Application of Solidification Theory to Rapid Solidification Processing

W. J. Boettinger, J. W. Cahn, S. R. Coriell
J. R. Manning and R. J. Schaefer

Metallurgy Division
National Bureau of Standards
Gaithersburg, MD 20899

Defence Advanced Research Projects Agency
1400 Wilson Boulevard
Arlington, VA 22209

Approved for public release. Distribution unlimited.

Solidification theory can be used to predict and control processes occurring during rapid solidification. Two papers prepared for publication provide results showing such predictions. (1) The effects of rapid solidification velocity on microstructure and phase solubility extension in NiAl-Cr quasi-binary alloys are reported. (2) Segregation behavior and microstructural spacings in Ag-15 wt% Cu alloys are reported as a function of solidification velocity around and below the transition velocity from cellular to banded microstructures.
Application of Solidification Theory to Rapid Solidification Processing

Metallurgy Division
Center for Materials Science
National Bureau of Standards
Gaithersburg, MD 20899

Semi-Annual Technical Report
Period Covered: April 1, 1984 to September 30, 1984
Report Issued: February 1985

Prepared for
Defense Advanced Research Projects Agency
Arlington, VA 22209

Program Code No: 4D10
Effective Date of Contract: April 1, 1979
Contract Expiration Date: September 30, 1986
Principal Investigator: J. R. Manning (301/921-3354)

"The views and conclusions contained in this document are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of the Defense Advanced Research Projects Agency or the U.S. Government."
# Table of Contents

1. Task Objective
   Technical Problem and General Methodology
   Technical Results

2. Appendix - Papers Reporting Detailed Results
   The Effect of Rapid Solidification Velocity on Microstructure and Phase Solubility Extension in NiAl-Cr Quasibinary Alloys
   Cellular Microsegregation in Rapidly Solidified Ag-15 wt% Cu Alloys

---

Accession For

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>NTIS GRA&amp;I</td>
<td>Distribution/Availability Codes</td>
</tr>
<tr>
<td>DTIC TIB</td>
<td>Avail and/or Special</td>
</tr>
<tr>
<td>Unannounced</td>
<td></td>
</tr>
<tr>
<td>Justification</td>
<td></td>
</tr>
</tbody>
</table>

By

Dist

Avail

Special

A-1
Application of Solidification Theory to
Rapid Solidification Processing

This semi-annual technical report for ARPA Order 3751 covers the period
April 1, 1984 to September 30, 1984.

Task Objective

The objective of this work is to develop guidelines based on the kinetic
and thermodynamic aspects of solidification theory for prediction and control
of rapid solidification processes. In particular, segregation effects and rules
governing the formation of equilibrium and non-equilibrium phases, including
metallic glasses, will be investigated. Areas where microstructural opportunities
exist for significant improvements in alloy properties will be emphasized.

Technical Problem and General Methodology

Rapid solidification techniques make it possible to produce new types of
materials having significantly better properties than conventionally processed
materials. However, improved predictive techniques and control of rapid
solidification processes are needed. The current studies are focussed on the
science underlying areas where improved materials can be obtained in order to
provide such prediction and control. This work is both theoretical and
experimental.

Two major ways in which rapid solidification technology provides improved
materials are:

1. Production of alloys with new compositions and phases.
2. Production of improved alloy properties by control of microstructures
   and homogeneity in rapidly solidified alloys.
The general method followed in this work has been to identify critical questions in these major rapid solidification application areas where solidification theory, when properly developed and checked by experiment, can provide improved understanding of important rapid solidification processes. This understanding then is pursued to provide guidelines that can be used by alloy producers to obtain new improved materials and to select optimum alloy compositions and processing conditions for rapid solidification applications.

Technical Results

1. Production of Alloys with New Compositions or Phases -- Extended Solid Solubility

Rapid solidification, if it is sufficiently rapid, can prevent the separation of alloy constituents into equilibrium phases during solidification and allow the freezing-in of metastable phases, for example, metallic glass phases or other phases not normally found by conventional solidification. These new phases can have properties that are drastically different from the properties of the equilibrium phases. The conditions for producing such rapidly solidified alloys having compositions in two-phase regions of alloy phase diagrams are being investigated. It has been found that in some cases, such as Ag-Cu, homogeneous crystalline alloys can be produced by partitionless solidification if the solidification velocity is above a critical value, dependent on composition. In other more complex cases, such as NiAl-Cr a different crystal structure than might have been expected can be produced by rapid solidification in the two-phase region. In other cases, entirely new phases can be produced. Work in this project is continuing on new phases found in Al-Mn (and other rapidly solidified alloys) and on precipitation
processes in rapidly solidified Al-Cr alloys. It is believed that the new phases and structures being produced in these alloys may have great scientific and practical importance.

One of the major ways in which rapid solidification can be expected to lead to technological and scientific breakthroughs is by producing entirely new types of alloys that cannot be produced by conventional means. For this reason, one of the main emphases of the present work has been to investigate phenomena in the extended solid solubility regime. This composition regime is not normally accessible for investigation by conventional metallurgy and hence is a regime where new and unexpected effects and processes are more likely to be found.

In work completed during the reporting period, a paper was written on "The Effect of Rapid Solidification Velocity on Microstructure and Phase Solubility Extension in NiAl-Cr Quasihinary Eutectic" by W. J. Boettinger, D. Shechtman, T. Z. Kattamis and R. J. Schaefer. A copy of this paper is included as part of this report in the Appendix. This work was done in collaboration with D. Shechtman, Johns Hopkins University and the Technion, and T. Z. Kattamis, University of Connecticut, during times they spent at the National Bureau of Standards.

2. Production of Improved Alloy Properties by Control of Microstructures and Homogeneity in Rapidly Solidified Alloys

Even in cases where the equilibrium solid solubility is not exceeded, it is frequently possible to obtain striking improvements in alloy properties by means of rapid solidification. These improvements result from the differences in alloy microstructure and homogeneity produced by rapid solidification.
Previous work in silver-rich Ag-Cu done on this project has mapped out regions in a plot of composition vs. electron beam scan velocity (closely related to solidification velocity) where particular types of microstructures could be found. At the highest solidification velocities, microsegregation-free alloys were produced, either by creation of planar solidification interfaces or by partitionless solidification. By contrast, at the lower solidification velocities (below a scan velocity of approximately 20 cm/s, the exact value depending on composition), cellular microstructures formed with segregation of Cu to the intercellular regions.

At intermediate velocities for compositions above the equilibrium solubility limit (approximately 9 wt% Cu), a banded microstructure was found, alternating between microsegregation-free bands and cellular structured bands normal to the solidification direction. Since variations in the spacings and other features in the cellular regime can vary significantly with solidification velocity, alloys with solidification velocities around and below the transition velocity from cellular microstructure to banded were examined for Ag-15 wt% Cu alloys. Changes in segregation behavior and microstructural spacings were determined. Some results from this work were reported in a paper "Cellular Microsegregation in Rapidly Solidified Ag-15 wt% Cu Alloy" by L. A. Rendersky and W. J. Roettinger. A copy of this paper is included as part of this report in the Appendix. This work was done in collaboration with L. A. Bendersky, Johns Hopkins University, during time he spent at the National Bureau of Standards.
THE EFFECT OF RAPID SOLIDIFICATION VELOCITY ON MICROSTRUCTURE AND PHASE SOLUBILITY EXTENSION IN NiAl-Cr QUASIBINARY EUTECTIC

W. J. BOETTINGER
Metallurgy Division, National Bureau of Standards, Washington, D.C., USA

D. SHECHTMAN*
Technion, Haifa, Israel and Center for Materials Research, Johns Hopkins University, Baltimore, MD, USA

T. Z. KATTAMIS*
University of Connecticut, Storrs, CT, USA

R. J. SCHAEFER
Metallurgy Division, National Bureau of Standards, Washington, D.C., USA

The transition from a two-phase rod-type eutectic microstructure to a single-phase Cr-supersaturated NiAl microstructure for the NiAl-Cr quasibinary eutectic composition is determined as a function of growth rate by electron beam melting and solidification scans. At growth rates below 1 cm/s the alloy exhibits a two-phase eutectic structure. Above 2.5 cm/s the structure solidifies as single phase Cr-supersaturated NiAl which subsequently decomposes spinodally.

1. INTRODUCTION

The NiAl-Cr quasibinary eutectic composition is Ni-33 at% Al-34 at% Cr and is of interest for the study of extended solubility because of the similarity of crystal structures (CsCl for γ-NiAl and BCC for α-Cr) and lattice parameters of the two phases in the eutectic. Previous work has shown that melt spun ribbons exhibit a variety of microstructures: extremely fine eutectic, supersaturated γ-NiAl phase (which undergoes solid state decomposition) and a mixture of the two. The thermodynamic possibility of solubility extension of the two phases was evaluated using T0 curves and was found to be consistent with the formation of supersaturated γ-NiAl rather than α-Cr from eutectic melts.

The present work seeks to establish the kinetic aspects of the transition from eutectic growth at low solidification rates to the supersaturated single phase structure observed in melt spun ribbons. By careful microstructural analysis of the shape of molten pools during electron beam surface scans performed at speeds between 0.1 cm/s and 50 cm/s, the local growth rate within solidified zones is determined and correlated to the local microstructure obtained by TEM.

2. EXPERIMENTAL PROCEDURE

Rapidly solidified samples were prepared using one dimensional scans of a focused electron beam across the surface of the alloy. These scans produce a melted and resolidified trail, typically 0.5 mm wide and 0.1 mm deep. Due to the relatively poor thermal diffusivity of the alloy, the growth direction, even at the top center of the trail, differs significantly from the scan direction. Under steady state
conditions, the true growth rate, \( V \), is the product of the scan velocity with the cosine of the angle between the growth direction and the scan direction. For scan speeds below 2.5 cm/s these angles were measured for each specimen by longitudinal sections through the trail centerline and were typically 30°. The measured angles were employed to describe the growth rate for the microstructures. For scan speeds above 2.5 cm/s the angles were not measured but are estimated to be about 60° leading to a 50% reduction of the actual growth rate compared to the scan rate. TEM specimens were prepared by ion milling full disks cut parallel to the surface of the alloy or half disks cut perpendicular to the scan direction. In all cases care was taken to locate the thin area near the top center of the melted trail where the growth rate is known from the above arguments.

3. RESULTS

For growth rates below 1 cm/s the alloy solidifies as a fine eutectic structure of \( \beta \)-NiAl and \( \alpha \)-Cr phases as shown in Fig. 1. The observed eutectic spacings, \( \lambda_e \), are plotted on the left side of Fig. 4 along with an extrapolation of the relationship between spacing and growth rate determined at slower rates by

![Fig. 1. Eutectic structures of \( \alpha \)-Cr and \( \beta \)-NiAl solidified at (a) 0.09 cm/s and (b) 0.8 cm/s with spacings of ~ 80 nm and ~ 20 nm respectively. TEM.](image)

Walter and Cline.\(^4\) \( \lambda_e^2 \approx 7 \times 10^{-12} \text{ cm}^3/\text{s} \)

For eutectic growth at rates on the order of 1-10 cm/s, the interfacial undercooling due to solute redistribution and interface curvature becomes sufficiently large that the temperature dependence of the liquid diffusion becomes important.\(^3\) Hence the \( \lambda_e^2 V \) relationship cannot be extrapolated past this range. In fact, in the present case at a growth rate of 2.5 cm/s and above, the alloy does not solidify as with a eutectic structure.

Fig. 2 shows the microstructure obtained at 2.5 cm/s. It consists of columnar grains of \( \beta \)-NiAl which have undergone spinodal decomposition. The average composition appears quite uniform across the grain interiors as
judged by the uniformity of the decomposition structure across the grains. Antiphase domains (not shown) are present within the grains with sizes which are very large compared to the scale of the spinodal structure. This fact indicates that the structure was ordered before it decomposed and consequently that the super-
saturated γ-NiAl formed directly from the melt. Identical structures were obtained in melt-spun ribbons.

A high magnification view of the nature of the region near a grain boundary is shown in Fig. 2b. On the right is seen the spinodal structure present throughout the grains. The structure shows no direction of elongation regardless of the plane of section and therefore is not eutectic. On the left, close to the edge of the grain, a fine structure aligned perpendicular to the boundary is present. Even though this resembles a fine eutectic, it is
thought to arise in the solid state by a peculiarity of coarsening of the spinodal structure near a grain boundary. In melt spun ribbons, similar structures were observed but also intergranular regions which were clearly composed of eutectic. This latter structure was not seen in the electron beam melted specimens, possibly due to the absence of recalescence effects in surface melted specimens.

The general features of the microstructure do not vary significantly at increased growth rates (see Fig. 3) except that the spinodal spacing decreases with increasing growth rate. These spacings are shown on the right side of Fig. 4.

4. DISCUSSION

Three topics warrant discussion in the present paper: (1) the existence of a maximum growth rate of ~1-2 cm/s for the γ-Cr and γ-NiAl eutectic; (2) the formation of the supersaturated γ-NiAl phase at the relatively low growth rates of 2.5 cm/s and above; and (3) the refinement of the spinodal spacing with increasing growth rate.

4.1 Eutectic Growth Rate Maximum

The observed growth rate maximum for the eutectic structure is consistent with theoretical arguments and results on other systems. Inclusion of the temperature dependence of the liquid diffusion coefficient into eutectic growth theory predicts a maximum growth rate in the range of 1-10 cm/s for most eutectics. This modification of the theory also leads to a modification of the $\alpha$ relation obtained at slow rate. However, this modification only becomes detectable experimentally very close to the growth rate maximum. This fact is reflected in the present work by the good agreement of the measured eutectic spacings with the extrapolated $\alpha$ relationship of Cline and Walter. Presumably measurements of spacings between 1 and 2.5 cm/s would show a marked deviation from the extrapolated $\alpha$ relationship.

4.2 Supersaturated γ-NiAl

As described previously, the formation of γ-NiAl by partitionless solidification from
partitioning with solid forming at the metastably extended solidus curve can produce micro-segregation-free solids. The published phase diagram data is sparse but would be inconsistent with this second possibility. Future analysis of this result is necessary.

4.3 Spinodal Spacing

For the case of a moving heat source the average cooling rate in the solid behind the freezing interface can be estimated as being proportional to the source speed, \( V \). For the case of continuous cooling the spinodal spacing, \( \lambda_3 \), should vary as a power of the solid cooling rate.\(^{9}\) For the present case where extensive coarsening has taken place the power is roughly \(-1/3\) and hence \( \lambda_3 \sim V^{-1/3} \). The variation of spinodal spacing with electron beam scan rate in Fig. 4 is not inconsistent with this relationship.

REFERENCES

5. J. W. Cahn, private communication.
ELLULAR MICROSEGREGATION IN RAPIDLY SOLIDIFIED Ag-15 wt% Cu ALLOYS

A. BENDERSKY*

enter for Materials Research, The Johns Hopkins University, Baltimore, MD, USA

J. BOETTINGER

metalurgy Division, National Bureau of Standards, Washington, DC, USA

Microstructural and microchemical analysis has been performed on Ag-15 wt% Cu alloys produced by electron beam melting with solidification velocities of 2.5, 12 and 18 cm/s. Cellular structures of the Ag-rich phase are produced with spacings of 0.8, 0.3 and 0.2μm, respectively. Intercellular regions contained fine eutectic at the lowest speed but only Cu-rich phase at the higher speeds. The composition within the cells was found to be nearly uniform and 12.5 ± 1 wt% Cu. The uniformity and level of the Cu content within the cells are discussed.

INTRODUCTION

Many rapidly solidified crystalline alloys exhibit very fine cellular microsegregation patterns. The amount of solute incorporated into the cell interiors has a strong influence on the volume fraction of intercellular phases and precipitation in the cell interiors during subsequent thermomechanical treatment. At extremely high rates of solidification (~1 m/s), microsegregation-free alloys may be produced by solute trapping. However, many important rapid solidification processes do not impose such high growth rates. Hence the details of microsegregation patterns were examined at lower growth rates where significant solute trapping is not expected.

Several authors have measured cellular solute profiles in rapidly solidified alloys produced with unknown or calculated growth rates. In the present work the growth rate is determined experimentally using the electron beam melting and resolidification technique.

The theory of alloy dendritic and/or cellular growth under conditions of local interfacial equilibrium is being continually refined. Solari and Biloni, using the model of Burden and Hunt for the tip concentration, have modeled the entire microsegregation profile as a function of growth rate under the assumption of no lateral concentration gradients in the liquid between solidifying cells. Such an approach is only valid when the cell spacing, 1, is much less than D/V, where D is the liquid diffusion coefficient and V is the growth rate. As will be shown in the present paper, this assumption is questionable for rapid solidification.

EXPERIMENTAL PROCEDURE

Rapidly solidified samples were prepared using one dimensional scans of a focussed electron beam across the surface of a Ag-15 wt% Cu sample at speeds of 2.5, 12, and 18 cm/s. Due to the relatively high thermal diffusivity of Ag, the growth direction and solidification speed of the resolidified alloy near the top center of the melted region is nearly parallel and equal to the electron beam scan velocity. TEM samples were prepared by ion milling on a

*Present worker, Metallurgy Division, National Bureau of Standards, Washington, DC, USA.
liquid nitrogen cooled stage thin half disks cut transverse to the scan direction.

Composition profiles were determined using analytical electron microscopy. Compositions were quantified using the Cliff-Lorimer ratio technique\textsuperscript{11} for the L\textsubscript{a} and K\textsubscript{a} x-rays for Ag and Cu with a constant determined experimentally from measurements on a homogeneous Ag-28 wt\% Cu alloy, rapidly solidified in a partitionless manner at a velocity of 70 cm/sec.\textsuperscript{6} The thin-film criterion\textsuperscript{11} is satisfied for a specimen thickness less than 153 nm for both characteristic x-rays. The usual thickness of specimens was less than 150 nm. The spatial resolution was determined using the beam broadening equation.\textsuperscript{11} For the foil thickness, 150 nm, the beam broadening was calculated to be 42 nm, and the total broadening with the probe size 5 nm (in our experiments) was 42.2 nm.

3. RESULTS AND DISCUSSION

3.1 Microstructure

Figure 1 shows micrographs of cellular structures of Ag-rich phase seen in Ag-15 wt\% Cu alloys solidified at 2.5, 12, and 18 cm/s. The distance between cells are approximately 0.8, 0.3, and 0.2 μm respectively. Note that, these values when divided by D/V, the characteristic diffusion length, are in excess of 10. (D is taken as 2 x 10\textsuperscript{-5} cm\textsuperscript{2}/s).

The volume fraction of intercellular regions is small compared to that found in conventionally cast alloy of the same composition. This is due to the high level of solute present in the cell interiors (see Section 3.2). At a growth rate of 2.5 cm/s (Fig. 1a), those intercellular regions which are wide, contain a fine eutectic structure of the Ag- and Cu-rich phases. The eutectic spacing is ~48 nm. In narrow intercellular regions, only the Cu-rich phase is seen. This feature, which also occurs in ordinary cast microstructures, is called a divorced eutectic and is present whenever the width of an intercellular region is smaller than the eutectic spacing which would occur at the imposed growth rate.

Figure 2 shows a high magnification micrograph of intercellular regions typical of those seen at 12 and 18 cm/s. No eutectic is seen at these growth rates. The intercellular regions

\textbf{Fig. 1. Cellular structures in Ag-15 wt\% Cu solidified at (a) 2.5 cm/s (dark field), (b) 12 cm/s, and (c) 18 cm/s. TEM.}

\textbf{Fig. 2. Intercellular region in alloy solidified at 12 cm/s. TEM.}
the foil where the Ag-rich phase has been completely removed by ion milling, the composition of the Cu-rich intercellular phase was found to be ~90 wt% Cu.

A similar profile for finer cells grown at 12 cm/s is shown in Figure 4. The cell interior is uniform with 12.3 ± 1.2 wt% Cu. The center composition of a number of the very fine cells produced at 18 cm/s were measured as shown in Figure 5. The average of these measurements was 13.6 ± 1.6 wt% Cu.

Two aspects of these profiles warrant discussion: the uniformity of the compositions within the cells and the level of solute within the cells. The slight increase in cell compositions from 11.8 to 13.6 wt% Cu with increasing

Fig. 3. STEM micrograph and composition profile across intercellular region of alloy solidified at 2.5 cm/s.

are comprised solely of the Cu-rich phase (fringe pattern). This divorced eutectic occurs for a different reason at high growth rates. It is known that the Ag-Cu eutectic cannot grow faster than 2.5 cm/s. Hence the eutectic should also be absent as an intercellular microconstituent at growth rates higher than 2.5 cm/s.

3.2. Microanalysis

Figure 3 shows a STEM micrograph and an associated microanalysis profile of the relatively coarse cellular structure formed at 2.5 cm/s. Typical spatial and composition resolutions are 40 nm and 2 wt% Cu. Within these limitations, the composition of the cell interiors is uniform with 11.8 ± 1.3 wt% Cu. The measured compositions in the cell walls are lower than the true composition due to the beam broadening and the fact that the cell wall is slightly oblique to the electron beam with Ag-rich phase also being probed. In regions of

Fig. 4. Composition profile across a cell solidified at 12 cm/s.

Fig. 5. STEM micrograph of cellular structure solidified at 18 cm/s. The compositions at the centers of the cells marked 0, 1, 2, 7 respectively are 12.5, 13.0, 13.8, 15.5, 14.8, 13.8, 12.0, 13.2 wt% Cu.
growth rate cannot be documented with certainty in the present work and the solute level of all the cells will be taken as \(12.5\) wt% Cu.

At growth rates used in the present work, the assumption of local interfacial equilibrium at the liquid/solid interface should be valid and in fact partitionless solidification is only observed in Ag-15% Cu at growth rates above 2 m/s. Hence the phase diagram is of interest. Recently Murray included in her assessment an evaluation of the free energy of the phases which permits the calculation of the metastable Ag-rich solidus below the eutectic temperature. The solidus has a metastable retrograde at 10.5 wt% Cu and 700°C. Under interfacial equilibrium conditions solid cannot form with composition higher than the retrograde composition. The observed level of solute in the cells is very close to the retrograde composition. The agreement may be even better considering the fact that minor adjustments of the free energy functions can increase this retrograde composition by a few percent.

The observation of uniform compositions across cell interiors but with a high degree of segregation to the cell walls is a seemingly curious result. Mazur and Flemings in work on Al-Cu did not see uniformity within cell interiors. However the spacings of the cells measured in their work were greater than 2 μm whereas the cells measured in the present work are less than 1 μm.

The theory of Solari and Biloni while predicting a reduced level of microsegregation at high growth rates, does not predict uniform profiles within cell interiors. This is due to their assumption which does not allow lateral solute gradients. Non-equilibrium trapping of solute is used as an explanation of flat microsegregation profiles. However, McFadden and Coriell have numerically calculated solute concentrations, temperature fields and interface shapes for two-dimensional cellular interfaces in a self-consistent manner. They have shown that compositions may be quite uniform across the major fraction of a cell with strong segregation to cell walls even when local equilibrium exists at the liquid-solid interface. Such microsegregation profiles should be very common whenever \(10 \leq \frac{D}{l} \leq 100\). Such is the case in the present experiments.

ACKNOWLEDGEMENT

The authors wish to thank S. R. Coriell, G. B. McFadden and R. J. Schaefer for many helpful discussions.

REFERENCES