Gigawatt Microwave Emission from a Relativistic Reflex Triode

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**Gigawatt Microwave Emission from a Relativistic Reflex Triode.**

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**Abstract**

Single microwave bursts in X-band of 10-ns duration at gigawatt power levels have been obtained at the Harry Diamond Laboratories with the relativistic reflex triode. The associated relativistic space-charge oscillations have rich high-frequency content. The dominant radiated modes are determined by gap spacing, beam diameter, and gap voltage. The theory of the collective electron space-charge oscillations and the resultant microwave power spectrum is reviewed and compared with experiment.
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1. INTRODUCTION

Gigawatt microwave power levels in X-band have been obtained\(^*\) at the Harry Diamond Laboratories by using a relativistic-electron-beam reflex triode.\(^1\) In these experiments, explosive electron emission\(^2\) from a carbon cathode delivered \(\sim 15\) to \(20\) kA average current through the triode region in a \(25\)-ns pulsed accelerating potential of \(1\) to \(2\) MV (peak). The grid, \(\sim 1\) cm from the emission cathode, consisted of a \(0.25\)-mil (6.35-\(\mu\)m) aluminized Mylar foil. An external magnetic field directed along the triode axis was \(0.1\) to \(0.4\) Tesla. The associated relativistic space-charge oscillations\(^3\) had rich frequency content. The dominant modes were determined by gap spacing, gap voltage, and magnetic field. The polarization was primarily along the beam. Single microwave bursts of \(\sim 10\) ns at gigawatt power levels were achieved. The conversion efficiency of electron beam power to microwave power was \(\sim 1\) to \(2\) percent.

The theory of the collective electron space-charge oscillations in the reflex triode and the resultant microwave power spectrum and comparison with experiment were recently summarized in an oral presentation at the 21st Annual Meeting of the Division of Plasma Physics of the American Physical Society in Boston.\(^4\) This report documents that presentation.

In section 2, the reflex triode design is described. In section 3, the one-dimensional time-dependent relativistic sheet model of the triode dynamics is outlined. In section 4, the calculated space-charge oscillations, charge bunching, virtual cathode formation, and potential are discussed. In section 5, the calculated microwave spectrum is described; in section 6, several conclusions are presented.

2. RELATIVISTIC REFLEX TRIODE

The relativistic reflex triode\(^1\) is a high-voltage electron tube with an electrode configuration analogous to that of the older and much smaller triode tube of conventional electronics. Figure 1 shows the tank containing the reflex triode connected to the FX-45 pulsed power source.\(^5\) The latter is a 60-ohm coaxial transmission line charged by a Van de Graaff generator and discharged via a triggered spark gap. The line is charged to a potential 3.0 MV, thereby storing 0.8 kJ of energy. The X-band and Ku-band microwave diagnostic waveguides also are seen in figure 1 facing the window of the triode tank. The reflex triode itself is located inside the tank as shown in figure 2. The anode (grid) consists of an 8-in. (20.3-cm)-diameter copper-plated fiberglass anode holder supporting a thin 6.35-μm aluminized Mylar foil and is connected to the positive center conductor of the FX-45 pulse line. The carbon cathode is 5 cm in diameter, and the cathode-anode gap is 1 cm. The cathode-ground plane gap is 10.5 cm. The emission cathode is attached to the outer conductor of the pulse line, and both are at ground plane potential. A slow pulsed (~300 Hz) axial magnetic field of peak amplitude 0.4 Tesla is applied along the cathode-anode axis in figure 2 (p. 8). Also shown in figure 2 are carbon activation targets for monitoring ion currents produced at the anode.

When the reflex triode is fired, a voltage pulse of ~1 MV moves down the pulse line and across the cathode-anode gap, explosively\(^2\) pulling 15 to 20 kA of average current of electrons from the emission cathode. The physics of the explosive cathode emission is complex.\(^2\) The triode region fills with a relativistic gas of electrons, which undergoes collective relativistic space-charge oscillations about the anode foil. These electron space-charge oscillations are naturally accompanied by intense radiative emissions transverse to the beam and polarized parallel to the beam.

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3. SHEET MODEL OF TRIODE DYNAMICS

To describe the essential underlying electron dynamics in the triode region, we approximate the real three-dimensional time-dependent configuration by the one-dimensional time-dependent configuration shown in Figure 3. The primary motivation for a one-dimensional representation is minimization of computational cost. In support of this is the fact that the applied magnetic field confines the beam in the radial direction. In the limit of an extremely strong magnetic field, the electron motion would be confined to the magnetic field lines. Although
this extreme does not apply for the given experimental configuration, we assumed that the dominant force is that due to the high applied voltage so that, to first order, the electron motion is predominantly along the triode axis. Full determination of the importance of transverse effects awaits the completion of a simulation including the effects of transverse electric and magnetic fields due to electron space charge and currents. In the relativistic regime, magnetic field effects are often very important; however, the one-dimensional model precludes the inclusions of magnetic forces. One would expect the one-dimensional model to be best for the case of a very large ratio of cathode diameter to cathode-anode gap. In this case, ignoring magnetic field effects at least in the interior region of the discharge would be justified.

Figure 2. Reflex triode attached to FX-45 pulse line.
In Figure 3, the cathode and plate planes are taken to be at ground (zero) electrical potential. The anode plane is at the potential of the prescribed voltage pulse.

The next level of abstraction is to represent the relativistic electron gas within the triode region by a sheet representation as depicted in Figure 4. Thus, the electron space-charge density, \( \rho(x,t) \), at any instant, \( t \), as a function of distance, \( x \), from the emission cathode plane is represented by

\[
\rho(x,t) = \lim_{M(t) \to \infty} \sigma_M \sum_{m=1}^{M(t)} \delta(x - x_m(t)).
\]

(1)

Here, \( M(t) \) is the number of sheets in the triode region at time \( t \), \( \sigma_M \) is the charge density of each sheet and is taken to be the same for each sheet, \( \delta \) is the one-dimensional Dirac delta function, and \( x_m(t) \) is the position of the \( m \)th sheet at time \( t \). In practice, the infinite limit in equation (1) must clearly be replaced by a finite one, which we take to be the time averaged number of sheets in the triode region. \( M \) should be chosen as large as simulation cost permits. The dynamics will control coordinates \( x_m(t) \) and spacing of the constant and equal charge density sheets so that regions of high charge density will have a high density of sheets.

A primary theoretical weakness of the sheet model is that, in practice, each sheet will correspond to \( \sim 10^{10} \) electrons, whose separate degrees of freedom are ignored and which are effectively constrained to move bound together as a whole. This same fundamental criticism holds also for particle in-cell models and, for that matter, for any "fluid element" representation. For the model at hand, this problem is less serious, the larger the choice of \( M \). The final justification for the
sufficient largeness of \( M \) is the convergence of quantities of interest. However, in practice, establishing such convergence is prohibited by cost and the difficulty of even quasi-analytical proof.

![Figure 4. Sheet model.](image)

In the simple model presented here, ion formation at the anode and the resulting ionic component of the charge distribution are ignored on the grounds that significant ion displacement will be relatively delayed because of the large ion-to-electron-mass ratio. It is the ion current that ultimately produces gap closure and limits the duration of the applied voltage pulse.

The electric field, \( E(x_n,t) \), at location \( x_n \) of the nth sheet at time \( t \), due to both the externally applied voltage, \( V(t) \), and the space-charge fields arising from all the other sheets, is determined by solving Poisson's equation, which results in

\[
E(x_n,t) = \begin{cases} 
\frac{\sigma}{\varepsilon_0} \left[ -\frac{M_1(t) - M_{11}(x_n(t))}{2} \right] & , 0 < x_n < d_1 \\
\frac{\sigma}{\varepsilon_0} \left[ -\frac{M_2(t) - M_{21}(x_n(t))}{2} \right] + \frac{V(t)}{d_2 - d_1} & , d_1 < x_n < d_2 
\end{cases}
\]

\[ E(x_n,t) = \left\{ \begin{array}{ll}
\frac{\sigma}{\varepsilon_0} \left[ -\frac{M_1(t) - M_{11}(x_n(t))}{2} \right] & , 0 < x_n < d_1 \\
\frac{\sigma}{\varepsilon_0} \left[ -\frac{M_2(t) - M_{21}(x_n(t))}{2} \right] + \frac{V(t)}{d_2 - d_1} & , d_1 < x_n < d_2 
\end{array} \right. 
\]
The upper expression holds at a sheet lying on the emission cathode side of the anode and the lower expression, on the plate side. Here $d_1$ is the cathode-anode gap, $d_2$ is the cathode-plate separation, $c$ is the sheet charge density, $\varepsilon_0$ is the permittivity of free space, $M_1(t)$ and $M_2(t)$ are the number of sheets on the cathode and plate sides of the anode, respectively, at time $t$, $M_{11}(x_n(t))$ is the number of sheets between the cathode and the $n$th sheet when it is on the cathode side of the anode, $M_{21}(x_n(t))$ is the number of sheets between the anode and the $n$th sheet when it is on the plate side, and $\bar{X}_1(t)$ and $\bar{X}_2(t)$ are the mean separations from the cathode for all sheets on the cathode and plate sides, respectively, of the anode.

The time step for the model is taken to be a small fraction of a cathode-anode light transit time. Since the electrons are limited by relativity to velocities less than the velocity of light, this choice of time step should provide sufficient time resolution of the electron dynamics. Thus, the time step, $\Delta t$, is given by

$$\Delta t = \frac{d_1}{Nc}$$

where $N$ is some large number and $c$ is the speed of light.

Sheet electron momenta $p_n(t+\Delta t)$ and positions $x_n(t+\Delta t)$ at time $t + \Delta t$ are then easily expressed in terms of those at time $t$ by use of the Lorentz force equation, by which one obtains

$$p_n(t+\Delta t) = p_n(t) + eE_n(t)\Delta t$$

$$x_n(t + \Delta t) = x_n(t) + \frac{1}{2} \left[ 1 + \left( \frac{p_n(t)}{mc} \right)^2 \right]^{-3/2} \left[ \frac{p_n(t)}{mc} \right] \frac{p_n(t+\Delta t)}{mc} \Delta t$$

Index $n$ corresponds to the $n$th sheet, and $e$ and $m$ are the charge and the mass of the electron, respectively. A sheet is allowed to enter the triode region only at those time steps for which the total electric field points into the emission cathode. A sheet is taken to leave the system whenever it hits the plate or returns to the emission cathode. A sheet is also subtracted whenever the energy that it loses in passing through the anode foil reduces its kinetic energy to zero. Thus, the number of sheets, $M(t+\Delta t)$, at time $t + \Delta t$ is given in terms of the number of sheets at time $t$ by
\[ N(t+\Delta t) = \mathcal{N}(t) + \Theta(-\mathbf{E}(0,t)) \]

\[
\begin{align*}
\mathcal{N}(t) & - \sum_{m=1}^{\mathcal{N}} \left[ \Theta(d_2 - x_m(t)) \Theta(x_m(t+\Delta t) - d_2) \\
+ \Theta(x_m(t)) \Theta(-x_m(t+\Delta t)) \\
+ \Theta(d_1 - x_m(t)) \Theta(x_m(t+\Delta t) - d_1) \Theta(\Delta p_m - p_m(t+\Delta t)) \\
+ \Theta(x_m(t) - d_1) \Theta(d_1 - x_m(t+\Delta t)) \Theta(\Delta p_m + p_m(t+\Delta t)) \right] 
\end{align*}
\]  

Here, \( \Theta \) is the theta function, \( \mathbf{E}(0,t) \) is the total electric field at the emission cathode, and \( \Delta p_m \) is the momentum loss experienced by the \( m \)th sheet in passing through the anode foil as determined by ionization and radiative loss tables.

The surface charge density, \( \sigma \), of the sheets is determined by the following considerations. The triode charge in the triode region will build up to the point where it can contain no more; namely, further injection of charge will result in charge ejection. Under such a condition of space-charge saturation, we have shown\(^3\) that, in the parameter regime of interest, the total time averaged charge, \( \bar{Q} \), in the triode region is proportional to the applied voltage, \( V \), namely,

\[ \bar{Q} = KV \]  

We call the constant of proportionality, \( K \), the space-charge capacity of the triode. It is independent of applied voltage and is determined only by the triode geometry.

The time averaged charge may be expressed in terms of the time averaged number of sheets, \( \bar{N} \), by

\[ \bar{Q} = A \sigma \bar{N} \]  

where \( A \) is the cross-sectional area of the beam, which is assumed equal to the cathode area, and \( \sigma \) is the sheet surface charge density. By combining equations (7) and (8), the required sheet surface charge density is given by

\[ \sigma = \frac{KV}{A} \]  

---

Therefore, in practice one chooses the averaged number of sheets to be some large, but affordable number to faithfully represent the space-charge distribution; the space-charge capacity is self-consistently calculated under conditions of space-charge saturation; the voltage and the beam area are given; and the sheet surface charge density is thereby determined.

Equations (1) to (9) form the algebraic basis for the numerical simulation. A FORTRAN program has been written whose present run cost is between $30 and $100 on the IBM System 370 computer. A typical set of program parameters in the experimental regime of current interest is \(d_{1} = 1\) cm and \(N = 120\), resulting in 0.3-ps time resolution; \(K = 8\) pF; a voltage ramp, \(V(t)\), rises to \(V = 2\) MV in 25 ns and then falls off linearly in 10 ns; \(R = 300\) sheets; \(d_{2} = 10.5\) cm; and \(A = 20\) cm\(^2\). In the following sections, the results of such simulations are discussed.

4. ELECTRON SPACE-CHARGE DYNAMICS

Numerical simulations based on the dynamical model presented in the preceding section reveal several significant characteristics of the relativistic electron space-charge dynamics in the triode. At the onset of the voltage pulse across the cathode-anode gap, electrons are explosively pulled out of the cathode plasma and fill up the triode region. The total space charge, however, is not monotonically increasing, but oscillates in time while rising to a saturated time averaged total charge. Electrons entering the gap with favorable phases relative to a given frequency component of the resultant space-charge fields give up energy to the fields and remain in the triode region, while those with unfavorable phases gain energy from the fields and are ejected from the triode region. Favorably phased electrons tend to be grouped together spatially since they enter about the same time. Also, space-charge limiting periodically limits the subsequent entrance of electrons at the emission cathode. These mechanisms give rise to electron space-charge bunching. While the electron bunches oscillate back and forth about the anode, they also interact with one another, ejecting and capturing electrons from one another and thereby being depleted and growing in size. Bunches are born and bunches die. This is the regime of strong Langmuir-like turbulence of the relativistic electron plasma.

Once the triode is saturated, the total charge oscillates about the mean saturated value. A fluctuating virtual cathode forms on the plate side of the anode at a time averaged distance approximately equal to the cathode-anode gap. Figure 5 displays a characteristic partial time evolution of the electron space-charge distribution in the triode region. This case is for a cathode-anode gap of 1 cm, a beam area of 20 cm\(^2\), and a constant applied voltage of 1 MV. The plot covers a 100-ps time span that is 564 ps into the applied voltage pulse. This time span
was chosen to correspond to the period associated with the dominant spectral component of the space-charge oscillations, which in this case is 10 GHz. The spatial axis has its origin at the emission cathode, 1 cm down this axis is the anode plane, and the plate is beyond the plot at 10.5 cm. The electrons are concentrated within ~2 cm from the emission cathode with highest concentration just beyond the anode plane on the plate side. Transient bunching is evident with effective high-frequency sloshing about the anode. Spectral analysis of these space-charge oscillations reveals a broad spectrum of peaks in the gigahertz regime separated by ~0.2 to 0.4 GHz and peaking at 10 GHz. The location of the virtual cathode, which is characterized by a strong depletion of the charge density, is about 2 cm from the cathode and undergoes high-frequency oscillations. Thus at 564 ps and 664 ps, it is at ~2.5 cm, and at 614 ps it is at ~1.7 cm. For this example, at least, its position oscillates at the dominant frequency of ~10 GHz. One would expect a frequency of this order of magnitude to dominate, based on qualitative geometric considerations of near light velocity periodic transits of the 1-cm gap. Also of note is that small bunches of electrons do exist beyond the virtual cathode on the plate side. In fact, periodically some of these bunches hit the plate and are thereby ejected from the system.

Figure 5. Space-charge density over one dominant cycle as function of distance from cathode for constant applied voltage of 1 MV.

The characterization of the virtual cathode dynamics is more evident in figure 6, which plots the total electrical potential during extremals of the virtual cathode position in figure 5 corresponding to a half cycle displacement. The location of the virtual cathode is characterized by a near discontinuity in the slope of the potential with a near linear spatial dependence on the plate side. The latter is to be ex-
pected on the basis of Poisson's equation and the approximately vanishing charge density on the plate side of the virtual cathode. Also of note is that the electrical potential at the virtual cathode is large. This feature is unique to the inherently time-dependent dynamics. Both the position and the potential of the virtual cathode undergo high-frequency oscillations.

One would expect the high-frequency oscillations of the transient space-charge bunches in the triode region to radiate coherently like a superposition of dipole oscillators with polarization parallel to the beam. In the next section, the resultant calculated microwave power spectrum is discussed.

5. MICROWAVE SPECTRUM

It is assumed here that the real three-dimensional beam dynamics may be approximated by the one-dimensional model. For the cylindrical beam of radius $R$, the average power spectral density per steradian, $<d^2P_\perp/d\omega\,d\Omega>$, radiated perpendicular to the beam can be shown to be given by

$$\left\langle \frac{d^2P_\perp}{d\omega\,d\Omega} \right\rangle = \frac{\mu_0\pi\sigma^2p^0}{4cT} \omega^2 |\Sigma(\omega)|^2 F^2(\omega)$$

(10)
where

$$\Sigma(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} dt \ e^{-i\omega t} \ M(t) \ \sum_{m=1}^{\infty} v_m(t)$$

and

$$F(\omega) = \frac{2J_1 \left( \frac{\omega R}{c} \right)}{\omega R/c}.$$  \hspace{1cm} (11)

Here, $d\Omega$ is the differential solid angle, $\mu_0$ is the permeability of free space, $\sigma$ is the sheet surface charge density, $R$ is the beam radius, $c$ is the speed of light, $T$ is the voltage pulse duration, $\omega$ is the angular frequency, $M(t)$ is the number of sheets at time $t$, $v_m(t)$ is the velocity of the $m$th sheet at time $t$, and $J_1$ is the first order Bessel function of the first kind. Equation (10) is obtained by solving the wave equation with a current distribution represented by the calculated sheet dynamics, including radiative time delays only perpendicular to the beam, and by using the ordinary dipole far field approximation. The quantity $\Sigma(\omega)$ is the time Fourier transform of the sum of the sheet velocities. The quantity $F(\omega)$ is a geometric interference form factor resulting from the relative radiative time delays across the beam cross section. Computations of the power spectrum for an applied voltage ramp rising to 1 MV in 10 ns with a 9.5-mm gap are shown in figure 7. Those for 2 MV in 25 ns and a 1-cm gap are shown in figure 8. Plotted is the average transverse power spectral density as a function of frequency. The dips in the spectra around 7, 13, and 19 GHz, etc., are caused by the interference form factor, equation (12); namely, at those frequencies, $F(\omega)$ is vanishing and one has destructive interference. Aside from the modulation due to the interference form factor, the overall spectrum is broad with a high density of narrow spectral peaks separated by ~0.2 to 0.4 GHz. These multitudinous peaks are associated with the many mechanical modes of electron oscillation discussed in section 4.

However, the most intense spectral peak is at ~10 GHz in X-band, and it is fortuitous that the interference form factor also peaks there. This peak corresponds to the dominant mode of electron space-charge oscillation and also to that of the virtual cathode motion as discussed in section 4. Intense microwave emission also occurs in the L-, S-, C-, Ku-, and X-bands of the spectrum.
Figure 7. Calculated average power spectrum for applied voltage ramp rising to 1 MV in 10 ns with 9.5-mm gap.
Figure 8. Calculated average power spectrum for applied voltage ramp rising to 2 MV in 25 ns with 1-cm gap.
Comparisons of these calculated microwave spectra with experiment show close agreement between calculated and observed frequencies and agreement to within a factor of two in average power. Thus, in recent experiments at the Harry Diamond Laboratories, average power levels of ~0.1 GW and peak power levels of ~1 GW centered in X-band at ~10 GHz were observed. Intense emissions in S-, Ku-, and K-bands also were observed. Experimental uncertainties in the voltage, current, and microwave measurements further underline the near agreement with the model calculations. Of particular importance is that the observed microwaves are dominantly polarized parallel to the electron beam; such polarization lends additional credence to the one-dimensional model.

The conversion efficiency of electron beam to X-band microwave power was only ~2 percent. However, this low efficiency does not indicate any fundamental limitation and most likely results from the poor impedance match between the triode (~6 ohms) and the FX-45 (~60 ohms). Of note is that 30-percent efficiency at gigawatt power levels in S-band has been achieved with a triode at the Tomsk Polytechnical Institute in the Soviet Union. The higher efficiency is likely due to the lower frequencies involved, the use of a resonant structure, and a good machine-triode impedance match. Earlier related microwave production experiments with a reflex triode at the Naval Research Laboratory resulted in 1.5-percent efficiency in X-band at 100-MW power levels.

6. CONCLUSIONS

The relativistic one-dimensional time-dependent sheet model of the electron space-charge dynamics in the reflex triode reveals the occurrence of extensive transient space-charge bunching, a broad spectrum of multigigahertz frequency space-charge oscillations about the anode, and formation and high-frequency oscillation of a virtual cathode. Calculations of the resultant microwave spectra reveal broad band intense microwave production centered in X-band and consistent with experimental observation.

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Although the model ignores possible important three-dimension-1 effects—in particular, those due to magnetic fields—and employs a coarse grained sheet model representation, it does successfully characterize the main features of the radiated microwave spectrum. In particular, the model explains the occurrence of near gigawatt microwave power levels in X-band with polarization parallel to the beam.

It should be emphasized, however, that the one-dimensional model precludes parametric analyses of the effects of applied and induced magnetic fields. Recent experiments at the Harry Diamond Laboratories reveal a sensitive dependence of microwave production on the applied magnetic field.\textsuperscript{10,11} The fundamental theoretical problem of sheet dynamics as a representation of autonomous electron motion also should be kept in mind, especially as it might bear on very-high-frequency or low-wavelength phenomena.

Of special importance is the fact that gigawatt power levels are obtainable in the reflex triode without the aid of resonators. It is likely that tens of gigawatts could be obtained by careful resonator design. Special problems arising from the requirement of high voltage breakdown avoidance between the electrodes and the resonators must be solved. Also, the presence of a resonator will significantly alter the spectral distribution of the space-charge oscillations, and therefore the one-dimensional model will be inadequate for resonator design.


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