ANALYSIS OF DUCTILE-BRITTLE TRANSITION TEMPERATURES FOR CONTROLLED-ROLLED.
(U) DAVID TAYLOR RESEARCH CENTER BETHESDA MD SHIP MATERIALS ENGINEERING.

UNCLASSIFIED R W ARMSTRONG ET AL. MAY 88 DTRC/SME-88-38 F/G 11/6 1 NL
ANALYSIS OF DUCTILE-BRITTLE TRANSITION TEMPERATURES
FOR CONTROLLED-ROLLED, MICROALLOYED, C-Mn BASED STEELS

by
R. W. Armstrong
L. R. Link
G. R. Speich

Approved for public release; distribution is unlimited.
ANALYSIS OF DUCTILE-BRITTLE TRANSITION TEMPERATURES FOR CONTROLLED-ROLLED, MICROALLOYED, C-Mn BASED STEELS

R.W. Armstrong, L.R. Link, G.R. Speich

Charpy V-notch ductile-brittle transition temperatures reported for a conventional C-Mn steel and for several controlled-rolled microalloyed steels are compared with transition temperatures computed on a dislocation model basis. The computed transition temperature, $T_c$, is specified by equating the tensile cleavage fracture stress and the effective yield stress at the Charpy V-notch. Increased friction stress resistances to dislocation movement provided by solutes, precipitates, and other dislocations raise the yield stress and, thereby, increase $T_c$. A residual dislocation based friction stress resistance occurs within untransformed ferrite grains (that is, the ferrite present at the rolling temperature) when finish rolling is done in the austenite-ferrite region. Grain size refinement normally lowers $T_c$ because the cleavage stress is increased to a greater extent than the yield stress. When cleavage is controlled by the growth of a crack from grain boundary carbide, as might occur in a low-carbon microalloyed steel, $T_c$ is raised to an increased extent as the ratio of ferrite grain diameter and carbide plate thickness is smaller.
# CONTENTS

<table>
<thead>
<tr>
<th>ABBREVIATIONS</th>
<th>v</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABSTRACT</td>
<td>1</td>
</tr>
<tr>
<td>ADMINISTRATIVE INFORMATION</td>
<td>1</td>
</tr>
<tr>
<td>CONTROLLED-ROLLED STEEL PROPERTIES</td>
<td>2</td>
</tr>
<tr>
<td>DISLOCATION MODEL ANALYSIS FOR T&lt;sub&gt;C&lt;/sub&gt;</td>
<td>4</td>
</tr>
<tr>
<td>THE INFLUENCE OF GRAIN BOUNDARY CARBIDE</td>
<td>7</td>
</tr>
<tr>
<td>SUMMARY</td>
<td>11</td>
</tr>
<tr>
<td>REFERENCES</td>
<td>13</td>
</tr>
</tbody>
</table>

## FIGURES

1. Yield stress, $\sigma_y$, versus reciprocal square root of grain diameter, $l^{-1}$, for different controlled-rolled steels ................. 15
2. Fracture appearance transition temperature (FATT) versus $l^{-1}$ for different controlled-rolled steels ........................................... 16
3. FATT versus $\sigma_y$ for different controlled-rolled steels, with computed transition temperatures, $T_c$, for C-Mn steel ............... 17
4. Microscopic cleavage fracture stress dependence on reciprocal square root of carbide plate thickness or width, $t^{-1}$, for a variety of steel microstructures, in comparison with the computed $\sigma_c'$ dependence on $t^{-1}$ for different grain diameters .......... 18
5. Computed $T_c$ dependence on $l^{-1}$ for different carbide thicknesses, $t$, and friction stresses, $\sigma_G$ .......................... 19
TABLES

1. Temperature, $T$ and strain rate, $\dot{\varepsilon}$, parameters ($B_0$, $\beta_0$, $\beta_1$) for the thermal component of friction stress:

$$\sigma_{TH} = B_0 \exp(-[\beta_0 \beta_1 \ln\dot{\varepsilon}]T),$$
for mild steel, C-Mn steel and Armco iron .......... 5

2. Comparison of measured and computed grain size and friction stress influences on ductile-brittle transition temperatures ................. 7

3. Comparison of measured and computed grain diameter and carbide thickness influences on ductile-brittle transition temperatures .......... 10
ABBREVIATIONS

\( \alpha \) Triaxial stress state at a notch
\( \dot{\varepsilon} \) Strain rate
FATT Fracture appearance transition temperature
\( G \) Shear modulus
\( k_y \) Microstructural stress intensity
\( L \) Grain diameter
\( \sigma_c \) Cleavage fracture stress
\( \sigma_G \) Athermal stress component of the friction stress
\( \sigma_o \) Friction stress
\( \sigma_{TH} \) Thermal stress component of the friction stress
\( \sigma_y \) Yield stress
TASRA Thermal activation-strain rate analysis
\( T_C \) Transition temperature
\( t \) Carbide plate thickness
\( \gamma_p \) Surface energy
\( \nu \) Poisson's ratio
ABSTRACT

Charpy V-notch ductile-brittle transition temperatures reported for a conventional C-Mn steel and for several controlled-rolled microalloyed steels are compared with transition temperatures computed on a dislocation model basis. The computed transition temperature, $T_c$, is specified by equating the tensile cleavage fracture stress and the effective yield stress at the Charpy V-notch. Increased friction stress resistances to dislocation movement provided by solutes, precipitates, and other dislocations raise the yield stress and, thereby, increase $T_c$. A residual dislocation based friction stress resistance occurs within untransformed ferrite grains (that is, the ferrite present at the rolling temperature) when finish rolling is done in the austenite-ferrite region. Grain size refinement normally lowers $T_c$ because the cleavage stress is increased to a greater extent than is the yield stress. When cleavage is controlled by the growth of a crack from grain boundary carbide, as might occur in a low-carbon microalloyed steel, $T_c$ is raised to an increased extent as the ratio of ferrite grain diameter and carbide plate thickness is smaller.

ADMINISTRATIVE INFORMATION

This report was prepared as part of the Materials and Fabrication Block Program under the sponsorship of Mr. Ivan Caplan, David Taylor Research Center (DTRC Code 011.5). The effort was supervised by Mr. T. W. Montemarano, DTRC Code 2814, under Program Element Number 62234N, Task Area RS 34S50, Work Unit 1-2814-208. This report satisfies FY87 Milestone 2803-117.
CONTROLLED-ROLLED STEEL PROPERTIES

Speich and Dabkowski (1) have reported ferrite grain diameter, \( l \), yield strength, \( \sigma_y \), and fracture appearance transition temperature, FATT, measurements obtained for controlled-rolled C, C-Mn, C-Mn-Nb, and C-Mn-Mo-Nb steels. The steels were finish-rolled in the austenite or austenite-ferrite regions of the phase diagram. Substantially different finishing temperatures were involved. Inclusive of all the steels, a wide range in resultant \( l \) values was obtained.

Figure 1 shows the influence of finishing temperature on the yield stress-grain size dependence for each steel. The experimental results are plotted on a Hall-Petch basis (2,3) as

\[
\sigma_y = \sigma_o + k_y l^{1/2}
\]  

(1)

where different friction stress, \( \sigma_o \), resistances are shown for the different steels as compared with their having the same slope, \( k_y \), value, recently described as a microstructural stress intensity (4). The lower dashed reference line in Figure 1, following Equation (1), was shown previously by Morrison (5) to apply for low carbon steels over a wide range of grain diameters.

The trend established for the steels in Figure 1 is that the yield stress first increases at lowered austenitic finishing temperatures because of ferrite grain size refinement, whereas, at the lowest finishing temperatures in the austenite-ferrite region, \( \sigma_y \) increases because deformation of untransformed ferrite occurs during finishing. This deformation gives an increase in friction stress without much further reduction in grain size. Solid solution and precipitation strengthening are shown to have raised \( \sigma_o \) for the alloy steels even when finished at the highest temperatures.

An interesting comparison occurs in Figure 1 at the arrow markers for the C-Mn-Nb and C-Mn-Mo-Nb steels. Relatively greater ferrite grain size reduction was
proposed to occur for the latter steel at all finishing temperatures because of the measured effect of Mo on lowering the ferrite transformation temperature (1). The precipitation of NbC in the ferrite was consequently retarded, hence, a lower initial value of \( \sigma_0 \) was measured relative to that for the C-Mn-Nb steel. Dilatometric measurements indicated that as much as 45% ferrite was present during controlled rolling of the C-Mn-Mo-Nb steel at 760°C. Yet, finishing at this temperature left \( \sigma_0 \) unchanged. Very probably, Mo, through its solid solution strengthening of ferrite, particularly at 760°C in the austenite-ferrite region, caused the major portion of finishing deformation to be borne by the austenite. In this way the Mo addition to the alloy would have contributed very significantly to greater grain size reduction in the newly transformed ferrite, with a much lesser effect on \( \sigma_0 \) overall because of the less heavily strained untransformed ferrite.

The influence of finishing temperature on the measured FATT-\( L^{-1/4} \) relationship is shown in Figure 2. The dependence is especially interesting because of the reversal in behavior which occurs for the FATT. Beginning from relatively large grain diameters for each steel, that is, small \( L^{-1/4} \) values, linear decreases in the FATT are shown with decrease in finishing temperature and increase in \( L^{-1/4} \). The linear dependences of the different FATT values on \( L^{-1/4} \) are in reasonable agreement with the dashed line (slope) dependence shown from previous transition temperature measurements reported for annealed steel materials by Heslop and Petch (6). The reversed behavior of an increase in FATT with increase in \( L^{-1/4} \), observed beyond a minimum FATT value in each case, is seen by referring to Figure 1, to have occurred when the increase in \( \sigma_y \) was produced by an increase in \( \sigma_0 \). This is clearly established for the C-Mn steel results. The C-Mn-Mo-Nb steel results in Figure 2 show the beneficial effect on the FATT from a lower \( \sigma_0 \) and continued reduction in grain size.
DISLOCATION MODEL ANALYSIS FOR $T_C$

Grain size and friction stress influences on the notch-sensitive ductile-brittle transition properties of materials can be obtained from the Hall-Petch dislocation pile-up based equations for $\sigma_y$ and the cleavage fracture stress, $\sigma_c$. At transition the relationship between the stresses is as follows (7-9).

$$\sigma_c = a\sigma_y(T, \epsilon)$$

(2)

where $a$ is a measure of the triaxiality of the stress state at the notch; and, emphasis is given in the equation to the temperature, $T$, and strain rate, $\epsilon$, dependences of $\sigma_y$. The Hall-Petch constants for $\sigma_c$ have now been measured at relatively low $T$ or high $\epsilon$ such that cleavage occurred before the condition of general plastic yielding was reached. The experimental constants, $\sigma_{oc}$ and $k_C$, are essentially athermal and related to their $\sigma_y$ counterparts by the inequalities:

$$\sigma_{oc} < \sigma_y \text{ and } k_C > k_y.$$  

The latter inequality is supported by the dislocation theory prediction that a greater microstructural stress intensity is required to initiate cleavage than is required for general plastic yielding.

The thermal activation-strain rate analysis (TASRA) for plastic straining by dislocation movement within single crystals or polycrystal grains accounts for $\sigma_o$ in terms of an athermal stress component, $\sigma_G$, and a thermal stress component, $\sigma_{Th}$, dependent also on $\epsilon$. The stress components are combined in the equation

$$\sigma_o = \sigma_G + B_0 \exp \left[ \beta_0 - \beta_1 \ln \epsilon \right] T$$

(3)

where $B_0$, $\beta_0$ and $\beta_1$ are experimental constants evaluated in terms of dislocation model calculations (10). Experimentally, $B_0$ is the value of $\sigma_{Th}$ at $T=0$. The constants $\beta_0$ and $\beta_1$ are determined from the strain rate dependence of the different bracketed slope values obtained from $\ln \sigma_{Th}$ plotted against $T$ at various constant $\epsilon$ values. Table 1 gives comparable values of the TASRA constants determined in this
Table 1. Temperature, T, and strain rate, $\epsilon$, parameters $(B_o, \beta_o, \beta_1)$ for the thermal component of friction stress (10): $\sigma_{Th}=B_o\exp[-(\beta_o-\beta_1\ln\epsilon)T]$, for mild steel (11), C-Mn steel (12), and Armco iron (13).

<table>
<thead>
<tr>
<th>$l$ (µm)</th>
<th>$\sigma_C$ (MPa)</th>
<th>$T_{NDT}$ (°K, meas.)</th>
<th>$T_C(\sigma_C)$ (°K)</th>
<th>$t$ (µm)</th>
<th>$\sigma_C'$ (MPa)</th>
<th>$T_C(\sigma_C')$ (°K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>1400</td>
<td>$\approx 180$</td>
<td>160</td>
<td>0.8</td>
<td>1296</td>
<td>185</td>
</tr>
<tr>
<td>20</td>
<td>1087</td>
<td>$\approx 220$</td>
<td>220</td>
<td>1.2</td>
<td>1028</td>
<td>240</td>
</tr>
<tr>
<td>65</td>
<td>750</td>
<td>$\approx 280$</td>
<td>317</td>
<td>2.0</td>
<td>724</td>
<td>331</td>
</tr>
</tbody>
</table>

way from measurements on related steel materials (11-13). Most measurements have indicated that $k_y$ is athermal so that the total temperature and strain rate dependence of $\sigma_y$ is in $\sigma_o$.

By substitution into Equation (2) of the Hall-Petch parameters for $\sigma_C$ and of the terms for $\sigma_o$ from Equation (3), with $k_y$ included also, then, the ductile-brittle transition temperature, $T-T_C$, is obtained as

$$T_C = \left[ \frac{1}{\beta_o - \beta_1\ln\epsilon} \right] \left[ \ln (aB_o) - \ln [(k_C - a\epsilon)_1^{b_1} + (\sigma_{oc} - a\sigma_C)] \right]$$  \hspace{1cm} (4)

Equation (4) gives a quantitative guide for the explicit lowering of $T_C$ by the several variables of grain size refinement, reduction in athermal friction stress, and for testing at a reduced strain rate (8,9). Sandstrom and Bergstrom (12) have employed the same type of analysis as given above, but they have neglected $\beta_o$ in
Equation (3), to describe their measurements of the nil ductility Charpy V-notch transition temperature dependence on grain size for a C-1.32Mn mild steel. Their measurements have been employed in Equation (3) to obtain the $B_0$, $\beta_0$, and $\beta_1$ values given in Table 1.

Equation (4) has been applied in the present study, with further assistance from other measurements reported by Sandstrom and Bergstrom, to computing $T_c$ for the 0.06C-1.26Mn steel results reported by Speich and Dabkowski (1). Sandstrom and Bergstrom computed tensile cleavage fracture stresses from notched bend test results obtained for various grain sizes and determined $\sigma_{oc}=300$ MPa and $k_c=107$ N/mm$^{3/2}$. They estimated that values of $\alpha=1.94$ and $\epsilon=400$ s$^{-1}$ were appropriate for the Charpy V-notch test measurements. With $k_y=17.9$ N/mm$^{3/2}$ for the C-Mn results in Figure 1 and a computed value of $\sigma_T\approx40$ MPa at $\epsilon=3\times10^{-4}$ s$^{-1}$, then, $\sigma_G=84$ MPa for the fully austenitic finished material. The increases in $\sigma_o$ shown at the smallest grain sizes in Figure 1 are attributed to added increases in $\sigma_G$. The values of $T_C$, thus computed from the total information put into Equation (4), are shown in Figure 3, superposed on the graph of FATT measurements reported by Speich and Dabkowski (1). With the exception of one point, at $\sigma_y=300$ MPa, remarkable agreement is obtained between the computed $T_c$ and measured FATT values.

Detailed comparisons of the transition temperatures and their differences are listed in Table 2. By comparison of Figures 1-3, the initial decrease in $T_c$ with increase in $\sigma_y$ in Figure 3 has been attributed solely to a reduction in grain size, and the subsequent increase in $T_c$, attributed to an increase in $\sigma_G$. In fact, the computed lowering of $T_c$ through grain size reduction, though greater than that indicated experimentally for the C-Mn steel, is in line with that indicated in Figure 3 for the grain size reduction effect on the FATT of all of the other steels. This is encouraging because an examination of Equation (4) shows that the
Table 2. Comparison of measured (1) and computed grain size and friction stress influences on ductile-brittle transition temperatures.

<table>
<thead>
<tr>
<th>$l^{-\frac{1}{3}}$ mm$^{-\frac{1}{3}}$</th>
<th>$\sigma_G$ MPa</th>
<th>FATT/°C, meas.</th>
<th>$T_C$ °C, calc.</th>
<th>$\frac{\text{FATT}}{\Delta l^{-\frac{1}{3}}}$ meas.</th>
<th>$\frac{\text{T}_C}{\Delta l^{-\frac{1}{3}}}$ calc.</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.5</td>
<td>84</td>
<td>-59</td>
<td>-59</td>
<td>-11</td>
<td>≈ -18</td>
</tr>
<tr>
<td>9.0</td>
<td>84</td>
<td>-87</td>
<td>-109</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9.5</td>
<td>141</td>
<td>-81</td>
<td>-89</td>
<td>0.33</td>
<td>0.49</td>
</tr>
<tr>
<td>9.5</td>
<td>201</td>
<td>-59</td>
<td>-59</td>
<td>0.34</td>
<td>0.34</td>
</tr>
</tbody>
</table>

Grain size dependence of $T_C$ should be similar for the different steels. Figure 2 gives some experimental support for this consideration. The computed increase in $T_C$ with increase in friction stress seems quite reasonable. Speich and Dabkowski attributed the increase in $T_C$ to the occurrence of splitting failures. The indication is that the magnitude of the friction stress change associated with splitting is the major factor to consider when this type of behavior occurs.

**THE INFLUENCE OF GRAIN BOUNDARY CARBIDE**

A factor to consider for having contributed to the relatively high value of the FATT measurement at $\sigma_y=300$ MPa in Figure 3 is that cleavage fracture may have been promoted at this particular grain size because of the presence of carbide plates formed at some boundaries within the totally transformed ferrite grains. The situation has been analyzed recently by Petch (14). From his analysis, the lowered cleavage fracture stress, $\sigma_C'$, for unstable growth of a cleavage crack from a grain boundary carbide plate of thickness, $t$, is obtained as
where \( k_c \) is specified as

\[
k_c = \left[ \frac{8G\gamma_p}{\pi(1-\nu)} \right]^{1/4}
\]

with \( G \) being the shear modulus, \( \gamma_p \), the surface energy, and \( \nu \), Poisson's ratio. For sample calculation, Petch chose \( \gamma_p=10 \) J/m², which, with \( G=8.2\times10^4 \) MPa and \( \nu=0.28 \), gives \( k_c=53.9 \) N/mm³/². The reduction in \( k_c \), for example, from the 107 N/mm³/² value estimated on a grain size basis by Sandstrom and Bergstrom, becomes increasingly important at small grain sizes.

Bowen and Knott (15) have reported values of the microscopic cleavage fracture stresses determined for a variety of steels, spanning pearlitic, bainitic, and martensitic microstructures, in relation to the width or thickness of the coarsest carbides contained in the materials. Figure 4 shows their results in comparison with several hypothetical cases of different \( \gamma_p \) and \( \ell \) values employed in Equations (5) and (6), plus the condition employed by Petch at the ductile-brittle transition that

\[
\sigma_c' \leq \left[ \frac{\pi k_c^2}{(1+1/\ell')k_y} \right] \ell^{-1/4}
\]

The Figure shows the transition in behavior between carbide thickness and grain size control of \( \sigma_c' \) for different values of \( \gamma_p \). For \( \gamma_p=10 \) J/m², carbide thickness control occurs for \( t\geq0.4 \)μm when \( \ell=10 \)μm and for \( t\geq0.1 \)μm when \( \ell=4 \)μm. For \( \gamma_p=40 \) J/m², carbide thickness control occurs for \( t\geq0.5 \)μm when \( \ell=50 \)μm. The trends which are obtained from these estimates seem reasonable.
The influence of carbide plate thickness on increasing $T_c$ was described by Petch on the basis of Equation (2) but employing an even less complicated constitutive relation for $\sigma_{Th}$ than is given in Equation (3). Figure 5 shows the result of extending these calculations to finer grain sizes as apply for controlled-rolled steels. Also, the influence of the athermal friction stress, $\sigma_G$, on raising $T_c$ is demonstrated. Clearly, the earliest carbide thickness influence on lowering $\sigma_c$ to $\sigma_c'$ has the effect of reducing the rate of decrease of $T_c$ with grain size refinement. This is the effect suggested to be involved at $\sigma_y=300$ MPa in Figure 3.

Sandstrom and Bergstrom (12) also have reported measurements of maximum carbide plate thickness in their complete study of temperature, strain rate, grain size, and plastic constraint influences on the Charpy V-notch transition properties of C-Mn mild steel. With values of $\sigma_C=130$ MPa, $k_y=14.9$ N/mm$^3/2$, and other parameters as given previously, Equation (4) was applied first to computing $T_c$ values. The computed results are given in Table 3 under the heading $T_c(\sigma_c)$, in comparison with the experimentally estimated nil ductility temperatures which were reported. Reasonable agreement is indicated.

The full Charpy curves were reported by Sandstrom and Bergstrom so that further comparison of transition temperatures can be made. The lowest $T_c$ value in Table 3 is of concern because of the general observation that transition temperatures are increasingly abrupt and well-defined at lower temperatures for finer grain size materials. An explanation of the effect was given by Armstrong (9) on the basis of the steeper increase in yield stress which is observed at lower temperatures. The Charpy curve for the 10 $\mu$m grain size material appeared to deviate from this trend in that the change in Charpy energy with temperature was more gradual than that for the 20 $\mu$m grain size material. Petch (14) proposed that carbide-initiated cleavage could produce this type of behavior. So, consideration
was given to reducing $\sigma_c$ to $\sigma_c'$ in accordance with Equation (5) in order to
determine whether improved agreement could be obtained for the transition
temperature of the low temperature 10 $\mu$m grain size result. With $k_c=43$ N/mm$^3/2$ for
$\gamma_p=6.4$ J/m$^2$, the second set of values of $T_c(\sigma_c')$ in Table 3 were obtained. The
computed $T_c(\sigma_c')$ values are in accordance with the results shown in Figure 5 of
carbide-affected cleavage transition temperatures being raised over the grain size
determined ones.

An interesting consequence of the computations given for $T_c(\sigma_c)$ and $T_c(\sigma_c')$
in Table 3 is that the upward shift in transition temperature produced by grain
boundary carbide is increasingly larger as the ratio of grain diameter to carbide
plate thickness is smaller. The ratio decreases with decrease in grain size in
Table 3 from 32.5 to 12.5 to give transition temperature shifts increasing from
14°C to 25°C. This consideration builds on the important result shown in Figure 4,
from Bowen and Knott (15), that continued improvement of strength and toughness

Table 3. Comparison of measured (12) and computed grain diameter and
carbide thickness influences on ductile-brittle transition
temperatures.

<table>
<thead>
<tr>
<th>Material</th>
<th>$B_0$, MPa</th>
<th>$\beta_{01}$</th>
<th>$\beta_{11}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>mild steel</td>
<td>1170</td>
<td>0.0066</td>
<td>0.00034</td>
</tr>
<tr>
<td>C-Mn steel</td>
<td>1000</td>
<td>0.0075</td>
<td>0.00040</td>
</tr>
<tr>
<td>Armco iron</td>
<td>1033</td>
<td>0.0070</td>
<td>0.00042</td>
</tr>
</tbody>
</table>
properties by grain size refinement requires for grain boundary carbide prone low carbon steels that special attention be given to keeping the carbide thicknesses proportionately much smaller. The requirement becomes especially difficult for ultrafine grain microalloyed steels because of the small carbide dimension which are involved.

**SUMMARY**

The separate strengthening effects achieved by controlled-rolling over the widest range of finishing temperatures to produce, first, a reduced ferrite grain size and, then, an increased athermal friction stress give opposite influences of lowering and raising the Charpy FATT, respectively. This result is in agreement with predictions from the dislocation mechanics based Hall-Petch stress-grain size equations. An important part of the improved FATT properties achieved for a C-Mn-Mo-Nb steel is attributed to the enhanced grain size reduction and lowered athermal friction stress obtained by finish rolling austenite in a two-phase field containing a relatively strong, high temperature Mo solution strengthened, ferrite constituent. Grain boundary carbide plates give an increasingly raised FATT at ultrafine grain sizes through lowering the pile-up stress intensity needed for cleavage fracturing, particularly, at small ratios of grain diameter and carbide plate thickness where the individual dimensions are experimentally difficult to measure.
REFERENCES


Fig. 1. Yield stress, $\sigma_y$, versus reciprocal square root of grain diameter, $\ell^{-1/2}$, for different controlled-rolled steels.
Fig. 2. Fracture appearance transition temperature (FATT) versus $\ell^{-1/2}$ for different controlled-rolled steels.
Fig. 3. FATT versus $\sigma_y$ for different controlled-rolled steels, with computed transition temperatures, $T_c$, for C-Mn steel.
Fig. 4. Microscopic cleavage fracture stress dependence on reciprocal square root of carbide plate thickness or width, \( t^{-1/2} \), for a variety of steel microstructures, in comparison with the computed \( \sigma_c' \) dependence on \( t^{-1/2} \) for different grain diameters.
At $T = T_c$, $\alpha \sigma_y = \sigma_c$  
$\sigma_y = B^* - \beta^* T + k_\gamma \ell^{-1/2}$  
$\sigma_c = \sigma_c \{ \ell, t, \gamma \}$

$T_c = \frac{1}{\beta^* \left(B^* + k_\gamma \ell^{-1/2} - \frac{\sigma_c}{\alpha} \right)}$

$\Delta \sigma_{\alpha q} = 200$ MPa

$t = 1.0 \mu m$

$t = 0.25 \mu m$

Fig. 5. Computed $T_c$ dependence on $\ell^{-1/2}$ for different carbide thicknesses, $t$, and friction stresses, $\sigma_G$. 

19
<table>
<thead>
<tr>
<th>Copies</th>
<th>Copies</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>012.3</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>012.5</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>17</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>172</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>172.4</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>172.5</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>173</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>173.3</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>174</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>174.3</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>174.4</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>28</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2801</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>2803</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2809</td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>281</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2812</td>
</tr>
<tr>
<td>20</td>
<td>1</td>
<td>2812  (TMS)</td>
</tr>
<tr>
<td>1</td>
<td>5</td>
<td>2814</td>
</tr>
<tr>
<td>1</td>
<td>25</td>
<td>2814  (LRL)</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>2814  (MEN)</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2814  (MGV)</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2815</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>522.2</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>5231</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td></td>
</tr>
</tbody>
</table>

| 12 DTIC |

21
END DATE FILMED DTIC 10-88