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13. **ABSTRACT (Maximum 200 words)**
    - NRL theoretical and computational studies in support of the ATA Multi-Pulse Propagation Experiment (MPPE) are summarized in a series of papers which were presented at the 1989 Annual DARPA/SDIO/Services Charged Particle Beam Review. The six papers presented here were all written prior to the completion of the experiment. The first of these papers presents simulation results which modeled beam stability and channel evolution for an entire five pulse burst. The second paper describes a new air chemistry model used in the SARLAC propagation code and discusses the role of CO₂ in speeding channel heating. An overview of NRL studies on beam propagation in reduced-density channels is provided in the next paper. The fourth paper describes hydrodynamic simulations of convective mixing in beam-generated channels using a new flux-corrected transport algorithm developed for NRL's Connection Machine. The relative importance of high frequency (BBU-generated) and low frequency perturbations in triggering resistive hose instability is treated in the fifth paper, using results from the SARLAC beam simulation code. Finally, the last paper describes the various options for conditioning the ATA beam prior to injection into the propagation tank and concludes that a passive ion-focused regime (IFR) will produce the desired tailoring results.

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CONTENTS

OVERVIEW ........................................................................................................ 1

BEAM STABILITY AND RANGE EXTENSION PREDICTIONS FOR THE ATA
MULTI-PULSE PROPAGATION EXPERIMENT ...................................................... 4

AIR CHEMISTRY ASPECTS OF THE ATA MULTIPULSE EXPERIMENT ............. 9

BEAM PROPAGATION IN CHANNELS ................................................................... 13

HYDRODYNAMIC SIMULATIONS OF BEAM-GENERATED TURBULENCE
IN CHANNELS ..................................................................................................... 17

SENSITIVITY OF HOSE INSTABILITY TO FREQUENCY OF INITIAL PERTURBATION
IN LOW AND HIGH CURRENT BEAMS ................................................................. 21

BEAM CONDITIONING OPTIONS FOR THE ATA MULTI-PULSE EXPERIMENT .... 25

DISTRIBUTION LIST ............................................................................................ 29
NRL 1989 BEAM PROPAGATION STUDIES IN SUPPORT OF THE 
ATA MULTI-PULSE PROPAGATION EXPERIMENT

OVERVIEW

This report contains six short papers which will appear in the 
proceedings of the 1989 Annual DARPA/SDIO/Services Charged Particle Beam 
Review which took place at the Naval Postgraduate School in Monterey, CA 
during 18-21 September, 1989. The report describes electron beam 
propagation and beam conditioning studies which have been carried out at NRL 
in support of the ATA Multi-Pulse Propagation Experiment (ATA/MPPE). These 
papers were all written prior to the actual propagation experiments which 
took place at the Lawrence Livermore National Laboratory during December, 
1989 and January, 1990. Analyses of the experimental results will appear in 
the 1990 annual review.

ATA/MPPE was the first serious attempt to study the physics of beam 
propagation in the low density channel produced by a train or burst of 
pulses. The target beam parameters were 6 kA beam current, 10 MeV energy, 
0.5 cm beam radius, 30 nsec pulse length, and 5 pulses separated by 1.2 
msec. The two major experimental objectives were to investigate beam 
stability in a beam-produced channel to determine if the channel 
destabilized the beam and to demonstrate that subsequent pulses could travel 
farther than the first pulse ("range extension"). The papers presented here 
focused heavily on those objectives. It was recognized from the outset that 
the virulent resistive hose instability could disrupt the beam and prevent a 
range extension demonstration, and much of the experimental and theoretical 
effort concentrated on various beam conditioning techniques for suppressing 
that instability. In spite of these efforts, hose instability usually 
disrupted propagation during the first three meters of propagation.

A brief summary of each paper and a list of coauthors for each are 
given below. Papers on NRL theoretical studies of other CPB experiments 
will be published elsewhere.

A. Beam Stability and Range Extension Predictions for the ATA Multi-
Pulse Propagation Experiment: Numerous simulations of the MPPE were 
undertaken. These simulations used the SIMMO particle simulation code for 
beam propagation during the pulse and the CHMAIR and HINT channel physics 
codes to treat the longer time scale behavior between successive pulses. 
For 6 kA, 5 mm, 33 nsec beams, range extension can be shown by about a 50%

Manuscript approved May 21, 1990.
increase in transported charge within 1 cm of the axis between the 1st and 5th pulses. The propagation range was 6 m. Channel depth is very sensitive to the amount of cooling present, ranging from around 1/4 ambient at the nozzle with no cooling to 1/2 with modest cooling. Four-to-one tailoring is sufficient for stable propagation to 6 m, if the initial offsets are under 0.1 mm. Hose displacement appeared to be more sensitive to initial displacement than to the presence of the channel. (Slinker, Hubbard, Ali, Fernsler, Joyce)

B. Air Chemistry Aspects of the ATA Multi-Pulse Experiment: A new air chemistry model for use in the propagation codes simulating the MPPE was developed by making analytic fits to benchmark runs with CHMAIR II. Range extension predictions were found to be not sensitive to the chemistry model. Beam stability was slightly worse. The use of CO₂ in the propagation chamber was also studied. It helps quench vibrational excitation of N₂, thereby opening the channel sooner. Although range extension can be seen without adding CO₂, its use, in small concentrations (~1%), is warranted. (SLinker, Ali)

C. Beam Propagation in Channels: This paper contains an overview of NRL research on propagation in channels and provides a brief summary of most of the other papers included in this report. Most of the work has been in support of the ATA Multi-Pulse Propagation Experiment (MPPE). Included are hose instability simulations, detailed air chemistry and channel physics calculations of ATA/MPPE. Simulation studies of SuperIBEX, PULSERAD and RADLAC propagation experiments are also briefly discussed. (Hubbard, Slinker, Taylor, Fernsler, Ali, Joyce, Boris)

D. Hydrodynamic Simulations of Beam-Generated Turbulence in Channels: A major uncertainty in the range extension simulations described in Section A above is the degree of convective mixing in the channel during the five pulse burst. To study this problem, we have developed a 2-D hydrodynamic simulation code which runs on NRL's new massively-parallel Connection Machine. The approach is the same as in the original Picone-Boris channel turbulence studies, but the simulations for MPPE parameters involve much longer time scales and require a finer mesh. Preliminary results indicate that the choice of a low value for the phenomenological convective mixing form factor used in the axisymmetric range extension simulations by Slinker, et al. is reasonable. (P. Boris, J. Boris, Hubbard, Oran, Picone, Slinker)
E. Sensitivity of Hose Instability to Frequency of Initial Perturbations in Low and High Current Beams: Increases in the solenoidal guide field $B_z$ used in the ATA accelerator tend to reduce the growth of high-frequency BBU growth in the accelerator but enhance the generation of low-frequency sweep within the pulse. Hose instability in the propagating beam arises from initial perturbations generated by BBU and/or sweep. To examine the trade-offs between these two effects, a series of SARLAC simulations of ATA/MPPE were performed with an 830 MHz BBU-like perturbation in the x-direction and a simple linear sweep in the y-direction. The relative amplitudes of these perturbations were estimated from analytical models. In all cases, the BBU-like perturbations grew more rapidly as the beam propagated in air and eventually dominated even when suppressed by a 3 kilogauss guide field. One encouraging result was that sweep amplitudes much larger than the 0.01 cm design target for ATA/MPPE could apparently be tolerated. The results strongly suggest that suppression of BBU growth will be an important operational consideration. Similar simulations were carried out for the higher current RADLAC parameter regime; these simulations also showed that high frequency perturbations were more dangerous. One should be aware that high frequency perturbations within the beam lead to low frequency oscillations in $z$ because the perturbations couple to hose in the beam head where the dipole decay length is short but the betatron wavelength is long. (Hubbard, Slinker, Taylor)

F. Beam Conditioning Options for the ATA Multi-Pulse Experiment:
Stable propagation of the ATA/MPPE beam in air will require a head-to-tail emittance variation. Three strategies have been considered for introducing this variation: a multi-foil cell, a passive IFR cell and a differential focusing cell. All three have been analyzed using analytical models and axisymmetric FRIEZR simulations, and all are capable in principle of producing substantial emittance tailoring. The multi-foil cell, however, will probably scatter the beam too much and produces a less favorable tailoring profile. The passive IFR cell appears to produce the best results, especially when operated at low gas pressures. The differential focusing cell requires careful tuning, but it offers considerable flexibility and is the most compatible with the sweep-correcting FCC system. Current plans call for using the differential focusing cell with IFR as a backup. (Hubbard, Slinker, Fernsler, Joyce, Ali)
BEAM STABILITY AND RANGE EXTENSION PREDICTIONS, FOR THE ATA MULTI-PULSE PROPAGATION EXPERIMENT

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Berkeley Research Associates

P. Boris
Science Applications Int. Corp.

Introduction. This paper summarizes our predictions for the ATA MPPE. For the nominal parameters, $I_b = 6$ kA, $r_b = 0.5$ cm, $\tau_p = 33$ ns, $N_p = 5$ pulses, we predict that range extension can be shown by charge collection diagnostics at propagation distances of 3-6 meters into full density dry air. Longer propagation distances were not analyzed. For maximum initial hose perturbations under 0.1 mm, hose amplification of under 70 is seen for 6 meters of propagation. Stability, measured as an offset at a fixed laboratory position, is comparable for the first and fifth pulses. A 4 to 1 emittance tailoring over 12 ns was assumed. It also appears that hose displacement, at least for moderate propagation distances, is determined more by the initial perturbation than by the channel.

Other papers$^{1-3}$ in these proceedings discuss various aspects of this experiment.

Simulation Model. Several codes, which have been developed over the years, were combined to model this problem. Propagation was done with the particle simulation codes SIMMO, for axisymmetric cases, or SARLAC, for non-axisymmetric studies. These codes dumped the beam current density at specified propagation distances. For SARLAC, the current density was symmetrized because the hydro models were one-dimensional. The current density and channel profile were input to the detailed air chemistry code CHMAIR II. This code calculates the beam deposition, population of species, and channel temperatures but does not assume hydrodynamic expansion. CHMAIR II simulated about 100 ns, enough time for ohmic deposition to finish and for the electron and vibrational temperatures to equilibrate. The particle densities are then
consolidated and used as input to HINT. HINT is a one-dimensional hydro
code which calculates the channel for the rest of the interpulse time
(-1ms). The channel for the next pulse is then input to the propagation
code and the process repeats for the next pulse. HINT has a simplified
air chemistry model which includes 7 species and the gas and vibrational
temperatures. It has cooling by thermal conduction, but not by
radiation. Non-axisymmetric cooling is modeled by the Picone-Boris theory. The fields are assumed to have decayed away.

**Axisymmetric Studies.** The following table summarizes the results of six
axisymmetric simulations of the MPPE:

### 5 PULSE AXISYMMETRIC PROPAGATION RESULTS

<table>
<thead>
<tr>
<th>Case</th>
<th>Chem.</th>
<th>Enhanced Cool. (f)</th>
<th>Enhanced Vib. Rel.</th>
<th>$\rho_{\text{min}}$ z=0m</th>
<th>$\rho_{\text{min}}$ z=4m</th>
<th>$Q_1$</th>
<th>$Q_5$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Old</td>
<td>0.0</td>
<td>No</td>
<td>.25</td>
<td>.64</td>
<td>11.0</td>
<td>20.4</td>
</tr>
<tr>
<td>B</td>
<td>Old</td>
<td>0.05</td>
<td>No</td>
<td>.53</td>
<td>.73</td>
<td>11.0</td>
<td>18.5</td>
</tr>
<tr>
<td>J</td>
<td>New</td>
<td>0.0</td>
<td>No</td>
<td>.26</td>
<td>.80</td>
<td>12.5</td>
<td>18.0</td>
</tr>
<tr>
<td>K</td>
<td>New</td>
<td>0.0</td>
<td>Yes</td>
<td>.25</td>
<td>.66</td>
<td>12.5</td>
<td>21.4</td>
</tr>
<tr>
<td>KM</td>
<td>New</td>
<td>0.05</td>
<td>Yes</td>
<td>.53</td>
<td>.74</td>
<td>12.5</td>
<td>18.9</td>
</tr>
<tr>
<td>KL</td>
<td>New</td>
<td>0.05</td>
<td>Yes</td>
<td>.55</td>
<td>.80</td>
<td>12.1</td>
<td>17.2</td>
</tr>
</tbody>
</table>

For Cases A and B the pulse separation was 1 ms; for the other cases it
was 1.25 ms. In Case KL the nominal beam radius was 0.6 cm. The "Old"
air chemistry is the standard VIPER model. The "New" air chemistry was
obtained by benchmarking MPPE-type beams with the detailed air chemistry
code CHMAIR II. The enhanced cooling factor f is the phenomenological
form factor in the Picone-Boris cooling theory which models
non-axisymmetry hydrodynamic effects by using an enhanced thermal
diffusivity. "Enhanced Vibrational Relaxation" means the inclusion of
carbon dioxide in the propagation chamber to thermalize the vibrational
energy of nitrogen to aid hole boring. $\rho_{\text{min}}$ is the minimum fractional
density at the entrance of the fifth pulse. $Q_1$ and $Q_5$ are the
transported charges (uc) for pulses 1 and 5 within 1.125 cm of the
chamber axis at a propagation distance of \( z = 6 \text{ m} \). Six meters is roughly twice the Nordsieck length of the initial pulse.

By comparing columns 7 and 8, all of these cases show at least an almost 50\% increase in transported charge clearly verifying range extension.

Cases A and J differ in two ways: pulse separation time and air chemistry model. Case A shows slightly better range extension properties, particularly in channel depth at large propagation ranges. Its shorter pulse separation time allowed less thermal cooling, but the major reason for the deeper channel is a 15\% greater direct deposition rate used with the "old" chemistry.

Non-axisymmetric hydrodynamic effects are modeled by using an enhanced thermal conduction

\[
\lambda_T = \rho c_p s^2 \tau \frac{1}{4\pi} \ln \left[ \frac{\rho_m}{\rho_0} \right] f, \quad \text{ergs/cm-sec-°K},
\]

where \( \tau \) is the pressure equilibration time and \( f \) is a form factor.\(^3,4\) We have chosen \( f = 0.05 \) assuming an individual pulse has a symmetric deposition and the offsets between pulses are small compared to a beam radius. Cases A and B and Cases K and KM differ only in the value of \( f \). A large difference in channel depth at the nozzle is shown even for \( f = 0.05 \). The channels with the nonzero \( f \) are slightly broader. At 4 m, the contrast is not as great. Charge transported 6 m is 10-15\% lower with enhanced cooling but it is still appreciably higher for the fifth pulse than the first one. The amount of cooling is difficult to predict and the MPPE results will be very valuable.

The only difference between Cases J and K is the addition of carbon dioxide in the propagation chamber to aid in the thermalization of the vibrational energy of nitrogen. The channels at the nozzle at the entrance of the fifth pulse are very similar although the Case K channel opened much sooner\(^2\). At larger propagation distances Case K is definitely better and 15\% better transport to 6 m is predicted. The use of carbon dioxide is recommended, though levels should be kept as low as possible, say ~1\%, to avoid other air chemistry effects.

Cases KL and KM differ only in the nominal beam radius, which was 0.5 cm for KM and 0.6 cm for KL. The broader beam showed only slightly worse range extension at 6 m.
Non-axisymmetric Studies. Three of the non-axisymmetric simulations will be discussed here. The first modeled the beam into ambient air. The other two considered the fifth pulse: in one simulation the beam was injected into the (axisymmetric) channel of Case KM and the other into the deeper channel of Case K. The initial maximum perturbation was 0.1 mm in the x or y direction with the standard form. Sensitivity to the exact form of the initial perturbation is discussed in Reference 1. The following table shows the total charge and deposition centroids for several propagation distances.

<table>
<thead>
<tr>
<th>Z(M)</th>
<th>X(CM)</th>
<th>Y(CM)</th>
<th>X</th>
<th>Y</th>
<th>X</th>
<th>Y</th>
<th>X</th>
<th>Y</th>
<th>X</th>
<th>Y</th>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.03</td>
<td>.03</td>
<td>.04</td>
<td>.04</td>
<td>.05</td>
<td>.03</td>
<td>.04</td>
<td>.03</td>
<td>.04</td>
<td>.03</td>
<td>.04</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>-.12</td>
<td>-.10</td>
<td>-.15</td>
<td>-.15</td>
<td>-.16</td>
<td>-.17</td>
<td>-.13</td>
<td>-.12</td>
<td>-.16</td>
<td>-.16</td>
<td>-.15</td>
<td>-.16</td>
</tr>
<tr>
<td>3</td>
<td>-.10</td>
<td>-.15</td>
<td>-.03</td>
<td>-.10</td>
<td>.00</td>
<td>-.06</td>
<td>-.10</td>
<td>-.16</td>
<td>-.02</td>
<td>-.11</td>
<td>.00</td>
<td>-.06</td>
</tr>
<tr>
<td>4</td>
<td>.10</td>
<td>.04</td>
<td>.20</td>
<td>.15</td>
<td>.25</td>
<td>.20</td>
<td>.11</td>
<td>.04</td>
<td>.21</td>
<td>.16</td>
<td>.23</td>
<td>.19</td>
</tr>
<tr>
<td>5</td>
<td>.28</td>
<td>.25</td>
<td>.28</td>
<td>.28</td>
<td>.22</td>
<td>.36</td>
<td>.30</td>
<td>.27</td>
<td>.29</td>
<td>.30</td>
<td>.21</td>
<td>.33</td>
</tr>
<tr>
<td>6</td>
<td>.15</td>
<td>.19</td>
<td>-.06</td>
<td>-.06</td>
<td>-.06</td>
<td>-.23</td>
<td>.16</td>
<td>.20</td>
<td>-.07</td>
<td>-.07</td>
<td>-.07</td>
<td>-.21</td>
</tr>
</tbody>
</table>

Through 5 m the centroids of all three pulses track each other to within a millimeter. This indicates that the hose displacement is determined more by the initial perturbation than by the presence of the channel. Thus, employing a moveable charge collection diagnostic to catch the hosing beams may be successful. The maximum offset of any beam slice in the beam body is around 0.5-0.7 cm for all three cases over the 6 m range.

Conclusions. If the design parameters are met, the MPPE should be successful. The beam will be stable enough to travel over 6 m and dig enough of a channel to show range extension. Beam stability will not be very sensitive to the channel. The greatest unknown will be the effect of anomalous cooling.
References.

1. R.F. Hubbard, et al., "Sensitivity of Hose Instability to Frequency of Initial Perturbations in Low and High Current Beams", these proceedings.

2. S. Slinker, et al., "Air Chemistry Aspects of the ATA Multipulse Experiment", these proceedings.


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Air Chemistry Aspects of the ATA Multipulse Experiment

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Introduction. Two studies involving air chemistry aspects of the MPPE are discussed in this paper. The first study develops a simple air chemistry model, appropriate for the conditions encountered in the MPPE, which was incorporated in the propagation codes SIMMO and SARLAC. The second study considers the use of carbon dioxide in the experimental tank to help relax the beam-pumped vibrational excitation energy of nitrogen in order to aid channel formation. How the results of these studies affect the predictions for the MPPE are discussed elsewhere in these proceedings.

Air chemistry model. The air chemistry relevant to intense beam propagation and channel formation is quite complex and can be sensitive to reaction rates. Air chemistry codes involving many species and reactions have been written which describe the situation in great detail. However, these models are much too expensive computationally to be directly coupled to a propagation code and so simplified air chemistry models need to be written. An equation for electron production is used which has bulk coefficients for the various processes. These coefficients are functions of the reduced electric field only. They are found from benchmark runs with the detailed air chemistry code CHMAIR II.

The propagation code model equations for the electron production and conductivity are

\[ \frac{dn_e}{dt} = \frac{1}{\Delta W} \frac{d}{dx} J_b \left( \frac{1}{e} + \frac{1}{\sigma} \right) \left\{ \alpha(\xi)n_e - \beta(\xi)n_e^2 - \chi(\xi)n_eP \right\} \]

and

\[ \sigma = \frac{e^2}{m} \frac{n_e}{v_0(\xi)P + v_1(n_e,T_e)} \]

where \( n_e \) is the electron density, \( \sigma \) is the conductivity, \( \Delta W \approx 34 \text{ eV/ion-pair} \), \( d\xi/dx \approx 2500 \text{ eV/cm} \), \( J_b \) is the beam current density, \( P \) is the

*Work supported by the Defense Advanced Research Projects Agency, ARPA Order No. 4395, Amendment No. 80, monitored by the Naval Surface Warfare Center.
fractional background density and $\nu_{ei}$ is the electron-ion collision frequency. The bulk coefficients are the avalanche coefficient $\alpha$, the recombination coefficient $\beta$, the attachment coefficient $\chi$, the electron-neutral collision frequency $\nu_m$ and the electron temperature $T_e$. These are all functions of $\xi = E/N$, the electric field over the particle density.

The five bulk coefficient functions are obtained from fitting data from a 4 pulse MPPE holeboring run with CHMAIR II. The data were taken at 0, 2, 4 and 6 m from the nozzle and at 14 radial points, 0 to 2.5 cm from the axis. The simple two parameter fitting form $A \exp (B \xi)$ was chosen. There is no fundamental reason for choosing this form other than simplicity. In practice, rather than calculate the chemistry coefficients on the run, the propagation codes create tables of the coefficients indexed by the reduced electric field and then do fast table lookups.

### PROPAGATION AIR CHEMISTRY USED FOR THE MPPE SIMULATIONS

<table>
<thead>
<tr>
<th>COEF.</th>
<th>A</th>
<th>B</th>
<th>RANGE</th>
<th>COEF.</th>
<th>A</th>
<th>B</th>
<th>RANGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$</td>
<td>2.73x10^-9</td>
<td>1.32</td>
<td>0&lt;\xi&lt;11.19</td>
<td>$\nu_m$</td>
<td>5.82x10^{11}</td>
<td>1.234</td>
<td>0&lt;\xi&lt;3.02</td>
</tr>
<tr>
<td>1.54x10^{-5}</td>
<td>0.548</td>
<td>11.19&lt;\xi&lt;30</td>
<td>7.66x10^{11}</td>
<td>0.0327</td>
<td>3.02&lt;\xi&lt;12.99</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.78x10^{-2}</td>
<td>0.3129</td>
<td>30&lt;\xi&lt;65</td>
<td>8.85x10^{11}</td>
<td>0.0215</td>
<td>12.99&lt;\xi</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8.02x10^{3}</td>
<td>0.1126</td>
<td>65&lt;\xi&lt;200</td>
<td>$T_e$</td>
<td>0.187</td>
<td>0.1233</td>
<td>0&lt;\xi&lt;3.69</td>
<td></td>
</tr>
<tr>
<td>$\beta$</td>
<td>1.45x10^{-7}</td>
<td>-0.234</td>
<td>0&lt;\xi&lt;4.93</td>
<td>0.255</td>
<td>0.0389</td>
<td>3.69&lt;\xi&lt;13.88</td>
<td></td>
</tr>
<tr>
<td>4.87x10^{-8}</td>
<td>-0.0124</td>
<td>4.93&lt;\xi</td>
<td>0.306</td>
<td>0.0257</td>
<td>13.88&lt;\xi</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\chi$</td>
<td>3.75x10^{-7}</td>
<td>-0.159</td>
<td>0&lt;\xi&lt;6.49</td>
<td>0.49x10^{-6}</td>
<td>0.649</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

( $\xi$ is measured in Townsends: 1 Td = $10^{-17}$ \(v-\text{cm}^2\) = 246 \(v/\text{cm}\) @ 1 atm.)

Several differences with the "VIPER" air chemistry model which has been our standard propagation model can be noted. Attachment was not in the VIPER chemistry. The avalanche ionization coefficient is much higher here at low values of $\xi$. This is because there is considerable nitrogen oxide ($\sim 10^{16}$) in the channel and it is easier to ionize than $N_2$ or $O_2$. Nevertheless, avalanche ionization is a very small effect for MPPE parameters. Because of clusters the bulk recombination coefficient is larger than the VIPER value. No systematic study has been made to show the effect of the chemistry model change on beam stability predictions. The initial pulse into ambient air shows the hose growth to be slightly larger with the new chemistry. Range extension predictions are not altered. \(^1\)
Vibrational Relaxation of Nitrogen. Considerable beam-deposited energy can be tied up in the vibrational excitation of nitrogen. The relaxation time, which depends on the gas and vibrational temperatures and the composition, can be quite long (>ms). If that energy could be released rapidly into thermal energy, hole boring would be faster. One technique for doing this is to add a buffer gas which has the property that it quenches the vibrational excitation. Two candidates are water vapor and carbon dioxide. Both of these are present in ambient air. Because water vapor enhances cluster formation and attachment, possibly affecting beam stability, carbon dioxide should be a better first choice. McDonnell-Douglas has shown experimentally that the addition of carbon dioxide can aid in channel formation and a simple analysis by Ali et al.\textsuperscript{2} has shown this to be the case.

The following rates (cm\(^3\)/sec) are used to relax the vibrational energy: \(8.5 \times 10^{-7} \exp(-12.06/T^{1/3})\) for collisions with \(N\) and \(O_2\), \(1.07 \times 10^{-10} \exp(-3.18/T^{1/3})\) for collisions with \(O_2\), \(6 \times 10^{-13}\) for collisions with \(CO_2\) and \(3.1 \times 10^{-15}\) for collisions with \(H_2O\).

Two MMPE runs were made to illustrate the effect of carbon dioxide in the propagation chamber. CASE J had an initial background of 80% nitrogen and 20% oxygen. CASE K had 80% nitrogen, 20% oxygen and 0.03% carbon dioxide (=7.4 \times 10^{15} /cc). This is about the normal carbon dioxide particle density in ambient air. With the rate quoted this gives a relaxation time of \(\sim 0.2\) ms. The dissociation fraction of the carbon dioxide was assumed to be the same as that of nitrogen and oxygen and the density was proportional to the local density. No other chemistry effects of carbon dioxide were included.

The graph shows the channel conditions at propagation distances of \(z = 0, 2, 4, 6\) m at the entrance of the fifth pulse. At the nozzle the channels with and without carbon dioxide are similar. This is because the temperature has been raised enough and there is sufficient atomic oxygen around that the other channels for vibrational relaxation are open. Nevertheless, the hole at the nozzle was opened quicker in the carbon-dioxide-aided case. At greater propagation distances the channel is clearly deeper for CASE K.

Charge transport results predict that either case will show range extension. However, the addition of carbon dioxide to the propagation chamber is probably worth the effort. Bieniosek (private communication).
was not able to see channel enhancement until the fraction of carbon dioxide was around 1% or greater, and he found the best effect was with 6%. This may indicate that the rate quoted above was too high or else the efficiency for transfer of the excited carbon dioxide energy to heat is less than expected. A few percent of carbon dioxide may not alter the air chemistry much, however, carbon dioxide has a momentum transfer cross section \( \geq 10 \) times that of nitrogen at electron energies \(< 0.2 \text{ eV} \) and also it decreases as the electron energy increases. These complications suggest using the minimum amount having the desired effect. However, a detailed analysis of energy exchange and radiation from \( \text{CO}_2 \) is required for a comprehensive understanding of the role of \( \text{CO}_2 \) in hole boring.

References.
1. S. Slinker, et al., "Beam Stability and Range Extension Predictions For the ATA Multi-Pulse Propagation Experiment", these proceedings.
BEAM PROPAGATION IN CHANNELS

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I. INTRODUCTION

Beam propagation in density channels is a major focus of the current DARPA experimental program. The ATA Multi-Pulse Propagation Experiment (MPPE) will attempt to demonstrate stability, tracking, and range extension in the channel formed by a five-pulse burst of 10 MeV, 6-8 kA beams. Also, tracking experiments at NRL using the PULSERAD and SuperIBEX beams in laser-guided electric discharge (LGED) channels are in progress. This paper provides an overview of theoretical work at NRL in support of these propagation experiments. More detail can be found in Refs. 1-7.

II. ATA MULTI-PULSE PROPAGATION STUDIES

Overview: Detailed predictions for an ATA/MPPE burst require treatment of the complicated coupling between beam propagation and channel physics over times scales up to 5 msec. To address these problems, we have carried out five-pulse axisymmetric simulations which combine existing NRL propagation and channel physics codes. The results are used to predict the range of each pulse and to provide realistic channels for SARLAC hose stability simulations. Supporting these simulations are more detailed studies of air chemistry effects and convective cooling. We have also studied the sensitivity of lead pulse hose instability growth to the amplitude of BBU and corkscrew-induced perturbations and choice of emittance tailoring method. We have assessed the feasibility of an ATA pulse-decoupling experiment.

Typical parameters for these studies are beam energy $E_0 = 10$ MeV, peak current $I_0 = 6$ kA, nominal beam radius $a_b = 0.5$ cm, pulse length $T_p = 33$ nsec, pulse separation $T_s = 1.25$ msec, and an emittance variation of 4:1.

Multi-pulse axisymmetric propagation and channel dynamics: In these simulations, the SIMMO particle code is used for $\tau < T_p$ to propagate the beam and dump beam current density $J_b(r, \zeta, z)$. Here, $\zeta$ is the distance from the
beam head, z is the propagation distance, and $\zeta = \zeta T = \zeta T - z$. CHMAIR II uses the $J_b$ input from SIMMO to calculate beam and ohmic deposition and detailed air chemistry for $\tau < \tau < 2 \tau_p$ at several $z$-locations. HINT is then used to calculate the long-time-scale behavior of the channel ($\tau < \tau_s$), including the effects of hydrodynamic expansion, thermal and convective cooling, and vibrational relaxation. This generates a density profile, $\rho(r,z)$, which is input into SIMMO for the next pulse in the burst, and the process is repeated.

Six simulations were run to determine the sensitivity of the channel depth and the transported beam fluence to model assumptions. The fluence, $Q_n(R,z)$, is defined as the transported beam charge for the $n$th pulse within a radius, $R$, of the beam axis at a fixed location $z$. The ratio $Q_5/Q_1$ for $R = 1.1$ cm and $z = 6$ m varied between 1.4 and 1.85, indicating modest range extension. The channel depth at $z = 0$ was very sensitive to the assumed Picone-Boris form factor $f$ for convective cooling; the on-axis density at the fifth pulse was a factor of two higher when $f$ was raised from 0 to 0.05. However, the predicted fluence at $z = 6$ m changed by less than 15% because the convectively-cooled channel was significantly broader. Changes in the assumed chemistry model for SIMMO and the inclusion of enhanced vibrational cooling from CO$_2$ produced only modest changes in the fluence.

Chemistry effects and convective cooling in ATA/MPPE: A new chemistry model for SIMMO and SARLAC was developed using these same basic approach as in the standard "VIPER" model. The new model includes attachment and revised rate coefficients benchmarked against detailed CHMAIR II calculations in the ATA/MPPE regime. The new model gives similar axisymmetric behavior and generates slightly more hose instability growth. The second major focus of the air chemistry studies was a treatment of the transfer of the energy stored in N$_2$ vibrational excitations to gas heating. This process occurs on the millisecond time scale but can be speeded up by adding a small amount of CO$_2$.

The Picone-Boris convective cooling form factor, which we and others have used in MPPE hydro simulations is a phenomenological model which has not been benchmarked against full 2-D hydro code results in the appropriate parameter regime. A new 2-D hydro code that treats the convective cooling process directly has been developed. The code runs on NRL’s massively-parallel Connection Machine and is much faster than the version used by Picone and Boris. Preliminary results suggest that the value $f = 0.05$ used in the HINT code is reasonable for the level of asymmetry expected for ATA/MPPE.
Hose instability growth in MPPE: SARLAC simulations\(^1\) have been carried out in the channels generated by the SIMMO-CHMAIR-HINT simulation sequence described above. Hose amplitudes in the beam body grow from an assumed initial level of 0.01 cm to 0.5-0.7 cm in 6 m of propagation. Similar hose amplitudes were observed in the absence of a channel.

Increasing the guide field \(B_z\) in ATA increases low frequency sweep displacements but suppresses high frequency BBU-induced perturbations.\(^4\) The effect of this tradeoff on hose instability was investigated using SARLAC by initiating a BBU-like mode in \(x\) and a linear sweep in \(y\). The BBU-induced mode was much more unstable in the simulations, while relatively large sweep amplitudes could be tolerated. In one set of SARLAC runs, increasing \(B_z\) from 1 to 3 kG caused hose amplitudes at \(z = 6\) m to drop by almost a factor of 3.

Other SARLAC simulations considered the effects of different possible emittance tailoring techniques.\(^5\) Beam radius and emittance profiles were generated by FRIEZER for various tailoring schemes, and the results were used to initialize SARLAC. A multi-foil tailoring cell simulation produced hose amplitudes in excess of 1 cm in 4.8 m of propagation, while a similar run using a 5 mtorr IFR cell grew to only 0.1 cm.

Pulse decoupling experiment for ATA:\(^6\) SARLAC was used to investigate the feasibility of studying pulse decoupling experimentally on ATA by applying a weak deflecting guide field just before the last pulse. The simulation results suggest that the phenomenon would likely be obscured by wall forces.

Summary: The ATA/MPPE beams are likely to propagate with only moderate hose growth if the stringent beam conditioning goals are met. Range extension effects should be modest but observable.

III. SUPERIBEX AND PULSERAD TRACKING STUDIES

PULSERAD stability and tracking simulations: A data base now exists for the 1988 NRL tracking experiments which used the 1 MeV PULSERAD beam. SARLAC simulations were performed with a weakly-tailored beam with the estimated experimental parameters. The hose amplitudes were somewhat higher in a centered density channel than in full density air, but the difference could be attributed entirely to scattering effects. Increasing \(I_0\) appeared to destabilize the beam. The tracking distance was typically 30 cm. All of these results are consistent with the experimental data.
SuperIBEX stability and tracking simulations: SARLAC was used to model the 4.5 MeV SuperIBEX tracking experiments currently in progress. The simulations assumed moderate emittance tailoring and relatively large amplitude, but low frequency initial hose perturbations. Peak simulation beam currents varied between 10 and 40 kA. Hose amplitudes increased with I₀ and were smaller in the presence of a channel than in full density air, in contrast to the PULSERAD result. Tracking distances were predicted to be only 20-30 cm in the presence of an offset channel.

A separate series of SARLAC simulations modeled propagation in a 10 m long tank in uniform 0.5 atm air and in a centered, 0.1 atm density channel. The beam was well-conditioned, as might be produced by a two-stage IFR/active-wire conditioning cell currently being considered for future experiments. The perturbations were the same as used in the RADLAC simulations described in Ref. 4. Hose amplitudes grew to only 0.2-0.3 cm in the SuperIBEX simulations.

Summary: PULSERAD simulation results were consistent with the data from the successful 1988 tracking experiment. Simulations of the current SuperIBEX tracking experiment predict short tracking distances and moderately-strong hose growth. Future SuperIBEX experiments with well-conditioned beams could exhibit "stable" propagation to ranges beyond 10 m.

IV. REFERENCES

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** Berkeley Research Associates, Springfield, VA 22150
*** Science Applications International Corp., McLean, VA 22102
HYDRODYNAMIC SIMULATIONS OF BEAM-GENERATED TURBULENCE IN CHANNELS*

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INTRODUCTION

Heated columns or channels have been produced at several laboratories using lasers, guided discharges, or propagating relativistic electron beams. These experiments\(^1\) have shown that turbulent or convective mixing of the hot air with the cooler gas outside the channel causes the channels to cool much more rapidly than expected from classical thermal conduction. Picone and Boris\(^2\) modeled this process using a standard 2-D FCT hydro code and developed simple phenomenological models for incorporating convective cooling in axisymmetric models. These simple models use a form factor \(f\) to model the cooling process and have been used by several groups\(^3,4\) to predict range extension effects in the upcoming ATA Multi-Pulse Propagation Experiment (ATA/MPPE).

ATA/MPPE will attempt to produce beams which can propagate with modest hose instability growth, thus producing nearly axisymmetric deposition patterns. However, most previous experiments and simulations treated cases with highly asymmetric deposition profiles, so relatively little is known in the regime of interest to ATA/MPPE. In this paper, we describe 2-D hydro calculations using a new FCT\(^5\) algorithm developed for NRL's massively-parallel Connection Machine. Since the time scales of interest for ATA/MPPE are much longer than those in the original Picone–Boris study\(^2\) and a finer spatial grid is required, these simulations would have been very expensive to run on a CRAY. A major goal of this study is to estimate the scaling of the Picone–Boris form factor \(f\) in the nearly-axisymmetric regime.

PROBLEM DEFINITION

A version of the LCPFCT\(^6\) code was run for several sets of possible ATA/MPPE parameters. Both two pulse and five pulse cases were studied. The turbulence problems were set up on a 256 by 256 grid with periodic boundary conditions. Both a stretching and a damping factor were added to the grid in order to limit errors caused by reflected shock waves feeding back into the calculations through the boundary conditions. The simulations assumed that the first pulse generated a smooth gaussian density depression, and the calculations began at the arrival of the second pulse, which created an offset gaussian overpressure. In the five pulse cases, a third pulse was added after 2.0 ms, a fourth after 4.0 ms, and so forth. Each pulse after the second was offset from the channel center randomly in a square pattern at a distance \(L\) 0.5 cm in this case. The random placement of these pulses simulated the inherent uncertainty in aiming the particle beam in the experiment.

The physical parameters for the two pulse case were: characteristic channel radius, \(R_c = 0.800\) cm, characteristic beam radius, \(R_b = 0.600\) cm, channel center density, \(\rho_c = 8.90 \times 10^{-4}\) gm/cc, and beam center overpressure, \(\delta P_b = 2 \times P_a\). The numerical parameters were set to a cell size of 0.1 cm in both the x and y directions and to a simulation run time of 2.0 ms.
The multi-pulse case had these parameters: characteristic channel radius, $R_c = 0.888$ cm, characteristic beam radius, $R_b = 0.600$ cm, channel center density, $\rho_c = 5.90 \times 10^{-4}$ gm/cc, and beam center overpressure, $\delta P_b = 2 \times P_a$. The numerical parameters were set to a cell size of 0.1 cm in both the x and y directions and to a simulation run time of 6.8 ms.

DESCRIPTION OF CODE

Compressible gasdynamic problems generally involve both rotational effects (vortices, turbulence, etc.) and compressible effects (sound waves, shocks, etc.) but are described by a set of multidimensional continuity equations (partial differential equations) which express the physical laws of mass, momentum, and energy conservation. In 2-D gasdynamics there are four continuity equations all having basically the same form. Each of these equations requires an accurate, high-resolution algorithm for its solution because fluid problems generally generate very steep gradients in the solution such as at shocks and vortex interaction boundaries.

Each of the four individual continuity equations, in each of the two Cartesian directions is solved by a single, highly optimized algorithm called Flux-Corrected Transport which guarantees the physically important positivity property of fluid mass and energy densities. This fluid convection module to solve the set of coupled continuity equations, is the most recent one-dimensional version of the FCT algorithm. This flexible general module is used with direction and timestep splitting to construct two-dimensional simulations which allow physically realistic boundary conditions in a number of non-periodic geometries. The kernel of the algorithm consists of about 30 lines of C-star which has been specifically designed and optimized for parallel computation on the Connection Machine.

A Connection Machine consists of many thousands of individual scalar processors connected in a hypercube configuration. Communication to and control of these processors is through a front-end computer. At NRL, there are two Connection Machines, one with 16,384 (16K) processors and one with 8,192 (8K) processors. The user controls these through one of several kinds of front ends: a VAX, a Symbolics, or a Sun. Each of the individual processors can be reconfigured into a larger number of virtual processors, typically in powers of two, the actual number limited by the storage required for the algorithm and the size of the computational grid. Floating-point arithmetic is carried out by Weitek chips, each of which does pipelined processing of the floating-point operations for 32 of the scalar processors.

RESULTS

In order to estimate the Picone–Boris form factor, $f$: the equation given by $f = \kappa / g(\delta P_b / P_a)(R^2_b / \tau_{eq}) \ln(\rho_a / \rho_c)$ must be solved. Here, $\kappa$ was the integrated vortex filament strength, $g = (R_{bf} - R_b)^2 / R^2_b$ was a measure of the beam expansion rate to its final value $R_{bf}$, $\delta P_b$ was the beam-generated overpressure, $P_a$ was the ambient pressure, $\tau_{eq}$ was the equilibration time for the vortex filament strength, and $\rho_a$ and $\rho_c$ were the ambient and channel densities, respectively. For the parameters listed above, the quantity $g = 0.23$.

Values of $f$, $\kappa$, and $\tau_{eq}$ are listed in table 1 for various values of the beam–channel offset, $L$. Table 1 yielded the graph in figure 1 which represented one curve of the family of curves that make up the form factor. The curve obtained by this code strongly resembled the curves generated by Picone and Boris and for $L < R_b$, $f$ was proportional to $L$, thus supporting the
assumptions made in Ref. 3.

The following pictures show graphically the turbulent effects that can occur with multiple particle beams in air. The first set of parameters was for a two pulse simulation and figures 2 and 3 show density contours and vorticity contours. The second set of parameters was for a five pulse case where figures 4 and 5 correspond to the same quantities as described in the two pulse case.

CONCLUSIONS

Figure 2 showed that over the 2 ms time scales of relevance for ATA/MPPE the channel did not deform significantly for the listed parameters. This figure, coupled with the lack of turbulence seen on the vorticity plot in figure 3 and with the velocity data taken from the FCT code (vmax after equilibrium of 2-3 meters/second) lead to the conclusion that turbulence won’t be a factor in the two pulse experiments.

The five pulse case was very different, however. Figure 4 showed much greater channel deformation after the fifth pulse than was seen in the two pulse case. This deformation, added to the complex vorticity pattern shown in figure 5 and the large maximum fluid velocities (10-15 meters/second) lead to the conclusion that turbulence would play a major role in the beam propagation experiment modeled by this simulation. The turbulence effect could be lessened if the beam-channel offsets are kept small (i.e. less than ≈ 0.1 Rb) and interpulse separation short (i.e. less than ≈ 1 ms).

The beam-channel offset used for the five pulse simulations in this paper was probably too large for the ATA/MPPE experiment. The pulse to pulse overpressure ratio in the actual experiment will decrease with pulse number. As a result of these factors, more simulations will have to be conducted to better model the experiment.

REFERENCES

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* Supported by the Defense Advanced Research Projects Agency, ARPA Order No. 4395.
* Amendment 80, monitored by the Naval Surface Warfare Center.
** Science Applications International Corp., Mclean, VA
Table 1: Form Factor Terms

<table>
<thead>
<tr>
<th>L</th>
<th>$\kappa$ (cm$^2$/sec)</th>
<th>$\tau_{99}$</th>
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<tr>
<td>0.0</td>
<td>0.0</td>
<td>0.0 $\mu$s</td>
<td>0.0</td>
</tr>
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<td>44.5 (cm$^2$/sec)</td>
<td>90 $\mu$s</td>
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<tr>
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<td>148.2 (cm$^2$/sec)</td>
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<td>62.3 (cm$^2$/sec)</td>
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</table>

Fig. 1: Form Factor Curve

Fig. 2: Two-Pulse Density Contour

Fig. 3: Two-Pulse Vorticity Contour

Fig. 4: Multi-Pulse Density Contour

Fig. 5: Multi-Pulse Vorticity Contour
SENSITIVITY OF HOSE INSTABILITY TO FREQUENCY OF INITIAL PERTURBATION IN LOW AND HIGH CURRENT BEAMS

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I. INTRODUCTION

Most studies of resistive hose instability in propagating electron beams have assumed that the frequency spectrum of the initial perturbation cannot be experimentally controlled. However, Fawley has pointed out that for the ATA Multi-Pulse Propagation Experiment (MPPE), the relative amplitudes of low frequency sweep and high frequency (BBU-induced) perturbations are sensitive to the guide field, $B_z$, in the accelerator. Increasing $B_z$ reduces the growth of BBU but enhances corkscrew-induced sweep.

We have used the SARLAC hose instability code to determine which class of perturbations is the more dangerous. SARLAC models beam propagation in the atmosphere using the doppler-shifted coordinates $z$ and $\zeta = \omega t - z$. Here, $z$ is the propagation distance in air and $\zeta$ is the distance from the beam head. A BBU-like 830 MHz perturbation, $X(\zeta,z=0)$, is imposed in the $x$-direction using an asymptotic BBU growth model from Caporaso. A low frequency (LF) sweep perturbation is imposed in the $y$-direction. In general, the hose growth in the $x$-direction dominates even when its initial amplitude is substantially lower, suggesting that ATA should be operated with a high $B_z$. Similar results have been obtained by Feinstein and Keeley. HF perturbations also generate more instability growth in RADLAC simulations. These HF perturbations initiate hose growth in the "neck" of the beam where the dipole decay length is relatively short. Since the local betatron wavelength is usually long in this region, an HF perturbation may generate low frequency oscillations in $z$.

II. ATA HOSE SIMULATIONS

BBU perturbation model: Following Caporaso, the beam exits the accelerator with a displacement $X(\zeta,z=0) = X_0 \exp(KN_{b_{0}}(\zeta)Z_0/\omega_0/B_z) \sin(\omega_0 \zeta/c)$. Here, $I_{b_{0}}$ is the beam current in kA, the cavity impedance $Z = 30 \Omega$, $\omega_0/2\pi = 8.3 \times 10^8$ sec$^{-1}$, the number of cavities $N = 50$, $B_z = 1-3$ kG, $X_0 = 10^{-4}$ cm and
the coefficient $K = 1.16 \times 10^{-13}$ kG-sec(kA-ohm)$^{-1}$. The beam is assumed to have an energy of 10 MeV with the current ramping to its nominal value $I_0 = 6$ or 8 kA over a distance $\zeta_r = 360$ cm. The injected radius and emittance profiles follow the form shown in Fig. 4 of Ref. 4 which are generated from a FRIEZR simulation of a 5 mtorr passive IFR conditioning cell.

Corkscrew or sweep perturbation model: Low frequency sweep or corkscrew arises from the coupling between energy variations $\Delta \gamma$ within the pulse and field or alignment errors. This produces a phase advance, $\delta \phi = (\Delta \gamma/\gamma) f_k dz$, where the cyclotron wavenumber $k_c$ is proportional to $B_z$. For $\delta \phi \ll 1$, the phase advance and sweep amplitudes are proportional to $B_z$. In SARLAC, this effect is modeled by imposing an initial perturbation in the $y$-direction given by $Y(\zeta, z=0) = \alpha B_z \zeta$. The coefficient $\alpha$ is chosen to be $3 \times 10^{-5}$ (kG)$^{-1}$.

Results: Four long SARLAC simulations were run with the parameters described above. Cases A1, A2 and A4 were for $I_0 = 6$ kA and $B_z = 1, 1.5$ and 3 kG, respectively, while Case A3 used an 8 kA beam with a 1.5 kG guide field. Results are summarized in the table below. The displacements $X$ and $Y$ are taken in the beam tail at $\zeta = 750$ cm (25 nsec) and are tabulated at injection ($z = 0$) and at $z = 5.4$ m.

<table>
<thead>
<tr>
<th>Case</th>
<th>$I_0$ (kA)</th>
<th>$B_z$ (kG)</th>
<th>$X(0)$ (cm)</th>
<th>$Y(0)$ (cm)</th>
<th>$X(5.4m)$ (cm)</th>
<th>$Y(5.4m)$ (cm)</th>
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<td>0.0006</td>
<td>0.068</td>
<td>0.11</td>
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</table>

Figure 1 plots the initial perturbations $X(\zeta, 0)$ and $Y(\zeta, 0)$ for Case A2, showing that the HF perturbation (solid curve) is an order of magnitude lower than the sweep perturbation (dashed curve). However, Fig. 2 shows that at $z = 6$ m, the HF modes induced in the $x$-direction have surpassed those in the $y$-direction. Increasing $I_0$ to 8 kA results in a substantial increase in $X$, both because the BBU-induced initial perturbation is larger and because the higher current beam travels more betatron wavelengths. The resulting hose amplitudes are shown in Fig. 3. The results suggest that ATA should be operated with a relatively high guide field to suppress BBU and that relatively large sweep amplitudes may be tolerated without initiating serious instability growth.
III. RADLAC HOSE INSTABILITY SIMULATIONS

Overview: Both HF and LF perturbations are produced in RADLAC even though BBU is thought to be unimportant. A series of SARLAC simulations were performed using a 0.02 cm, 830 MHz HF perturbation in x and a 0.2 cm (at $\zeta = 900$ cm) sweep perturbation in y. Nominal beam parameters in the simulations were $I_0 = 25$ kA, $Y_0 = 41$ (ramped in some cases), beam radius $a_b = 2$ cm, rise length $\zeta_r = 300$ cm and normalized emittance taper $\epsilon_t = 2-4$.

RADLAC simulation results: Six simulations were performed as described in the table below. $E_{\text{min}}$ and $E_{\text{max}}$ define the range of the energy ramp, and $X_{\text{max}}$ and $Y_{\text{max}}$ are the maximum hose amplitudes at $\zeta = 900$ cm and $z < 12$ m.

<table>
<thead>
<tr>
<th>Case</th>
<th>$E_{\text{min}}$</th>
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<th>$\eta_t$</th>
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<tr>
<td>R4</td>
<td>5</td>
<td>20</td>
<td>4</td>
<td></td>
<td>4.5</td>
<td>1.5</td>
</tr>
<tr>
<td>R5</td>
<td>5</td>
<td>20</td>
<td>4</td>
<td>$Y_0=0.02$ cm</td>
<td>4.5</td>
<td>0.6</td>
</tr>
<tr>
<td>R6</td>
<td>10</td>
<td>20</td>
<td>4</td>
<td>Faster y-ramp</td>
<td>1.1</td>
<td>0.4</td>
</tr>
</tbody>
</table>

As in the ATA simulations, the high frequency modes dominate even though they are initiated at a smaller amplitude. Comparing Cases R1 and R3, it is apparent that relying on the natural tailoring which comes about from the energy ramp may lead to unacceptably large hose amplitudes. This is, in part,
because the head is so hot that it is quickly lost, leaving behind a poorly-tailored beam. Even when the 4:1 emittance variation is restored to a beam with a γ-ramp (Case R4), the beam is more unstable than in the constant energy case. Figure 4 plots $X(z)$ and $Y(z)$ at $\zeta = 675$ cm for Case R4, showing an initial damping of the LF mode followed by an eventual coupling to the faster-growing HF mode. Hose amplitudes versus $\zeta$ at $z = 120$ cm are shown for this case (Fig. 5) and for the more unstable weakly-tapered Case R3 (Fig. 6).

![Graphs showing X(z) and Y(z) at ζ = 675 cm for RADLAC Case R4. Note initial decay in Y (dash line).](image)

IV. CONCLUSIONS AND REFERENCES

For both ATA and RADLAC, high frequency perturbations appear to couple more strongly to the resistive hose instability and should be suppressed if possible even at the expense of higher sweep amplitudes.

4. R. Hubbard et al, "Beam Conditioning Options for the ATA Multi-Pulse Expeiment," these proceedings.

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24
I. INTRODUCTION

The ATA Multi-Pulse Propagation Experiment (MPPE) will be the first serious attempt to study beam stability, tracking and range extension for a WIPS-mode pulse train. The accelerator is expected to produce 5 beam pulses separated by 1.25 msec with peak current \( I_0 = 6-8 \text{ kA} \), radius \( a_0 = 0.5 \text{ cm} \) and a nominal energy of 10 MeV. However, it is expected that the beam will be disrupted by the resistive hose instability unless a substantial head-to-tail variation in beam emittance is introduced.\(^1\) This paper examines three emittance tailoring techniques which are currently being considered for ATA/MPPE: a multi-foil cell, a classical (passive) IFR cell and a differential focusing or energy variation system. All three techniques introduce a beam radius variation \( a_b(\zeta) \) where \( \zeta = ct - z \) is the distance from the beam head; the beam is then passed through a final scattering foil which converts much of this variation to a variation \( \varepsilon_n(\zeta) \) in the normalized emittance. Our studies have primarily been performed using the FRIEZR axisymmetric simulation code.

II. MULTI-FOIL TAILORING CELLS

Description of technique: When a relativistic beam passes through a thin conducting foil, the radial electric field is shorted out, and the beam experiences a focusing force similar to that produced by a solenoidal magnetic lens.\(^2,3\) The focal length \( f_L \) scales with \( a_b \gamma / I_b \). Fawley\(^4\) has proposed using three thin foils positioned so that the beam body \( I_b = I_0 \) is focused to a small radius while the lower current beam head expands to a larger radius. Since \( \gamma \) is nearly constant in ATA, the radius profile \( a_b(\zeta) \) arises from the rise in beam current \( I_b(\zeta) \) in the beam head.

Modifications to FRIEZR simulation code: The FRIEZR code has been upgraded to include foil focusing, scattering, and solenoidal lenses. Foils and lenses may be located anywhere in the beamline. Foil focusing is treated using a thin lens approximation:\(^2,3\) each beam electron is given an inward impulse with a focal length whose variation with \( r \) is shown in Fig. 1 of Ref. 3, assuming a Bessel beam profile. Foil scattering is treated by imparting an appropriate random kick to each simulation particle as it passes through the
foil. Solenoidal lenses are treated by specifying a focal length $f_L$ at the lens location and adding an impulse $\delta p_x/p_Z = -x/f_L$ and $\delta p_y/p_Z = -y/f_L$.

**Simulation results for multi-foil cell:** A series of simulations were performed for a 6 kA, 10 MeV beam with an injection beam radius $a_b(0) = 0.8$ cm, wall radius $b = 7$ cm, beam rise length $\zeta = 360$ cm, initial normalized emittance $\varepsilon_n(0) = 0.5$ rad-cm and an upstream lens placed so that $da_b/dz = 0.03$ at the first foil. Carbon foils 2 mils thick were placed at $z = 0, 39$, and 50 cm with a thicker 30 mil foil at $z = 78$ cm. (Fawley suggested similar foil locations for a shorter three-foil cell). Figure 1 plots the half-current and rms beam radii (lower and upper curves, respectively) as functions of $\zeta$ at the final foil. The desired beam taper is produced with $a_{1/2}$ varying by a factor of 4.5. The corresponding emittance taper is shown in Fig. 2. At $\zeta = 600$ cm, $\varepsilon_n$ is almost a factor of four above its injection value. This is due primarily to scattering, but a portion arises from weak variations in focal length length contained in Eq. (1). The latter effect is proportional to $a_b \nu \beta / \gamma$ and can result in huge emittance increases for high $\nu \beta / \gamma$ beams such as SuperIBEX.

![Fig 1. Beam $a_{1/2}$ and $a_{rms}$ vs $\zeta$ at end of 78 cm long 2-2-2-30 mil carbon multi-foil cell.](image)

![Fig 2. Emittance vs $\zeta$ for the cell used in Fig. 1. Location is just after final foil.](image)

![Fig 3. Beam $a_{1/2}$ and $a_{rms}$ vs $\zeta$ at end of 78 cm long 5-5-5-30 mil carbon multi-foil cell.](image)

When foil scattering is eliminated, the minimum half-current radius drops from 0.7 cm to 0.4 cm. However, even 2-mil foils are unlikely to survive multi-pulse ATA operation. When the first three foils are 5-mil, $a_b$ rises to an unacceptable 1.3 cm, as shown in Fig. 3. Thus, foil scattering may severely limit the usefulness of this technique for ATA. Also, the relatively sharp radius taper in Fig. 1 is not favorable for hose stabilization.
III. PASSIVE IFR TAILORING CELL

Description of technique: Passive or classical IFR cells have been extensively used on ATA in the past to taper the beam. The beam is passed through a low pressure gas, producing a plasma column whose density, \( n_1(\zeta) \), increases during the pulse. Provided \( n_1 < n_b \), the radial electric field produced by the beam density, \( n_b \), expels plasma electrons, leaving behind an ion column which electrostatically pinches the beam. FRIEZER has been extensively used in the past to model such conditioning cells.

IFR cells in multi-pulse operation: Although passive IFR cells have not been operated in a multi-pulse machine, we believe the beam will be tailored in the same manner as in single pulse operation. The dominant atomic physics process between pulses is expected to be charge exchange between fast ions and ambient neutral gas atoms or molecules. Hole boring should be insignificant because the collisional mean free paths are large at these gas densities. By the time the next pulse arrives, the plasma density is expected to be much too low to influence the beam. We believe that IFR cells on ATA have performed well, especially considering the inverse tailoring apparently produced by laser-ion guiding in the accelerator.

Fig 4. Beam \( a_{1/2} \) and \( a_{\text{rms}} \) vs \( \zeta \) at end of a 5 mtorr passive IFR cell.

Fig 5. Beam emittance vs \( \zeta \) just before final scattering foil for the IFR cell in Fig. 4.

Fig 6. Beam \( a_{1/2} \) and \( a_{\text{rms}} \) for a differential focusing cell with a 20% energy variation.

Simulation results for a passive IFR cell: Although most experiments and simulations in the past have utilized IFR cell pressures of 20 mtorr or higher, lower pressures may be more effective if the beam emittance is not too large. Figure 4 plots \( a_{1/2}(\zeta) \) and \( a_{\text{rms}}(\zeta) \) at \( z = 90 \text{ cm} \) for a beam similar to that described in the previous section. The gas was assumed to be air at 5
morr. Figure 5 plots $\varepsilon_n(\zeta)$ just before the exit foil, showing essentially no emittance growth from the injected value. When the same beam is propagated in 20 mtorr, the beam tapers more quickly, and $\varepsilon_n$ rises during the pulse, reaching a maximum value of 1.1 rad-cm. The results are in approximate agreement with a simple analytical model which assumes free expansion at the beam head and an equilibrium pinch in the beam body.

IV. ENERGY VARIATION (DIFFERENTIAL FOCUSING) TAILORING CELL

Description of Method: This scheme involved deliberately introducing a 10-20% energy variation in the beam and passing it through a magnetic lens tuned to focus the highest energy portion in the beam body onto a scattering foil. Lower energy portions are overfocused and expand before striking the foil. FRIEZR uses the thin lens approximation to model this approach.

Simulation results for differential focusing cell: Figure 6 plots the beam radius at the nominal focal point (30 cm) of a beam injected through a lens at an initial radius of 5 cm. The desired beam taper is attained, although the difference between $a_{1/2}$ and $a_{rms}$ indicates an undesirable core-halo current density profile. The system must be tuned very accurately; a shift in the scattering foil position of only 3 cm in either direction alters the taper dramatically.

V. SUMMARY AND REFERENCES

All three conditioning techniques are capable of producing the desired radius taper although the multi-foil method may not be acceptable because of foil scattering. The IFR cell can in principle produce an excellent beam taper for stabilizing hose, but the differential focusing method is more compatible with the ATA fast corrector coil and can produce similar beam tailoring profiles if carefully tuned.


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