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ADAPTIVE FILTERING FOR
SEISMIC SIGNAL DETECTION

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I. Statement of the Problem

This project is concerned with the adaptive digital processing to remove (or reduce) noisy signals generated by sensors at large distance away from the sensors. The noisy signals need to be removed because only those signals generated near the sensors are of interest for detection. The signals to be detected may correspond to footsteps of a walking man. The practical approach to this problem at the Waterways Experiment Station is to use two or more spatially separated sensors. Each sensor may consist of a number of transducer elements—each contributing constructively to the total response of the sensor. Figure A is a sketch of the sensor layout.

In this sketch, the seismic energy from the far-field source is very similar at both sensors 1 and 2. Therefore, we should be able to reduce the final signal used for processing by removing the correlated portions of the signal observed at sensors 1 and 2. When a person is very near to sensor 1 (sensor 2 being 3 meters away or more), he generates a much different signal in sensor 1 than in sensor 2. Therefore, the signals of interest should not be correlated. Mathematically the problem is to detect the footstep signal from the correlated background noise caused by e.g. moving vehicles at some distance away plus additive sensor noises. The adaptive procedure is needed because of the non-stationary nature of the data considered.

II. Methods of Approach

Two classes of digital processing techniques are considered; namely the adaptive Kalman filtering and the adaptive digital filtering. The
adaptive Kalman filter continuously monitors the "state jumps" due to the presence of personnel. Without state jumps the filter performs as an ordinary Kalman filter. The filter parameters are adjusted if a state jump is detected. False detection can be minimized by averaging over a sufficiently large "window." A generalized likelihood ratio is used for detection of state jumps. The method was originally proposed by Willsky and Jones [1] and was successfully employed by us in detecting the object boundary in image scan lines [2].

The block diagram of the adaptive digital filter considered is shown in Figure B. The input-output relation of the non-recursive Adaptive Digital Filter (ADP) is given by (Figure C),

\[ g_m = \sum_{n=0}^{N} b_{n,m} f_{m-n} \]  

where \( g_m \) is the filter output, \( b_{n,m} \) is the filter coefficient, and \( f_n \) is the filter input. Define the vectors

\[ B_m = [b_{0,m}, b_{1,m}, \ldots, b_{N,m}] \]

and

\[ F_m = [f_m, f_{m-1}, \ldots, f_{m-N}] \]

where \( N \) is the order of the filter, and \( m \) is the number of iterations in adjusting the filter coefficients. Eq. (1) can be written as

\[ g_m = B_m F_m = F_m B_m \]  

We use the Noisy LMS Algorithm [3] in our computer program to calculate the filter coefficients \( b_{n,m} \), i.e.
\[
\begin{align*}
B_{m+1} &= B_m + \nu e_m F_m \\
e_m &= y_m - q_m \\
q_m &= B_m F_m
\end{align*}
\tag{3}
\]

where \( \nu \) is a constant. After adjusting the values of \( \nu, N, m, \) and delay time, we can obtain the desired result with a greatly improved signal-to-noise ratio.

III. Implementation and Computer Results

Extensive effort was made to implement the two methods described above on the PDP 11/45 computer with the seismic data supplied by the Waterways Experiment Station. The data are stored in two magnetic tapes. The first tape consists of 4-channel data while the second tape consists of 14-channel data. Mr. Mark Flohr of the Waterways Experiment Station was particularly helpful to acquaint us with the structure of the data format during his visit in August 1979. The computer results presented are based on a data set of footstep signal plus a small amount of noise. To cope with the memory capacity of the minicomputer, every fifth data sample is taken from the 4-channel data tape with a resulting sampling rate of 200 sample/sec. A sequence of 960 sample points are taken for detailed study (Record 327 to 356). Figures 1a, 2a, 3a and 4a show the digitized data from the four channels with corresponding Fourier amplitude spectra given by Figures 1b, 2b, 3b and 4b, respectively.

The Adaptive Kalman Filtering was implemented to detect the jumps. Figures 5, 6, 7 and 8 show the waveforms before and after detection along with a printout of the number of jumps detected. These numbers are gene-
rally correct. The complete listing of the computer program has been forwarded to the Waterways Experiment Station. Further improvement of the program is desirable to demonstrate the effect of noise reduction while performing the jump detection. The parameters are fairly sensitive to the result and the following list is the best set of parameters:

- AA (transition coefficient) = 1.0
- Q (covariance of the system driving noise) = 1.0
- R (noise power) = 1.0
- TH (threshold) = 10.0
- M (length of window) = 10

There is no estimation of parameter R or transition matrices W and P. Total number of samples is 960 per channel.

For the implementation of the Adaptive Digital Filter on the PDP 11/45, the subroutine AF serves as the Adaptive Filter, and the subroutine SHIFTR serves as the Shift-Right Register. The meanings of all variables and arrays in the subroutine AF are stated below.

- ND: Noisy data array, i.e. input data
- NF: Number of noisy data points
- NDELAY: Number of delay points
- M: Number of iterations
- N: The order of the ADF
- V: The constant v of the ADF
- B: Coefficients of the ADF, stored in an array
- DND: Delay elements for storing delayed data points
- F: The variables $f_m$ in the ADF, as an array
- G: The variables $q_m$ in the ADF, i.e., the output data
- E: The variables $e_m$ in the ADF
- Y: The variable y
Array B and array F are initially set to zero. The program processes the data on a channel-by-channel basis. The complete program named as SPAN4 also includes an ANFFT Subroutine which performs FFT on the original input data and also on the filtered output data. The complete program listing is in the Appendix.

Figure 9 shows a sequence of filtered waveforms for channel 1. The best result is given by Figure 9e with a corresponding FFT given by Figure 9f. Here $M = 1$, $N\text{DELAY} = 30$, $N = 18$, and $V = 0.0112$. Figure 10 shows a sequence of filtered waveforms for channel 2. The best result is given by Figure 10e with a corresponding FFT given by Figure 10f. Here $M = 1$, $N\text{DELAY} = 30$, $N = 17$ and $V = 0.00145$. It is noted that the parameter choice is also very sensitive in the adaptive digital filtering operations. The filtered results clearly illustrate the suppression of background noise and the enhancement of footstep signals. The filtered results are so good that further process of jump detection appears unnecessary. All Fourier spectra correspond to a frequency range of 0 to 100 Hz.

Both adaptive filtering techniques have been shown to be very effective for the seismic detection tasks under consideration. They both are computationally efficient. Proper choice of parameters is an important step to derive the best results. Although mathematically the Kalman filter and the adaptive digital filter are somewhat equivalent, the implementations of the two techniques are different and thus the results are different also. The adaptive Kalman filtering in fact has more flexibility to adjust itself to the change in data characteristics.
References


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DIMENSION F(4,32), X(1024), Y(1024), C(257)
COMPLEX EY(1024)
INTEGER CHNO, IREF, DLY, ITR, OK
COMMON F, NP, INDEX
hi; h FILE' (50, "W", II, INDEX)
FORMAT (0)

6 FORMAT ( INPUT IGD, NP, IREF, DLY, ITR, OK, NTE, V )
7 FORMAT (715, F12.5)
WRITE (4, 5)
WRITE (6, 6)
READ (6, 7) IGD, NP, IREF, DLY, ITR, OK, NTE, V
IF (IGD NE 0) GO TO 71
CALL GDATA

71 NF = 960
DO 8 I = 1, 1024
X(I) = FLOAT(I)
9 DO 10 CHNO = 1, 4
INDEX = 1
DO 11 I = 1, 30
READ (3, INDEX) X
L = (J-1)*32
DO 15 J = 1, 32
L = L + 1
Y(L) = F(CHNO, I)
15 CONTINUE
112 CONTINUE
DO 35 J = 1, NF
Y(I) = Y(I)/1000
35 CONTINUE
DO 41 I = 961, 1024
Y(I) = 0
41 CONTINUE
FORMAT ( "#### PLOT OF ORIGINAL DATA: CHANNEL", J )
IF (NP NE 0) GO TO 56
WRITE (5, 54) CHNO
24 FORMAT ( "#### ORIGINAL DATA FUNCTION VALUES OF CHANNEL", J )
WRITE (5, 55) Y
95 FORMAT (1X, 10=13 5)
WRITE (6, 21) NF
41 FORMAT (1X, NF = X, )
CALL NP(X, 0, N)
WRITE (5, 20) CHNO
WRITE (6, 20) CHNO
WRITE (6, 21) NF
30 FORMAT (1X)
CALL NDAT(X, Y, 1024, 0, 1024, 10, 700)
READ (0, 0) NX
CALL NP(V)
IF (IREF NE 1) GO TO 93
CALL NP(Y, NF, DLY, ITR, OK, NTE, V)
831 WRITE (1, 1024)
1024 FORMAT ( I, 1024 )
10 CONTINUE
IF (FREE EQ 0) GO TO 2100
WRITE (8,31) CHNU

87 FORMAT ('** **** PLOT OF PREFILTERED DATA OF CHANNEL ,I2)
CALL KBPLOT (X, Y, 1024, 1, 1000, 10, 700)
READ (6, 30) NX
CALL NEWPAG
IF (NF NE 0) GO TO 2100
WRITE (5, 2110) CHNU

2110 FORMAT ('** **** PREFILTERED DATA OF CHANNEL ,I2)
WRITE (5, 55) Y

2100 CALL ANFFT (CY, 10)
DO 50 I = 1, 1024
Y (I) = CAB (CY (I))
CONTINUE
WRITE (6, 50) CHNU

50 FORMAT ('** TYPE RERUTN FOR PLOT OF FFT DATA. CHANNEL ,I2)
READ (6, 30) NX
CALL KBPLOT (X, Y, 512, 0, 1023, 10, 700)
READ (6, 30) NX
IF (NF NE 0) GO TO 175
WRITE (5, 171) CHNU

171 FORMAT ('** FFT DATA FUNCTION VALUES OF CHANNEL ,I2)
WRITE (5, 55) Y

175 READ (6, 30) NX
CONTINUE
CALL EXIT
END

SUBROUTINE UDATA
INTEGER CH, RATE
BYTE B (1280)
DIMENSION IA (1280), F (4, 32)
COMMON F, NF, INDEX
INDEX = 1
DO 200 NR = 1, 80
CALL READLINE (E, NPT)
NF = NPT / 8 * 8
WRITE (6, 50) NPT

50 FORMAT ('** TOTAL BYTES READ FROM TAPE = ', I7)
DO 70 I = 1, NPT
CALL BY2IN (B (I), II)
IA (I) = II
CONTINUE

70 FORMAT (12I5)
DO 80 I = 1, NPT, 2
IA (I + 1) = IA (I) * 256 + IA (I + 1)
CONTINUE

80 NT = NPT / 2
DO 90 CH = 1, 4
I = 1
DO 90 J = 1, NT, 20
F (CH, J) = FLOAT (IA (I))
I = I + 1
WRITE (3, INDEX) F
CONTINUE
RETURN
END
SUBROUTINE ANFFT(X, M)
COMPLEX X(1), U, W, T
N=2**M
N2=N/2
N1=N-1
J=1
DO 3 I=1, N1
IF (I GE J) GO TO 1
T=X(J)
X(J)=X(I)
X(I)=T
1 T=N2
IF (I GE J) GO TO 3
J=J-K
K=K/2
GO TO 2
3 J=J+K
PI=3.1415926
DO 5 L=1, M
LE=2**L
LE1=LE/2
U=(1.0, 0.0)
W=CMPLX(COS(PI/LE1), SIN(PI/LE1))
DO 5 J=1, LE1
DO 4 I=J, N, LE
ID=I+LE1
T=X(ID)*U
X(ID)=X(I)-T
4 X(I)=X(I)+T
5 U=U*W
RETURN
END
SUBROUTINE AF(ND, NF, NDELAY, M, N, NTE, V)
REAL ND(1), F(40), B(40), DND(400)
DOUBLE PRECISION G
N=0
IF=N+1
DO 50 I=1, IF
B(I)=0
F(I)=0
50 CONTINUE
DO 40 I=1, NDELAY
J=NDelay-I+1
DND(I)=ND(I)
40 CONTINUE
IIF=NDELAY+1
DO 100 IND=IIF, NF
Y=ND(IND)
CALL SHIFTR(Y, DND, NDELAY, TEMP)
CALL SHIFTR(TEMP, F, NP, TEMPI1)
DO 200 IM=1, M
I=-I
CALL SHIFTR(TEMP, FNP, TEMPI2)
110 IM1=1, M
0=0
DO 500 I=1, NP
G=G+F(I)*E(F(I))
500 CONTINUE
F=Y-G
DO 400 I=1, NP
B(I)=B(I)+V*E*F(I)
400 CONTINUE
IF(NTE NE 0)GO TO 200
PRINT 600, IND, IM, E, G
600 FORMAT(1X, 'SAMPLE', IS, 'ITERATION', IS, 'F=', F15.5, 'G=', F15.5)
PRINT 601, B
601 FORMAT(1X, 12F10.2)
PRINT 602, F
602 FORMAT(1X, 12F10.2)
200 CONTINUE
700 ND(IND)=G
100 CONTINUE
RETURN
END

SUBROUTINE SHIFTR(SHIN, A, L, SOUT)
REAL A(I)
SOUT=A(L)
NDIM=L-1
DO 100 K=1, NDIM
I=L-1+1
L=L-1
A(I)=A(J)
100 CONTINUE
A(I)=SHIN
RETURN
END
Figure A

Figure B

Figure C