1=&BUFF1-1 Decrement buffer counter
LEAVE BFFR1 Leave the buffer

 Process 3 Product 1

SEIZE STA3X1
SEIZE PRCS3X1
BLET &MEAN3X1=&MN3X1+((FRN(14)-0.5)*2)*&MN3X1^&DELT)
ADVANCE &MEAN3X1
RELEASE PRCS3X1
RELEASE STA3X1
TEST E F(STA4X1),0
Process 4 Product 1

SEIZE STA4X1
TEST LE FRN(15),&POF,SRT41
FUNAVAIL PRCS4X1
ADVANCE 2*&MN4X1
FAVAIL PRCS4X1

3RT41 SEIZE PRCS4X1

BLEM &14EAN4XI=&MN4X1+((FRN(16)-0.5)*2)*&MN4X1*DELT)
ADVANCE &MEAN4X1
RELEASE PRCS4X1
RELEASE STA4X1

TEST G &WIP1,&MWIP1,BPSS1 Determine if current WIP
BLET &WIP1=&WIP1 level is the maximum
BPSS1 BLET &WIP1=&WIP1-1 Decrement WIP counter

PDCTI TERMINATE 0

Joining of Subcomponents B and C

PDT2 ADVANCE 0
ASSEMBLE 2

Buffer 2

ENTER BFFR2
TEST E F(STA3X2),0
BLET &BUFF2=&BUFF2-1
LEAVE BFFR2

F-8
Process 3 Product 2

************************************************************
* *
* SEIZE STA3X2
* *
* SEIZE PRCS3X2
* *
* BLET &MEAN3X2=6MN3X2+((FRN(17)-0.5)*2)*6MN3X2*6DELT
* *
* ADVANCE &MEAN3X2
* *
* RELEASE PRCS3X2
* *
* RELEASE STA3X2
* *
* TEST E F(STA4X2),0
* *
************************************************************
* *
Process 4 Product 2

************************************************************
* *
* SEIZE STA4X2
* *
* TEST LE FRN(18),&POF,SRT42
* *
* FNAVAIL PRCS4X2
* *
* ADVANCE 2*6MN4X2
* *
* FAVAIL PRCS4X2
* *
* SRT42 SEIZE PRCS4X2
* *
* BLET &MEAN4X2=6MN4X2+((FRN(19)-0.5)*2)*6MN4X2*6DELT
* *
* ADVANCE &MEAN4X2
* *
* &RELEASE PRCS4X2
* *
* RELEASE STA4X2
* *
* TEST G &WIP2,&MWIP2,BPSS2
* *
* BLET &MWIP2=6WIP2
* *
* BPSS2 BLET &WIP2=6WIP2-1
* *
* PDCT2 TERMINATE 0
* *
************************************************************
* F-9
Model Timing

Run model for 40 hour week

GENERATE 60.*8.*5.
TERMINATE 1

GPSS/H Control Statements

Process Time Variability (&DELT) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &DELT=0.0

Probability of Station Failure (&POF) initialized.
The values in successive models ranged between
0.0 and 0.40 in increments of 0.05.

LET &POF=0.0

LET &BFSZ=1
DO &J=1,8
BFFR1 STORAGE &BFSZ Initialize the buffers
BFFR2 STORAGE &BFSZ
DO &I=1,100 100 iterations at each set-point
LET &BUFF1=0 Initialize buffer counters
LET &BUFF2=0
LET &WIP1=0
LET &WIP2=0
START 1,NP 40 hour warm-up
RESET
LET &MWIP1=0
LET &MWIP2=0
START 4,NP 160 hour data gathering

Calculation of Maximum Work-in-Process

LET &MWIP= &MWIP1+&MWIP2
Output data to file

PUTPIC
FILE=OUTA,(&DELT,&POF,N(PDCT1),N(PDCT2),
N(PDCT1)+N(PDCT2),&MWIP)

CLEAR
ENDDO

LET &BFSZ=&BFSZ+1
ENDDO
END
Bibliography


Karmarkar, Uday S. Push, Pull, and Hybrid Control Schemes. William E. Simon Graduate School of Business Administration, Working Paper Series No. QM 86-14, University of Rochester, Rochester NY (1986).


Vita

Captain Lynn A. Sines was born on 29 August 1961 in Indianapolis, Indiana. He graduated from Lewis Cass Jr-Sr High School in Walton, Indiana in 1979 and attended Purdue University, graduating with a Bachelor of Science in Electrical Engineering (specialty: Control Systems) in December 1983. Upon graduation, he attended Officer Training School and was commissioned in the USAF in March 1984. He served his first tour of duty at Tinker AFB, Oklahoma as a Technical Activities Management Engineer in the Directorate of Maintenance, Oklahoma City Air Logistics Center where he was responsible for the Electrical Engineering support of accessory items for all USAF aircraft. In February 1987 he was transferred to Wright Patterson AFB, Ohio where he was assigned as a Logistics Plans Officer in the Air Force Contract Maintenance Center (AFCMC) where he was responsible for the initial planning of world-wide contract administration activities. In June 1989 he was reassigned as Chief, Plans and Programs Division for AFCMC. There he was responsible for the planning of support for overseas coproduction and offset programs. He entered the School of Systems and Logistics, Air Force Institute of Technology, in May 1990.

Permanent Address: 2500 Sherman Dr.
Kokomo, IN 46902

VITA-1
This study compared the characteristics of scheduling using two approaches: Just-in-Time (JIT) and the Theory of Constraints (TOC). Computer simulation was used to evaluate changes in the throughput of the systems due to system variability and varying work-in-process (WIP) levels. The independent variables were processing time, probability of failure, and WIP level. The literature search revealed that these variables impacted performance of JIT systems. Simulation models of three different production systems were developed to determine if the TOC scheduled system would provide greater or equivalent throughput for equivalent levels of WIP, and to determine if the system production flow path had an impact on the performance of the TOC system. The models were scheduled using both JIT and TOC methodologies. The mean throughput for each combination of independent variables was calculated along with the 95 percent confidence interval. The mean and confidence intervals were then graphed for analysis. Simulation results indicated that the TOC system outperforms the JIT system for single product systems while the results of the multiple product system were inconclusive. There was no difference between the TOC systems for process time variability, but there was a difference for process station failure.
AFIT RESEARCH ASSESSMENT

The purpose of this questionnaire is to determine the potential for current and future applications of AFIT thesis research. Please return completed questionnaires to: AFIT/LSC, Wright-Patterson AFB OH 45433-6583.

1. Did this research contribute to a current research project?
   a. Yes        b. No

2. Do you believe this research topic is significant enough that it would have been researched (or contracted) by your organization or another agency if AFIT had not researched it?
   a. Yes        b. No

3. The benefits of AFIT research can often be expressed by the equivalent value that your agency received by virtue of AFIT performing the research. Please estimate what this research would have cost in terms of manpower and/or dollars if it had been accomplished under contract or if it had been done in-house.
   Man Years ________________  $ ________________

4. Often it is not possible to attach equivalent dollar values to research, although the results of the research may, in fact, be important. Whether or not you were able to establish an equivalent value for this research (3 above), what is your estimate of its significance?

5. Comments

Name and Grade ___________________________  Organization ___________________________

Position or Title ___________________________  Address ___________________________