A FLUIDIC VOICE COMMUNICATION SYSTEM
AND DATA LINK

by
Tadeusz M. Drzewiecki

March 1980

Thesis Advisor: R. H. Nunn

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**Title:** A Fluidic Voice Communication System and Data Link

**Authors:** Tadeusz M. Drzewiecki

**Performing Organization Name and Address:**
Naval Postgraduate School
Monterey, CA 93940

**Report Date:** March, 1980

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**Abstract:**
This thesis presents a comprehensive dynamic analysis of fluidic laminar proportional amplifiers (LPA) and a subsequent design of a broad-band voice communication system and narrow-band data link that demonstrates the utility of the analysis.

Starting from first principles, the governing equations for the lumped parameter representation of the various flow regimes found in an LPA are derived. From these governing equations, in the Laplace domain, equivalent...
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Using the analysis as a tool, an engineering guide was developed for the dynamic characteristics of LPAs especially the HDL STD MOD 3.1.1.8. Operating bandwidths of greater than 14 kHz can be expected for amplifiers with a nozzle width of 0.25 mm. Ultrasonic operation is feasible with smaller devices.

Using the engineering guide, an intercom and an FM data transmission system were designed, built and experimentally evaluated. Performance parameters include a bandwidth of 1-4 kHz for the voice system and a narrow band of 6-6.7 kHz for the FM carrier. FM demodulation results in a dynamic range of 400 at 3 Hz with a frequency discrimination of 0.5 - 40 Hz depending on input amplitude. Transmission distances of 5-10 m have been demonstrated.
A FLUIDIC VOICE COMMUNICATION SYSTEM AND DATA LINK

by

Tadeusz M. Drzewiecki

B.E. (Mechanical), City College of the City University of New York, 1966
M.E. (Mechanical), City College of the City University of New York, 1968

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for the degree of

DOCTOR OF ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL

March 1980

Author

Tadeusz M. Drzewiecki

Approved by

D. J. Collins, Professor
Aeronautics

T. M. Houlihan, Assoc. Prof.
Mechanical Engineering

D. E. Kirk, Professor
Electrical Engineering

J. M. Kirshner
Harry Diamond Laboratories

P. J. Marto, Professor
Mechanical Engineering

R. H. Nunn, Assoc. Professor
Mechanical Engineering

R. D. Strum, Assoc. Professor
Electrical Engineering

Chairman, Department of Mechanical Engineering

Approved by

Jack L. Boles
Academic Dean
ABSTRACT

This thesis presents a comprehensive dynamic analysis of fluidic laminar proportional amplifiers (LPA) and a subsequent design of a broad-band voice communication system and narrow-band data link that demonstrates the utility of the analysis.

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Using the analysis as a tool, an engineering guide was developed for the dynamic characteristics of LPA's especially the HDL STD MOD 3.1.1.8. Operating bandwidths of greater than 14 kHz can be expected for amplifiers with a nozzle width of 0.25 mm. Ultrasonic operation is feasible with smaller devices.
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FOREWORD

The analysis of fluidic amplifiers has been considered by many authors, but I would like to think that the present effort culminates the pioneering work started by Frank Manion of the Harry Diamond Laboratories. It was his experience and insight that led to the successful development of laminar jet devices as we know them today. It was his dynamism and keen engineering acumen that resulted eventually in the successes of laminar systems such as the tank turret stabilization system. I hope that this thesis will be accepted as a contribution to the technology, but it should be remembered that the original concepts of laminar systems are attributable to Frank Manion.
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NOMENCLATURE

\( a_1 \) - spillback coefficient
\( A \) - cross-section area, m\(^2\)
\( b \) - channel width, m
\( B \) - dimensionless channel width, \( b/b_s \)
\( c \) - speed of sound, m/s
\( c_d \) - LPA supply nozzle discharge coefficient
\( c_{\theta} \) - LPA supply nozzle momentum flux discharge coefficient
\( C \) - capacitance, m\(^3\)/Pa
\( d \) - internal tube diameter, m
\( db \) - decibel
\( E \) - electric potential, volts
\( f \) - frequency, Hz
\( F \) - dimensionless frequency, \( f_b/(c_d (2P_s/\rho)^{1/2}) \)
\( F_y \) - force in \( y \)-direction, N
\( G \) - pressure gain, \( \frac{dp}{dp_c} \)
\( h \) - height, m
\( Hz \) - hertz
\( I \) - electric current, amperes
\( j \) - \((-1)^{1/2}, \)
\( k \) - empirical constant in duct resistance equation
\( K_{1,2} \) - constants in transfer function consolidation
\( L \) - length, m
\( L \) - inductance, kg/m\(^4\)
\( LPM \) - litres per minute
\( m \) - mass, kg
\( mmHg \) - millimeters of mercury of pressure
Nomenclature (con't)

- integer number

**n**

- Reynolds number, \((b_s / \nu) (2 P_s / \rho)^{1/2}\)

\(N_R\)

- modified Reynolds number \(N_R / ((\chi / b_s + 1)(1+1/\sigma)^2)\)

\(NR\)

- pressure, Pa

\(p\)

- dimensionless pressure, \(p / P_s\)

\(P\)

- volumetric flow, \(m^3/s\)

\(Q\)

- radius, m

\(r\)

- resistance, \(kg/(m^4 s)\)

\(R\)

- gas constant, \(m^2/(s^2 \cdot K)\)

\(R_g\)

- Laplace operator

\(\text{Laplace}\)

- time, s

\(t\)

- temperature, °K

\(T\)

- x direction velocity, m/s

\(u\)

- x-direction supply nozzle velocity, m/s

\(U_s\)

- y-, or lateral direction, velocity, m/s

\(v\)

- Bernoulli velocity, \((2P_s / \rho)^{1/2}, m/s\)

\(V_s\)

- general velocity, m/s

\(V\)

- length dimension, m, or coordinate axis

\(x\)

- dimensionless length, \(x / b_s\)

\(X\)

- complex admittance, \(1/Z, m^4 s/kg\)

\(Y\)

- coordinate axis, m

\(z\)

- complex impedance, \(kg/(m^4 s)\)

\(Z\)
Nomenclature (con't)

Greek Symbols

<table>
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<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>( \beta )</td>
<td>bulk modulus, Pa</td>
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<td>( \delta )</td>
<td>deflected jet space, m</td>
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<tr>
<td>( \Delta )</td>
<td>change</td>
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<td>( \zeta )</td>
<td>attenuation factor</td>
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<td>( \pi )</td>
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<td>( \rho )</td>
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<td>( \tau_w )</td>
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<td>( \omega )</td>
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<tr>
<td>( \Omega )</td>
<td>dimensionless circular frequency, ( b_s/c_d W_s )</td>
</tr>
</tbody>
</table>
Nomenclature (con't)

Subscripts

B - blocked
bw - bandwidth
c - control
d - spill back resistance
e - entrained
f - fitting
fb - feedback
g - gas
h - hydraulic
i - input or integer
in - in
j - jet
k - pseudo-impedance
L - load
LPA - laminar proportional amplifier
LJARS - laminar jet angular rate sensor
m - modulus
min - minimum
n - integer
N - noise
o - output
out - out
r - returned
RC - resistive capacitive
RL - resistive inductive
s - supply
sp - splitter
t - distance between downstream control edges
Nomenclature (cont')

Subscripts (cont')

th - supply nozzle straight section
v - vent
w - wall
x - x-direction
XSP - distance to splitter
XVI - distance to vent vane
y - y-direction
1 - side 1
2 - side 2
a - ambient or atmospheric
6 - deflection of jet

Superscripts

- "bar," average value
' - 'prime'
'' - "double dot," second derivative with time
1. INTRODUCTION

1.1 A Historical Perspective

Communication of data, speech and other information in the military and civilian sphere probably goes back as far as the time when the first cave man grunted once for danger and twice for all clear to his compatriots during a hunt. Oral and acoustic communication has persisted through the ages until the dawn of the electronic age with the invention of the telegraph which permitted the virtually instantaneous transfer of electrical pulses along a conductor that were later converted into sounds. With growing sophistication telegraphic information could be imposed directly into markings on paper thus providing a permanent record of the data transmitted. The telephone and finally the radio permitted the transfer of much more data content and of actual speech. These inventions revolutionized the economic, social and military environments. They enabled the military to broaden their scope of operations with information regarding the enemy and deployment of friendly forces. The modern age of electronics ushered in during World War II dramatically increased the rate and quantity of data being transmitted. In addition, with the invention of the radar, electronic air waves were being used for detection as well as transmission. During all this technological expansion, simultaneous efforts were being made to provide for secure transmission as well as the overt and covert interruption and interception of transmissions. Jamming signals were added to the ever increasing spectrum of electromagnetic (EM) signals propagating through space. With the advent of the electronic computer the data rates and handling capabilities took a quantum jump. The number of channels in the radio frequency (RF) spectrum has become fantastic. Sophisticated techniques to increase the capacity of a single channel have allowed the RF spectrum to keep up with demand. With the EM spectrum already
crowded, the nuclear age has provided yet another source of radiated energy, and the recent development of EMP (electromagnetic pulse) devices and particle beam weapons provides more. The overt disruptive transmission of energy such as jamming, EMP and particle beam weapons is aimed at destroying the transmissive medium or the actual transmitting or receiving devices. In a recent article in SIGNAL magazine, the authors describe the modern battlefield and its requirements for reliable communication. This battlefield is a blaze of light and noise in addition to a mass of radio transmissions. Hearing, sight and speech are impaired as well as are electromagnetic transmissions.

Let us regress in time for a moment and paint a different scenario. The preceding perspective has primarily relied on a land based view. Consider, however, the problems of communication within a rigidly bounded structure as in a naval vessel, an aircraft, or for that matter, a large residential dwelling. Ever since the days of the Roman warships directional acoustic transmission of voice has been used. The Romans used crude megaphones to channel human voice energy into a small section of space, while on steamships, passive speaking tubes were effective in providing a communications link between the bridge and various deck levels such as the boiler room. These same tubes were commonly in use at the turn of the century in large residences and hotels as means of summoning servants and relaying household requirements. The electronic age had its effect on this mode of communication wherein the telephone or intercom has replaced these old standby’s. The development of the aircraft occurred totally within the electronic age time frame and as such was not touched by such quaint antiques as the speaking tubes.

*Numerical superscripts refer to bibliographical references.
The development of the battleship and aircraft carrier as a wholly self contained entity or community has posed an interesting dilemma regarding the safety aspects as of high intensity of electromagnetic radiation. Fuel and munitions are stored in this hazardous EM environment. Fumes are ever-present below decks even in well ventilated places, hence, there is an ever-present danger of conflagration or explosion due to electrical sparks, heating or radiation. An interesting example of the latter is the propensity of small bridge wires, used to detonate munitions, to act as antennae for RF signals thus inducing a current and hence producing sufficient heat for initiation of a charge. The safety aspect is the reason why the Navy has been most interested in nonelectrical schemes for doing things, to include communications.

The historical perspective on interpersonal communication systems is one of rapid development following the invention of the telegraph with an ever increasing traffic load and mutual and active interference. As an example of this interference, even hard wire intercoms in an armored vehicle suffer tremendously during the heat of battle with intelligibility deteriorating to the point that communications are often lost between a commander and driver over a space as short as two meters. It is this problem, the loss of communications at relatively close quarters, that this work attempts to solve by applying the non-electrical technology of fluidics.

1.2 The Role of Fluidics in Communication

In 1959, Horton, Bowles and Warren coined the term "fluid amplification" for the process of controlling relatively high energy streams or jets of fluid by low energy ones. Kirshner relates that the principles of this new technology were disclosed in a press release in March 1960. The basis of operation of a fluidic amplifier is shown in figure 1.
Figure 1. Operation of a fluidic amplifier

In the neutral, undeflected or centered position, a jet of fluid emanates from a nozzle, traverses a given distance, and impinges on a dividing wedge commonly called a splitter, whereupon the flow divides equally. If there is no restriction in the channels on either side of the splitter, then equal amounts of flow will exit through the output ports. If the output ports are restricted, then the flow will turn approximately 90° and exit through the vents to ambient. While the flow undergoes the 90° change in direction, it develops equal static pressures at the output ports. When a low energy stream of fluid (or a small pressure difference) is applied to the jet in the vicinity of the nozzle exit, the effect is to deflect it slightly. This small deflection becomes considerable, by geometry, at some distance downstream, hence the amount of fluid impinging on one output is increased and
simultaneously reduced on the other. This, then, produces a differential pressure at the outputs that is considerably greater than the differential pressure that produced the deflection. The ratio of the output pressure differential to the input or control differential describes the function of signal or input amplification, and is called, therefore, "gain." Although this principle has been known and used since 1959, it was not until the early part of the 1970's that low noise, high input impedance, laminar proportional amplifiers (LPA) became available for convenient systems utilization. The laminar nature of the flow accounts for the low noise, and since the narrow disturbance-free jet may be caused to flow in such a way as to almost block off the control channels, the input impedance is made quite high.

Despite the lack of availability of such critical components as the LPA, the basic concept of a fluidic amplifier as a pressure amplifier coupled with the fact that sound is a pressure wave phenomenon led Horton in 1960 to propose the fluidic speech amplifier shown in figure 2.

![Figure 2. Horton's speech amplifier concept.](image-url)

He described the function in the following manner:

"In this figure exponentially curved horn 29 is attached to tube 26. Source 31 provides a constant, continuous source of air to nozzle 15. Anyone speaking into the
enlarged end of this horn will cause pressure pulsation to occur in tube 26. These pulsations will be amplified by system 10. The amplified pulsations pass through tubes 27 and 28 and into horns 37 and 38 respectively. Amplified voice issues from horns 37 and 38.

This simple idea lay fallow for many years for the already cited lack of proper components of sufficient bandwidth and dynamic range. In 1969 HDL working under a Navy contract studied a public address system for use on flight decks, resulting in a public demonstration of the system at the 10th Anniversary of Fluidics ASME sponsored meeting at Georgia Tech in 1970. Although this system did not meet the Navy requirements at that time, it did demonstrate that the bandwidth of fluidic amplifiers was adequate to pass speech. Subsequently, in 1976, a laminar fluidic public address system was built and demonstrated again at the Harry Diamond Laboratories (HDL). The most objectionable drawback, that of background hiss or noise was eliminated. In addition, the task was performed with LPA's that were twice the size of those used previously and since there was considerably more gain and bandwidth, fewer stages of amplification were required. Also due to the laminar nature of the flow, the operating power pressure was considerably lower, 3 kPa as opposed to 45 kPa.

Another fluidic technique for speech amplification and transmission originated a few years after Horton's disclosure of his beam deflection amplifier (figure 1 shows the jet being deflected much as a rigid beam, hence the term beam deflection amplifier) that utilized the inherent amplification of disturbances of a particular frequency in a free shear layer. Unfried discusses such a system and uses the inherent non-linearities to provide modulation and demodulation of a basic carrier frequency at bandwidths to 8 kHz on carriers of up to 17.5 kHz. Figure 3 shows schematically Unfried's
Figure 3. Unfried's\textsuperscript{12} free shear layer acoustic amplifier concept.
concept. The chief drawback of this system was the requirement of a transitional free jet where the breakdown eddies would be modulated. This type of jet is very susceptible to being tripped into turbulence and requires quite precise flow regulation to maintain the appropriate Strouhal and Reynolds numbers.

The transmission of data insofar as communications is concerned can occur at any frequency as is obvious from a comparison of the low bit-rate of the original hand coded Morse messages to the super sophisticated computer-controlled systems used to transmit data from satellites at huge baud rates. All fluidic systems, in fact all communication systems, involve the transmission of data over some distance at some bandwidth. Maximum distance for transmission of fluidic signals with closed loop control is about 10 meters in order to keep the acoustic delay low enough so that the overall bandwidth is over 40 Hz in air. Transmission of data up to 100 meters is discussed by Kirszenblat. The theory of acoustic transmission lines is well developed. Almost any text on acoustics deals with the subject. For example, Rschevkin has an excellent treatment. Indeed, his treatment of the fundamental lumped parameter approach to acoustics is excellent and forms the basis for much analysis in the literature. With regard to fluidic transmission lines, Kirshner and Katz present an excellent treatise thereof. They consider both the lumped and distributed parameters approach and present a quasi-method of characteristics for the solution of the signal propagation problem in long ducts. Roffman and Deadwyler consider signal transmission through circular cross-section lines for their public address system and conclude that audio band pass is possible.

Finally, the concept of an intravehicular fluidic communication system was published by Alexander and Drzewiecki and is shown in figure 4.
Figure 4. A fluidic voice communication system schematic.

At this point excerpts from the introduction to the proposal for this thesis cover some of the remaining points.

"The ability to communicate in the military environment constitutes perhaps the one most important factor that determines the outcome of armed combat. Whether it is the tank commander talking with his gunner, the pilot talking with his bombardier or the ship's captain talking with his missile officer, if there is any loss of information content then there exists an excellent chance that either the target will be lost or that the tables will be turned. With the expansion of modern day technology to include computers, microprocessors and other sophisticated electronics in most major weapons systems, the area of communications has expanded to include man-
machine interaction in addition to the already mentioned man-to-
man interaction. Ship control may be communicated to the steering
mechanism by electronic means, from a potentiometer to a servo
mechanism. The fly-by-wire concept introduced in both the Navy
and Air Force and currently used on the F-16 aircraft is an excel-

lent example of man-machine interaction in that it requires that
human command information be transmitted to the actuators and con-
trollers by wire. Introduce now the electronic warfare environment-
jamming, broad-band electromagnetic (EM) signal traffic, and spurious
EM effects from motors, engines and electronic devices. It has
been estimated that hard-wire radio communications within an M60
tank in a typical combat EM environment can be reduced to as little
as 30-35% information content. There are no comparable figures
available on the failure rate of electronic control systems in EM
environments; however, current design practice for military avionics
requires six-times redundant control paths and control systems.
The use of Kalman filters has become increasingly popular in radar
and fire-control systems but has not as yet made an impact in other
areas, perhaps due to the added complexity.

1.3 Statement of the Problem

While there is some repetition from the earlier two sections,
this helps focus the problem. It is clear that two main areas of
work are identified--research and development.

The research must necessarily involve the mathematical analysis
from first principles of the frequency response of fluidic amplifiers
so that rational design may proceed. As early as 196518 researcher's
have remarked on the high order frequency response of fluidic pro-
portional amplifiers. They noted the appearance of high gain, high
frequency regions that they tacitly assumed could not be explained
by lumped parameter equivalent circuit techniques. Figure 5 is
typical of the observed frequency response at relatively high aspect
ratios *(nozzle height-to-width ratio, h/b)* or = 2.5, for a turbu-
lent jet device. The solid line has been faired in to point out the
multiply resonant character of the amplitude response. In 1967, Moore
et al19 attempted to capitalize on the resonant regions by enhancing
them and thus getting high frequency and high Q, hence good noise rejection in otherwise very low signal-to-noise turbulent devices. They met with limited success in that they were only able to achieve about 1.5 kHz operation. They did, however, provide experimental evidence of the high order modes of operation as shown in figure 6. The solid line represents their attempt to represent the observed data trends.

![Graph](image)

**Figure 6.** Typical response data from Moore et al. The solid line represents their attempt to represent the observed data trends between actual data points depicted by circles. The fluidic amplifier used in obtaining these data is shown in figure 7 to distinguish it from the laminar devices shown in figure 1.
Figure 7. Typical geometry of fluidic amplifier used by Moore et al.\textsuperscript{19}

The devices all are turbulent and would involve considerably more empiricism to analyse than would a laminar device. In 1973 Healey and Shipp\textsuperscript{20} summarized the available work on proportional amplifiers and presented data of their own. Typical of the results for amplifiers with adjustable vents are those shown in figure 8 where the three individual curves correspond to three operating supply pressures. Healey\textsuperscript{21} comments on this behaviour to the effect that the high frequency behaviour is a jet dynamic effect and he limits his discussion of amplifier operation to frequencies well below this point. He also states that no satisfactory theory exists to quantitatively predict the high frequency gain although a qualitative jet bending argument can be made for their general existence. Up to this point all amplifiers examined were turbulent. However, in 1972, Manion and Mon\textsuperscript{13} published their results on laminar proportional amplifiers (LPA's). These were inherently low frequency devices because of the predominant wide control ports that are of a low pass nature. Kirshner and Katz\textsuperscript{17} describe the jet dynamics...
Figure 8. Turbulent amplifier frequency response from Healey et al.\textsuperscript{20,21}
as a pressure feedback phenomenon; however, they also do not show any numerical examples related specifically to fluidic amplifiers.

It follows, therefore, that consideration must be given to the behavior of an LPA at high frequencies. As such, this effort will consider the fluid dynamics of the flows through the LPA passages and will consider the overall jet coupling with the structure.

Insofar as the development of a communication system is concerned, it is an objective of this thesis to present feasibility arguments for a design and a working demonstration of fluidic communication. To this end, broad band voice transmission and amplification will be considered and, to demonstrate overall utility (although probably not practicality), a duplex system for the simultaneous transmission of frequency modulated data will be built. It is intended that this overall system will demonstrate all the capabilities of LPA's in the high frequency modes.

In keeping with the engineering design/analysis tenor of this work, the analysis will be approached from a control volume, block diagram aspect.

The thesis is divided into 12 sections as follows:

1. INTRODUCTION - An outline of the problem, a literature survey, plan of analytical attack and design methodology.

2. ANALYSIS - The governing equations for an LPA will be developed, tying together past analyses and introducing the additional dynamics. Control volume methods will be stressed. Flow visualization data will be used to demonstrate step response and signal eddy convection. A block diagram approach will then be used to develop the overall transfer function and an equivalent lumped parameter circuit approach will be used to develop the input and loading dynamic response. Comparison will be presented between theory and data.
3. **VOICE SYSTEM DESIGN** - This section will be broken down into the sub-systems outlined in a matrix. Each part will have its own analysis, computation, and hardware section. In addition, there will be a section dealing with human engineering as well as system engineering.

4. **DATA LINK SYSTEM DESIGN** - This section also will be broken down into sub-systems outlined in a matrix as in part 3. Performance data and characteristics will be presented.

5. **SYSTEM IMPLEMENTATION** - This section will deal with the installation of FVCDL systems in military vehicles to include M60 and XM-1 class tanks, F-14, 15, 16 type fighter aircraft and LVTP-type assault craft.

6. **ENVIRONMENTAL SENSITIVITY** - This section will be divided into two major subsections: gaseous property changes due to temperature and altitude and basic environment such as contamination, vibration and EMI/EMP/nuclear effects.

7. **COST AND RELIABILITY** - This section will consider the production costs, producibility, life-cycle costs, maintainability and overall system life. Based on studies conducted on typical fluidic systems, all this information can be extracted.

8. **SUMMARY**

9. **CONCLUSIONS**

10. **RECOMMENDATIONS**

11. **BIBLIOGRAPHY**

12. **APPENDICES** - This will be the repository for the various computer programs used.
2. ANALYSIS

This section will deal with the theoretical considerations involved with the problem. The first section shall deal with the dynamic modeling of the laminar proportional amplifier (LPA). The next two sections will deal with transmission lines and passive components, respectively.

2.1 The Laminar Proportional Amplifier (LPA)

Considerable mention has been made of the LPA in the text so far. Historically, this device has evolved for three distinct reasons. The first is the dynamic range. In the early portion of the seventies the problem of fluidically stabilizing a gun turret in two axes was posed. It was established that in order to meet the specifications of a maximum rate of 100°/s and a threshold of 0.1°/s an overall dynamic range of 1000:1 was required. Since no turbulent device has a signal-to-noise ratio of any better than 500:1\(^3\), it was clear that the specification could not be met by any combination of turbulent devices. Griffin and Gebben\(^2\) disclosed an amplifier that was subsequently used in the laminar regime\(^3\) and was the basis for the evolution of the HDL LPA. Significantly, at about the same time G.E. showed operation of their commercially available amplifier in the laminar regime; however, with significant loss in gain.\(^2\) The ultimate LPA dynamic range is essentially unmeasurable since in the limit only thermal noise due to random molecular motion exists; however, practically flow-borne noise and common-mode ambient disturbances in conjunction with a finite common-mode rejection ratio normally limit the dynamic range of multiple LPA systems to the order of 100,000:1.\(^2\) For most practical applications this is quite sufficient.
Figure 9. Flow visualization photograph of an LPA interaction region. Dark flow is the power jet.
The second reason for laminar flow devices was that the reduction in entrained flow allowed the placement of the laminar jet in such a way as to effectively block off the control channel as shown in figure 9, thus giving rise to a high input impedance.

The third reason for the use of laminar devices is their inherent low power consumption. Normally operating in air only several millimeters of mercury pressure, only a few milliwatts of power are required as opposed to a typical value of almost one watt for turbulent devices operating at 10 kPa.

It is of interest, therefore, to examine the LPA to see what its bandwidth is and to see if the design can be improved.

2.1.1 Flow Through Ducts and Channels

Consider therefore the LPA geometry shown in figure 10.

![Diagram of a laminar proportional amplifier](image)

Figure 10. Schematic of a laminar proportional amplifier.

With the exception of the vent vanes and the close proximity of the control edges, this is the same as the beam deflection amplifier described in the literature.\textsuperscript{25,26,27,17} It is composed of inflow,
outflow, and through flow passages. Thus, the behavior of flow through rectangular cross-section channels forms the basis of this analysis. The steady flow character of these channels is well understood and documented in the literature. The frequency response is also known under certain circumstances. With the requirement of small amplitude deviations around steady flow, it has been found that the pressure drop is made up of steady and reactive components. Iseman goes to particular pains to describe the equivalent circuit topology (network arrangement) of capillaries as various combinations of single resistances, inductances and capacitances, and Kirshner and Katz go into some considerable discussions of rectangular passages. Unfortunately, there has not been any real effort to describe the equivalent circuit of an LPA device other than in the simplest terms. Following the example of Kirshner and Katz where they describe the differential equivalent circuit of a transmission line as an "all" circuit shown in figure 11 this author will attempt to describe a useful equivalent lumped circuit for a short channel such as the input or output of an LPA.

![Figure 11. Infinitesimal transmission line element after Kirshner and Katz.](image)

The equivalent circuit of figure 11 is only valid in the infinitesimal size when one may make the assumption that the voltage across the admittance Y is approximately E. Consider how this analogy was
developed. Zalmanzon\textsuperscript{29} derives the momentum and continuity equations for a control volume in a duct. This derivation is presented here in a slightly altered fashion. Consider a duct and a control volume within that duct as shown in figure 12.

\begin{figure}[h]
\centering
\includegraphics[width=0.7\textwidth]{control_volume.png}
\caption{Control volume in a duct.}
\end{figure}

The forces acting on this differential element must equal the mass times the acceleration of the fluid according to Newton's Second Law. Hence

\[ \rho A - A(p + \frac{\partial p}{\partial x} dx) - 2\tau_w dx(b + h) = \rho A dx \frac{\partial u}{\partial t} \]

or

\[ - \frac{\partial p}{\partial x} - 2\tau_w (b + h) = \rho \frac{\partial u}{\partial t} \]  \hspace{1cm} (1)

Defining the flow \( Q = Au \) then

\[ - \frac{\partial p}{\partial x} = 2\frac{\tau_w (b + h)}{A} + \frac{\rho}{A} \frac{\partial Q}{\partial t} \]  \hspace{1cm} (2)

The continuity equation states that mass is conserved hence

\[ \rho uA - Ap (u + \frac{\partial u}{\partial x} dx) = \frac{dm}{dt} = \frac{d}{dt} \rho A dx \]  \hspace{1cm} (4)
or \[ -\rho \frac{\partial q}{\partial x} = A \frac{\partial p}{\partial t} \] 

(5)

For a gas, the equation of state will be \[ p = \rho R T \] 

(6)

For a liquid \[ dp = \beta \frac{dp}{\rho} \] 

(7)

so that the derivative of density in (5) can be replaced. Consider the gaseous, isothermal case

\[ \frac{\partial p}{\partial t} = \frac{1}{R} \frac{\partial}{g} \frac{\partial p}{\partial t} \] 

(8)

hence equation (5) becomes

\[ -\rho \frac{\partial q}{\partial x} = A \frac{\partial p}{R T} \frac{\partial}{\partial t} = - \frac{p}{R T} \frac{\partial}{\partial x} \] 

where the ambient density, \( p \), is related to the absolute ambient pressure, \( p \), and the absolute temperature, \( T \).

or \[ -\frac{\partial q}{\partial x} = A \frac{\partial p}{\partial t} \] 

(9)

Equations (3) and (9) form a set of differential equations that when \( \tau_w = 0 \) are identical to the wave equation. Taking now the Laplace transform of both equations result in

\[ -\frac{\partial p}{\partial x} = 2\tau_w \frac{(h + b)}{A} \frac{\rho}{} + \frac{p}{A \ s \ Q} \] 

(10)

\[ -\frac{\partial q}{\partial x} = \frac{As}{p} \frac{p}{\rho} \] 

(11)
Now the term with the friction forces is represented by the pressure drop due to friction per unit length of a given duct. The resistance of a duct is defined as

\[ R = \frac{\Delta P}{Q} \]  \hspace{1cm} (12)\]

analogous to the electrical voltage drop divided by current where pressure is analogous to voltage and volume flow to current. The pressure drop per unit length is then

\[ \frac{RQ}{\ell} \]

where \( R \) has been computed for various geometries by various authors. For circular ducts it is determined by the Hagen-Poiseuille equation

\[ R = 8 \mu L/\pi r^4 \]  \hspace{1cm} (13)\]

For rectangular ducts the Cornish solution may be used, but an approximate solution by Kirshner and Katz has been improved with an empirical constant by Manion and Drzewiecki and Drzewiecki so that

\[ R = \frac{12 \mu L}{(hb)^2} [b/h + h/b + k] + \frac{0.475 \rho Q}{(bh)^2} \]  \hspace{1cm} (14)\]

where \( 0.35 \leq k \leq 0.5 \), \( 1 \leq b/h \leq 2 \)

and \( k = 0.5 \) for \( b/h > 2 \)

Notice here that entrance effects have been considered giving an accurate representation for all laminar flows for ducts of length \( \ell \). The pressure per unit length is substituted into equation (10) yielding

\[ -\partial P/\partial x = RQ/\ell + (\rho s/A) Q = (R/\ell + \rho s/A) Q \]  \hspace{1cm} (15)\]

along with equation (11)

\[ -\partial Q/\partial x = (\bar{A}/\bar{P}) s P \]  \hspace{1cm} (16)\]
Equations (15) and (16) form the governing equations for an infinitesimal section of flow through a duct. Now recall the equivalent circuit of a transmission line segment of figure 11. The governing equations are obtained from the input impedance and shunt admittance. The voltage drop $\Delta E$ is

$$\Delta E = -(Z \Delta x) I$$  \hspace{1cm} (17)$$

and the current drop is

$$\Delta I = -(Y \Delta x) (E + \Delta E)$$  \hspace{1cm} (18)$$

where $Z$ and $Y$ are the impedance and admittance per unit length. Neglecting second order terms and taking the limit as $\Delta x \to 0$, these two equations become

$$\frac{\partial E}{\partial x} = -Z I$$  \hspace{1cm} (19)$$

$$\frac{\partial I}{\partial x} = -Y E$$  \hspace{1cm} (20)$$

Differentiating equation (19), with respect to $x$ and substituting in equation (20) yields the wave equation

$$\frac{\partial^2 E}{\partial x^2} = ZYE$$  \hspace{1cm} (21)$$

However, note the form of equations (19) and (20) and notice that they are identical to (15) and (16) when $P$ is analogous to $E$, $I$ to $Q$, and

$$Z = \frac{R}{k} + \frac{B}{A} s$$  \hspace{1cm} (22)$$

and

$$Y = \frac{A}{P} s$$  \hspace{1cm} (23)$$

This then means that an infinitesimal section of a duct may be represented by a resistive, inductive (inertive) and capacitive circuit in an "ell" as in figure 13.
The question now arises, "What equivalent circuit does one use for a single-lump model of a duct?" Most workers in fluidics have opted for the "ell" RLC of figure 13. Iseman, Belsterling, Kirshner, Foster et al. all tacitly assume this form. Blackburn et al. however, assume a different form for hydraulic lines. They arbitrarily chose a "tee" as in figure 14 and do not offer any reasons.

Drezewlocki found that lines used as loads on fluidic elements were best modeled by a "tee" also but with the resistance first as in figure 15.
Figure 15. Lumped parameter representation of a fluidic line after Drzewiecki.\textsuperscript{32}

The basic argument for placing the capacitance (due to fluid compressibility) in the middle was that the average amount of compression is due to an average pressure which is better represented by the node pressure in the middle rather than at either end. Actually, a more satisfying model would be one that is symmetric about the capacitance as in figure 16.

Figure 16. Symmetric equivalent circuit model of a duct.

The disadvantage is, of course, the increased complexity. Consider now the governing equations for the duct as a whole single lump. Equations (15) and (16) become

\[
P_1 - P_2 = (R + \frac{\partial p}{\partial A} s) Q
\]  

(24)
and
\[ Q_1 - Q_2 = \frac{AP}{P} \]  \hspace{1cm} (25)

Now the equivalent circuit of figure 11 no longer holds for the second order. Terms cannot be neglected in writing the flow through the shunt. Consider, however, the 'tee' circuit of figure 15 as a single normal circuit. The pressure drop is

\[ \Delta P = P_0 - P_1 = -RQ_1 - LsQ_0 \]
\[ Q_0 = Q_1 - Q_c = Q_i - \frac{P}{Z_c} \]

where \( Z_c = \frac{1}{C_s} \)

so that
\[ \Delta P = -RQ_1 - Ls\left( Q_1 - \frac{P}{Z_c} \right) \]
\[ \Delta P = -(R + Ls)Q_1 - \omega^2 LCP_c \]

where \( j\omega = s \), \( \omega \) is the circular frequency and \( j = \sqrt{-1} \). When
\[ \frac{P_c \omega^2 L C}{(R + Ls)Q_1} \ll 1 \], then the pressure drop is
\[ -\Delta P = (R + Ls)Q_1 \]  \hspace{1cm} (26)

Similarly the flow drop \( \Delta Q \) is

\[ \Delta Q = Q_0 - Q_1 - Q_c = -CsP_c \]

so that
\[ \Delta Q = \frac{P - P_0}{Ls} - \frac{P - P_c}{R} \text{ and eliminating } P_c \]
\[ \Delta Q = -\left( \frac{Z_c \Delta Q + P_0}{Ls} - \frac{P_1 + Z_c \Delta Q}{R} \right) \]

or
\[ -\Delta Q = P_0/(Ls+1/Cs+L/CR) + P_1/(R+R/(LCs^2)+1/Cs) \]
when \( R \) is sufficiently small this reduces to

\[ Q_1 - Q_0 = C s P_1 \]  

(27)

Now we compare equations (26) and (27) to (24) and (25) and find that they are identical when the inductance (called by Blackburn et al. and others in fluidics inertance, due to inertia forces),

\[ L \equiv \rho \ell / A \]  

(28)

and the capacitance is

\[ C \equiv \frac{A \ell}{P} \]  

(29)

The resistance \( R \) is already understood.

The restrictions on frequency and resistance are that they be small. The frequency limitations can be estimated by requiring that

\[ \omega^2 LC = 0.1 \]

The following typical values

\[ L = \rho \ell / A \text{ and } C = \kappa A / P \]

\( \rho = 1.2059 \text{ kg/m}^3 \) (density of air at STP)

\( \kappa = 0.005 \text{ m} \)

\( P = 1.01 \times 10^5 \text{ Pa} \) (atmospheric pressure)

yield

\[ \omega = \frac{0.1}{\sqrt{LC}} = \frac{0.1}{\sqrt{\rho \ell^2 / P}} = 5800 \text{ rad/s} \]

or \( f = 924 \text{ Hz} \)

Therefore, the equivalent circuit of figure 15 will be valid for frequencies roughly below 1 kHz for the dimensions given as typical of moderate size LPA. This is not to say that the LPA will not
operate at higher frequencies, but that accurate modelling beyond 1 kHz may require a more complex equivalent circuit.

The equivalent circuit of figure 15 is therefore chosen to describe the input and output channels of the LPA shown in figure 10.

The supply nozzle is described merely as a nozzle since no dynamics are associated with it. It merely supplies a constant flow of fluid. This is true as long as the dc level at the nozzle exit is constant in time. This requires the assumption of push-pull signals at either side of the jet or essentially infinite common mode rejection. The nozzle is treated as an ideal orifice with a discharge coefficient. Drzewiecki\textsuperscript{33,34} has solved the general problem of flow through a planar nozzle by solution of the modified Karman-Pohlhausen integral equation that describes the displacement thickness boundary layer growth. He has found that for most smoothly converging nozzles there exists a single function that describes the discharge coefficient $c_{d}$. This implicit function is given in equation (30). Figure 17 is a plot of this equation taken from reference (33) showing numerous experimental data verifying its universatility.

$$c_{d} N_{R}' = 2.667 \left( e^{6.6c_{d}^2} - 1 \right)$$

The flow through a space defined by an edge and a jet barrier as is seen in figure 9 and through which the streamlines in that photograph pass, is described as that through an ideal orifice of unity discharge coefficient if the flow is in the direction of the jet stream. If, on the other hand, the flow is from the vents to the controls, the discharge coefficient is chosen to be, quite arbitrarily, one half. The present analysis does not consider the latter case but to justify the choice of unity $c_{d}$ one can look at figure 18 where an artist's rendition of the velocity profile demonstrates the argument that reduction in flow due to wall shear
Figure 17. Comparison of theory and data for discharge coefficient for nozzles of widely varying planview and low Reynolds number.
is offset by flow increase by viscous drag in the vicinity of the jet.

![Flow past an edge by a jet barrier](image)

Figure 18. Flow past an edge by a jet barrier.

While no actual solution of the flow field or comparison with velocity data has been made, this assumption appears to be valid in that it gives good agreement with actually measured LPA input resistances. The volume of the orifice is exceedingly small, hence, there is no capacitance but there are inertia effects requiring an inertance (inductance) term as previously derived. Rschevkin describes in detail the inductive properties of orifices and in table 6 pp 238-244 lists the common equivalent circuits for acoustic components. The inertance, however, is defined in equation 28.

One comment has to be made. The channels of an LPA are hardly ever of constant cross-section viz. figure 10. However, typically the flow rate is very small, hence, the Reynolds numbers are small especially in the inputs. Here the flows are of the order of 5% of the jet flow through areas 3-5 times the nozzle area. For typical nozzle Reynolds numbers of 1000 this means the channel Reynolds numbers are about 10. Viscous effects predominate over the acceleration terms and the width averaged over the length may be used with no ill effects.
Lastly, the flow of the jet from the nozzle between parallel plates to the splitter is observed to be a steady dc axial flow since there is no axial forcing. There are viscous losses as described by Manion and Drzewiecki\textsuperscript{35} and by Drzewiecki\textsuperscript{35}. There is a lateral time dependent motion but for the time being, this is assumed, as others have done, not to be impeded by either inertial or viscous forces. The major frequency dependent contribution of the jet stream is the time delay which occurs at one half the jet average velocity. A signal at the nozzle exit forms a signal eddy that has a centroid that travels like a wheel at about one-half the outer velocity which is typically the average jet velocity. This is depicted pictorially in figure 19.

![Diagram of jet flow](image)

**Figure 19.** Signal convection along a jet.

This then completes the review and analysis of the through flows to be encountered in analysing an LPA.
2.1.2. Amplifier Input Analysis

Now that the basic flow parameters have been identified, consider the control-volume modeling for the input impedance dynamics of an LPA. A pressure is imposed on an input causing flow to enter the LPA and deflect the jet. A control volume is drawn in the vicinity of the jet edge in order to determine the pressure therein and, hence, the amount of jet deflection. Figure 20 shows such a control volume.

![Control volume for jet edge pressure.](image)

The terms in the figure are defined below.

- $Q_c$: control flow
- $Q_v$: flow to vent
- $Q_r$: flow returned to control volume due to spillage
- $Q_e$: entrained flow
- $Q_s$: flow through deflected space
- $Q_s$: supply jet flow
- $b_d$: control width
- $b_s$: supply width
\( \delta \) - deflected space width at downstream control edge

\( P_C \) - input or control pressure

\( P_s \) - supply pressure

\( P_J \) - jet edge pressure

\( P_V \) - pressure in vent downstream of control

1,2 - side 1 or side 2, respectively

Following the established procedure for determining the input impedance (see for example Manion and Drzewiecki\(^4\)) one now writes the continuity equation for the control volume.

\[
Q_{cl} - Q_e - Q_{v1} - Q_{\delta 1} + Q_{r1} = \frac{d \text{(Volume)}}{dt} \quad (31)
\]

Now using the chain rule

\[
\frac{d \text{(Volume)}}{dt} = \frac{d \text{(Volume)}}{dp} \frac{dp}{dt} \quad (32)
\]

The change in volume with pressure is called the compliance and is a capacitive term. This term has been modelled in several ways. Kirshner and Katz examine it from both a jet barrier approach and a jet dynamic approach, the latter reducing to the jet barrier solution at frequencies encountered in fluidics. The jet barrier capacitance is the change of volume due to jet deflection relative to the change in pressure required to cause the deflection. Consider a fluid slug issuing from a nozzle as in Figure 21 at the average jet exit velocity \( \bar{u} \).

![Figure 21. Slug of fluid under the action of a uniform pressure difference.](image-url)
Newton's Second Law requires that the lateral displacement of this slug be such that the sum of the lateral forces equal that mass times the acceleration

\[ \Sigma F_y = m \ddot{y} = P_1 dx h - P_2 dx h \]

or

\[ \ddot{y} = \frac{(P_1 - P_2) dx h}{(odx h b_s)} \]

so that

\[ \ddot{y} = \frac{(P_1 - P_2)}{\rho b_s} \]  \hspace{1cm} (33)

with zero initial conditions. Under a constant pressure difference the displacement as a function of time is then

\[ y(t) = \frac{(P_1 - P_2) t^2}{(2b_s \rho)} \]

The displacement as a function of downstream distance is determined by the time it takes to travel the distance \( x \), \( t_x \),

\[ t_x = \frac{x}{\bar{u}} \]

where \( \bar{u} \) is the \( x \)-velocity at which the particle is traveling assuming small deflections. Hence

\[ y(x) = \frac{(P_1 - P_2) x^2}{(2b_s \rho \bar{u}^2)} \]  \hspace{1cm} (34)

Now notice that this is in effect an interaction of the pressure with the jet momentum flux \( \rho \bar{u}^2 \). This may be written in terms of the jet supply pressure in that

\[ \rho \bar{u}^2 = 2b_s P_s \]  \hspace{1cm} (35)
where $c_0$ is the momentum flux discharge coefficient or the ratio of actual flux to ideal flux. This term has been developed for nozzles by Manion and Drzewiecki and related to the discharge coefficient $c_d$ where

$$c_0 = 1.32 c_d^2$$

When equation (35) is substituted into (34), one gets

$$y(x) = \frac{p_1 - p_2}{4b_s c_0^2} x^2$$

(36)

The volume per unit depth swept out by this deflection over the control width can be calculated from the integral of equation (36):

$$\Delta (\text{Vol}) = h \int_0^b y(x) \, dx = \frac{b^3 h (p_1 - p_2)}{12 c_0^2 p_s}$$

(37)

One may therefore define the jet capacitance as

$$\frac{\Delta (\text{Vol})}{\Delta P} = C_j = \frac{b^3 h}{12c_0^2 p_s}$$

(38)

Now if one considers only push-pull signals so that the increase in pressure on one side is equal to the decrease on the other, then $\Delta P_j = 0.5 \Delta P$ and equation (38) for the capacitance may be written for the change in pressure on one side as

$$C_j \equiv \frac{\Delta (\text{Vol})}{\Delta P_j} = b_c^3 h/6 c_0 p_s$$

(39)
This forms the basis for a complex impedance \( Z_j = 1/C_j \) of the jet. In a more detailed jet impedance analysis, Kirshner and Katz have found that this impedance has a dissipative component due to particles being swept out of the control volume. This term is \( R_j/R_s = 6 c_d^2/B_c^2 \), so that \( Z_j = R_j + 1/C_j \). Now take the Laplace transform of the continuity equation (31)

\[
Q_{ci}(s) - Q_e(s) - Q_v(s) - Q_{\delta 1}(s) + Q_{r1}(s) = \frac{P_{j1}(s)}{Z_j}
\]

and

\[
Q_{cl} = (P_{cl} - P_{j1})/Z_{cl}
\]

\[
Q_v = (P_{j1} - P_v)/Z_v
\]

\[
Q_{\delta 1} = (P_{j1} - P_v)/Z_{\delta 1}
\]

so that

\[
\frac{P_{cl} - P_{j1}}{Z_{cl}} - \frac{P_{j1} - P_v}{Z_v} - \frac{P_{j1} - P_v}{Z_{\delta 1}} - (Q_e - Q_{r1}) = P_{j1}/Z_j
\]

(42)

where the channel impedance is characterized by the equivalent circuits as before in 2.1.1. The resistive part of the impedance to vent \( Z_v \) has been shown to be a constant. The inductance is due to the slug inertia. The impedance \( Z_{\delta 1} \) is merely the resistance of an orifice of width \( \delta \) and an inertia of a slug of the same width, hence, the d.c. flow is defined by

\[
Q_{\delta 1} = \delta h \sqrt{2(P_{j1} - P_v)/\rho}
\]

(43)

so that the resistance is

\[
R_{\delta 1} = \frac{P_{j1} - P_v}{Q_{\delta 1}} = \frac{\sqrt{\rho(P_{j1} - P_v)/2}}{\delta h}
\]

(44)
and the complex impedance is

\[ Z_{\delta 1} = R_{\delta 1} + \frac{x_{\delta 1}}{\delta_{1} h} \rho s \]  \hspace{1cm} (45)

where from equation (28) the inductance in its general form \( \rho L/A \) is here \( \rho x_{\delta 1}/\delta h \). The length is \( x_{\delta 1} \). It is somewhat difficult to assign a value to this dimension since the gap, \( \delta_{1} \), is bounded on one side by a curved wall of small radius. I have chosen twice this radius as \( x_{\delta 1} \).

Now let the jet impedance be as before

\[ Z_{j} = \frac{1}{C_{j} s^2} + R_{j} \]  \hspace{1cm} (46)

so that equation (42) becomes

\[ \frac{P_{c1}}{Z_{c}} - \frac{P_{1}}{Z_{c}} = P_{j1} \left( \frac{1}{Z_{c}} + \frac{1}{Z_{\delta 1}} \right) = Q_{e} - Q_{r1} \]  \hspace{1cm} (47)

Now one notes that we are looking for an expression for the small signal input impedance while the jet is deflected through an additional deflection, \( \delta \),

\[ Z_{1} = \frac{dP}{dQ} \]  \hspace{1cm} which by the chain rule is

\[ Z_{1} = \frac{dP}{d\delta} \frac{d\delta}{dQ} \]  \hspace{1cm} (48)

Therefore, differentiate equation (47) with respect to \( \delta \), a small deflection of the jet relative to the deflected position \( \delta_{1} \). Equation (47) thus becomes, when \( P_{v} \) is assumed to be zero,
\[
\left( \frac{\partial P}{\partial \delta} - \frac{\partial P_D}{\partial \delta} \right) / Z_c - \left( \frac{1}{Z_v} + \frac{1}{Z} + \frac{1}{Z_j} \right) \frac{\partial P_D}{\partial \delta}
\]

- \[ P_{j1} \left[ h\left( \frac{1}{\left( P_{j1}/2 \right)^{1/2} + \rho x_{\delta} s} \right) \right] - \delta \left( \frac{0.5\left( P_{j1}/2 \right)^{1/2} + x_{\delta} \rho s}{\left( P_{j1}/2 \right)^{1/2} + x_{\delta} \rho s} \right) \]/

\[
\left( \frac{\partial P_{j1}}{\partial \delta} \right) = \delta (Q_e - Q_r) / \partial \delta \quad (48)
\]

Now recall the jet deflection from equation (36) and note the assumption of push-pull pressure where \( P_{j1} = 0.5 \) \( P_j \) then with \( x = b_c \) and \( y(x) = \delta \)

\[
\frac{\partial P_{j1}}{\partial \delta} = 2 c_b b P_{s} / b_c^2 \quad (49)
\]

Substituting equation (49) into (48) and solving for \( \frac{\partial P_{c1}}{\partial \delta} \) for the symmetrical case, \( \delta \) = 0, yields

\[
\frac{\partial P_{c1}}{\partial \delta} = \left( 2 c_b b P_{s} / b_c^2 \right) \left( 1 + Z_c \left( 1/Z_v + 1/Z_j \right) \right) +

Z_c P_{j1} h / \left( \left( P_{j1}/2 \right)^{1/2} + \rho x_{\delta} s \right) +

Z_c \delta (Q_e - Q_r) / \partial \delta \quad (50)
\]

Drzewiecki has determined the term

\[
\left( 2 b_s / Q_s \right) \delta (Q_e - Q_r) / \partial \delta
\]

as the net entrainment coefficient \( a_1 \), which is a constant for a given geometry and flow condition. This term is computed by the program given in Appendix 1. No reactive component is ascribed to this term. Experimental evidence of this is shown later. If now equation (50) is normalized by \( P_{s} \) and \( b_s \) and \( R = P / Q_s \), so that capitalized dimensions are normalized, e.g. \( B_{c1} = b_c / b_s \), \( X = x / b_s \) etc., then

\[
\frac{\partial (P_{c1}/P_s)}{\partial (\delta/b_s)} = \left( 2 c_b b^2 \right) \left( 1 + Z_c \left( 1/Z_v + 1/Z_j \right) \right) +

\left( Z_c Q_s / P_s \right) \left( h b_s P_{j1} / \left( \left( P_{j1}/2 \right)^{1/2} + \rho x_{\delta} s \right) Q_s + a_1 / 2 \right)
\]
and

\[ \theta\left(\frac{P_{cl}}{P_s}\right) / \theta(\delta/b) _s = (2c_\delta / B_c^2)(1 + (Z_c / R_s)(R_s / Z_c + R_s / Z_j)) + \]

\[ (Z_c / R_s)((P_j / P_s)/(2c_d((P_j / P_s)^{1/2}/2 + j\omega X_c c_d) + a_1 / 2)) \]

(51)

where \( \Omega \) - normalized radian frequency = \( \omega b_s / c_d (\frac{s}{\rho})^{1/2} \) and \( c_d \) is defined by equation (30). Now define a normalized pseudo-impedance

\[ Z_k = (c_d \sqrt{\frac{(P_j - P_j) / P_s}{2}} + 2c_d^2 X_c / \Omega) / (P_j / P_s) \]

(52)

and note that it is of the form

\[ Z_k = R_k + jL_k \Omega \]

(53)

where \( R_k \) and \( L_k \) are the resistance and inductance, respectively. Similarly define a pseudo-resistance

\[ R_d / R_s = 2 / a_1 \]

(54)

Equation (51) becomes

\[ \frac{\theta(P_{cl}/P_s)}{\theta(\delta/b) _s} = \frac{2c_\delta}{B_c^2 \left[ 1 + \frac{Z_s}{R_s} \left( \frac{R_s}{Z_c + Z_j} \right) + \frac{Z_c}{R_s} \left[ \frac{R_s}{Z_j} + \frac{R_s}{Z_k} + \frac{R_s}{R_d} \right] \right] \}

(55)

Notice that normalization of any impedance by \( R_s = P_s / q_s \) results in a normalized time or frequency term as shown below.

\[ Z/R_s = R/R_s + j\omega L/R_s = R/R_s + j\omega x / (b h R_s) \]
where \( x \) and \( b \) are the length and breadth of some channel.

Now

\[
R_s = \frac{P_s}{Q_s} = \frac{P_s}{(c_d b h \sqrt{2p_s/p})} = \frac{\sqrt{p_s/2}}{(c_d b h)}
\]

Therefore

\[
\frac{Z}{R_s} = \frac{1}{R_s} + \frac{jwxc_d b_s h}{(b h \sqrt{p_s/2})}
\]

The reactive term alone is

\[
jwxc_d b_s / (b \sqrt{p_s/2}) = jw \sqrt{x_c d / b} \sqrt{p_s/2}
\]

where \( B = b/b_s \)

but \( \tau = b_s / (c_d (2p_s/p)^{1/2}) \) is the transport time for one nozzle width

so that \( \omega_t \) is the radian frequency per transport time, or \( \Omega \). The reactive term thus becomes

\[
\frac{jw \sqrt{pxc_d}}{b \sqrt{p_s/2}} \frac{b c_d \sqrt{2p_s/p}}{b_c_d \sqrt{2p_s/p}} = j\Omega 2Xc_d / B
\]

so that inertance is \( 2 \times c_d^2 / B \) in the normalized frequency domain.

Now recall that one must obtain \( \partial Q_c / \partial \delta \) to complete the derivation

of the input impedance. Consider, therefore, again equation (40) in

its Laplace transformed state and differentiate it with respect to the

deflection.

\[
Q_{c1} - Q_v - Q_\delta + Q_r1 - Q_e = P_j1 / Z_j
\]

\[
\frac{\partial Q_{c1}}{\partial \delta} - \frac{\partial Q_v}{\partial \delta} - \frac{\partial Q_\delta}{\partial \delta} + \frac{\partial Q_r1}{\partial \delta} = \frac{1}{Z_j} \frac{\partial P_j1}{\partial \delta}
\]
and solving for \( \frac{\partial Q_{c1}}{\partial \delta} \) and substituting for \( Q_v \) and \( Q_6 \) yields

\[
\frac{\partial Q_{c1}}{\partial \delta} = \frac{\partial P_{j1}}{\partial \delta} + \frac{\partial (\frac{P_{j1} - P_v}{Z_6})}{\partial \delta} + \frac{1}{Z_v} \frac{\partial P_{j1}}{\partial \delta} + \frac{\partial (Q_e - Q_{c1})}{\partial \delta}
\]

and remembering that \( \frac{\partial P_{j1}}{\partial \delta} \) is defined by the jet deflection equation (49), performing the differentiation on the deflected impedance of equation (45) as before and normalizing results in

\[
\frac{\partial (Q_{c1}/Q_s)}{\partial (\delta/b_s)} = \frac{2 c_\theta}{Z_v} \left( \frac{R_s + R_j}{Z_j} + \frac{R_j + R_s}{R_d + Z_k} \right)
\]

When this result is divided into equation (55), the complex input deflection impedance is obtained

\[
\frac{\partial (P_{c1}/P_s)}{\partial (Q_{c1}/Q_s)} = \frac{Z_c}{R_s} \left( R_s \frac{R_s + \frac{B^2}{2} R_j}{Z_v} + \frac{1}{Z_j} \right) + \frac{1}{Z_c} \frac{R_s}{Z_6} \left( \frac{R_s + \frac{B^2}{2} R_j}{Z_k} \right)
\]

Now let all normalized terms appear without their normalizing parameter. In other words, all quantities of pressure, flow, impedance and dimensions appear now as normalized quantities (e.g. \( b/b_s \rightarrow B \), \( P/P_s \rightarrow P \), \( Q/Q_s \rightarrow Q/R_s \rightarrow Z \), etc.). In addition, define two new pseudo-impedances

\[
R_D = \frac{2 c_\theta}{B_c} R_d \text{ and } Z_K = \frac{2 c_\theta}{B_c} Z_k
\]

and remember that symmetry has been assumed where \( P_{c1} = \Delta P_c/2 \), etc., then equation (59) becomes
When the control channel is assumed to have a capacitance due to compressibility in a shunt to ground as previously discussed, equation (61) becomes

\[ Z_1 = R_c + 1/( \frac{1}{Z_A + Z_L} + \frac{1}{Z_p} ) \]  

(61a)

where \( 1/Z_A = 1/Z_v + 1/Z_j + 1/Z_K + 1/R_D \), \( Z_L = L_c \) and \( Z_p = 1/C_c \).

Equation (61a) is the input impedance of an LPA or the impedance seen by a differential input signal. Consider now the equivalent circuit between the input, the jet edge and ground (the vent pressure) that this circuit describes. It is a series combination of a channel impedance with a lumped parallel combination of the vent, deflection, bias effect \((\Delta P_j)\) and jet compliance impedances. This is shown in figure 22. Note that the node pressure is the jet edge pressure since the pressure drop across the channel is defined as the drop from the input to the jet edge pressure.

---

**Figure 22. Equivalent circuit of LPA input impedance.**
The normalized quantities are defined by the following equations:

\[ R_c = \frac{24X_c c_d (\sigma/\overline{B}_c + \overline{B}_c/\sigma + K) / (\overline{B}_c^2 \cdot N_R)}{+ 0.95 c_d^2 Q_c / B_{cmin}^2} \] (62a)

\[ L_c = 2 c_d^2 \frac{X_c}{\overline{B}_c} \] (62b)

\[ C_c = \overline{B}_c X_c \left( \frac{P_s}{P_\infty} \right) (P_\infty \text{ - absolute ambient pressure}) \] (62c)

where \( P_s / P_\infty = \left( \frac{N_R}{120} \right)^2 \left( 1/\sigma^2 \right) \left( 1/\overline{B}_s^2 \right) 760 \) with \( b_s \)

in mm.

\[ R_D = \frac{4 c_\beta}{(a_1 B_c^2)} \] (62d)

\[ C_{j1} = B_c^3 / 6 c_\theta \] (62e)

\[ R_K = 2 c_\delta c_d / (B_c^2 \sqrt{\left( \frac{P_{j1} - P_v}{P_c} \right)}) \] (62f)

\[ L_K = 4 c_\delta c_d^2 X_\delta / (B_c^2 (P_{j1} - P_v)) \] (62g)

\[ L_V = 2 c_d^2 \frac{X_\delta}{B_j} \] (62h)

\[ R_j = 6 c_d^2 / B_c^2 \] (62i)

where \( \overline{B}_c \) - average channel width
\( \sigma \) - aspect ratio
\( K \) - empirical constant 0.35 < \( K \) < 0.5
\( B_{cmin} \) - minimum channel width

\( X_c \) - channel length
\( X_\delta \) - length of jet-edge space
\( B_j \) - width of jet-edge space = \( (B_t - 1)/2 \)
\( B_t \) - distance between downstream control edges.
$B_c$ - control width
$N_{Re} - Reynolds$ number $= (b_s/v) \sqrt{2P_s/\rho}$

are all constant for a given LPA and operating point.

The vent resistance, $R_v$, has been determined as a function of average bias pressure by Manion and Drzewiecki. The value must be calculated for each geometry and is in general proportional to the jet edge gap size but depends also on how far downstream from the nozzle it is because it depends on the jet spreading. Hence, it is also dependent on control width. A typical value for $R_v = 3.0$ when $B_c = 1$, $B_t = 1.25$.

It is interesting to compare this model, that has been essentially derived from first principles, to those used by others for the inputs of fluidic amplifiers. Figure 23 shows three such circuits.

(a) Amplifier input due to Belsterling

(b) LPA input due to Manion and Mon

(c) LPA input due to Kirschner and Katz

Figure 23. Various equivalent circuits used for amplifier inputs.
Belsterling\textsuperscript{27} considers the input as a simple second-order R-L-C as in 23a. Manion and Mon\textsuperscript{3} are much closer, as in figure 23b, to the complete equations in that they consider a second inertive term. It is not clear, however, how they derived their added inductance. In Kirshner's\textsuperscript{17} work, see figure 23(c), the jet edge inductance is neglected; however, a vent impedance is assumed which gives rise to additional terms. Kirshner also derives an energy loss term in the form of a resistance in series with the jet compliance and explains its function as representing the energy lost from the control volume due to particles being swept out by the jet. In each case the capacitance of the control channel is neglected. This is not always a valid assumption. Equations (62c) and (62e) define the two capacitances in the model. Consider an LPA of \( \sigma = 0.25, \ X_c = 10, \ B = 2.75, \ B_c = 1.50, \ P_s = 64 \text{ mmHg}, \ P_a = 760 \text{ mmHg} \) and \( b_s = 0.5 \text{ mm} \). This yields capacitances of

\[
C_c = 2.3 \quad C_j = 0.879
\]

which indicates that for low aspect ratio, fairly high pressure, LPA operation, the channel capacitance is predominant and may not be neglected.

The assumptions used in the foregoing analysis should be recapitulated and the inferred ones stated for clarity.
1. Laminar flow, \((c_d N_d R/(1 + 1/\sigma)^2 \leq 180)\)
2. Small amplitude signals (so that derivatives are good approximations).
3. Small compressibility effects - fluid is essentially incompressible thus reducing the problem to one of acoustics.
4. Dimensions small compared to wavelengths - implies constant pressures in control volumes and low frequencies.
5. Two-dimensional laminar jet net entrainment characteristics but not necessarily velocity distributions.
6. The pressure downstream of the control jet edge region is constant and ambient.
7. The mean pressure level at the jet edge \((P_{J1} + P_{J2})/2 = \text{constant-push-pull signals.}\)
8. Geometrical symmetry about the LPA centerline.

The last assumption allows the solution of the governing equations around the point of zero jet deflection. For static cases, the problem of non-symmetry is examined by Drzewiecki and Manion. In general, it was found that offsets produce deterioration of gain.

Low frequency increases in gain could possibly be due to a frequency dependence of the mean pressure level. Perhaps if \(P_j\) were a function of frequency, it would explain the low frequency "hump" in the frequency response as shown for example by Healey in figure 8. The mean value of the jet edge pressure is predominantly a function of the jet entrainment characteristics, hence, if entrainment were to dramatically increase with frequency, then the input impedance could resonate as can be seen from the \(R_k\) term which, in itself, depends on \(P_j\). Experiments by Roffman and Toda and Hoglund and Simcox, the results of which are shown in figures 24 and 25, indicate that spreading significantly affects entrainment. Sato indicates also that sound may affect laminar jet spreading. Shields and Karamcheti present instantaneous
Power jet pressure is 0.051 cm H₂O, Reynolds number is 307, and excitation frequency applied through polyflow tube is 180 Hz.

Figure 24. Jet spreading data due to Roffman and Toda.¹⁴
Figure 25. Change in turbulent jet spreading with sound amplitude after Hoglund and Simcox. 

\[ N_R = 1550 \]
\[ x/b_s = 12 \]
\[ f = 2000 \text{ Hz} \]
velocity profile data on a laminar jet in an edgetone oscillation as shown in figure 26. There is considerable skewing and distortion of the profiles. Kirshner \(^1\) speculates on this and offers the explanation that the slower velocity particles at the jet edges are in the force field longer than the peak velocity particles, hence, they get out of phase. While this probably leads to phase distortion, it does not appear to affect the overall entrainment of the jet although there may be some apparent periodicity of entrainment. This appears as a broadening of the jet on one side and a narrowing on the other. There is also some periodic increase in the velocity gradients so that mixing, if it were a factor could increase. Since the flow is laminar, this does not seem to be the case. The jet, however, except for some skewing due to the phase difference of various slower travelling particles, merely deflects as is assumed in the quasi-steady assumption. For frequencies below a value determined Stiffler and Shearer, \(^3\) turbulent jets show no added spreading at all when under the influence of sinusoidal pressures, thus verifying the quasi-steady assumption. \(^3\) The fact that laminar entrainment is not affected is dramatically proven by experiments that were carried out under the aegis of this program. If the entrainment changes, then the mean pressure will change. This mean pressure was measured in three different aspect ratio LPA's as a function of frequency by a static tap mounted just at the end of the control passage as shown in figure 27. The frequency was varied to 3 kHz (essentially the whole bandpass of an LPA of nozzle width \(b_s = 0.5\) mm). The results are shown in figure 28. As can be seen, there is no deviation from constancy (except for some experimental noise). This is an important verification of one of the simplifying assumptions in the model. From this assumption one also can make the statement that the change of entrainment with deflection is negligible, hence, the only parameter that may be frequency dependent is the returned flow. The assumption here, however, is that there is no significant dynamic contribution of this term.
Figure 26. Instantaneous mean jet profiles due to Shields and Karamcheti 37.
Figure 27. Line drawing of the standard HDL LPA 3.1.1.8 showing the location of a static tap used to measure the mean jet edge pressure.
Figure 28. Experimental data for the mean jet edge pressure, $\bar{P}_j$, of an LPA.
This then concludes the analysis of the input of an LPA. What now remains is to tie this to the complete device.

2.1.3 Modeling of the Complete LPA

Early dynamic tests on high aspect ratio LPA's indicated a region of multiple resonances. In fact, as the Reynolds number was increased to just below transition, sustained oscillations would occur attributable only to some form of internal feedback. This coupled with the insight gained from discussions with J. M. Kirshner, formerly of HDL, and physical observations on a large scale water tunnel model of an LPA led to the conclusion that jet dynamic effects and internal acoustic feedback caused the resonances. In fact, if one considers an oscillating jet in an LPA geometry, it seems clear that the spillage of flow to one side or the other must cause a pressure to develop at the sides of the jet. If this pressure feeds back to the sensitive area of the jet (the controls) and it arrives in phase or 360° out of phase with the input, it will augment deflection and give rise to a substantially greater output due to positive feedback. Figure 29 is a series of photographs taken during a single cycle of an LPA in oscillation. Figure 29(a) shows the jet swinging to the left. Figure 29(b) shows the same jet starting to swing to the right at the control region but still travelling right near the outputs. In figure 29(c), the jet is swinging to the right over its entire length. What should be observed is the modulation of the flow through the upper vents. Consider, therefore, the verbal description of the phenomenon. A signal is put in the control, is attenuated and then deflects the jet. The jet deflection is delayed by the jet transport time. The deflection reaches the outputs where some jet flow is spilled to the vents and some is delivered to the outputs and hence the load. The flow into the vents causes a pressure to
Figure 29 a. Flow visualization photograph of an oscillating jet in an LPA.

(Jet is swinging from right to left.)
Figure 29 b. Flow visualization photograph of an oscillating jet in an LPA.

(Jet is swinging from left to right at the nozzle exit but just at the end of right to left travel by the splitter.)
Figure 29 c. Flow visualization photograph of an oscillating jet in an LPA.

(Jet is swinging from left to right.)
develop that is radiated out acoustically. This signal reaches the control region and acts to help or hinder jet deflection. A block diagram of this is shown in figure 30.

![Block Diagram](image)

**Figure 30.** Conceptual block diagram for LPA dynamic response.

It is apparent that there may be multiple feedback paths if flow is spilled at more than one location. In the typical LPA, there are vent vanes (see for example in figure 29) where flow interaction may take place as, perhaps in figure 29b. Figure 31 illustrates this possibility.

Additional dynamic effects have been observed when a laminar jet is subjected to a step input. Rather than having a single sided pulse travel downstream, a whiplash effect is seen such as that shown in the photograph of figure 32. The physical explanation of this apparently anomalous behaviour is that the step control signal causes a pulse of high velocity flow (due to the tiny orifice between the jet and control edge) to form along side of the jet as shown in figure 33. This causes an initial or leading eddy to form and preceed the eddy that is
Figure 31. Oscillating Jet showing edge feedback interactions.
Figure 32. Flow visualization photographs of the step response of an HDL standard LPA, illustrating a twin eddy, whiplash, effect.
formed by the sudden acceleration of stagnant flow on the opposite side of the jet. Two eddies now must be convected to the outputs. The time required for this is longer than it would be if only one eddy were being convected. The leading eddy also causes the jet to cross over the centerline and as a result, causes a negative differential pressure to occur prior to the establishment of the positive final steady state output pressure. This can be reasonably explained by the fact that the leading eddy grows in size as it is convected downstream. The velocity component of the leading edge of that eddy is in the negative lateral direction. This also can be seen in the sketch of figure 33. Clearly then, the step response is nonlinear and does not fall into the category of small signals as assumed in the analysis section.

It should be mentioned here that the presence of these two signal eddies is a strong argument for more time delay and hence added phase shift over that expected from assuming two transport times for a single eddy. Conceivably, four transport times could be argued as the time for signal propagation. Certainly this would hold true for large signals as observed in the present experiment and in experiments reported by Drzewiecki and Manion\textsuperscript{35} when step changes in angular rates were applied to laminar jet angular rate sensors. Initial attempts at placing LPA resonances at low frequency involved using four transport time delay. Subsequent identification of the internal processes (feedback, etc.) allow the use of two transport times when considering small signals.

The acoustic feedback signal is attenuated by the viscous impedance of the bounding planes of the amplifier. Beranek\textsuperscript{39} gives a relationship for the attenuation of nearly square passages that is proportional to the square root of the frequency and inversely proportional to a characteristic dimension, hence

\[
20 \log \left( \frac{P(x)}{P_0} \right) = 0.00664 \sqrt{\frac{f}{h}} \quad \text{x(db)}
\]  

(63)
or

\[
\frac{P}{P_{xsp}} = 10 \left( -2.767 \times 10^{-5} \left[ c_d \nu (v g_R s) / b \right]^{1/2} \sqrt{F} x_{sp} / \sigma^{3/2} \right)
\]  

(63a)

is assumed to be the attenuation of a square cross-section distance of length \( x_{sp} \) alongside the jet from the splitter back to the control. This agrees with experimental evidence that shows that as the aspect ratio or depth diminishes, the resonances disappear. Resonances also vanish, however, as the Reynolds number decreases.

As Reynolds number decreases the jet spreads out and reduces the space between itself and the vent vanes as shown in the following figure, figure 34. The fed back signal is thus further attenuated. Experimental evidence in the form of the frequency response of amplifiers with and without vent vanes illustrates this point quite dramatically as shown in figure 35. The response without the vanes is considerably more peaked indicating that feedback is enhancing gain at resonant points.

The model of an LPA thus is taken to follow the block diagram of figure 30. In figure 36 the complete model is shown in block diagram form. This feedback network may be reduced to the mere compact form illustrated in figure 37. This transfer function and the expression for the impedances have been programmed in FORTRAN IV for an IBM 370/168 computer. The listing is given in Appendix 1. A typical computer plot for a self-staged case (LPA driven by and loaded into an identical LPA) is shown in figure 38. Compare this typical plot to a typically obtained experiment plot of the frequency response of a high aspect ratio LPA as is shown in figure 39 (see also figure 35). Typical of the response is a very broad band hump centered at a normalized frequency of 0.01 that is predicted by the current model. This location and amplitude is found to be a function of the inductance of the
Figure 34. Jet spreading at low Reynolds number showing interaction with vent vanes.
Figure 35. Experimental comparison of the effects of vent vanes on the acoustic feedback characteristics of LPA's.
Figure 36. Full block diagram model of an LPA, including acoustic feedback.
Figure 37. The LPA transfer function.
Figure 38. Computer plot of the frequency response of an LPA -- analytical.
Figure 39. Experimental BAFCO gain plot of frequency response of the standard HDL LPA. High aspect ratio case.
downstream vents. When inductance is low, the response is flat as shown in figures 40 and 41. Figure 40 shows the self-staged response, and figure 41 shows the blocked \(Z_L = \infty\) response when the inductance is that for a channel one nozzle width long and four nozzle widths wide as opposed to the figure 38 response where the length was four nozzle widths. Notice that the locations of the second peak in figures 38 and 40, due to feedback from the splitter, are unaffected by the vent inductance. It is difficult to judge the values of inductance for all possible cases and configurations of manifolds and cover plates. For example, if the device is not cross-coupled and an apparently wide opening is provided for side venting, the vent may still have a considerable inductance if the length to width ratio is large. When the vents are collected through manifolds, as is often the case, the length and breadth of the channels prior to the common volume must be considered. In addition, if volumes are large, it is conceivable that capacitive effects may have to be considered. The low frequency gain increase is generally only 3-4 db and does not affect the bandwidth. It is of interest to note that this peak does not appear in the low aspect ratio cases where the velocities are much higher and the Reynolds number based on jet width is very high. In those cases, the feedback appears to be insignificant. The main resonances seem to line up fairly well as can be observed in figure 42 for the case when the load is an Identical LPA. The phase shift is remarkably well predicted as shown in figure 43. Although of considerable importance, the experimental methods are not especially germane to the topic at hand, so the details of the experiments and the gathering of data are relegated to Appendix II.

In order to see that the feedback terms in the model are having a significant effect, runs were made with the feedback terms zero. One such resulting Bode plot is shown in figure 44. As is observed, a single peak occurs that is due to a resonance of the inductive and
Figure 40. Theoretical frequency response of the standard HDL LPA with low vent inductance. Self-staged case.
FREQUENCY RESPONSE OF AN LPA

Figure 41. Theoretical frequency response of the standard HDL LPA with low vent inertance. Blocked output case.
Figure 42. Comparison of theory and experiment for the frequency response of an HDL standard LPA at high aspect ratio.
Figure 43. Comparison of theory and experiment for the phase shift as a function of frequency in a high aspect ratio HDL standard LPA. Self-staged case. (Note: In order to display the phase angle within the bounds of the figure, *360° has been added to the results, where necessary.)
Figure 44. LPA frequency response when acoustic feedback is zero. (vents act as perfect ground of zero resistance)
compliant terms. Under the same conditions with non-zero feedback terms but low values of inductance, the plot is as shown in figure 45. The second peak is at the same frequency as the resonance of figure 44, hence, it is not due to feedback; whereas, the first and all others are due to feedback. For the case when the outputs are blocked \( (Z_L = \infty) \) the resonances are more pronounced as shown in figure 46. When the feedback terms are again neglected, no resonances occur as is seen in figure 47. This then explains the origin of the second resonance in the self-staged case and the increase in overall gain as being due to the lead function of the load (the LPA input).

Coming back for a moment to the feedback mechanism of the resonances, it is essentially the same as postulated for edgetones by Kirshner\(^7\). It is therefore of interest to see if the regions of high gain correspond to the edgetone eigenfrequencies. In figure 46 the resonances are due only to acoustic feedback hence let us examine them. The theoretically observed resonant normalized frequencies are:

\[
F_1 = 0.05, 0.113, 0.175, 0.27
\]

and the ratios relative to the first are

\[
F/F_1 = 1.0, 2.26, 3.5, 5.4
\]

These values are not harmonics and are very close to the edgetone eigenfrequency ratios reported by Brown\(^40\).

\[
f/f_1 = 1.0, 2.3, 3.8, 5.4 = j_1
\]

If now the frequency is put into Brown's form

\[
f = 0.466(u_o/\lambda)j_1 \tag{64}
\]
Figure 45. Theoretical LPA frequency response for small values of vent inerteance.
Figure 46. Theoretical blocked output LPA frequency response for the same conditions as in figure 45.
Figure 47. Theoretical LPA frequency response for a blocked output case with no acoustic feedback.
where \( u_0 = c_d V_s \) the average jet exit velocity, then

\[
f = 0.466 \left( \frac{c_d V_s}{x_{sp}} \right) (X_{sp} F_s / 0.466) \tag{65}
\]

where by inspection

\[
j_1 = X_{sp} F_s / 0.466 = 17.167 F_s \tag{66}
\]

where \( x_{sp} = 8.00 \). In such a case then the matched eigenfrequencies are

\[
j_1 = 0.858, 1.94, 3.0, 4.635
\]

These represent the absolute values of frequency at which oscillations would occur given sufficient gain. They are close to those values observed by Brown. It is of interest to note that this result was obtained by a lumped parameter approach as opposed to a particle mechanics or other more detailed approach. This independently supports the theoretical analysis and indicates perhaps some generality.

Following this edgetone problem a little further, one may observe that when the Reynolds number is decreased, the predominance of the second resonance is reduced in favor of the first as can be seen in figure 48 where the Reynolds number is one-half of that previously shown \( (N_R = 150 \) as opposed to 300 for the previous cases). The reason for this is seen in the values of the parameters as a function of Reynolds number. The vent impedances are predominantly inductive as can be seen in comparing terms for a typical geometry, hence

\[
Z_v = R_v + j\omega L_v \tag{67}
\]

For a short channel \( \frac{X_v}{L_v} = 1, B_v = 4, N_R = 400, \sigma = 2, c_d = 0.7 \) the equation for duct resistance gives

\[
R_v = 0.003
\]
Figure 48. Theoretical LPA frequency response at reduced Reynolds number.
and the inertance
\[ L_v = 2 \frac{c_d^2}{d_x/B_v} = 0.25 \]
so that at high frequency, e.g. \( F = 0.05 \) or \( \Omega = 2\pi F = 0.3 \), the inductive reactance exceeds the resistive by a factor of almost 30. Now observe that as Reynolds number decreases, so does inertance since discharge coefficient decreases. This means that less pressure is developed to be fed back and as a consequence the resonances are smaller. At the same time the jet compliance is dramatically increasing since it depends on the inverse square of discharge coefficient. This means that the frequency response is rolling off sooner and the second resonance is down further while the first resonance is still near the flat response. This kind of superposition argument seems to be appropriate in light of observations.

That, indeed, a sustained oscillation like an edgetone is feasible is demonstrated by increasing the vent impedance to a large value about 20 times that found in a well vented LPA. Figure 49 shows the Bode plot for this case where the extremely dominant resonance indicates the point at which the device would oscillate. That this is qualitatively true has been observed time and again when inadequate venting is provided for LPA's. Experience has shown that jet devices must be well vented and cross-coupled to prevent oscillation. Figures 50 and 51 are photographs of an LPA laminate with coverplates that allow venting directly at the edge of the jet. In effect, the jet is bounded by planes only over the lateral distance of full jet deflection, plus a bit. When such venting is not observed, the LPA will oscillate at high Reynolds numbers prior to transition-to-turbulence. As a matter of fact, the point of transition-to-turbulence is moved to a lower Reynolds number if laminar oscillations are allowed to occur due to poor venting. Figure 52 shows photographs of spectrum analyser traces of a poorly
FREQUENCY RESPONSE OF AN LPA

Figure 49. Theoretical LPA frequency response when a long vent with high inertance (e.g., long manifold) occurs, showing high resonant peak conducive to oscillation.
Figure 51. Photograph of an LPA lamination and its associated venting plate as found in normal stacking.
Figure 52. Spectrum analyser traces of transition to turbulence in an LPA, showing edgetone oscillation just prior to transition.
vented amplifier of a long nozzle LPA silhouette as shown. Figure 52(a) shows a clean, sharp resonance at 2500 Hz which is the first edgetone eigenfrequency (f = 2500 Hz corresponds to F = 0.05). Each photograph shows two traces; the lower one with no flow and the superimposed upper one with flow. When the two traces coincide as in 52(a) (except for the resonance), the flow is defined to be laminar. Figures 52(b), (c) and (d) show the progression of turbulence from high frequencies to low with 52(b) showing that the oscillation vanishes just before transition. This seems to support the theoretical consideration since at transition the jet spreads and both gain and pressure recovery are lost so that oscillation ceases. If one were to attempt to tie the occurrence of edgetone oscillation to transition, it would require considerably more work and analysis into the hydrodynamic stability of the flow. It is not attempted here but note is made of it.

As the aspect ratio is decreased, one observes that to maintain the nominal operating modified Reynolds number, the supply pressure must be increased. This increases the parasitic or channel capacitance and also increases the feedback signal attenuation because the bounding walls are closer. These two effects both reduce the normalized bandwidth. The increased capacitance promotes faster rolloff by attenuating the input signal and the increased feedback attenuation reduces the acoustic feedback.

It should be remembered at this point, in defense of prior analyses, that the LPA has a geometry quite different from those in existence at the time of early work by those such as Brown, Belsterling, Healey and Kirshner and Katz. A particular difference lies in the high input impedance and close proximity of the jet to the control edges. Prior amplifiers always had large clearances so that the clearance reactance could be neglected.

This analysis is in relatively acceptable agreement both qualitatively and quantitatively with experimental data as shown in figures
42 and 43 and in more detail in the Appendix II where various aspect ratios and Reynolds numbers are considered. Therefore, it can be used to generate the engineering guidelines that follow.

2.1.4 Bandwidth Guidelines

For the cases of various loading on the high aspect ratio, HDL standard LPA, model 3.1.1.005 shown in figure 27, the frequency characteristics will lie generally between the blocked case and the self-staged case. In each case the overall maximum bandwidth over which useful gain occurs is $F \propto 0.1$ so that a map of bandwidth, size, aspect ratio and supply pressure can be made for a nominal modified Reynolds number of 120 ($c_{d} \propto 0.7$). When modified Reynolds number $N_R = N_R/(l + X_{th})(1 + 1/\sigma)^2$ is substituted into the normalized frequency the actual frequency (bandwidth in hertz) is

$$f_{bw} = 16.8 \nu (1 + 1/\sigma)^2/b_s^2$$  \hspace{1cm} (68)

Now noting that supply pressure at $N_R = 120$ is defined by

$$P_s|_{N_R = 120} = 28,800 \nu^2 (1 + 1/\sigma)^4/b_s^2$$  \hspace{1cm} (69)

then the aforementioned map is generated for air at 20°C where $\nu = 1.4864 \times 10^{-5}$ m/s and $\rho = 1.2059$ kg/m$^3$ as shown in figure 53. The numerical coefficients in equations (68) and (69) were obtained using a nominal value of $X_{th} = 1.0$.

Similarly one notes in the frequency response characteristic that there exists a region of essentially uniform gain. For the blocked case, the gain is down 3 db at a frequency an order of magnitude lower than that given above or $F \propto 0.01$. For the self-staged case, the lead in the load increases this bandwidth to $F \propto 0.03$. From these
Figure 53. Engineering guide for the frequency response bandwidth of the HDL standard LPA, 3.1.1.8 for high aspect ratios.
observations one can stipulate a bandwidth for the worst case for a single LPA as being \( F \sim 0.01 \). It should be noted, therefore, that if many amplifiers are staged together in series and the last stage is blocked, then care must be taken to describe the overall bandwidth with the reduced frequency response of the last stage taken into account. Looking ahead for a moment to the case where headsets are the load, they are essentially an inductive load (e.g. a long, low-resistance duct) and they may provide some gain compensation, (or "equalization" as is the term used in acoustics).

Based on the premise that feedback from edges and protrusions augments gain of an amplifier, a concept for a broadband amplifier augmented by such feedback has been proposed and a patent disclosure made. The patent disclosure is given in Appendix III. Basically, one may use an extended distance to the splitter that gives increased gain and several intermediate vent vanes to provide extra resonances. Several such devices can be placed in parallel and operated at slightly different supply pressures; thus, the peaks will be shifted from each other. Addition of the output signals will be such that peaks of one occur at anti-peaks of another so that a broad band, fairly uniform gain may be achieved. A favorable internal review of this disclosure has been made and a formal application has been made with in the U. S. Patent Office.

This then completes the analysis of the LPA. As can be seen from the various experimental and theoretical curves presented and especially from the engineering guide in figure 53, the current HDL standard LPA has sufficient bandwidth to be used in audio amplification and the analytical means at hand are sufficient to understand why. Prognosis for ultrasonic operation of these devices is excellent as long as the small dimensions can be manufactured, see for example in figure 53 devices where \( b_s = 0.25 \text{ mm} \).
2.2 Transmission Lines

The communication system will necessarily require a means for transmission of speech and other data from one distant point to another. This will be accomplished by use of acoustic transmission lines. Acoustic transmission through ducts of constant area is treated in every elementary text on the subject, hence, no analysis will be presented here other than that already presented in the previous sections. The texts by Rseatkin16, Zalmanzon29 and Beranek39 form the required background information. Beranek presents the most needed information in that the duct (transmission line) will attenuate the signal as a function of the square root of frequency and inversely as the radius. The pertinent loss coefficient is that the loss in db/meter is

\[ 0.278 \frac{\sqrt{F(\text{Hz})}}{r(\text{mm})}. \]  

(70)

Kirszenblat15 makes note that a transmission line will exhibit a resonant response if it is blocked, loaded with a termination other than the characteristic impedance \( Z = \rho c/A \), where \( c \) is the speed of sound, \( A \) is the cross-sectional area and \( \rho \) is the density), or has a sharp discontinuity or sudden change in areas such as an expansion or contraction. He points out that the use of matching exponential horns eases the problem of reflections and it is for that reason that all terminations in this project are matched through exponential horns.

2.3 Other Passive Components

Other components involved in the communication system are the exponential horns mentioned above, junctions and fittings.
The effects of fittings on the fluidic response are assumed to be negligible when the volumes are small and the changes in area smooth. Their effects in the acoustic region, however, are not small. When acoustic signals converge in a junction where the exit area equals the sum area of the input lines, acoustic summing occurs, wherein the amplitude of the fluctuations add. This is in contradistinction to the case of lumped parameter operation of the fluidics where flows add but not pressure. This brings up the very important distinction between what are called fluidic signals and acoustic signals. Fluidic signals require that the wavelength of a given frequency be large compared with the dimensions of the components under consideration. This is sometimes known as "slowly varying dc." It is intuitively obvious that pressure will distribute itself in such a manner as to accommodate a given flow-rate. However, when one operates acoustically, pressures can add as in the example of reverberant rooms with standing waves. This distinction has often been overlooked, especially when fluidics engineers—not acousticians—attempt to work with acoustics. A particular example is demonstrated in the work that was done on the public address system in 1976. In order to get a high amplitude signal out of large exponential horns with a large column of air, 17 standard LPA's were paralleled to produce enough flow and provide dynamic matching. This is illustrated in figure 54 which shows the PA amplifier. Here five stages of amplifiers make up a three-stage pressure amplifier (pre-amplifier) and a two-stage flow (or power) amplifier that delivers the flow to move the large column of air in the horns. However, when preliminary audio amplifiers were made, the concept of power output was thought to be synonymous with loudness, and a two-parallel stage power amplifier was provided. Instead of an increase in loudness actually a slight decrease was observed. This was because the ear responds to pressure (see Randall) and adding a parallel stage of amplification
reduced the loud impedance on the pre-amplifier and hence dropped the gain slightly. This occurred when the two amplifiers were stacked one on the other, and the pressure was drawn off a common port. When the parallel stages were separated and the signals drawn off separately and recombined in a constant cross-section junction, the loudness was considerably increased. Figure 55 shows schematically the physical arrangement.

The signal transfer within the fluidics package itself is essentially identical; however, the resultant acoustic levels are considerably different. This type of "passive amplification" is very useful in personal-type communication systems and is quite often used by acousticians.
2.4 Concluding Remarks on the Analysis

This section has attempted to tie together many existing analyses, has expanded on them and has provided new insight into the lumped parameter approach for the analysis of the dynamics of fluidic components. As such, the significant results of the analytical and experimental effort are:

1. Entrainment effects such as bias pressures have been shown to be independent of frequency at least to frequencies in the bandwidth of LPA's.

2. The double eddy (whiplash) large signal transient or step response has been shown to be a nonlinear effect that does not materially affect the small signal frequency response; however, it does explain increases in phase shift observed when large signals are used.

3. The development of an improved high order equivalent circuit model for the input impedance of an LPA.

4. A combined acoustic feedback, lumped parameter model of an LPA has been developed that correctly predicts the performance and frequency character of LPA's from the initial broadband low frequency gain increase to the high frequency resonances which occur near the edgetone eigenfrequencies.

5. The prediction of the edgetone eigenfrequencies and their ratios. In addition, both the qualitative and quantitative description of their behavior, within an LPA, has developed as a function of Reynolds number. It is shown that for large Reynolds numbers, the higher edgetone frequencies give rise to resonant peaks in gain. An explanation for the propensity of edgetones to jump from one frequency to another is offered by noting that different peaks are higher (more energy) than others at different Reynolds numbers.
6. The development of engineering guidelines for the estimation of overall system bandwidth to include acoustic and fluidic considerations.

7. The identification of physical quantities such as geometry and fluid properties with equivalent circuit elements.

8. The development of an equivalent model for short fluidic channels as a "tee" network.

9. A broadband fluidic amplifier scheme has been proposed.

The above are highlights only. The insight and the intuition gained has been invaluable. Items of interest were noted in such a way that their relevance could be maintained intact when they were learned. What has really been learned is that there is a lot more that is unknown than is known. For example, the transition between fluidics and acoustics should be carefully examined. The role of edgetones or high frequency gain should be examined in terms of its effect on the transition-to-turbulence. Lumped parameter analysis approaches may be appropriate for a broader area of transition problems. The differences and similarities between a feedback system's stability and hydrodynamic stability of shear layers should be examined. The fluid mechanics of confined jet-like flows should be examined to tie in differences in phase. Integral and differential effects should be examined--for example, the effects of velocity profiles on transport delays.

These are only some of the fundamental single amplifier areas of interest that appear. Whole areas of multiple amplifier dynamic interactions appear as well as those fluidic/acoustic interactions between amplifier components and transmission components. The whole area of generation of interactive engineering models is opened up. Already this author is using the basic transfer function presented herein for multiple component analyses. This model is currently being examined by others as the basis for design of oscillators that will be used as pressure-to-frequency transducers. More will be said about this in a later section dealing with signal frequency generators.
3. FLUIDIC VOICE COMMUNICATION SUB-SYSTEM DESIGN

This section deals with the design and development of hardware for the broad band audio transmission system and considers design analysis and hardware development. The concluding parts of section 3 will be devoted to human and system engineering.

Consider, however, that both the voice and the data link systems are composed of subsystems and components that can be tabulated into a matrix. Both the voice and data subsystems have in common the following: a signal generator, an input, a transmission section, an amplifier, a signal processor, an output, and a power supply. These then form the structure of the two systems.

3.1 The Voice System Feasibility

At the start of the experimental program, feasibility of speech transmission was of paramount importance, so a rough cut was made with an existing high gain amplifier that had dimensions and an operating point that indicated probable voice bandwidth. This was a three-stage, self-staged, ceramic amplifier manufactured to HDL specifications (HDL-STD-MOD 3.1.1.8 amplifiers) by Corning of aspect ratio $\sigma = 1.5$ and nozzle width, $b_s = 0.25$ mm. According to the engineering
map, see figure 53, and equations (68) and (69), this should require that the bandwidth $f$ is in the range $(0.01 < F < 0.1)$ of:

$$100 \frac{\sqrt{P_s}}{b_s} < f < 1000 \frac{\sqrt{P_s} (\text{mmHg})}{b_s (\text{mm})}$$

so that at $P_s = 8 \text{ mmHg}$ (corresponding to $N_{R_1} = 120, \sigma = 1.5$) and $b_s = 0.25 \text{ mm}$, the bandwidth should be between 1.1 and 11 kHz. This amplifier is shown in figure 56 and its single-sided frequency response (differential gain is 6 db higher) is shown in the Bode plot of figure 57. This frequency response very closely spans the human speech pressure spectrum given by Randall in figure 58 and is no worse at frequencies below 2 kHz than a typical loudspeaker shown in figure 59 (also due to Randall). This device was then tested as a speech processing unit by attaching airline-type headphones (merely a 1/8 in diameter plastic tube connected directly to the earhole) to the outputs. The signals in the two lines are $180^\circ$ out of phase; however, the brain does not discriminate the phase relationship and allows the sound to appear twice as loud rather than cancelled. For the first tests an 1/8 in (3 mm) diameter input tube was connected to one control and a tank (low pass filter) to the other so that signals would enter only one control. Speech was not only passed but amplified as expected. The experiment was then broadened to make a full communication link by incorporating two amplifiers and two lines. This also was successful. Then, in an effort to cut down on the number of lines, and the dynamic absorption of the compliant plastic a single copper tube 12.5 mm 10 and 10 meters long was used and the input teed in.

Several important design characteristics were discovered during this portion of the effort. The input could be achieved by a "throat microphone" consisting of a closely clamped "U" tube connected to the
Figure 56. Photograph of a Corning-made three stage gain block (HDL STD LPA 3.1.1.8[3])
CORNING 3-STAGE BLOCK
\( b_s = 0.25 \text{ mm}, P_s = 8.0 \text{ mmHg} \)
NEW - DATA
INPUT HEATED AT 70 DB \( = 0.0007 \mu \text{bar} \)

Figure 57. Frequency response Bode Plot of the ceramic Corning three stage audio amplifier \( (b_s = 0.25 \text{ mm}) \).
Figure 58. Pressure - frequency distribution in normal speech after Randall.42
Figure 59. Typical measured response of a loudspeaker in a "live" room. Smooth line represents the effect to the average ear. (Randall 42).
neck at or near the larynx. This was an extremely important finding because of the superior background noise rejection afforded. Ambient noise must pass through the tubing and through the skin/tube-end interface. Ambient room noise suppression of as much as 40 db was found compared with speaking into an open-ended tube. This type of speech input was investigated because vehicular noise levels may approach 100 db and passing and amplifying this noise is one of the most severe drawbacks of existing intercoms. Personal communication with individuals with expertise in the tank intercom area has resulted in this author's rejection of an open microphone concept. The Air Force routinely uses throat microphones on aircraft for this very reason.

Another characteristic investigated empirically in the early efforts was the output or the headphone arrangement. The best fidelity and loudness could be achieved with the "airline-type" head sets where the outputs of the amplifier were directly fitted into the ear. Exponential horns that fit into ear protection devices as shown in figure 60 were examined. Under certain circumstances when the ear-headphone cavity was large, it was found that loudness could be increased by blocking the ends of the horns with a thin steel diaphragm. When the horn was held directly against the ear, no appreciable difference was noticed. The geometry of the horn was such that the neck diameter was 3 mm flaring out exponentially to 37 mm over an 80 mm length.

The attenuation of the 10 m line is computed from equation (70) based on the highest frequency to be passed, say 3 kHz. Then the loss per meter is

\[
\frac{0.278 \sqrt{3000}}{6.25} = 2.4 \text{ db/m}
\]

or 24 db for a 10 m line. This implies that the gain of the system must be greater than 24 db just to overcome line losses. From figure 57 it can be deduced that a gain of about 46 db is available from the Corning units.
Figure 60. Photograph of prototype fluidic headphone with exponential horns.
Commercial airline crew radios use headsets with metal tubes that swivel and fit into the ear. These lightweight devices provide a maximum of fidelity with a minimum of encumberance.

3.2 The Voice System Design

These preliminary tests proved feasibility of an intercom system and validated the engineering guide to some extent. Consider therefore the design of a workable system for inclusion in a combat vehicle such as a tank or armored personnel carrier. The following matrix of components in table 1 may now be used as a guide for the analysis and design and appropriate choice for the final system.

Table 1. Voice Communication System Component Matrix

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Components</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>signal</td>
<td>human speech</td>
<td>external noise? engine</td>
</tr>
<tr>
<td>Input</td>
<td>throat tube</td>
<td>external noise rejection vs. input loss</td>
</tr>
<tr>
<td></td>
<td>open tube</td>
<td></td>
</tr>
<tr>
<td></td>
<td>diaphragm</td>
<td></td>
</tr>
<tr>
<td>signal transmission</td>
<td>rigid tube</td>
<td>length and diameter to be determined</td>
</tr>
<tr>
<td></td>
<td>compliant radiation</td>
<td></td>
</tr>
<tr>
<td></td>
<td>tube</td>
<td></td>
</tr>
<tr>
<td>amplification</td>
<td>fluidic amplifier</td>
<td>size, gain</td>
</tr>
<tr>
<td>signal processing</td>
<td>output high pass</td>
<td>low frequency</td>
</tr>
<tr>
<td></td>
<td>filter</td>
<td>rumble</td>
</tr>
<tr>
<td></td>
<td>passive input</td>
<td></td>
</tr>
<tr>
<td></td>
<td>low pass filter</td>
<td></td>
</tr>
<tr>
<td>output</td>
<td>direct fitting</td>
<td>human engineering into helmets-comfort</td>
</tr>
<tr>
<td></td>
<td>tubes</td>
<td></td>
</tr>
<tr>
<td></td>
<td>exponential horns</td>
<td></td>
</tr>
<tr>
<td>power</td>
<td>self contained</td>
<td>reliability and redundancy</td>
</tr>
<tr>
<td></td>
<td>parasitic</td>
<td></td>
</tr>
<tr>
<td>interconnections</td>
<td>acoustic</td>
<td>system integration penalties</td>
</tr>
<tr>
<td></td>
<td>flow</td>
<td></td>
</tr>
</tbody>
</table>
3.2.1 The Signal

The signal to be transmitted is human voice. The signals available are basically threefold: the voice; engine or operating noise; and external random noise such as of the battlefield. Typically the ambient sound level in a tank is of the order of 100 db re. 0.00026 bar, hence, hearing protection is required. This is accomplished by ear muff type headphones in the electronic system, which are mounted in a plastic helmet as shown in figure 61. Notice also the boom type microphone that is susceptible to all the sound airborne at the speaker's mouth. Normal speech, 70 db at 1 meter, is a signal about 100 - 110 db at the larynx.

3.2.2 The Input

As previously noted, the feasibility studies were conducted using a clamped tube at or near the larynx. This "throat mike" concept has been chosen for this program primarily due to its superior noise rejection. This concept also removes an obstruction from the face; however, the penalty is wearer discomfort. When the tube ends are clamped very close to the larynx, unacceptable discomfort occurs, but when the tube is placed too far away, the signal is lost. Based on standard throat mike designs, a "U" tube spacing of 10 cm was settled upon. This is consistent with the average neck dimensions of the American male which is about 40 cm (16 inches) in circumference or 12.5 cm in diameter. The chosen microphone arrangement places two open tubes flush against the neck at the one quarter point around the neck centered on the larynx. The two tubes are joined together in an equal area "tee" (the output area equals the input area) so that reflections and distortion are minimized.

Some consideration was given to the use of diaphragms or membranes over the open tube ends to avoid system contamination by particles of dust and moisture such as perspiration and to avoid dc flow saturation of the LPA. Thin neoprene rubber about 0.05 mm (0.002 in) in thickness
1. Microphone on adjustable boom.

2. Switch box with 3-position switch — forward (hold-on) to talk on radio; backward (lock-on) to talk on inter-com; center to listen only.

3. Cable with quick-disconnect plug, a clothes clip, and a coiled cord.

1. Earphones in earpads.

2. Three adjustable web straps.

3. Sweatband.


5. Sponge rubber spacers.

Figure 61. Standard issue US Army tankers helmet showing headphone installation
was found to have little or no attenuation since it lies flat on the skin and falls within the general dimensions of the epidermal layer of the human neck.

A disadvantage of the "throat mike" and blocking membrane concept is that it is a dc blockage that allows no entrained flow, hence, the controls of the amplifier would operate at a suction or negative head. This is undesirable from the standpoint of amplifier stability. LPA operation at negative bias is the basis for the digital operation of a laminar digital amplifier (LDA)\(^43,44\). Typically, the gain of an LPA increases with increasingly negative bias and becomes unstable. While the blocked control pressure is not very negative, only about \(-5\%\) of supply pressure it still could be a problem. Provision of a bleed is one solution, but this provides for undesirable ingestion of ambient air. A slight pressurization of the common transmission line can however be achieved by providing a high resistance shunt from the main pressure supply.

The LPA is inherently a differential device where signals may enter either side. If a time varying signal is impressed on one side of the amplifier, the conditions of loading must be specified on the opposite side. If the condition is such that the opposite side is open to ambient (the opposite control pressure is zero gage) then the instantaneous differential pressure is merely the input signal amplitude since \(\Delta P = P_1 - P_2\) and \(P_2 = 0\) so that \(\Delta P = P_1\). This, however, is not the case at hand. The opposite control must be shielded from all signals. Certainly the voice and noise will radiate towards that port. In addition, since the device is differential but operation is desired around jet centered conditions, the dc level on the opposite side must be adjusted for a dc null output condition. This is accomplished by a variable resistor to ground. High frequency noise and
signals can be eliminated by placing a volume (tank) in series with the resistor to provide a low pass filter. When one anticipates a high pass output filter, as in the matrix of Table 1, then the low frequencies entering will wind up being filtered at the output. The variable resistor (valve) will allow individual adjustment of null so that the volume of the tank must be determined. The circuit, however, is complicated by the fact that the amplifier input impedance is involved. However, at low frequencies it is fortunately mostly resistive. The equivalent circuit of the nulling low pass filter then is as shown in Figure 62.

\[ P_2 / P_n = \frac{R_{\text{valve}} Z_T}{[R_{\text{valve}} (R_{\text{LPA}} + Z_T) + R_{\text{LPA}} Z_T] + R_{\text{LPA}} Z_T] + R_{\text{LPA}} Z_T} \]

which reduces to equation (72) when it is noted that \( Z_T = 1/C_s \).

\[ P_2 / P_n = \frac{[R_{\text{LPA}} (R_{\text{LPA}} + R_{\text{VALVE}})]}{[R_{\text{VALVE}} R_{\text{LPA}} + R_{\text{VALVE}} + R_{\text{LPA}}] C_s + 1} \]
The break point frequency is
\[ f_{\text{-3db}} = \frac{1}{2\pi RC} \]

where \( RC \) is the RC time constant

\[ \tau_{RC} = \frac{R_{\text{VALVE}} R_{LPA}}{R_{\text{VALVE}} + R_{LPA}} \]  \( (73) \)

and where the volume capacitance is given as

\[ C = \frac{V}{P_{\infty}} \]  \( (74) \)

With a breakpoint frequency of 100 Hz this results in a volume of

\[ V = \frac{\frac{P_{\infty}}{200\pi}}{\left(\frac{1}{R_{\text{VALVE}}} + \frac{1}{R_{LPA}}\right)} \]  \( (75) \)

For typical values of \( R_{LPA} = 10^8 \text{ Pa/(m}^3/\text{s}) \), \( R_{VALVE} = 10^9 \text{ Pa/(m}^3/\text{s}) \),
and \( P_{\infty} = 1.01 \times 10^5 \text{ Pa} \), \( V = 1.77 \times 10^{-6} \text{ m}^3 \) or a volume of 1.77 cm\(^3\). This is fairly small, hence, any reasonable volume of several centimeters dimensions will provide more than adequate filtration.

With this nulling filter circuit as the load on the opposite control, the opposite side control pressure is a constant essentially equal to the blocked control bias pressure. This pressure is determined from the static characteristics of the LPA as determined by this author previously and shown in figure 63. This program has been amended and rewritten in FORTRAN and the current dynamic analysis has been incorporated. The static analysis program is required to compute the various resistive parameters required herein. The complete listing is given in Appendix II. As can be observed from figure 63, the blocked control pressure is available from the centered jet input characteristic when FLOW = 0. This normalized pressure is -0.06 or -6% of supply pressure.
Figure 63. Computer plots and printout for the static performance characteristics of a high aspect ratio (σ = 3.0) HDL standard LPA as computed by Drzewiecki's program.
3.2.3 Signal Transmission

It has already been demonstrated that audio signals can be transmitted over a distance of 10 m. It is now of concern to actually determine the distance required in a combat vehicle. The choice of vehicle is somewhat arbitrary, and since this author is involved and familiar with the M60 class of tanks, an M60 tank is chosen for this problem. Figure 64 shows the side and top views of an M60. The longest distance occurs between the driver in the front and the commander who sits up high in the turret. The straight line distance is 2 meters but allowing for bends and detours, 5 meters is the maximum distance encountered.

It has been established that elastic tubes add considerable signal attenuation due to the added compliance, hence, they are ruled out. But even if not for that reason, elastic tubes act as antennas to motion since small geometric changes can induce pressure signals. Copper tubing was used in the feasibility demonstration; however, copper is expensive and relatively soft. For this reason rectangular cross-section wave guide was chosen. Studies on audio transmission through rectangular ducts indicate that circular duct analysis can be used if the hydraulic diameter is utilized. The hydraulic diameter is

\[ d_h = \frac{2bh}{b + h} \]  

(76)

hence, in the present case \( d_h = 1.667 \) cm, and the attenuation from equation (70) is 1.8 db/m or 9.0 db for a 5 m length. It is desirable to keep the losses as small as possible since more losses are expected in connections and area mismatches.

3.2.4 Amplification

Randall\textsuperscript{42} states that the ear is best attuned to understanding and intelligibility when the sound pressure level to the ear is about
Figure 64. Side and top views of an M60 tank.
The sound pressure level in a tank is about 0.0002 μbar. The sound pressure level within the ear protection devices is down 15-20 dB at 42 J. Randall further states that a certain background level must be exceeded for intelligibility as shown in figure 65.

![Figure 65. Increase of sound pressure level over a masking background noise due to Randall.](image)

For engineering purposes, consider signals must be a minimum of 20 dB above the background noise to be understood and, say, 26 dB (an extra factor of two) to include a safety factor and to prevent straining. Thus, the signal to the ear must be at about 106 dB. The input signal is at a similar level, so that the amplification required must overcome only the losses. Typically, losses are mainly due to area changes, and acoustic losses occur proportionately to the area change. Upon expansion, sound level is lost due to the Bernoulli effect—the velocity decreases. The area decreases, reflections are the main cause of signal losses.

Exponential horns reduce the losses considerably between tube...
sections; however, the main losses due to area changes occur at
the fitting as the circular cross-section changes to the planar
cross-section. Assuming that the overall losses are minimized to the
acoustic attenuation in lines, then the losses into an LPA can be
characterized as $\zeta_{\text{LPA}}$

$$\zeta_{\text{LPA}} = \frac{A_{\text{FITTING}}}{A_{\text{CONTROL}}}$$  \hspace{1cm} (77)

where $A_{\text{FITTING}} = \pi d_f^2 / 4$, $d_f$ is the internal diameter of the control port
fitting which is usually made equal to the maximum width of the
control. $\zeta_{\text{LPA}}$ is a measure of the energy allowed to pass into an LPA
assuming that the incident energy is reflected back from the mismatched
area. This can be seen on the drawing of the LPA in figure 7. The
area of the control, $A_{\text{CONTROL}}$, is the maximum width, $d_f$, multiplied
by the depth, $h = \sigma b$, hence the losses are

$$\zeta_{\text{LPA}} = \frac{\pi d_f^2}{4 b \sigma}$$  \hspace{1cm} (78)

For the standard LPA, however, $d_f/b = 4.65$ so that the input losses are

$$\zeta_{\text{LPA}} = 3.65/\sigma$$

where as expected the losses decrease with aspect ratio. This same
ratio occurs on the outputs, hence, an engineering figure of merit can
be obtained using $\zeta_{\text{LPA}} = 7.3/\sigma$ for the whole LPA.

The input tubing from the "throat mike" is 3.175 mm diameter so
that equation (70) gives a loss of 9.6 db/meter. A 1.0 m section is used
to connect to the transmission line to allow freedom of movement.
Similarly, if a 1.0 m line of the same dimensions is used to transmit
the audio from the amplifier to the ear, then the total line losses are 28.2 db. The loss in the LPA will depend on the aspect ratio of the device. Taking a worst case of \( \sigma = 0.6 \) the loss will be 22 db. To summarize then, if the output power is to equal the input power the net amplifier gain must equal the sum of the losses, that is:

\[
G_p = \zeta_{LPA} + \zeta_{\text{transmission}} + \zeta_{\text{input}} + \zeta_{\text{output}} + \zeta_{\text{safety factor}}
\]

\[
= 22.0 + 9.0 + 9.6 + 9.6 + 6.0 = 56.2
\]

The gain of the LPA must therefore equal the predicted losses, or \( G_p = 56.2 \text{ db} \) \( (G_p = 630) \) if a factor of 2 (6 db) is added to ensure that there is sufficient bandwidth to pass audio. At very low frequencies, of course, the losses are negligible so that not much dc gain is needed.

The development of a gain block proceeds essentially from a static analysis of single amplifiers. A three-stage self-staged gain block will have a blocked gain of roughly 200, and a self-loaded gain of 125. In any event an additional gain of less than 10 will put the device at a gain greater than required here. The range of choices of staging schemes is quite large. If one wishes to maximize dynamic range, then each succeeding stage should be of a lower aspect ratio and operate at a higher pressure as described by Manion et al.\(^4\) and Drzewiecki et al.\(^5\). In such an arrangement a gain of 630 can easily be achieved in three stages. Such a gain block can be constructed using the simple engineering guide lines given below for the HDL standard LPA:

1. The operating point is \( \sigma N_R = 10^3 \)
2. At the operating point \( c_d = 0.7 \)
3. The Reynolds number is \( N_R = 1000 \frac{b_s}{\sigma} \sqrt{\frac{P_s}{\text{mmHg}}} \)
4. The operating pressure is in mmHg

\[
P_s = \left( \frac{N_R}{120} \right)^2 \frac{1}{\sigma^2} \frac{1}{b_s^2}, \text{ where } b_s \text{ is in mm.}
\]
5. The operating flow in LPM is
\[ 0.3 \left( \frac{N_R}{120} \right) \left( \frac{b_s}{0.5} \right) = Q_s \]

6. The supply resistance is in mmHg/LPM
\[ R_s = P_s/Q_s = 13.3 \left( \frac{N_R}{120} \right) (1/\sigma)^2 (0.5/b_s)^3 \]

7. The input resistance is
\[ R_I = 0.75 R_s \]

8. The output resistance is
\[ R_o = 0.5 R_s \]

9. The blocked gain is \( G_{pB} = 10.0 \)

10. The loaded gain is
\[ G_p = G_{pB} \left( \frac{1}{1 + R_o/R_s} \right) \]

11. The saturation output signal is twice the pressure recovery where \( P_R = 0.35 P_s \)

The above are based on geometric similarity and Reynolds number scaling with a standard reference

\[ b_s = 0.5 \text{ mm} \]
\[ \sigma = 1.0 \]
\[ N_R = 120 \]
\[ P_s = 4 \text{ mmHg} \]
\[ Q_s = 0.3 \text{ LPM} \]

and the results of the static computer program.
From this design guide it is apparent that staged gain is maximized when the load impedance is large compared with the output impedance. Dynamic range is the ratio of maximum input signal to minimum detectable input signal. This is similar to signal-to-noise ratio. If a staging arrangement is chosen so that the last stage saturates before first stage saturation occurs, then the first-stage dynamic range is reduced since the maximum output is limited to that which saturates the last stage. Dynamic range therefore is maximized when each succeeding stage saturates at the same time. This means that the saturation output of each preceding stage should be sufficient to saturate its load stage so that with a gain of $G_p'$, the output pressure of the $(n-1)$ stage is related to the $n$th stage by:

$$P_{o(n-1)} = \frac{P_{on/G_p}}{G_p}$$

and since the supply pressure is related to the output saturation pressure, then

$$0.7 \frac{P_{sn}}{G_p} = 0.7 \frac{P_s(n-1)}{G_p}$$

so that $P_s(n-1) = \frac{P_{sn}}{G_p}$ or with $G_p = 10$ each succeeding stage must operate at a pressure equal to 10 times the latter stage. From guideline 4 the different aspect ratios can be determined

$$P_s(n-1) = \left(\frac{1}{\sigma_{n-1}}\right)^2 \left(\frac{1}{b_{sn(n-1)}}\right)^2 = \left(\frac{1}{\sigma_n}\right)^2 \left(\frac{1}{b_{sn}}\right)^2 \frac{1}{G_p}$$

so that for the same size ($b_{sn} = b_{sn(n-1)}$)

$$\sigma_n/\sigma_{n-1} = \sqrt{1/G_p} = 0.3$$

Now the limit on aspect ratio is generally kept at $\sigma = 0.3$ for below this value gain and other characteristics are adversely affected due to viscous boundary layer losses. Hence, the last stage minimum is

$$\sigma_n = 0.3$$

then $\sigma_n-1 = 1.0, \sigma_n-2 = 3.3, \sigma_n-3 = 11.0, \text{ etc.}$
It becomes clear very quickly that beyond three stages of the same size the first stage aspect ratio is large requiring a very low pressure, perhaps beyond the realm of practicality. If the ratios of aspect ratio are not optimum, then dynamic range is sacrificed and the last stage will saturate before the first stage.

A three stage gain block of maximum dynamic range will have a gain approaching $10^3$ (60 db). Guideline 10 is used where

$$\frac{R_o}{R_L} = \frac{R_o(n-1)/R_n}{0.5 R_s(n-1)/0.75 R_s}$$

$$= 0.667 \left(\frac{\sigma_n}{\sigma_{n-1}}\right)^2 = 0.0667$$

so that $G_{p\text{ total}} = G_{p1} G_{p2} G_{p3} = G_p^3 (0.9375)^2$

where the last stage is blocked so that a net gain of $G_p = 879$ is achievable. Notice, however, that three separate pressures must be supplied.

If one pressure were supplied, thus eliminating manifolding and reducing resistors to reduce line pressure, the load impedance ratio would be self-staged ($R_{s1} = R_2 \ldots$)

$$\frac{R_o}{R_L} = 0.5 R_s/0.75 R_s = 0.667$$

so that a three-stage block would have a gain of 360 and a four stage blocked gain of

$$G_{p\text{ total}} = G_{p1} G_{p2} G_{p3} = G_{p4}^4 (0.6)^3 = 2160$$

and self-loaded gain of 1296. This, then, allows a degree of flexibility in the choice of circuit topology (choice of staging schemes) since either 3 or 4 stages can do the job.
Now the choice of size and aspect ratio must be involved with the frequency response. Notice that a single stage response as shown in figure 40 and 41 has useful gain out to a normalized frequency of $F = 0.1$; however, there are regions of low gain which, when amplified in multiple stages, cause considerable degradation. For example, the low gain region between $F = 0.01$ and $F = 0.05$ is down only 5 db in a single stage, but in a self-staged, four-stage block this will be down 20 db (a factor of 10). This is clearly undesirable. The gain should be as uniform as possible over the desired bandwidth while non-uniform high frequency gain beyond say 4 kHz may enhance, picking up and transmitting some higher harmonics. The bandwidth chosen here is that of a telephone, 3 - 4 kHz, since this is all that is required for intelligibility and individual recognition. The voice spectrum is down 14 db at 4 kHz so that if the amplifier is down, say 5 db at that point, the signal should be still clear. The single amplifier transfer function can be expanded to consider a multiple amplifier configuration by successive multiplication of the transfer function for successive amplifiers. In the self-staged case for moderate vent inductance (say due to extra manifolding, $L_V = 1.0$) a four stage frequency response is shown computed in figures 66 and 67. The gain is down 6 db at a frequency of $F = 0.012$. However, in the maximum dynamic range case, each succeeding stage has a higher actual frequency response so that when the first stage is rolling off, no succeeding stage is yet doing so. In such a case the -6 db point of a single amplifier can be used to determine the bandwidth. From figure 42 the -6 db point occurs at about $F = 0.03$. There can be considerable advantage to using the maximum dynamic range scheme if the first-stage is the same as that in the self-staged component. Not only is bandwidth increased, but also phase shift is reduced since most of the phase lag will occur in the slow first stage. A three-stage gain block with a lower aspect ratio fourth stage can also
Figure 66. Frequency response of a four stage, self staged LPA (gain only) (theoretical).
Figure 67. Frequency response phase shift of a four-stage, self-staged LPA (theoretical).

(Note: In order to display the phase angle within the bounds of the figure, ±360° has been added to the results, where necessary.)
Increase the actual bandwidth in that the normalized frequency for three stages is \( F = 0.015 \) as can be deduced from the -6 db point from figure 68. With this one can deduce a function for the usable bandwidth of a gain block whose frequency response is limited by a different number of stages. This is shown in the log-log plot of figure 69.

The three stage gain block would require a first stage aspect ratio of \( \sigma = 3.3 \) if the normalized bandwidth is \( F = 0.03 \), or

\[
\text{f}_{\text{bw}} = 300 \sqrt{P_s / b_s} \quad \text{(mm)}
\]

For \( \sigma = 3.3 \), \( P_s = 0.6 \) and 2.5 mmHg respectively for \( b_s = 0.5 \) mm and \( b_s = 0.25 \) mm. In the case of the smaller and higher frequency device, the bandwidth is only 1.9 kHz and, hence, not acceptable. For a four stage gain block whose first three stages are a selfstaged pre-amplifier, the limiting bandwidth would be

\[
f = 150 P_s \sqrt{P_s} / b_s \quad \text{(mm)}
\]

so that for \( f = 3000 \) Hz, \( P_s = 25 \) mmHg when \( b_s = 0.25 \) mm or \( \sigma = 0.8 \) and \( P_s = 100 \) mmHg when \( b_s = 0.5 \), or \( \sigma = 0.25 \). This latter case is beyond the limit for laminar operation and also an undesirably low aspect ratio. This analysis then shows that the size of the device should be smaller than \( b_s = 0.5 \) mm. The next size down that is readily available is \( b_s = 0.25 \) mm. The Corning 3-stage device of figure 57, \( \sigma = 1.5 \) and \( b_s = 0.25 \), is down 6 db at 2000 Hz at \( P_s = 8 \) mmHg. From the above theoretical equation we get 1700 Hz which is slightly low but still reasonably close. However, the theory is conservative and slightly underestimates bandwidth, so that higher aspect ratios can be used than predicted.

As a compromise therefore, let the preamplifier be of aspect ratio \( \sigma = 1.2 \) that operates at \( P_s = 10 \) mmHg. It is important to reduce the supply pressure on the initial stages so as to reduce power supply flow noise, which can be amplified by later stages when the common
Figure 68. Gain frequency response of a three stage, self-staged LPA (theoretical).
Figure 69. Engineering guide for uniform bandwidth as a function of number of stages that determine cutoff frequency.
mode rejection ratio is not infinite. It is for this reason then that it is desirable to operate at as high a first stage aspect ratio as possible. The last stage is made to be aspect ratio \( \sigma = 0.8 \) since its one-stage bandwidth is 6000 Hz and well above affecting the overall bandwidth. Two such amplifiers in parallel will thus allow the addition of acoustic signals as described in section 2.3, figure 55 for some increased output. The two in parallel will load down the pre-amplifier, but there still will be sufficient gain.

The gain of a four-stage amplifier comprising a three-stage pre-amplifier of \( \sigma = 1.2 \) and an acoustic power amplifier of \( \sigma = 0.8 \) will have a gain

\[
G_p(4) = G_{pB}(0.6)^2(1 + \frac{R_{03}}{R_{14}})
\]

but \( R_{14} \) will be one half of a single \( \sigma = 0.8 \) or

\[
\frac{R_{03}}{R_{14}} = \frac{2.2}{3} \left( \frac{\sigma}{\sigma_3} \right)^2 = 0.593
\]

and

\[
\frac{1}{1 + \frac{R_{03}}{R_{14}}} = 0.63
\]

so that

\[
G_p(4) = G_{pB}(0.6)^2(0.63) = 2268
\]

or a value just slightly greater than a four-stage self-staged device, but with more dynamic range and bandwidth.

Just such an amplifier was constructed with photochemically metal etched laminations that were over-etched slightly. The result was that the blocked gain was 8.0 so that theoretically a four stage blocked gain of 930 should have been recorded for the whole block and 110 for the preamp. Figure 70 shows the pre-amplifier dc transfer characteristic as

\[\text{Common mode rejection ratio is a measure of the insensitivity of the LPA to identical signals applied simultaneously to both controls.}\]
Figure 70. Experimental data for differential output pressure versus differential control pressure for the $\sigma = 1.2$ pre-amplifier. (Slope is the gain $G_p = \frac{dP_o}{dP_c}$)
taken on an x-y recorder with different supply pressures and $G_p$ is seen to be just over 100 so that with a last stage of gain of 8.0, 800 overall gain can be achieved. (Note that the overall transfer function was not measured at dc because a high pass filter is incorporated in the stack, as will be discussed in the next section, which is an L-R shunt to ground between the pre-amp and the last stage.) The Bode plot will be shown later but the extrapolated dc gain is indeed about 58 db as desired. A schematic of the gain block and manifolding is shown in figure 71.

3.2.5 Signal Processing

It has already been mentioned that a high pass filter is to be used. The purpose of this device is to remove unwanted low frequency rumble and harmonics of 60 Hz found in machinery. Additional low frequency (less than 800 Hz) noise comes from the engine and the harmonics of the hull motion of the tank such as the suspension resonances. A high pass filter in acoustics is merely an open ended tube that is short compared with the wavelengths of the frequencies to be considered. The tube segment can then be treated as a single lumped inerance and parasitic resistance. When placed between two stages of an LPA gain block, the output impedance of one stage and the input of the next form the branches of a "tee" circuit. For low frequencies, as before, treat these as resistances and the equivalent circuit appears as in figure 72.
Figure 71. Schematic drawing of the four stage audio amplifier.
The input pressure to the last stage will be within 6 db of the pressure without a shunt when the magnitude of the shunt impedance equals the input resistance.

\[
\sqrt{R_{SHUNT}^2 + L_{SHUNT}^2 \omega^2} = R_1
\]

so that \( \omega = \sqrt{R_1^2 - R_{SHUNT}^2/L_{SHUNT}} \) \( \text{(83)} \)

Since \( L_{SHUNT} = \rho \ell / A_{SHUNT} \), the desired frequency \( f = \omega / 2 \pi = 1000 \text{ Hz} \) and the area is the area of a control port fitting \( A_{SHUNT} = d_f^2 / 4 \) where \( d_f = 1.2 \text{ mm} \) for a half-size device with \( b_s = 0.25 \text{ mm} \), then the length of tube required is 8.4 cm if the input resistance of two parallel amplifiers \( \sigma = 0.8 \) is \( R_1 = 5.6 \times 10^8 \text{ Pa/m}^3/\text{s} \). The shunt resistance \( R_{SHUNT} = 8 \mu \ell / \pi r^4 \) is very small compared with \( R_1 \). The frequency at which the length dimension is a half wavelength is about 2 kHz. At this frequency the acoustic signal leaving the shunt will
cause a rarefaction wave to be reflected back and will put a notch in the input signal. The notch must be moved to a higher frequency to avoid interference with audio transmission. This can be done by halving the shunt length and area. The inductance remains the same, but the resonant frequency is doubled.

The final high pass filter then is a tube 4.0 cm long and 0.85 mm in diameter. With this filter installed between the pre-amplifier and the last stages, an additional benefit accrues—the d.c. signal is shorted to ground, hence, d.c. null offsets are eliminated preventing the saturation of the last stage due to asymmetries in the pre-amplifier. Figure 73 shows both a photograph of the final hardware of the gain block and its ultimate frequency response. Notice that the Bode plot is not very different from the Corning gain block except for the high pass characteristics at low frequencies and that the bandpass is greater. As pointed out in the previous section, the bandpass gain is about as expected and actually a bit higher due to the operation on the slight hump in the vicinity of $F = 0.01$.

Signal conditioning or processing also involves the conditioning of the power supply. As a general rule it is desirable to remove noise from the supply flow. This is normally done with a low-pass filter or a tank in-line with the supply flow. The dimensions are essentially the same as for the low-pass on the opposite control. Further conditioning is required if the power supply itself generates a particular frequency. In such a case a notch-filter using for example a blocked, resonant line tuned to the undesired frequency will additionally remove fluctuations of this particular frequency. Section 3.2.7 will discuss the power supply in detail.

† This is the basis of a notch filter temperature sensor described by Drzewiecki et al.^[45]
Figure 73. Experimental BAFCO Bode plot of the audio amplifier frequency response at $P_s = 22$ mm Hg.
3.2.6 The Output

The output is composed of the transmission lines from the audio amplifier to the termination at the ear. The two types of terminations considered have been discussed previously as direct termination in the ear or termination in the volume of an ear protector through an exponential horn. In either case the response is affected by the resonances set up in the line. The effect is quite pronounced when the terminations are direct; whereas, with the horns, reflections are minimized. The low end cut off frequency of an exponential horn is determined by its length. For a length less than a quarter wavelength, low frequencies are reflected and a mismatch occurs. The cutoff for the 8 cm long horns described previously is 1 kHz. Since the band pass is to be about 1 - 4 kHz, this horn is adequate.

Both types of outputs have been adopted. The horns are mounted in helmets while the headsets can be used without the helmet when it is not desirable to wear it. A photograph of the complete intercom system (without power supply) is shown in figure 74.

3.2.7 The Power Supply

In any powered vehicle there is normally a source of pneumatic pressure already available from the engine in the form of a manifold vacuum or compressor bleed. In any event, either mechanical or electrical power is available to drive a pump. The power supply requirement for the audio portion is miniscule. A two-way circuit composed of ten amplifiers that consume 0.15 LPM of flow each and are supplied from a 22 mmHg source require 73 milliwatts. Considering that the supply is regulated and that say 10 kPa are driving the same
Figure 74. Photograph of the audio portion of the fluidic voice communication system installed into a tanker's helmet.
1.5 LPM, then 0.25 watts are required. If the data link circuit has the same order of magnitude requirement, then with a factor of safety of 2, a 1-watt supply is more than sufficient. This is a very small drain on the total vehicular system no matter which power source is used. For that matter human breath would be sufficient to operate the system in a pinch.

The question arises then which power source to use? Obviously, the system must work when the engines are off. This eliminates direct bleed from the engine. The engine could be used to charge an accumulator tank, however. This is very attractive since this approaches operating from bottled gas which is a very quiet power source. An accumulator, however, would be large and have to be pressurized quite high in order to provide long term power. In addition, a compressor would be required that delivers the high pressure. This is a distinct disadvantage. On the other hand, operating off the main batteries would be easy and, as pointed out above, would require little power drain.

Vibrating diaphragm, industrial grade air pumps are available in many sizes and are generally low cost. One such pump is manufactured by a company called WISA. The series 120 pumps shown in figure 75 and whose characteristics are given in figure 76 amply satisfy the pneumatic requirements set forth here. Electrical consumption is 4 watts. The model 120 is a pressure output pump that puts out over 15 kPa at a rated flow of 1.5 LPM which will be sufficient to drive a regulator (if desired) and the complete system. As it turns out, if the voltage is fixed to the pump and the load is fixed--as it will be, then the system supply pressure will be constant without the need of a regulator. Since d.c. drift does not affect the operation because of the high pass output filter used, small variations in supply will not materially affect the operation. Bandwidth is proportional to the square root of supply pressure so that variations in
Model 120

dimensions: area of base = 158 x 67 mm,
height = 80 mm, weight = 1.00 kilogram
dimensions without casing: area of base = 130 x 42 mm,
height = 50 mm, weight = 0.6 kilogram
consumption = 35 milliamp

Model 120

This is also a pressure pump, but smaller in size and with a lower performance than Model 200. This, of course, means a further saving in cost.

Model 120 VDS

This is a suction pump with these smaller dimensions.

Model 120 VDS-vD

This is the same pump as before, designed for a higher degree of vacuum. Those two last-named models are only available without casing, for incorporation. The whole of the Model 120 series is suited to constant running.

Figure 75. Physical characteristics of a WISA vibrating diaphragm pump
Figure 76. Operating characteristics of the series 120 WISA pumps.
supply of as much as 10 percent will result in bandwidth changes of 5 percent or less. This is about ±150 Hz and is tolerable.

The vibrating pump puts out a rippled pressure signal which is adequately damped out by a small volume tank and the volume and resistance in the supply lines. Notice that the preamplifier uses a dropping resistor to drop the common supply down. This fairly high resistance gives rise to a large time constant so that no ripple can be perceived at the output.

Although pumps and compressors are available, these industrial grade pumps (essentially aquarium-type pumps) have an extremely good history of reliability and low cost. They may operate continuously for several years (30,000 hours) and cost less than $30 each in quantity. These pumps have been extensively used by the HDL Fluid Control Branch for operating portable displays and the like with excellent results. For these reasons then, the WISA model 120 is chosen as the power supply for the system.

One should note here that this electrical component will not be adversely affected by EMI or radiation as would electronic components.

3.2.8 Interconnections

Two types of Interconnections have been primarily discussed. Acoustic tee junctions and exponential horns. The tees are machined to maintain constant cross-sectional area. The horns, however, posed a problem, since machining various sizes to reduce or expand from the various size lines to fittings and so forth, would require mandrills or cams.

A simple solution was arrived at for the system put together in the laboratory. By heating a hard plastic tube over a given length
and then applying tension the heated portion will neck down into a shape similar to that of an exponential horn. The large diameter is chosen, and the neck down procedure is carried out until the desired small diameter is achieved. Figure 74 shows the horn constructed in this manner for the input to the audio amplifier. This does not appear, however, to be a practical way of manufacturing metal parts that will be required of a production system. Mandrills can be used then to cast the desired shapes.

The output horns into the ear protection devices were available as cast items from NASA, Langley Field, VA.

3.3 Human Engineering and Systems Engineering Considerations

Most good engineering design considers both the human and the systems aspects of the problem by the very virtue of making a workable system. Certainly if the Intercom system caused unbearable discomfort, it would not be considered as a viable alternative. For this reason wearer comfort has been considered. Unfortunately, the constraints of working with existing equipment, namely the standard issue helmet, have not been conducive to ultimate comfort. Ideally, the headset comfort of stereo headphones would be nice; however, only one helmet type is manufactured. (The standard helmet will not fit people with large heads, say size 7 5/8 and over.)

The current system uses an open-faced, boom microphone. This is a mechanical protrusion in front of the face. While it in no way obstructs the field of vision when in the proper position, it does, however, since it is moveable, offer the distinct possibility that it can move up and obstruct vision and even poke at the face if pushed in, say in a rough riding condition or a collision. The throat microphone
arrangement considered herein does not have these problems. It does, however, require the wearing of a device in addition to the helmet and may take a few seconds longer to put on and take off.

The output has been similarly considered. Attachment of tubes directly into the ear may be an additional chore or at least require manipulation of the ear protectors. This is really the device that can cause severe discomfort after wearing for a short time. Any one who has flown on a long trip on an airplane can attest to the fidgeting required to maintain comfort while watching the movie or listening to music. Operational suitability has to give way here to user comfort. The option is left for using insertion devices since it is simple to change over and because the fidelity of insertion devices is much better than that of the horns in the ear pads.

Since this system is envisioned as a backup to the standard system, it must be unobtrusive during non-use. This has been accomplished by the small size of the audio amplifiers. They can easily be made to fit in the standard interphone control box which has dimensions of roughly 15 x 10 x 10 cm. The laboratory outside dimensions of the audio amplifier are 1.5 x 2.5 x 2.5 cm. These dimensions can be reduced in an integrated bonded amplifier to 1.5 x 2.5 x 1.0 cm. An additional switch can be provided on the interphone control box, labeled for example "STANDBY" or "BACKUP," at the upper right corner of the commander's control box to turn on the air pressure to activate the system. The commander's control box is shown in figure 77. In such a way the fluidic audio system will readily integrate with the electronic system.

The only apparent hardware in the vehicle will be the transmission ducting. The commander, gunner and loader all sit within the cupola which rotates. The driver is in the tank hull. Emplacing the fixed
Figure 77. A view of the M60 commander's control box and frequency selector.
ducting in the cupola does not appear to be difficult. It needs only to trace or follow the existing wiring which is shown in figure 78. The difficulty arises in communicating with the driver. A pneumatic slip-ring or rotating fitting must be provided and mounted near the slip-ring box. Care must be taken that noise is not generated. The dotted lines in figure 78 show a possible layout of the acoustic transmission lines. As is observed, there is no particular disruption evident.

With regard to the systems engineering aspects of the intercom the following morphology of design has been adopted, much as suggested by Simon in his excellent treatment on engineering design.

1. Needs analysis - was presented in the introduction.
2. Feasibility study - was conducted in the preliminary effort.
3. Preliminary design - was completed and demonstrated feasibility.
4. Detailed design - was completed.
5. Production - a brass-board system was built and considerations for actual implementation were discussed.

Simon considers the logical completion of total design to include distribution, consumption and eventual retirement. This was not possible under the present constraints.

The systematic approach to the choice of components and, wherever possible, the logical arrival at a solution, has permitted a relatively uncomplicated flow of design.
Figure 78. Cording diagram of the control boxes in an M60 tank showing the possible location of the acoustic transmission lines.
4. DATA LINK SUB-SYSTEM

This section will consider the design of a system to transmit narrow band frequency modulated information that operates concurrently with the broadband voice system. The applicability of such a system to the tank becomes apparent when one considers the need to either manually or automatically control such devices as the engine or the hydraulic turret drive. If it is possible to use the acoustic transmission lines, then not much additional burden is placed on space requirements.

As was stated in section 3 and as is the intent of this design, there are several components that overlap the audio and the data link subsystems. These are the input connections, the transmission lines and the interconnections. The items that differ are the signal generator and the amplifier/output configuration; these are treated in this section.

4.1 Data Link Design

The data link system has been envisioned as having a high frequency carrier that is inaudible so as not to disrupt the audio portion. Initial studies were conducted to develop an oscillator of a frequency greater than 20 kHz. An edgetone oscillator of about 37 kHz was fairly quickly demonstrated; however, subsequent amplification and demodulation of this signal fluidically proved to be beyond the capabilities of the available hardware. In addition, signal attenuation at this frequency was excessive. It was apparent, however, that since the audio system was not passing signals beyond about 4 kHz, carriers above 4 kHz could be acceptable as long as they could not be heard above the background noise. The sub-system components, therefore, that are described in the following sections are based on this concept.
4.1.1 Input Narrow-band Oscillator

The determination of the carrier frequency will consider the tradeoff between signal attenuation and the availability of signal processing by standard fluidic amplifiers of the smallest practical size with nozzle widths of 0.25 mm as used in the audio portion. Maximum bandwidth occurs at the lowest aspect ratio and the highest supply pressure. Standard laminations are 0.05 mm thick so that two laminations will give the minimum acceptable aspect ratio, $\sigma = 0.4$. On the other hand at aspect ratio of over 1.5, usable high frequency gain occurs at the resonant peaks. From figure 53 it is apparent that the maximum bandwidth is about 10 kHz. For the low aspect ratios, the maximum normalized bandwidth is $F_n = 0.03$ corresponding to 14 kHz for an aspect ratio of 0.4 at a supply pressure of 135 mmHg. These numbers indicate that the carrier frequency must fall within the limits,

$$4 \text{ kHz} < f_{\text{carrier}} < 10 \text{ kHz}.$$  

A convenient frequency in the mid-range is 7 kHz.

To design a 7 kHz oscillator, consider exciting the first edgetone or splitter resonance in an LPA which occurs at $F_n = 0.05$. This can be done by directly feeding back the outputs onto the inputs in the manner of a feedback oscillator. If the feedback line does not attenuate the signal to any great extent and the signal propagates acoustically, then an oscillator is generated since the feedback signal is large. For the feedback mechanism in the LPA, however, the developed feedback pressure near the splitter is low due to signal loss to the vent impedance. In the case of the oscillator, the entire jet dynamic head (loss line losses) can be fed back to the inputs without encountering other losses such as the vent vanes, etc. The equation for frequency as a function
of supply pressure and size in terms of the normalized frequency $F$ and convenient units of mmHg and mm is

$$f = \frac{F \times \sqrt{P_s \text{(mmHg)}}}{b_s \text{(mm)}} \times 10^4$$

(84)

For $f = 7000$ Hz and $F = 0.05$ and $b_s = 0.25$ mm, the supply pressure is $P_s = 12.25$ mmHg. But for moderate aspect ratios from the design guide, $N_R = 10^3$ and $N_R = 10^3 b_s \sqrt{P_s}$ so that $\sigma = 1.14$ and the nearest increment that can be built is $\sigma = 1.2$. An amplifier with an aspect ratio of $\sigma = 1.2$ amplifier was modified by the addition of short feedback lines of square cross-section $0.5 \times 0.5$ mm in the bottom cover plate. A sketch of the oscillator is given in figure 79 showing the location of the feedback lines, and figure 80 is a photograph of the physical arrangement of the oscillator with clear plastic cover plates showing the lines. The oscillator indeed meets the requirement of oscillating at about 7 kHz; in fact, its frequency output varies with supply pressure much as expected. The frequency versus supply pressure characteristic is given in figure 81 and is seen to be non-linear with supply pressure. Deviations from the exact value of frequency are due to the fact that the supply nozzles are not exactly $0.25$ mm wide (they are slightly under) and the fact that the loading circuit affects the frequency. The output level right at the fitting is $100$ db ref. $0.0002$ mbar. It is virtually inaudible when placed in a baffle box and will certainly be inaudible in the $100$ db background noise of a tank.
Figure 79. Sketch of an LPA oscillator designed for operation at the first splitter resonance, $F = 0.05$. 

FEEDBACK LINES

VENTS

0.5 mm

0.25 mm

$P_a$
Figure 80. Photograph of the embodiment of the frequency modulating oscillator for the data link sub-system.
Figure 81. Experimental oscillator frequency output as a function of supply pressure.
Since the frequency shifts with oscillator supply pressure, this is one way to provide frequency modulation. One problem occurs, in that the amplitude also changes with supply pressure. It is, however, desirable to have a signal with constant amplitude since the demodulating scheme may be both amplitude and frequency dependent. The oscillator output may thus be fed into an amplifier stage with constant supply pressure and the output of this buffer amplifier can then be used as the frequency modulated signal.

A different modulating scheme was used in the final design. As observed previously, the frequency output is a function also of the load circuit or the feedback line. When a $3.175 \text{ mm ID line 10 cm long}$ is connected to the unused output by an exponential horn, the frequency may be reduced by almost 300 Hz by merely blocking that tube. Virtually no change in amplitude at the active output occurs. Therefore, frequency modulation may be achieved by variation of either the active source or by variation of a passive component. The former is the basis for a pressure controlled oscillator which is basically an analog-to-frequency (A/F) converter. The latter may be used as a mechanical action-to-frequency converter.

For the problem at hand it is only desired to send two frequencies so that choosing a mid-range frequency of 6.58 kHz results in a reduction to 6.2 kHz when the line is blocked. Thus signal encoding can be achieved by a simple switching arrangement.

In order to prevent pressurization of the transmission line by the dc content of the oscillator, the output is blocked by a thin neoprene rubber membrane.
4.1.2 Signal Transmission

As stated before, the narrow band FM signal will be sent concurrently along the audio transmission lines. All that must be determined is the amplitude attenuation.

From equation (70) for the 5 m line with a hydraulic diameter of 1.667 cm, the attenuation is 13.5 db at 6.5 kHz.

4.1.3 Amplification and Demodulation

The demodulation of a flueric frequency signal into an analog signal is carried out by using the known amplitude/frequency relationship of some circuit. Typically, a first order lead or lag is used where the amplitude changes at 20 db/decade. The amplitude signal is rectified in a non-linear device and the output is then low-pass filtered to get the mean which is then a function of the input frequency. The non-linear device is called a flueric frequency multiplier/rectifier. It is a single output device with an identical input geometry to that of an LPA. The single output is centered on the location where the splitter would be in an LPA. In dc operation the output pressure mirrors the total head profile of the jet impinging on it as it is deflected as shown in figure 82. For small variations of the input, the output stays high since the jet is nearly centered on the output. For large variations the output excursions swing lower so that the mean pressure is lower also. In addition the output stays at only positive values of pressure and for each cycle of input variation, the output has two maxima; hence, if a given frequency is input, then the resultant output frequency is twice the input. This is shown in figure 83. This then means that the carrier will be 13 kHz when leaving the rectifier. This greatly eases the filtration of the output since relatively small volumes and moderate size resistors only will be required.
Figure 82. Fluidic multiplier/rectifier output characteristic, low aspect ratio.
Figure 83. Schematic representation of the operation of the rectifier.
The input required to saturate the rectifier is about 8 mmHg. The input signal is attenuated by the line loss and the fitting loss of 23.2 db down to 76.8 db (10^{-3} mmHg) so that a gain of 8000 would be required for maximum dynamic range. Since only two discrete frequencies will be transmitted however, it is only necessary to have a usable output signal above the noise which is postulated to be 100 db. For a signal of 10 times the noise a 120 db (0.15 mmHg) output signal is needed. The slope of the rectifier transfer characteristic is about 3.0 so that an output change of 0.15 mmHg is attained with an input of 0.05 mmHg so that the .001 mmHg signal available must be amplified at least by a factor of 50. A three stage, self-staged amplifier provided a loaded gain of 120 when loaded into the controls of the rectifier.

The rectifier frequency response must be flat to include the carrier frequency so that at \( F = 0.015 \) from equation (84) with \( b_s = 0.25 \) mm and \( f = 7000 \), then the supply pressure must be \( P_s = 135 \) mmHg with \( \sigma = 0.34 \) for \( \sigma_{NR} = 1000 \). Rectifier laminations in the small size \( b_s = 0.25 \) mm come in increments of \( \sigma = 0.25 \) therefore one uses \( \sigma = 0.5 \) as the lowest acceptable aspect ratio. Amplifier laminations come in increments of 0.2 so that the amplifier can have \( \sigma = 0.4 \) or 0.6. It is most convenient to operate all the devices from a common pressure, and the supply pressure for \( \sigma = 0.6 \) is 45 mmHg, for \( \sigma = 0.5 \) it is 64 mmHg and for 0.4 it is 100 mmHg. It is easiest thus to use a gain block of \( \sigma = 0.6 \) with the rectifier running slightly low. The dc transfer characteristic for the gain block/rectifier circuit is shown in figure 84. Notice the offset from zero. This is caused by the null offset in the gain block. It, however, can easily be nulled out by use of a trim resistor on the opposite control of the pre-amplifier gain block in the same fashion as the null was removed from the audio amplifier.
Figure 84. Experimental transfer function for the gain block/rectifier circuit.
The output now should have a flat response to frequencies beyond 7 kHz. If a resonant circuit is emplaced at the oscillator carrier frequency, then the RMS output will decrease dramatically at that frequency. Such a resonance can be induced in the amplifier circuit by placing acoustic cavities between stages of a length such that the resonant frequency equals the desired frequency. Randall gives this frequency to be

$$f_{\text{resonant}} = \frac{1}{2\pi} \sqrt{\frac{\text{Area}}{\text{Volume} \cdot \xi}}$$  \hspace{1cm} (85)$$

and if the volume is a rectangular channel, then the resonance occurs at

$$f_{\text{resonant channel}} = \sqrt{\frac{c}{2\pi \xi}}$$

where $c$ is the speed of wave propagation and $\xi$ is the length. This also requires a low resistance to eliminate damping. For a resonant frequency of 6.7 kHz, this requires an 8 mm channel. A gain block can be built by physically placing the amplifiers one after another. In so doing, with a standard format LPA, connectors of 16 mm in length can easily be machined in between stages. One expects multiple resonances to occur, the first at 3350 Hz and the second at 6700 Hz.

Figures 85 and 86 respectively show a schematic of the gain block, with cavities and the rectifier and a photograph of the final embodiment of the circuit to include the RC low pass filter (valve and tank) on the output to provide the analog output level. From equation (73) for a pass band of 3 Hz, a volume of 12 cm$^3$ is needed. Figure 87 shows the rectified analog output of the device. Notice that there are indeed considerable notches at 3.5 and 6.7 kHz as expected from the resonances of the interconnecting volumes. The output is effectively the dc null output pressure for frequencies below 3 kHz since a high pass filter
Figure 85. Schematic layout of the frequency demodulating and amplifying circuit block.
Figure 86. Photograph of the demodulating circuitry, $b_g = 0.25$ mm.
Figure 87. Experimental data for the analog output of the demodulating circuit as a function of frequency showing the two resonant notches due to the resonant cavities.
is incorporated to filter out the low frequency audio portions. Figure 88 shows a linear plot expanding the data around the carrier frequency of 6.7 kHz. Notice that at this high input level, frequency discrimination is good. Certainly an output level of 0.05 mm can be discriminated which at 0.024 mmHg/Hz corresponds to less than 0.5 Hz over a band of 200 Hz which is a dynamic range of 400.

Figures 89(a) and (b) show the operation of the modulator/demodulator circuit under the extreme situation of transmission over a distance of 10 m in a 12.5 mm diameter line. The input signal level to the demodulating circuitry was 60 db. The noise level out of the RC filter was less than 0.01 mmHg, and an output signal of 0.1 mmHg was readily achieved for a step change in frequency of 380 Hz. Even at these low signal levels a frequency discrimination of less than 40 Hz is possible with the present system. Figure 89(b) shows an approximate frequency response of the system. The output filter was designed to break at 3 Hz and as the input is modulated (not sinusoidally unfortunately) by alternately blocking and unblocking the resonant line at a more rapid rate, one can observe that the amplitude does decrease. The amplitude is down to 70%(-3 db) of its original value at the point where 3 cycles per second occur. This is in good agreement with the desired design.

Most carrier systems reported on to date have been low frequency because of the limited bandwidth of the amplifiers. In their 1974 paper on fluidic carrier techniques, Boothe and Ringwall cite the state of the art operating ranges of carrier systems as 100 Hz - 3 kHz but speculate about higher carriers of up to 100 kHz. The present carrier of 6.7 kHz, therefore, represents a significant step to the realization of the increased capabilities of fluidic carrier systems.
Figure 88. Expanded experimental plot of the first harmonic notch around the FM oscillator carrier frequency.

$P_s = 50 \text{ mmHg}$

INPUT LEVEL - $\pm 0.03 \text{ mmHg peak-to-peak}$
Figure 89. Oscilloscope traces of transient and frequency responses of FM demodulator/modulator when signals are transmitted 10.0 m
4.2 Human Engineering Considerations

As mentioned previously, the carrier frequency is audible when the background levels are below 100 db. However, enclosing the oscillator in a small box packed with plastic foam provides for a considerable attenuation. Further attenuation is afforded by the audio headsets whether they are of the helmet or the airline types.
5. **FLUIDIC VOICE COMMUNICATION SYSTEM AND DATA LINK IMPLEMENTATION**

Sections 3 and 4 have separately considered the design of the two subsystems: the broadband voice subsystem and the narrow band data transmission system. This section will briefly deal with the implementation of the combined system in a vehicle. The complete system is shown schematically in figure 90. Only the power supply connections have been omitted for clarity.

Implementation of this system can be carried out in vehicles wherein the communication span is of the order of 5 - 10 m. The M60 class of tanks have the general dimensions of the generic species of armored vehicles to include the M48 and XM1 tank, the Infantry Combat Fighting Vehicle XM-2, and armored personnel carriers such as the Army's MICV and Marine Corps LVTP-7. In addition, this system may be implemented in such vehicles as the Army's Lighter, Air Cushion Vehicle (LACV-30), the Navy's V/STOL aircraft, and generically in most fighter aircraft. Control of the lifting surfaces and engine may possibly be done by the narrow band portion of this system. Voice or intercom functions in a fighter aircraft occur over a very short distance, normally about 2 m. In bomber aircraft the bombardier is often considerably removed so that this system may be inappropriate.

The audio and data link subsystems were integrated as shown schematically in figure 90. The total system operation was in accordance with the design goals. No mutual interference was noted. The FM carrier could only be detected in a quiet room within about 2 m of the baffle box. This indicates that the assumption made about its lack of interference was correct. When the head sets are in place, the carrier is inaudible. Speech between two rooms is of telephone quality. The speaker can be readily understood and recognized. FM signal transmission does not
Figure 90. Schematic representation of the full Voice Communication System and Data Link.
affect speech transmission in the least. This demonstrates the feasibility of dual mode signal transmission.

Qualitative tests of bandwidth show that the whole system indeed does perform as the sum of its parts. The long distance, however, does add phase shift to both the audio and data response. For the audio portion, this merely appears as an undetectable delay. For the data system this may prove to be a significant limitation if it is considered for a closed loop control. Insufficient phase margin will significantly affect the frequency response of a closed loop controller.
6. ENVIRONMENTAL SENSITIVITY

The operating characteristics of fluoric laminar proportional amplifiers are dependent on the viscosity and the density of the medium in which they are operating through the Reynolds number and the Strouhal number (inverse of the normalized frequency).

The gain of an LPA decreases with decreasing $N_R$ as shown in figure 91 which is a plot of the self-staged gain of an HDL standard LPA.

![Figure 91](image)

**Figure 91.** Self-staged gain as a function of modified Reynolds number for the HDL STD MOD 3.1.1.8 LPA.

For pneumatic operation the kinematic viscosity of air changes by a factor of two over the standard military temperature range -45°C to +80°C, hence the Reynolds number at constant supply pressure also changes by a factor of two. As is observed from figure 91, one may allow the Reynolds number to decrease from a nominal 120 to 60 and incur only about a 10 percent change in gain. The net change in gain for a gain block of $n$-stages is therefore approximately $10 \times n$ percent. Since each device herein has four stages, that means that a gain change...
of over 40 percent will occur if the supply pressure is held constant. A design around 20°C allowing for a +60°C shift in operating temperature will nominally give a +20 percent variation in gain. This will affect the audio portion to the greatest extent since there is just sufficient gain. However, since there is a factor of two margin incorporated, the voice signal will always be above the background noise.

The frequency response also suffers due to the change in density. The normalized bandwidth remains constant; hence, the bandwidth at constant supply pressure depends on the inverse square root of density. Density changes ±20 percent for temperature changes of ± 60°C around 20°C. This results then in a ±10 percent variation in bandwidth. This is definitely well within allowable bounds giving rise to a low end bandwidth of 3200 Hz at the highest temperature of 80°C. Since operation at the temperature extremes will probably occur infrequently, one may expect even smaller variations. Operation over the temperature range so far has been discussed assuming constant supply pressure. Consider, however, the operation of a pump loaded with a temperature sensitive resistance such as are the LPA supplies and the various manifold resistors. As the viscosity increases, the air herts up, the resistance of the load increases so that the pressure actually increases somewhat. This effect therefore tends to compensate for temperature in that $P_s$ increases as does $v$. The amount of compensation, however, is small and should not be materially counted on.

Frequency of the oscillator is similarly affected. However, since the modulator and demodulator are affected in the same way the fact that the carrier frequency shifts slightly will have no effect on operation. Reduction in gain will have an effect in reducing the dc output slightly.
Variations in altitude will have a significant effect. At 10,000 meters altitude the ambient pressure is one-fifth that at sea level so that density also is one-fifth. This would considerably affect the bandwidth. However, if the device is emplaced in a pressurized box connected to ambient by a sonic orifice as is suggested for aircraft operation of fluidic devices by McDonnell-Douglas, then density variations will be greatly minimized. This has an additional benefit of isolating the amplifiers from ambient noise effects which cannot propagate across the sonic orifice.

Vibration has been demonstrated to have no effect on the dc operation of fluidic devices. Frequency signals induced in the common mode also have little or no effect on the frequency content of the differential outputs. However, due to the low pass filters on the audio amplifier unused controls, vibrations in the transmission line will be transmitted if they are in the band-pass.

The most serious environmental problem is contamination. Particulate matter will eventually clog the LPA's. Based on accelerated time testing reported in the literature (see Drzewiecki for a comprehensive listing), the mean time to failure, MTTF, for laminar devices operating off conventional power supplies will be in the area of 50,000 hours of continuous duty. This is almost 6 years. Since any vehicle operates only intermittently, say one-third of the time, conservatively, then the fluidics should be expected to operate for over 17 years. This undoubtedly approaches the useful life of most vehicles. Even armored vehicles such as the M48 tank that have seen service since the late 1940's (30 years) are periodically completely refurbished. A dust enclosure, however, is necessary to prevent blockage of the vents and also to serve as a baffle to wind currents that may temporarily saturate the amplifiers, rendering them useless.
The effects of nuclear radiation, electromagnetic interference (EMI) and electromagnetic pulses (EMP) are essentially non-existent. The fluidic circuit has only a possible sensitivity to the heat generated by some form of radiation. In most cases except perhaps at the epicenter of an explosion, these heating effects are negligible. Certainly fluidic circuits have demonstrated the capability to operate at radiation levels far in excess of those above which life ceases. Since this circuit requires a "live audience" Is is immaterial if it should fail under huge radiation doses.

Typical intercom systems are affected by EMI. Clicks are heard when electrical components are turned on, interference and buzz occurs when short-wave, micro-wave or other equipment is on. This fluidic audio system has been tested in the presence of radio waves as generated by a citizens-band radio and in the presence of numerous electronic devices which have been turned on and off. No effects could be heard whatsoever. While these elementary tests do not comprise an exhaustive set, they are indicative of the expected performance. Radio waves are not expected to affect the performance of the audio portion.

As an aside, one should note that the output of the narrow band sub-system is a dc pressure level. If it is incorporated in a control system and must interface with electronics, the pressure transducer interface may be EMI/EMP sensitive and thus require shielding.

If operation is caused to occur at a Reynolds number such that

\[ c_d \frac{N_R}{(1 + 1/\sigma)^2} > 180 \]

then the flow is not entirely stable and may be transitional. The jet becomes sensitive to specific frequencies, the band of sensitivity increasing with increasing Reynolds number. When the jet flow becomes turbulent, a hissing noise is evident, clarity and fidelity are lost, and considerable distortion occurs. Care must be taken, therefore, to ensure that the Reynolds number stays in the laminar range for the entire operating region.
7. COST AND RELIABILITY

The cost of a production version of the Fluidic Voice Communication System and Data Link (FVCSDL) may be estimated in two ways. The costs of the individual parts may be added up and added to estimates on labor, profit, overhead and so forth. Alternatively, a cost may be extrapolated from past experience on systems that include similar parts.

Typical production costs of photochemically etched metal LPA laminations are $0.25 each. Each amplifier consists of enough laminations to form the appropriate aspect ratio and laminations that form cross-coupling and venting. Normally, the venting dimensions require a height equal to or greater than the amplifier itself. However, since non-amplifier laminations do not require the same kind of precision (accuracy is proportional to etching depth), then the pieces may be thicker. As a rule one may count on a minimum of eight non-amplifier laminates per amplifier, four vent and four cross couplers, with integrated resistors, and perhaps as many as there are amplifier laminations in high aspect ratio cases.

The system uses 10 amplifiers in the audio portion and five in FM portion for a total of 15. The audio has six LPA's \( \sigma = 1.2 \) for 36 laminates and four at \( \sigma = 0.8 \) for another 16 laminates. The FM portion has one at \( \sigma = 1.2 \), three at \( \sigma = 0.6 \) and one at \( \sigma = 0.5 \) for a total of 26 laminates. The total number of HDL STD MOD 3.1.1.8 (\( b_s = 0.25 \) mm) LPA laminates is 78 for a cost of $19.50. Fifteen amplifiers with eight extra laminates each is another 120 laminations for $30.00.

The resonant cavity transfer blocks in the demodulation circuit require three piece construction, therefore add $1.50.
The individual components will have to be bonded together to prevent laminates from shifting. Diffusion bonding in a high vacuum furnace normally takes about one hour and the number of systems handled at once depends on furnace size. An hour of a technician and the furnace may cost $30 and assuming that five circuits at a time can be bonded, this reduces to $6/system.

The cost of the transmission line is about $2/meter or $10 total. Power supply lines, fittings and horns will run about $25. The pump cost $30 as previously mentioned.

System labor costs are based on time for semi-skilled personnel to assemble the parts. Mass production type facilities will allow no more than one hour and probably considerably less for assembly and a "go," "no-go," test. Typical production personnel costs are $20/hr. The following table itemizes the costs.

<table>
<thead>
<tr>
<th>Item</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laminates</td>
<td>$ 51.00</td>
</tr>
<tr>
<td>Bonding</td>
<td>6.00</td>
</tr>
<tr>
<td>Fittings and lines</td>
<td>25.00</td>
</tr>
<tr>
<td>Pump</td>
<td>30.00</td>
</tr>
<tr>
<td>Labor</td>
<td>20.00</td>
</tr>
<tr>
<td><strong>Sub total</strong></td>
<td>$142.00</td>
</tr>
<tr>
<td><strong>10% profit</strong></td>
<td>14.20</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td>$156.20</td>
</tr>
</tbody>
</table>

The costs when determined by extrapolation are based on the production costs of DC-10 thrust reverser system manufactured by AIResearch.
Corporation. This is an 11 component device composed of metal etched laminations diffusion bonded together. It sells for an estimated cost of $220. This is a figure over that estimated above on a parts basis. The "true" cost probably lies somewhere in between.

It should be noted that a lack of competition in the fluidics area in recent years has given rise to unrestrained costs. Mass production of parts by competing sources will help keep costs down so that the figure of $156.20 per system may be realistic.

Life cycle costs for the fluidics are nil. The purchase price and installation costs can be amortized over the life of the vehicle so that for a 10-year life, the cost is only $15.62/year. This cost is negligible when compared to the total price of a fighting vehicle, say $1.5 million for an XM-1 and $4-5 million for a fighter aircraft.

Reliability has already been estimated by the system MTTF. The limiting factor will most probably be the pump. Experience has shown the pump life to be several years of continuous operation in an industrial environment. This, however, is a fairly constant temperature environment. The military environment includes extremes of heat and cold. This will undoubtedly affect the life of the rubber diaphragms and may actually dictate the use of a different pump should the problem be severe. Pump replacement at one year intervals seems appropriate. This then changes the life cycle costs to $30/year over the initial purchase price. This figure is still small compared with costs of a shielded electronic system. Overall reliability therefore as measured by pump life is about 9000 hours.
8. SUMMARY

This investigation has considered the analysis of the dynamics of laminar proportional amplifiers and the application of the analysis to the design of both a broadband voice and a narrowband frequency modulation demonstration system.

Beginning with first principles, the governing equations for the flow in the channels of an LPA have been developed. As a result, a complete equivalent circuit description for moderate frequencies that depends solely on the geometry has been evolved. The equivalent circuit for a duct in its simplest form has been determined to be a tee network composed of a resistance and inductance in series with a capacitance to ground from the RL node. This is in direct contradistinction to the lumped parameter model used up to now wherein the capacitance to ground comes after the RL series branch. The present model is in better intuitive agreement (not to mention qualitative agreement) with the physics of the problem since it seems that an average pressure should be used to determine the degree of compression in the duct. A basic analysis on the jet barrier compliance is combined with the channel analyses to develop a complete fifth-order model for the input impedance of an LPA, that includes inertive effects of the clearance spaces between the jet and the control edges. The channel capacitance due to compressibility is shown to be significant for low aspect ratio operation and should not be neglected as has been done in previous analyses.

The input dynamics having been determined then allowed the modeling of the jet deflection in the LPA in the region between the controls and the outputs. A finite transport time of twice the average jet velocity has been shown to be the main cause for phase shift and gives excellent agreement with physical observations. Previous analyses used the average particle velocity and generally underestimated the
phase shift. By postulating an acoustic feedback along the sides of the jet of the pressure developed downstream before the vents due to spilled jet flow, an augmentation in gain is computed and verified. The locations of resonances, so prevalent in high aspect ratio LPA's, have been precisely determined, and the amplitudes are generally well represented. Accuracy is especially good for frequencies up to the first splitter induced resonance. Recognizing that the acoustic feedback phenomenon is the basic mode of operation in edgetone systems, it has been found that the LPA resonances line up almost exactly with the edgetone eigenfrequencies with the main difference being that in the LPA the resonant regions are merely augmented gain regions not sustained oscillations. It has been demonstrated, however, that sustained oscillations can be induced by appropriate choice of geometric configuration both analytically and experimentally. A computer based algorithm has been developed and is listed in the Appendix 1.

Based on the insight developed by the modelling and the actual ability to compute bandwidth, gain and impedances, a dual purpose system was designed and built. A broad band voice spectrum audio amplifier was designed for operation as an intercom in an Army tank. In addition a narrow band frequency modulating system to transmit digital pulses was also designed and built. As a result of both designs, the state of the art in frequency response of fluidic systems was dramatically advanced. The audio system operates to 4 kHz but does not push the capability of the size LPA used. A 10 kHz system could easily be built. Similarly, a 6.7 kHz FM carrier system was built that exceeds the state of the art by at least a factor of two. Again the capability has not been stretched. Consideration of even smaller LPA's ($b_s = 0.1$ mm) indicates the possibility—even the feasibility—of operating ultrasonically.

The fluidic components of the demonstration system will operate for the expected life of a military vehicle. The system is so designed
as to be applicable to a wide range of military vehicles to include tanks, armored personnel carriers, air cushion vehicles and fighter aircraft. The specifications are summarized below in Table II.

### Table II  Fluidic Voice Communication System and Data Link (FVCSDL) Specifications

<table>
<thead>
<tr>
<th>PARAMETER</th>
<th>VOICE SYSTEM</th>
<th>DATA LINK</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall dimensions</td>
<td>2.0 x 1.5 x 3.0 cm per channel</td>
<td>2.0 x 1.5 x 6.5 cm (demodulator)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.0 x 3.0 x 3.0 cm (oscillator)</td>
</tr>
<tr>
<td>LPA nozzle width</td>
<td>$b_s = 0.25$ mm</td>
<td></td>
</tr>
<tr>
<td>Power supply</td>
<td>4 watts at 120 VAC (50 mmHg at 2.25 LPM ± 10%)</td>
<td></td>
</tr>
<tr>
<td>Bandwidth</td>
<td>1 - 4 kHz</td>
<td>6 - 6.7 kHz</td>
</tr>
<tr>
<td>Bandwidth temperature</td>
<td>+ 400 Hz</td>
<td>N/A</td>
</tr>
<tr>
<td>variation</td>
<td>for +60°C around 20°C</td>
<td></td>
</tr>
<tr>
<td>-45°C - +80°C</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Output level</td>
<td>110 PNDB at 20°C</td>
<td>2.6 x $10^{-4}$ mmHg/Hz</td>
</tr>
<tr>
<td></td>
<td></td>
<td>at 60 db input level</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6.7 x $10^{-3}$ mmHg/Hz</td>
</tr>
<tr>
<td></td>
<td></td>
<td>at 105 db input level</td>
</tr>
<tr>
<td>Threshold</td>
<td>limited only by ambient noise</td>
<td>40 Hz at 60 db</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.5 Hz at 105 db</td>
</tr>
<tr>
<td>Output</td>
<td>Exponential horns in helmet or direct insertion headsets</td>
<td>static pressure in a volume</td>
</tr>
<tr>
<td>Input</td>
<td>Throat clamped &quot;U&quot; tube &quot;throat microphone&quot;</td>
<td>Mechanical switch or motion of tube</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>-45°C - +80°C</td>
<td></td>
</tr>
<tr>
<td>EMI/EMP sensitivity</td>
<td>None</td>
<td>None on fluidics some possible on pressure transducer if used.</td>
</tr>
<tr>
<td>Cost</td>
<td>$156.00</td>
<td></td>
</tr>
</tbody>
</table>
9. CONCLUSIONS

As a result of the successful analysis of the dynamic behavior of LPA's, two main conclusions can be made:

1. Fluidic systems can operate over bandwidths in excess of 10 kHz with standard size components.

2. Fluidic systems can operate well into the ultrasonic range when nozzle widths are about 0.1 mm.

The implications of operating at ultrasonic frequencies are interesting, however. Note that the definition of high frequencies in fluidics differs by a factor of $10^6$ from that in electronics. This is the ratio of the speed of electromagnetic propagation to that of sound. This implies then that 1 Hz operation in air is akin to 1 megahertz operation electronically and 10 kHz fluidic is like 10 gigahertz electronically. In electronics, various three-dimensional effects (skin effects) occur at the elevated frequencies, similarly in fluidics when the wavelengths approach the device dimensions lumped approximations fail. In addition, the viscous signal losses are tremendous at ultrasonic frequencies. For example, a 30 kHz signal is attenuated at a rate of 10 db/meter in a 1 cm ID tube. This means that signals cannot be transmitted far without use of relay amplifiers. A signal loss of 100 db may be tolerated from a source at 150 db but what are the physiological implications and effects of sustained exposure to ultrasonic sound at high amplitudes.

Certainly one can conclude that high frequency operation in a densely packed integrated circuit will allow an increase in the computational capability of fluidics, especially on the speed of computation.

One other conclusion, which is perhaps more far reaching, is that the LPA may be considered as a pressure transducer of extremely good...
resolution with wide bandwidth. A typical dynamic range for an LPA gainblock of a gain of $10^3$ operating at a first stage supply of 10 mmHg is $10^5$. This indicates that if the maximum output differential is of the order of the supply, then the input threshold is of the order of $10^{-7}$ mmHg ($2 \times 10^{-9}$ psi) for an output signal of $10^{-4}$ mmHg. Now consider the measurement of pressure differentials of the order of just $10^{-5}$ mmHg. If an electronic transducer is used, a large diaphragm device must be used. Typically, an electronic manometer (Barocel) transducer may be used; however, the bandwidth is limited to about 20 Hz so that if dc is desired to say 5 kHz, an electronic transducer cannot do the job. A microphone will not go to dc. However, if the signal is fluercally preamplified without loss of bandwidth, then a low cost, pressure sensitive transistor can easily transduce the 0.01 mmHg LPA output, with the result of a hybrid pressure transducer...a fluercic pressure preamplifier and an electronic interface. This then allows a host of low pressure output sensors to be utilized where before their use was impractical.

This program has provided design algorithms for the practical utilization of standard LPA's and for the customization of LPA design to a particular application. The broadband amplifier concept is one such outcome of this program. The ability to \textit{a priori} predict the frequency response of LPA's will allow the shaping of desired frequency characteristics to meet specifications. Indeed, the ability to produce a specified shape frequency response may in the future obviate the need for passive circuitry. Resonant circuits may be replaced by edgetone augmented amplifiers, thus considerably simplifying circuit construction by eliminating the need for separate volumes and resistors.

The design algorithm also has specified the Input Impedance of LPA's so that rational design can be used for complex computation.
circuits. While LPA input impedance was not directly measured and the fifth order model was not directly verified, its validity has been established indirectly from the good agreement of the complete LPA response model with experimental data.
10. RECOMMENDATIONS

This program has pointed out several areas of possible additional fundamental research and several areas of developmental interest. Perhaps the area of greatest fundamental interest is the relationship between the onset of edgetone oscillations and turbulence. This phenomenon appears to involve such areas as the hydrodynamic stability of jets and confined flows. The present research has been on a macroscopic level and efforts should be tied to some microscopic level evaluation of the actual velocities and spatial distributions of energy.

Another area of fundamental interest is the examination of the transition of flows from the acoustic to the fluidic region. Clearly LPA's can operate at large signal levels as well as small. What is the relationship between the highly nonlinear step response observed and the large signal sinusoidal response? How do induced secondary flows interact with the large deflections of an oscillating jet?

Yet another possible area for basic research is the solution of the flow between a solid wall and a jet boundary as found in the control-jet edge interaction. While a plausible engineering analysis has been made, certain assumptions do not hold at low and negative biases. The reverse or counterflow condition accounts for the physical explanation of digital amplifiers, yet the actual values of impedance have analytically eluded researchers.

An area for future development is certainly the high volume public address systems as originally desired for aircraft carrier flight deck operation. The development of acoustic summing to provide high volume output (140 db) should be reexamined.
The area of compensation circuit techniques using active devices should receive attention.

The development and refinement of the present algorithm to include interactive circuit analysis should be pursued. This will allow closer examination of system stability and aid in the design of pressure controlled oscillators. These devices are useful as pressure-to-frequency transducers. The output pressure of a fluidic sensor or preamplifier becomes the supply pressure of an oscillator which gives out a frequency related to the supply pressure. By appropriate choice of feedback circuitry, the relationship may be made linear or as in the case shown here. If the feedback is allowed to be purely acoustic, then the frequency is related to the square root of pressure. Low cost pressure transducers can easily read the pressure frequency and the signal can be directly used with digital microprocessors.

The use of high frequency fluidic amplifiers is limited only by the imagination. It is hoped that this present work will stimulate the development of new systems. Plans are already in the works for developing generalized circuit analysis programs for the LPA so that it can be used as a standard circuit element just like a resistor and an op amp or a capacitor, based on the above recommendations.
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APPENDIX I  COMPUTER PROGRAM FOR THE DYNAMIC RESPONSE OF AN LPA AND
AN EXAMPLE PROBLEM.

***** FILE: FOR. 1 PRGM HANDBOY. ****

TO MAKE A COPY, Y.E.E.T.

C THIS PROGRAM WILL COMPUTE THE FREQUENCY RESPONSE OF A FLUIDIC
C LAMINAR PROPORTIONAL AMPLIFIER (LPA) FROM THE GEOMETRY ALONE.
C
C IN ORDER TO COMPILE AND RUN THIS PROGRAM THE ELECTRONICS TERMINAL
C PLATING LAYOUT MUST BE ATTACHED. THE FOLLOWING STATEMENT
C MUST BE MADE AT THE BEGINNING OF EACH DAY:
C
C FTRKGL DYN3 LMT('SYSTEXTCS.LOAD' 'SYSTERCAS.LOAD')
C
C THEREFORE REFER TO THE DAY USED ONLY "CALL SYMT" TO RUN.
C
C ALL INPUT SHOULD BE IN THE FREE FLOATING POINT FORMAT AS BELOW:
C
C INPUT THROAT WIDTH,ET, NOZZLE LENGTH, Lb
C
C 1.25 1.0
C
C ANSWER ALL QUESTIONS AS INDICATED.
C
C SET ASIDE SPACE FOR VARIABLES TO COMPUTE DISCHARGE COEFFICIENT
C
DIMENSION C(25), F(25)
C
C SET ASIDE SPACE FOR VARIABLES TO BE PLOTTED
C
DIMENSION F(300), X(300), PHS(300)
C
C DEFINE ALL COMPLEX VARIABLES
C
COMPLEX S(1,2, ZV,ZC,X, ZJ, ZP, ZF, ZG, ZL, ZL, ZK)

1000 WRITE(6,2000)
2000 FORMAT('***************O N K Y N O ***************')
 WRITE(6,2001)
2001 FORMAT('THIS PROGRAM WILL COMPUTE THE FREQUENCY RESPONSE OF AN LPA')
 WRITE(6,2002)
2002 FORMAT('LPA GIVEN ITS GEOMETRY AND OPERATING POINT')
 WRITE(6,999)
999 FORMAT('IF THIS IS AN HOD STD MOD 3.1.1.8 LP'; ENTER 1')
 READ(5,999) IN
 IF (IN.EQ.1) GO TO 598
 WRITE(6,1000)
1000 FORMAT('IMPU: THROAT WIDTH, ET, NOZZLE LENGTH, Lb')
 READ(5,1001) ET, X
 WRITE(6,1002)
1001 FORMAT('IMP: CONTROL LNCHT,XC,AVG, XTH, XCAM, XH, WTH, EC')
 READ(5,1001) XC, XCA, XCA, XCH
 WRITE(6,1002)
1002 FORMAT('IMP: SPLITTER LNCHT, XSPL, WTH, MSP, INPUT WIDTH, GC')
 READ(5,1002) XS, YS, ST, RE
 WRITE(6,1003)
1003 FORMAT('IMP: ENTRAIN MT RADIUS, EC, EC, PRESSURE, RB')
 READ(5,1003) RC, VB
 WRITE(6,1004)
1004 FORMAT('')
1064 FORMAT(10) INPUT REYNOLDS NO., Aspect Ratio, Sigma, Nozzle Width, 
            1, 3.14159
            READ(5,9) X1, X2
            WRITE(6,10)

1065 FORMAT(10) CONTROL WIDTH, NO., SPLITTER DIST., XSP
            READ(5,9) X1, X2
            WRITE(6,10)

506 FORMAT(10) INPUT LENGTHS OF VENTS, XLVI, XLVII
            READ(5,9) X1, X2
            WRITE(6,10)

601 FORMAT(10) YAV/AVE, DIST, XLVI, OUTPUT LENGTH, XPL, AVG. WIDTH, ETA
            READ(5,9) X1, X2
            WRITE(6,10)

999 CONTINUE
            WRITE(6,10)

822 FORMAT(10) INPUT NUMBER OF STACKS
            READ(5,9) NSTACK
            WRITE(6,10)

804 FORMAT(10) IF YOU WANT TABULATION OF EACH POINT SET PRINT=1
            WRITE(6,10)

805 FORMAT(10) PRINT
            READ(5,9) PRINT
            WRITE(6,10)

906 FORMAT(10) IF YOU WANT BLOCKED RESPONSE SET AA=1
            WRITE(6,10)

807 FORMAT(10) INPUT AA
            READ(5,9) AA

C
C THIS IS THE MUL STD MOD 3, 1, 1, 8 GEOMETRY
C
ST=1.25
X1=1.0
X2=10.0
X1R=2.75
X2L=1.0
XPL=1.75
SS=0.0
SL=1.5
RE=2.25
PB=0.0
LE=1.0
XSP=4.0
XLVI=5.0
XPI=15.0
R0=1.25
XLVI=1.0
XLVII=4.75

C
C ENTER VALUES OF REYNOLDS NO., ASPECT RATIO AND SIZE
C
WRITE(6,110)

810 FORMAT(10) INPUT ENTR, SIGMA, NOZZLE WIDTH AS IN MN
            READ(5,9) ENTR, SIGMA, 38

997 CONTINUE
C
C COMPUTE THE MODIFIED REYNOLDS NUMBER
C
ENRMD=ENR/(XH+1.0)/(1.0/SIGMA)**2
C
C COMPUTE DISCHARGE COEFFICIENT BY REGULA FALSI ON THE IMPLICIT
A = (S1*S2 + S1 + S2 + 1) \times S1
A = A + 1
IF(Y.L.T. 1/2) GO TO 1040
GO TO 1
GO TO 1030
CONTINUE
C
C. compute channel resistance correction and coefficients
C
IF(SC.RA/<SIGMA.GT.2.5) GO TO 690
AK2 = 0.16
GO TO 790
690
T4 = 24.2*642*(SIGMA/SC.RA*23.15/SIGMA*AK2)/115.7*22.5*SIGMA
LENK
TS = 0.45**(1/0.85)**2
CHM = 1.533*2.5
IF(GO.GT.4.9) GO TO 770
END=2.1065
GO TO 790
770
END=1.
790
CONTINUE
C
C. compute displacement thickness, DO
C
C. effective nozzle length, x
C
C. virtual origin, av
C
DO = 11.5*SIGMA/2.5 + 16.9*SIGMA/(1.5*S1) + (1.5*SIGMA)**2/4. -(1.5*SIGMA)**2/4.
x = ENR/C1/(C1.5/X) + 25/25*EN
X0 = x + 1.4/2 + 2.6**2 - 1.
x = 0.4596/0.0048
C
C. choose boundary layer coefficients for plate losses for low
C. aspect ratios and high aspect ratios
C
IF(SIGMA.LT.1.) GO TO 626
EN5 = 46
EN6 = 6
GO TO 830
626
EN5 = 26
EN6 = 3
830
CONTINUE
C
C. compute plate loss coefficient, CO
C
IF(XD.GT.1.) GO TO 850
CC = (1.2 + X)/XVG**(3.2/3.)
GO TO 900
850
IF(XD.LT.0) GO TO 890
IF(CD.GT.3) GO TO 850
GO = (1.5 + CD - 2.0)/XVG**(-3.2/3.)
GO TO 790
890
GO = (1.5 + CD - 2.0)/XVG**(3.2/3.)
1/SIGMA/1.5 = 0.4596/RT(X/VK)/SIGMA
870
CONTINUE
GO TO 860
C COMPUTE THE BLOCKED PRESSURE_RECOVERY, PR

PC = PR

3C = 0.5*(T4+T5)/TF + 5RT + 252((T4+T5)/15) + 2*([RR + RV] + [RE - RCS])

1475

C = T4 + T5 + CC

PC = (PC + CC / (1.0 - RCS))/HC + RV / (AC + 5)

GL = [PC + 5 * CC] / (AC + CC)

C COMPUTE THE OUTPUT CHARACTERISTIC AND INPUT CHARACTERISTIC

30L = [CC + UT + CC] / (SIGMA / (AC + CC) + 30R / (SIGMA + A2)) / (50L + C1 + CC)

40K = 41 * CC / 20**2

40L = 0.

40T = 0.

40B = 0.

40T = 0.

134 C14 = (1.0 - 2.0 * CC) / (SIGMA + A2) + 2 * CC + 25 * SIGMA / (CC + 25)

1144 R = PC*(1.0 + 2.0 * CC) / (SIGMA / (AC + CC) + 25 * SIGMA + 25 + (CC + 25))

1100 B = CC + (1.0 - 2.0 * CC) / (SIGMA / (AC + CC) + 25 * SIGMA + 25 + (CC + 25))
GO TO 1410

1410 ALGORITHM 4.2

1411 CONTINUE

1420 COMPUTE JETS' EJECT PRESSURE, PJ; JETS' PRESSURE RESISTANCE, RK

C

PJ = (PC + 1) - GC/CSV) + GC*PK/(RCSS + RV)
RK = 2.0*G5TA+CC3/((CC+2.033)^2+35RT(PJ))
10 = 3.0*G5TA/(14.0CC+2.066)2)

C
COMPUTE THE IMPEDANCES:

C
CONTROL, LLC
C
JETS' PRESSURE, FLK
C
JETS' EDGE SPACE, CLV
C
UPSTREAM VENT, ELV1
C
DOWNSTREAM VENT, ELV2
C
OUTPUT, ELO
C

LLO = 2.0*CC3+CC4/4CC6
ELK = 4.0*CC2+CC5/(CC+2.033)^2*PJ
ELV = 2.0*CC2+CC4/(CC+2.033)^2
ELV = 2.0*CC2+CC4/(CC+2.033)^2
ELV = 2.0*CC2+CC4/(CC+2.033)^2

C
COMPUTE THE Parasitic CAPACITANCE, CR, AND JETS' COMPLIANCE, CJ

C
CP = 3.0CC2+CC3+CC4/100.0/3.0376.0
CJ = (CC+2.033)^2/17.62*CC+CC)
C
COMPUTE THE RESISTANCES:

C
CONTROL, RC
C
UPSTREAM VENT, EV1
C
DOWNSTREAM VENT, EV2
C
OUTPUT, RO
C

EV1 = X1 - (C + V)
EV2 = X2+XSP+XPL - KV
RC = RCSS
RV = 2.0*XR1 + (SIGMA + EV1 + EV1/3.0376.0)2/(RV2+2.033*RV3)
RV = 2.0*XR1 + (SIGMA + EV1 + EV1/3.0376.0)2/(RV2+2.033*RV3)
RD = R2UTSE
WRITE (4, 42)
954 FORMAT (' THE FOLLOWING ARE A FEW VALUES FOR A CHECK:"
WRITE (4, 42)
959 FORMAT (' RC RV RO RD PH) WRITE (4, 951) RC, RV, RO, RD, PH
951 FORMAT (' R = (C + V)
WRITE (4, 950)
4000 FORMAT (' EV1 EV2 PJ RK CP)
WRITE (4, 42) EV1, EV2, PJ, RK, CP
4400 FORMAT (' EV1 EV2 EV1 EV2, PJ, RK, CP
WRITE (4, 42) EV1, EV2, EV1, EV2, PJ, RK, CP
952 FORMAT (' LC LV LK LV1 LV2 LS
WRITE (4, 953) LC, LV, LK, LV1, LV2, LS
191
953 FORMAT (4F10.4)
955 FORMAT (I2) IN ORDER FOR THE PROGRAM TO CONTINUE ENTER ANY #
96=10(19) ANY

C COMPUTE PROBLEM CONSTANTS:
C TRANSPORT DELAY TO SPLITTER, T1
C TRANSPORT DELAY T. VALVE, T2
C JET DEVIATION COEFFICIENT, VJ
C NOZZLE WIDTH IN METERS, GS

C T1=5.**XSP
T2=2.**XVI
AKJ=("C+3.%)**2/(E,75625.D0)

C PROGRAM AIR KINEMATIC VISCOSITY IN ([M/S])
C
C VISC=1.41642-5

C THIS LOOP COMPUTE THE GAIN AND PHASE SHIFT OF THE LPV
C TRANSFER FUNCTION AT DISCRETE VALUES OF NORMALIZED FREQUENCY, F.
C
GO TO 10 I=1,756

C INCREMENT FREQUENCY F

C F(I)=10.**(I4.01-3.)

C COMPUTE NORMALIZED RATION FREQUENCY, W AND LAPLACE OPERATOR, S.
C
W=2.**X3.1+158*F(I)
4=CHPLX(W,1)

C COMPUTE THE COMPLEX ATTENUATING FACTOR, ZE9
C
ZE9=10.**(1-2.767E-5*PI/COS*VISC*ENR*F(I)**XSP/DSIGMA))

C COMPUTE THE COMPLEX IMPEDANCES:
C UPSTREAM VENT, ZV1
C DOWNSTREAM VENT, ZV2
C JET EDGE, ZV
C JET BARRIER, ZJ
C BIAS PRESSURE, 7X
C CONTROL, ZC
C LOAD, ZL
C
ZV1=SV1+S**2 LV1
ZV2=SV2+S**2 LV2
ZV=SV+S**2 LV
ZJ=1.1/(4CPI)+.0*G+C**2/SC**2
ZC=2K+LC**2
ZL=K+LC**2
ZC=K+LC**2
Z7=1./ZV+1./ZC+1./ZJ+1./RC1
7P=1./ZV+1./ZL+Z.C+Z.LC)
ZL1=ZV*2/10E**-1./Z*SC**2LC)
IF (AA #0.35) GO TO 34
ZL=K+2P

GO TO 35

192
C \align{34} \text{CL} = \text{COMPLEX}(10000000, 10000000) \\
\align{38} \text{CONTINUE}

C \text{ADJUST VENT IMPEDANCE BY ACOUSTIC ATTENUATION FACTOR}

\text{ZV}2 = \text{ZV}2 \times \text{RE}
\text{ZV}1 = \text{ZV}1 \times \text{RE}

C \text{COMPUTE COMPLEX TRANSFER FUNCTION VALUE, T}

\text{TK1} = \text{AK1} \times \text{XP}(-1) \times (2 \times \text{XP}(\text{LC} \times \text{CL} - \text{RE}) - 1) / ((1 + \text{AK1} \times \text{EXP}
\text{TK2} = \text{PI} \times \text{TV1} / (\text{SL} + \text{PI} - \text{RE}) - 1) \times \text{ALL} \times \text{ZV2}
\text{TK3} = 4 \times \text{PI} \times \text{TV2}
\text{TK4} = \text{TK2} \times \text{TK3} / (\text{SL} + \text{TK2} \times \text{TV2}) \times \text{INT}

C \text{COMPUTE MAGNITUDE OF TRANSFER FUNCTION T, AR}

\text{AN}1 = \text{CABS}(\text{CABS}(\text{I}))
\text{AN1} = \text{CABS}(\text{I})

C \text{COMPUTE PHASE SHIFT AS ARCTAN(\text{I}/\text{REAL})}

\text{TR} = \text{REAL}(\text{I})
\text{TI} = \text{REAL}(\text{I})
\text{PH} = \text{ATAN2}(\text{TI}, \text{TR})
\text{PHS} = \text{PHASE}(\text{I}, \text{ZL}, \text{PH})
\text{PHS}(\text{I}) = \text{PHS}
\text{IF} (\text{PRINT} = 2, 1, 00) \text{GO TO} 27
\text{GO TO} 10

C \text{PRINT VARIABLES OF INTEREST IF DESIRED}

27 \text{WRITE}(6, *) \text{F(1), AN(1), PHASE, M1}
16 \text{CONTINUE}

C \text{CALL PLOT IC ROUTINE AND PLOT OF AMPLITUDE RATIO AND PHASE}
C \text{SHIFT VERSUS FREQUENCY ON A SEMILOG GRID.}

\text{CALL} \text{LOGC} \text{F,1,AR,0,250,1, \text{NORMALIZED FREQUENCY,F,22,}
\text{1GAIN, ON,18, \text{FREQUENCY RESPONSE OF AN LPA,26,2,IER})}
\text{CALL} \text{LOGC} \text{F,1,PHS,0,250,1, \text{NORMALIZED FREQUENCY,F,22,}
\text{1IPASE SHIFT, DEGREES,19, \text{FREQUENCY RESPONSE OF AN LPA,26,2,IER})}
\text{PRINT} = \text{PRINT} + \text{1}

3000 \text{FORMAT(*) IF YOU WANT TO DO ANOTHER CASE ENTER 1,(*)}
\text{READ(*) AGAIN}
\text{IF} (\text{AGAIN} = 32, 1, 4) \text{GO TO} 1999

C \text{END OF PROGRAM}

\text{STOP}

\text{END}
IF YOU WANT TO DO ANOTHER CASE ENTER 1.0

1.

*****************************************************************************
THIS PROGRAM WILL COMPUTE THE FREQUENCY RESPONSE OF AN
LPA GIVEN ITS GEOMETRY AND OPERATING POINT
IF THIS IS AN HDL STD MOD 3.1.1.8 LPA ENTER 1

1

INPUT NUMBER OF STAGES

1

IF YOU WANT TABULATION OF EACH POINT SET PRINT=1.
PRINT=

1

IF YOU WANT BLOCKED RESPONSE SET AA=1.0
INPUT AA=

0

INPUT EH, SIGMA, NOZZLE WIDTH BS IN MM

330.0 3.0 0.5

THE FOLLOWING ARE A FEW VALUES FOR A CHECK

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<thead>
<tr>
<th>RC</th>
<th>RU</th>
<th>RD</th>
<th>RO</th>
<th>PR</th>
</tr>
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<td>1.8995</td>
<td>0.1203</td>
<td>0.2698</td>
<td>0.3591</td>
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<td>RU1</td>
<td>RU2</td>
<td>PJ</td>
<td>RK</td>
<td>CP</td>
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<td>0.0031</td>
<td>0.0023</td>
<td>0.2792</td>
<td>0.5329</td>
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<td>LC</td>
<td>LU</td>
<td>LK</td>
<td>LU1</td>
<td>LU2</td>
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<td>3.5626</td>
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<td>2.0170</td>
<td>0.2613</td>
<td>0.1959</td>
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</table>

IN ORDER FOR THE PROGRAM TO CONTINUE ENTER ANY NO.
Table A-1. Computer printout of the frequency response of the LPA in figure 42.

<table>
<thead>
<tr>
<th>F</th>
<th>G_p (db)</th>
<th>PHASE (degrees)</th>
<th>G_p (ratio)</th>
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</thead>
<tbody>
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<td>14 5372063</td>
<td>-42 2659689</td>
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<td>0.52489496E-02</td>
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<td>3.1839461</td>
</tr>
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<tr>
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<tr>
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</table>

195
Figure A-1. Frequency response plot from Table A-1.
APPENDIX II. The Experimental Method

The data collected on characteristics for the verification of the analysis presented in sections 2, 3 and 4 was comprised of:

1. Measurements of mean jet edge pressure.
2. Bode plots or pressure gain and phase shift versus frequency.
3. Static transfer characteristics.
4. Output pressure noise spectral analysis.
5. Carrier oscillator output frequency versus supply pressure.
6. Rectifier static transfer characteristic.
7. Demodulator analog output level versus frequency.
8. Demodulator transient response.

This appendix will specify the experimental techniques and apparatus used for each test and in the case of the LPA Bode plots will compare the numerous results with the computer model.

A.1 Measurement of Mean Jet Edge Pressure

The static pressure at the end of the control channel is to be measured as close to the jet edge as possible. To this end a 0.4 mm static tap was drilled in the cover plate of an LPA with 51 = 0.5 mm in the location already shown in figure 27. A low 10 Hz bandpass electronic manometer, tradename BAROCEL, was connected by a tank and plastic tubing to the tap. In this manner the frequency component (ripple) will be filtered out and the mean level only can easily be observed. A buffer amplifier of the same aspect ratio was used to drive the test amplifier so that operation was self-staged. The buffer amplifier was driven by an acoustic driver. The amplitude of the input signal was maintained at a constant level of 80 db by a General Radio Company 1569 Automatic Level Regulator tied to a 1/4 in (6.35 mm) B & K microphone placed at the fitting to the test LPA. Three different aspect ratio LPA's were tested 51 = 0.5, 51 = 1.0, 51 = 2.0. Figure A1 shows the test arrangement schematically. The test data has already been presented in figure 28.
Figure A1. Schematic of the test apparatus for determining the mean jet edge pressure in an LPA.
A2. Measurement of LPA Frequency Response (Bode Plots)

The measurement of the LPA transfer function (gain) as a function of applied frequency is of the greatest importance to this research and development program. It is critically important that the measurement means not affect the LPA performance and that the data is truly representative of the LPA.

One means of estimating the LPA frequency response is called an insertion gain measurement which is described in detail by Toda et al. (Toda, K. Roffman, G., and Talkin, A., "The Matched Acoustic Generator," J. Dyn. Syst. Meas. and Control, March 1972). This gives a measure of the insertion gain of an LPA loaded into an infinite line. This, however, is not sufficient data for staged operation. It is necessary to avoid reflections and this is afforded by the infinite line.

If one were to measure the pressures directly at the port locations in a configuration where the distances between any two adjacent nodes is less than a wavelength, then reflections and standing waves should not develop. In addition, a meaningful gain measurement is desired of the LPA under loaded conditions on both the controls and outputs. Furthermore, it is desired to produce a truly differential (push-pull) control signal. To this end it was decided that mounting matched microphones flush in the control and output ports of an LPA driven by a buffer LPA and driving a load LPA would allow the measurement of self-staged gain. The microphone is not a differential device, so that the signals measured are one half the differential signal, but since gain is the ratio of output to output, this factor is common and cancels out resulting in a true gain measurement. (Note that when a single side acoustic input is measured, this is the whole input (since $P_2 = 0$) but the output is push-pull, hence, only half the output is measured and the ratio of the microphone signals is 6 db down (a factor of two)
from the true gain. (This was the case with the measurement of the Corning gain block.)

Figure A2 shows schematically the microphone emplacement and the buffer and load LPA arrangement. Figure A3 shows the complete apparatus schematically.

Figures A4 - A12 are Bode plots taken in this manner. The xy recorder plots give the data points. In some cases a Hewlett Packard 3575A Gain-Phase meter was used for point by point measurement when the BAFCO was down. Notice that blocked output response is obtained by placing a metal rod in the output manifold so that it is flush with the plane of the lower bounding plate of the test LPA. Each data set has the corresponding theoretical prediction plotted with it. Agreement on the whole is satisfactory.

Care must be exercised in not allowing standing waves to occur anywhere in the test arrangement. When the supply line to the LPA's was long, about 25 cm, an anomalous Bode plot could be generated with a resonance augmenting the F = .01 peak as shown in figure A13. This frequency, f \sim 300 Hz is very close to the quarter wavelength of the tubes (f = 330 Hz). Perhaps standing waves are generated in the supply so that the supply pressure may appear to increase at that frequency. This effect can be eliminated by using short tubing or manifolding to break up any standing waves. It is interesting to note, however, how the gain of an LPA may be shaped by external circuitry. This is an area of current interest. It may be useful or detrimental.
Figure A3. Schematic layout of the test apparatus for the dynamic testing of LPAs.
Figure A4. Bode plot of self-staged gain for an HDL STD LPA, \( \sigma = 0.5 \).

\( b_s = 0.5 \text{ mm} \)
Figure A5. Bode plot of self-staged gain of HDL STD LPA, $\sigma=1.0, b_s=0.5$ mm.
Figure A6. Bode plot of HDL STD LPA self-staged gain and phase, $\sigma = 2.0$. 
Figure A7. Bode plot of gain and phase for HDL STD LPA, $\sigma = 3.0$. 

HDL STD LPA 3.1.1.8

$P = 0.65$ mm Hg

$\beta' = 0.50$ mm

$\sigma = 3.0$
Figure A8. Bode plot of self-staged gain for HDL STD LPA, $\sigma = 4.0$. 

HDL STD LPA

$P = 0.457$ mm Hg

$\alpha = 0.50$ mm

$\sigma = 4.0$
Figure A9. Bode plot of self-staged gain for a microminiature LPA of standard format, $b_s = 0.1 \text{ mm}$, $\sigma = 1.0$. 

HDL STD LPA 3.1.1.8

- $b_s = 0.1 \text{ mm}$ (1/8 in microphones)
- $\sigma = 1.0$
Figure A10. Bode plot of the blocked gain of an HDL STD LPA, $\sigma = 3.0$, low Reynolds number.
Figure A11. Bode plot of the blocked gain of an HDL STD LPA, $c = 3.0$, and moderate Reynolds number.
Figure A12. Bode plot of blocked gain of an HDL STD LPA, $\sigma = 3.0$, for high Reynolds number.

HDL STD LPA

$P_s = 0.84$ mm Hg

$b_s = 0.5$ mm

$\sigma = 3.0$

$N'_R = 129$
Figure A13. Bode plot affected by resonances in supply lines of 25cm length.
A.3. Static Transfer Characteristic

This test is conducted under the same input loading conditions as the dynamic tests. A buffer amplifier is used to drive the test amplifier. Differential control and blocked output pressures are measured with Barocel Electronic Manometer pressure transducers. The setup is shown in figure A14. Test data was shown in figure 70.

A.4. Output Pressure-Noise Spectral Analysis

To determine such quantities as dynamic range and transition-to-turbulence, the output noise level spectrum is required. An LPA is block loaded (worst case with maximum adverse pressure gradient) by a flush mounted microphone and the noise spectrum is examined on a Hewlett Packard 3580 A spectrum analyser.

The procedure results in a conservative measurement since differential noise is not measured. It is expected that differential noise is at least an order of magnitude lower than the single sided noise measured by the microphone. This is because if there is any isotropy or homogeneity to the disturbances, they will tend to make themselves felt equally on both outputs so that differential signals are small. With the development of ultrasensitive pressure sensitive transistors, a differential measurement may one day be possible. Currently, these sensors are proprietary laboratory curiosities. The use of PVF2 (polyvinylate difluoride) sheet may allow a differential measurement; however, noise and impedance mismatches do not yield the present threshold of microphones.

The procedure is generally to obtain a spectrum with the LPA turned off and then with it turned on. If the traces are identical as in figure A15a and b, then the LPA is considered to be operating laminar. If noise appears, then the output level increases over the laminar operation as already discussed (see section 2, figure 52). This is shown in the analyser trace of figure A15c.
Figure A4. Schematic drawing of the test apparatus for in-stage d.c. hane measurement.
Figure A15. Spectrum analyser traces of the noise in an LPA.

(a) Spectrum of Room Noise, Electronic Noise Jet Off

(b) Spectrum of Room Noise, Electronic Noise Plus Laminar Jet

(c) Spectrum of Room Noise Electronic Noise, Laminar Jet and Superimposed Turbulent Jet

Total Frequency Range ≥ 5000 Hz
Turbulent/Laminar Noise Ratio for f < 100 Hz ≥ 70 db
Using this technique, the empirical guide for transition used in section 3 was established. If \( c_d N_R / (1 + 1/\sigma)^2 < 180 \), the flow will be laminar.

A.5. Carrier Oscillator Frequency Versus Supply Pressure

The oscillator was connected to a supply of air. A tee in the large diameter line (3.175 mm compared with the 0.25 mm nozzle width) measures the stagnation supply pressure. A microphone is "teed" into the output line so that the microphone cavity is negligible (for high resonant frequency) as shown in figure A16. The amplified microphone output is connected to an H/P 5512A electronic counter that displays the frequency. Figure A17 shows a schematic of the test arrangement.

A.6. Rectifier Static Transfer Characteristic

This test was conducted in an identical manner to the LPA static transfer characteristic test with the exception that the rectifier is a single output device so that the Barocel used on the output had one port grounded to atmosphere.

A.7. Demodulator Analog Output Level Versus Frequency

This test was conducted in a similar fashion to the oscillator frequency/output test. The output pressure level is measured in a 12 cc tank with a Barocel transducer. The input frequency is measured with a B/K 1/4 in. microphone in a "tee" as in figure A16 at the input to the block. The schematic is shown in figure A18.

A.8. Demodulator Transient and Frequency Response

A Barocel has a frequency response of about 10 Hz. Since the output transient response is expected to be less than this (3 Hz),
Figure A16. Exploded view of the microphone holder "tee" with small parasitic volume for high frequency response. (Volume Helmholtz frequency is 24.5 kHz).
Figure A17. Schematic drawing of the test apparatus for measuring LPA oscillator output frequency as a function of supply pressure.
Figure A18. Schematic of the test apparatus used in obtaining the frequency demodulator characteristics.
then a Barocel transducer closely coupled to the output (the line volume is much less than the output volume) will not affect operation. A 10 cm, 3.175 mm line has a volume of 0.74 cc compared to the 12 cc of the tank.

The oscillator output is connected to the demodulator input by a 10 m, 12 mm diameter copper line. The oscillator step output is generated by quickly blocking the offside output. This can be achieved in less than 0.05 seconds. The output changes 380 Hz. This then produces a demodulator output shown in figure 89a. The test arrangement is shown in figure A19.

The frequency response is approximated by repeating the transient response test but repeatedly blocking and unblocking the oscillator output at an increasing rapid rate. The results were shown in figure 89b.
Figure A19. Schematic drawing of the test arrangement for measuring the transient and frequency response of the narrow band data link system.
A3. US PATENT DISCLOSURE, "FLUERIC BROAD BAND AMPLIFIER".
A broad band fluidic amplifier is disclosed which comprises means to increase the deflection of the fluid jet within the amplifier at higher frequencies of oscillation of the jet. The means for increasing jet deflection comprises vanes or protrusions positioned closely adjacent the jet path at selected distances from the nozzle. Acoustic feedback from these vanes or protrusions will assist the control pulse in deflecting the jet at selected frequencies of oscillation.

The invention described herein may be manufactured, used and licensed by or for the United States Government for governmental purposes without the payment to me of any royalty thereon.

Typically, the bandwidth of AC fluidic or fluidic amplifiers has been limited by the dynamic response of the input impedance. This impedance is such that the input control signal is generally attenuated significantly at higher frequencies. Often, the bandwidth of available devices is insufficient for many purposes. Particularly, the increasing use of fluidic amplifiers for FM and speech processing requires a wider band of operating frequencies.

Accordingly, it is an object of the invention to overcome the deficiencies of the prior art devices noted above.
Specifically, it is an object of the invention to provide a fluidic or fluidic amplifier having a significantly increased bandwidth.

It is an object of the invention to provide a fluidic amplifier which will operate at a broad range of frequencies yet be simple in structure, having no moving parts.

SUMMARY OF THE INVENTION

Fluidic amplifiers such as the laminar proportional amplifier (LPA) are generally designed with a low aspect ratio (height/width ratio) to get wide bandwidth. This invention makes use of observed performance of high aspect ratio devices, having an aspect ratio greater than two. By placing multiple protrusions in an LPA amplifier, multiple peaks in gain can be achieved. Pressure feedback from the protrusions provides an amplification of jet deflection. This is the result of a phenomenon not unlike edgetones except that there is no instability present. This results in a device which has an order of magnitude wider bandwidth. Data shows that a device normally having a bandwidth of 300 Hz can exhibit a bandwidth of 3,000 Hz when this feedback is provided.

Several of the amplifiers of the invention can be operated in parallel, the peaks in gain of one amplifier being shifted in relation to the peaks in gain of another amplifier. The result will be an output which is smoother, having increased gain across a broad continuum of frequencies.

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 illustrates an exemplary embodiment of the amplifier of the present invention.

Figure 2 graphically illustrates the relationship between frequency of oscillation and the effective control energy applied to an oscillating jet in a laminar proportional amplifier.
Figure 3 shows the relationship between frequency of oscillation and gain in the amplifier of the present invention.

Figure 4 illustrates an embodiment of the invention comprising two modified amplifiers operating in parallel.

Figure 5 graphically illustrates the gains of the respective amplifiers of figure 4 as they relate to frequency, and the effective gain of the composite system shown in figure 4.

DESCRIPTION OF THE PREFERRED EMBODIMENT

Referring to figure 1, there is shown an amplifier comprising the essential features of the present invention. Supply 3 comprises a pressurized source of fluid which directs a jet out of nozzle 4. Control inputs 6 and 8 direct control pressure pulses through outlets 10 and 12, respectively. Vents 14 and 16 are maintained at constant pressure in the usual and well known manner for such devices. Either or both of outlets 18 and 20 will receive the fluid of the jet depending upon the position of the jet resulting from deflection by pressure pulses through outlets 10 or 12.

Vanes 1 and 2 are placed within the vent region between nozzle 4 and splitter S which separates outputs 18 and 20. The vanes extend to a position closely adjacent the path of the jet. The outer-most edge of each vane should extend to a position which is at a distance from the edge of the undeflected jet which does not exceed one-half the width of nozzle 4. The deflected jet should just touch the vane when the output of the amplifier is fully saturated.

In operation, fluid from supply 3 exits as a jet through nozzle 4 toward splitter S. Control pressures through inputs 6 and 8 generate control pulses at ports 10 and 12, respectively. These control pulses act to deflect the jet toward either output 18 or output 20. As the control pulses at ports
and "21re...}

As the jet passes closely adjacent the edge of one of the vanes 1 or 2
acoustic energy will be generated and fed back toward the nozzle 4. This will
also occur as the jet passes closely adjacent the splitter S. This acoustic
energy will provide a pressure on the side of the jet adjacent to the protrusion
or vane. This pressure, along with the pressure pulses from ports 10 and 12,
will act on the jet to determine the deflection thereof. If the acoustic
feedback pulse and the control pulse from the port 10 or 12 are exactly in
phase with one another, the two will combine to significantly increase the
deflection of the jet. However, since there is a finite transport time for
the fluid of the jet from nozzle 4 to any point downstream of the nozzle the
acoustic pulse cannot be precisely in phase with the pulse from the control
port. Therefore, the two pulses will combine to increase the deflection of
the jet when they are 360° out of phase with one another, or exactly one wave-
length apart.

At low frequencies of oscillation of the control pulse the position of
the jet with respect to the outputs will always be substantially in phase
with the control pulse. For example, when a positive pulse is applied at
port 10, the jet will follow a path through output 20. As the frequency of
oscillation of the control pulse is increased, the downstream position of the
jet moves out of phase with the control pulse. As seen in figure 1, the
control pulse \( P_j \) is applied through port 10 while the downstream position
of the jet, shown by dashed lines, is at output 18. The position of the
jet at splitter S is therefore 180° out of phase with the pressure pulse \( P_j \).
Also, there is a normal phase lag between the jet position downstream
and the control signal of 180° due to the finite jet transport time between
the upstream and downstream positions. (This lag can be observed in a
stream of water exiting from the nozzle of a garden hose as the hose is rapidly
moved back and forth.) The result is that the acoustic feedback, shown by
arrow F in figure 1, generated at the splitter is 360° out of phase with the control impulse at port 10. Since the acoustic energy travels at the speed of sound, much more rapidly than does the jet, the acoustic pressure may be considered to instantly combine with the pulse from port 10 to increase the deflection of the jet.

The manner in which this phenomenon increases the operation bandwidth of the amplifier will be described with reference to figures 2 and 3. In figure 2, $P_c$ represents the control pressure which exists at input 6 or 8 of the amplifier, while $P_j$ represents the actual pressure pulse generated at the output ports 10 and 12. Since the input signal $P_c$ is fed through an impedance, the signal $P_j$ becomes significantly attenuated at higher frequencies. This is illustrated in figure 2 by the rapidly decreasing ratio of $P_j$ to $P_c$ at increasing frequencies. Due to this loss of control pressure at higher frequencies, the gain of prior art amplifiers significantly diminished or disappeared at such frequencies. The present invention alleviates this problem by providing the above discussed acoustic pressure signals in the higher frequency range, thus increasing the gain of the amplifier in this range.

Figure 3 graphically illustrates the relationship between frequency and the ratio of the output pressure to the control pressure (gain) in the amplifier of the present invention. At lower frequencies the device operates substantially in the same manner as the prior art devices. This can be seen in that portion of the gain curve which terminates at point $N$ along the axis which represents frequency. Point $N$ signifies the normal bandwidth of a prior art amplifier since it is at this point where the gain diminishes substantially due to the loss of pressure at the control port, as discussed with reference to figure 2. In this device of the present invention, as the frequency increases beyond the value $N$, the wavelength of the deflected jet becomes such that the position of the wave at the splitter $S$ becomes 180° out of phase with the control pulse as discussed with reference to figure 1. At
that point the acoustic pressure signal is 180° out of phase with the control pulse, and combines therewith to increase the deflection of the jet, thereby increasing the gain of the amplifier. The acoustic signal generated by the device compensates for the loss in pressure at the control ports.

As the frequency of oscillation increases still further, the acoustic pulse generated at the splitter moves further out of phase with the pulse at the control port, and therefore will not combine therewith to effectively increase the deflection of the jet. However, the increasing frequency will shorten the wavelength of the deflected jet to the extent that the jet position at vane 2 will then be 180° out of phase with the pulse at the control port. The acoustic signal generated at vane 2, as shown by arrow H in figure 1, will then be 180° out of phase with the signal at the control port, and will combine therewith to again increase the deflection of the jet. The result will be a second increase in the gain of the amplifier, as shown by point 2 in figure 3. The same will again occur as the frequency is increased to bring the deflected jet 180° out of phase with the control signal at vane 1.

As can be seen in figure 3, the successive peaks in the gain of the amplifier at higher frequencies extend the operational bandwidth of the device to a frequency represented by point B. While figure 1 illustrates a device having two sets of vanes 1 and 2, it is to be noted that any number of vanes may be used. The position of the vane, that is the distance of the vane from the nozzle 4, will determine the frequency at which the acoustic energy will be effective to assist the control pulse in deflecting the jet. Therefore, an amplifier may be readily designed which will generate peaks in the gain thereof at preselected frequencies.

Figure 4 illustrates an embodiment of the invention which comprises two amplifiers of the invention operating in parallel. It is to be understood that three or more amplifiers may also be operated in parallel as shown in the drawing. The embodiment of figure 4 comprises common inputs 6 and 8 for the control pulses of the respective amplifiers, and common outputs 18 and 20. The upper-most amplifier comprises vanes 1 and 2 positioned at distances
\(d_1\) and \(d_2\) from the nozzle 4, respectively. The lower-most amplifier comprises nozzles 31 and 32 set at distances \(d_{31}\) and \(d_{32}\) from nozzle 4, respectively. It is noted that the distances \(d_1, d_2, d_{31}, d_{32}\) are all different from one another. Assuming that the velocities of the respective jets in the amplifiers are equal the peaks in gain generated by vanes 1 and 2 will be generated at frequencies different from the peaks in gain generated by vanes 31 and 32.

Figure 5 graphically illustrates the gain of the composite amplifier of figure 4. The lower curves marked LPA 1 and LPA 2 signify the gain curves of the respective individual amplifiers of figure 4. It is noted that each of these lower curves corresponds in shape generally to that of figure 3. The composite curve of figure 5 illustrates the effective gain of the composite device shown in figure 4. Note that since the peaks in gain of the respective lower curves are shifted relative one another the summation of the two results in a curve which is much smoother, having less sharply defined peaks and valleys. The result is an amplifier which has a much more even operation across a wide continuum of frequencies.

As noted above the frequency at which an amplifier of the invention will generate a peak in amplifier gain is determined by the position of the protrusions or vanes in the device. This frequency may also be affected by varying the velocity of the jet from nozzle 4. The velocity of the jet determines the transport time of the fluid to a position adjacent one of the protrusions or vanes, thereby affecting the time at which the jet will be in or out of phase with the pulse at the control port.
While the invention has been disclosed with reference to the specification and attached drawings, I do not wish to be limited to the specific details disclosed therein as obvious modifications can be made by one of ordinary skill in the art.
CLAIMS:

1. A broadband flueric amplifier comprising:
   means for directing a jet of fluid outwardly from a nozzle;
   output means comprising at least two output channels;
   control means for deflecting the jet toward an output channel and for
   causing the jet to oscillate between output channels; and
   means for increasing the deflection of the jet at specific frequencies
   of oscillation thereof.

2. An amplifier as in claim 1, wherein said means for increasing the deflection
   of the jet comprises means for generating acoustic feedback.

3. An amplifier as in claim 2, wherein said means for increasing the deflection
   of the jet comprises at least one protrusion having an edge situated
   closely adjacent the path of the jet between said nozzle and said output
   means.

4. An amplifier as in claim 3, which comprises at least one set of said
   protrusions situated closely adjacent opposite sides of the jet path.

5. An amplifier as in claim 3 or 4, wherein said means for directing the
   jet/fluid comprises a nozzle having a given width, and said protrusions
   are situated at a distance from the edge of said jet which does not exceed
   one-half said width.

6. An amplifier as in claim 2, wherein a splitter is positioned between
   said output channels to separate said channels, and interaction of said jet
   with said splitter generates acoustic feedback.
7. An amplifier as in claim 3, wherein the frequency at which the jet deflection will be increased is determined by the distance between the nozzle and said protrusion.

8. An amplifier as in claim 4 comprising more than one set of protrusions positioned at selected distances from said nozzle, whereby the deflection of said jet will be increased at several frequencies of oscillation thereof.

9. An amplifier as in claim 1 or 7, wherein the frequency at which the jet deflection will be increased is determined by the velocity of said jet.

10. A system comprising at least two amplifiers as in claim 4, wherein the amplifiers have common output channels and a common control means, wherein the distances of the protrusions from the nozzle in one of said amplifiers differs from said distances in other of said amplifiers, whereby the respective amplifiers will increase the deflection of their respective jets at differing frequencies of oscillation.
FIG. 1

FIG. 2

FIG. 3
FIG. 4

FIG. 5

\[ \frac{P_o}{P_c} \]

COMPOSITE

LPA 1

LPA 2

FREQUENCY

FIG. 5
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