FORBIDDEN LINE RADIATION COOLING OF HIGH ALTITUDE PLASMAS

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19 February 1982

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High Altitude Nuclear Explosions
Metastable States
Forbidden Line Radiation

Ionospheric Plasma
Electron Impact Excitation

Time dependent rate equations describing electron impact excitation (and De-excitation) of and forbidden line radiation from ionospheric constituents have been integrated to obtain excited state population densities, radiation rates, ion and electron temperatures, and energy partitions as a function of time. Radiations from low-lying metastable states of oxygen and nitrogen ions, oxygen and nitrogen atoms, and molecular oxygen excited by electrons in the one eV energy range have been computed for plasma compositions characteristic of selected high altitude nuclear explosions.
PREFACE

The author wishes to acknowledge helpful discussions and criticisms from D. H. Archer, F. E. Fajen, R. W. Kilb, and D. S. Sappenfield.
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SECTION 1
INTRODUCTION

It is well known that optical emissions resulting from deposition of energy in the upper atmosphere by natural and man-made events (e.g., aurora and high altitude nuclear explosions) can serve as useful diagnostics to aid in understanding the detailed physics and chemistry which are operative. It is also well known that hot plasmas (temperatures of several eV to tens of eV or more) which are formed by nuclear explosions may cool quite effectively by emission of electromagnetic radiation via allowed electronic transitions. (Hydrodynamic expansion, of course, produces a great deal of cooling also.) However, once the temperature, or more precisely the electron temperature of such a plasma, has dropped to about an electron volt or so, electron impact excitation of atmospheric constituents effectively is limited to low lying electronic states (and vibrational states in molecules). For the dominant atmospheric species, these states are metastable, so "rapid" radiation cooling is shut off. At this point, interest in radiation as a plasma cooling mechanism traditionally has diminished quite rapidly, although spectroscopic interest remained strong.

The purpose of this paper is to illustrate that warm plasmas (~1 eV temperature) at high altitudes (where interactions with the neutral atmosphere are minimal) can rid themselves over a period of hours of considerable excess energy by forbidden radiation. Such slow but steady cooling turns out to be significant in the case of nuclear explosion produced plasma. In addition, the partition of energy between thermal and excited metastable states is explored.
Spectroscopic and other studies of emissions from the upper atmosphere have aided understanding of a variety of physical phenomena. For example, thermospheric temperatures and neutral winds have been inferred from Doppler measurements of OI 6300 Å radiations, precipitating electron energetics in the auroral region have been deduced from airglows at ionospheric altitudes, and F-region plasma depletions and propagating waves have been observed by OI 6300 Å emissions. A recent review of optical processes as they apply to the F-region, particularly at high latitudes, is available.

In the realm of nuclear weapons effects, optical phenomena induced by high altitude nuclear detonations have produced both dazzling displays and scientific diagnostic information. In 1962, a 1.4 megaton nuclear device (Starfish) was detonated at 400 km altitude near Johnston Island in the Pacific. As this was an announced test with both scientific and military objectives, numerous groups stationed equipment at a variety of locations across the Pacific. Spectroscopic observations of optical radiation both immediately following and several minutes after detonation confirmed the presence of allowed and forbidden radiation from atmospheric species in the immediate vicinity of the burst point and in regions of optical activity ("artificial" aurora, etc.) well removed from the burst point. A review article by Hoerlin contains color photos of Starfish which illustrate some of the striking optical features which produced the spectroscopic records of references 9 and 10.

This report attempts to provide reasonable estimates of radiation cooling processes which operate over extended periods (i.e., hours) in such high altitude plasmas. Forbidden radiations arising from radiative decay of low-lying metastable states of O+, O, N+, N, and O2 have been computed under the assumption that the low-lying states have been populated by electron impact. Quenching of excited states by electron collisions has been included, but heavy particle quenching has been
ignored. Time dependent rate equations for the ground and excited states of the five emitting species have been numerically integrated to obtain self-consistent solutions free from assumptions of equilibrium excited state populations. Section 2 of the report describes the radiating systems of interest and presents the relevant equations. Section 3 contains the results of detailed calculations which span radiation periods of several hours, and Section 4 presents a discussion of results and some conclusions.
SECTION 2
RADIATION COOLING EQUATIONS

Each of the atmospheric species of interest here ($0^+$, $O$, $N^+$, $N$, and $O_2$) possesses a series of low-lying metastable states which can be populated by electron impact. These states are displayed schematically in Figure 1. In order to simplify the calculations a bit, each set of closely spaced (doublet or triplet) states, shown in the figure, has been lumped together into a composite state.† Thus, for the calculations described here, each of the species is modelled as a system with two excited states above the ground state.

These excited states can be populated (and de-populated) by collisions with electrons, processes for which the cross-sections seem to be reasonably well known. (Collisions with other particles also can alter excited state populations. More about this later.) For the present work, it has been assumed that radiation emitted from a plasma volume element is not reabsorbed and that the total radiation field is sufficiently weak that stimulated emission is insignificant. Under these conditions, the rate equations describing the excited state populations of a generic three level system are

\[
\frac{dn_0}{dt} = -k_{01}n_0n_e - k_{02}n_0n_e + A_{10}n_1 + k_{10}n_1n_e + k_{20}n_2n_e + A_{20}n_2
\]  

(1)

Figure 1. Schematic of metastable states of interest.
In this notation, $k_{ij}$ is the collisional excitation (or deexcitation) rate coefficient from state $i$ to state $j$, $A_{ij}$ is the Einstein coefficient for spontaneous emission, $n_i$ is the number density of particles in state $i$, and $n_e$ is the electron density. The ground state, first excited state, and second excited state are denoted by subscripts 0, 1, and 2, respectively. Because photon absorption and stimulated emission are assumed insignificant in the present work, terms containing the Einstein $B$ coefficient are absent from these rate equations.

The electron impact excitation and deexcitation rate coefficients used for $O^+$, $O$, $N^+$, and $N$ were from Ali$^{12}$ and Ali, et al.$^{13}$ These coefficients were obtained by integrating cross-section data with an electron Boltzmann distribution. (Other rate coefficients or cross-sections that one might want to consider are available.)$^{14-16}$ Note that the excitation rate coefficient, $k_{ij}$, is related by detailed balance to the deexcitation rate coefficient, $k_{ji}$, by

$$g_i k_{ij} = g_j k_{ji} e^{-\Delta E_{ij}/kT} \quad (4)$$

where the $g$'s are statistical weights$^{17}$, $\Delta E_{ij}$ is the $i$-$j$ energy level spacing, $k$ is the Boltzmann constant, and $T$ is the electron temperature.

Excitation rate coefficients for transitions from the ground state ($\chi^3\Sigma_g^-$) to the first excited ($a^1\Delta_g$) and second excited ($b^1\Sigma_g^+$) states of $O_2$ were computed by integrating excitation cross-sections multiplied by
electron velocity over a Boltzmann energy distribution:

\[ k_{\text{excit}} = \frac{2}{m} \left( \frac{2\pi}{m kT} \right)^{3/2} \int_{0}^{\infty} E \sigma(E) e^{-E/kT} dE \]  

(5)

where \( m \) is the electron mass. The cross section for ground to first excited state transitions was assumed to be

\[ \sigma = 3.5 \times 10^{-14} \left( \frac{0.98}{E} \right)^3 \left[ 1 - \left( \frac{0.98}{E} \right)^{0.1} \right]^3 \]

\[ + 8.0 \times 10^{-13} \left( \frac{2.2}{E} \right)^{2.5} \left[ 1 - \left( \frac{2.2}{E} \right)^{0.05} \right]^3 \] (cm²)  

(6)

The cross-section for ground to second excited state transitions was assumed to be

\[ \sigma = 3.09 \times 10^{-17} \left( \frac{1.63}{E} \right)^{2.5} \left[ 1 - \left( \frac{1.63}{E} \right) \right]^3 \]

\[ + 4.67 \times 10^{-16} \left( \frac{2.3}{E} \right)^{2.1398} \left[ 1 - \left( \frac{2.3}{E} \right)^{0.4} \right]^3 \] (cm²)  

(7)

In Equations 6 and 7, the energy, \( E \), has units of electron volts. The square bracketed terms are to be interpreted as

\[ \left[ 1 - \frac{E_0}{E} \right] \begin{cases} 1 - \frac{E_0}{E}, & E > E_0 \\ 0, & E < E_0 \end{cases} \]  

(8)

These cross sections are due to Archer and result from his analytic fit to cross-section data of Trajmar, et al. Deexcitation rate coefficients for these transitions were computed with the aid of Equation 4. Unfortunately, no suitable cross-sections or excitation rate coefficients for first to second excited state transitions appear to be available. Therefore, the rate coefficients for excitation and deexcitation through this transition are assumed to be zero.
The probabilities (Einstein $A$ coefficients) used for radiative decay of the metastable states of 0+, 0, N+, and N are due to Wiese, et al\textsuperscript{17}. The reader's attention is called to Appendix B of that publication wherein rules are given for combining transition probabilities for members of a multiplet into a composite transition probability. Transition probabilities for O\textsubscript{2} (0-0 band) are due to Bader, et al\textsuperscript{20} (a\textsubscript{1}A\textsubscript{g} + X\textsubscript{3}\Sigma\textsubscript{g}\textsuperscript{-} transition), and from the life time data assembled by McGowan, et al\textsuperscript{22} (b\textsubscript{1}\Sigma\textsubscript{g} + X\textsubscript{3}\Sigma\textsubscript{g}\textsuperscript{-} transition).

Transition probabilities, statistical weights, etc., for the five systems of interest are summarized in Table 1. Electron impact excitation and deexcitation rate coefficients are summarized in the Appendix.

Once the excited state populations have been determined, the instantaneous radiation rates can be computed as the products of the state densities and the transition probabilities. Thus, the rate at which energy is lost from the plasma is obtained.

If electron thermal energy were the only energy reservoir to be tapped, then our model for radiation cooling would be reasonably complete. However, at the plasma densities of interest here, ion-electron collisions are sufficiently frequent to insure some measure of thermal energy transfer, with the result that radiation cooling indirectly removes at least some of the ion thermal energy. In order to compute this process, collisional heat transfer between ions and electrons was assumed to obey

\begin{equation}
\frac{3}{5} \left( \frac{2}{3} N_e kT_e \right) = N_i N_e h_{ie} (kT_i - kT_e)
\end{equation}

where

\begin{equation}
h_{ie} = 3.6 \times 10^{-9} \left( kT_e \right)^{-1.5} \text{cm}^3/\text{sec.}
\end{equation}
## Table 1

<table>
<thead>
<tr>
<th>Species</th>
<th>Transition</th>
<th>$g_{\text{upper}}$</th>
<th>$g_{\text{lower}}$</th>
<th>$A(\text{sec}^{-1})$</th>
<th>Approximate Transition Energy (eV)</th>
<th>$\lambda(\text{A})$</th>
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<tbody>
<tr>
<td>O</td>
<td>$^1\text{D} \rightarrow ^3\text{P}$</td>
<td>5</td>
<td>9</td>
<td>0.00677</td>
<td>1.96</td>
<td>6300</td>
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<tr>
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<td>$^1\text{S} \rightarrow ^3\text{P}$</td>
<td>1</td>
<td>9</td>
<td>0.0674</td>
<td>4.17</td>
<td>2958</td>
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<tr>
<td></td>
<td>$^1\text{S} \rightarrow ^1\text{D}$</td>
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<td>5</td>
<td>1.34</td>
<td>2.22</td>
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<tr>
<td>O$^+$</td>
<td>$^2\text{D}^0 \rightarrow ^4\text{S}^0$</td>
<td>10</td>
<td>4</td>
<td>0.000097</td>
<td>3.33</td>
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<td>$^2\text{P}^0 \rightarrow ^4\text{S}^0$</td>
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<td>6</td>
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<tr>
<td>N</td>
<td>$^2\text{D}^0 \rightarrow ^4\text{S}^0$</td>
<td>10</td>
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<td>N$^+$</td>
<td>$^1\text{D} \rightarrow ^3\text{P}$</td>
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<td>$^1\text{S} \rightarrow ^3\text{P}$</td>
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<td>$^1\text{S} \rightarrow ^1\text{D}$</td>
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<td>$\text{O}_2$</td>
<td>$^1\Delta \rightarrow ^3\Sigma$</td>
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<td>0.000258</td>
<td>0.98</td>
<td>3071</td>
</tr>
<tr>
<td></td>
<td>$^1\Sigma \rightarrow ^3\Sigma$</td>
<td>1</td>
<td>3</td>
<td>0.085</td>
<td>1.63</td>
<td>5755</td>
</tr>
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Here the subscripts refer to ions and electrons; the N's are number densities \((\text{cm}^{-3})\); \(kT_i\) and \(kT_e\) are in eV. The heat transfer coefficient, \(h_{ie}\), is due to Kilb, Stagat, and Stoeckly\(^2\).

In principle, ion-neutral, electron-neutral, and electron-vibrational mode (of neutral molecules) heat transfers also should be computed. Processes involving ion-neutral and electron-neutral collisions can be evaluated with the aid of heat transfer coefficients from reference 22. For the purpose of estimating relative rates, a 700°K Jacchia atmosphere\(^2\) has been used. For altitudes above 200 km, electron-neutral heat transfer is negligible. In the 300 km altitude regime, and at the densities considered here, ion-neutral transfer roughly is on a par with ion-electron transfer. With increasing altitude, heat transfer involving neutrals diminishes as the neutral density decreases exponentially. Energy transfer between electrons and the vibrational modes of nitrogen molecules can be computed also. If we assume the vibrational state distribution can be characterized by a temperature \(T_v\), then Equation 9 (with \(T_i\) replaced by \(T_v\)) can be used provided we adjust the rate coefficient. Thus, instead of \(h_{ie}\), we have used an electron - \(N_2\) vibrational modes heat transfer coefficient which is based on vibrational excitation cross sections due to Schulz.\(^2\) This coefficient is

\[
h_{ev} = 2.0 \times 10^{-10} (kT_e + 0.3) \exp(-0.3/kT_e) \\
+ 8.3 \times 10^{-9} (kT_e + 2.3) \exp(-x) \quad (\text{cm}^3/\text{sec})
\]

where

\[
x = \begin{cases} 
-2.3/kT_e, & T_e > T_v \\
-2.0/kT_v, & T_e \leq T_v
\end{cases}
\]

with \(kT_e\) and \(kT_v\) in electron volts. One finds that below about 350 km (again using the neutral atmosphere of reference 13) electron - \(N_2\) collisions can be quite significant.
For the present work, the effects of ion-electron heat transfer collisions as prescribed by Equations 9 and 10 have been included. The other collisional energy transfer processes have been ignored, in order to avoid undue complexity. It must be recognized that a complete calculation of a high altitude plasma must include hydrodynamics, chemistry, etc., processes which we are not prepared to include in the present work. We leave that to full blown nuclear burst simulation which should include radiation cooling equations and all the relevant energy transfer processes.

Electron impact collisions are not the only means by which metastable state populations may be changed. Excited state populations also can be altered (quenched) by collisions with heavy particles, but results of such collisions may depend strongly on the initial and final states of the heavy particle. Given the large variety of potential target particle state and quenching heavy particle state combinations which are possible, one should not be surprised that cross-section or rate coefficient data for heavy particle quenching are rather spotty and tend to be fairly uncertain. If one uses the limited set of quenching rate coefficients suggested by Gerard\(^8\) or Ali, et al,\(^{13}\) and a nominal neutral atmosphere,\(^{23}\) and if one looks for the altitude above which radiative decay of a state exceeds heavy particle quenching, then one finds that the present calculations generally apply above 200-300 km altitude, the precise altitude depending on the particular excited species - quenchant combination.

For the present, heavy particle quenching has been ignored also. However, the lack of such quenching is consistent with the decision to ignore heat transfer processes which would tap the neutral thermal and \(N_2\) vibrational energy pools. Quenching collisions involving neutrals would tend to return energy from the metastable states to neutral thermal where, by heat transfer, it could find its way back to the electrons.
SECTION 3
RESULTS

This section contains results from a systematic set of calculations which was designed to illustrate the behavior of the various three level metastable systems under circumstances representative of conditions in the ionosphere/magnetosphere following a high altitude nuclear burst. The results are divided into two categories; the first illustrates single species systems collisionally excited by electrons at densities of $10^4$, $10^6$, and $10^8$ cm$^{-3}$. The second category represents calculations of multi-species systems based on conditions found in selected, detailed calculations of high altitude nuclear bursts.

Computational results are presented in four types of plots. The first type of plot shows ground and excited state population densities as a function of time. In most cases, the excited state densities remain less than a few percent of the total species density, so the ground state density curve usually appears as a horizontal line across the upper portion of this type of graph. The discerning eye, however, will find that the ground state curve is not simply a constant.

The second type of graph displays radiation cooling rates as a function of time. The third type of graph shows electron and ion temperatures as a function of time. At low ion and electron densities ($10^4$ cm$^{-3}$), one frequently finds that collisional thermal energy transfer is slow compared to collisional excitation and radiation, so the ion and electron temperatures can depart significantly from each other.
The relative partition between excited state and thermal energies as a function of time is contained in the fourth type of plot. This class of graph displays the ratio of energy tied up in excited states to available energy. The available energy is defined as the sum of excited state and electron thermal energies, plus ion thermal energy provided that thermal energy transfer (Equation 9) is included in the calculation. (Equation 9 was included in all but two cases which are noted.)

Because the objective of this report was to emphasize energy partition and radiation cooling over extended periods, most calculations covered an interval of 30,000 seconds (8 1/3 hours). In order to insure legibility of plots which might span many decades, most graphs have been limited to no more than six decades. As a result, some curves (e.g., certain excited state densities) of particularly small magnitude rapidly disappear or don't appear at all. This plotting effect usually occurs, if at all, in low electron density calculations.

The calculations presented here are summarized in Table 2. In all cases, initial excited state densities were assumed to be zero. As Table 2 indicates, two categories of calculations were done. The first category is composed of a single species systems with the species and electron densities set equal. Electron densities were set to $10^4$, $10^6$, or $10^8$ cm$^{-3}$ to cover the range of interest in late-time high altitude nuclear burst problems; electron and ion temperatures were initialized to one electron volt.

The second category of cases is composed of multi-species systems which are representative of a range of conditions found in detailed two-fluid numerical simulations of high altitude nuclear bursts. Species densities, electron density, and ion electron temperatures were as indicated in Table 2.
### Table 2
**Summary of Calculations**

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<th>Figure No.</th>
<th>([O^+]) (cm(^{-3}))</th>
<th>([N^+]) (cm(^{-3}))</th>
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<th>([n_e]) (cm(^{-3}))</th>
<th>Initial (T_e) (eV)</th>
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It's worthwhile, perhaps, to note that excited state densities and radiation rates are not trivially related to the electron density. If, for example, we assume the quasi-steady state, then Equations 2 and 3 yield the ratio of first to second excited state densities for our generic three level system:

$$\frac{n_1}{n_2} = \frac{k_{01}\left([k_{20} + k_{21}] n_e + A_{20} + A_{21}\right) + k_{02}\left(k_{21} n_e + A_{21}\right)}{k_{02}\left([k_{10} + k_{12}] n_e + A_{10}\right) + k_{01} k_{12} n_e}$$

Even in the quasi-steady state, the A's are not negligible in general, so the population ratio and radiation rate ratios depend in a non-trivial manner on the electron density. This is, of course, already well known.

The first series of calculations presented here deals with fully ionized oxygen plasmas. In order to dispense at the outset with questions about the significance of collisional thermal energy transfer between ions and electrons, cases without and with the transfer process are presented in Figures 2, 3 (without) and Figures 4-6 (with). Thus, if one compares Figures 2 and 4 (electron density of $10^4$ cm$^{-3}$), it is seen that the $O^+(2D^0)$ densities are virtually identical during the first 10,000 seconds and then gradually deviate until the curve in the absence of energy transfer (Figure 2) is about 20% below the curve with the transfer (Figure 4). A comparison of radiation rates in these two figures shows the same trend, e.g., at 30,000 seconds, the $2D^0 \rightarrow 4S^0$ transition is cooling about 20% slower in Figure 2 than in Figure 4. Both of these observations are readily understood by comparing the electron temperature curves of Figures 2 and 4. During the first few thousand seconds both curves compare favorably, and the ion temperature curve in Figure 4 indicates very little energy transfer from ions to electrons. At 30,000 seconds, however, the electron temperatures differ by about 10% and the ion temperature (Figure 4) has dropped by about a tenth of an eV.
Figure 2. Radiation properties of O$^+$ at an electron density of $10^6$ cm$^{-3}$. Ion-electron heat transfer (Equation 9) is absent from this calculation.
Figure 2 (Continued)
Figure 3. Radiation properties of $O^+$ at an electron density of $10^9$ cm$^{-3}$. Ion-electron heat transfer (Equation 9) is absent from this calculation.
Figure 3 (Continued)
Figure 4. Radiation properties of $O^+$ at an electron density of $10^4 \text{ cm}^{-3}$.
Figure 4 (Continued)
Figure 5. Radiation properties of O⁺ at an electron density of 10⁶ cm⁻³.
Figure 5 (Continued)
Figure 6. Radiation properties of O\(^+\) at an electron density of 10\(^8\) cm\(^{-3}\).
Figure 6 (Continued)
Finally, the curves denoting the fraction of available energy which is tied up in excited states may be compared. Both curves peak at about 10,000 seconds, but the curve in Figure 4 peaks at a lower value (even though the electron temperature and excited state densities are higher than found in Figure 2) because the available energy has been doubled by coupling to the ions. The most significant point here is that in each case the fraction of available energy tied up in excited states is a few percent.

With the aid of Figures 3 and 6 one can make a parallel set of comparisons at the other electron density extreme considered here \((10^8 \text{ cm}^{-3})\). As one would expect, the case with ion-electron energy transfer (Figure 6) maintains a slightly (-30%) higher electron temperature than the case without (Figure 4), so excited state densities and radiation rates are also somewhat larger. Unlike the preceding pair of cases, the ion and electron temperatures are now locked together by collisional coupling which transfers energy to the electrons faster than it can be pumped into excited states and radiated away. In Figure 3, the energy fraction in excited states very rapidly peaks at about 10% while in Figure 6 the corresponding peak is at about 8%.

These comparisons (and similar comparisons, not presented, for the other emitting species) lead us to observe that for the range of electron and species densities considered (where the electron and species densities are equal) failure to couple ion and electron thermal energy reservoirs results at most in a modest alteration of the excited state densities, radiation rates, and energy partition. Now that the magnitude of such coupling has been established, we proceed to the remaining calculations, all of which included the coupling.

One can now consider Figures 4, 5, and 6 as a set of calculations which illustrate the electron density dependence of radiation cooling by the \(O^+\) system. This series of figures shows that at an electron
density of $10^4$ cm$^{-3}$ it takes roughly 10,000 seconds to reach a quasi-steady distribution of excited states, radiation rates, etc. At $10^6$ cm$^{-3}$ density, the time required to reach the quasi-steady state is about 200 seconds; at $10^8$ cm$^{-3}$ density, the quasi-steady state is attained "instantly" as compared to the time scale of the plots. (Note that the ion-electron energy transfer rate can alter the scaling of this time constant because the electron temperature can remain higher for a longer time.) As one would expect, the high ion-electron density case radiates much more rapidly than the lower density cases. In addition note that at the $10^6$ cm$^{-3}$ density, the dominant transition is $2\,^1D_1\rightarrow ^1S_0$. At higher densities, the $2\,^3P\rightarrow ^1D$ and $2\,^3P\rightarrow ^1S_0$ transitions dominate. This switch results from the shift in relative populations of the excited states, as expressed in Equation 13, which occurs as the electron density is altered. It is the interplay of excitation rates and transition probabilities which is primarily responsible for this effect.

As noted earlier, the curves denoting the fraction of available energy tied up in excited states all remain in the range of a few percent or less. Thus, from the ion and electron temperature curves we conclude that the time required to radiate one-half the energy is about 6,000 seconds at $10^8$ cm$^{-3}$, about 30,000 seconds at $10^6$ cm$^{-3}$, and (very) roughly $2 \times 10^5$ seconds at $10^4$ cm$^{-3}$.

The excitation and radiation characteristics of nitrogen ions at the electron densities of interest are displayed in Figures 7, 8, and 9. Upon inspection of these figures, one notes that the excited state densities and radiation rates attain a quasi-steady state virtually instantly as compared to the 30,000 second time scale of the plots. Only the case at $10^4$ cm$^{-3}$ electron density (Figure 7) shows a perceptible period (a few hundred seconds) when departures from a quasi-steady distribution of states are evident.
Figure 7. Radiation properties of $N^+$ at an electron density of $10^n$ cm$^{-3}$. 
Figure 7 (Continued)
Figure 8. Radiation properties of $N^+$ at an electron density of $10^6$ cm$^{-3}$. 

**N* STATE DENSITIES**

- $N^{'(4)}P$
- $N^{'(4)}D$
- $N^{'(3)}S$

**N* RADIATION COOLING RATES**

- $N^{'(2)}P$
- $N^{'(2)}D$
- $N^{'(3)}P$

TIME (seconds)

DENSITY (cm$^{-2}$)

RADIATION RATE (eV/cm$^3$/sec)
Figure 8 (Continued)
Figure 9. Radiation properties of N\textsuperscript{+} at an electron density of $10^8$ cm\textsuperscript{-3}. 
Figure 9 (Continued)
It's worth noting the variation with electron density of the ratio of radiation rates for the $^1D$-$^3P$ and $^1S$-$^1D$ transitions. For the $10^4$ cm$^{-3}$ and $10^6$ cm$^{-3}$ electron density cases, this ratio is always greater than one. At $10^8$ cm$^{-3}$ electron density and while the electron temperature is above ~0.53 eV (during the first ~1500 seconds), the ratio is less than one. This behavior can be understood in terms of Equation 13. Based on transition probabilities and photon energies, one can compute that the ratio of $^1D$ to $^1S$ state densities needs to be ~233 or less if the radiation rate for the $^1S$-$^3P$ transition is to dominate. At low electron density, electron impact excitation is insufficient to generate a ratio this small. One observes in Figure 9 (early time) that the $^1D$ to $^1S$ state density ratio is about 100 (electron density is $10^8$ cm$^{-3}$), but in Figure 8 the ratio has jumped to roughly 1000 (electron density is $10^6$ cm$^{-3}$).

As in the case for radiation from oxygen ions, the nitrogen ion calculations indicate that energy associated with excited states is at most a few percent of the available energy. Thus, the temperature curves allow us to readily calculate that a bit more than 2000 seconds is required to radiate one-half the available energy at $10^8$ cm$^{-3}$; about 5500 seconds are required at $10^6$ cm$^{-3}$. One also notes that at the $10^4$ cm$^{-3}$ electron density, excitation and radiation is able to remove energy from the electrons faster than it can be replaced by transfer from the ions. As the higher electron densities, this is not the case.

The radiating characteristics of oxygen atoms over the electron density range of interest are presented in Figures 10, 11, and 12. The reader is reminded that the radiating species density has been set equal to the electron density (and also to a non-radiating ion density). This rather arbitrary choice influences quite strongly the magnitudes of various results. The particular choice of equal densities was made because it provides a reasonable balance between the heat capacity of the ion-electron gas and energy stored in excited states. From these results
Figure 10. Radiation properties of O atoms at an electron density of $10^4$ cm$^{-3}$. 
Figure 10 (Continued)
Figure 11. Radiation properties of O atoms at an electron density of $10^6$ cm$^{-3}$. 
Figure 11 (Continued)
Figure 12. Radiation properties of O atoms at an electron density of $10^8$ cm$^{-3}$. 
Figure 12 (Continued)
the reader can extrapolate, in a limited sense, to other density combinations. If the oxygen atom density had been substantially larger than the electron and ion densities, then most of the available energy would have gone mainly into the lowest excited state at the same time the electron and ion temperatures dropped to low values. The resultant curves would be relatively flat and uninteresting. (Clearly, the best approach is to compute for the precise conditions of interest in a particular problem.)

The first point to note in this series of three figures is that the quasi-steady state is obtained, even at the lowest electron density, rather quickly as compared to the time scale of the plots. However, at 10^4 cm⁻³ electron density (Figure 10), the radiation cooling and temperature curves are quite flat as a result of relatively low excitation rates. One sees that less than a percent of the available energy is tied up in excited states, so it readily can be inferred from the temperature curves that only about 6 percent of the original energy has been radiated over the 30,000 second period.

The calculation at 10^6 cm⁻³ electron density shows more interesting temporal behavior and achieves substantial cooling over 30,000 seconds. Once again, the fraction of available energy which is tied up in excited states is quite small (< 2%), so we readily estimate from the temperature curves that one-half the initial energy was radiated by about 11,000 seconds. Note that radiation from the long lived ¹D→³P transition is the dominant loss channel, a result which is not too surprising in light of the fact that the ¹D state has at least three orders of magnitude greater population density than does the ¹S state. One might expect the relatively short lived ¹S→¹D transition to dominate, but the ratio of transition probabilities (¹S→¹D to ¹D→³P) is only about 200 and can't compensate for the (at least) three orders of magnitude difference in populations (Refer to Table 1).
Inspection of results corresponding to an electron density of $10^8 \text{ cm}^{-3}$ (Figure 12) reveals that at early times the $^1S$ state density is about two orders of magnitude smaller than the $^1D$ state density. In view of the ratio of transition probabilities, it's not surprising to find that initially the $^1S+^1D$ transition dominates. Note that the rapid drop in temperature reduces the $^1S$ state density and the $^1S+^1D$ radiation rate so that after several hundred seconds the $^1D+^3P$ transition dominates. This shift from predominantly green to predominantly red radiation is consistent with observations\textsuperscript{10} of the Starfish high altitude nuclear explosion. (One should not expect these simplified calculations to accurately reproduce the temporal behavior observed in the actual nuclear burst event because too many relevant aspects of the magnetohydrodynamics, air chemistry, etc. have been omitted here.) Finally, we note that in this calculation one-half the initial energy was radiated during the first 2500 seconds.

We now turn our attention to radiation from atomic nitrogen; Figures 13, 14, and 15 contain computational results at the selected electron densities. The reader is reminded that as in the atomic oxygen calculations, nitrogen atom, electron, and non-radiating ion densities are equal. Figure 13 presents the results for an electron density of $10^4 \text{ cm}^{-3}$. Note that the excited state population densities never really reach a quasi-steady distribution, i.e., the excited state densities continue to increase as the electron temperature falls during the entire 30,000 second interval. Also note that at zero time the $^2p^0$ state density "instantly" jumps to a value near $10^{-1} \text{ cm}^{-3}$, and the radiation rates for transitions which originate from this level similarly jump to finite values. A plot with a greatly expanded time scale shows that the $^2p^0$ state density rises with an e-folding time of about 10 seconds, so the rise appears instantaneous on a 30,000 second time scale. Finally, the fraction of available energy tied up in excited states is seen to reach 7% at 30,000 seconds. If excited state energy and temperature drops are taken together, one can see that only about 3% of the initial energy has been radiated by the end of this calculation.
Figure 13. Radiation properties of N atoms at an electron density of $10^4$ cm$^{-3}$.
Figure 13 (Continued)
Figure 14. Radiation properties of N atoms at an electron density of $10^6$ cm$^{-3}$. 

52
Figure 14 (Continued)
Figure 15. Radiation properties of N atoms at an electron density of $10^8$ cm$^{-3}$. 
Figure 15 (Continued)
Calculations at electron densities of $10^6$ and $10^8$ cm$^{-3}$ show quite different behavior. Both of these cases rapidly reach a quasi-steady configuration (less than 1000 seconds required at $10^6$ cm$^{-3}$) and substantial fractions of the initial energy have been radiated. Although the curves denoting the energy fraction in excited states peak a bit above 10%, they decay to about 3.5% by the time one-half the initial energy has been radiated (-20,000 seconds at $10^6$ cm$^{-3}$; -3000 seconds at $10^8$ cm$^{-3}$). In these cases, the infrared ($^2p^0_2^2p^0_0$) transition is responsible for the bulk of the cooling. Observe that in both Figures 14 and 15, the $^2p^0$ state density peaks at about 13% of the total nitrogen atom density. This common feature arises because the radiative transition probability from the state (see Table 1) is quite low, so collisional excitation and deexcitation is responsible for establishing the state density in accord with a Boltzmann distribution, i.e., the ratio of excited state densities in Equation 13 becomes independent of electron density.

Calculations of radiations from $O_2$ are considered next. Once more, the $O_2$ density has been equated to the ion and electron densities. Figures 16, 17, and 18 contain the relevant plots. The ground and excited states, $X^3\Sigma^-_g$, $a^1\Delta_g$, and $b^1\Sigma^+_g$, have been abbreviated as $^3\Sigma$, $^1\Delta$, and $^1\Sigma$ in these figures. Also note that the present calculations considered only two optical transitions, as mentioned earlier.

Figure 16 details the excitation and radiation characteristics of $O_2$ at an electron density of $10^4$ cm$^{-3}$. From the first parts of the figure, it's clear that the $^1\Delta$ state requires about 10,000 seconds to attain a quasi-steady state but the $^1\Sigma$ state is populated virtually instantly as compared to the time scale of these calculations. The radiation rates reflect these excitation characteristics. At this electron density, much less than a percent of the available energy goes into excited states, and only about 2-1/2% of the initial energy is radiated during the calculation time.
Figure 16. Radiation properties of \( \text{O}_2 \) at an electron density of \( 10^4 \text{ cm}^{-3} \).
1. I0

0.90

0.80

0.70

0.60

0.50

0.40

0.30

0.20

0.10

0.00

1.00

1.10

TEMPERATURE (eV)

TIME (seconds)

FRACTION OF ENERGY IN EXCITED STATES

Figure 16 (Continued)
Figure 17. Radiation properties of O₂ at an electron density of 10⁶ cm⁻³.
Figure 17 (Continued)
Figure 18. Radiation properties of $O_2$ at an electron density of $10^9$ cm$^{-3}$. 
Figure 18 (Continued)
At higher electron densities, the O\textsubscript{2} radiation characteristics are quite different. At 10\textsuperscript{6} cm\textsuperscript{-3} (Figure 17), the quasi-steady state is attained in about 2500 seconds, and radiation removes nearly one-half the initial energy, as indicated by the temperature curves. At most, only about 5\% of the available energy is tied up in excited states. Note that prior to -10,000 seconds, radiation from the \(1\Sigma^+ - 3\Sigma\) transition was the dominant cooling mechanism, but afterwards the \(1\Delta - 3\Sigma\) transition dominates.

Figure 18 illustrates that at 10\textsuperscript{8} cm\textsuperscript{-3} electron density, the quasi-steady state is obtained instantaneously as compared to the computation time span. The \(1\Sigma^+ - 3\Sigma\) transition is seen to be dominant over the full 30,000 second period and is chiefly responsible for the energy loss over the entire computation. About 1500 seconds were required to radiate one-half the initial energy. Note that in this case, radiation cooling lowered both ion and electron temperatures to 0.22 eV after 30,000 seconds. This particularly low temperature could be achieved because the metastable levels of O\textsubscript{2} are quite low as compared to the metastable states of O\textsuperscript{+}, O, N\textsuperscript{+}, and N (Refer to Figure 1). Finally, observe that in this calculation the peak fraction of available energy in excited states was about 7\%.

To complete the discussion of these three cases, it's worth pointing out the trend as to which of the O\textsubscript{2} transitions dominates. At 10\textsuperscript{4} cm\textsuperscript{-3} electron density (Figure 16), the \(1\Sigma^+ - 3\Sigma\) transition is dominant for only the first 2000 seconds; at 10\textsuperscript{6} cm\textsuperscript{-3} (Figure 17) it's dominant for the first 10,000 seconds, and at 10\textsuperscript{8} cm\textsuperscript{-3} (Figure 18), it dominates for the entire 30,000 seconds. This trend is not a direct temperature effect (lower ultimate temperatures at higher electron densities) because the \(1\Delta\) state is lower energy than is the \(1\Sigma\) state. Instead, the trend is explained by Equation 13, i.e., it is the play-off between collisional and radiative processes which is important. There is an indirect temperature effect insofar as the collisional excitation and deexcitation rate coefficients are temperature dependent.
The discussion of single species systems is now complete. The remainder of this section will be devoted to calculations based on species densities and initial electron and ion temperatures extracted from detailed high altitude nuclear burst calculations. In these calculations, the time scale has been adjusted to span the most interesting phase of the radiation cooling process.

The Starfish high altitude nuclear test event, conducted on 9 July 1962 during the Fishbowl series, consisted of a 1.4 megaton device detonated at 400 km altitude above Johnston Island in the Pacific. Recently, Fajen has performed a series of detailed two-fluid magneto-hydrodynamic calculations of the Starfish event. The results of his computer simulations contain the best available spatially and temporally resolved estimates of electron and species densities, ion and electron temperatures, and coupled ion-neutral dynamics. Numerical data corresponding to 90 seconds after detonation have been extracted from Fajen's calculations and have been used as the time equals zero initial conditions for radiation cooling calculations which are presented in Figures 19 and 20. The reader may wish to refer to Table 2 for a summary of these data.

Figure 19, which corresponds to an altitude of 395 km, illustrates an element of fireball plasma which is predominantly atomic neutrals (N and O) at a total atom density of $9.6 \times 10^8$ cm$^{-3}$. Oxygen ions are the least populous species ($10^4$ cm$^{-3}$); the nitrogen ion density is about 0.75% of the neutral atom density. Molecular oxygen has a density of about 0.25% of the neutral atom density. The plots indicate that with the exception of $O_2$, the initial transients required to populate the excited states are finished in a few tens of seconds. As one might expect, based on the preponderance of oxygen atoms and the relatively low temperature, radiation in the oxygen red line ($^1D^+_3P$ transition) is the major cooling mechanism; the electron temperature is too low to effectively excite the oxygen green line ($^1S^+_1D$ transition). The second most
Figure 19. Radiation properties based on the 90 second environment at 395 km altitude in Fajen's Starfish calculation.
Figure 19 (Continued)
Figure 19 (Continued)
Figure 19 (Continued)
Figure 19 (Continued)
Figure 19 (Continued)
active transition (energy-wise) is the infrared \( ^2p_0^0 + ^2D_0^0 \) transition in atomic nitrogen, but after about 50 seconds (i.e., 140 seconds after detonation) the energy loss rate is about a factor of ten below that for the oxygen red line. For this particular calculation, other transitions and species are relatively unimportant to the cooling process.

The fraction of available energy tied up in excited states is seen in Figure 19 to peak at about 45%, a value substantially larger than found in previous calculations. This large fraction occurs because the ratio of atoms to free electrons is large (-100), and the electrons have sufficient thermal energy to populate the excited states. Thus, nearly half the available energy is rapidly stored as excited state energy.

The calculation depicted in Figure 20 corresponds to conditions extracted from Fajen's Starfish simulation at 90 seconds after burst at 550 km altitude. In this case the electron density and neutral atom densities are nearly equal. The \( O^+ \) density is about a factor of 2 larger than the \( N^+ \) density, while the \( O \) density is about a factor of 3 larger than the \( N \) density. Molecular oxygen is a minor constituent. Although both ion and electron temperatures were about 1.5 eV initially, very rapid collisional processes caused these temperatures almost instantly to drop to about an eV. In conjunction, we note that the fraction of available energy in excited states peaks at nearly 18% quite early in the calculation. It's also interesting to observe that except for \( N \) and \( O_2 \), the population densities of the first excited states of the species reach 10% of the density of the respective ground states. For \( N \) and \( O_2 \), the first excited state populations reach about 25% of the respective ground state densities.

The combined action of the ionic and atomic radiators, all of which are radiating at roughly the same rate, is to remove about 59% of the initial energy over the 1000 second time span. (Keep in mind that
Figure 20. Radiation properties based on the 90 second environment at 550 km altitude in Fajen's Starfish calculation.
Figure 20 (Continued)
Figure 20 (Continued)
Figure 20 (Continued)
Figure 20 (Continued)
Figure 20 (Continued)
these calculations do not include effects of fluid motion, deionization chemistry, etc., which would act in a complete and self-consistent calculation during the 1000 second span to alter the available thermal energy and, hence, the radiation rate.) Radiation from molecular oxygen is negligible, from the cooling standpoint, because the O₂ density is so low.

In order to investigate radiation cooling and energy partition long after a nuclear detonation, we consider the high altitude environment predicted by a detailed, two-fluid numerical simulation of a megaton-range explosion at 200 km altitude. Calculations depicted in Figure 21 and 22 represent, at time zero, species densities and temperatures extracted from the detailed simulation at 60 minutes after detonation. These radiation computations span almost 3 hours.

The calculation presented in Figure 21 represents the environment at 850 km altitude within a dense portion of the geomagnetic field aligned fireball/plume. As indicated in Table 2, the electron density is slightly above 10⁸ cm⁻³, and the predominant species are ions. Ion and electron temperatures were both initialized to 0.504 eV at the beginning of the radiation cooling calculation. One finds that this system almost instantaneously attains a quasi-steady state with only a bit more than one percent of the available energy associated with excited states. An examination of radiation rate curves reveals that nitrogen ions are the most active radiators. In fact, N⁺ transitions radiate, over 10,000 seconds, more energy than all of the other species combined; about 30% of the initial energy is radiated during this interval.

The final case to be considered is shown in Figure 22 and represents conditions extracted from the aforementioned simulation at 60 minutes after detonation. This set of species and temperatures represents the environment at 1000 km altitude in a region within the geomagnetic field aligned fireball/plume plasma but outside of its dense core. Ionic
Figure 21. Radiation properties based on the 60 minute environment at 850 km altitude in a calculation of a megaton-range nuclear explosion at 200 km altitude.
Figure 21 (Continued)
Figure 21 (Continued)
Figure 21 (Continued)
Figure 21 (Continued)
Figure 21 (Continued)
Figure 22. Radiation properties based on the 60 minute environment at 1000 km altitude in a calculation of a megaton-range nuclear explosion at 200 km altitude.
Figure 22 (Continued)
Figure 22 (Continued)
Figure 22 (Continued)

91
Figure 22 (Continued)

O₂ STATE DENSITIES

DENSITY (cm⁻³)

O₂(³P)

O₂(⁴S)

O₂(⁴Σ)

O₂ RADIATION COOLING RATES

RADIATION RATE (eV/cm²/sec)

O₂(Δ→Σ)

O₂(Π→Σ)

TIME (seconds)
Figure 22 (Continued)
and atomic species all have nearly equal densities of about $10^6$ cm$^{-3}$, and molecular oxygen is present only as a very minor species. The initial ion and electron temperatures have values of 0.393 eV, so this case describes plasma which is initially much cooler than that in previous cases. The radiation cooling curves indicate that, at these low temperatures, nitrogen ions and oxygen atoms are the effective radiators. In both species, it is the red lines which account for the cooling. In view of the low temperatures and approximate equality between electron and radiating species densities, it's not surprising that at most about one percent of the available energy was contained in excited states. The temperature curves indicate that about 17% of the initial energy was radiated over the 10,000 second period.
SECTION 4
DISCUSSION AND CONCLUSIONS

The sample calculations of the preceding section rather conclu-
sively demonstrate that, on a time scale of hours, forbidden line radia-
tion from low lying metastable states of atmospheric constituents can
remove substantial fractions of the available thermal energy. From the
standpoint of computing the behavior and decay of fireball plasma from a
high altitude nuclear explosion, a process, such as radiation cooling,
which significantly changes the ion and electron temperatures may be quite
important. In addition to altering temperature dependent deionization
chemistry rate coefficients and the ion-electron scale height, radiation
cooling may result in a reduction in the diamagnetic levitation of a
plasma in the geomagnetic field. This last effect derives from the fact
that ion-electron thermal energy drives a system of electrical currents
within the plasma which interact with the geomagnetic field and cause the
plasma to move, transverse to the field, toward a region of reduced field
(i.e., generally upward).

The results presented are a bit artificial in the sense that
they represent the response of an initially cold system of particles to a
delta-function heating pulse at zero time. In a more realistic calcula-
tion, the system at some non-zero initial temperature would be subject to
non-instantaneous heating (and cooling) as the result of hydrodynamic
evolution. Nevertheless, the results provide a basis for estimating
e-folding time constants for cooling and for particular forbidden line
radiation rates under a variety of conditions. Although most of these
forbidden lines are in the visible, a few are in the ultraviolet and short
wavelength infrared.
Earlier, in Section 2, it was pointed out that excited state populations and radiation rates do not scale in a simple way with electron density. The mathematical statement of the scaling under quasi-steady conditions was presented in Equation 13, and the computed results nicely demonstrate the variation of excited populations with electron density under more general conditions. The intertwining of temperature dependent excitation and deexcitation rate coefficients and radiative transition probabilities makes it difficult to sort out the significance of individual line radiations relative to the others without doing quite a bit of work.

A very interesting result of the calculations concerns the partition of available energy between excited state and thermal energies. The computations indicate that when the temperature is an electron volt or lower, and when the electron density is comparable to or exceeds the density of radiating species, then the fraction of available energy tied up in excited states is -10% or less. However, if the radiating species density substantially exceeds the electron density (e.g., far more N or O atoms than electrons), then a large fraction of the available energy may go to producing excited states, even if the temperature is fairly low (<0.4 eV). Under such circumstances, fluid dynamical calculations which compute ion-electron pressures without accounting for thermal energy which would be absorbed in the production of excited states will possibly miscompute pressure gradient forces and diamagnetic effects by perhaps a factor of two. One remedy for this problem would be to carry explicitly excited state populations. However, the present calculations indicate that at electron densities of greatest interest (10^6 cm^{-3} and larger), the quasi-steady state is attained rather rapidly. Therefore, it should be possible, in all but highly dynamic situations, to compute by the quasi-steady approximation the excited state populations without explicitly carrying them. Thus, standard fluid treatments could be improved by computing the energy tied up in excited states and by subtracting this.
energy from the thermal energy prior to a calculation of ion electron pressure or temperature.

In summary, it has been determined that high altitude nuclear burst simulations which span substantial time intervals (hours) need to include radiation cooling by forbidden line radiation. The quasi-steady state approximation, which avoids the necessity of carrying excited state densities explicitly, appears to be acceptable for all but highly dynamic problems. Furthermore, it has been shown that failure to account for the partition between excited state and thermal energies can introduce non-trivial errors into pressure and other temperature dependent terms of the magnetized fluid equations.
REFERENCES


25. Fajen, F. E., private communication.

APPENDIX

The following tables summarize electron impact and deexcitation rate coefficients for $O^+$, $N^+$, $O$, $N$, and $O_2$.

**TABLE A-1.† DEEXCITATION RATE COEFFICIENTS FOR THE LOW-LYING METASTABLE STATES OF $O^+$ ($T_e$ in eV)**

<table>
<thead>
<tr>
<th>Transition</th>
<th>Deexcitation Rate Coefficient (cm$^3$/sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2D^0 - 4S^0$</td>
<td>$1.3 \times 10^{-8} (T_e)^{-1/2}$</td>
</tr>
<tr>
<td>$2P^0 - 4S^0$</td>
<td>$6.3 \times 10^{-9} (T_e)^{-1/2}$</td>
</tr>
<tr>
<td>$2P^0 - 2D^0$</td>
<td>$2.4 \times 10^{-8} (T_e)^{-1/2}$</td>
</tr>
</tbody>
</table>

† From reference 13.

**TABLE A-2.† DEEXCITATION RATE COEFFICIENTS FOR THE LOW-LYING METASTABLE STATES OF $N^+$ ($T_e$ in eV)**

<table>
<thead>
<tr>
<th>Transition</th>
<th>Deexcitation Rate Coefficient (cm$^3$/sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1D - 3p$</td>
<td>$4.8 \times 10^{-8} (T_e)^{-1/2}$</td>
</tr>
<tr>
<td>$1S - 3p$</td>
<td>$3.2 \times 10^{-8} (T_e)^{-1/2}$</td>
</tr>
<tr>
<td>$1S - 1D$</td>
<td>$3.3 \times 10^{-8} (T_e)^{-1/2}$</td>
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</tbody>
</table>

† From reference 13.
### Table A-3. † Electron Impact Excitation and Deexcitation Rate Coefficients for the Low-Lying States of Atomic Oxygen.

<table>
<thead>
<tr>
<th>( T_e (eV) )</th>
<th>( ^3P - ^1D ) ( a )</th>
<th>( ^3P - ^1S )</th>
<th>( ^1D - ^1S )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>1.92 (-18) ( a )</td>
<td>1.78 (-28)</td>
<td>2.25 (-19) *</td>
</tr>
<tr>
<td>0.2</td>
<td>5.28 (-14)</td>
<td>1.96 (-19)</td>
<td>1.76 (-14)</td>
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<td>0.3</td>
<td>1.76 (-12)</td>
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<td>8.07 (-13)</td>
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<td>0.5</td>
<td>3.28 (-11)</td>
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<td>5.20 (-10)</td>
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<td>20.0</td>
<td>2.23 (-9)</td>
<td>3.7 (-10)</td>
<td>6.4 (-10)</td>
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</tbody>
</table>

* Numbers in parenthesis indicate the power of ten by which the entries are multiplied.

*\( a \) Excitation rate coefficient.

*\( b \) The corresponding deexcitation rate coefficient.

† From reference 13.
### TABLE A-4.† ELECTRON IMPACT EXCITATION AND DEEXCITATION RATE COEFFICIENTS FOR THE LOW-LYING STATES OF ATOMIC NITROGEN.

<table>
<thead>
<tr>
<th>( T_e (eV) )</th>
<th>( ^4S^0 - ^2D^0 )</th>
<th>( ^4S^0 - ^2p^0 )</th>
<th>( ^2D^0 - ^2p^0 )</th>
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<td>0.1</td>
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</tr>
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<td>2.34 (-9)</td>
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<td>1.0 (-8)</td>
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<td>1.8 (-9)</td>
<td>9.7 (-9)</td>
</tr>
</tbody>
</table>

* Numbers \( \times \) p enthesis indicate the power of ten by which the entries are multiplied.

\(^{a}\) Excitation rate coefficient.

\(^{b}\) The corresponding deexcitation rate coefficient.

† From reference 13.
### TABLE A-5. ELECTRON IMPACT DEEXCITATION RATE COEFFICIENTS FOR LOW-LYING STATES OF MOLECULAR OXYGEN

<table>
<thead>
<tr>
<th>$T_e$(eV)</th>
<th>$a^1\Delta_g + x^3\Sigma_g^-$</th>
<th>$b^1\Sigma^+ + x^3\Sigma_g^-$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>2.595 (-11)*</td>
<td>2.058 (-11)</td>
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<tr>
<td>0.2</td>
<td>8.968 (-11)</td>
<td>8.089 (-11)</td>
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<td>0.3</td>
<td>1.560 (-10)</td>
<td>1.575 (-10)</td>
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<tr>
<td>0.4</td>
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</tr>
<tr>
<td>0.5</td>
<td>2.989 (-10)</td>
<td>3.341 (-10)</td>
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<tr>
<td>0.6</td>
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<td>4.262 (-10)</td>
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<td>0.7</td>
<td>4.733 (-10)</td>
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<tr>
<td>0.8</td>
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<td>1.532 (-9)</td>
<td>1.242 (-9)</td>
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<td>2.0</td>
<td>1.687 (-9)</td>
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<td>8.0</td>
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<tr>
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<td>2.784 (-9)</td>
<td>1.596 (-9)</td>
</tr>
<tr>
<td>10.0</td>
<td>2.733 (-9)</td>
<td>1.548 (-9)</td>
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</tbody>
</table>

* Numbers in parenthesis indicate the power of ten by which the entries are multiplied.
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