DESIGN AND ANALYSIS OF COMPOSITE ROADWHEELS FOR LVTP7 AND M113A1

August 1984

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ABSTRACT

Three composite design concepts are presented, a detailed analysis of one concept shows the feasibility of using advanced composites for the construction of LVTP7 and M113A1 roadwheels. The other two potential designs given may offer improved performance through lower internal shear stresses in the structure and lower cost manufacturing. Weight savings of about 30% were achieved with the composite designs. These designs will fit the existing vehicles with no modifications required.

While the manufacturing analysis shows that the composite wheels will be more expensive to manufacture than the aluminum wheels using current techniques, production efficiency and experience gained during prototype fabrication may result in a composite roadwheel which is more cost competitive. High production techniques such as injection molding with thermoplastics will not yield a wheel with the required performance or weight savings. Resin transfer molding, compression molding, and autoclave molding do offer some potential for economical manufacture and their merits are discussed.
FOREWORD

This final report was prepared by Fiber Materials, Inc., Biddeford, Maine, for the U.S. Army Materials and Mechanics Research Center, Watertown, Massachusetts under contract DAAG46-83-C-0026. Mr. Keith Burgess was the Program Manager and performed the manufacturing analysis while Mr. John Pepin and Mr. Stephen Biddle conducted the design and analysis work. Mr. Michael Edwards assisted with computer code set-up and Mr. Ted Grethe with graphics. The AMMRC COTR was Mr. Peter G. Dehmer. This work was done during the period of 20 May, 1983 to 20 October, 1983.
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1.0 INTRODUCTION

This report presents the design and analysis to establish feasibility and design criteria for reinforced plastic (RP) roadwheels for the LVTP7 and M113A1 armored personnel carriers. The study includes the redesign of existing metal roadwheels using RP materials.

Additional goals of reducing weight and lowering production cost while retaining or increasing service life as compared to the current metal construction, were examined.

An analysis of the existing metal wheels was first undertaken to establish areas of high stress and deflection. The finite element analysis was used to evaluate these critical areas for the LVTP7 roadwheel. Because of the geometric similarities between the two roadwheels, knowledge of high stress regions for the LVTP7 roadwheel was used to infer critical areas of the M113A1 wheel. Stress in these areas was then bounded by analyzing discrete ring and disc segments. The data acquired from this step were used to select materials, fiber architecture and geometry for the design of the composite roadwheels. A feasibility analysis was undertaken to determine whether or not reinforced composite materials could be used for this application. Various design alternatives were investigated along with manufacturing schemes. The composite roadwheels were designed and analyzed with respect to mechanical integrity, reliability, and environmental aging. A detailed manufacturing and cost analysis was undertaken to determine manufacturing methods, material costs, labor and tooling costs, and available volume for production. The report also makes recommendations concerning the practical feasibility of producing the composite roadwheels.
2.0 Analysis of Existing Roadwheels

2.1 LVTP7 Roadwheel

2.1.1 Finite Element Analysis Description

The static analysis of the LVTP7 roadwheel was performed using a finite element computer program called NISA (Numerically Integrated Elements for System Analysis) developed at the Engineering Mechanics Research Corporation.

The purpose of this analysis was to investigate the internal stresses and deformations of the wheel for two different loading conditions. These stresses were then used in the design of a composite roadwheel.

Note that a finite element analysis was conducted only on the LVTP7 roadwheel and not on the M113A1 roadwheel. The design team felt that because of the similarities in the geometry and loading directions of the two wheels, only the LVTP7 roadwheel needed the finite element analysis. Critical areas of the M113A1 were inferred from the results of the LVTP7 analysis and were investigated by solving loaded ring and disc problems to obtain stress upper bounds.

The following is a brief description of the process undertaken in construction of the finite element model. The geometry of the wheel had to be established in a form that could be easily coded into the program. From the engineering drawings, one repeatable sector or arc of the wheel, was broken up into 3-D finite elements, each containing 20 nodes as shown in Figure 2.1. The coordinates of each node of every element of the repeatable sector were determined from the drawings (in cylindrical coordinates), and listed as data in the input file of the program. Then the connectivities, or lines between nodes were established, thus defining each element. The result was a sector of the wheel containing 12 elements as shown in Figure 2.2. Using a system subprogram, this sector was reproduced in such a way as to generate the remainder of the model shown in Figure 2.3. Note that only half of the wheel needed to be modeled because of symmetry with respect to the vertical axis of both the geometry and loading boundary conditions.
It was intended that the elements be broken into more subelements, but difficulties with the mesh generating routine prevented this. At this point, the model has been generated but additional information was required before the program was executed. Since the wheel is mounted to an immovable hub, the displacements and rotations of the nodes at the mounting holes are zero. Also, because only half the wheel is present in our model, all the nodes along the interface between the existing model and the unmodeled half, had to be constrained to translate only along the wheel plane of symmetry. At this point, loading information was provided for two different load cases. The first load case, Figure 2.4, involved a uniform line load equivalent to 15,000 lbs; however, because only half the wheel was present in our model, only half of this load or 7,500 lbs was required for our analysis.

The second load case, Figure 2.5, involved a uniform line load equivalent to 1,901 lbs, as well as a uniform line load applied to the side of the wheel of 1,098 lbs located along the wear ring. As in the previous case, only half of these loads were used in the analysis because only half of the actual wheel was used as the model. This combination side and vertical loading was used to simulate the loads applied as the vehicle is traversing a 30° side slope.

At this point, the model was ready for execution. Stress plots were obtained for different views of the model. Contour plots of front, back and plane of symmetry cross-section views of maximum principle stress, minimum principle stress, Von Mises equivalent stress and maximum shear stress, were made and are given in Appendix 1. The results of these plots indicated areas of high stress. In the design of the composite wheel we used this information to minimize these areas of high stress and to develop a reliable lightweight composite replacement.
3-D SOLID ELEMENT

FIGURE 2.1

WHEEL SLICE

FIGURE 2.2
VERTICAL LOAD CASE

MID PLANE CROSS SECTION VIEW

FIGURE 2.4

15,000 LB. LOAD UNIFORMLY DISTRIBUTED
COMBINED VERTICAL AND SIDE LOAD CASE

MID PLANE CROSS SECTION VIEW

FIGURE 2.5

1098 LB. LOAD UNIFORMLY DISTRIBUTED ALONG WEAR RING SEAT

1901 LB. LOAD UNIFORMLY DISTRIBUTED
2.1.2 Analysis Results

Some unexpected results were obtained using the finite element analysis. In comparing the combined side and vertical load case with the vertical load case, the locations of the high stress levels occurred in the same areas. The side loading did not contribute to the bending stresses at the bolt hole areas as expected. The stress magnitudes were of course different because the applied loads were different. The vertical load case of 15,000 lbs imposed the highest stresses in the wheel, and as a result the investigation was focused on stresses and displacements of this loading case.

The most critical stresses imposed on the wheel occur in the outer ring area near the load application point (refer to Figures 2.6 and 2.7). These stresses are in the order of 60,000 psi compression on the lower portion of the outer ring area, and 30,000 psi tension on the upper portion. These are hoop stresses that act normal to radial planes. In the transition area high bending stresses had been expected due to the cantilever effect of the applied load acting along the inside and outside rim. The hoop stiffness was sufficient to minimize this cantilever effect, and the bending stresses in this region were not critical. Shear stress exists in the outer ring area, and oriented in the hoop direction. The magnitude of these stresses are 30,000 psi. As with the high normal stresses previously described, the shear stresses are caused primarily by the bending of the hoop or inner and outer ring portions of the wheel.

The deflections caused by the 15,000 lb vertical load were found to be high. As shown in the scale drawings of Figures 2.9 and 2.10, the tip of the outer rim area is displaced to the right and up about 0.2 inches. It should be emphasized that this deformed geometry is from a very severe, worst case type, loading condition. A deformed geometry, probably more representative of actual service conditions, is shown as circled dots on the end of the outer ring area of Figure 2.9. This corresponds to the combined vertical and horizontal load case.
NOMENCLATURE USED IN DESCRIBING THE LVTP7 WHEEL

FIGURE 2.6
NORMAL STRESSES
MID PLANE CROSS SECTION
FIGURE 2.7
30,000 PSI SHEAR STRESS DUE TO HOOP EFFECT

SHEAR STRESSES
MID PLANE CROSS SECTION

FIGURE 2.8
5.0 INCHES TO CENTER OF ROTATION

DEFORMED GEOMETRY
WHEEL MID PLANE CROSS SECTION

FIGURE 2.9

ACTUAL SIZE

--- DEFORMED GEOMETRY 15,000 LB. VERTICAL CASE
--- UNDEFORMED GEOMETRY
○ END POINT LOCATIONS OF DEFORMED GEOMETRY WITH VERTICAL AND SIDE LOAD CASE

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Figure 2.10 shows a deformed geometry front surface view. The figure is scaled to 42% of its actual size. The applied load is 15,000 lbs.
2.1.3 Alternative Analytical Approach

In order to establish an analytical approach to be used for the M113A1 roadwheel, each of the major stress areas on the LVTP7 was evaluated manually and compared to the results of the Finite Element Method (FEM). The intent of this approach was to establish reasonable upper bounds for the predicted stresses in order to allow feasibility studies to be completed.

The approach used to establish the analytical methods was to first examine the output of the FEM analyses to observe the nature of the stresses and deformation of the wheel, and then to develop analytical models that incorporated these observations and yielded comparable results.

Stresses in the Disk Near the Bolt Circle. The results of the FEM indicated that the curvature in the disks area did not contribute significantly to the strength of the disk. This was verified by calculating the stresses by assuming that the disk was flat and fixed at the edges by the rim. Case 821 from page 8368 of Roark's "Formulas for Stress and Strain" (5th Edition) was used.

Based on the FEM, the stresses were

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<tr>
<td>Tension</td>
<td>14,000 psi</td>
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Notation:

- \( \sigma \) = calculated stress
- \( a \) = effective outer radius of the disk = 11.75"
- \( b \) = restrained inner radius of the disk = 6.12"
- \( \beta \) = factor per Roark
- \( M \) = applied moment
- \( F \) = force on bottom of wheel = 15,000#
- \( t \) = thickness at radius location "b" = .531
- \( m \) = moment arm = 3.06"
\[ b/a = 0.521 \]
\[ \beta = 1.06 \text{ (per Roark)} \]
\[ M = Fm = 45,900 \text{ in lb} \]
\[ \sigma = \frac{BM}{at^2} \text{ (per Roark)} \]
\[ \sigma = 15,000 \text{ psi (versus an average of 17,000 by FEM)} \]

Compressive stresses due to radial support loads in the disk were estimated by assuming that, at the point in question, the effective width of the disk was equal to two-thirds of the restrained inner diameter of the disk. This resulted in a compressive stress.

\[ \sigma = \frac{15,000}{(2/3 \times 2b \times t)} = 3100 \text{ psi} \]

The total of the stresses was then found by adding the above values.

\[ \sigma = 15,000 - 3000 = 12,000 \text{ in tension} \]
\[ \sigma = 15,000 + 3000 = 18,000 \text{ in compression} \]

These values are comparable to the FEM values of 14,000 and 20,000 respectively.
Stresses in the Outer Rim  The FEM results indicated that the principal stresses in the outer rim were circumferential and caused by deflecting the outer rim section into a non-circular shape. This result is reasonable in that the bending stiffness of the rim (in the hoop direction) is substantial compared to the bending restraint of the disk. The result of this is a deflection of the outer edge of the rim both towards the axis and towards the disk (the disk behaves like a simple support to the rim). The above condition was approximated by calculating the bending stress in a rim of 1/2 of full width, i.e., the outer half of the rim. Half of the load was assumed to be carried by the disk and the other half by the rim.

In order to account for the interaction between the disk and the rim, the disk was assumed to be providing distributed support to the rim. This support was applied over 90° of rim which coincided with the deflection nodes as shown in Figure 2.10.

Based on the FEM, the stresses were

Compression 60,000 psi
Tension 30,000 psi

Roark's 5th edition, page 226, case 68 was used for the following calculations:

Notation:

\[ \theta = 135^\circ \]
\[ F_r = \text{Force on the rim} = 7,500 \] lb
\[ R = \text{Radius of the rim} = 11.4" \]
\[ I = \text{Moment of inertia through the section centroid} = 0.081 \text{ in}^4 \]
\[ C = \text{Distance to extreme fiber} = 0.45" \]
\[ K = \text{Constant per Roark (K_m)} \]
\[ w = \text{Effective loading of the rim} \]
\[ \sigma_r = \text{Calculated stress} \]
\[ F = 2 w R \sin \theta \]
\[ w = 466 \#/\text{in} \]
\[ K = -0.149 \text{ for } \theta = 135^\circ \]
\[ M = K (wR^2) \]
\[ M = 9000 \text{ in. lb. at } \theta = 180^\circ \]
\[ \sigma = \frac{Mc}{I} \]
\[ \sigma = 50,000 \text{ psi (versus an average of 45,000 psi per FEM)} \]
2.2 M113A1 Roadwheel

2.2.1 Analysis Method

From the finite element method (FEM) of the LVTP7 roadwheel, specific areas and values of high stress were located. Since the basic geometry of the two wheels is similar, critical areas of the M113A1 can be identified from the previous analysis. These areas were:

1. Hoop stress in the outer rim.
2. Radical bending stresses in the disk near the bolt circle.
3. Circumferential shear stresses in the outer rim.

By applying the methods used in section 2.1.3, the stresses can be calculated for the M113A1 roadwheel. All notation corresponds to section 2.1.3.

### Stresses in the Disk Near the Bolt Circle

\[
a = 10.8'' \\
b = 4.1'' \\
b/a = 0.38 \\
b = 1.92 \\
M = 8,450 \text{ in. lb.} \\
\sigma = 50,000 \text{ psi (bending stresses)}
\]

**Compression Stresses:**

\[
\sigma = \frac{4525}{(2/3 \times 2 \times 4.1 \times 0.31)} \\
\sigma = 2700 \text{ psi} = \text{approximately 3000}
\]

**Combined Stresses:**

\[
\sigma = 50,000 + 3,000 = 53,000 \text{ compressive} \\
\sigma = 50,000 - 3,000 = 48,000 \text{ tensile}
\]
Stresses in the Outer Rim

\[ I = 0.0832 \]
\[ c = 0.86 \text{ (inside)} \]
\[ c = 0.384 \text{ (outside)} \]
\[ w = 305\# / \text{in.} \]
\[ M = K (wR^2) \]
\[ M = -5010 \text{ in. lb.} \]
\[ J = \frac{Mc}{I} \]

\[ \sigma = 49,000 \text{ psi tension on inside edge} \]
\[ \sigma = 23,000 \text{ psi compression on outside edge} \]

Bearing Stresses at Bolt Holes  Bearing stresses at the bolt holes were conservatively estimated by assuming all the load on two bolts.

\[ d = \text{bolt diameter} \]
\[ t = \text{laminate thickness} \]
\[ \sigma = \frac{F}{2d/t} \]
\[ \sigma = \frac{4525/2}{0.685 \times 0.31} = 11,000 \text{ psi} \]
3.0 Feasibility Analysis

Based on the analyses of the metal roadwheels and on factors peculiar to composites, the feasibility of using composites was reviewed prior to developing the design of the laminates.

Strength  The character of the stresses and strains developed in a wheel very quickly eliminate thermoplastics and short fiber composites. High modulus composites are required to limit the rim deflections and to provide resistance to fatigue. A composite consisting of primarily carbon/epoxy will be considered in more detail due to the combination of light weight, high strength and high stiffness.

Wear Ring Attachment  Holes subjected to bending or axial loading in a composite material are subject to high stress concentrations in the vicinity of the hole area. The wear rings on both of the existing wheels is riveted in place. On the composite wheel design however, the wear rings would be held in place using an adhesive. The first major consideration in the selection of adhesive for the composite wheels was strength. The required adhesive strength was determined by calculating the rivet shear strength, and comparing this value to the adhesive shear strength assuming the entire mating surface of the wear ring is bonded to the wheel.

Adhesives that easily possess the required shear strength characteristics when bonded to steel are: cyanoacrylate, and epoxy. If a thermoset adhesive is used, the softening point temperature must be lower than the softening point of the graphite epoxy wheel. To remove the wear ring for routine replacement, it must be heated carefully and stripped off. The surface of the wheel must be abraded and cleaned, and the new wear ring abraded and degreased before replacement. Adhesive must be applied to the mating surface of the wear ring and pressed into place. It would then be cured for a specific time and temperature depending on the adhesive used.

It was assumed that the main mode of failure for the existing rivets that fasten the wear ring to the wheel is shear. The method of analysis for the replacing these rivets with an epoxy based adhesive is to determine the maximum shear forces the existing rivets can support, and then calculate the shear requirements for the adhesive.
For this analysis, the ultimate shear stress for the rivets is assumed to be 49,000 psi as per Mil-HDBK-5C. This is based on Monel rivets per Table 8.1.2(b).

LVTP7 roadwheel-

for the rivets $D = 0.385$ inches 15 rivets per wheel

$$A_r = \frac{\pi D^2}{4} = 0.116 \text{ in}^2$$

Maximum load supported per rivet $(F/r) = S_{su} A$

$$F/r = 49,000 \times 0.116 = 5,684 \text{ lbs.}$$

$Di = 19.375$ inches (inside diameter of wear ring)
$Do = 22.875$ inches (outside diameter)

Area of wear ring: $Aw = \frac{\pi}{4} (Do^2 - Di^2)$

$$= 116.1 \text{ in}^2$$

Theoretical wear ring area supported by each rivet

$$A/r = \frac{Aw}{\# \text{ of rivets}}$$

$$= \frac{116.1 \text{ in}^2}{15}$$

$$A/r = 7.7 \text{ in}^2$$

the required shear strength of the adhesive is $\frac{F/r}{A/r}$

$$\frac{F/r}{A/r} = \tau = \frac{5,684 \text{ lbs}}{7.74 \text{ in}^2}$$

$$\tau = 734 \text{ psi}$$ (required shear strength of adhesive)
M113A1 roadwheel—
for the rivets D = 0.25 inches
18 rivets per wheel

\[ Ar = \frac{\pi D^2}{4} = 0.049 \text{ in}^2 \]

\[ F/r = S_{su} A \]
\[ = 49,000 \times 0.049 \]

\[ F/r = 2401 \text{ lbs.} \]

Di = 16.69 in.

Do = 21.81 in.

\[ Aw = \frac{\pi}{4} (Do^2 - Di^2) \]
\[ Aw = 154.8 \text{ in}^2 \]

\[ A/r = \frac{Aw}{\# \text{ of rivets}} \]
\[ = \frac{154.8 \text{ in}^2}{18} \]

\[ A/r = 8.6 \text{ in}^2 \]

\[ \frac{F/r}{A/r} = \frac{2401 \text{ lbs.}}{8.6 \text{ in}^2} \]

\[ \tau = 279 \text{ psi (required shear strength of adhesive)} \]
Based on this review, it is concluded that the wear plates can be bonded due to the low strengths required. In the event that riveting is desired, then this option may be available depending on the actual strength requirements. The primary consideration against rivets is that close tolerances are required to avoid fatigue damage to the composite. Shock and impact loads were not evaluated and may affect these conclusions.

Fatigue Considerations - Requirements given for the wheel show a cyclic environment to about $0.5 \times 10^5$ cycles. High strength unidirectional graphite/epoxy can be cycled in tension to up to 130 ksi for a half million cycles (from reference 3, Figure 1.2.5-17). This cyclic stress level corresponds to about 0.6% strain in tension. Since these composite wheel designs attempt to align fibers with principal stress directions, effects of cyclic loading on in-plane properties will be small. However, the interlaminar shear strength drops to 55% of its static value after a half million cycles while the stiffness remains close to 90% (Figure 1.2.5-25, reference 3). Given this fact, the resin systems used, a working level interlaminar shear strength of 4 ksi must be obtained.

Reliability and Environmental Effects - Reliability and maintainability of the composite wheels is a function of several factors such as preventing damage from heavy impact. A glass reinforced plastic (GRP) outer protective covering will sacrificially protect the wheel from abrasion and small scale impact.

The titanium sleeve in the holes was chosen to protect the graphite laminate holes from wear and corrosive contact with bolts.

Environmental effects such as heat, moisture, and high strain rate change the mechanical properties of graphite epoxy composites. Heat and moisture studies that have been conducted show that these environmental effects are matrix dependent. The graphite fibers are affected little by temperature or humidity increases while the epoxy matrix is
susceptible to these environmental influences; hence, the longitudinal properties (those in the direction of the fibers) for a unidirectional composite remain fairly constant. The tensile strength is, in fact, found to be slightly higher in the longitudinal direction after being subjected to a heat and moisture environment as shown by Figure 3.9. This is presumably due to uneven tension on the fibers and the behavior of the matrix material near broken fibers. Properties for the transverse direction (perpendicular to the longitudinal direction) are degraded by heat and moisture as shown in Figure 3.10. The transverse strength decreases with an increase of either temperature of humidity, caused by a weakening of the epoxy matrix material. The transverse modulus becomes less temperature dependent with an increase in moisture content. Figure 3.11 shows that the axial shear modulus is the property most affected by humidity, temperature, and strain rate. In addition, the shear modulus is dependent on the level of the applied shear stress. As expected with polymeric materials, the stiffness decreases with increasing temperature and moisture content. Also, the stiffness increases with increasing applied strain rate. Figs 3.1, 3.2 & 3.3 are based on Ref (8).

For this particular application, environmental effects will be minimal. The operating temperatures are moderate enough for thermal degradation effects to be insignificant. For thermal cycling between room temperature and 270°F for 500 cycles, (much more demanding than this application), the data shows only a slight decrease in interlaminar shear strength with other physical properties unaffected.

Physical aging effects are also slight. Aging is primarily a matrix bound phenomena. The graphite fibers are unaffected by aging, and so for a unidirectional composite, the properties in the longitudinal direction are unaffected. Available data suggests that a 10% decrease of interlaminar shear strength and transverse strength can be expected in 10 years.
VARIATION OF AXIAL STRENGTH WITH TEMPERATURE AND MOISTURE CONTENT

FIGURE 3.1
EFFECT OF TEMPERATURE AND MOISTURE CONTENT ON TRANSVERSE STRENGTH

FIGURE 3.2
STRAIN RATE 50 x 10^{-6}/SEC
TEMPERATURE 96°C
MOISTURE CONTENT 1.15%

STRAIN RATE 2000 x 10^{-6}/SEC
TEMPERATURE 24°C
MOISTURE CONTENT 0.1%

AXIAL SHEAR STRESS-STRAIN CURVES FOR TWO LOADING CONDITIONS

FIGURE 3.3
4.0 Design of Composite Wheels

4.1 LVTP7 Roadwheel Design

4.1.1 Design Criteria

The design of the composite roadwheel was based on the maximum wheel load of 15,000 lbs. in the vertical direction. The finite element analysis showed that this condition was the worse loading case causing high stresses in the wheel rim and bolt hole areas. A margin of safety of 1.25 was established for the composite roadwheel design. To allow for design uncertainty in composite degradation due to moisture, environmental factors, and damage tolerance, the ultimate composite stress shall be 1.25 times that stress encountered at the 15,000 lb. vertical load in any area of the wheel.

The basic structural material selected for this design is a high strength, intermediate modulus graphite fiber such as T-300 in an epoxy resin matrix.

Several factors were considered in the selection.

1. Graphite/epoxy is lightweight over glass and has better compressive properties than Kevlar. Many areas of this wheel experience high compressive stresses.

2. High stiffness.

3. Good data base from which to design.

4. Good fatigue properties compared to glass.

Glass and Kevlar composites will be used as secondary materials to protect the graphite laminate from impact, abrasion and contact with metals.
The strain at selected areas of the wheel will be compared to the aircraft industry standard of .6% allowable for a graphite/epoxy laminate. Typically, the maximum tensile strain of a T-300 unidirectional composite is .8% while for a ±45 angle ply laminate it is 2.2%. The .6% allowable reflects, again, the general lack of firm knowledge about the onset of delamination and the tolerance of the structure to delamination growth.

The thickness of the laminate in the bolt hole area was kept the same as the aluminum to preserve the symmetry and alignment of the wheels when mounted. This is required in order to maintain the same center line between a set of roadwheels without resorting to two different designs.

4.1.2 Composite Design Considerations Resulting from Aluminum Wheel Analysis

First, the deformation and stress state of the aluminum wheel are reviewed to determine how the selective reinforcement of a structural composite can best be used. Figures 2.9 and 2.10 show a cross section and end view of the wheel with the deformed shape at maximum wheel load shown in dotted lines. Several deformation mechanisms are evident.

1. Rim distortion out-of-round leading to beam loading type stresses in radial planes of the rim. A hoop compression of the rim is also taking place leading to a hoop compressive stress.

2. Out-of-plane bending of the wheel disc causing flexural stresses through the thickness of the disc.

3. Cantilever type bending of the rim along the line of high pressure contact with the ID of the rubber tire.

Each type of deformation results in a stress state within all points of the wheel. By limiting the magnitude of certain types of deformation using selective orientation of the reinforcing fibers, stress magnitudes can be reduced in critical areas. For example, the flexural stiffness of
of the rim cross sections (EI) offer resistance to out-of-round deformation of the rim. Using preferential reinforcement of the hoop direction in the rim, the rim flexural stiffness will be increased over that of the aluminum. This will both lower the hoop stresses in the rim and flexural stresses in the corner joint between the rim and disc.

4.1.3 Composite Design Concept for LVTP7 Roadwheel

To design the composite wheel as a laminate with much the same envelope as the aluminum wheel, it is important to reduce deformations of the rim as much as possible to avoid high interlaminar shear stresses in the rim itself and in the transition corner between the rim and disc. Also, since the primary loading of the wheel disc is compression and tension in the radial direction and flexure out-of-plane, the primary reinforcement of the wheel disc is radial. Figure 4.3 shows the lamina orientations selected for each area of the wheel. They exhibit the preferential radial and hoop reinforcement as well as multi-axial reinforcement around the bolt holes. Dimensions of the wheel are shown in drawing #740-0008 found in Appendix 3.

4.1.4 LVTP7 Composite Design Analysis

The analysis of the composite wheel is performed by checking the strain and laminate stress in critical areas of the wheel. This is done by making upper bound assumptions on the internal loading in these areas.

The laminate rim shown in Figure 4.3 is strongly reinforced in the hoop direction with a 2:1 ratio of hoop to $\pm 15^\circ$ fibers in the ID of the rim and 1:1 ratio at the OD. To prevent possible shear failure on a $45^\circ$ plane from the horizontal plane, $\pm 15^\circ$ fiber reinforcement of 50% was maintained and the rim outer corner was rounded to a radius of .25 inches. The hoop flexural stiffness of this composite laminate rim is 1.72 times that of the aluminum rim at the outer edge as shown by the calculation of Appendix 2. This reduces the change in diameter of the rim by the same factor and will more effectively transmit the bearing load into the wheel disc. This load is transmitted through shear at the rim/disc interface, and, if transmitted uniformly, would result in a shear stress of 470 psi. The actual gradient of interlaminar shear stress from the contact point along the wheel disc should be established by subscale test.
LVTP7 COMPOSITE ROADWHEEL
LAMINATE DESIGN

T-300 laminates

\[ [15/45/-45/-15] \]

\[ [15/-15] \]

Note: Average angles from radial direction

Titanium sleeve .10 wall
.431 long bonded into
graphite laminate hole

.050 woven glass or kevlar fabric

RIM LAMINATES
Uniform gradient from \([15/-15]\) at
corner to the following laminates
at the edge of the rim:

\[ [H_2/15/H_2/-15] \]

H: Hoop Fibers
15: 15 degree angle is
from longitudinal
axis of wheel
The disc laminate is primarily a ± 15° to the mid-radial angle ply with a core of [15/45/-45/15]. The core is required for bearing strength around the holes while the ± 15° cross ply supports the radial tension, compression and flexure stresses. From reference 3, Figure 2.4.2-26 and Figure 4.4, a conservative value of the ultimate bearing stress for this laminate is 50 ksi for a single lap, bolted - only joint. This is confirmed by bearing test results at FMI on an eight harness satin cross ply laminate. Unclamped pin bearing resulted in bearing stresses of 48.5 ksi in the fill and 62.1 ksi in the warp direction. The margin of safety of 1.25 results in a 40 ksi bearing strength allowable. At this level, each hole should be capable of supporting 15,000 lbs. in clamped bearing.

GEOMETRIC PARAMETERS NEAR A HOLE

Figure 4.4

D = .87 in.
E = 1.06 in.
e/D = 1.25 in.
D/t = .87/.431 = 2.02

An important parameter in the bolt hole area of the wheel is the maximum in-plane strain which may be expected. To estimate its value, a force of 7500 lbs. is assumed to
be distributed uniformly along the length of the diameter - .87 inches. The strain in a symmetric laminate is given by (Reference 1):

\[
\begin{align*}
\varepsilon_1 &= a_{11} N_1 + a_{12} N_2 + a_{16} N_6 \\
\varepsilon_2 &= a_{21} N_1 + a_{22} N_2 + a_{26} N_6 \\
\varepsilon_6 &= a_{61} N_1 + a_{62} N_2 + a_{66} N_6
\end{align*}
\]

where: \( \varepsilon_{1,2,6} \) = components of rotated longitudinal, transverse, and shear strain.

\( a_{ij} \) = laminate compliance components

\( N_i \) = stress resultants; average stress multiplied by laminate thickness.

When \( N_1 = 8620 \) lbs./in. and assuming it to be the major contributor to strain in the \( l \) direction, that strain becomes:

\[
\varepsilon_1 = a_{11} N_1 = (8620 \text{ lbs./in.}) \times (1.642 \times 10^{-7} \text{ in./lb.})
\]

\[
\varepsilon_1 = .0014
\]

where \( a_{11} \) is taken from Table 4.1.

Another component of strain in the disc is due to bending of the disc out of its original plane. The maximum bending moment per unit width of laminate was estimated in two ways. First, the maximum radial stress of a circular plate twisted from a central hole (Figure 4.5) is calculated in section 2. This model gives a conservative answer which is desired at this stage of design.
BENDING OF A DISC WITH A CENTRAL HOLE

FIGURE 4.5

\[ \sigma_r = \frac{\beta M}{at^2} \]

b/a = 0.426
\[ \beta = 2.062 \]
M = 42600 in.-lbs. from the 15,000 lb. loading boundary condition
\[ t = 0.431 \text{ in.} \]

\[ \sigma_r = \frac{(2.062)(42600)}{(11.75)(0.431)^2} \]

\[ \sigma_r = 40244 \text{ psi} \]

The moment per unit width caused by the stress gradient through the thickness would be from the flexure formula,

\[ \sigma_r = \frac{Mv}{I} \]

\[ M = \frac{\sigma_r I}{Y} = \frac{(40244)(1)(0.431)^3}{12} \]

M = 1248 in.-lbs./in.
Secondly, if it is assumed that the moment is evenly distributed along a chord line of the disc passing horizontally through the center of the lowest bolt hole, the resulting moment distribution becomes 42,600 in.-lbs./22 in. = 1,936 in.-lbs./in.

To obtain the strain due to this moment, the curvature must first be found. The moment-curvature relation for a symmetric laminate is given by,

\[ k_1 = d_{11} M_1 + d_{12} M_2 + d_{16} M_6 \]
\[ k_2 = d_{21} M_1 + d_{22} M_2 + d_{26} M_6 \]
\[ k_6 = d_{61} M_1 + d_{62} M_2 = d_{66} M_6 \]

where: \( k_1 \) = laminate curvature,
\( M_1 \) = bending moment per unit laminate depth,
\( d_{ij} \) = components of flexural compliance of a symmetric laminate

We assume that the primary bending moment \( M_1 \) is large compared to its transverse counterpart \( M_2 \) and the twisting moment \( M_6 \). Then;

\[ k_1 = d_{11} M_1 \]
\[ k_1 = [9.14 \times 10^{-6} (\text{lb.}-\text{in.})^{-1}] \times [1936 \text{ in.}-\text{lbs./in.}] \]
\[ k_1 = .0177 \text{ in}^{-1} \]
\[ \varepsilon_{lb} = k_1 (1/2 \text{ laminate thickness}) \]
\[ \varepsilon_{lb} = (.077 \text{ in}^{-1}) (.215 \text{ in.}) \]
\[ \varepsilon_{lb} = .0038 \]
The assumptions made to arrive at this strain were conservative in that the entire bending moment was assumed to have been absorbed by the wheel disc neglecting the contribution of the rim. The actual bending moment in the disc laminate will decrease from the center outward along the chord line since the flexural rigidity varies with angle as shown by the values for $d_{\gamma}$ in Table 4.1.

Adding the in-plane and bending strains yields

$$\epsilon_{total} = \epsilon_{1} + \epsilon_{lb} = .0014 + .0038 = .0052$$

which is still within the .006 'guideline.

4.2 M113A1 Composite Roadwheel Design

4.2.1 Design Considerations

The baseline composite design for this roadwheel shown in Figure 4.6 is similar to the LVTP7 wheel. It incorporates a laminate for the disc portions and a rim with preferential reinforcement in the hoop direction. Again, the worst loading case for this wheel is the maximum vertical load of 4,525 lbs. and the design is based on this load condition. The dimensioned drawing #740-0009 for this wheel is again found in Appendix 3.

Since the stresses in this roadwheel are not as high as for the LVTP7 wheel, a uniform laminate [15/45/-45/-15] was chosen for the entire disc area. The 15 and 45° angles are nominal angles at the mid radius of the wheel. As this laminate turns the corner into the rim it becomes mixed with layers in the hoop direction until, at the outer portion of the rim, there are two hoop layers for every layer from the disc laminate. This again is to reduce hoop deformation which prevents high interlaminar shear stresses at the loading point by distributing the load more evenly at the disc/rim interface. The high hoop fiber volume was maintained even at the contact surface unlike the LVTP7 wheel. This is due to the lower contact load and large radius of curvature at the rim outer corner. The thickness of the structural disc laminate is maintained at .31 in. to retain bending stiffness. It will be shown in the following analysis that a .21 in. thick laminate with a .050 abrasion covering on each side was not acceptable from a disc bending standpoint. The structural material chosen for this wheel is again a high strength graphite/epoxy with an impact abrasion covering of Kevlar or glass/epoxy.
**COMPOUNENTS OF IN-PLANE AND FLEXURAL STIFFNESS FOR LAMINATE IN THE BOLT HOLE AREA OF THE LVTP7 WHEEL**

**Table 4.1**

<table>
<thead>
<tr>
<th>γ(deg)</th>
<th>0</th>
<th>15</th>
<th>30</th>
<th>45</th>
<th>60</th>
</tr>
</thead>
<tbody>
<tr>
<td>A_{11}</td>
<td>lb/in</td>
<td>6.846 E+06</td>
<td>6.289 E+06</td>
<td>5.077 E+06</td>
<td>3.641 E+06</td>
</tr>
<tr>
<td>A_{22}</td>
<td>1.293 E+06</td>
<td>1.612 E+06</td>
<td>2.529 E+06</td>
<td>3.905 E+06</td>
<td>5.394 E+06</td>
</tr>
<tr>
<td>A_{12}</td>
<td>9.817 E+05</td>
<td>1.100 E+06</td>
<td>1.248 E+06</td>
<td>1.278 E+06</td>
<td>1.159 E+06</td>
</tr>
<tr>
<td>A_{66}</td>
<td>1.248 E+06</td>
<td>1.366 E+06</td>
<td>1.514 E+06</td>
<td>1.544 E+06</td>
<td>1.425 E+06</td>
</tr>
<tr>
<td>A_{16}</td>
<td>-1.173 E+05</td>
<td>-9.051 E+05</td>
<td>-1.338 E+06</td>
<td>-1.337 E+06</td>
<td>-1.015 E+06</td>
</tr>
<tr>
<td>A_{26}</td>
<td>-1.462 E+04</td>
<td>-5.972 E+05</td>
<td>-1.133 E+06</td>
<td>-1.439 E+06</td>
<td>-1.323 E+06</td>
</tr>
</tbody>
</table>

| \( a_{11} \) in/lb | 1.642 E-07 | 1.879 E-07 | 2.592 E-07 | 4.027 E-07 | 6.043 E-07 |
| \( a_{22} \) | 8.679 E-07 | 7.911 E-07 | 6.003 E-07 | 3.903 E-07 | 2.417 E-07 |
| \( a_{12} \) | -1.245 E-07 | -9.796 E-08 | -3.819 E-08 | -4.947 E-09 | -3.148 E-08 |
| \( a_{66} \) | 8.029 E-07 | 9.090 E-07 | 1.148 E-06 | 1.281 E-06 | 1.175 E-06 |
| \( a_{16} \) | 1.397 E-08 | 8.167 E-08 | 2.004 E-07 | 3.441 E-07 | 4.013 E-07 |
| \( a_{26} \) | -1.528 E-09 | 2.810 E-07 | 4.512 E-07 | 3.596 E-07 | 2.020 E-07 |

| D_{11} \( \text{lb-in} \) | 1.196 E+05 | 1.062 E+05 | 7.926 E+04 | 5.032 E+04 | 2.852 E+04 |
| D_{22} | 1.348 E+04 | 1.853 E+04 | 3.348 E+04 | 5.872 E+04 | 8.885 E+04 |
| D_{12} | 1.143 E+04 | 1.559 E+04 | 2.160 E+04 | 2.345 E+04 | 1.929 E+04 |
| D_{66} | 1.554 E+04 | 1.970 E+04 | 2.571 E+04 | 2.755 E+04 | 3.339 E+04 |
| D_{16} | -3.436 E+03 | -2.096 E+04 | -2.856 E+04 | -2.519 E+04 | -1.605 E+04 |
| D_{26} | -7.626 E+02 | -9.209 E+03 | -1.949 E+04 | -2.786 E+04 | -2.780 E+04 |

| d_{11} \( \text{lb-in}^{-1} \) | 9.140 E-06 | 1.226 E-05 | 2.104 E-05 | 3.682 E-05 | 5.713 E-05 |
| d_{22} | 8.077 E-05 | 7.234 E-05 | 5.346 E-05 | 3.290 E-05 | 1.792 E-05 |
| d_{12} | -7.655 E-06 | -4.996 E-06 | 5.108 E-08 | 2.439 E-06 | -2.200 E-07 |
| d_{16} | 1.646 E-06 | 1.071 E-05 | 2.341 E-05 | 3.613 E-05 | 3.894 E-05 |
| d_{26} | 2.272 E-06 | 2.850 E-05 | 4.058 E-05 | 3.550 E-05 | 2.114 E-05 |

[D_{ij}] and [d_{ij}] denote flexural stiffness and compliance.

[A_{ij}] and [a_{ij}] denote in-plane stiffness and compliance.
COMPONENTS OF IN-PLANE 
AND FLEXURAL STIFFNESS FOR LAMINATE 
at outer radius of wheel disc 
TABLE 4.2

<table>
<thead>
<tr>
<th>γ(deg)</th>
<th>0</th>
<th>15</th>
<th>30</th>
<th>45</th>
<th>60</th>
</tr>
</thead>
<tbody>
<tr>
<td>A&lt;sub&gt;11&lt;/sub&gt;</td>
<td>lb/in</td>
<td>7.415 E+06</td>
<td>6.839 E+06</td>
<td>5.372 E+06</td>
<td>3.625 E+06</td>
</tr>
<tr>
<td>A&lt;sub&gt;22&lt;/sub&gt;</td>
<td></td>
<td>1.020 E+06</td>
<td>1.300 E+06</td>
<td>2.174 E+06</td>
<td>3.625 E+06</td>
</tr>
<tr>
<td>A&lt;sub&gt;66&lt;/sub&gt;</td>
<td></td>
<td>8.336 E+06</td>
<td>9.817 E+05</td>
<td>1.278 E+06</td>
<td>1.426 E+06</td>
</tr>
<tr>
<td>A&lt;sub&gt;16&lt;/sub&gt;</td>
<td></td>
<td>1.099 E+06</td>
<td>1.248 E+06</td>
<td>1.544 E+06</td>
<td>1.692 E+06</td>
</tr>
<tr>
<td>A&lt;sub&gt;26&lt;/sub&gt;</td>
<td></td>
<td>0.0</td>
<td>-1.056 E+06</td>
<td>-1.641 E+06</td>
<td>-1.599 E+06</td>
</tr>
</tbody>
</table>

| a<sub>11</sub> | in/lb | 1.485 E-07 | 1.758 E-07 | 2.761 E-07 | 4.738 E-07 | 7.418 E-07 |
| a<sub>22</sub> | | 1.080 E-06 | 9.825 E-07 | 7.418 E-07 | 4.738 E-07 | 2.761 E-07 |
| a<sub>12</sub> | | -1.214 E-07 | -8.630 E-08 | 1.608 E-08 | 1.902 E-08 | -1.608 E-08 |
| a<sub>66</sub> | | 9.096 E-07 | 1.050 E-06 | 1.331 E-06 | 1.471 E-06 | 1.331 E-06 |
| a<sub>16</sub> | | 0.0 | 1.113 E-07 | 2.817 E-07 | 4.657 E-07 | 5.250 E-07 |
| a<sub>26</sub> | | 0.0 | 3.545 E-07 | 5.250 E-07 | 4.657 E-07 | 2.817 E-07 |

| D<sub>11</sub> | lb-in | 1.241 E+05 | 1.154 E+05 | 8.858 E+04 | 5.617 E+04 | 3.025 E+04 |
| D<sub>22</sub> | | 1.150 E+04 | 1.496 E+04 | 2.723 E+04 | 5.035 E+04 | 8.151 E+04 |
| D<sub>12</sub> | | 1.017 E+04 | 1.279 E+04 | 2.007 E+04 | 2.472 E+04 | 2.209 E+04 |
| D<sub>66</sub> | | 1.427 E+04 | 1.689 E+04 | 2.417 E+04 | 2.882 E+04 | 2.620 E+04 |
| D<sub>16</sub> | | 2.625 E+03 | -1.853 E-04 | -3.054 E+04 | -2.932 E+04 | -1.939 E+04 |
| D<sub>26</sub> | | 2.856 E+02 | -7.101 E+03 | -1.677 E+04 | -2.698 E+04 | -3.082 E+04 |

| d<sub>11</sub> (lb-in)<sup>-1</sup> | E-06 | 8.716 E-06 | 1.075 E-05 | 2.003 E-05 | 3.841 E-05 | 6.298 E-05 |
| d<sub>22</sub> | | 9.375 E-05 | 8.535 E-05 | 6.421 E-05 | 4.033 E-05 | 2.212 E-05 |
| d<sub>12</sub> | | -7.670 E-06 | -4.491 E-06 | 1.441 E-06 | 4.194 E-06 | 1.015 E-06 |
| d<sub>16</sub> | | 7.035 E-05 | 8.307 E-05 | 1.068 E-04 | 1.178 E-04 | 1.051 E-04 |
| d<sub>26</sub> | | -1.450 E-06 | 9.909 E-06 | 2.631 E-05 | 4.301 E-05 | 4.782 E-05 |

Diagram showing laminate orientation.
FIGURE 4.6

Titanium sleeve .10 in. wall
.31 in. long bonded into
graphite laminate hole

Increasing proportion
of hoop fibers from
disc toward edge of
rim to a maximum of
\([15/45/-45/-15]_n\)

Graphite epoxy
laminate

Note: Average
angles from radial
direction

Wear ring
bonded to
laminate

Rubber tire

M113A1 COMPOSITE ROADWHEEL
LAMINATE DESIGN
4.2.2 Analysis of Critical Areas

Rim  The hoop flexural rigidity of the composite rim was compared to that of the aluminum rim by approximating the outer rim of the composite wheel by a set of rings with rectangular cross sections. The hoop flexural rigidity of the outer .75 in. of the aluminum rim was calculated previously as

\[ EI_{0.75al} = 1.25 \times 10^6 \text{ lb-in}^2 \]

while the entire aluminum rim including the transition to the disc was

\[ EI_{2.91al} = 2.22 \times 10^6 \text{ lb-in}^2 \]

The 2:1 hoop laminate chosen has about twice the flexural rigidity in the hoop direction as an equivalent aluminum ring. The equivalent EI of the composite rim was found by calculation of the [D] matrix for the cross-sections of each of two rings .375 in. wide. The flexural rigidity of the outer .75 in. of the composite rim was found to be

\[ EI_{0.75gr} = 5.72 \times 10^6 \text{ lb-in}^2 \]

This value assumes that the hoop bending moment is the major contributor to change in hoop curvature. This value is more than twice the rigidity for the full width aluminum rim.

The maximum strain in the hoop direction resulting from rim flexure was found using the maximum moment \( M_1 = 12111 \text{ in.-lbs} \), calculated in section 2 for the full width of the roadwheel. Assuming the entire moment is supported by the outer .75 in. of the composite rim we have for the curvature from the inverse of equation \( k_1 = d_{11}^{-1} M_1 \),

\[ M_1 = D_{11}k \quad (3.6) \]

\[ k_1 = (12111 \text{ in-lbs/in})/(7.621 \times 10^6 \text{ in-lbs}) \]

\[ k_1 = .00159 \text{ in}^{-1} \]
To get the strain $\varepsilon_H$, the curvature is multiplied by the distance from the neutral axis to the outer fiber which for this case is taken as .61 in. from the previous calculation of flexural stiffness.

$$\varepsilon_H = (.61 \text{ in.}) (0.00159 \text{ in}^{-1})$$

$$\varepsilon_H = .00097$$

This strain level is well within the boundary of .006.

Holes

The bearing stress at the holes assuming all the load of 4,525 lbs is supported at one hole is

$$\sigma_b = \frac{(4,525 \text{ lbs})}{(.7 \text{ in}) (.31) \text{ in}} = 20,852 \text{ psi}$$

Even this condition is well within the clamped bearing capability of the disc laminate (referring again to reference 3 Figure 2.4.2-26).

The maximum in-plane strain near a hole is estimated by assuming all the load is taken by one hole and uniformly distributed across its diameter of .7 in.

$$\varepsilon_1 \text{ disc} = a_{11} N_1$$

where $a_{11} = 3.081 \times 10^{-7} \text{ in/lb}$ from Table 4.3

$$N_1 = 6,464 \text{ lbs/in}$$

$$\varepsilon_1 \text{ disc} = .002$$

Bending of the Disc. As before $\sigma = \frac{8M}{(at^2)}$ will be used to estimate the maximum local bending moment within the disc.

$$\sigma_r = \frac{8M}{at^2}$$

$$M = (4,525 \text{ lbs}) (.66 + \frac{2.91}{2} \text{ in})$$

$$M = 9,570 \text{ in-lbs}$$
COMPONENTS OF IN-PLANE AND FLEXURAL STIFFNESS
FOR THE LAMINATE IN THE DISC AREA OF THE
M113A1 ROADWHEEL

TABLE 4.3

<table>
<thead>
<tr>
<th>$\gamma (\text{deg})$</th>
<th>0</th>
<th>15</th>
<th>30</th>
<th>45</th>
<th>60</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_{11}$</td>
<td>3.970 E+06</td>
<td>3.879 E+06</td>
<td>3.568 E+06</td>
<td>2.995 E+06</td>
<td>2.252 E+06</td>
</tr>
<tr>
<td>$A_{22}$</td>
<td>1.337 E+06</td>
<td>1.599 E+06</td>
<td>2.252 E+06</td>
<td>2.995 E+06</td>
<td>3.568 E+06</td>
</tr>
<tr>
<td>$A_{12}$</td>
<td>9.845 E+05</td>
<td>8.992 E+05</td>
<td>7.285 E+05</td>
<td>6.431 E+05</td>
<td>7.285 E+05</td>
</tr>
<tr>
<td>$A_{16}$</td>
<td>1.176 E+06</td>
<td>1.091 E+05</td>
<td>9.199 E+05</td>
<td>8.346 E+05</td>
<td>9.199 E+05</td>
</tr>
<tr>
<td>$A_{26}$</td>
<td>0.0</td>
<td>-1.812 E+05</td>
<td>-4.221 E+05</td>
<td>-6.581 E+05</td>
<td>-7.178 E+05</td>
</tr>
</tbody>
</table>

| $b_{11}$            | 3.081 E-07  | 2.971 E-07  | 3.049 E-07  | 4.049 E-07  | 6.081 E-07  |
| $b_{22}$            | 9.146 E-07  | 8.224 E-07  | 6.081 E-07  | 4.049 E-07  | 3.049 E-07  |
| $b_{12}$            | -2.268 E-07 | -1.752 E-07 | -7.193 E-08 | -2.030 E-08 | -7.193 E-08 |
| $b_{16}$            | 8.503 E-07  | 1.057 E-06  | 1.470 E-06  | 1.676 E-06  | 1.470 E-06  |
| $b_{26}$            | 0.0          | -2.724 E-08 | 8.376 E-08  | 3.032 E-07  | 4.415 E-07  |

| $C_{11}$            | 3.197 E+04  | 2.919 E+04  | 2.557 E+04  | 2.109 E+04  | 1.605 E+04  |
| $C_{22}$            | 1.064 E+04  | 1.357 E+04  | 1.984 E+04  | 2.680 E+04  | 3.166 E+04  |
| $C_{12}$            | 7.837 E+03  | 7.755 E+03  | 6.435 E+03  | 5.199 E+03  | 5.282 E+03  |
| $C_{16}$            | 9.371 E+03  | 9.288 E+03  | 7.969 E+03  | 6.732 E+03  | 6.815 E+03  |
| $C_{26}$            | -2.093 E+03 | -3.092 E+03 | -3.855 E+03 | -4.667 E+03 | -4.714 E+03 |

| $D_{11}$            | 3.855 E-05  | 4.041 E-05  | 4.348 E-05  | 5.617 E-05  | 8.021 E-05  |
| $D_{22}$            | 1.148 E-04  | 1.018 E-04  | 7.347 E-05  | 4.676 E-05  | 3.392 E-05  |
| $D_{16}$            | 1.084 E-04  | 1.308 E-04  | 1.812 E-04  | 2.093 E-04  | 1.869 E-04  |
| $D_{26}$            | 6.340 E-06  | 2.118 E-06  | 1.272 E-05  | 3.651 E-05  | 5.171 E-05  |

<table>
<thead>
<tr>
<th>$[15/45/-45/-15]_{16s}$</th>
<th>32 layers total</th>
</tr>
</thead>
<tbody>
<tr>
<td>symmetric graphite/epoxy laminate</td>
<td>.31 in. thick</td>
</tr>
</tbody>
</table>
\[ a = 10.97 \text{ in.} \]
\[ b = 2.63 \text{ in.} \]
\[ t = .31 \text{ in.} \]

for \( b/a = 2.39 \) \( \beta = 3.8 \)

\[ \sigma_x = 34,495 \text{ psi} = \frac{M_{\text{local}}}{I} \]

\[ M_{\text{local}} = \frac{(1)(.31)^3}{(12)(.155)}(34,495) \frac{\text{in-lbs}}{\text{in}} \]

\[ M_{\text{local}} = 552 \text{ in-lbs/in} \]

The alternate approach of assuming that the entire imposed bending moment is supported along a chord line passing through the bolt hole closest to the ground yields.

\[ M_{\text{local}} = \frac{9,570 \text{ in-lbs}}{11 \text{ in}} = 870 \text{ in-lbs/in} \]

Using this larger value to determine strain due to bending

\[ k_1 = \frac{M_{\text{local}}}{D_{11}} \]

\[ k_1 = \frac{870 \text{ in-lbs/in}}{3.197 \times 10^4 \text{ in-lb}} \]

\[ k_1 = .0272 \text{ in}^{-1} \]

\[ \epsilon_{\text{bend}} = (.155)(.0272) = .0042 \]

If a laminate thickness of .21 in. were used

\[ D_{11} = 1.038 \times 10^4 \text{ in-lbs} \]

and the distance from the neutral axis to the laminate outer fiber would be .105 in.

The maximum strain would then be

\[ \epsilon_{\text{bend}} .21 = (.105 \text{ in.})(\frac{870 \text{ in-lbs/in}}{1.038 \times 10^4 \text{ in-lbs}}) = .0088 \]

This value is higher than the .006 allowable so the thinner laminate cannot be used given the assumptions made.
4.3 Additional Design Concepts

Two other design approaches are presented to show that a variation in geometry with application of a lightweight core material may allow more efficient load introduction into the composite structure. In design with structural composite materials, introducing the load into the laminates or 3D structures is usually the biggest problem. In this case the vertical load is imposed along a narrow band at the high pressure contact area of the rim with the rubber tire. In the previous designs this vertical load was supported by a stiff rim which transmitted the vertical load to the disc through shear at the corner of the disc/rim interface. The distribution of this shear stress from the point of load application along the rim is best determined through prototype testing. The two alternate designs -- the Laminated Cone Concept of Figure 4.7 and the Double Walled Core Concept of Figure 4.8 -- are attempts to introduce the compressive loading directly into the disc of the wheel. This eliminates a potentially high interlaminar shear stress at the corner of the wheel.

The laminated cone concept is shown for the M113Al roadwheel in Figure 4.7. Its structure is a stack of four (or perhaps more) laminates on the order of .10 in. thick. In the bolt hole area, they are bonded together to form a thick laminate but separate and flare out to form four separate discs at the OD of the wheel. To prevent buckling of the separated laminates and also transmit shear loading from one laminate to the other, the spaces between laminates are filled with a lightweight core material such as Rohacell foam. Typical properties of this foam core are given in Table 4.4. The laminates are built up slightly at the edges to provide a wider bearing surface. Assuming each carries a nominal 1,000 lb. compressive load distributed over a .20 x .25 surface, the resulting stress would be 20 ksi -- a feasible level for the [±15 ±45] laminate. Since transmitting the bearing loads into the laminate discs through shear would be difficult for the foam core or rubber, an overwrapped rim is added. This can be a [0, ±45] laminate with the 0° direction parallel to the wheel axis to support bending between the disc laminate bearing points.

One possible disadvantage of this concept is that the direct bearing load introduction reduces the global compliance of the wheel as a whole. Depending on fiber orientations within the lamina, it can become very stiff causing problems in a shock loading environment.
LAMINATED CONE CONCEPT
Figure 4.7

Graphite/Epoxy Laminates

Light Weight Core

Overwrapped Rim
DOUBLE WALL ED CORE

DESIGN CONCEPT

FIGURE 4.8
Typical Mechanical Properties of Rohacell® Foam Core

Table 4.4

Density 7 lb/ft$^3$
Max. tensile stress 525 psi
Max. flexural stress 738 psi
Max. compressive stress 511 psi
Max. shear stress 341 psi
Young's Modulus 25,560 psi
Shear Modulus 7,100 psi
Max. strain to failure 3%

The second alternate concept, the double walled core, involves the features of both the pure laminated and laminated cone concepts. The core is again required to prevent buckling of the laminated skins whose thickness would be typically half the thickness of the laminate in the bolt hole area. The interlaminar shear distribution in the contact area is again an area of concern and is best resolved by subscale or prototype testing. From a design point-of-view, this concept has the potential advantages of slightly higher overall compliance and possibly lower shear stresses at the corners depending on the interaction between the core and the covering laminates. In both this and the laminated cone concept, the wheel's bending rigidly about a horizontal axis through the wheel center is increased over the pure laminated design.

Table 4.5 gives a comparison of the weights for the existing wheels and estimated weights for the composite wheels. It shows a weight savings of 17 lbs or 27% for the LVTP7 wheel. The laminate design for the M113A1 wheel saves 5 lbs over the aluminum wheel while the laminated cone design for this wheel saves 10 lbs or 28%. The difference is due to a more efficient use of the structural material in the laminated cone design.

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WEIGHT COMPARISONS

TABLE 4.5

<table>
<thead>
<tr>
<th>LVTP7 Existing Wheel</th>
<th>wt. (lbs.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aluminum Wheel</td>
<td>38.63</td>
</tr>
<tr>
<td>Wear Ring</td>
<td>8.23</td>
</tr>
<tr>
<td>Rubber Tire</td>
<td>15.14</td>
</tr>
<tr>
<td></td>
<td>62.00 lbs.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>LVTP7 Laminate Design Composite</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Graphite/Epoxy Structure</td>
<td>19.18</td>
<td></td>
</tr>
<tr>
<td>Glass Cover</td>
<td>3.00</td>
<td></td>
</tr>
<tr>
<td>Wear Ring</td>
<td>8.23</td>
<td></td>
</tr>
<tr>
<td>Rubber Tire</td>
<td>15.14</td>
<td></td>
</tr>
<tr>
<td></td>
<td>45.55 lbs.</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>M113A1 Existing Wheel</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Aluminum Wheel</td>
<td>22.35</td>
<td></td>
</tr>
<tr>
<td>Wear Ring</td>
<td>6.13</td>
<td></td>
</tr>
<tr>
<td>Rubber Tire</td>
<td>7.52</td>
<td></td>
</tr>
<tr>
<td></td>
<td>36.00 lbs.</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>M113A1 Laminate Design</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Graphite/Epoxy Structure</td>
<td>15.25</td>
<td></td>
</tr>
<tr>
<td>Glass Cover</td>
<td>3.00 (approximate)</td>
<td></td>
</tr>
<tr>
<td>Rubber Tire</td>
<td>7.52</td>
<td></td>
</tr>
<tr>
<td>Wear Ring</td>
<td>6.12</td>
<td></td>
</tr>
<tr>
<td></td>
<td>31.89 lbs.</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>M113A1 Laminated Cone Concept (w/.10 in. rim)</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Graphite/Epoxy Structure</td>
<td>8.15</td>
<td></td>
</tr>
<tr>
<td>Rohacell Foam</td>
<td>2.10</td>
<td></td>
</tr>
<tr>
<td>Wear Ring</td>
<td>6.12</td>
<td></td>
</tr>
<tr>
<td>Rubber Tire</td>
<td>7.52</td>
<td></td>
</tr>
<tr>
<td></td>
<td>23.89 lbs.</td>
<td></td>
</tr>
</tbody>
</table>
5.0 Manufacturing Analysis

5.1 Fabrication Concepts

A review was conducted of the available fabrication concepts that might be used to produce a fiber reinforced composite roadwheel. Each concept was examined relative to the advantages and disadvantages in general and to the suitability for the design concept presented in section 4.0.

(a) Injection Molding

Advantages
- very low labor cost
- good part consistency
- good toughness properties
- intricate shape capabilities

Disadvantages
- poor thermal properties
- low physical strength of materials
- difficult to control fiber orientation caused by resin flow
- tooling costs

Conclusion
The method is not acceptable due to poor environmental properties, low stress allowable around bolt holes, and poor shear stress capabilities.

(b) Resin Transfer Molding (RTM)

Advantages
- lower material cost that prepeg
- two finished surfaces
- low cost tooling

Disadvantages
- resin systems have moderate shear strength
- physicals are limited by moderate fiber volume

Conclusion
The method is not acceptable for this application due to poor physicals resulting from the moderate fiber volume and from the poor properties of the low viscosity resins.
(c) Press Molding

Advantages
- more economical than autoclave molding for large volume
- two finished surfaces
- high fiber volume
- allows high quality resins to be used

Disadvantages
- shape is limited due to the requirements for positive draft for the molds
- the mold surface should be as near to perpendicular to the ram stroke as possible
- the long cure cycle of the high quality epoxy resins will limit output to about one part every two hours

Conclusion
The advantages relative to autoclave molding do not appear to warrant the required expenses for the tools and the large number of presses

(d) Autoclave Molding

Advantages
- very good part quality
- economical tooling
- high fiber volume
- allows high quality resins to be used

Disadvantages
- one finished surface
- some increased labor due to vacuum bagging
- material costs tend to be high

Conclusion
The method meets the requirements for the part quality both in terms of resin quality and fiber volume

(e) Filament Winding

Advantages
- lowest cost for materials
- lowest labor cost

Disadvantages
- fiber orientation has limitations
- fiber placement has limitations
Conclusion  Filament winding is not suitable due to the inability to achieve control over both the fiber orientation and wall thickness on the disc face.

5.2 Selected Fabrication Method

Only two of the five fabrication methods for the AMMRC Composite Roadwheel application were deemed practical. Injection molding and transfer molding are unsuitable because of their insufficient physical properties as a result of the lower fiber content necessary to apply these processing methods.

Press molding and autoclave molding were the two options that allowed for very high fiber content with resultant higher physical properties. Both methods however, involve higher quality and therefore higher priced prepeg. Autoclave molding is the most practical method of the two. Press molding offers no significant benefits over autoclave molding other than a part with finished surfaces on both sides.

Autoclave molding requires far less tooling costs than press molding. The extra time required to apply a vacuum bag would be about 1/2 hour resulting in extra labor costs of roughly $5. Against this cost increase of approximately 1/2 of 1 percent, the autoclave process has the further benefit of being more easily adapted to variations in production rate due to the capability of curing several wheels at one time.

5.2.1 Process Description

The fabrication process that would be used for the design concept shown in Figure 4.3 is based on using unidirectional prepeg for material to be placed on ±15 degree angles or for the hoop wraps on the rim. The ±45 degree material would be made from balanced weave (5H) prepeg pattern cut on the bias. Placement of the prepeg on the male mold will require that the material be cut in pie-shaped sections with a maximum of about four inches. This is necessary in order to form the material over the rim of the wheel as it is a 3-D curve and the prepeg is a 2-D material. Approximately 2000 pieces will be required for each wheel. The hoop wrap material on the rim would be applied as a continuous tape by winding it on the mold. Application of vacuum bags, bleeders and curing cycles would be in accordance with current practice.

The male molds would be constructed composites and would be made in several pieces to allow for part molding with negative draft.
5.3 Cost Analyses

Estimates were made for the tooling and manufacturing costs for 30 and 24,000 unit quantities (20,000 for the M113A1). The estimates were based on production during a one-shift day with 250 production days.

5.3.1 LVTP7 Estimates

Estimates for both LVTP7 and the M113A1 were based on similar production methods and materials.

**LVTP7 Estimate**

<table>
<thead>
<tr>
<th>Item</th>
<th>30 Units</th>
<th>24,000 Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tooling Master</td>
<td>8,900</td>
<td>8,900</td>
</tr>
<tr>
<td>Glass/Epoxy Molds (one)</td>
<td>3,100</td>
<td>-</td>
</tr>
<tr>
<td>Glass/Epoxy Molds (100)</td>
<td>-</td>
<td>168,000</td>
</tr>
<tr>
<td>Engineering</td>
<td>29,000</td>
<td>40,000</td>
</tr>
<tr>
<td>C/Ep Prepreg (26.7#ea.)</td>
<td>29,790</td>
<td>23,830,000</td>
</tr>
<tr>
<td>Glass/Epoxy Prepreg (7.1#ea.)</td>
<td>4,560</td>
<td>3,648,000</td>
</tr>
<tr>
<td>Production Labor (20 hrs./pc)</td>
<td>12,000</td>
<td>-</td>
</tr>
<tr>
<td>(13.4 hrs./pc)</td>
<td>-</td>
<td>6,432,000</td>
</tr>
<tr>
<td><strong>Total Costs</strong></td>
<td>$87,350</td>
<td>$34,126,900</td>
</tr>
<tr>
<td><strong>Cost/Wheel</strong></td>
<td>$2,912</td>
<td>$1,422</td>
</tr>
</tbody>
</table>

**M113A1 Estimate**

<table>
<thead>
<tr>
<th>Item</th>
<th>30 Units</th>
<th>20,000 Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tooling Master</td>
<td>8,900</td>
<td>8,900</td>
</tr>
<tr>
<td>Glass/Epoxy Molds (one)</td>
<td>3,100</td>
<td>-</td>
</tr>
<tr>
<td>Glass/Epoxy Molds (80)</td>
<td>-</td>
<td>143,000</td>
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<tr>
<td>Engineering</td>
<td>29,000</td>
<td>40,000</td>
</tr>
<tr>
<td>C/Ep Prepreg (23#ea.)</td>
<td>25,660</td>
<td>17,108,000</td>
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<tr>
<td>Glass/Epoxy Prepreg (4.5#ea.)</td>
<td>2,890</td>
<td>1,927,000</td>
</tr>
<tr>
<td>Production Labor (17 hrs./pc)</td>
<td>10,200</td>
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<tr>
<td>(11.2 hrs./pc)</td>
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<td>4,480,000</td>
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<tr>
<td><strong>Total Costs</strong></td>
<td>$79,750</td>
<td>$23,706,900</td>
</tr>
<tr>
<td><strong>Cost/Wheel</strong></td>
<td>$2,658</td>
<td>$1,185</td>
</tr>
</tbody>
</table>

The above cost estimates are based on the following cost factors:

- **Shop labor rate** = $20/hr.
- **Engineer rate** = $60/hr.
- **G & A on Material** = 30%
- **Fee** = 10%
- **Material Waste** = 50%
5.4 Alternative Design Concept

The four plate concept shown in Figure 4.7 was examined for possible cost savings. Due to the predominance of the effects of material cost, this concept results in an estimated cost reduction of approximately 15%.

<table>
<thead>
<tr>
<th>Tooling</th>
<th>300,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Engineering</td>
<td>55,000</td>
</tr>
<tr>
<td>Material</td>
<td>12,354,000</td>
</tr>
<tr>
<td>Labor</td>
<td>7,200,000</td>
</tr>
</tbody>
</table>

Total $19,909,000
Cost/Wheel $995 ea.

\[
\frac{1185-995}{1185} = 16\%
\]

5.5 Alternative Materials

Due to the high material costs, other resin systems were considered. Use of a 250°F curing system would reduce the prepreg cost from $26/# to about $22/# but it was not done at this time due to the task of resistance to heat. The $26/# value is on the low side for 350°F curing systems.

5.6 Materials Qualifications

The prepreg materials will be certified to the manufacturers' specifications and will be tested for tensile and shear strength per ASTM standards for carbon/epoxy laminates.
6.0 Conclusions and Recommendations

The results of this study indicate that advanced composite materials are a feasible alternate material for roadwheel construction from a performance point-of-view. That is, the objective of significant weight saving while maintaining the current level of reliability/maintainability of aluminum wheels can be met. Economical manufacture of these roadwheels, however, is doubtful. A continuous graphite fiber composite was chosen as the structural material from the necessity to meet both static structural, fatigue and weight savings goals. Manufacturing analysis showed that the wheel cost is largely material cost dependent due to the conservative analyses done in this study; there is a possibility that further cost reductions could be achieved by additional analysis or testing.

It is recommended that the demonstrator wheels be manufactured as originally planned; however, results of this design and analysis task indicate the need for limited subscale and prototype testing to verify analytical results and establish an optimum design. If promising results are obtained with the demonstrator program, a manufacturing technology program should be undertaken to reduce the single part cost for the large scale production run.
6.0 REFERENCES


APPENDIX 1

LVTP7 ROADWHEEL STRESS CONTOURS
VERTICAL LOAD CASE

MID PLANE CROSS SECTION VIEW

FIGURE A1.1

15,000 lb. LOAD UNIFORMLY DISTRIBUTED
MAXIMUM PRINCIPAL STRESS CONTOURS

MID PLANE CROSS SECTION
VERTICAL LOAD CASE

FIGURE A1.2
MAXIMUM PRINCIPAL STRESS CONTOURS

FRONT SURFACE
VERTICAL LOAD CASE

FIGURE A1.3

58
MAXIMUM PRINCIPAL STRESS CONTOURS
BACK SURFACE
VERTICAL LOAD CASE

FIGURE A1.4
MINIMUM PRINCIPAL STRESS CONTOURS

MID PLANE CROSS SECTION SURFACE
VERTICAL LOAD CASE

FIGURE A1.5
MINIMUM PRINCIPAL STRESS CONTOURS

FRONT SURFACE
VERTICAL LOAD CASE

FIGURE A1.6
61
MINIMUM PRINCIPAL STRESS CONTOURS

BACK SURFACE
VERTICAL LOAD CASE

FIGURE A1.7
LEGEND

A = +1.265E+3
B = +7.816E+3
C = +1.437E+4
D = +2.092E+4
E = +2.747E+4
F = +3.402E+4
G = +4.057E+4
H = +4.712E+4
I = +5.366E+4
J = +5.023E+4
K = 0.000E 0

VON MISÉS EQUIVALENT STRESS CONTOURS

MID PLANE CROSS SECTION SURFACE
VERTICAL LOAD CASE

FIGURE A1.8
VON MISES EQUIVALENT STRESSS CONTOURS
FRONT SURFACE
VERTICAL LOAD CASE

FIGURE A1.9
VON MISSES EQUIVALENT STRESS CONTOURS
BACK SURFACE
VERTICAL LOAD CASE

FIGURE A1.10
MAXIMUM SHEAR STRESS CONTOURS

MID PLANE CROSS SECTION SURFACE
VERTICAL LOAD CASE

FIGURE A1.11
MAXIMUM SHEAR STRESS CONTOURS
FRONT SURFACE
VERTICAL LOAD CASE

FIGURE A1.12
MAXIMUM SHEAR STRESS CONTOURS
BACK SURFACE
VERTICAL LOAD CASE

FIGURE A1.13
COMBINED VERTICAL AND SIDE LOAD CASE
MID PLANE CROSS SECTION VIEW

FIGURE A1.14

1098 LB. LOAD UNIFORMLY DISTRIBUTED ALONG WEAR RING SEAT

1901 LB. LOAD UNIFORMLY DISTRIBUTED
MAXIMUM PRINCIPAL STRESS CONTOURS

WHEEL MID PLANE CROSS SECTION SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.15
70
MAXIMUM PRINCIPAL STRESS CONTOURS

FRONT SIDE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.16
MAXIMUM PRINCIPAL STRESS CONTOURS
BACK SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.17
MINIMUM PRINCIPAL STRESS CONTOURS

WHEEL MID PLANE CROSS SECTION SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.18
MINIMUM PRINCIPAL STRESS CONTOURS

FRONT SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.19
MINIMUM PRINCIPAL STRESS CONTOURS

BACK SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.20
von Mises Equivalent Stress Contours
Wheel Mid Plane Cross Section Surface
Combined Side and Vertical Load Case

Figure A1.21
VON MISES EQUIVALENT STRESS CONTOURS

FRONT SURFACE

COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.22
VON MISES EQUIVALENT STRESSES CONTOURS

BACK SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.23
MAXIMUM SHEAR STRESS CONTOURS

WHEEL MID PLANE CROSS SECTION SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.24
MAXIMUM SHEAR STRESS CONTOURS
FRONT SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.25
MAXIMUM SHEAR STRESS CONTOURS
BACK SURFACE
COMBINED SIDE AND VERTICAL LOAD CASE

FIGURE A1.26
APPENDIX 2

CALCULATION OF FLEXURAL STIFFNESS COMPONENT
OF LVTP7 WHEEL RIM
APPENDIX 2

CALCULATION OF PRIMARY FLEXURAL MODULUS OF LAMINATE IN RIM OF LVTP7 ROADWHEEL

Figure A.2.1

The flexural stiffness of a laminate is given by Tsai and Hahn as:

\[
\begin{bmatrix}
    K_1 & K_2 & K_6 \\
    M_1 & D_{11} & D_{12} & D_{16} \\
    M_2 & D_{21} & D_{22} & D_{26} \\
    M_6 & D_{61} & D_{62} & D_{66}
\end{bmatrix}
\]  

(A.2.1)

eg. \(M_1 = D_{11}K_1 + D_{12}K_2 + D_{16}K_6\)

where \(M_i\) are the applied movements \(K_i\) as the curvatures of the laminate and \(D_{ij}\) are the components of flexural modulus which couple curvatures in all in-plane directions to applied moments. For hoop flexure of the composite wheel rim, the curvature components along the longitudinal hoop...
axis $K_2$ and in the plane of the laminate $K_6$ are small compared to $K_1$. We seek to find $D_{11}$. For a general laminate:

$$D_{ij} = \frac{h^j}{3} \sum_{t=1-n/2}^{n/2} Q_{ij} \left[ t^j - (t-1)^j \right] \quad (A.2.2)$$

where $h^j = \text{ply thickness}$

$Q_{ij} = \text{components of in-plane modulus}$

$t = \text{ordinal number of plies as they go from } 1-n/2 \text{ to } n/2$

$n = \text{total number of plies}$

$D_{11}$ will be calculated for a 16 ply laminate simulating the fractions of hoop to $\pm 15^\circ$ layers.

<table>
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<tr>
<th>PLY</th>
<th>ORIENTATION</th>
<th>$t^j - (t-1)^j$</th>
<th>$Q_{11} \times 10^6$ psi</th>
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<tr>
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Figure A.2.2
\( Q_{11} = 21 \times 10^6 \) psi for hoop layers

\( Q_{11} = 1.7 \times 10^6 \) psi for \( \pm 15 \) layers

\( h_o = .0625 \) in.

\[
D_{11} = \frac{h^3}{3} \frac{8}{5} Q_{11}^{(t)} \left[ t^3 - (t-1)^3 \right]_{t = -7}
\]

\( D_{11} = 1.164 \times 10^6 \) lb-in

The equivalent EI or flexural rigidity of the composite rim, \( bD_{11} \) where \( b = .5 \) in., an assumed rim width

\[
bD_{11} = EI|_{e_r} = .582 \times 10^6 \text{ lb-in}^2
\]

For a 1/2 inch width of the outer most portion of the aluminum rim

\[
EI_{al} = (10.6 \times 10^6) \frac{(0.5)(0.9)^3}{12}
\]

\[
EI_{al} = .339 \times 10^6 \text{ lb-in}^2
\]

The ratio of hoop flexural rigidity of the graphite/epoxy to the aluminum rim is 1.72.
APPENDIX 3

DRAWINGS OF LVTP7 AND M113A1
COMPOSITE WHEELS

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The program goal was to evaluate the feasibility and establish the design criteria for reinforced plastic roadwheels for the LVT77 and M113 1 armored personnel carriers. Additional objectives included reducing weight and lowering production costs while retaining or increasing the service life as compared to the current metal roadwheels. An analysis of the existing roadwheels was first undertaken to establish areas of high stress and deflection. The data acquired from these analyses was then used to select materials, fiber architecture and geometry of the composite roadwheels. Epoxy reinforced with carbon fibers was selected as the preferred material. A weight reduction of about 30% is predicted for the composite designs relative to the current metal wheels. Manufacturing analyses were done to establish the most suitable production techniques and the estimated costs. Autoclave molding was selected as the preferred construction method.

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