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THESIS

A STATISTICAL ANALYSIS OF MONTHLY RAINFALL FOR MONTEREY PENINSULA AND THE CARMEL VALLEY IN CENTRAL CALIFORNIA

by

David Frederick Davis
March 1981

Thesis Advisor: P.A. Jacobs

Approved for public release; distribution unlimited
This thesis presents a statistical analysis of the monthly rainfall for the Monterey Peninsula and the Carmel Valley in Central California. The analysis begins with the simple first-order autoregressive Markov model, which is found to be weak. Next, 2x2 contingency tables are used to identify predictors, one of which is found to be January rainfall. Finally, logistic analysis is used to quantify the predictive ability.
of January.

This paper attempts to analyze rainfall time series in the statistical sense. No attempt is made to provide a physical explanation of the findings from the point of view of a meteorologist.
A Statistical Analysis of Monthly Rainfall for Monterey Peninsula and the Carmel Valley in Central California

by

David Frederick Davis
Captain, United States Army
B.S., Colorado School of Mines, 1972

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

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March 1981

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Second Reader

Chairman, Department of Operations Research

Dean of Information and Policy Sciences

3
ABSTRACT

This thesis presents a statistical analysis of the monthly rainfall for the Monterey Peninsula and the Carmel Valley in Central California. The analysis begins with the simple first-order autoregressive Markov model, which is found to be weak. Next, 2x2 contingency tables are used to identify predictors, one of which is found to be January rainfall. Finally, logistic analysis is used to quantify the predictive ability of January.

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I. INTRODUCTION

A. THE PROBLEM

The Monterey Peninsula Water Management District, in Central California coastal area has as one of its responsibilities the duty to recommend and/or impose water rationing on its constituents. To do this in a rational way requires the District to have some formula for predicting future water availability. Although the techniques of modern meteorology are becoming more sophisticated and exact there is still the inability to make good long-range predictions. This thesis analyzes three series of Monterey County monthly rainfall data by purely statistical methodology in order to identify possible predictive formulas.

B. NOTATION

Rainfall will be denoted as $R_{t,m}$ which will represent inches of rain recorded for the $t^{th}$ year and the $m^{th}$ month. The year to be used is the California Water Year which begins in October and ends the following September. Thus $R_{1,1}$ is the monthly rainfall for October of year '1' and $R_{6,8}$ is the monthly rainfall of May of year '6'.

An overstruck bar as in $\bar{R}$ will indicate the arithmetic average of a variable; in this case it is the arithmetic average of all years and months of rainfall. $\bar{R}_m$ is the average of rainfall over the years for month $m$; $\bar{R}_t$. 

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C. METHODS OF ANALYSIS

Three methods were used to analyze the data. The first method was to model the series using autoregressive moving averages as described in Box and Jenkins [Ref. 1]. The second was to use 2×2 contingency tables to identify possible predictors. The third was logistic regression to quantify the findings of the 2×2 contingency table analysis. These three methods will be described in further sections of this paper.

1. ARMA(p,q) Models

A widely used approach to time series modeling proposed by Box and Jenkins is the ARMA(p,q) model. This model is actually a joining of two types of model, the autoregressive and the moving average.

In the notation of Box and Jenkins:

let \( \{Z_t, t=1,2,...,n\} \) be a time series, then an ARMA(p,q) process may be written as:

\[
\tilde{Z}_t = \phi_1 \tilde{Z}_{t-1} + \cdots + \phi_p \tilde{Z}_{t-p} + a_t - \theta_1 a_{t-1} - \cdots - \theta_q a_{t-q}
\]

the \( \{a_t, t=1,2,...,n\} \) are assumed to be random shocks distributed as independent and identically distributed (iid) random variables with mean zero and variance \( \sigma_a^2 \) and \( \tilde{Z}_t = Z_t - \bar{Z} \). The further assumption of normality is also usually made.

For purposes of this paper, a mapping of \( R_{t,m} \) into \( Z_r, r=12(t-1)+m \) was made, and an ARMA analysis was
then conducted on this index transformed series. This analysis is described in section III.

2. **2x2 Table Analysis**

In the validation of section IV it is found that the ARMA model is not very successful in describing the data. In section V the data is analyzed by means of 2x2 contingency tables. These tables are good tools for exploratory data analysis in that they provide a visual display of the data. Statistical procedures based on the null hypothesis of independence can be used to quantify the departure from independence. The theory of 2x2 tables, and contingency tables in general may be found in Fleiss [Ref. 3], Dixon and Massey [Ref. 5], Brownlee [Ref. 6], and Mood, Graybill, and Boes [Ref. 7].

For this paper, the contingency table approach is used to identify a month or group of months of a year whose rainfall can serve as a predictor for the rainfall during the remaining months of the year. One predictor that was suggested is the rainfall in the month of January.

3. **Logistic Analysis**

Once a predictor is tentatively identified it becomes necessary to quantify the degree, direction and accuracy of the predictor.

A logistic analysis is conducted by dividing the data for a year into two sets, the predictor or control set, and predictand or complement set. For this analysis, the predictor
is the logged anomaly of January rainfall for the year; that is, if $X_t$ denotes the predictor or control for year $t$, then

$$X_t = \ln(R_t,4) - \frac{1}{N} \sum_{t=1}^{N} \ln(R_t,4) \quad (I.2)$$

(The logarithm is used to better symmetrize the model.) The complement is the raw anomaly of the total rainfall for the immediately subsequent eleven months; that is, if $Y'_t$ denotes the complement for year $t$, then;

$$Y'_t = \frac{12}{\sum_{m=5}^{12} R_{t,m} + \sum_{m=1}^{3} R_{t+1,m}} \quad (I.3)$$

Finally, the data are transformed into a binary representation, relative to zero as;

$$Y_t = \begin{cases} 0 & \text{if } Y'_t < 0 \\ 1 & \text{if } Y'_t > 0 \end{cases} \quad (I.4)$$

In section VI the model fit is

$$P(Y=1|X=x) = \frac{e^{a+\beta x}}{1 + e^{a+\beta x}} \quad (I.5)$$

Where $x$ is as before and $P(Y=1|X=x)$ is interpreted as: "the conditional probability that the subsequent eleven month total rainfall will be above its mean, given that the logged anomaly of January rainfall was 'x'".
II. THE DATA

A. GENERAL

Three data sets were used for this analysis. The location at which these data sets were gathered is shown in Figure 1. As the figure indicates, two of the data sets are on the Monterey Peninsula proper, while the third set, SC, represents the Carmel River Watershed at the San Clemente Dam.

Although data exists in all cases to the present, all three sets were truncated at September of 1974. The remaining data, up through September of 1980 was reserved for validation of the models and methodology.

The data coordinates are:

Data set RN: 36° 35' 42" North Latitude
121° 54' 43" West Longitude

Data set FL: 36° 35' 30" North Latitude
121° 56' 30" West Longitude

Data set SC: 36° 26' 12" North Latitude
121° 42' 30" West Longitude
Figure 1. Location of rainfall data sets and the years available.
B. DATA SET RN

Data set RN consists of monthly rainfall amounts gathered by Professor R.J. Renard, Cooperative Observer for the National Weather Service Climatological Station, Monterey, California. The data set begins in June 1951 and currently terminates in September 1980. As was stated above, the analysis was conducted only on that data between and including October 1951 and September 1974.

1. Raw Data

Appendix A contains a listing of data set RN. Figure 2 shows the raw data set. Month 1 is October 1951, month 148 is January 1964, and up to month 288 which is September 1974. As can be seen the data are strongly seasonal. This is enough to indicate that the series, as stated, is highly non-stationary.

The data presented so far deals with only monthly data. Next to be considered is the series of yearly total rainfalls. The results are shown in Figure 3 (Yearly total rainfall), 4 (Correlogram of yearly rainfall), and Table 1 (Estimated Autocorrelations). In this case, the correlogram indicates stationarity and independence of the yearly series. A plot of the lag one relationships, Figure 5, reinforces this indication of independence.
Figure 2. Monthly rainfall in inches for data set RN.
The correlograms and Partial Correlograms to follow indicate the 95% approximate significance levels using dashed lines. For development of these significance levels see Box and Jenkins [Ref. 1].

Figure 3. Yearly total rainfall for data set RN (1951 - 1974).
Figure 4. Correlogram of Yearly total rainfall for data set RN.

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Figure 5. Lag one plot of yearly rainfall data for data set RN.

2. Swept Data

Pierce [Ref. 9] and Hipel [Ref. 11] suggest various ways to remove the seasonality of data sets like RN, FL, and SC. The basic, and most straightforward of these methods is to remove the various monthly means. This is accomplished by the following replacement:

\[ R_{t,m}^{'} = R_{t,m} - \bar{R}_m \]

where \( \bar{R}_m \) represents the mean of the month \( m \).

One statistic that is a byproduct of the calculations of \( \bar{R}_m \) is \( S_m^2 \) defined as the estimated variance of the
monthly data points:

\[ S_m^2 = \frac{1}{N-1} \sum_{t=1}^{N} R_{t,m}^2 - NR_{m}^2; \]  

These statistics for data set RN are shown in Table 2, and illustrated in Figure 6. In the same way as the raw data mapped into a series, a series is created from \( \tilde{R}_{t,m} \) as:

\[ \tilde{z}_r = \tilde{R}_{t,m}, r = 12(t-1)+m \]

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<th>VARIANCE</th>
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<tr>
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Figure 6. Monthly means for data set RN
Figure 7. Monthly rainfall anomalies in inches for data set RN
Figure 8. Correlogram of the monthly rainfall anomalies for data set RN

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</tbody>
</table>
3. **Logged and Swept Data**

The data should now be stationary in the means. However, as seen in Table 2, the variances of monthly rainfall amounts are not homogeneous. Kilmartin [Ref. 10] discusses various transformations of the data to remove this heteroskedasticity. A plot of the variance versus mean, Figure 9 below, indicates that the logarithmic transform of the data might be useful.

![Plot of monthly variance against monthly means for data set RN](image)

**Figure 9.** Plot of monthly variance against monthly means for data set RN
Since the data contain zeros, the following modified logarithmic transformation is done

\[ R'_{t,m} = \ln(R_{t,m} + 1) - \frac{1}{N} \sum_{t=1}^{N} \ln(R_{t,m} + 1) \]  

where the effect of the addition of the one is mostly to preserve the mapping of zeros into zeros. A more in depth discussion of this transformation is found in Kilmartin. The mapping is performed again as before and \( R'_{t,m} \) and \( S'_{t,m} \) are calculated in a manner similar to II.6 and shown in Table 4 and Figures 10 and 11.

**TABLE 4**

MONTHLY MEANS AND VARIANCE FOR LOGGED DATA SET RN

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Figure 10. Monthly means of logged data set RN

Figure 11. Plot of monthly variance against monthly means for logged data set RN
These transformations, the logarithm followed by the removal of the monthly means of the logged data, result in the series listed in Appendix A and described in Figures 12 and 13 with Table 5.

These displays indicate that a suitably stationary series has been obtained. Other methods, such as differencing, scaling, and Box-Cox transformations, see Hipel [Ref. 11], were tried but with less success.

Figure 12a. Logged anomalies of monthly rainfall for data set RN. Months 1–148
Figure 12b. Logged anomalies of monthly rainfall for data set RN

Figure 13. Correlogram of logged anomalies of monthly rainfall from data set RN
TABLE 5

ESTIMATED AUTOCORRELATIONS OF LOGGED
ANOMALIES OF MONTHLY RAINFALL FROM
DATA SET RN

<table>
<thead>
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</table>

C. DATA SET FL

The label for these data derives from its location, Forest Lake, on the Monterey Peninsula, in Pebble Beach, California. Data set FL consists of monthly rainfall figures gathered by the California-American Water Company since 1896. Although this data set started quite early, the data prior to 1937 has frequent missing observations. Therefore, this data set is taken as October 1937 through September 1974, with October 1974 through September 1980 reserved for validation.

Analysis of this data set is identical to that of data set RN, therefore only the pertinent figures and tables are shown.
Figure 14a. Months 1 - 296 of rainfall in inches for data set FL
Figure 14b. Months 297-444 of rainfall in inches for data set FL

Figure 15. Yearly total rainfall for data set FL (1937 - 1974).
Figure 16. Correlogram of yearly total rainfall for data set FL

TABLE 6
ESTIMATED AUTOCORRELATIONS OF YEARLY TOTAL RAINFALL FOR DATA SET FL

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2. Swept Data

TABLE 7
MONTHLY MEANS AND VARIANCE FOR DATA SET FL

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Figure 17. Monthly means for data set FL
Figure 18a. Months 1 - 296 of rainfall anomalies in inches for data set FL
Figure 18b. Months 297-444 of rainfall anomalies in inches for data set FL

Figure 19. Correlogram of monthly rainfall anomalies for data set FL
### TABLE 8

**ESTIMATED AUTOCORRELATIONS OF MONTHLY RAINFALL ANOMALIES FOR DATA SET FL**

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3. **Logged and Swept Data**

![Figure 20. Plot of monthly variance against monthly means for data set FL](image)

*Figure 20. Plot of monthly variance against monthly means for data set FL*
TABLE 9
MONTHLY MEANS AND VARIANCE FOR LOGGED DATA SET FL

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Figure 21. Monthly means of logged data set FL
Figure 22. Plot of monthly variance against monthly means for logged data set FL

Figure 23a. Months 1 - 148 of logged rainfall anomalies for data set FL
Figure 23b. Months 149 - 444 of logged rainfall anomalies from data set FL.
Figure 24. Correlogram of logged anomalies of monthly rainfall from data set FL.

<table>
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TABLE 10

ESTIMATED AUTOCORRELATIONS OF LOGGED ANOMALIES FROM MONTHLY RAINFALL OF DATA SET FL
D. DATA SET SC

The label for this data derives for its location, San Clemente Dam, on the Carmel River in Central California, approximately 26 kilometers southeast of data sets RN and FL on the Monterey Peninsula. Data set SC consists of monthly rainfall figures gathered by the California-American Water Company since 1926.

Analysis of this data set is again very close to that of the previous data sets and only the displays will be given.

1. Raw Data

Figure 25a. Months 1 (October 1926) - 148 (January 1938) of rainfall in inches for data set SC.
Figure 25b. Months 149 - 444 of rainfall for data set SC
Figure 25c. Months 445 - 576 of rainfall for data set SC

Figure 26. Yearly total rainfall for data set SC (1926 - 1974)
Figure 27. Correlogram of yearly total rainfall for data set SC

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TABLE 11
ESTIMATED AUTOCORRELATIONS OF YEARLY TOTAL RAINFALL FOR DATA SET SC
2. Swept Data

TABLE 12
MONTHLY MEANS AND VARIANCES
FOR DATA SET SC

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<td>.017</td>
<td>.0055</td>
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<tr>
<td>12</td>
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Figure 28. Monthly means for data set SC
Figure 29a. Months 1 - 296 anomalies in inches for data set SC
Figure 29b. Months 297 - 576 anomalies in inches for data set SC
Figure 30. Correlogram of monthly rainfall anomalies for data set SC

TABLE 13

ESTIMATED AUTOCORRELATIONS OF MONTHLY RAINFALL ANOMALIES FOR DATA SET SC

<table>
<thead>
<tr>
<th>LAG</th>
<th>VALUE</th>
<th>LAG</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
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<td>2</td>
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<td>.012</td>
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<td>.015</td>
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<td>18</td>
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<td>6</td>
<td>-.019</td>
<td>19</td>
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<td>23</td>
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<td>.014</td>
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<td>.011</td>
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<td>.051</td>
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<tr>
<td>13</td>
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<td></td>
</tr>
</tbody>
</table>

59
3. **Logged and Swept Data**

![Figure 31. Plot of monthly variance against anomaly means for data set SC.](image)

**TABLE 14**

MONTHLY MEANS AND VARIANCES OF LOGGED DATA SET SC

<table>
<thead>
<tr>
<th>MONTH</th>
<th>MEAN</th>
<th>VARIANCE</th>
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</thead>
<tbody>
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<td>.1623</td>
</tr>
<tr>
<td>2</td>
<td>.961</td>
<td>.3999</td>
</tr>
<tr>
<td>3</td>
<td>1.408</td>
<td>.3949</td>
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<tr>
<td>4</td>
<td>1.583</td>
<td>.3117</td>
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<tr>
<td>5</td>
<td>1.444</td>
<td>.4928</td>
</tr>
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</tr>
<tr>
<td>7</td>
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<td>.0726</td>
</tr>
<tr>
<td>9</td>
<td>.092</td>
<td>.0227</td>
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<tr>
<td>10</td>
<td>.015</td>
<td>.0040</td>
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<td>11</td>
<td>.031</td>
<td>.0083</td>
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<tr>
<td>12</td>
<td>.075</td>
<td>.0351</td>
</tr>
</tbody>
</table>
Figure 32. Monthly means of logged data set SC

Figure 33. Plot of monthly variance against monthly means for logged data set SC
Figure 34a. Months 1 - 296 of logged rainfall anomalies from data set SC
Figure 34b. Months 297 - 576 of logged rainfall anomalies from data set SC
Figure 35. Correlogram of logged anomalies of monthly rainfall from data set SC

TABLE 15

ESTIMATED AUTOCORRELATION OF LOGGED ANOMALIES OF MONTHLY RAINFALL FROM DATA SET SC

<table>
<thead>
<tr>
<th>LAG</th>
<th>VALUE</th>
<th>LAG</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.096</td>
<td>14</td>
<td>-.057</td>
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<tr>
<td>2</td>
<td>-.065</td>
<td>15</td>
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<td>3</td>
<td>-.066</td>
<td>16</td>
<td>-.023</td>
</tr>
<tr>
<td>4</td>
<td>.038</td>
<td>17</td>
<td>.021</td>
</tr>
<tr>
<td>5</td>
<td>.012</td>
<td>18</td>
<td>-.017</td>
</tr>
<tr>
<td>6</td>
<td>-.061</td>
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<td>-.005</td>
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<tr>
<td>7</td>
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<tr>
<td>8</td>
<td>-.001</td>
<td>21</td>
<td>-.011</td>
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<tr>
<td>9</td>
<td>-.056</td>
<td>22</td>
<td>.092</td>
</tr>
<tr>
<td>10</td>
<td>-.021</td>
<td>23</td>
<td>-.019</td>
</tr>
<tr>
<td>11</td>
<td>.007</td>
<td>24</td>
<td>.050</td>
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<tr>
<td>12</td>
<td>.091</td>
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<tr>
<td>13</td>
<td>.091</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
III. FIRST ORDER MARKOV MODEL

A. THEORY

As first shown by equation I.1, the general ARMA(p,q) model is:

$$\tilde{z}_t = \phi_1 \tilde{z}_{t-1} + \cdots + \phi_p \tilde{z}_{t-p} + \alpha_t - \theta_1 \alpha_{t-1} - \cdots - \theta_q \alpha_{t-q} \quad \text{III.1}$$

The development and discussion of this type of model is contained in detail in Box and Jenkin [Ref. 1] and Nelson [Ref. 8]. The modeling process is a three fold procedure. The parts are:

1. Identification
2. Estimation
3. Diagnosis.

Identification is conducted using the correlogram and a plot of the partial-autocorrelations (or partial correlogram). The partial autocorrelations are related to the autocorrelations, see Box and Jenkins [Ref. 1], Nelson [Ref. 8], or Richards and Woodall [Ref. 12]. These partial autocorrelations are used to determine the order of the moving average process much like the autocorrelations may be used to determine the order of the auto-regressive process.

Once the autocorrelations and partial autocorrelations have been found, the degree of the ARMA may be estimated by
techniques described in Box and Jenkins, Nelson or Richards and Woodall. Each of the data sets, once logged and swept, indicated that the most probable model was an ARMA(1,0) or AR(1) or more commonly a first-order autoregressive Markov model. This model is simply;

\[ \tilde{Z}_t = \rho \tilde{Z}_{t-1} + a_t \]  

where the \( \rho \) is the autocorrelation of lag one. Thus, this model indicates that any persistence in the data are conditionally independent of the past given the lag one value.

Subsections B, C, and D below show this model as applied to the three data sets of interest. The residuals of the model \( \tilde{Z}_t - \rho \tilde{Z}_{t-1} \) are examined. The residuals appear to be independent, however, they do not appear to be normally distributed; for example, there is a high peak around zero.

One possible reason for this discrepancy may be the dichotomy of winter and summer rain as indicated in Tables 2, 4, 7, 9, 12, and 14. The existence of months with zero rainfall during the summer suggests that one should consider the summer, when rain is sparse, completely separate from the winter when rain is more abundant. Therefore, also shown in the subsections below is the autoregressive model applied to the winter months only. This is accomplished by stripping out months 9 through 12 (June through September) of the data sets and treating the remaining data as a continuous set. In other words, the first ten months are then

\[ R_{1,1}', R_{1,2}', R_{1,3}', R_{1,4}', R_{1,5}', R_{1,6}', R_{1,8}', R_{2,1}', R_{2,2}' \]
The appropriate correlograms and partial correlograms are displayed prior to the model applications.

B. DATA SET RN

1. Twelve Month Series

This data set is described in section II.b. The remaining diagnostic device needed is the partial correlogram of Figure 36 and the corresponding values in Table 16.

![Partial Correlogram](image)

Figure 36. Partial correlogram of the logged rainfall anomalies of data set RN
TABLE 16
ESTIMATED PARTIAL-AUTOCORRELATIONS FOR
LOGGED RAINFALL ANOMALIES OF DATA SET RN

<table>
<thead>
<tr>
<th>LAG</th>
<th>VALUE</th>
<th>LAG</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
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<td>-.040</td>
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<td>5</td>
<td>.006</td>
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<td>19</td>
<td>.039</td>
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<tr>
<td>7</td>
<td>.037</td>
<td>20</td>
<td>.012</td>
</tr>
<tr>
<td>8</td>
<td>-.034</td>
<td>21</td>
<td>-.001</td>
</tr>
<tr>
<td>9</td>
<td>-.028</td>
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<td>-.034</td>
</tr>
<tr>
<td>13</td>
<td>.047</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The model of interest is then
\[ \tilde{z}_t = 0.191 \tilde{z}_{t-1} + \alpha_t \]  
III.3

where the random shocks \( \{\alpha_t\} \) are assumed to be distributed iid \( N(0, \sigma_a^2) \) and \( \sigma_a^2 \) is estimated as
\[
\frac{1}{N-1} \sum_{t=1}^{N} (\tilde{z}_t - 0.191 \tilde{z}_{t-1})^2
\]  
III.4

The goodness of this fit may be viewed in two ways. Firstly, are the residuals, \( \{\alpha_t\} \) independent? Secondly, are the residuals distributed as Normal (Gaussian) random variables? A plot of the residuals follows in Figure 37. The question of independence is addressed in Figure 38 (Correlogram), Figure 39 (Lag one plot), Figure 40 (Residuals vs. lag one), and Table 17 (Turning points). For a discussion of the usefulness of the turning points see Kendall [Ref. 14].
All of these displays and tests tend to indicate that the residuals are in fact serially independent. The statistics of the residuals are in Table 18. A Normal Plot of the residuals (Figure 41), in which the sample is normalized by removing the mean and scaling by the standard deviation and then plotted on normal paper, should yield a nearly straight line corresponding to the dashed line of the figure. The Normal Plot accompanied by the sample histogram (Figure 42) addresses the normality of these data. As may be seen from the kurtosis, the fluctuations of the sample CDF near the midpoint, and the peak of the histogram, the normality of this data are questionable. To confirm this a chi-squared goodness of fit test was conducted yielding a value of 49.18 with 17 degrees of freedom, again rejecting any hypothesis of normality at a significance level of $5 \times 10^{-5}$.

![Figure 37. First order Markov residuals from logged rainfall anomalies of data set RN. Months 149 - 292](image)
Figure 37b. First order Markov residuals from logged rainfall anomalies of data set RN. Months 149 - 292
Figure 38. Auto correlations of residuals from first order Markov process applied to the logged rainfall anomalies of data set RN

Figure 39. Lag one plot of first order Markov residuals from logged rainfall anomalies of data set RN
Figure 40. First order Markov residuals versus lag one data point from logged rainfall anomalies of data set RN

TABLE 17
ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FOR THE FIRST ORDER MARKOV RESIDUALS FROM THE LOGGED RAINFALL ANOMALIES OF DATA SET RN

NUMBER OF TURNING POINTS = 191
E[P] = 190.667  V[P] = 15.899

PHASE LENGTHS

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<th>OBS.</th>
<th>E[*]</th>
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<td>0</td>
<td>0.0</td>
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</table>
### TABLE 18
**GENERAL STATISTICS OF FIRST ORDER MARKOV RESIDUALS FROM LOGGED RAINFALL ANOMALIES OF DATA SET RN**

#### Moments

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Value</th>
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<tbody>
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<td>Mean</td>
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<td>Variance</td>
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<tr>
<td>Skewness</td>
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<tr>
<td>Kurtosis</td>
<td>.523</td>
</tr>
</tbody>
</table>

#### Percentiles

<table>
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<th>Value</th>
</tr>
</thead>
<tbody>
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<td>-.463</td>
</tr>
<tr>
<td>Lower Quartile</td>
<td>-.174</td>
</tr>
<tr>
<td>Median</td>
<td>-.014</td>
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<tr>
<td>Upper Quartile</td>
<td>.211</td>
</tr>
<tr>
<td>Upper Eight</td>
<td>.436</td>
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<tr>
<td>Upper Sixteenth</td>
<td>.706</td>
</tr>
<tr>
<td>Maximum</td>
<td>1.246</td>
</tr>
</tbody>
</table>

**Figure 41.** Standardized normal plot of first order Markov residuals from logged rainfall anomalies of data set RN
Figure 42. Histogram of first order Markov residuals from logged rainfall anomalies of data set RN

2. Winter Series

As stated above, the number of summer months with zeros indicated that a look at the winter months only might be worthwhile. The Figures 43 (Winter months), 44 (Correlogram), and 45 (Partial correlogram), which deal only with winter months, still indicate a first order autoregressive Markov model as:

\[ \tilde{z}_t = 0.218 \tilde{z}_{t-1} + a_{t-1} \]  

III.5
Figure 43. Winter months only of logged rainfall anomalies of data set RN
Figure 44. Correlogram of winter months only of logged rainfall anomalies from data set RN

Figure 45. Partial autocorrelations of winter months only logged rainfall anomalies from data set RN
Now, as with the full twelve month model, a look at the residuals yields the Figures 46 (Residuals), 47 (Correlogram), and 48 (Lag one plot), 49 (Residuals vs. lag one), and Table 19 (Turning points). It appears that the residuals are, in fact, independent. This is similar to the twelve month model.

The question of the normality of the residuals is addressed by Table 19 and Figures 50 (Normal plot) and 51 (Histogram). The results of these plots and a basic chi-squared goodness of fit of 22.11 with 17 degrees of freedom indicate that this winter month data set is much more normal than was its twelve month counterpart. This chi-squared value is significant at the .181 level.

Figure 46a. First order Markov residuals of logged rainfall anomalies for winter months only of data set RN. Years 1 - 12
Figure 46b. First order Markov residuals of logged rainfall anomalies for winter months only of data set RN. Years 12 - 24
Figure 47. Correlogram of first order Markov residuals of logged rainfall anomalies for winter months only of data set RN

Figure 48. Lag one plot of first order Markov residuals from logged rainfall anomalies for winter months only of data set RN
Figure 49. First order Markov residuals versus lag one data point from lagged rainfall anomalies of winter month only data from data set RN

TABLE 19

ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FIRST ORDER MARKOV RESIDUALS OF THE LOGGED RAINFALL ANOMALIES OF DATA SET RN

NUMBER OF TURNING POINTS = 129
E[P] = 126.667  V[P] = 15.84

PHASE LENGTHS

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<th>OBS.</th>
<th>E[*]</th>
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<td>9.9</td>
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<tr>
<td>7</td>
<td>0</td>
<td>0.0</td>
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</table>
**TABLE 20**

**GENERAL STATISTICS OF FIRST ORDER MARKOV RESIDUALS FROM LOGGED RAINFALL ANOMALIES OF DATA SET RN**

**Moments**

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>-0.001</td>
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<tr>
<td>Variance</td>
<td>0.247</td>
</tr>
<tr>
<td>Skewness</td>
<td>-0.161</td>
</tr>
<tr>
<td>Kurtosis</td>
<td>-0.521</td>
</tr>
</tbody>
</table>

**Percentiles**

<table>
<thead>
<tr>
<th>Percentile</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum</td>
<td>-1.148</td>
</tr>
<tr>
<td>Lower Sixteenth</td>
<td>-0.845</td>
</tr>
<tr>
<td>Lower Eight</td>
<td>-0.616</td>
</tr>
<tr>
<td>Lower Quartile</td>
<td>-0.368</td>
</tr>
<tr>
<td>Median</td>
<td>0.025</td>
</tr>
<tr>
<td>Upper Quartile</td>
<td>0.339</td>
</tr>
<tr>
<td>Upper Eight</td>
<td>0.591</td>
</tr>
<tr>
<td>Upper Sixteenth</td>
<td>0.762</td>
</tr>
<tr>
<td>Maximum</td>
<td>1.078</td>
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---

**Figure 50.** Standardized normal plot of first order Markov residuals from logged rainfall anomalies of winter months only from data set RN.
Figure 51. Histogram of first order Markov residuals from logged rainfall anomalies of winter month only of data set RN

C. DATA SET FL

As in the previous section on the data sets, the analysis of section III.B above carries forward fairly well to data sets FL and SC. This section, and the following, contain only the Figures and Tables corresponding to those in the previous section on data set RN.
1. Twelve Month Series

![Partial correlogram of the logged rainfall anomalies for data set FL](image)

Figure 52. Partial correlogram of the logged rainfall anomalies for data set FL

**TABLE 21**

**ESTIMATED PARTIAL AUTOCORRELATIONS FOR \( \text{LOGGED RAINFALL ANOMALIES OF DATA SET FL} \)**

<table>
<thead>
<tr>
<th>LAG</th>
<th>VALUE</th>
<th>LAG</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
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<td>14</td>
<td>-0.072</td>
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<tr>
<td>2</td>
<td>-0.057</td>
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<td>0.011</td>
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<td>-0.069</td>
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<td>4</td>
<td>0.077</td>
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<td>0.027</td>
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<td>0.018</td>
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<td>0.022</td>
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<td>-0.025</td>
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<td>0.081</td>
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<td>0.067</td>
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<td>0.012</td>
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<tr>
<td>13</td>
<td>0.055</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[ \tilde{z}_t = 0.185 \tilde{z}_{t-1} + a_t \]  

III.6

83
Figure 53a. First order Markov residuals from logged rainfall anomalies of data set FL. Months 1 - 296
Figure 53b. First order Markov residuals from logged rainfall anomalies of data set FL. Months 297 - 444.

Figure 54. Autocorrelations of residuals from first order Markov process applied to the logged rainfall anomalies of data set FL.
Figure 55. Lag one plot of first order Markov residuals from logged rainfall anomalies of data set FL

Figure 56. First order Markov residuals versus lag one data points from logged rainfall anomalies of data set FL
TABLE 22

ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FIRST ORDER MARKOV RESIDUALS FROM DATA SET FL

NUMBER OF TURNING POINTS = 294

PHASE LENGTHS

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<td>293.7</td>
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</table>

TABLE 23

GENERAL STATISTICS OF FIRST ORDER MARKOV RESIDUALS FROM LOGGED RAINFALL ANOMALIES OF DATA SET FL

Moments

Mean .000
Variance .163
Skewness -.044
Kurtosis .717

Percentiles

Minimum -1.276
Lower Sixteenth -.702
Lower Eight -.426
Lower Quartile -.156
Median .012
Upper Quartile .184
Upper Eight .481
Upper Sixteenth .648
Maximum 1.124
Figure 57. Standardized normal plot of first order Markov residuals from logged rainfall anomalies of data set FL.

Figure 58. Histogram of first order Markov residuals from logged rainfall anomalies of data set FL.
This data set yielded a chi-square value of 107.66 for 17 degrees of freedom. The significance of the value is in the zero plus range.

2. Winter Series

Figure 59a. Years 1 - 12 of winter months only of logged rainfall anomalies of data set FL.
Figure 59b. Years 13 - 37 of winter months only, logged rainfall anomalies of data set FL
Figure 60. Correlogram of winter months only, logged rainfall anomalies from data set FL.

These displays indicate a model like

\[ \tilde{Z}_t = 0.199 \tilde{Z}_{t-1} + a_t. \]
Figure 62a. Years 1 - 24, first order Markov residuals of logged rainfall anomalies for winter months only, data set FL
Figure 62b. Years 25 - 37, first order Markov residuals of logged rainfall anomalies for winter months only, data set FL

Figure 63. Correlogram of first order Markov residuals of lagged rainfall anomalies from winter months only, data set FL
Figure 64. Lag one plot of first order Markov residuals from logged rainfall anomalies of winter months only, data set FL

Figure 65. First order Markov residuals versus lag one data point from logged rainfall anomalies of winter months only, data set FL
TABLE 24

ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FIRST ORDER MARKOV RESIDUALS OF THE LOGGED RAINFALL ANOMALIES OF DATA SET FL

NUMBER OF TURNING POINTS = 209
\( E[P] = 196 \)
\( V[P] = 15.902 \)

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<td>8</td>
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TABLE 25

GENERAL STATISTICS OF FIRST ORDER MARKOV RESIDUALS FROM LOGGED RAINFALL ANOMALIES OF WINTER MONTHS ONLY, DATA SET FL

Moments

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<table>
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<td>Kurtosis</td>
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</table>

Percentiles

<p>| | |</p>
<table>
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</thead>
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<td>Lower Sixteenth</td>
<td>-.798</td>
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<tr>
<td>Lower Eight</td>
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<tr>
<td>Lower Quartile</td>
<td>-.315</td>
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<tr>
<td>Median</td>
<td>.011</td>
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<tr>
<td>Upper Quartile</td>
<td>.323</td>
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<tr>
<td>Upper Eight</td>
<td>.551</td>
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<td>Upper Sixteenth</td>
<td>.748</td>
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<tr>
<td>Maximum</td>
<td>1.136</td>
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A STATISTICAL ANALYSIS OF MONTHLY RAINFALL FOR MONTEREY PENINSULA...
Figure 66. Standardized normal plot of first order Markov residuals from logged rainfall anomalies of winter months only, data set FL

Figure 67. Histogram of first order Markov residuals from logged rainfall anomalies of winter months only, data set FL
The chi-squared was calculated at 15.35 for 17 degrees of freedom. This is a significance level of .570, thus indicating possible normality.

D. DATA SET SC

1. Twelve Month Series

![Partial correlogram of the logged anomalies for data set SC]

Figure 68. Partial correlogram of the logged anomalies for data set SC
### TABLE 26

**ESTIMATED PARTIAL AUTOCORRELATIONS FOR LOGGED RAINFALL ANOMALIES OF DATA SET SC**

<table>
<thead>
<tr>
<th>LAG</th>
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<th>LAG</th>
<th>VALUE</th>
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<td>.007</td>
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<td>-.014</td>
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<td>-.061</td>
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<td>.004</td>
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<td>.042</td>
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<td>8</td>
<td>-.016</td>
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<tr>
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<td>24</td>
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<tr>
<td>13</td>
<td>.084</td>
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This information yields the model as

$$z'_t = .096z'_{t-1} + a_t.$$  

**DATA IS FROM SOLEIN**

![Figure 69a. First order Markov residuals from logged rainfall anomalies of data set SC. Months 1 - 148.](image-url)
Figure 69b. First order Markov residual from logged rainfall anomalies of data set SC. Months 149 - 444
Figure 69c. First order Markov residual from logged rainfall anomalies of data set SC. Months 445 - 596.

Figure 70. Autocorrelations of residuals from first order Markov process applied to the logged rainfall anomalies of data set SC.
Figure 71. Lag one plot of first order Markov residuals from logged rainfall anomalies of data set SC.

Figure 72. First order Markov residuals versus lag one data points from logged rainfall anomalies of data set SC.
### TABLE 27

**ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FIRST ORDER MARKOV RESIDUALS OF DATA SET SC**

**NUMBER OF TURNING POINTS** = 367  
**E[P] = 382.667**  
**V[P] = 15.9**

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<td>381.7</td>
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### TABLE 28

**GENERAL STATISTICS OF FIRST ORDER MARKOV RESIDUALS FROM LOGGED RAINFALL ANOMALIES OF DATA SET SC**

<table>
<thead>
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<th>Moments</th>
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<tr>
<td>Mean</td>
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<tr>
<td>Variance</td>
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<td>Skewness</td>
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<td>Kurtosis</td>
<td>.805</td>
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<table>
<thead>
<tr>
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<td>Lower Sixteenth</td>
<td>-.744</td>
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<td>Lower Eight</td>
<td>-.462</td>
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<td>Lower Quartile</td>
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<td>Median</td>
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<td>Upper Quartile</td>
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<td>Upper Eight</td>
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<td>Upper Sixteenth</td>
<td>.783</td>
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<tr>
<td>Maximum</td>
<td>1.344</td>
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</table>

102
Figure 73. Standardized normal plot of first order Markov residuals from logged rainfall anomalies of data set SC

Figure 74. Histogram of first order Markov residuals from logged rainfall anomalies of data set SC
This data set yielded a chi-square value of 273.95 for 17 degrees of freedom. This is equivalent to a significance of zero plus.

2. Winter Series

Figure 75a. Years 1 - 12 of winter months only, logged rainfall anomalies of data set SC.
Figure 75b. Years 13 - 36 of winter months only, logged rainfall anomalies of data set SC
Figure 75c. Years 37 - 48 of winter months only, logged rainfall anomalies of data set SC

Figure 76. Correlogram of winter months only, logged rainfall anomalies from data set SC
Figure 77. Partial correlogram of winter months only, logged rainfall anomalies from data set SC

This information indicates the model

\[ \tilde{z}_t = 0.107 \tilde{z}_{t-1} + a_t. \]
Figure 78a. Years - 24 first order Markov residuals of logged rainfall anomalies, for winter months only, data set SC
Figure 78b. Years 25 - 48, first order Markov residuals of logged rainfall anomalies for winter months only, data set SC.
Figure 79. Correlogram of first order Markov residuals of logged rainfall anomalies from winter months only, data set SC.

Figure 80. Lag one plot of first order Markov residuals from logged rainfall anomalies of winter months only, data set SC.
Figure 81. First order Markov residuals versus lag one data point from logged rainfall anomalies of winter months only, data set SC

**TABLE 29**

**ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FIRST ORDER MARKOV RESIDUALS OF THE LOGGED RAINFALL ANOMALIES OF THE WINTER MONTHS ONLY, DATA SET SC**

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<td>10</td>
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<tr>
<td>TOTALS</td>
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### Table 30

**General Statistics of First Order Markov Residuals from Logged Rainfall Anomalies of Winter Months Only, Data Set SC**

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<td>Skewness</td>
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<table>
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<tr>
<td>Lower Eight</td>
<td>-0.663</td>
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<tr>
<td>Lower Quartile</td>
<td>-0.359</td>
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<tr>
<td>Median</td>
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<td>Upper Quartile</td>
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<td>0.882</td>
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<tr>
<td>Maximum</td>
<td>1.338</td>
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</table>

**Figure 82.** Standardized normal plot of first order Markov residuals from logged rainfall anomalies of winter months only, data set SC
Figure 83. Histogram of first order Markov residuals from logged rainfall anomalies of winter months only, data set SC

The chi-square was calculated at 16.60 for 17 degrees of freedom. This is significant at the .482 level thus indicating probable normality.
IV. VALIDATION OF FIRST ORDER MARKOV MODELS

A. THEORY

The general model proposed by a first order Markov process is, as stated before;

$$\tilde{z}_t = \rho \tilde{z}_{t-1} + a_t$$

IV.1

where \( \{a_t\} \) are distributed iid \( N(0, \sigma_a^2) \). To validate this model, preferably independent data should be subjected to the model, and an analysis of the residual, or forecast errors, made.

As stated previously, years 1975 through 1980 were reserved for the purpose of validation. The method of validation was to use the model to construct a series of one step ahead forecasts. Let \( e_t(1) \) be the error in a forecast of time \( t+1 \) from the model at time \( t \). Then the minimum mean squared error forecast (see Box and Jenkins) is;

$$e_t(1) = \tilde{z}_t - \rho \tilde{z}_{t-1}$$

IV.2

If the model is correct, the sequence \( \{e_t(1)\} \) will be independent normally distributed with mean zero and variance \( \sigma^2_a \). In the following sections the models are applied to the reserved data sets (which may also be found in the appendixes), and these forecast errors are calculated. The forecast errors are then analyzed to determine if

(1) The errors are serially independent
(2) The errors are distributed as normal random variables with mean zero, and variance $\sigma^2$.

Since the residual analysis of the twelve month model already indicates a poor fit, the twelve month model will not be validated. Only the winter month models will be checked for validity.

B. DATA SET RN

Figures 84 (Raw data) and 85 (Logged anomalies) display the reserved data set. The logged anomalies were formed by removing the means of the analyzed data, Table 4, not the means of the logged reserved data. This was done to remove any bias from the validation.

![Reserved rainfall data for data set RN](image)

Figure 84. Reserved rainfall data for data set RN
Figure 85. Logged rainfall anomalies of reserved data set RN

The forecast errors, Figure 86, their correlogram, Figure 87, and independence tests, Table 31 indicate that the errors are indeed independent.
Figure 86. Forecast errors from first order Markov model applied to winter months of reserved data set RN

Figure 87. Correlogram of forecast errors from first order Markov model applied to winter months of reserved data set RN
### TABLE 31

**ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCY IS FOR THE FORECAST ERRORS OF THE FIRST ORDER MARKOV MODEL APPLIED TO THE WINTER MONTHS OF RESERVED DATA SET RN**

**NUMBER OF TURNING POINTS = 32**  
$E[P] = 30.667$  
$V[P] = 15.39$

**PHASE LENGTHS**

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</thead>
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<td><strong>29.7</strong></td>
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The normality of the forecast errors is addressed by Table 32 (Statistics), Figure 88 (Normal plot), 89 (Histogram), and a simple chi-squared test. The chi-squared was calculated as 7.82 with 5 degrees of freedom which is significant at the .167 level. However, the normality of the errors is somewhat questionable due to the other displays.
TABLE 32
GENERAL STATISTICS OF FORECAST ERRORS FROM
THE FIRST ORDER MARKOV MODEL APPLIED TO THE
WINTER MONTHS OF RESERVED DATA SET RN

Moments
Mean .001
Variance .259
Skewness -.276
Kurtosis -.955

Percentiles
Minimum -1.156
Lower Sixteenth -.791
Lower Eight -.634
Lower Quartile -.397
Median .069
Upper Quartile .409
Upper Eight .569
Upper Sixteenth .614
Maximum .855

Figure 88. Standardized normal plot of forecast errors
from the first order Markov model applied to the winter
months of reserved data set RN
Figure 89. Histogram of forecast errors from the first order Markov model applied to the winter months of reserved data set RN.
C. DATA SET FL

As before, the similarity of results for the different data set allows the analysis to be portrayed using the displays only.

Figure 90. Reserved rainfall data for data set FL
Figure 91. Logged rainfall anomalies of reserved data set FL.

Figure 92. Forecast errors from the first order Markov model applied to the winter months of reserved data set FL.
Figure 93. Correlogram of forecast errors from first order Markov model applied to the winter months of reserved data set FL

TABLE 33

ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCIES FROM THE FORECAST ERRORS OF THE FIRST ORDER MARKOV MODEL APPLIED TO THE WINTER MONTHS OF RESERVED DATA SET FL

NUMBER OF TURNING POINTS = 34

\[ E[P] = 30.667 \quad V[P] = 15.396 \]

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<td>29.7</td>
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TABLE 34

GENERAL STATISTICS OF FORECAST ERRORS
FROM THE FIRST ORDER MARKOV MODEL APPLIED
TO THE WINTER MONTHS OF RESERVED DATA SET FL

<table>
<thead>
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<td>Skewness</td>
<td>-0.155</td>
</tr>
<tr>
<td>Kurtosis</td>
<td>-0.970</td>
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</tbody>
</table>

<table>
<thead>
<tr>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>-1.031</td>
</tr>
<tr>
<td>Lower Sixteenth</td>
<td>-0.724</td>
</tr>
<tr>
<td>Lower Eight</td>
<td>-0.549</td>
</tr>
<tr>
<td>Lower Quartile</td>
<td>-0.396</td>
</tr>
<tr>
<td>Median</td>
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</tr>
<tr>
<td>Upper Quartile</td>
<td>0.369</td>
</tr>
<tr>
<td>Upper Eight</td>
<td>0.479</td>
</tr>
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<td>Upper Sixteenth</td>
<td>0.531</td>
</tr>
<tr>
<td>Maximum</td>
<td>0.904</td>
</tr>
</tbody>
</table>

Figure 94. Standardized normal plot of forecast errors from the first order Markov model applied to the winter months of reserved data set FL
Figure 95. Histogram of forecast errors from the first order Markov model applied to the winter months of reserved data set FL.

The chi-squared statistic was calculated as 12.58 with 7 degrees of freedom, thus yielding a significance level of 0.083. This statistic and the displays imply that the data are only marginally normal if at all.
D. DATA SET SC

Figure 96. Reserved rainfall for data set SC

Figure 97. Logged anomalies of reserved data set SC
Figure 98. Forecast errors from first order Markov model applied to the winter months of reserved data set SC.

Figure 99. Correlogram of forecast errors from first order Markov model applied to the winter months of reserved data set SC.
### TABLE 35

**ACTUAL AND EXPECTED NUMBER OF TURNING POINTS AND ACTUAL AND EXPECTED PHASE FREQUENCES FROM THE FORECAST ERRORS OF THE FIRST ORDER MARKOV MODEL APPLIED TO THE WINTER MONTHS OF RESERVED DATA SET SC**

NUMBER OF TURNING POINTS = 34  
\[ E[P] = 30.667 \quad V[P] = 15.396 \]

**PHASE LENGTHS**

<table>
<thead>
<tr>
<th>D</th>
<th>OBS.</th>
<th>( E[\ast] )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>24</td>
<td>18.8</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
<td>8.1</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>2.3</td>
</tr>
<tr>
<td>4</td>
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</tr>
<tr>
<td>5</td>
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<td>0.0</td>
</tr>
<tr>
<td>6</td>
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<td>0.0</td>
</tr>
<tr>
<td>7</td>
<td>0</td>
<td>0.0</td>
</tr>
<tr>
<td><strong>TOTALS</strong></td>
<td><strong>34</strong></td>
<td><strong>29.7</strong></td>
</tr>
</tbody>
</table>

### TABLE 36

**GENERAL STATISTICS OF FORECAST ERRORS FROM THE FIRST ORDER MARKOV MODEL APPLIED TO THE WINTER MONTHS OF RESERVED DATA SET SC**

<table>
<thead>
<tr>
<th>Moments</th>
<th></th>
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</thead>
<tbody>
<tr>
<td>Mean</td>
<td>-.003</td>
</tr>
<tr>
<td>Variance</td>
<td>.296</td>
</tr>
<tr>
<td>Skewness</td>
<td>-.298</td>
</tr>
<tr>
<td>Kurtosis</td>
<td>-.413</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Percentiles</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>-1.386</td>
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<tr>
<td>Lower Sixteenth</td>
<td>-.846</td>
</tr>
<tr>
<td>Lower Eight</td>
<td>-.559</td>
</tr>
<tr>
<td>Lower Quartile</td>
<td>-.434</td>
</tr>
<tr>
<td>Median</td>
<td>.031</td>
</tr>
<tr>
<td>Upper Quartile</td>
<td>.414</td>
</tr>
<tr>
<td>Upper Eight</td>
<td>.588</td>
</tr>
<tr>
<td>Upper Sixteenth</td>
<td>.735</td>
</tr>
<tr>
<td>Maximum</td>
<td>1.005</td>
</tr>
</tbody>
</table>

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Figure 100. Standardized normal plot of forecast errors from the first order Markov model applied to the winter months of reserved data set SC.

Figure 101. Histogram of forecast errors from the first order Markov model applied to the winter months of reserved data set SC.
The chi-squared statistic was calculated as 9.71 with 7 degrees of freedom, thus yielding a significance level of .205.

E. CONCLUSIONS

The application of a Markovian model was indicated by the apparent dependence of adjacent months and the apparent lack of dependence at any other lag. The preceding sub-sections, however, indicate that the first order Markovian model is weak at best.

The structure of the data, visually, still points toward some sort of underlying order. The following sections attempt to discover this order.
V. 2x2 TABLES

A. THEORY

As seen in sections III and IV, the classical ARMA time series approach does not seem to adequately describe the data. Another technique used to explore possible relationships is the 2x2 contingency tables.

The idea to be explored is whether or not some subset of the data, to be called the control, may be used to predict in some way the behavior of another subset of the data, to be called the complement. Here, the data are reduced from monthly observations to yearly observations as described below.

Let $X$ be the subset of a year, to be called the control, and let $Y$ be the subset to be called the complement. It is necessary that $X \cap Y = \emptyset$; that is, the intersection of these two sets is empty. The data are then compared for some quality in $X$ and for some quality in $Y$. The question is then: does the presence (or absence) of the quality in $X$ affect the presence (or absence) of the quality in $Y$? An example of a typical table is shown below in Figure 102.
The table elements, $n_{ij}$, represents the number of years which display quality $i$ in the control and quality $j$ in the complement. The marginal entries $n_{1.}$ and $n_{.j}$ represents the numbers of years for which the control has quality $i$ and the number of years the complement has quality $j$ respectively. The overall number of years, $n_{..}$, is in the lower right of the table.

Brownlee [Ref. 6] contains a very good discussion of the theory and use of 2x2 contingency tables. Using the notation of Brownlee, let $\theta_{ij}$ be the probability that any given year
will have a control quality i and a complement quality j.

Then estimates of the \( \theta_{ij} \)'s are

\[
\hat{\theta}_{ij} = \frac{n_{ij}}{n_{..}} \\
\hat{\theta}_i = \frac{n_i}{n_{..}} \\
\hat{\theta}_j = \frac{n_j}{n}
\]

If the control and complement are independent,

\[
\theta_{ij} = \theta_i \cdot \theta_j
\]

These simple assumptions allow for a thorough investigation of the possible interrelationships within the data sets.

Another way to view the assumption of independence is through the use of proportions. Thus, if the basic division is made via the quality of the control, the the proportions

\[
P_1 = \frac{n_{11}}{n_1} \quad \text{(respectively } P_2 = \frac{n_{21}}{n_2} \text{)}
\]

represent, in words, the proportion of the years that have quality 1 in the control and have quality 1 (respectively 2) in the complement.

The question of independence may be approached in several ways as described below.

1. **Fishers Exact Test**

   A test for the significance of any dependence was proposed by Fisher in the case in which the marginal totals, \( n_{1..}, n_{..}, \) and \( n_{..} \) are known a priori (cf. Brownlee [Ref. 6]).

To draw from Brownlee, knowledge of the marginal and \( n_{11} \) gives knowledge of all the other elements of the table. The
probability of the event of having exactly \( n_{11} \) years that
display quality 1 in both the complement and the control is:

\[
P(N_{11} = n_{11}) = \frac{n_1 \cdot 1 \cdot n_2 \cdot 1}{n_{..}! n_{12}! n_{21}! n_{22}!}
\]

A test may then be applied, using V.4, to determine the
significance of any dependence. This test is usually applied
by simply summing these probabilities in the tail of the
distribution (V.4) in the same direction as the noted extreme.

The usual procedure to provide a two-sided test of
significance is to double a one sided figure. This procedure
is acceptable due to the symmetric appearance of the distribu-
tion.

Under the assumptions of independence

\[
E \left[ N_{11} \right] = \frac{n_1 \cdot 1}{n_{..}} \quad V.5
\]

\[
V \left[ N_{11} \right] = \frac{n_1 \cdot 1 \cdot n_2 \cdot 2}{n_{..} (n_{..} - 1)} \quad V.6
\]

and the random variable \( U \) defined as

\[
U = \frac{N_{11} - E[N_{11}]}{\sqrt{V[N_{11}]}} \quad V.7
\]

is asymptotically distributed as a normal random variable
with mean zero and variance one. This asymptotic result
combined with a continuity correction yields a test statistic
of
\[ u' = \frac{\{n_{11} n_{22} - n_{12} n_{21} \mid -\nu/2\}\sqrt{n_\cdot \cdot}}{\sqrt{n_1 n_\cdot 1 n_2 n_\cdot 2}} \] \hspace{1cm} V.8

The statistic \( u' \) may then be used as a test, using standard normal tables, of the significance of any variation from the assumption of independence. It should be noted at this point that if the random variable \( u' \) is squared, \( u'^2 \) will be distributed as a chi-square with one degree of freedom. The squaring of \( u' \) with simplifying algebra yields the Yates correction to a standard chi-squared goodness of fit statistic
\[ (u')^2 = \frac{\{n_{11} n_{22} - n_{12} n_{21} \mid -\nu/2\}^2 n_\cdot \cdot}{(n_{11} + n_{12})(n_{11} + n_{21})(n_{12} + n_{22})(n_{21} + n_{22})} \] \hspace{1cm} V.9

see Dixon and Massey [Ref. 5]. This allows the use of the chi-square tables as an equivalent test to that of V.8.

2. Odds

Subsection V.A.1 above deals with the significance of any observed interdependence between the control and the complement. The question of the degree of dependence should also be addressed. The measure to be used is the odds ratio. Using the notation of Fleiss [Ref. 3], a measure of seeing quality 1 in the complement \( Y \) may be
\[ \Omega_1 = \frac{P(Y=1 \mid X=1)}{P(Y=2 \mid X=1)} ; \] \hspace{1cm} V.10

this is then the odds that quality 1 will occur in the complement given that quality 1 is present in the control. In a
similar manner;

\[ \Omega_2 = \frac{P(Y=1\mid X=2)}{P(Y=2\mid X=2)} \]

is the odds that quality 1 will occur in the complement given that quality 2 was observed in the control. The currently most often used measure is the odds ratio \( \omega \), or

\[ \omega = \frac{\Omega_1}{\Omega_2} \]

Note that, if the appearance of quality 1 in the complement is independent of whether or not it appears in the control, then \( \omega = 1 \). While \( \omega > 1 \) implies that the odds of the complement having quality 1, given that quality 1 was observed in the control, are greater than the odds of the complement having quality 2. This would indicate that the control would be some sort of predictor for the complement, relative to the selected qualities.

In the same continuity correcting spirit, as was used with the Yates chi-square, an estimate for \( \omega \) may be obtained from the Table as

\[ \hat{\omega} = 0 = \frac{(n_{11}+.5)(n_{22}+.5)}{(n_{12}+.5)(n_{21}+.5)} \]

with a standard error of

\[ \text{s.e.}(0) = 0 \sqrt{\frac{1}{n_{11}+.5} + \frac{1}{n_{12}+.5} + \frac{1}{n_{21}+.5} + \frac{1}{n_{22}+.5}} \]

The natural logarithm of this odds ratio will be discussed more fully in section VI.
B. ANALYSIS

The theory of subsection A above is applied to the three data sets as discussed below. The control is typically taken as a monthly anomaly, say October. Here, the quality is taken as either a positive or a negative anomaly. Thus $X=1$ occurs when the month of October falls below its mean and $X=2$ occurs when it falls above its mean. The complement consists of the sum of the rainfall for the succeeding eleven months, or in symbols:

$$X_t = R_{t,1} - \bar{R}_t.$$  
$$Y_t = \sum_{m=2}^{12} R_{t,m} - \frac{1}{N} \sum_{t=1}^{N} \left( \sum_{m=2}^{12} R_{t,m} \right).$$  

Where it is understood that $X=1$ when $X_t < 0$, $X=2$ when $X_t > 0$ and similarly for $Y_t$.

Various control subsets are used; October through September were investigated by themselves as were all adjacent pairs, triples, and four-tuples of months. For an example, consider the spring (April, May, and June) and its complement (July through March). In this case

$$X_t = \sum_{m=7}^{9} R_{t,m} - \frac{1}{N} \sum_{t=1}^{N-1} \left( \sum_{m=7}^{9} R_{t,m} \right).$$  

$$Y_t = \sum_{m=10}^{12} R_{t,m} + \sum_{m=1}^{6} R_{t+1,m} - \frac{1}{N-1} \sum_{t=1}^{N-1} \left( \sum_{m=10}^{12} R_{t,m} + \sum_{m=1}^{6} R_{t+1,m} \right).$$  

Equations V.15 and V.16 imply that the data are always analyzed as deviations from the arithmetic mean. However, the data are also analyzed as deviations from the median.
and the lower quartile. In the tables to follow, 'A' refers to both control and complement having the arithmetic mean removed, 'M' refers to both control and complement having their respective medians removed, and 'QL' refers to the control having the lower quartile removed while the median was removed from the complement.

The first four Tables (37 through 40), give the significance levels of observed departures from independence of the control and complement. Only those values having a Yates corrected chi-square of greater than 1.00 are listed. The entries represent the two-tailed probability of a random deviation in excess of that observed. Although the cut off criterion was the Yates chi-square, the agreement between its probability and that obtained from the Fisher exact and normal tests did not differ in the first two decimal places.

<table>
<thead>
<tr>
<th>Data set</th>
<th>RN</th>
<th>FL</th>
<th>SC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Differentiator</td>
<td>A</td>
<td>M</td>
<td>QL</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Control</th>
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</tr>
</thead>
<tbody>
<tr>
<td>October</td>
<td>.18</td>
</tr>
<tr>
<td>November</td>
<td>.10</td>
</tr>
<tr>
<td>December</td>
<td>.14</td>
</tr>
<tr>
<td>January</td>
<td>.14</td>
</tr>
<tr>
<td>February</td>
<td>.002</td>
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<td>March</td>
<td>.11</td>
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<tr>
<td>April</td>
<td>.13</td>
</tr>
<tr>
<td>May</td>
<td>.18</td>
</tr>
<tr>
<td>June</td>
<td>.14</td>
</tr>
<tr>
<td>July</td>
<td>.24</td>
</tr>
<tr>
<td>August</td>
<td>.21</td>
</tr>
<tr>
<td>September</td>
<td>.14</td>
</tr>
</tbody>
</table>

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### Table 38
**Significance of Observed Departures from Independence of Pairs of Months Versus Succeeding Ten Month Complements**

<table>
<thead>
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<th>Data Set</th>
<th>RN</th>
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<th>SC</th>
</tr>
</thead>
<tbody>
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<td>Differentiators</td>
<td>A</td>
<td>M</td>
<td>QL</td>
</tr>
<tr>
<td>Control</td>
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<td></td>
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</tr>
<tr>
<td>Oct+Nov</td>
<td>.18</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nov+Dec</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jan+Feb</td>
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<td>.30</td>
<td></td>
</tr>
<tr>
<td>Feb+Mar</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Mar+Apr</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Apr+May</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jun+Jul</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jul+Aug</td>
<td></td>
<td>.19</td>
<td></td>
</tr>
<tr>
<td>Aug+Sep</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table 39
**Significance of Observed Departures from Independence of Triples of Months Versus Succeeding Nine-Month Complements**

<table>
<thead>
<tr>
<th>Data Set</th>
<th>RN</th>
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<th>SC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Differentiators</td>
<td>A</td>
<td>M</td>
<td>QL</td>
</tr>
<tr>
<td>Control</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Oct+Nov+Dec</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nov+Dec+Jan</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dec+Jan+Feb</td>
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<td>Jan+Feb+Mar</td>
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</tr>
<tr>
<td>Feb+Mar+Apr</td>
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<td></td>
<td></td>
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<tr>
<td>Mar+Apr+May</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Apr+May+Jun</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>May+Jun+Jul</td>
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<td>.30</td>
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<tr>
<td>Jun+Jul+Aug</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jul+Aug+Sep</td>
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</tbody>
</table>
### TABLE 40

**SIGNIFICANCE OF OBSERVED DEPARTURES FROM INDEPENDENCE OF FOUR-TUPLES OF MONTHS VERSUS SUCCEEDING EIGHT-MONTH COMPLEMENTS**

<table>
<thead>
<tr>
<th>Data set</th>
<th>RN</th>
<th>FL</th>
<th>SC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Differentiator</td>
<td>A</td>
<td>M</td>
<td>QL</td>
</tr>
<tr>
<td>Control</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Oct+Nov+Dec+Jan</td>
<td>.26</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nov+Dec+Jan+Feb</td>
<td>.22</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dec+Jan+Feb+Mar</td>
<td>.22</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jan+Feb+Mar+Apr</td>
<td></td>
<td>.31</td>
<td></td>
</tr>
<tr>
<td>Feb+Mar+Apr+May</td>
<td>.22</td>
<td>.27</td>
<td></td>
</tr>
<tr>
<td>Mar+Apr+May+Jun</td>
<td>.20</td>
<td>.31</td>
<td></td>
</tr>
<tr>
<td>Apr+May+Jun+Jul</td>
<td>.30</td>
<td></td>
<td></td>
</tr>
<tr>
<td>May+Jun+Jul+Aug</td>
<td>.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jun+Jul+Aug+Sep</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Several choices for predictors are suggested in the previous tables. However, the apparent strongest candidate for a predictor is January. The control of January by itself and January paired with December, are the most consistently significant entries. Tables 41 below gives the odds ratio, V.13, for January, and January and December, as controls.
TABLE 41

ODDS RATIO OF JANUARY VERSUS FEBRUARY
THROUGH DECEMBER AND JANUARY PLUS
DECEMBER VERSUS FEBRUARY THROUGH NOVEMBER

<table>
<thead>
<tr>
<th>Differentiator</th>
<th>A</th>
<th>M</th>
<th>QL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data set RN</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>January</td>
<td>4.59</td>
<td>3.15</td>
<td>5.13</td>
</tr>
<tr>
<td>Jan+Dec</td>
<td>3.15</td>
<td>3.15</td>
<td>2.01</td>
</tr>
<tr>
<td>Data set FL</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>January</td>
<td>10.71</td>
<td>4.72</td>
<td>4.30</td>
</tr>
<tr>
<td>Jan+Dec</td>
<td>7.42</td>
<td>6.02</td>
<td>4.30</td>
</tr>
<tr>
<td>Data set SC</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>January</td>
<td>2.45</td>
<td>2.49</td>
<td>2.23</td>
</tr>
<tr>
<td>Jan+Dec</td>
<td>3.00</td>
<td>2.49</td>
<td>1.44</td>
</tr>
</tbody>
</table>

At this point in the analysis it was decided to explore more fully the power of January as a predictor. It should be stated that other possibilities for predictors are suggested by the tables, but time did not allow an exhaustive study of all of these.

C. OTHER RESULTS

The results of section V.B suggest that a more detailed analysis of January as a predictor is in order. The first method tried for this was ordinary least squares regression of the rainfall total in January versus the total for February through December. This is the model below.

Let $X_t = R_{t,4}$

$$Y_t = \sum_{m=5}^{12} R_{t,m} + \sum_{m=1}^{3} R_{t+1,m}$$

V.17
then assume that

\[ Y_t = \alpha + \beta X_t + \varepsilon_t \]  

as the standard, linear model where \( \{\varepsilon_t\} \) are assumed to be independent and identically distributed with mean zero and variance \( \sigma^2 \). If the predictability of January is strong, this model, V.18, may result in a good fit of the data.

Table 42 below is the resulting ANOVA for this regression. As may easily be seen, the model does not appear to have any significance.

**TABLE 42**

ANOVA FOR REGRESSION OF SIMPLE LINEAR MODEL FOR ALL DATA SETS

<table>
<thead>
<tr>
<th>SOURCE</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>22</td>
<td>404.798</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Regression</td>
<td>1</td>
<td>41.821</td>
<td>41.821</td>
<td>2.42</td>
</tr>
<tr>
<td>Jan-Control</td>
<td>1</td>
<td>41.821</td>
<td>41.821</td>
<td>2.42</td>
</tr>
<tr>
<td>Residual</td>
<td>21</td>
<td>362.977</td>
<td>17.285</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
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90% Confidence Limits

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R-squared = .1033

Standard error of estimate = 4.1574

RN
R-squared = .2066
Standard error of estimate = 4.2804

AOV

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The same model with means removed, V.19, below was tried and, although slightly better, is still not strong.

\[ Y_t - \bar{Y} = \alpha + \beta (X_t - \bar{X}) + \varepsilon_t \]  

V.19
TABLE 43
ANOVA FOR REGRESSION OF SIMPLE LINEAR MODEL WITH MEANS REMOVED FOR ALL DATA SETS

R-squared = .1033
Standard error of estimate = 4.1575

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90% Confidence Limits

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R-squared = .1747
Standard error of estimate = 4.4276

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90% Confidence Limits

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<tr>
<td>Beta</td>
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</table>
R-squared = .5617
Standard error of estimate = .7589

AOV

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90% Confidence Limits

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The amount of rainfall in January does not appear to be a strong predictor for the amount of rainfall in February through December. This seems to indicate that the relationships between January rainfall and rainfall during the next eleven months is not as strong as expected. However, a further technique is available, that of log-odds and logistic regression, which are the subjects of the next section.
VI. LOGISTIC ANALYSIS

A. THEORY

The logistic analysis to be described in the section was developed from Gaver [Ref. 2] and Fleiss [Ref. 3]. This analysis derives from the model of 1.5 as stated in the introduction.

The basic approach is to view the complement as having a binary representation, with success being defined as a complement above its mean (see equations 1.3 and 1.4) and failure as the complement below its mean. The problem then is to find the conditional probability of a success (the complement being above its mean for a year) given that the control (January rainfall) takes on a particular value.

The control is now taken to be the logged rainfall anomaly of January and is found in equation 1.2 repeated below.

\[ X_t = \ln(R_t,4) - \frac{1}{N} \sum_{t=1}^{N} \ln(R_t,4) \]  

If the probability of success, given \( X_t \) is written as

\[ P(\text{Success} | X_t) = \theta_t \]  

a superficially attractive model for \( \theta_t \) is

\[ \theta_t = \alpha + \beta X_t + \epsilon_t \]  

This model has two difficulties, the worst of which is that probabilities of greater than one or less that zero are
allowed. Secondly, the $\theta_t$ are not available in proportion form to fit the model.

 Initially, the problem of estimating $\theta_t$ is approached by grouping the data. Section II indicated that each year seemed to be independent of the next and that there was no trend. This allows for the ordering of the $X_t$'s into their order statistics $X(t)$'s. Once the ordering has been done, non overlapping groups of arbitrary size may be formed as shown. Let $X_1, X_2, X_3, \ldots, X_{12}$ be a series of 12 years from an arbitrary data set, with associated order statistics $X(1), X(2), X(3), \ldots, X(12)$. The if groups of size three are desired, the data are partitioned below.

$$X(1), X(2), X(3) | X(4), X(5), X(6) | \ldots | X(10), X(11), X(12)$$

Given these groups, let $\tilde{X}_j$ be a measure of location for the $j^{th}$ group. This analysis used the median, therefore $\tilde{X}_j = X(3j+1)$. Also associated with each group is $R_j$ (not rainfall), the number of success in group $j$, and $n_j$, the number of elements in group $j$. From this set up, the required probabilities may be estimated as;

$$\hat{\theta}_j = \frac{R_j}{n_j} \quad \text{VI.4}$$

A solution to the first problem, that of the model yielding probabilities outside of $(0,1)$, is to use the log odds, instead of $\theta_j$ where;

$$\text{Log odds} = \phi_j = \ln \left( \frac{\theta_j}{1-\theta_j} \right) \quad \text{VI.5}$$
which is equivalent to the logarithm of the odds ratio as given in V.13. Gaver [Ref. 2] suggests that a correction of .5 be applied to guard against the problem of 0 and 1 within the logarithm and to reduce the bias. The statistic then becomes:

\[ \phi_j' = \ln \left( \frac{\theta_j + .5}{1.5 - \theta_j} \right) \]

The temptation is to go directly to the model

\[ \phi_j' = \alpha + \beta \tilde{X}_j \]

yet \( V[\theta_j] = \theta_j(1-\theta_j)/n_j \) which is not constant. This suggests the need for a weighting scheme.

The weighting scheme used was that of iteratively reweighted least squares, (IRWLS), using the bi-weights. This method is discussed in detail in Mosteller and Tukey [Ref. 13].

Although grouping of the data and the model of VI.7 provide adequate representation of the underlying structure, the logistic model itself, I.5, when viewed through the eyes of maximum likelihood theory can yield more insight.

The model is assumed to be

\[ \theta_t = \frac{e^{\alpha + \beta X_t}}{1 + e^{\alpha - \beta X_t}} \]

where the \( X_t \) are independent.
The likelihood function is then

$$L(X,Y;\alpha,\beta) = \prod_{t=1}^{N} \left( \frac{e^{\alpha X_t + \beta Y_t}}{1 + e^{\alpha X_t + \beta Y_t}} \right)^{Y_t} \left( \frac{1}{1 + e^{\alpha X_t + \beta Y_t}} \right)^{1-Y_t}$$

and the log-likelihood is

$$L(X,Y;\alpha,\beta) = \alpha \sum_{t=1}^{N} X_t Y_t + \beta \sum_{t=1}^{N} X_t Y_t$$

$$- \sum_{t=1}^{N} \ln (1 + e^{\alpha X_t + \beta Y_t})$$

The gradient, and Hessian of VI.9 are

$$\frac{\partial L}{\partial \alpha} = \sum_{t=1}^{N} Y_t - \sum_{t=1}^{N} \left( \frac{\psi_t}{1 + \psi_t} \right)$$

$$\frac{\partial L}{\partial \beta} = \sum_{t=1}^{N} X_t Y_t - \sum_{t=1}^{N} X_t \left( \frac{\psi_t}{1 + \psi_t} \right)$$

and

$$H_L = \begin{pmatrix}
- \sum_{t=1}^{N} \frac{\psi_t}{1 + \psi_t^2} & - \sum_{t=1}^{N} \frac{X_t \psi_t}{(1 + \psi_t)^2} \\
- \sum_{t=1}^{N} \frac{X_t \psi_t}{(1 + \psi_t)^2} & - \sum_{t=1}^{N} \frac{X_t^2 \psi_t}{(1 + \psi_t)^2}
\end{pmatrix}$$

where

$$\psi_t = e^{\alpha + \beta X_t}.$$
A simple way to solve for \( \hat{a} \) and \( \hat{b} \) is to use Newton's Method a.

\[
\begin{pmatrix}
\hat{a}
\hat{b}
\end{pmatrix}_{k+1} = \begin{pmatrix}
\hat{a}
\hat{b}
\end{pmatrix}_k - H^{-1}_L y^t_L
\]

since all necessary elements may be calculated in one pass of the computer algorithm.

One beneficial byproduct of the maximum likelihood approach is the asymptotic information matrix, \( H^{-1}_L \). Gaver [Ref. 2] states that the diagonal elements of this matrix provide good estimates of \( V[\hat{a}] \) and \( V[\hat{b}] \) under assumptions of normality.

B. ANALYSIS

1. Grouped Data

The first approach taken was that of grouping the data as described above. Groups of 3, 4, and 5 were used, as were two separate methods of regression, ordinary least squares (OLS), and iteratively reweighted least squares (IRWLS). Tables 44 (RN), 45 (FL), and 46 (SC) present the data and Tables 47 (OLS), and 48 (IRWLS) present the results of the regressions.
TABLE 44

DATA SET RN, LOGGED JANUARY ANOMALIES AND SUCCESSES FOR GROUPED AND UNGROUPED FORMS

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153
**TABLE 47a**

**ORDINARY LEAST SQUARES REGRESSION WITH THE MODEL OF EQUATION VI.7 FOR DATA SET RN**

R-squared = .0423  
Standard error of estimate = 6.1508

R-squared = .4068  
Standard error of estimate = 1.2099

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90% Confidence Limits  
Lower limit | Upper limit
--- | ---
Alpha | 11.9680 | 17.1988
Beta  | -.0446  | .9157

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90% Confidence Limits  
Lower limit | Upper limit
--- | ---
Alpha | -1.1675 | .8284
Beta  | 1.7688  | 3.8288

154
R-squared = .5973
Standard error of estimate = .9995

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TABLE 47b

ORDINARY LEAST SQUARES REGRESSION WITH THE MODEL OF EQUATION VI.7 FOR DATA SET FL

R-squared = .2862
Standard error of estimate = .8949

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R-squared = .5370  
Standard error of estimate = 1.0484

AOV

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R-squared = .6311
Standard error of estimate = .8809

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<td>-.7525</td>
<td>.4740</td>
</tr>
<tr>
<td>Beta</td>
<td>.5673</td>
<td>2.4777</td>
</tr>
</tbody>
</table>

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TABLE 47c
ORDINARY LEAST SQUARES REGRESSION WITH
THE MODEL OF EQUATION VI.7 FOR DATA SET SC

R-squared = .1404
Standard error of estimate = .9901

GROUP=3

<table>
<thead>
<tr>
<th>SOURCE</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>15</td>
<td>15.965</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Regression</td>
<td>1</td>
<td>2.241</td>
<td>2.241</td>
<td>2.29</td>
</tr>
<tr>
<td>Jan-Control</td>
<td>1</td>
<td>2.241</td>
<td>2.241</td>
<td>2.29</td>
</tr>
<tr>
<td>Residual</td>
<td>14</td>
<td>13.724</td>
<td>.980</td>
<td></td>
</tr>
</tbody>
</table>

Variable Coefficient Standard Error T
 Alpha -.3039 .249 -1.22
 Beta .5059 .335 1.51

90% Confidence Limits
<table>
<thead>
<tr>
<th>Lower limit</th>
<th>Upper limit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alpha</td>
<td>-.7090</td>
</tr>
<tr>
<td>Beta</td>
<td>-.0386</td>
</tr>
</tbody>
</table>

R-squared = .1872
Standard error of estimate = .8959

GROUP=4

<table>
<thead>
<tr>
<th>SOURCE</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>11</td>
<td>9.875</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Regression</td>
<td>1</td>
<td>1.848</td>
<td>1.848</td>
<td>2.30</td>
</tr>
<tr>
<td>Jan-Control</td>
<td>1</td>
<td>1.848</td>
<td>1.848</td>
<td>2.30</td>
</tr>
<tr>
<td>Residual</td>
<td>10</td>
<td>8.026</td>
<td>.803</td>
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</tr>
</tbody>
</table>

Variable Coefficient Standard Error T
 Alpha -.2284 .260 -.88
 Beta .5447 .359 1.52

90% Confidence Limits
<table>
<thead>
<tr>
<th>Lower limit</th>
<th>Upper limit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alpha</td>
<td>-.6618</td>
</tr>
<tr>
<td>Beta</td>
<td>.5447</td>
</tr>
</tbody>
</table>

157
R-squared = .2862

Standard error of estimate = .8949

<table>
<thead>
<tr>
<th>SOURCE</th>
<th>DF</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>9</td>
<td>8.976</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Regression</td>
<td>1</td>
<td>2.569</td>
<td>2.569</td>
<td>3.21</td>
</tr>
<tr>
<td>Jan-Control</td>
<td>1</td>
<td>2.569</td>
<td>2.569</td>
<td>3.21</td>
</tr>
<tr>
<td>Residual</td>
<td>8</td>
<td>6.407</td>
<td>.801</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Standard Error</th>
<th>T</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alpha</td>
<td>-.1838</td>
<td>.287</td>
<td>-.64</td>
</tr>
<tr>
<td>Beta</td>
<td>.6573</td>
<td>.367</td>
<td>1.79</td>
</tr>
</tbody>
</table>

90% Confidence Limits

<table>
<thead>
<tr>
<th>Variable</th>
<th>Lower limit</th>
<th>Upper limit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alpha</td>
<td>-.6736</td>
<td>.3061</td>
</tr>
<tr>
<td>Beta</td>
<td>.0303</td>
<td>1.2843</td>
</tr>
</tbody>
</table>

TABLE 48

ITERATIVELY REWEIGHTED LEAST SQUARES
REGRESSION USING BI-WEIGHTS FOR THE MODEL OF EQUATION VI.7

GROUP SIZE 3

<table>
<thead>
<tr>
<th>C=9</th>
<th>Data sets</th>
<th>ˆα</th>
<th>1.013</th>
</tr>
</thead>
<tbody>
<tr>
<td>RN</td>
<td>-.048</td>
<td></td>
<td></td>
</tr>
<tr>
<td>FL</td>
<td>-.063</td>
<td>.664</td>
<td></td>
</tr>
<tr>
<td>SC</td>
<td>-.116</td>
<td>.351</td>
<td></td>
</tr>
</tbody>
</table>

C=4

<table>
<thead>
<tr>
<th>Data sets</th>
<th>ˆα</th>
<th>1.031</th>
</tr>
</thead>
<tbody>
<tr>
<td>RN</td>
<td>-.052</td>
<td></td>
</tr>
<tr>
<td>FL</td>
<td>-.197</td>
<td>1.049</td>
</tr>
<tr>
<td>SC</td>
<td>.154</td>
<td>.480</td>
</tr>
</tbody>
</table>

GROUP SIZE 4

<table>
<thead>
<tr>
<th>C=9</th>
<th>Data sets</th>
<th>ˆα</th>
<th>.665</th>
</tr>
</thead>
<tbody>
<tr>
<td>RN</td>
<td>-.103</td>
<td></td>
<td></td>
</tr>
<tr>
<td>FL</td>
<td>-.093</td>
<td>.705</td>
<td></td>
</tr>
<tr>
<td>SC</td>
<td>-.169</td>
<td>.280</td>
<td></td>
</tr>
</tbody>
</table>

GROUP SIZE 5

<table>
<thead>
<tr>
<th>C=9</th>
<th>Data sets</th>
<th>ˆα</th>
<th>.865</th>
</tr>
</thead>
<tbody>
<tr>
<td>RN</td>
<td>-.065</td>
<td></td>
<td></td>
</tr>
<tr>
<td>FL</td>
<td>-.107</td>
<td>.723</td>
<td></td>
</tr>
<tr>
<td>SC</td>
<td>-.126</td>
<td>.413</td>
<td></td>
</tr>
</tbody>
</table>

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2. **Maximum Likelihood**

Table 49 displays the final points for each data set along with the inverse Hessian at that point. Figures 103 (RN), 104 (FL), and 105 (SC) are interesting in that they portray the contours of the likelihood functions for each data set. These contours show the variance of the estimated parameters in a graphic way. Note how data sets RN and FL seem to have some sort of horizontal ridge indicating a good pick of the slope parameter, yet the contours of data set SC are almost circular about the origin of the axes indicating no significant difference from zero for either parameter.

**TABLE 49**

**MAXIMUM LIKELIHOOD ESTIMATES OF \( \hat{\alpha} \) AND \( \hat{\beta} \) ALONG WITH ESTIMATES OF THEIR VARIANCE FOR ALL THREE DATA SETS**

<table>
<thead>
<tr>
<th>Data set</th>
<th>( \hat{\alpha} )</th>
<th>( \hat{\beta} )</th>
<th>( H^{-1}_L )</th>
<th>( V[\hat{\alpha}] )</th>
<th>( V[\hat{\beta}] )</th>
</tr>
</thead>
<tbody>
<tr>
<td>RN</td>
<td>.062</td>
<td>2.918</td>
<td>( \begin{pmatrix} .257 &amp; -.043 \ -.034 &amp; 1.720 \end{pmatrix} )</td>
<td>.257</td>
<td>1.720</td>
</tr>
<tr>
<td>FL</td>
<td>-.171</td>
<td>.933</td>
<td>( \begin{pmatrix} .129 &amp; -.040 \ -.040 &amp; .298 \end{pmatrix} )</td>
<td>.129</td>
<td>.298</td>
</tr>
<tr>
<td>SC</td>
<td>-.303</td>
<td>.171</td>
<td>( \begin{pmatrix} .088 &amp; -.035 \ -.035 &amp; .113 \end{pmatrix} )</td>
<td>.088</td>
<td>.113</td>
</tr>
</tbody>
</table>
Figure 103. Contours of log likelihood function for data set RN

Figure 104. Contours of log likelihood function for data set FL
C. DISCUSSION

A recapitulation of all the parameter values is in Table 50. Some interesting observations to be made from this table are:

(1) The slope for data set RN, as found by maximum likelihood, is much greater than that of any other method or data set. The first temptation is to treat this as an outlier, yet the evidence of the contour plot and of the validation of the next section tend to back up this number. The reason for this difference is a possible subject for further research.

(2) Except for the intercept values, the slopes of data sets RN and FL seem to be fairly consistent within and between
regression methods. This comment is made in light of the difference of these data sets and that of SC.

(3) Data sets RN and FL seem to be similar in many ways, yet data set SC appears to be different in both degree and significance.

No other strong pattern is apparent in these parameter values. Graphical displays of the parameters, as used with grouped data are given in Figures 106 (RN), 107 (FL), and 108 (SC). Again, note the significant difference of the maximum likelihood line for data set RN. Table 51 contains the data points from which Figures 106, 107 and 108 were drawn.

After viewing these figures, the maximum likelihood approach is the preferred method for the Peninsula data sets, whereas the robust(C=4) IRWLS may be best for the Valley data set. Although fits were made to data set SC, it appears as if no great significance has been found.
### TABLE 50
PARAMETER FIT RECAPITULATION
FOR ALL DATA SETS

<table>
<thead>
<tr>
<th>Method</th>
<th>RN</th>
<th>PL</th>
<th>SC</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Maximum Likelihood</td>
<td>( \alpha ) : 0.062</td>
<td>-0.171</td>
<td>-0.303</td>
</tr>
<tr>
<td></td>
<td>( \beta ) : 2.918</td>
<td>0.933</td>
<td>0.171</td>
</tr>
<tr>
<td>2. OLS</td>
<td>( \alpha ) : -0.195</td>
<td>-0.146</td>
<td>-0.304</td>
</tr>
<tr>
<td>Group=3</td>
<td>( \beta ) : 1.771</td>
<td>1.052</td>
<td>0.506</td>
</tr>
<tr>
<td>Group=4</td>
<td>( \alpha ) : -0.170</td>
<td>-0.115</td>
<td>-0.228</td>
</tr>
<tr>
<td></td>
<td>( \beta ) : 1.769</td>
<td>1.357</td>
<td>0.545</td>
</tr>
<tr>
<td>Group=5</td>
<td>( \alpha ) : -0.265</td>
<td>-0.139</td>
<td>-0.184</td>
</tr>
<tr>
<td></td>
<td>( \beta ) : 1.719</td>
<td>1.523</td>
<td>0.657</td>
</tr>
<tr>
<td>3. IRWLS</td>
<td>( \alpha ) : 0.048</td>
<td>-0.063</td>
<td>-0.116</td>
</tr>
<tr>
<td>Group=3</td>
<td>( \beta ) : 1.013</td>
<td>0.664</td>
<td>0.351</td>
</tr>
<tr>
<td>( C=9 )</td>
<td>( \alpha ) : 0.052</td>
<td>-0.197</td>
<td>0.154</td>
</tr>
<tr>
<td>( C=4 )</td>
<td>( \beta ) : 1.031</td>
<td>1.049</td>
<td>0.480</td>
</tr>
<tr>
<td>Group 4</td>
<td>( \alpha ) : -0.103</td>
<td>-0.093</td>
<td>-0.169</td>
</tr>
<tr>
<td>( C=9 )</td>
<td>( \beta ) : 0.665</td>
<td>0.705</td>
<td>0.280</td>
</tr>
<tr>
<td>Group=5</td>
<td>( \alpha ) : -0.065</td>
<td>-0.107</td>
<td>-0.126</td>
</tr>
<tr>
<td>( C=9 )</td>
<td>( \beta ) : 0.855</td>
<td>0.723</td>
<td>0.413</td>
</tr>
</tbody>
</table>
Figure 106. Estimated probability of greater-than-average total rest-of-year rainfall versus the anomaly of logged rainfall for January for data set RN.
Figure 107. Estimated probability of greater-than-average total rest-of-year rainfall versus the anomaly of logged rainfall for January for data set FL
Figure 108. Estimated probability of greater-than average total rest-of-year rainfall versus the anomaly of logged rainfall for January for data set FL
### TABLE 51a

**ACTUAL VALUES FOR MODEL FITS OF RN**

<table>
<thead>
<tr>
<th>LOGGED ANOMALY</th>
<th>ACTUAL VALUE</th>
<th>MLE</th>
<th>IRWLS C=9</th>
<th>IRWLS C=4</th>
<th>OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1.090</td>
<td>0.000</td>
<td>.042</td>
<td>.258</td>
<td>.255</td>
<td>.107</td>
</tr>
<tr>
<td>-.460</td>
<td>.330</td>
<td>.218</td>
<td>.397</td>
<td>.396</td>
<td>.267</td>
</tr>
<tr>
<td>-.190</td>
<td>.330</td>
<td>.379</td>
<td>.464</td>
<td>.464</td>
<td>.370</td>
</tr>
<tr>
<td>.010</td>
<td>.670</td>
<td>.523</td>
<td>.515</td>
<td>.516</td>
<td>.456</td>
</tr>
<tr>
<td>.160</td>
<td>.670</td>
<td>.629</td>
<td>.552</td>
<td>.554</td>
<td>.522</td>
</tr>
<tr>
<td>.360</td>
<td>.670</td>
<td>.753</td>
<td>.602</td>
<td>.604</td>
<td>.609</td>
</tr>
<tr>
<td>.500</td>
<td>.670</td>
<td>.821</td>
<td>.635</td>
<td>.638</td>
<td>.666</td>
</tr>
<tr>
<td>.980</td>
<td>1.000</td>
<td>.949</td>
<td>.739</td>
<td>.743</td>
<td>.824</td>
</tr>
</tbody>
</table>

### TABLE 51b

**ACTUAL VALUES FOR MODEL FITS OF FL**

<table>
<thead>
<tr>
<th>LOGGED ANOMALY</th>
<th>ACTUAL VALUE</th>
<th>MLE</th>
<th>IRWLS C=9</th>
<th>IRWLS C=4</th>
<th>OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1.820</td>
<td>.330</td>
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<td>.219</td>
<td>.108</td>
<td>.113</td>
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<tr>
<td>-1.000</td>
<td>0.000</td>
<td>.249</td>
<td>.326</td>
<td>.223</td>
<td>.232</td>
</tr>
<tr>
<td>-.460</td>
<td>0.000</td>
<td>.354</td>
<td>.409</td>
<td>.336</td>
<td>.348</td>
</tr>
<tr>
<td>-.200</td>
<td>.670</td>
<td>.412</td>
<td>.451</td>
<td>.400</td>
<td>.412</td>
</tr>
<tr>
<td>.110</td>
<td>.330</td>
<td>.483</td>
<td>.503</td>
<td>.480</td>
<td>.492</td>
</tr>
<tr>
<td>.140</td>
<td>.330</td>
<td>.490</td>
<td>.507</td>
<td>.487</td>
<td>.500</td>
</tr>
<tr>
<td>.200</td>
<td>0.000</td>
<td>.504</td>
<td>.517</td>
<td>.503</td>
<td>.516</td>
</tr>
<tr>
<td>.340</td>
<td>.670</td>
<td>.536</td>
<td>.541</td>
<td>.540</td>
<td>.553</td>
</tr>
<tr>
<td>.500</td>
<td>.670</td>
<td>.573</td>
<td>.567</td>
<td>.581</td>
<td>.594</td>
</tr>
<tr>
<td>.610</td>
<td>.670</td>
<td>.598</td>
<td>.585</td>
<td>.609</td>
<td>.621</td>
</tr>
<tr>
<td>.750</td>
<td>1.000</td>
<td>.629</td>
<td>.607</td>
<td>.643</td>
<td>.655</td>
</tr>
<tr>
<td>1.140</td>
<td>1.000</td>
<td>.709</td>
<td>.667</td>
<td>.731</td>
<td>.741</td>
</tr>
</tbody>
</table>

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TABLE 51c

ACTUAL VALUES FOR MODEL FITS OF SC

<table>
<thead>
<tr>
<th>LOGGED ANOMALY</th>
<th>ACTUAL VALUE</th>
<th>MEL</th>
<th>IRWLS C=9</th>
<th>IRWLS C=4</th>
<th>OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1.410</td>
<td>.330</td>
<td>.367</td>
<td>.352</td>
<td>.372</td>
<td>.266</td>
</tr>
<tr>
<td>-1.070</td>
<td>0.000</td>
<td>.381</td>
<td>.380</td>
<td>.411</td>
<td>.300</td>
</tr>
<tr>
<td>-.960</td>
<td>.330</td>
<td>.385</td>
<td>.389</td>
<td>.424</td>
<td>.312</td>
</tr>
<tr>
<td>-.550</td>
<td>.330</td>
<td>.402</td>
<td>.423</td>
<td>.473</td>
<td>.358</td>
</tr>
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<td>-.260</td>
<td>.670</td>
<td>.414</td>
<td>.448</td>
<td>.507</td>
<td>.393</td>
</tr>
<tr>
<td>-.100</td>
<td>.330</td>
<td>.421</td>
<td>.462</td>
<td>.526</td>
<td>.412</td>
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<tr>
<td>.020</td>
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<td>.426</td>
<td>.473</td>
<td>.541</td>
<td>.427</td>
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<td>.433</td>
<td>.489</td>
<td>.562</td>
<td>.449</td>
</tr>
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<td>.670</td>
<td>.437</td>
<td>.496</td>
<td>.572</td>
<td>.460</td>
</tr>
<tr>
<td>.400</td>
<td>.670</td>
<td>.442</td>
<td>.506</td>
<td>.586</td>
<td>.475</td>
</tr>
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<td>.460</td>
<td>1.000</td>
<td>.444</td>
<td>.511</td>
<td>.593</td>
<td>.482</td>
</tr>
<tr>
<td>.560</td>
<td>.670</td>
<td>.448</td>
<td>.520</td>
<td>.604</td>
<td>.495</td>
</tr>
<tr>
<td>.690</td>
<td>0.000</td>
<td>.454</td>
<td>.532</td>
<td>.619</td>
<td>.511</td>
</tr>
<tr>
<td>.780</td>
<td>.670</td>
<td>.458</td>
<td>.539</td>
<td>.629</td>
<td>.523</td>
</tr>
<tr>
<td>.970</td>
<td>.330</td>
<td>.466</td>
<td>.556</td>
<td>.650</td>
<td>.547</td>
</tr>
<tr>
<td>1.250</td>
<td>1.000</td>
<td>.478</td>
<td>.580</td>
<td>.680</td>
<td>.581</td>
</tr>
</tbody>
</table>
VII. VALIDATION OF LOGISTIC MODELS

A. GENERAL

The various parameters that were estimated in the previous section all may be subject to some sort of validation. However, this paper will only view the validation for the maximum likelihood approach on all data sets and the IRWLS (C=4) approach on data set SC. The validation will be conducted against the reserved, independent, data sets of years 1975 through 1980. These are the same data sets as used in section IV.

Table 52 portrays the reserved data, in a form for logistic analysis, and Figure 109 is a display of the derived contingency tables for the reserved data.
<table>
<thead>
<tr>
<th>YEAR</th>
<th>DATA SET RN</th>
<th>X</th>
<th>COMPLEMENT</th>
<th>Y</th>
<th>DATA SET FL</th>
<th>X</th>
<th>COMPLEMENT</th>
<th>Y</th>
<th>DATA SET SC</th>
<th>X</th>
<th>COMPLEMENT</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>1975</td>
<td>-0.739</td>
<td></td>
<td>12.92</td>
<td></td>
<td>1975</td>
<td>-0.470</td>
<td>12.58</td>
<td></td>
<td>1975</td>
<td>-0.535</td>
<td>17.97</td>
<td></td>
</tr>
<tr>
<td>1977</td>
<td>-0.477</td>
<td></td>
<td>11.14</td>
<td></td>
<td>1977</td>
<td>-0.470</td>
<td>11.10</td>
<td></td>
<td>1977</td>
<td>0.352</td>
<td>10.03</td>
<td></td>
</tr>
<tr>
<td>1978</td>
<td>0.883</td>
<td></td>
<td>19.62</td>
<td>1</td>
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<td>---</td>
<td></td>
<td>1980</td>
<td>0.405</td>
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</tr>
</tbody>
</table>

**TABLE 52**

RESERVED DATA IN FORM FOR THE LOGISTIC ANALYSIS
Figure 109. 2x2 contingency Tables of reserved data controlled by the anomaly of January rainfall. The complement is the anomaly of the rest-of-year rainfall.

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<thead>
<tr>
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<td>3</td>
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<table>
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<td>1</td>
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<table>
<thead>
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</tr>
<tr>
<td></td>
<td>+</td>
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<td></td>
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<td>2</td>
<td>5</td>
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</tr>
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</table>
B. RESULTS

1. Data set RN

The model proposed by the maximum likelihood parameters is

$$\theta_t = \frac{e^{0.0618+2.9183X_t}}{1 + e^{0.0618+2.9183X_t}}$$

This model, when applied to the reserved data yields Table 53.

<table>
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<th>YEAR</th>
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<th>0</th>
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<tbody>
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<td>-</td>
<td>.91</td>
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</table>

The $\theta_t$ is interpreted, again, as: The conditional probability that the complement, the total rainfall for February through December, will be above its mean value, given that the logged January anomaly was $X_t$. Thus it appears that this model tends to predict the direction of the complement's deviation well. Figure 110 is a plot of the estimated probabilities against the actual complement anomaly. For an acceptable fit, this plot should show an upward to the right slope, which it does.
2. Data Set FL

This data set is quite similar to the RN data, except that the slope parameter is only a third of that of RN. The model is

\[ \theta_t = \frac{e^{-.171+.9325X_t}}{1 + e^{-.171+.9325X_t}} \]  

VII.2
TABLE 54

RESULTS OF LOGISTIC VALIDATION
ON DATA SET FL

<table>
<thead>
<tr>
<th>Year</th>
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<th>Y</th>
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<tr>
<td>1980</td>
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<td>-</td>
<td>0.60</td>
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</table>

A plot of the probabilities against the complement anomalies is in Figure 111.

Figure 111. Plot of θ versus complement anomalies for data set FL

This fit is not as good as that for data set RN. The outlier, or false prediction of 1979 may not, however, be far out of line. The sparsity of points for which the complement anomaly was positive detracts from the validation effort.
3. Data Set SC

The maximum likelihood model is

\[ \theta_t^{(1)} = \frac{e^{-\cdot3025+.171X_t}}{1 + e^{-\cdot3025+.171X_t}} \]  

and the IRWLS model is

\[ \theta_t^{(2)} = \frac{e^{\cdot1537+.4799X_t}}{1 + e^{\cdot1537+.4799X_t}} \]

and the tabular results are in Table 55.

TABLE 55

RESULTS OF VALIDATION ON DATA SET SC

<table>
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<tr>
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<th>Y</th>
<th>( \theta_t^{(1)} )</th>
<th>( \theta_t^{(2)} )</th>
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<td>.58</td>
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<td>1979</td>
<td>.512</td>
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<td>.45</td>
<td>.60</td>
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<tr>
<td>1980</td>
<td>.405</td>
<td>-</td>
<td>.44</td>
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and the plot of the probabilities versus the complement anomalies is in Figure 112.
C. DISCUSSION

The validation of the maximum likelihood models for data sets RN and FL appears to be acceptable. However, data set SC does not appear to be acceptably modeled. In fact, as Figure 112 shows, the complement appears to be almost independent of the control. This is also shown by Figure 105 where it can be seen that the contours are very flat and circular about the origin of the (α, β) coordinate system.

The one apparent outlier of data set FL may be viewed as very close, therefore that model can also be assumed to be validated.
VIII. FURTHER FINDINGS

A. SUMMER MONTHS

The further investigation of the summer months, to parallel the modeling of the winter months, yielded some interesting results. These results are shown here with no attempt at analysis.

The summer months appear to be increasing in total rainfall and in variance. This is more true for the Peninsula data sets than for the Valley data set. Figures 113 (RN), 114 (FL), and 115 (SC) show the by-month series of summer months. The total summer rainfall series by year are shown in Figures 116 (RN), 117 (FL), and 118 (SC). The reserved data are not included, yet it can be shown to continue the indicated trends.
Figure 113. Monthly plot of summer months only, means removed, for data set RN

Figure 114. Monthly plot of summer months only, means removed, for data set FL
Figure 115. Monthly plot of summer months only, means removed, for data set SC

Figure 116. Yearly plot of total summer rainfall for data set RN
Figure 117. Yearly plot of summer month rainfall for data set FL

Figure 118. Yearly plot of total summer rainfall for data set SC
A. SIGNIFICANCE OF JANUARY

The identification of January as a possible predictor for its eleven month complement raises further questions. One of the questions is in determining which part of the complement lends the most towards its predictability. Figure 119 is a plot of the log-odds and chi-square statistics for the cumulative complements. Each progressive column, to the right, of Figure 119 indicates these statistics for another cumulated month, i.e., the first column compares the anomalies of January and February by itself, the second column is a comparison of January to February plus March, and so on until the last column is a comparison of January to the entire eleven month complement.

Several occurrences to be noted from the figure are:

(1) The log-odds are consistently greater than zero.
(2) The lack of increased odds and significance during the summer months.
(3) The similarity of RN to FL and their combined difference to SC in the fall.

These indications suggested a further look at January versus the fall months only. This analysis is displayed in Figure 120. The vertical scales of Figure 119 and Figure 120 are the same, yet the horizontal scales differ. This figure has five major divisions. The left-most division looks at January versus singular months in the fall. The second division looks at January versus pairs
of months in the fall, and so on until the right-most column, which is January versus the total fall rainfall. This figure yields no apparent significance, and unstable odds.

The combined information of Figures 119 and 120 are mildly confusing. One possible explanation may be that the summer months somehow cumulate significance and deviation direction, in order to allow the fall contribution. This possible synergistic affect should be explored further.
Figure 119. Log-odds and significance versus additional months cumulated through the year.
Figure 120. Log-odds and significance versus additional months of the fall
IX. SUMMARY

The analysis of rainfall data is carried out in a comprehensive way. The autoregressive Markovian model of the early sections could not stand up to validation, but it did point to some sort of dichotomy between the seasons.

2x2 contingency analysis was effective in that it brought attention to the predictive ability of January. This identification of January, when followed by the logistic analysis was seen to be successful in two of the three data sets. Thus, the primary conclusion of this thesis is the predictive ability of January rainfall.

The physical reasoning behind this finding must be left to the meteorologist. Further study of the approach used here may lead to improvement in seasonal or annual rainfall forecasts for certain climatic regions.
### APPENDIX A

**DATA SET RN**

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<th>YEAR</th>
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187
Logged Anomalies

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Reserved Data

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| 1976 | 1.450 | .600 | 1.050 | 2.450 | .460 | 1.000 | .140 | .970 | .080 | 0.000 | 0.000 | .480 |
| 1977 | .020 | .400 | 5.600 | 9.990 | 8.400 | 7.070 | 3.600 | .030 | 0.000 | 0.000 | 0.000 | .360 |
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