# Identification of Tetragonal and Cubic Structures of Zirconia

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**Abstract**

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IDENTIFICATION OF TETRAGONAL AND CUBIC STRUCTURES OF ZIRCONIA

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X-ray diffraction from a synchrotron source was employed in an attempt to identify definitively the crystal structures in zirconia ceramics produced by sol-gel method. The particles of chemically precipitated zirconia, after calcination below 600°C, are very fine, and have a diffracting particle size in the range of 7-15 nm. Since the tetragonal and cubic structures of zirconia have very similar lattice parameters, it is difficult to distinguish between the two. The tetragonal structure can be identified only by the characteristic splittings of the Bragg profiles from the "c" index planes. However, these split Bragg peaks from the tetragonal phase in zirconia overlap with one another due to particle size broadening. In order to distinguish between the tetragonal and cubic structures of zirconia, three samples were studied using synchrotron radiation. The results indicated that a sample containing 13 mol.% yttria-stabilized zirconia possessed the cubic structure with $a_0 = 0.51420 \pm 0.00012$ nm. A sample containing 6.5 mol.% yttria stabilized zirconia was found to consist of a mixture of cubic and tetragonal phases with the cubic phase being the major constituent, with $a_0 = 0.51430 \pm 0.00008$ nm. Finally, a sample which was precipitated from a pH 13.5 solution was observed to have the tetragonal structure with $a_0 = 0.51441 \pm 0.00085$ nm and $c_0 = 0.51902 \pm 0.00086$. Raman studies on these samples corroborate the X-ray diffraction results. The X-ray diffraction data obtained from a synchrotron source are superior to the data obtained...
by conventional X-ray diffraction sources in identifying the crystal structures of very fine crystalline materials.

INTRODUCTION

Zirconia is a polymorphic ceramic which may exist in three well-known structural forms: monoclinic, tetragonal, and cubic\(^4\). Recently, a high-pressure allotropic form of zirconia (orthorhombic) has been reported; this phase is metastable at atmospheric pressure and reverts to the monoclinic form by such a mild treatment as grinding in a mortar\(^7\). Although a tremendous amount of research has been carried out to elucidate the crystal structures of industrially important zirconia ceramics, problems remain in assigning the structures accurately. Garvie et al.\(^8\) reported a cubic dispersion in the tetragonal structure; this appears to have been the only observation of this material. Mazdiyasni et al.\(^9\) reported that a cubic phase could be obtained by the addition of 6.5 mol.% yttria, following an alkoxide preparation route.

It has been observed that although the monoclinic phase is stable below 1100°C, the tetragonal phase may, under certain conditions, be stabilized at lower temperatures\(^10\). Several explanations for the low-temperature stabilization of the tetragonal phase have been postulated\(^11-16\). Garvie\(^10-12\) proposed that the low-temperature tetragonal phase stability is due to the lower surface energy of the tetragonal phase relative to that of the monoclinic phase. It has been suggested that small amounts (about 0.75 wt.%) of bound OH groups in solid solution stabilize the
tetragonal structure at room temperature. Others have reported that the presence of water vapor catalyzes the \( t \rightarrow m \) transformation in zirconia, and in this way determines which phase is observed. It has also been postulated that structural similarities between the precursor gels and the tetragonal structure are responsible for the low-temperature stabilization of the tetragonal phase in zirconia.

Clearfield recently offered an explanation to account for the formation of tetragonal or monoclinic; here he proposes precipitation following two pathways, one leading to tetragonal and one to monoclinic zirconia following calcination. As is apparent from the many conflicting studies, the actual mechanism for the low-temperature stabilization of tetragonal phase of zirconia remains obscure.

Mitsuhashi et al. prepared amorphous zirconia from \( \text{ZrOCl}_2 \cdot 8\text{H}_2\text{O} \) with ammonia and obtained pure tetragonal zirconia upon heating the product. It was reported that fine single-domain tetragonal particles, which are strain-free, are more easily transformed than the poly-domain particles. However, Mitsuhashi et al. did not specify the pH of the precipitation.

Katz reported that a metastable cubic phase results from the precipitation of \( \text{ZrOCl}_2 \) with NaOH, again without specifying the pH of the precipitation.

Davis found that the pH at which the precursor gels are precipitated causes the tetragonal or the monoclinic phase to be formed after calcining the material at 400 - 600°C. It was reported that the tetragonal phase could be obtained either at a low pH (3-5) range or at a high pH range (13-14), and that the monoclinic phase
could be obtained in the medium pH (8-11) range. Srinivasan et al.\textsuperscript{22} demonstrated that the tetragonal phase obtained at pH 13.5 was stable even after calcination at 500°C for 300 hours and later found that both the monoclinic and tetragonal phases could be obtained at a pH of 10.5, depending upon the time taken to effect the precipitation.\textsuperscript{23} Most recently, Jada and Peletis\textsuperscript{24} suggested that the solution chemistry of zirconia precursor materials plays a key role in controlling the formation of the crystal structure, polymorphic transformation, and crystalline growth. Mamott et al.\textsuperscript{25} using a time-resolved dynamic high-temperature XRPD (X-ray Powder Diffraction) technique, have reported on the onset of an ordering within the amorphous starting material, and on the progress of its conversion into crystalline zirconia.

The assignment of cubic and tetragonal structures, based solely on the X-ray diffraction analysis, can be misleading because the cubic and tetragonal structures ($a_0 = 0.5124$ nm for cubic, and $a_0 = 0.5094$ nm and $c_0 = 0.5177$ nm for tetragonal structures) are very similar.\textsuperscript{26} Srivastava et al.\textsuperscript{27} reported that the tetragonal structure can be distinguished from the cubic structure by the presence of the characteristic splittings of the tetragonal phase, such as (002) (200), (113) (311), (004) (400) and (006) (600) etc., whereas the cubic phase exhibits only single peaks at all of these positions. Garvie et al.\textsuperscript{28} utilized high-angle reflections to distinguish the cubic and tetragonal structures and to determine their relative proportions. In an investigation of plasma-sprayed yttria-stabilized zirconia coatings, Miller et al.\textsuperscript{29} used the (400)
region of the X-ray diffraction patterns in order to calculate the relative proportions of cubic and tetragonal phases. They reported that the dominant peaks in this region change from the monoclinic to tetragonal and gradually to the cubic reflections with an increase in the level of yttria. A "curve resolver" was used to separate the tetragonal and cubic peak components in the (400) region and the 'd' values for the (400) and (004) tetragonal peaks were calculated from the curve-resolved peak positions.

It should also be noted that in order to clearly observe the tetragonal splittings in the entire 2θ region in yttria-containing zirconia ceramics, the material must be sintered above 1100°C. Below 1100°C, the 2θ angle at which tetragonal reflections occur becomes a function of a number of parameters, such as the change in composition, different thermal treatments, variation of the lattice parameters with change in composition, etc. Hannink has commented that the (400) profile could not be resolved from the (400), and (004), reflections in diffractometer traces such that relative amounts of each phase could be determined. Paterson et al. reported the presence of the t' phase, that is strongly related to the cubic phase, and this t' phase was observed in the 2θ region 72-76°.

As these aforementioned works suggest, the 2θ region used in the assignment and calculation of tetragonal and cubic phases in ZrO₂ is complex; care must be exercised when evaluating these crystalline phases using XRD data alone. For samples prepared by precipitation, the doublets of the tetragonal phase at
intermediate 2θ positions are difficult to distinguish clearly because of the peak
broadening due to the small crystallite size. Davis\textsuperscript{21} and Srinivasan et al.\textsuperscript{22,23} have
suggested that the crystal structure obtained at low pH values and high pH ranges
is the tetragonal structure, although the tetragonal doublets are not readily apparent
in XRD. To confirm their crystal assignment, Davis\textsuperscript{21} and Srinivasan et al.\textsuperscript{22,23} utilized
Raman spectroscopy. In contrast to XRD, the monoclinic, tetragonal, and cubic
zirconia structures can be readily distinguished from one another by Raman
spectroscopy. Various experimental\textsuperscript{32,33} and group theoretical calculations\textsuperscript{34} reveal
that the Raman spectrum for the monoclinic phase should contain 18 bands, the
tetragonal phase spectrum 5 bands, and the cubic phase should possess only one
band. Recently, we assigned a tetragonal structure to a zirconia material precipitated
from a solution of pH 13.5. This assignment was based upon both XRD and Raman
spectral evidence that was in agreement with previously published spectroscopic
data for the crystalline phases. However, Benedetti et al.\textsuperscript{35} have recently reassigned
a cubic structure to a zirconia sample prepared in a similar manner. In this paper,
we report further XRD results obtained using a synchrotron source and Raman data
which support our previous assignment in yet another attempt to further the
understanding of the crystal structures in precipitated zirconia ceramic materials.

\textbf{EXPERIMENTAL}

The complete listing of the specifications for all of the zirconia samples used in
this study are presented in Table 1. The 13 mole\% yttria-stabilized zirconia labeled
as sample A was prepared from yttrium and zirconium nitrates using a coprecipitation technique and dried at 120°C. Sample B was prepared in a manner similar to Mazdiyasni et al.\textsuperscript{9} and contained 6.5 mole% yttria. Both samples A and B were calcined at 1150°C for 10 hours. Zirconia sample C was precipitated from a solution of 0.3 M ZrCl\textsubscript{4} that was adjusted to pH 13.5 with KOH. The resulting product was washed to a negative test for chloride ion (ca. 10 washings) and then calcined at 500°C for 200 hours\textsuperscript{22,23}.

Samples D and E were prepared in a manner similar to that reported by Benedetti et al.\textsuperscript{35}. Sample D, which corresponds to Sample III in reference 35, was washed twice while Sample E (Sample II in reference 35) was washed exhaustively. Subsequent atomic absorption analysis demonstrated that sample D contained ca. 3 wt.% Na and that sample E contained less than 0.5 wt.% Na.

The Raman system used to acquire the spectroscopic data consisted of a Coherent INNOVA 90 krypton ion laser source, a triple monochromator (Model 1877, Spex Industries), and a charge-coupled-device detector (Model CSF THF7882CDA, Thomson). Spectra were collected using a 10 minute counting time and ca. 5 mW illumination power at the sample. Following data collection, data were transferred to a microcomputer for subsequent analysis and plotting.

Much of the XRD data reported here were obtained using a synchrotron source. The experiments for our samples were conducted on the beam line X14 (Oak Ridge National Laboratory) at the National Synchrotron Light Source at
Brookhaven National Laboratory, Upton, New York. The experiments were performed at room temperature without a single crystal monochromator in the diffraction beam path. Diffraction data were collected by step scanning for times of one or two seconds per step and a step width of 0.02 or 0.01 degrees in 2θ. One of the primary objectives of this investigation was to obtain diffraction data using a synchrotron source that would allow us to clearly distinguish between the tetragonal and cubic structures in zirconia.

RESULTS AND DISCUSSION

Synchrotron radiation is a powerful tool for diffraction studies. In structural areas, it provides the ability to measure scattering curves to very large values of K (= Sinθ/λ)\(^3\). The high intensity and collimation of synchrotron radiation allows high resolution studies, both in the small and high angle regions, and also very close to Bragg reflections. This is useful in a number of applications, including structure analysis\(^3\).

A typical X-ray pattern collected on the synchrotron beam line from a sample of pure monoclinic (> 95%) zirconia is presented in Figure 1A. This material was prepared from a batch of zirconyl nitrate hydrate; another batch of zirconyl nitrate hydrate from this same supplier produced a material containing a high percentage of tetragonal zirconia. We have been able to obtain this high percentage of monoclinic form by precipitation at pH 10 only when the initial zirconium species is well dispersed, presumably as a monoatomic zirconium species. In most cases, zirconyl
salts appear to be polymeric dispersions and this invariably leads to a high percentage of tetragonal zirconia.

The importance of the starting zirconium salt has been ignored repeatedly by workers in the preparation of crystalline zirconia ceramics by precipitation, and we feel that this is a likely source for the diversity of results that have been reported. The XRD pattern for the tetragonal form of zirconia is shown in Figure 1B. It is obvious that the XRD pattern clearly distinguishes the tetragonal and cubic structures from the monoclinic form. However, the XRD patterns for (111) reflections of the cubic 13 wt.% yttria-stabilized zirconia (Figure 1C) and tetragonal zirconia (Figure 1B) are essentially coincident, and therefore the two cannot be distinguished readily from the XRD patterns. Thus, other means of distinguishing between tetragonal and cubic forms becomes necessary.

The 2θ region containing the (002) and (200) profiles of tetragonal zirconia for Samples A, B, and C is shown in Figure 2. The (200) cubic profile of Sample A is evident with a calculated crystallite size of about 103 nm using the Scherrer equation. This profile is very broad for Sample B and indicates a crystallite size of 10.2 nm. Although the doublets cannot be seen clearly in Sample C, the asymmetry of the peak indicates an overlap of tetragonal doublets. Because of particle size broadening, the (002) and (200) profiles are unresolved and appear as one broad peak (Figure 2C). The calculated size is ca. 10 nm for Sample C; this assumes only one peak is present.
Another $2\theta$ region of interest is 48-53°, where the (220) and (202) tetragonal peaks should appear as a doublet, and the cubic (220) peak should appear as a single peak. This region is shown in Figure 3, wherein the (220) cubic peak is observed for Sample A, and a broad peak for Sample B. For the pH 13.5 material, the tetragonal doublets are not well resolved. (This is further evidence for tetragonal doublets that overlap due to particle size broadening.) The crystallite size for Sample C, measured from the full width at half maximum intensity is 10.3 nm, and the crystallite size for Sample B is 9.5 nm. The measured crystallite size for Sample A is 105 nm, which is nearly ten times larger than the Samples B and C. The $2\theta$ region covering the (113) and (311) tetragonal doublets for the three samples is shown in Figure 4. For the pH 13.5 material (Sample C), the tetragonal doublets begin to appear as indicated by the peak asymmetry, whereas the 13 mol.% yttria stabilized zirconia (Sample A) shows only the (311) cubic peak. As can be seen, the particle size broadening certainly increases the difficulty in the assignment of the tetragonal doublets.

The $2\theta$ region containing (004) and (400) tetragonal doublets is presented in Figure 5 for all the three samples, and this region was plotted exclusively for Sample C in Figure 6. This $2\theta$ region has been extensively used by researchers in order to distinguish the cubic from the tetragonal structure in zirconia. For Sample A the (400) cubic peak is very sharp with a calculated crystallite size of about 96 nm. For Sample B (6 mol.% yttria stabilized zirconia) the profile is very broad and
appears to be a mixture of tetragonal and cubic phases with a crystallite size estimation of 8.5 nm. However, for Sample C (Figures 5c and 6), the (004) and (400) tetragonal doublets can be observed clearly.

The 2θ region from 79-86° (Figure 7) shows the (331) and (420) cubic peaks for Sample A. The tetragonal doublets (331) and (313) and (420) and (402) are not well resolved for Sample C. The high angle region from 120-134° is plotted in Figure 8. Here the (600) cubic peak is observed for Sample A; for Sample C (006) and (600) tetragonal doublets are observed.

Both the conventional X-ray source and synchrotron source were used to obtain patterns from samples B and C and these contained broad diffraction lines. This indicates the very small crystallite size of the chemically precipitated materials. Despite the broad diffraction lines, a complete XRD pattern was obtained for all the three samples so as to offer a reasonable definition of the crystal structures developed in these materials. Based on the above XRD results, the crystallite size data were calculated using Scherrer analysis, and these data are presented in Table 2.

The results obtained from Raman spectroscopy are shown in Figures 9 and 10. The spectrum from Sample A (Figure 9A) shows the characteristic Raman band for a cubic zirconia at 625 cm⁻¹. The spectrum from Sample D (Figure 9D) exhibits the characteristic Raman bands of tetragonal zirconia. We have obtained similar spectra for a number of samples that we have prepared at pH values in the 13-14
range\textsuperscript{23}. We experienced consistent difficulties in obtaining a complete Raman spectrum for Sample B.

Raman spectra (Figure 10) were obtained from the two samples that were prepared in like manner to Samples II and III of Reference 35. Sample D was washed only two times and was found to contain about 3 wt.% Na while Sample E was washed thoroughly and contained less than 0.5 wt.% Na. Samples D and E exhibit Raman spectra whose peak positions agree with those expected for the tetragonal form\textsuperscript{32}. However, the XRD for sample D does not show the anticipated two distinct peaks at about $2\theta = 35^\circ$. Due to peak broadening, we are unable to confirm the tetragonal form by the presence of the (002) diffraction line splitting at $2\theta = 35^\circ$. Also shown in Figure 10 is the Raman spectrum for the more completely washed material that was precipitated at pH 13.5 (Figure 10E, corresponding to Sample II, reference 35). This sample likewise displays a spectrum with band positions which indicate the tetragonal form. The band positions for both the minimally washed and thoroughly washed materials (spectra presented in Figure 10) are consistent with the tetragonal form although the spectra are of a poorer quality.

The literature for zirconia has inconsistencies, both with regard to structure and to lattice parameters. It is known that the stabilization of zirconia with 13 mol.% or 6 mol.% yttria will alter the lattice parameters, and we have considered these two samples only for comparative studies with a tetragonal zirconia precipitated at a pH of 13.5 (Sample C). The lattice parameters calculated from the diffraction data using
a least-square fit, indicate that Sample A has a cubic structure with \( a_0 = 0.51420 \pm 0.00012 \) nm. This conclusion is further substantiated by the Raman spectrum of sample A. Likewise, Sample C is undoubtedly tetragonal zirconia.

We feel that the statement of Benedetti et al. that the pH 13.5 material, if washed minimally, is cubic \( (a_0 = 0.5116 \text{ nm}) \), is questionable. The X-ray diffraction patterns from sample D (washed only 2 times) are presented in Figure 11. Although the (004), and (400), phases are not resolved well in the \( 2\theta \) region of 70-78\(^\circ\), the (006), and (600), phases are well resolved in the \( 2\theta \) range of 120-132\(^\circ\). Calling this peak 'cubic', based on the inability to observe the (004), and (400),, will be misleading without checking carefully at the higher angle peaks [i.e. (006), and (600),]. One must therefore exercise extreme caution in assigning a structure to the pH 13.5 material. One cannot assign either the tetragonal or the cubic structure relying solely on the \( 2\theta \) range of 70-76\(^\circ\), a region which contains only the (004) and (400) tetragonal doublets and the (400) cubic singlet. As a result of the ambiguity surrounding the true crystal structure of the pH 13.5 material, we have undertaken XRD studies using a synchrotron source. With conventional X-ray diffraction, because of the very small crystallite size, the tetragonal doublets often cannot be clearly resolved. On the other hand, XRD studies utilizing a synchrotron source have the capability of distinguishing further the tetragonal doublets even for a material consisting of very fine crystallites. Hence, one should examine higher order peaks, such as (006) and (600) tetragonal doublets in the \( 2\theta \) range of 120-132\(^\circ\), to ascertain
accurately the crystal identity. In order to corroborate this conclusion further, we recommend that Raman studies also be undertaken. The Raman spectrum for tetragonal zirconia in Figures 9 and 10 lends support to our conclusion that the pH 13.5 material is tetragonal. For zirconia precipitated employing NaOH to produce pH 13.5, the tetragonal form has been obtained whether the washing was limited or extensive. We have not obtained evidence to support the view that ca. 3% Na can stabilize the cubic form of zirconia as was reported in Reference 35.

CONCLUSIONS

X-ray diffraction using a high-intensity synchrotron source has been adopted to provide a better definition of certain controversial points in the assignment of the crystal structure in zirconia. It is clear that if zirconia is precipitated at a pH of 13.5, it develops the tetragonal phase and not the cubic form. Both Raman and XRD studies lend support to our conclusions about the developed structure in the precipitated zirconia. We have found that particle size broadening of XRD profiles can lead potentially to incorrect structural assignments. It is therefore concluded that a more complete analysis including Raman spectroscopy in addition to XRD should be undertaken before positively assigning the crystal structures to materials of very small crystallite size, a situation in which particle size broadening of XRD data can be overwhelming.
ACKNOWLEDGMENTS

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REFERENCES


FIGURE LEGEND

Figure 1. Typical X-ray diffraction patterns using a synchrotron source. (A) 100% monoclinic zirconia precipitated at pH 10.5 and calcined at 500°C - 5h, (B) 100% tetragonal zirconia (Sample C) and (C) 100% cubic zirconia (Sample A).

Figure 2. X-ray diffraction patterns in the 2θ region of 33-37°, in which the (200) cubic and (200) (002) tetragonal doublets occur. (A) Sample A, (B) Sample B, and (C) Sample C.

Figure 3. X-ray diffraction patterns for Samples A, B, and C in the 2θ region of 48-53°. In this region the (220) cubic peak is evident for Sample A (Curve A). The (202) and (220) tetragonal doublets can be seen overlapping, because of particle size broadening (Curve C).

Figure 4. X-ray diffraction patterns for Samples A, B, and C in the 2θ region of 58-61°. Curve (A) shows the (311) cubic profile for Sample A. Curve B shows a broad (311) cubic phase, and Curve C corresponds to Sample C. (The pattern for Sample C is broadened by the tetragonal doublets (113) and (311) peaks.)

Figure 5. X-ray diffraction pattern for Samples A, B, and C in the 2θ region of 71-76°, where the (400) cubic peak and (004) (400) tetragonal doublets should appear. Curves (A), (B), and (C) refer to Samples A, B, and C, respectively.
Figure 6. X-ray diffraction pattern for Sample C, where (004) and (400) tetragonal doublets can be seen clearly resolved.

Figure 7. X-ray diffraction patterns for Samples A, B, and C, in the 2θ region of 79-86°. The (331) and (420) cubic peaks are evident for Sample A (Curve A). These two peaks are broadened in Sample B (Curve B). The tetragonal doublets (331) (313) and (420) (402) are not well-resolved for Sample C (Curve C).

Figure 8. X-ray diffraction patterns for Samples A and C in the 2θ region of 120-134°. Sample A shows (531) and (600) cubic peaks. Sample C shows the overlapping (513) and (531) tetragonal doublets. The (006) and (600) tetragonal doublet can be observed clearly without overlap.

Figure 9. Raman spectra obtained for Samples A and D. Sample A has the cubic structure as indicated by the characteristic Raman band at 625 cm⁻¹. Sample D (the feebly washed pH 13.5 material) stands in absolute contrast with the cubic structure.

Figure 10. Raman spectra for Samples D and E. The characteristic Raman bands at 262, 330, 473, 613 and 643 cm⁻¹, suggest that the material is tetragonal. The relative band positions for D and E indicate that both samples possess the tetragonal structures.
Figure 11. X-ray diffraction patterns for Sample D. Although the (004), and (400), are not well resolved, the (006), and (600), profiles can be seen clearly resolved.
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<th>Sample ID</th>
<th>Specifications</th>
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<td>Sample B</td>
<td>7.5 mol.% yttria-stabilized ZrO₂ obtained from Ref. 9 - calcined at 1150°C - 10 h.</td>
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<tr>
<td>Sample C</td>
<td>ZrO₂ precipitated at pH 13.5 - calcined at 500°C for 200 hours.</td>
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<tr>
<td>Sample D</td>
<td>ZrO₂ precipitated using 4M NaOH at pH 14.0 - gels were washed two times only - containing about 3 wt.% Na.</td>
</tr>
<tr>
<td>Sample E</td>
<td>ZrO₂ precipitated using 4M NaOH at pH 14.0 - gels thoroughly washed - containing &lt; 0.5 wt.% Na.</td>
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Table 2

Crystallite Size Data for Samples A, B and C

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* Not available.
Fig 1
Fig 6