DEVELOPMENT AND EVALUATION OF CROSS-IMPACT ANALYSIS AS A CRISIS DECISION-AID

by

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Cross-Impact Analysis

This thesis reviews the decision-making dilemma caused by information uncertainty and ambiguity produced during crisis situations. Several cross-impact analysis techniques are reviewed and evaluated as possible crisis decision-aids. Cross-event analysis is selected and extended for demonstration in a hypothetical crisis situation involving South Asia. The selected technique is operationalized and employed in a controlled environment.
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Development and Evaluation of Cross-Impact Analysis as a Crisis Decision-Aid

by

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ABSTRACT

This thesis reviews the decision-making dilemma caused by information uncertainty and ambiguity produced during crisis situations. Several cross-impact analysis techniques are reviewed and evaluated as possible crisis decision-aids. Cross-event analysis is selected and extended for demonstration in a hypothetical crisis situation involving South Asia. The selected technique is operationalized and employed in a controlled environment to assess policy response options to the hypothetical crisis. The thesis then assesses the technique's conceptual limitations, and evaluates its utility as a potential crisis decision-aiding methodology.
# TABLE OF CONTENTS

## I. DECISION MAKING IN CRISIS SITUATIONS

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. INTRODUCTION</td>
<td>9</td>
</tr>
<tr>
<td>B. THE DECISION-MAKING PROCESS</td>
<td>10</td>
</tr>
<tr>
<td>C. THE CONCEPT OF CRISIS</td>
<td>12</td>
</tr>
<tr>
<td>1. High Threat</td>
<td>13</td>
</tr>
<tr>
<td>2. Short Response Time</td>
<td>14</td>
</tr>
<tr>
<td>3. Surprise</td>
<td>14</td>
</tr>
<tr>
<td>D. THE DILEMMA</td>
<td>15</td>
</tr>
<tr>
<td>E. FOREIGN POLICY ANALYSIS</td>
<td>17</td>
</tr>
<tr>
<td>1. Systems Approach</td>
<td>17</td>
</tr>
<tr>
<td>2. Decisions Approach</td>
<td>18</td>
</tr>
<tr>
<td>3. Information Theory</td>
<td>20</td>
</tr>
<tr>
<td>F. REDUCING THE DILEMMA</td>
<td>22</td>
</tr>
<tr>
<td>G. OBJECTIVES</td>
<td>23</td>
</tr>
<tr>
<td>H. CONCLUSIONS</td>
<td>24</td>
</tr>
</tbody>
</table>

## II. CROSS-IMPACT ANALYSIS

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. INTRODUCTION</td>
<td>26</td>
</tr>
<tr>
<td>B. THE CONCEPT</td>
<td>29</td>
</tr>
<tr>
<td>C. REQUIREMENTS FOR CONDUCTING CROSS-IMPACT ANALYSIS</td>
<td>30</td>
</tr>
<tr>
<td>1. Event Set Specification</td>
<td>31</td>
</tr>
<tr>
<td>2. Initial Probabilities</td>
<td>34</td>
</tr>
<tr>
<td>3. Cross-Impacts</td>
<td>35</td>
</tr>
<tr>
<td>4. Computational Procedure</td>
<td>37</td>
</tr>
</tbody>
</table>
I. DECISION-MAKING IN CRISIS SITUATIONS

A. INTRODUCTION

Accounts describing foreign policy-making indicate decision-makers frequently deal with profuse quantities of intelligence information; which may be inconclusive, ambiguous, or conflicting. In an analysis of the Pearl Harbor surprise attack, Wohlstetter reveals problems resulting from information quantity and unclear meaning. She characterizes the situation as one in which, "...the mass of signals grow increasingly dense and freighted with ambiguities." [Ref. 1, p. 3]. Sorensen points out that a recurring problem facing Presidents is that the facts concerning a situation "may be in doubt or dispute." [Ref. 2, p. 19]. Schlesinger highlights the ambiguity surrounding the 1963 Vietnam situation by observing that the President asked; "Were you two gentlemen in the same country?" [Ref. 3, p. 993], upon receiving two widely divergent situation assessments from two officials sent to Vietnam on a fact-finding mission. This story also demonstrates the important role individual perceptions play in decision-making.

Analysts suggest perceptions influence the decision process because decision-makers interpret information using their insights, expectations, experience, and goals. Sprout and Sprout refer to this as the "stateman's psychological environment (that is his image, or estimate, of the situation,"
setting, or milieu [which] may or may not correspond to the operational environment" [Ref. 4, p. 318]. Perceptions are a key factor in recognizing crisis situations [Ref. 5]. Yet, it is in just such situations that information overloads and inconsistencies, which may confound a decision-maker's perceptions, seem to occur most dramatically [Ref. 6].

This chapter develops the concept that a "dilemma" exists in decision-making resulting from information overload and ambiguity. Establishing the dilemma's relationship to crises, and establishing its effect on the decision process requires introducing several relevant concepts. These include, identifying a basic decision process model, defining the concept of crisis, identifying its stress and information overload effects on decision-making, and examining factors which may reduce the dilemma. The purpose is to establish the need for a decision-aiding methodology which can lessen the dilemma's impact on the policy-making process.

B. THE DECISION-MAKING PROCESS

According to general decision-making theory, as developed by Turban and Meredith [Ref. 7], the first step in the decision-making process is problem identification. The same

\[\text{Subsequent steps include: searching for the alternative courses of action, evaluating the alternatives, and solution selection. These steps were not examined in detail but should be kept in mind during the discussion of the approaches to foreign policy analysis.}\]
source suggests identifying problems through comparing desired and actual levels of goal attainment. This presupposes that organizational goals are explicit, and in a form which facilitates measuring their level of accomplishment.

Such a requirement may be met in product oriented organizations (capturing a specific share of the market, or obtaining a specific profit level) however, it becomes much more difficult in organizations which frame goals in terms of advancing or protecting the nation's interests. Thus, in starting the decision process, the policy-maker immediately faces a problem using available information to determine what national interests an emerging situation threatens. The available information's accuracy greatly influences the precision of national interest identification and measurement.

Turbin and Meredith [Ref. 7] propose using an evaluation scheme in completing the decision process. The evaluation scheme requires some technique which predicts alternative response outcomes, a means of relating outcomes to goals, and a decision rule applicable to response selection. The authors also describe factors which complicate the decision process.

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\(^2\)This problem directly relates to the requirement for a method of system monitoring which would be basic to a decision-aiding system. This aspect of the aid was not developed extensively in the current study due to its complexity and the time required to develop, and validate indicators. Significant research is being conducted in this area by C.A. McClelland and others in the Threat Recognition and Analysis Project [Ref. 8].
Complications develop in decision-making when incorporating multiple goals, evaluating an indefinite number of alternatives, and determining how sensitive outcomes are to changes in problem configuration. (Changes in problem configuration could result from incomplete or inaccurate information. These slight changes may alter a policy alternative's impact on overall situational outcomes, and require an analysis of the sensitivity of the policy option's effect to changing circumstances.) The above problems obviously exist in the policy decision process. This study's major premise is that an information processing dilemma, beyond the range of these problems, further complicates policy decision-making in a crisis situation. The characteristics defining a crisis situation produce this dilemma.

C. THE CONCEPT OF CRISIS

Traditional international relations studies often explore the relationship between "crisis" and "normal" interactions. These works, usually describing events surrounding a crisis, give the concept several intuitive interpretations. The most common among these view crises as marking "turning points" in international relations. Other interpretations describe crises as events which occur naturally within the system. 3

3 In the Marxist-Leninist perspective, the occurrence of international crisis is an expression of the process of world revolution. Traditional power theory explains crisis as the operation of the balance of power. Here, crisis results from changes in the distribution of power, or from policy makers applying "field-tests" to determine the status of the balance [Ref. 9].
In his essay on "The Acute International Crisis," McClelland reviews these interpretations and concludes:

The crises are thought to be connected with the international struggles for ideas and also for power. They are seen as indicators of the state of the international system, but are regarded as prime operations in the system as well. They seem to be related to going to war and to staying at peace. [Ref. 9, p. 188].

Obviously, crisis is a pivotal concept in international relations. The problem is to establish it as a distinct phenomenon with recognizable characteristics.

Recent theoretical approaches to international relations studies attempt to operationalize the concept of crisis. These approaches are examined in a later section developing the dilemma's impact on the policy decision process. The approach advanced by Hermann [Refs. 10 and 11] was selected as most relevant to the current study. He describes three dimensions which bound a crisis situation.

1. High Threat

   The first dimension defining crisis arises because the situation poses "a potential hindrance or obstruction to some object or state of affairs that a decision-making unit is motivated to achieve." [Ref. 10, p. 29]. A situation that threatens important goals produces fear that failure to make a "good" decision could leave these goals in jeopardy. Having accurate and timely information, therefore, becomes extremely important. The other dimensions bounding the situation make it less likely such information is available.
2. **Short Response Time**

Combining with the high threat factor is the realization that in a short period of time, if no action is taken, the situation may change in some major (unfavorable) way. This aspect requires reaching a decision quickly, allowing little time for collecting information. Furthermore, short response time does not permit establishing elaborate search routines to disclose alternative response options. Thus, information currently available forms the basis for the decision. While decision-makers may receive more information, its accuracy is questionable, and individual perceptions become more important in determining what policy actions are eventually taken. The third dimension limits the stored information's utility.

3. **Surprise**

This final dimension results from the "absence of awareness on the part of policy makers that the situation is likely to occur." [Ref. 10, p. 30]. This surprise aspect may stem from incomplete information, or result from a policy-maker's satisfaction with the situation, producing a reluctance to believe contrary reports. Surprise makes it unlikely advance preparations exist for coping with the situation, producing an "ad-hoc" decision process. Surprise also prevents serious data-collection which usually precedes significant anticipated events [Ref. 11, p. 416]. These characteristics produce a dilemma which inhibits effective crisis response.
D. THE DILEMMA

In responding to a developing crisis, policy-makers face a dilemma dealing with breakdowns in what information usually means. As a crisis situation emerges, policy-makers receive unanticipated information inputs. These inputs are unexpected because they differ from perceptions concerning "normal" information outputs which the situation should be generating. Thus, the dilemma's first aspect involves understanding seemingly "unique" events. Policy-makers must correctly assess this information to realize that a problem exists, and to determine its importance.

As the crisis continues, more unique inputs flow in, increasing the information load the policy-maker must process [Ref. 12]. This aspect taxes the decision units' ability to sort and rapidly interpret available information. Janis and Mann [Ref. 14] identify several compensating procedures individuals use in coping with information overload.

A large body of literature exists indicating that individuals are sub-optimal information processors. Fisher, et al. [Ref. 13] review the literature on individual's information processing abilities. Their report indicates that unaided human judgements in complex decision tasks are often less accurate than formal algorithms. For instance, evidence presented indicates that individuals are conservative in interpreting data due to misperception and misaggregation. This implies that decisions are normally based on a small number of information items, thus excess data and effort spent in its collection is "wasted". Other evidence, collected from "real-world" studies, indicates that decision-makers have difficulty using multiple cue information.

The current study examines the way in which crisis situations further reduce decision-makers' capabilities to utilize information. The Fisher report indicates that the existence of the basic problem is enough to justify a decision-aiding system.
Many of these inhibit the accurate evaluation of response alternatives.

Evaluation also requires dependable information. Unfortunately, information during a crisis may be inaccurate or conflicting due to source unavailability or distortion. Many factors might cause this distortion; however, the effect is to reduce useful information. The policy maker must discriminate between relevant and irrelevant; reliable and unreliable information. A crisis situation's high threat and time pressure components impair the discrimination ability which information ambiguity requires.

One of this study's central propositions is that: Policy-makers in a crisis situation must struggle to interpret large quantities of unusual data, having ambiguous or conflicting meaning. Because the situation involves high threat, the perception develops that the decision is crucial. The rapid event flows require accurate information evaluation, and allow a limited decision time. The situation's surprise characteristic precludes utilizing routine response measures. To interpret large quantities of ambiguous data the policy-maker must rapidly and efficiently focus all available information and expertise on the situation.

Reviewing current approaches to foreign policy analysis indicates that this dilemma affects the entire policy-making process. This review reveals the requirement for a real time decision-aiding methodology which can reduce the information dilemma's impact on policy formulation.
E. FOREIGN POLICY ANALYSIS

Traditional foreign policy studies developed the foundations for more systematic approaches in identifying threats to national interests (crises). Hermann [Ref. 10] and McClelland [Ref. 9] review the intuitive interpretations of crisis found in descriptive international relations studies. The early works these authors review describe crises as "turning points" in international relations.

Crises were believed to result from competing national interests, or as situations which developed from a series of events a nation viewed as somehow posing a threat to its interests. The effort to develop a more exact understanding of foreign policy and crises produced two broad analytic approaches. These approaches can be classified "systemic" and "decisions;" both advance theoretical arguments and research findings revealing the policy maker's dilemma. Parker [Ref. 15] describes the tenets of these two approaches and their major contributions.

A third approach stems from applying information theory to foreign policy analysis, contributing new insights about communications flows in policy-making. This technique attempts to quantify concepts such as uncertainty and "noise."

1. Systems Approach

   The systems approach views crisis as an indication of the overall state of the system, directly related to
system stability. The connection to the traditional intuitive interpretations is obvious. From this viewpoint it can be argued the occurrence of crises can be used to identify the emergence of a problem situation.

An alternative view of crisis in systems studies proposes that it is a prime operation in the system itself. This view utilizes March and Simon's bureaucratic process model [Ref. 17]. In this model, organizations (modernizing societies) strive for stability in their environment. Recognizing a problem as having been dealt with previously, the organization tends to employ repetitive responses. As a result the organization establishes routine procedures whenever possible. Crises, in this model, are complexes of events overflowing normal processing channels, forcing new outputs, which return to the environment producing new inputs until new solutions are found [Ref. 9]. This sequence demonstrates how information ambiguity and uncertainty impact the decision process.

2. Decisions Approach

The second major approach to foreign policy analysis suggests that a stimulus-response relationship exists between crisis and decision [Ref. 11]. This approach highlights

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McClelland [Ref. 9] derives this interpretation from Hans J. Morgenthau's Politics Among Nations. Price [Ref. 16] proposes that system stability and decision unit flexibility combine to define the range of options decision-makers consider in a crisis situation.
the importance that decision-makers' perceptions play in responding to incoming data.6

The decisions approach identifies crisis as a situational variable affecting the decision process in two ways. These result from crisis' stress inducing characteristics, and their impact on information processing. These factors are closely interrelated but, for reasons of clarity, are explored separately in this study.

Hermann [Ref. 10] proposes that crises are situations involving high threat, allowing short response time, and surprising the decision unit. Holsti [Ref. 6], and other authors [Ref. 14], present psychological evidence demonstrating that these characteristics are stress inducing.7 The findings indicate that crisis induced stress reduces decision-making capabilities, especially those involved in identifying, sorting, processing, and interpreting information.

Foreign policy studies [Ref. 6], and field experiments [Ref. 10], give credence to these conclusions. These

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6Sprout and Sprout fully develop this concept in their works [Ref. 4 and 18]. Holsti, et al, [Ref. 5] modeled the process utilizing this factor. The model included: (1) the stimulus (meaning policy) applied by the initiating state, (2) the perception of the stimulus by the receiving state's decision unit, (3) the receiving state's policy response, and (4) response perception by the initiating state's decision unit.

7A high degree of threat to important values produces anxiety and overreaction. Long working hours required by short response times, and the perception of that pressure, magnify stress. Unanticipated, novel situations (surprise) are generally more threatening to decision-makers [Ref. 6].
findings indicate that policy makers face a dilemma interpreting and using information throughout the entire decision process. Finally, indications are that stress is self-reinforcing, suggesting that the dilemma increases as the situation continues [Ref. 6].

These studies reveal how stress affects the decision process by reducing the decision unit's ability to process information. One study went further and examined information volume produced during the crisis leading to World War I [Ref. 6]. Holsti's findings indicate that both information flow and uncertainty rose during the pre-war period. This increases both stress and information overload [Ref. 14].

3. Information Theory

Using information theory in foreign policy analysis is a relatively new approach which clarifies the relationship between uncertainty and stress. It measures information levels and uncertainty contained in transmitted messages. Studies using this technique report findings which relate to interpreting incoming intelligence information.

Lee [Ref. 21] explains information measurement, and demonstrates that "noise" in the system produced by erroneous

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8Other studies have explored the role of uncertainty in the occurrence of war. Singer, et al. [Ref. 19] conclude that the changing role of uncertainty accounts for the different time spans for which their models predicted the occurrence of conflicts. An attempt to formalize the procedure used in the Singer study demonstrated the potential importance of uncertainty in the decision process [Ref. 20].
or conflicting information reports significantly reduces a message's information value. McClelland [Ref. 22] uses information theory in developing a measure of uncertainty, which he employed in studying the Berlin question. This value represents uncertainty levels present in a given situation. This uncertainty reflects analysts' efforts to respond to the other side's actions. Uncertainty, measured in terms of H-Rel values, increased fairly sharply during "obvious" crisis phases in the Berlin problem. 9

These findings demonstrate that policy decisions are made under uncertainty and increased information volume. This situation strains the decision-maker's ability to cope with an unfolding situation. Threat, time pressure, and surprise combine to increase stress, and further degrade decision-making capabilities.

The preceding discussion explored the information dilemma facing policy makers. This dilemma involved three aspects: (1) responding to unexpected information, (2) coping with increased information volume, and (3) interpreting ambiguous, conflicting reports. Because the dilemma reduces decision-making capabilities, the requirement exists for a decision-aid to reduce its impact on the decision process.

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9H-Rel is defined as the ratio of absolute uncertainty (some knowledge of performance) to maximum uncertainty (no performance data known). As this ratio approaches 1.00, it suggests that the behaviors have shown increasing signs of disorderliness, or indicates a large amount of "variety" in event emissions [Ref. 22, p. 172].
To be useful such an aid must perform several functions.

F. REDUCING THE DILEMMA

The problems of multiple goals, evaluating an indefinite number of options, possible slight changes in problem configuration, and the need to incorporate new information complicates the policy decision process [Ref. 7]. A useful decision-aid must, therefore, react to changing circumstances and incorporate diverse inputs.

Information relevant to a particular situation is often incomplete, outdated, or inaccurate. The decision-maker must, therefore, be able to draw on data other than information about the immediate situation [Ref. 11]. The perceptions and judgments of specialists in the field might be one source of such data. The decision-aid should focus specialists' expertise and knowledge to extract meaning from incomplete information.

A true decision-aiding system - as opposed to an information processing system - should help reduce the problem. It should facilitate problem identification, aid in enumerating options, and help determine their potential outcomes. It should also provide the means to evaluate outcomes, and indicate optimum responses.

The short response time inherent in a crisis situation requires rapid yet considered action. To reduce decision time and allow thorough evaluation, the decision-aid should
be computer adaptable. This capability would permit obtaining interactions from numerous, geographically separate analysts and specialists. It would also provide the capability for conducting sensitivity analysis, and hard copy results for later analysis.

G. OBJECTIVES

This research project will develop and evaluate a potential real time decision-aiding technique to examine policy options for response in a crisis situation. A decision analysis methodology which deals with alternative evaluation under uncertainty will be selected as the basis for the potential decision-aid.

After determining the methodology's information input requirements, working assumptions, limitations, and alternative operation procedures, the methodology will be adapted into a policy analysis format. Designing a policy analysis format requires structuring the methodology to identify and rank national objectives affected by a specific problem, to identify possible response options supporting those objectives, to determine each option's contribution to achieving those objectives, and to evaluate their relative merit.

The modified technique will then be demonstrated in a controlled environment. A study group, representing experts, will be presented with a hypothetical crisis situation in which the objective is to determine an effective response. The technique will be used to guide the group in their consideration of the problem, and to correlate their inputs.
Based on this demonstration, the analytic technique will be evaluated on its effectiveness in structuring and obtaining a solution to the problem. The technique's utility will be assessed regarding its flexibility, ease of application, performance, and potential for computerization.

H. CONCLUSIONS

A crisis is defined by three "situational" boundaries [Refs. 10 and 11].

1. High threat to decision unit goals.
2. Short response time available.
3. Surprising the decision unit by its occurrence.

These dimensions impact the decision process producing three complicating factors which reduce a decision-maker's already questionable abilities [Ref. 13] to perform effectively when it is vitally important to do so.

These factors are [Refs. 6 and 22]:

1. Stress
2. Uncertainty
3. Information Overload

Increases in the levels of these factors, combined with poor information processing capabilities, produces a dilemma in interpreting information concerning a rapidly evolving situation.

This dilemma reduces the decision-maker's ability to:

1. Identify relevant useful data.
2. Correlate and interpret information.
3. Use this information to draw accurate inferences, and make responsible judgments.
4. Determine appropriate response alternatives, and evaluate their utility.
5. Make a logical solution selection.
Reducing this dilemma to improve decision-making abilities requires a decision-aid which is:

1. Flexible enough to incorporate multiple goals, diverse options, and incomplete information.
2. Draws on the "stored information" of an expert's perceptions to interpret the situation.
3. Quickly focuses the expertise and knowledge of numerous specialists on a situation to evaluate possible responses.
4. Systematically evaluates alternatives and indicates an optimal response.
5. Is computer adaptable.

Subsequent chapters of this study will identify and examine an existing decision analysis technique, develop it into a possible policy analysis tool, demonstrate its application, and evaluate its utility.
II. CROSS-IMPACT ANALYSIS

A. INTRODUCTION

The previous chapter identified problems facing decision-makers operating in an environment characterized by uncertainty and ambiguous information. In a social or political environment, moving from problem awareness to effective control or corrective actions requires that decision-makers understand the complex relationships operating in the environment. Such understanding is inhibited when a problem's components are defined and related through imprecise concepts and incomplete theories.

As indicated earlier, social and political problems are not easily adaptable to systematic "scientific" analysis. In many cases, the problem elements are not adequately defined nor operationalized. Furthermore, no adequate theory exists which describes the complex relationships among problem elements and indicators. These difficulties are apparent in the attempts to construct theories, define variables, and identify reliable indicators for crises reviewed in Chapter One.

Socio-economic and political problems are defined using imprecise concepts based on a limited understanding of the relationships among the variables involved. For this reason, conducting systematic decision analysis requires an alternative approach to problem specification. The basis for one alternative approach is suggested by Helmer:
...we can either throw up our hands in despair and wait until we have an adequate theory enabling us to deal with socio-economic problems as confidently as we do with problems in physics and chemistry, or we can make the most of an admittedly unsatisfactory situation and try to obtain the relative intuitive insights of experts and then use their judgments as systematically as possible. [cited in Ref. 23, p. 2]

The Delphi Technique was an early approach to employing subjective judgments in problem evaluation. It was subjected to several criticisms, one being that it produced "linearly independent" estimates which failed to account for potential interactions among the events being considered [Ref. 24]. Cross-Impact analysis is a Delphi extension intended to overcome this problem.

This chapter will present a non-technical explanation of the fundamental notions underlying cross-impact analysis. It will identify and classify contentious issues which must be resolved before the technique can be used. This discussion is intended to provide a basis for systematically comparing the various approaches to conducting cross-impact analysis. Specific areas which will be explored include: (1) the technique's basic concepts, (2) its information requirements and their interpretations, (3) the computational procedure used, and (4) the technique's outputs and possible applications.

In their review of the literature on decision-making, Fischer, et. al. examine several decision-aiding technologies
which use subjective estimates. These technologies follow a "decomposition" approach involving six tasks:

1. Recognizing that a decision problem exists.
2. Identifying the possible courses of action.
3. Constructing a probabilistic model of the decision-making environment.
4. Constructing a model to evaluate the possible consequences of each available action.
5. Selecting a course of action.
6. Implementing the alternative selected.

[Ref. 13, p. 43-44].

Because steps 1, 2, and 6 involve understanding the creative and organizational processes inherent in decision-making, most decision-aiding technologies concentrate on steps 3, 4, and 5. As this study will show, cross-impact analysis fits in well with these techniques. Cross-impact analysis is similar to other subjective techniques in that:

10 It should be noted that, on occasion, an entire community's evaluation can "miss the mark". The recent events in Iran provide an example. Reportedly the entire intelligence community was surprised at the situation's rapid deterioration (two crisis dimensions) [Ref. 25]. A large body of psychology and organizational information processing literature addresses the causes of this phenomenon. These causes are outside this study's scope, which attempts to develop and evaluate an aid for reducing the information dilemma.
B. THE CONCEPT

Cross-impact analysis is a technique which attempts to identify a given situation's possible outcomes by quantifying the linkages between potential developments. This is accomplished by systematically assessing how any particular event impacts all other relevant events. The technique and its various applications are based on the realization that most events are connected in some way [Ref. 26]. As explained by Gordon and Hayward: "it is hard to imagine an event without a predecessor which made it more or less likely or influenced its form - or one which, after occurring, left no mark." They term these possible interrelationships "cross-impacts" [Ref. 26, p. 101].

A second principle behind this technique is, that due to the nature of the "inexact sciences", the only possible approach to quantifying these interrelationships is to employ an expert's subjective judgments as a "substitute for the exact laws of causality found in the physical sciences." [Ref. 24, p. 134]. When the technique is employed, estimates are obtained for three event aspects hypothesized to govern possible interactions among future developments: (1) Mode - whether an event "enhances" or "inhibits" another; (2) Strength - how strong an impact one event has on another; and (3) Time Lag - how long before an event's influence is felt by other events. These aspects are developed in Gordon, Enzer, and Martino [Refs. 26, 27, and 28]. While latter cross-impact approaches do not assess these aspects explicitly, understanding
the interaction concept is important to understanding the intention and approach behind the analysis.

As a corollary to using subjective estimates, group opinions are usually obtained on the basis that: "The accuracy of a group judgment is always greater than (or at least equal to) the average accuracy of the individual judgments." [Dalkey, cited in Ref. 29, p. 140].

Fischer, et al. report several other studies which support this conclusion [Ref. 13, p. 50].

C. REQUIREMENTS FOR CONDUCTING CROSS-IMPACT ANALYSIS

To develop a probabilistic model of the problem environment using cross-impact analysis requires that four procedures be accomplished. The first three encompass the subjective estimation process and include: (1) specifying an event set which defines the environment, (2) estimating the initial occurrence probabilities of those events, and (3) estimating their interactions with each other (or their cross-impacts). The final procedure manipulates the model formed by these estimates to produce the data with which possible courses of action are evaluated. This step requires (4) developing an algorithm to use in the manipulation process. These procedures will be explained in detail below.

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There are a number of subjective measurement techniques which depend upon aggregating group estimates. Subjective measurement, aggregation procedures and applications are discussed in Torgerson, Miller, and Coombs [Refs. 30, 31, and 32]. The commonly used, group-based subjective measurement techniques rely heavily on central tendencies (i.e., means and standard deviations) in order to determine judgmental scores.
1. **Event Set Specification**

The first process undertaken in cross-impact analysis is developing an event set. This is "a set of possible events which are thought to be important to the issue being explored" [Ref. 33, p. 33]. The event set may be obtained in any manner: delphi, conferences, literature searches, consultations with experts, analyst specification, and so forth. A single event may address any subject, and the entire set may address any combination of subjects such as, "potential technological developments, a list of social or political developments, a combination of these, or something entirely different." [Ref. 34, p. 344].

As broad and loose as these requirements may seem, the means by which the event set was formulated in several of the demonstrations discussed in this study has been criticized as faulty [Ref. 29, p. 137]. Therefore, it seems relevant to review recommendations for accomplishing this process.

Enzer suggests candidate events be developed from the likely consequences of inaction, or allowing the "status-quo" to continue [Ref. 27, p. 50]. He also proposes several criteria for including candidate events in the analysis:

1. **the development must be important to the subject being evaluated, in the sense that the event should have some impact on an action or a decision that is being contemplated.**

2. **only those important developments whose outcome is uncertain (that**
is, those that may occur as opposed to those that almost certainly will or will not occur) should be included in the set being analyzed.

(3) if the event set is to be highly limited it is also desirable for the items to be causally related to each other in some way. [Ref. 35, p. 345] 12

(4) Developments or events as referred to here denote specific items which may occur in the future. They are 'specific' in the sense that their occurrence or non-occurrence can be rigorously determined. [Ref. 27, p. 50].

Mitchell and Tydeman propose several rules for event formulation. Their purpose is to reduce possible respondent misinterpretation and thereby reduce response variation. These rules will be followed in the application section of this study.

(a) Except where the cause is part of the event to be studied, events should not be stated in the form 'A occurs because of B'.

(b) Events should be single rather than multiple, i.e., 'A occurs' rather than 'A, B, and C occur'.

(c) Events should, where possible, be definite and specific rather than vague and general, e.g.,'

12Enzer develops the requirement of being "causally related" through the concept of "coupling". He describes three types of event coupling, "totally uncoupled", "coupled", and totally included". Of these, totally uncoupled events are felt to be of little importance in the analysis, coupled events should be analyzed, and included events may be analyzed if their impacts are not estimated more than once [Ref. 27, p. 52].
'Costs will increase more than 20% in real terms' rather than 'Costs will increase significantly'. [Ref. 29, p. 136].

Formulation rules are necessary to insure that "the group involved reach agreement and understanding on the specification and wording of the event set." [Ref. 36, p. 333].

Although it is desirable that the event set completely define the problem under consideration, this is rarely possible. The uncertainties in the problem environment, and the complex issues involved could necessitate specifying many events. Since the possible first order interactions between events increases as the square of the number of events specified, estimating their interactions would quickly become extremely time consuming [Ref. 34]. Therefore, completeness is often obtained by fiat. Since it is almost impossible to specify an event set which includes every conceivable development most analysts limit the event set to a manageable size and attempt to include the most important or significant events. In such cases, events to be included in the analysis are selected from a large list of "candidate" events on the basis of subjective importance, desirability, or impact ratings. These procedures will be described in the next chapter.

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13This limitation's implications have been examined in several cross-impact approaches. The developers (Enzer, Turoff, and Mitchell and Tydeman) suggest different methods to identify the most important events and to retain the most sensitive or influential ones for analysis. In this manner, it is felt that the most serious aspects of a problem are considered. Furthermore, it is always possible to expand the event set as circumstances dictate. Thus, obtaining a complete event set by "fiat" is felt to be the only practicable method, and does not impose severe limitations.
2. **Initial Probabilities**

Once the event set is established and understood by the respondents, the next procedure obtains estimates for each event's "initial" likelihood of occurrence. These estimates are variously termed individual, initial or marginal probabilities. All refer to a particular event's likelihood of occurring by some specified date.

As with event specification, Enzer suggests that these estimates should be developed from an environment which might evolve naturally from the current situation [Ref. 35]. This interpretation recognizes that developments are typically seen in their total environment, and not in isolation.

This viewpoint poses a conceptual problem with cross-impact analysis which must be resolved before the technique can be operationalized. If events are viewed in their total environment when their initial probabilities are estimated, do these estimates include a consideration of the occurrence of other likely events in the set? In other words, in estimating the initial probability that event A will occur, do respondents implicitly consider the impact on A of another event (say B) if the other event also occurs? Each approach to cross-impact analysis must deal with this problem, and

\[14\] Different terms are applied by the various cross-impact analysis approaches to describe the technique's basic concepts. In this study these will be identified as they occur, and thereafter the most descriptive, or logically consistent term will be used.
it will be considered more fully while examining specific approaches.

A reasonable response to this problem appears to be that estimators do take the interrelationships among events into consideration, but only incompletely and not systematically. Therefore, some modification is necessary to obtain "consistent" estimates [Ref. 34, p. 342].

3. Cross-Impacts

The next process obtains "A qualitative description of the effect of the occurrence (or non-occurrence) of one event on the likelihood of occurrence of the other events in the set." [Ref. 27, p. 51]. These are subjective estimates concerning how an event's occurrence would change the probability of every other event's occurrence. These are binary estimates, dealing with the interactions between two events only.

In eliciting these estimates, respondents are told to assume certain occurrence (or non-occurrence) for an event and then assess its impact on each remaining event. Rules for event impact assessment state that the events are assumed to happen only once (i.e., non-repetitive), that they do not have to happen at all, and that they do not occur simultaneously [Ref. 36].

These estimates have been termed "conditional" or "causal" probabilities. This conflict in terms stems from another conceptual problem in cross-impact analysis, relating directly to the problem of obtaining consistent estimates.
The basic problem is determining how the cross-impacts should be interpreted. One interpretation is that the estimates are conditional probabilities in the "classical" sense (i.e., the probability of event A given event B has occurred, $P(A|B)$), or are used to derive conditional probabilities [Ref. 37]. Accepting this interpretation permits using Bayesian probability relationships to test estimate consistency. Several developers have derived conditions which are intended to insure consistency and can be used to compute probability bounds on subsequent estimates.\(^{15}\) Another interpretation is that the estimates are causal, time-dependent probabilities to which classical probability rules do not apply (i.e., the probability A will occur assuming B occurs first, $P(A|B_f)$). In this case Bayesian probability relationships have only limited application [Ref. 39].

A third interpretation is that the technique attempts to obtain subjective estimates for the correlation coefficients between events. In this case inconsistency is not readily apparent, as when probability values exceed unity or become negative. Turoff applies this interpretation in his cross-impact approach [Ref. 36].

This problem will be examined in detail in the next chapter. Initially, however, it appears that using classical probability relationships not only permits testing estimates

\[^{15}\text{See, for example, Dalkey and Sarin [Refs. 34 and 38] for consistency conditions and boundaries.}\]
for consistency, but provides relationships for adjusting inconsistent estimates, and furnishes a model for their manipulation. Without such a model, and recognizing the lack of causal knowledge in the social sciences, the technique faces problems in interpreting the subjective estimates, and justifying the manipulation algorithms.\textsuperscript{16}

4. Computational Procedure

The final cross-impact analysis process employs a technique to analyze estimates and provide useful information to decision makers. As noted by Dalkey, given the large numbers of possible interactions,

\textit{even if a matrix describing the interactions is available ... the task of thinking through the implications rapidly gets out of hand. Some computational aid is required to take account of the large number of interdependencies}. [Ref. 34, p. 341].

Frequently, the approach conducts "a Monte Carlo sampling of chains of events in which the probability of an event in the chain is modified by the cross-impact of the previously occurring event in the chain." [Ref. 34, p. 341]. This procedure requires an algorithm for calculating the cross-impact effects among events. Several methods of manipulation and analysis have been proposed and are examined in the next chapter.

\textsuperscript{16}It also seems that probability values imply that A and B are discrete events; whereas correlation coefficients, "r", imply that A and B are indicators of underlying variables to which the events are linked conceptually within a theoretical framework.
In the Monte Carlo process, an event is randomly selected, and its occurrence or non-occurrence randomly decided based on its initial probability. The remaining events' initial probabilities are adjusted using the selected algorithm, according to the first event's cross-impacts. At this point a second event is selected and decided, based on its new probability. The remaining probabilities are revised and the process continues until all events have been decided.

Completing the Monte Carlo procedure is termed a run. Conducting numerous runs permits calculating revised initial probabilities for each event based on the event's experimental frequency of occurrence. As an event is decided its occurrence of non-occurrence is recorded (either 1 or 0 respectively). Revised initial probabilities are then determined by dividing the number of times each event occurred by the total number of runs conducted.

Early research using the technique suggested conducting more than one thousand runs in order to reach stability and reduce random variation [Ref. 26]. However, during demonstrations as few as twenty runs produced adequate results [Ref. 27]. Johnson examined the requirements concerning how many runs were needed to produce significant probability shifts and stabilize inherent random variation [Ref. 40]. Using standard statistical techniques he concluded that: (1) The mean probability values for events reached stability within a small number of runs (< 50). This implies
that the model reached stability, or a consistent point, relatively quickly. (2) The standard deviations of modified probabilities decreased with increased numbers of runs. However, beyond fifty runs, the magnitude of these reductions was small. This indicates that stability was reached, and that random variation was only slightly reduced by increasing the numbers of runs. (3) As more events were included in the analysis set, no notable changes appeared in the average standard deviations obtained. This indicates that the numbers of runs does not have to increase as the number of events increases. (4) Furthermore, Johnson observed that while it is possible to obtain significant probability shifts from a statistical standpoint, there is no assurance that such shifts are significant from a policy standpoint [Ref. 40, p. 127-130].

D. CROSS-IMPACT ANALYSIS SYMBOLOGY

The different cross-impact approaches, besides using various terms to describe basic concepts, have also employed different symbologies in their demonstrations. This section is presented in an attempt to establish a consistent symbology for cross-impact computations. This will simplify comparing the different cross-impact approaches in the next chapter.

1. Event Set Specification

Let A, B, C, ... N be events which could develop from present circumstances, which seem to be related to each other (i.e., are coupled as previously described), and are
important to some problem being considered. These events were selected and formulated in accordance with the rules specified previously. Designating A as event one (E₁), B as event two (E₂), etc., produces a set of events {E₁, E₂, E₃, ..., Eₙ}.

2. **Estimate Initial Probabilities**

   Each event (E₁ through Eₙ) has an associated initial probability of occurring by some specified time in the future based on the present situation. It is possible for experts to estimate this probability (i.e., if present developments continue without change, the probability A, (E₁), will occur by time T is x). Designate this probability (of event A) as P(E₁) and similarly for all events in the set {P(E₁), P(E₂), P(E₃), ..., P(Eₙ)}. Or as Pᵢ for i = 1, 2, 3, ..., n.

3. **Estimate Cross-Impacts**

   The next step is to estimate the effect on the other events of the occurrence of any one event (i.e., if event B is certain to occur what is the new probability event A will occur?). P(E₁|E₂) or P(i|j) for i, j = 1, 2, 3, ..., n and j ≠ i. These estimates are obtained for each possible event pair (i, j) and designated in the form P(impacted event|certain event).

4. **Computational Procedure**

   The result from this series of estimates may then be arranged in an n by n matrix. Since the impact of an event on itself obviously has no meaning, the diagonal cell by
convention contains the events' initial probability. The matrix thus contains all $n^2$ required estimates.

FIGURE 1

BASIC CROSS-IMPACT MATRIX

<table>
<thead>
<tr>
<th>EVENT</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>if this event occurs</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>A</td>
<td>$P(E_1)$</td>
<td>$P(E_2</td>
<td>E_1)$</td>
<td>$P(E_3</td>
</tr>
<tr>
<td>B</td>
<td>$P(E_1</td>
<td>E_2)$</td>
<td>$P(E_2)$</td>
<td>$P(E_3</td>
</tr>
<tr>
<td>C</td>
<td>$P(E_1</td>
<td>E_3)$</td>
<td>$P(E_2</td>
<td>E_3)$</td>
</tr>
<tr>
<td>N</td>
<td>$P(E_1</td>
<td>E_n)$</td>
<td>$P(E_2</td>
<td>E_n)$</td>
</tr>
</tbody>
</table>

Note that $P(E_1|E_2)$ is not necessarily equal to $P(E_2|E_1)$.

The matrix is then manipulated using the Monte Carlo procedure previously described, or some other procedure may be substituted. Using numerous runs permits computing revised initial probabilities for each event based on its frequency of occurrence during the runs.

$$P'(E_n) = \frac{\text{# times } E_n \text{ occurred}}{\text{# runs conducted}}$$

E. OUTPUTS AND APPLICATIONS

This section will review the types of analyses conducted using the technique and their possible applications. The technique's proponents have demonstrated several types of
analyses using the data generated by the technique. Many applications claimed for these outputs seem to address effectively the difficulties identified with problem solving in the social sciences. These claims seem plausible in the context of the authors' arguments, however, final judgment on the technique's utility must be reserved until the claims can be verified with data from experiments or real world applications. These outputs and their supporting rationale will be described below, along with proposed applications. Specific procedures for conducting these analyses will be presented in the next chapter which develops the major cross-impact analysis approaches.

One often cited potential for the technique is the learning experience it provides. Due to its systematic approach, estimators are forced to develop and clarify their opinions regarding the causal linkages coupling potential developments in a field or several fields into a consistent picture [Ref. 33]. Estimators must be explicit when structuring their responses, and are forced to consider related impacts and overall consistency. This aids in organizing and evaluating an individual's views on a complex problem [Ref. 36].

Manipulating the matrix through the Monte Carlo process, or other procedures (other procedures will be discussed during the review of specific cross-impact approaches), produces event sequence scenarios which indicate the various ways in which a given situation might evolve. As used in
cross-impact analysis the term scenario has a very specific connotation. A scenario refers to the event outcome decision (either occurrence or non-occurrence) made when the estimates are manipulated, and the sequence in which the events are decided. For a six event set a possible scenario would be depicted in the following manner:

\[(1, 0, 0, 1, 1, 1,)\]

where events 1, 4, 5, and 6 occurred, and events 2 and 3 did not. In this study, subsequent discussions of the cross-impact methodology, of specific cross-impact approaches, and of the study's demonstration results will use the term scenario (or, event sequence scenario) to refer to these event occurrence chains.

Scenario generation provides decision-makers a background against which policy options may be evaluated.\(^{17}\) By specifying scenarios, and evaluating them using subjective event importance ratings, it might be possible to identify obscure

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\(^{17}\)Sarin discusses scenario generation and its importance [Ref. 38]. For a set of \(n\) events there are \(2^n\) possible scenarios, each with an associated scenario probability, \(P(x_n)\). Sarin proposes a method for computing these scenario probabilities from expert estimates. The scenario probabilities may also be computed, as were the revised initial event probabilities, through the Monte Carlo process. Each Monte Carlo run produces one scenario, \(P(x_n)\) for that scenario is computed by the frequency that it occurs divided by the number of scenarios generated.

\[P(x_n) = \frac{\text{\# } x_n \text{ produced}}{\text{\# runs}}\]

However, this requires that many Monte Carlo runs be conducted.
but important situations from among the vast number of possibilities [Ref. 33]. Used alone, scenario generation at least indicates to decision-makers the likely consequences of inaction. The scenario output is the technique's major tool in its most interesting application, policy analysis.

Through comparing the scenarios (produced by recording event sequence outcomes during a Monte Carlo simulation) to the cross-impact matrix it is possible to identify "critical" events which make a considerable difference in outcomes [Ref. 28]. This causal analysis also provides "a means of gaining insight into key branch points and items on which current actions and policies should be focused in order to increase the likelihood of achieving a desired outcome." [Ref. 33, p. 45].

By examining the cross-impact matrix with the scenarios it is also possible to identify possible "side effects" produced by the decision under consideration. This examination could aid the decision-maker in two ways. First, a nagging problem which faces decision-makers is to identify additional problems which may arise further down the line caused by their attempts to respond to the immediate problem situation. Determining a decision's possible side effects may reveal unanticipated developments which might stem from a particular situation or a particular policy option.

A second advantage offered by exploring a decision's side effects is that the examination may indicate less expensive means of attaining goals through investment in
high-payoff areas which may have seemed unrelated [Ref. 26, p. 101]. This advantage is reflected in attempts to use cross-impact analysis to evaluate resource allocation strategies. Gordon suggested resource allocation strategies could be tested by adjusting the initial probability estimates for one or several events to reflect policy decisions in order to improve or inhibit their likelihood. These adjustments are then manipulated as was the original matrix, and the output examined to determine the policy decision's effect on the various scenario probabilities observed [Ref. 24]. This process is termed sensitivity analysis, and can be used to explore the effects caused by changes in problem configuration.

Further cross-impact analysis applications derive from using the technique to model the relationships operative in a given situation [Ref. 4]. Enzer demonstrates that the matrix may be used to determine an event's dominance and sensitivity. In his approach, the sum of the absolute values in a matrix row can be interpreted as a measure of the magnitude of the impact one event's occurrence has on the occurrence likelihood of all other events (its dominance) [Ref. 27, p. 54]. As a minimum, this identifies the events which have the greatest and least effect, relatively, on the situation. Those events with the greatest overall effects are prime candidates for intervention through resource allocation.

Event sensitivity is computed from the algebraic sum of the matrix column values. This is a measure indicating how responsive an event is to the other events in the set [Ref. 27, p. 54]. It reveals events which may be susceptible
to change through secondary intervention. It could also indicate those events which most readily indicate changes in the system, and hence, should comprise the components of a monitoring mechanism.

By focusing on the opinion spread registered by the experts, Enzer develops an uncertainty measure reflecting the degree of estimator uncertainty concerning the cross-impacts. This is derived for each event by determining the distance between the upper quartile and lower quartile estimate values [Ref. 27, p. 54]. This "uncertainty" measure also highlights the level of agreement among the experts, and can be interpreted as a "confidence" measure. Such information would be an aid in resource allocation, allowing decision-makers to avoid investing effort in influencing an event whose impact was highly uncertain. If subjective estimates regarding an event's importance and desirability are obtained with the probability estimates more elaborate analyses are possible. These could aid decision-makers in identifying desirable actions and areas warranting further investigation [Ref. 27, p. 57].

The cross-impact technique also appears amenable to manipulation with digraph theory, and other techniques used in studies of individual and organizational information processing (esp. information theory). Digraph theory uses binary matrix entries to trace third- and fourth-level interrelationships among events. Turoff incorporated information theory

\[18\] The principles and methods of digraph theory are presented in Harary, et al. [Ref. 42]. Axelrod [Ref. 43], and Bonham, et al. [Refs. 44 and 45] have attempted to apply digraph theory to international relations theory and problems.
in his cross-impact approach to relate estimates for occurrence and non-occurrence [Ref. 36].

F. RATIONALE FOR SELECTING CROSS-IMPACT ANALYSIS

The preceding discussion has revealed several aspects of cross-impact analysis which make it attractive as a decision-aiding methodology for crisis situations. The technique's advantages will be summarized below as justification for selecting cross-impact analysis for demonstration and evaluation in this project. Specific aspects of the technique discussed include: (1) its subjective method of evaluation, (2) its systematic approach, (3) its flexibility, (4) its demonstrated application to policy analysis, and (5) its potential utility as a learning tool.

1. Subjective

Using expert's subjective evaluations precludes the need for a formal theory relating crisis elements, national interests, and policy options. The procedure takes into account the perceptions and accumulated knowledge of experts and decision-makers (which is not easily transferred) and uses them to process and interpret imprecise information. It minimizes the need to collect precise data on numerous, inadequately understood indicators, especially in situations where time and stored information is limited.\(^{19}\)

\(^{19}\)This is not intended to suggest that theory construction and indicator development are not important. As noted in Chapter One, these approaches are required for system monitoring, furthermore, they are necessary to achieve precision in the social sciences as indicated by Roszenau [Ref. 46]. What is intended is to establish the current need for subjective estimates in quantitative analyses of policy problems.
2. **Systematic Approach**

Because the technique is systematic in its approach, it encourages the consideration of the numerous interactions which could be overlooked in situations involving short response time and stress. In addition, it proceeds logically from problem identification through the selection of policy options. The subjective estimates obtained during the evaluation process are retained so the entire analysis can be replicated at will, rather than being lost after the crisis has passed.

Finally, because it is a systematic procedure cross-impact analysis may be conducted using a computer. Most applications demonstrated, especially those presented by Mitchell and Tydeman, Turoff, and Sarin [Refs. 29, 36, and 38], have utilized or advocated an interactive computer system for querying experts. This capability increases analysis speed and flexibility, both of which are desirable for a decision-aid in crisis situations.

3. **Flexibility**

Cross-impact analysis is not constrained by data requirements to evaluating only a few empirically quantifiable variables. The variables used in the technique are obtained from experts' perceptions concerning a specific problem. If, while obtaining subjective probability estimates, it becomes apparent some important aspect of the problem has been omitted it is possible to include it in the event set. This capability is particularly useful in analyzing a crisis situation involving uncertainty and incomplete information.
It allows the event set to be modified in response to changing circumstances. Such "last minute" modifications are possible because the values used in the analysis are subjective, and can be easily revised or expanded.

Using subjective judgments also permits the approach to address any problem for which an appropriate event set can be specified. This flexibility is evidenced by the broad spectrum of problems to which the technique has been applied.

4. Demonstrated Applications

Several cross-impact studies have been conducted in situations relevant to policy analysis. Heuer describes one such study in reviewing CIA efforts to use quantitative techniques to analyze policy relevant situations [Ref. 41]. The approach is future oriented and addresses the potential evolution of a current situation. Thus, cross-impact analysis attempts to be predictive, conducts sensitivity analysis, and indicates degrees of uncertainty. Other developers have applied the methodology to problems of evaluating transportation alternatives, population trends, and energy options [Refs. 26, 33, and 47]. Changing values and objectives are implicitly considered by using subjective estimates or may be explicitly stated in the cross-impact matrix. Finally, once the estimates' form and meaning are understood the procedure may be used by anyone. For these reasons, cross-impact analysis enhances the process of analyzing a situation and reaching a policy decision.
5. Learning Tool

Since respondent estimates can be retained, the technique can help close the feedback loop involved in assessing the direction in which a situation is moving. This can be accomplished by comparing estimates obtained over time \((T_1 - T_2)\). If a policy has been implemented between \(T_1\) and \(T_2\), then the comparison tests the policy’s success.

By monitoring the emergence of cross-impact matrices over time, it might be possible to gain insight into how organizations structure their knowledge about the environment. Thus, a series of matrices, taken from a particular situation, might reveal some mechanics of organizational information processing.

G. EVALUATION CRITERIA

The preceding overview highlighted cross-impact analysis’ potential applicability as a policy tool. However, the various conceptual problems identified here and by the technique’s developers have produced several alternative cross-impact approaches, each advancing different methods to deal with the technique’s conceptual problems, and leading to confusion regarding which variation of the technique is the best to operationalize.

Due to the confusion, selecting a variation for extension as a crisis decision-aid should be approached systematically using consistent evaluation criteria. These criteria should address each variation’s primary components, including its assumptions, underlying rationale, and implications. Specific
implementation problems should be evaluated by examining information requirements, computational procedures, and methodological approach. The goal is to select a practicable approach and develop it into a crisis decision-aid.

In developing consistent evaluation criteria, several considerations must be kept in mind. These stem from the characteristics defining crisis, and this project's time and computational resource limitations. Based on these considerations, discussed in the first chapter, the following criteria were formulated for comparing the various cross-impact approaches.

1. **Is the event formulation scope adequate?** This refers to the subject area addressed by the event set. In the intended analysis, events must cover such concepts as "national interests" threatened, and specific "policy options" available.

2. **Can events be rated on importance/desirability?** The need for such subjective estimates in sensitivity analysis and event set selection has been indicated. This refers to whether or not the specific technique includes procedures for obtaining and using such estimates.

3. **What types of analysis can be performed using the technique?**

4. **Is the technique computer adaptable?**

5. **Are the estimated relationships clearly formulated?** This refers to whether or not the procedure used to obtain estimates, and the questions asked, are understood by the respondents. Are the respondents asked for estimates they can reasonably be expected to supply?
6. Are the estimates consistent, or can consistency be obtained? This refers to the need for estimates which can be manipulated using a systematic, rigorous, methodology.

7. What algorithm is used to manipulate the estimates? This refers to the procedure by which the cross-impacts are "taken into account" [Ref. 34, p. 342], and how it is structured.

8. Is the procedure logical/justifiable? This refers to the assumptions made in adopting the algorithm, are they reasonable and what limitations do they impose?

9. How is consistency obtained? This refers to the computational procedure for checking consistency and revising estimates into a consistent set.

10. How are scenarios generated? This refers to the procedure used to develop event sequence scenarios, how complex it is and whether or not it provides a ranking system.

11. How many estimates does the technique require?

12. What types of computation are performed? This refers to the complexity of the calculations. Are they algebraic, quadratic, differentials, or linear programs?

13. How many terms are involved in each formula?

14. How many separate calculations are required? This refers to what computational steps are required for estimate manipulation, checking consistency, scenario generation and analysis.

These last four criteria are proposed in order to identify an approach which can be demonstrated using limited computational facilities. This study will replicate the
selected approach manually, therefore, the number and complexity of estimates and computations must be kept to a manageable number.

H. CONCLUSION

This chapter has presented a broad overview of cross-impact analysis, identifying its basic concepts and potential applications. Since there are a number of alternative approaches to implementing the methodology a set of evaluation criteria was developed to use in selecting an approach for operationalization. The next chapter will review the major cross-impact approaches, select one for demonstration, and extend it to deal with a crisis situation.

Subsequent chapters will discuss the implementation procedure used, identify the problems encountered in operationalizing the selected approach, and present the demonstration results. In the final chapter, these results and the implementation experience will be used to evaluate the selected cross-impact approach's potential utility as a crisis decision-aid.
III. THE MAJOR CROSS-IMPACT APPROACHES

A. INTRODUCTION

This chapter will identify and evaluate the major approaches to cross-impact analysis using the evaluation criteria developed in the preceding chapter. Four major approaches will be described and discussed in terms of their basic assumptions, procedures and outputs. In addition, three ancillary approaches which were felt to be too complex for demonstration will be reviewed briefly. The four major approaches will then be compared using the evaluation criteria, and one will be selected for demonstration and evaluation as a possible crisis decision-aid. The selection process will also highlight possible problems in operationalizing the selected approach.

Demonstrating the selected approach in a hypothetical policy relevant, crisis situation may require that it be extended to address specific problems inherent in such situations. These problems include short response time, and evaluating specific policy options. Possible extensions to cross-impact analysis will be developed once an approach has been selected.

B. THE BASIC APPROACH (GORDON)

The concept of cross-impact analysis was introduced by Gordon and Hayward in 1968 [Ref. 26]. As previously noted, it was a partial response to one of the Delphi criticisms
[Ref. 24]. Its first application was in a forecasting game, developed for the Kaiser Corporation, which tested resource allocation strategies [Ref. 24].

1. Assumptions

Cross-impact analysis is based on two assumptions. In response to the Delphi criticism, the developers hypothesized that most events are connected in some way. Further, they felt that it is possible to estimate these connections subjectively as to mode (enhancing or inhibiting), strength (amount of influence), and time lag (length of time required for effect to be felt) [Ref. 26, p. 101-4].

Given that linkages existed and could be estimated, the developers next addressed how the impacts worked, or how one event's occurrence $D_m'(E_j)$, changed a second event's $D_n'(E_i)$, occurrence probability. They assumed each event had some "individual" (initial) probability of occurring $P_n'(P_i)$, by a specific date. The change in probability $P_n'(P_i')$, caused by another event's occurrence was assumed to be a function of mode, strength, and time lag. However, an event's failure to occur (non-occurrence) was assumed to have no effect on the remaining probabilities.

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20 These relationships are more complex than indicated here. Gordon realized that the "connections are subtle and vary widely in strength. [sic] Composed of at least two major elements; probabilities of feasibility ($P_T$) and pursuit ($P_P$)." [Ref. 24, p. 139].

55
Stated mathematically, they assumed: [Ref. 26, p. 104].

\[ P'_{i} = f(P_{i}, M, S, t_{j}, t) \]

where:

\( f \) = function

\( M \) = estimated Mode

\( t_{j} \) = time in the future \( E_{j} \) occurs

\( S \) = estimated strength

\( t \) = time in the future for which probabilities are being estimated

The relationship between events was assumed to be quadratic [Ref. 26, p. 105],

\[ P'_{i} = aP_{i}^{2} + bP_{i} + c \]

By assuming known end conditions:

when \( P_{i} = 0 \) then \( P'_{i} = 0 \)

\( P_{i} = 1 \) \( P'_{i} = 1 \)

and if \( t_{j} = t \) (no time lag) \( P_{i} = P'_{i} \)

And assuming the mode, strength, and time effects are linear [Ref. 26, p. 106]:

\[ a = kS \frac{t - t_{j}}{t} \]
where

\[ k = \pm 1 \text{ (Mode)} \]
\[ S = \text{number between 0 and 1 (smaller representing weaker effect)} \]

Therefore, in the inhibiting case,

\[-1 < a < 0\]

and enhancing

\[ 0 < a < 1 \]

this produces:

\[ p'_i = kS \frac{t-t_i}{t} p_i^2 + [1 - kS \frac{t-t_i}{t}] p_i \]

2. Procedure

This equation was demonstrated in two applications, a historical context and a futures context. In these demonstrations, the estimates were made by the experimenters. The historical problem examined the Minuteman deployment decision, the future problem examined transportation developments in light of technological advances and changing societal attitudes [Ref. 26].

In both cases the procedure began by specifying relevant events and developments to be examined. These
events were obtained through literature searches, expert interviews, and the analysts' own opinions.

The next step was to estimate the initial probabilities and occurrence dates for each event. An event matrix was then constructed, and the potential interactions between each event and every other event were estimated.

These estimates assessed both the interaction's mode and its strength. They were made by assuming one event was certain to occur, and then predicting its impact on each remaining event. These values ranged from -1.0 to +1.0, and made up the matrix body. Upon reviewing the individual event pair interactions certain "predecessor-successor" relationships were apparent to the experimenters. In the subsequent manipulation, events which had to be predecessors were evaluated first.21

A computer was programmed with the quadratic relationship and the "Monte Carlo" procedure used to manipulate the matrix. If an event was decided to occur, its impact was calculated from its cross-impacts with each other event using the quadratic equation, and the remaining events' initial probabilities were adjusted accordingly. If non-occurrence was decided then the remaining probabilities

\[ \text{21 In the matrix, these relationships were indicated by appending a second digit to the interaction values. (0 = immaterial, 1 = likely predecessor, 2 = necessary predecessor) [Ref. 26, p. 107].} \]
were not changed. The computer run was conducted one thousand times so that "revised" probabilities could be computed for each event based on its occurrence frequency [Ref. 26, p. 108].

3. Analyses Performed

Using this procedure, Gordon and Hayward demonstrated that four potentially useful analytical methods could be developed from the initial matrix. These were: (1) final probability rankings, (2) probability shifts, (3) tracing causal effects, and (4) scenario sensitivity analysis.

Ranking by final probability produced a possible event sequence outcome scenario. In the example this was felt to be logically consistent (plausible). However, the developers realized it was no more consistent than other possible scenarios. (Alternative scenarios could be obtained by recording the "decisions" made in each computer run using 0 for non-occurrence and 1 for occurrence.) [Ref. 26, p. 108].

The ranking by probability shift (difference between $P_i$ and $P'_i$) was used to identify the events most affected by the suspected interactions. In other words: "the item [event] which had the highest probability shift could be expected to be the one most influenced by the external events depicted by the remainder of the list." [Ref. 26, p. 108].

In their forecasting analysis, the developers attempted to use the matrix to trace through the reasons
for an event's resulting probability shift. For example they concluded that:

Within the groups of items [events]
describing future transportation
modes, fast sub-surface trains
showed the highest probability
gain, suggesting that changing
customer preferences, social
customs, and technological
innovations might favor this role.
[Ref. 26, p. 113].

In essence, this is an elaborate way to state the probability shift conclusion, and later cross-impact developers would attempt to be more explicit in tracing causal effects.

The developers also used their model to examine the potential effects of conscious policy decisions. Policy decisions were interpreted as decisions to allocate re-
resources to making a particular event or set of events more likely. Such a decision was reflected by arbitrarily raising the initial probabilities for those events. The policy decision's results were then indicated by manipulating the matrix using the new initial values and comparing the effects produced, on the event sequence scenarios, with the initial run [Ref. 26, p. 115].

4. Critique

Gordon and Hayward recognized that their approach had several weaknesses. These would be expounded upon by later reviewers. The quadratic relationship had been selected due to its intuitive appeal and for convenience, however, the authors were not insistent that it be used. They suggested that other possible forms be examined. Gordon
and Hayward also recognized that there was little justification for assuming mode, strength, and time lag acted linearly. A logistic function was recommended as being more appropriate. The assumed non-effect of non-occurrence was felt to be an oversimplification which could be easily overcome. Finally, in future applications the developers proposed that estimates be obtained by a consensus-building technique such as Delphi [Ref. 26, p. 115].

One of Gordon and Hayward's critics, Enzer, criticized the quadratic adjustment assumption on the basis that it arbitrarily restricted the possible domain of change in $P'_i$. The greatest absolute change in $P_i$ could occur only when $P_i = 50\%$. The quadratic did not allow;

... the occurrence of one event to have a large positive absolute impact on an event whose initial probability is very low, or a large negative absolute impact on an event whose initial probability is very high. [Ref. 35, p. 352].

He notes that although this appears to violate intuitive thinking, it did prevent $P'_i$ from reaching unity or becoming negative.

Enzer also explained the limitations produced by ignoring an event's non-occurrence. He felt that failing to consider non-occurrence leads to ambiguity in defining the initial probabilities. This is because any cross-impact effects which may have been implicitly included in estimating the initial probabilities are not removed. However, Enzer
noted that it may be conceptually difficult to estimate the effect of non-occurrence [Ref. 27, p. 59].

In their estimation of the interrelationships, Enzer felt that Gordon and Hayward had not adequately defined the cross-impact factors [Ref. 27, p. 53]. This problem relates to how estimator responses should be interpreted, as discussed in the preceding chapter. Two other critics, Mitchell and Tydeman, indicated this problem's implications when they observed that Gordon and Harvard's "$...procedure contains no mechanism to ensure that basic pairwise probability relationships remained intact." [Ref. 29, p. 134].

The basic approach had other problems associated with its use. Dalkey points out that relative likelihoods for individual event sequences (scenarios) could not be assessed directly. This was because only binary interactions were considered [Ref. 34].

To make scenario computation useful it will be necessary either to obtain estimates of higher order interactions or find a more logically correct assumption concerning them [Ref. 34, p. 350].

Another problem noted by Mitchell and Tydeman was that the approach lacked an uncertainty measure with which to evaluate the expert's opinions [Ref. 29, p. 134]. Also, as discussed in Chapter Two, Johnson challenged the assumption that probability shifts which were significant from a statistical standpoint could be assumed to be significant from a policy standpoint [Ref. 40].
C. MODIFICATIONS TO THE BASIC APPROACH (ENZER)

In two successive cross-impact analysis applications Enzer attempted to overcome some of the problems discussed above [Refs. 27 and 33]. In his earlier work Enzer retained the basic method's approach to quantifying event interactions, to using a quadratic manipulation, and to ignoring non-occurrence. The major innovation was that he used the Delphi technique to obtain his event set and subjective estimates. This allowed him to extend the analyses he could perform [Ref. 27].

By using the Delphi technique Enzer was able to retain the estimators' opinion spread for each specific relationship examined. Opinion spread is defined as the range between the upper quartile and lower quartile response values, or one standard deviation above and below the mean value. With this information Enzer was able to conduct two analyses more systematically than Gordon and Hayward had. Enzer demonstrated that the mean response values could be used to identify dominant and sensitive events before their probability shifts were determined. In addition, the estimator's opinion spread could be used to indicate estimator uncertainty concerning the potential interactions.

An event's dominance was determined by summing the absolute values contained in a matrix row. Since these represented an event's impact on the other events, this measure was used to identify the events with the greatest overall impact. Event sensitivity was measured by algebraically summing the column values. These values represented
the degree to which all other events influenced a single event's occurrence probability. This measure was used to identify the events which responded most readily to changes in the problem situation.

The opinion spread in a row indicates the estimator's uncertainty regarding how an event's occurrence impacts the other events. The opinion spread in a column indicates the uncertainty concerning how an event is affected by the other events [Ref. 27, p. 55].

In addition to the standard estimates, Enzer elicited respondents' opinions concerning each event's importance. He suggested that these importance ratings, in conjunction with the above measures, can aid in identifying desirable events for resource allocation, and for selecting events to be used in sensitivity analysis. In this case, an important event which is insensitive to the others would require direct intervention, sensitive events might benefit from indirect action, and highly uncertain relationships would require closer analysis and evaluation before a decision could be made [Ref. 27, p. 57].

Although it introduced an uncertainty measure, and permitted more exact causal analysis Enzer's approach suffered from many of the same problems associated with the Gordon and Hayward method. These recurring problems included: the use of the quadratic manipulation, ignoring non-occurrence, and determining how to interpret the respondent's estimates. Furthermore, the Delphi technique,
while extending the analysis, has some inherent problems. Fischer, et. al. cite studies which suggest that the Delphi technique (where individuals make estimates; receive anonymous feedback about the estimates of other group members; and make additional estimates based on the feedback) is a poor way to elicit expert opinion. The studies reviewed in Fischer, et. al. indicate that the best procedure to elicit expert opinion uses a slightly different approach. The recommended procedure is to have the experts make individual estimates; then, bring the group together and allow the experts to discuss their estimates face to face; and finally, have the experts make a second set of individual estimates [Ref. 13, p. 55].

Enzer's second application introduced more fundamental changes to the Gordon and Hayward method. Enzer abandoned the quadratic manipulation, and introduced the concepts of "likelihood ratios" and "constant change of odds" to handle the procedure of manipulating estimates. In this approach, estimates were elicited as changes in probability and non-occurrence was considered. Enzer also attempted to resolve estimate inconsistencies [Ref. 33].

1. Assumptions

Using an event's importance rating, it was possible for Enzer to limit the number of events to be included in the analysis. Selecting the most important events avoided the necessity to specify the entire environment, thereby,
simplifying the analysis. However, this increased the complexity of the estimation process.

Interrelationships were estimated in terms of the change in likelihood of one event ($E_i$) produced by another event's ($E_j$) occurrence. This was defined as $P(i|j)$. The effect of non-occurrence could also be estimated in the same way, and was defined as $P(i|\overline{j})$. If this second estimate was too difficult for respondents to provide it could be calculated using a standard probability relationship [Ref. 33, p. 38]:

$$P(i) = P(j)P(i|j) + (1 - P(j))(P(i|\overline{j}))$$

These values were then used to compute the likelihood (cross-impact) ratio for each event pair [Ref. 34, p. 350]:

$$\lambda_{ij} = \frac{1 - P(j)}{P(j)} \times \frac{P(j|i)}{1 - P(j|i)}$$

This became the factor by which the initial occurrence probabilities were multiplied when an event's occurrence or non-occurrence was decided. Using this ratio expanded
the domain of change possible for an event's initial probability.\textsuperscript{22}

To track the many changes in probability produced by the occurrence or non-occurrence of numerous events, Enzer introduced the concept of "constant change of odds". He stated:

\[ \text{... the judgment concerning the impact on Event A of the occurrence of Event B is independent of the exact probability of occurrence of Event A, and that whenever Event A is preceded by the occurrence of Event B the change in likelihood of occurrence of Event A is known from the initial input. [Ref. 33, p. 41].} \]

This means that once the interaction between two events (A and B) has been estimated, its value is not changed if another event (C) occurs before B and changes event A's initial probability. As long as B occurs before A it will impact A's current probability to the same degree that it was believed to impact A's initial probability.

\textsuperscript{22}As Enzer explains in his earlier work: Changes in probability in the form of quantitative ratios opens the domain to the widest range of possibilities. Several of these are presented in Figure 6 in a form comparable with the previous figure. From Figure 6 it can be seen that an event whose initial probability was 20\% could, if impacted by an event that increased its likelihood by a factor of 20, be raised to 83\%. When the quadratic is used, the maximum positive impact for an event with an initial probability of 20\% is to raise it to 36\%. [Ref. 27, p. 61].
Figure 5. Effect of cross-impact factors when using quadratic equation

Figure 6. Effect of cross-impact factors when using changes in likelihood

\[ R_{CJ} = \text{Change in likelihood of event } R_j \text{ produced by occurrence of event } C_i \]
In order to assure pairwise consistency was maintained in the estimates Enzer adopted the following axioms [Ref. 33, p. 37]:

1. The initial probabilities of event pairs impose limits on the values of the impacted probabilities for that pair.

2. For any event pair, specification of the initial probabilities and one set of impacted probabilities (occurrence or non-occurrence) fixes the remaining set.

Thus, the relationship used to calculate non-occurrence could also be used to check for consistency. A simply boundary rule could then be applied to resolve inconsistencies. Pairwise consistency is required when dealing with probability estimates to insure the calculated probabilities do not exceed unity or become negative. Such values would be meaningless in probabilistic terms.

In applying this boundary rule Enzer assumed that the intention indicated by the respondents' estimates were correct, but that their actual values were incorrect. The boundary rule then makes the least adjustment required to restore consistency. For example, if a value given for \( P(i|j) \) in conjunction with those given for \( P(i) \) and \( P(j) \) produced a computed value for \( P(i|\overline{j}) \) which was <0 or >1, then it was inconsistent. A computer would set the value of \( P(i|\overline{j}) = 1 \) or 0 as required, and recompute \( P(i|j) \) [Ref. 33, p. 38].

2. **Procedure**

Enzer's approach followed the procedure developed by Gordon and Hayward. Candidate events for inclusion in the
analysis were obtained from a Delphi exercise. In order to limit the event set size, only those events considered most important (by subjective rating) were included.

The respondents were then asked to estimate each event's initial probability of occurring by a specified date, considering an environment which might evolve from the present circumstances without conscious human intervention to change the course of events. They were then asked to rate each event's desirability. This rating included two subjective estimates; the desirability of an event to the environmental aspect being considered (+ or -), and its impact on that environmental aspect should the event occur (0 = weak to 10 = strong) [Ref. 33, p. 46]. This desirability rating seems to relate to subjectively assessing whether an event enhances or inhibits policy goals, or whether an event influences a situation in a direction desired by the decision unit.

The respondents were next asked to assess the interrelationships between events. They provided the new likelihood of occurrence for each event given each other event's occurrence (and non-occurrence if possible, otherwise this value was computed). The estimates were then checked for consistency and revised as necessary using the boundary rule.

Likelihood ratios were then computed to fill in the matrix, and the estimates manipulated as in the basic method, using a Monte Carlo simulation.
3. **Analyses Performed**

With this approach Enzer was able to perform all the analyses permitted by the basic approach, including:

1. determining even sensitivity and dominance
2. scenario generation
3. exploring causal relationships
4. conducting scenario sensitivity analysis

In addition he had obtained an indication of respondent uncertainty using opinion spread. Rating events by desirability allowed selected events to be included in the sensitivity analysis. It also permitted choosing the more desirable events as subjects for testing resource allocation strategies.

Furthermore, desirability ratings provided criteria with which specific event sequence scenarios could be evaluated. Using these criteria, it was possible to determine which scenarios were the most desirable, and which strategies produced them.

4. **Critique**

This approach overcame several difficulties associated with the basic approach, specifically it

1. considered non-occurrence
2. eliminated the quadratic assumption
3. demonstrated that expert opinions could be used in analyzing complex situations
4. provided an uncertainty measure for evaluating estimates

Nevertheless, several problems still remain.
It was still difficult to identify significant probability shifts, although the desirability/impact and importance ratings had reduced the necessity for this determination. The interrelationships considered were still only binary, and even with desirability ratings it was still not possible to determine the most probable scenarios. Finally, it was still unclear what the respondents meant when they provided interaction estimates.

This last problem seems to have been, if anything, confounded by Enzer's attempt to introduce classical probability relationships. As Mitchell and Tydeman observed:

A fundamental difficulty with cross-impact analysis is to determine what respondents actually mean when they answer the conditional probability questions normally posed. Results of studies currently in progress indicate that (1) participants are frequently confused and unsure of the interpretation of such questions, and (2) respondents often interpret the question in terms of time-dependent conditional probability statements, namely 'If event A occurred (first), what is the probability of B occurring?' [Ref. 29, p. 133].

In addition, introducing conditional probability relationships stimulated the use of classical probability theory in determining estimate consistency. Also, Jackson and Lawton observe that the classical probability equation used to calculate non-occurrence and test consistency could also be used to derive half the matrix entries once the other half had been specified [Ref. 37, p. 265].
Mitchell and Tydeman point out that, if the cross-impact estimates are interpreted as being time-dependent, Enzer's approach may not be valid.

... the standard observation that
\[ P(A)P(B|A) = P(B)P(A|B) \]
becomes, with the inclusion of time-dependence
\[ P(A)P(B|A_{\text{first}}) = P(B)P(A|B_{\text{first}}) \]
In this restatement equality is not guaranteed - in fact, it would be pure coincidence other than when events A and B were independent. (Ref. 29, p. 135).

The consistency question led Enzer and Alter to address using Bayesian probability in cross-impact analysis. They suggested that confusion in interpretation was caused because the early approaches (Ref. 39, p. 231):

1. Described future events with no real sense of time sequence.
2. Used a data collection technique which blurred the distinction between correlation and causality.

They concluded that conditional probabilities were not directly applicable to causal situations (Ref. 39, p. 237). This conclusion also had been reached in 1972 by Turoff who proposed an alternative approach to cross-impact analysis (Ref. 36).

D. ASSUMED CONSISTENCY (TUROFF) APPROACH

Turoff attempted to accomplish several goals with his approach. One was to develop a method which could determine the causal impact of potential events not specified in the event set. He also wished to establish some relationship between an event's occurrence likelihood and the effort.
invested in either promoting or preventing the event. In presenting his approach Turoff acknowledged that because higher order interactions are difficult to estimate, "we in effect ignore terms of $P^2$ or greater, hoping that the three- or four-way interactions are small." [Ref. 36, p. 326]. Nevertheless, Turoff did attempt to derive a measure of the strength of these higher order interactions.

1. Assumptions

Turoff's approach was based primarily on the assumption that:

Given a set of events which may or may not occur over an interval of time, we assume that an individual asked to estimate the probability of occurrence of each event will supply a 'consistent' set of estimates [Ref. 36, p. 317].

This assumption effectively removed the requirement to check estimate consistency. Instead estimates were obtained using an interactive computer program. In this manner the respondent was shown the results produced by his estimates, and allowed to revise them at will until he felt the model they produced met his expectations.

A second assumption in this approach is founded on information theory, which is used to calculate cross-impact factors ($C_{ij}$) from estimates used to derive values for the effect of occurrence ($R_{ij}$), and non-occurrence ($S_{ij}$) for each event. The assumption was that "if a correlation exists between $R_{ij}$ and $S_{ij}$ is such as to maximize the
added information." [Ref. 36, p. 324]. The effect of this relationship can be shown simply.

If $\varepsilon$ is defined as a quantity close to 0 then [Ref. 36, p. 324],

\[ \text{If } P_j = \varepsilon \quad 1/2 \quad 1-\varepsilon \]

then \[ \frac{dR_{ij}}{dS_{ij}} = \varepsilon \quad 1 \quad 1/\varepsilon \]

and \[ P_i = \frac{R_i + S}{1+\varepsilon} \quad \frac{R+S}{2} \quad \frac{R+\varepsilon S}{1+\varepsilon} \quad R \]

This behaves physically as one would desire, for if $P_j$ is close to one, then a very large change in $R$ is necessary to make a small change in $S$. Conversely, if $P_j$ is close to zero, a very large change in $S$ is necessary to produce a small change in $R$. Also when $P_j = 1/2$ the relative change in $R$ and $S$ is equal. [Ref. 36, p. 322].

Finally, a likelihood measure is used in expressing the probability that an event occurs, called its occurrence ratio ($\phi$). This measure is similar to Enzer's likelihood ratio. Under assumed occurrence or non-occurrence it ranges from $+\infty$ to $-\infty$ [Ref. 36, p. 319]. The occurrence ratio is assumed to be directly proportional to a measure of effort, or [Ref. 36, p. 320]:

\[ \phi P_i \propto E_i^T \]
where

\[ S_i = \text{the occurrence ratio of event } i, \]

and

\[ E_i^T = \text{the total amount of effort expended in either bringing about or preventing } \text{"i"} \]

Assuming that estimators are consistent, the assumed maximization of added information allows a difference equation to be used for cases in which new information is received (i.e., an event's occurrence or non-occurrence becomes certain) [Ref. 36, p. 318]. Assuming certain occurrence \( (P_j = 1) \), then, the approach defines \( R_{ij} = P_i \), where \( R_{ij} \) is the probability of the \( i \)th event given that \( j \) is certain to occur. Turoff then derives a cross-impact factor (occurrence ratio) for occurrence [Ref. 36, p. 321, (eq. 19)].

\[ C_{ij} = \frac{1}{1-P_j}[S_{ij} - S_i] \]

Assuming certain non-occurrence \( (P_j = 0) \), then, the probability of the \( i \)th event given that the \( j \)th event is certain to not occur is defined similarly, \( S_{ij} = P_i \). A cross-impact for non-occurrence is derived [Ref. 36, p. 321, (eq. 21)].

\[ C_{ij} = \frac{1}{P_j}[S_i - S_{ij}] \]
Combining these two factors produces [Ref. 36, p. 321, (eq. 22)],

\[ C_{ij} = \psi_{R_{ij}} - \psi_{S_{ij}} \]

Obtaining values for all the \( C_{ij} \)'s permits calculating \( \gamma_i \), a term assumed to be a function of the unknown variables not specified in the event set [Ref. 36, p. 321, (eq. 23)]

\[ \gamma_i = \psi_{P_i} - \sum_{k \neq i}^n C_{ik} P_k \]

By assuming the most favorable case for event \( i \)'s occurrence, \( P_i^f \), and the least favorable case, \( P_i^u \), two \( \gamma_i \)'s can be computed, \( \gamma_i^f \) and \( \gamma_i^u \). This permits measuring explicitly the inaccuracy caused by ignoring higher order interactions [Ref. 37, p. 327, (eq. 45)].

\[ \gamma_i^f - \gamma_i^u \]

\[ \gamma_i \]

2. Procedure

The Turoff procedure is essentially the same as the basic approach until the point at which scenarios are generated. As in the basic approach it is necessary to: specify the event set, obtain initial probability estimates, and obtain "conditional probability" estimates. These are used to calculate the cross-impact factors as discussed.
previously. If there was no change in estimate from the initial probability then $C_{ij} = 0$. With this information it is possible to calculate the remaining measures described in the preceding section.

Turoff criticized the Monte Carlo procedure as not producing a "consistent set of estimates" because the assumptions underlying it imply estimator inconsistency [Ref. 36, p. 309]. Rather than employing a random process, Turoff generates an event sequence scenario using the assumption that the events are time-independent in their occurrence.

The first step under this assumption is to select the event whose initial probability is closest to 1 or 0. If $P(i)$ is close to zero he assumes the event did not occur, if it is close to one it is assumed to have occurred. Based on this decision the probabilities for the remaining events are recalculated using the appropriate $C_{ij}$. This process is repeated using the events' new probabilities until all events have been decided [Ref. 36, p. 331]. This produces a "unique" scenario. Other possible scenarios are produced by changing the initial probability estimates and repeating the above procedure. This is in effect, sensitivity analysis as done in the other two approaches.

3. **Analyses Performed**

In presenting his approach, Turoff demonstrates only a sensitivity analysis. As in the basic approach, this is
accomplished by adjusting one or more of the initial probabilities and holding the remaining probabilities and the cross-impact factors constant. In addition to reflecting a conscious policy decision, this is the method whereby the estimator determines if the behavior of the model built from his responses is in accordance with his expectations. If he is not satisfied, it is at this point that he goes back and changes his initial and/or conditional estimates [Ref. 36, p. 331].

Although other types of analysis were not demonstrated it seems most could be accomplished using this approach. Event dominance and sensitivity could be derived from Turoff's cross-impact matrix using a procedure similar to Enzer's. Since Turoff's cross-impacts are presented as a type of correlation coefficient (± in range), an indication of event desirability might be obtained through simple summing of the positive or negative effects. Desirability analysis would depend primarily on how the events were formulated.

Turoff's matrix also includes a measure (Gamma) of the effects of events not specified in the event set (and higher order interactions). This can be interpreted as an uncertainty measure. Estimator uncertainty could also

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23 The use of correlation coefficients offers an alternate method of interpreting respondent's meanings when they answer the cross-impact questions. Its implications and possible uses will be explored in Chapter Five.
be obtained by computing the range of opinion given by a group of estimators.

4. Critique

Two major conceptual problems exist in Turoff's technique. The first of these arises from the assumption that estimators can be expected to provide consistent responses. Mitchell and Tydeman reject this assumption stating:

[Turoff] argued that there is no need for usual traditional probability relationships to hold and included a small example to support this assertion. In this example, he considered two time specific events and by undertaking usual conditional probability analysis concluded that \( P(A|B) \) and \( P(B|A) \) were not standard conditional probabilities. This is not surprising given the definitions which Turoff used; in fact, the finding is consistent with a time-dependent interpretation of conditional probability. The result does not support his claim that traditional probability relationships are irrelevant to cross-impact studies, and that violation of the usual probability relationships can be justified. The fact that people answer as though an ordering among events was implied seems to be a reason for explicitly recognizing this fact in the definition of the probability statement rather than ignoring it. [Ref. 29, p. 135].

It is difficult to conceptualize a situation in which an individual is able to operationalize all the relevant components of a complex problem, and quantify their interrelationships to produce a consistent set of probability statements defining his paradigm on demand.
Furthermore, assuming consistency removes the formal structure provided the methodology by classical probability theory. Lacking an empirical base in the inexact sciences, it seems difficult to select an appropriate manipulation technique without some such formal theoretical basis.

The second conceptual problem arises in the scenario generation process. By assuming time-independence Turoff produced one scenario, or event outcome sequence, but there seems to be little justification for assuming that it is unique. The assumption that the most probable event in a situation would occur first, or indeed occur at all, is debatable. This would be especially true in a situation characterized by surprise. This indicates that the procedure was established arbitrarily and that several others could have been devised which would have functioned equally well (e.g., assuming the least probable event occurs and the most likely does not). Without some method of identifying and ranking all possible outcomes, production of a single scenario seems pointless.

A final criticism of this technique involves its procedure. Because respondents had to reiterate their estimates until satisfied with the resulting output, an interactive computer system was required. To replicate this reiteration process for several respondents manually would require an excessive number of calculations be performed, and much time be expended in querying respondents.
The approach to be discussed in the next section seems to overcome these problems.

E. CROSS-EVENT ANALYSIS (MITCHELL AND TYDEMAN)

This approach was developed by Mitchell and Tydeman and presented in 1978 as a variation to Duperrin and Godet's SMIC-74, which is discussed in the following section. As has been shown, Mitchell and Tydeman felt it was inappropriate to ignore time dependence when obtaining estimates. They felt that respondents normally interpret the questions posed for eliciting the conditional probabilities in a time-dependent manner. Mitchell and Tydeman attempted to use these time-dependent estimates to derive classical conditional probabilities [Ref. 39].

Mitchell and Tydeman also recognized that the elicited information could be inconsistent in terms of classical probability relationships. To minimize this problem they used average group responses which reduced the instances of pairwise inconsistency. In order to correct inconsistencies which did manifest themselves, they developed two fitting procedures, least squares and minimum standard deviations. These procedures will be reviewed below, the authors also suggested that Enzer's boundary rule could be used to resolve inconsistencies [Ref. 23, p. 18].

1. Assumptions

The major difference between this and the other approaches is that it uses causal time-dependent subjective
probability estimates to identify first order interrelationships among selected events, defining them as classical probability relations. This approach uses a specific time horizon, rather than treating time as a random variable.

Subjective estimates were obtained which completely identified the eight possible ordered outcomes permitted by any event pair. These outcomes can be identified explicitly for any event pair \((i,j)\), and each has an associated unique probability \((P_1 \text{ through } P_8)\). These are [Ref. 29, p. 139]:

\[
\begin{align*}
P_1 + P_2 + P_3 + P_4 + P_5 + P_6 + P_7 + P_8 &= 1 \\
\end{align*}
\]

Since these outcomes are exhaustive and mutually exclusive, certain conditions must apply [Ref. 39, p. 138]:

\[
\begin{align*}
P_1 + P_2 + P_5 + P_7 &= P(i) \quad \text{eq. 2} \\
P_1 + P_3 + P_5 + P_6 &= P(j) \quad \text{eq. 3}
\end{align*}
\]
The authors feel that respondents can be expected to supply four time-dependent conditional probabilities [Ref. 39, p. 139].

\[
P(i|j_{\text{first}}) = C_1 = P_5 \div (P_5 + P_6) \quad \text{eq. 4}
\]
\[
P(j|i_{\text{first}}) = C_2 = P_1 \div (P_1 + P_2) \quad \text{eq. 5}
\]
\[
P(i|\overline{j}_{\text{first}}) = C_3 = P_7 \div (P_7 + P_8) \quad \text{eq. 6}
\]
\[
P(j|\overline{i}_{\text{first}}) = C_4 = P_3 \div (P_3 + P_4) \quad \text{eq. 7}
\]

A fifth time-dependent relationship was also presented for estimation [Ref. 29, p. 139].

\[
P(i_{\text{first}} | i \ \text{and} \ j \ \text{occur}) = C_5 = P_1 - (P_1 + P_5) \quad \text{eq. 8}
\]

Solving these eight relationships as simultaneous equations, the developers demonstrate that the probabilities for an event pair's ordered outcomes can be calculated from the information provided by the respondents' estimates [Ref. 29, p. 140].

\[
P_1 = \frac{(C_3C_4) - (C_3P_1) - (C_4P_1)}{\gamma - \alpha C_4 - \beta C_3} \quad P_2 = \left[ \frac{(1-C_2)}{C_2} \right] P_1
\]

If these last two equations are too difficult to estimate, the developers derive a method whereby they can be computed [Ref. 29, p. 141].
\[ P_3 = P_1 - \frac{\alpha P_1}{C_5} \quad P_4 = \left[ \frac{(1-C_4)}{C_4} \right] P_3 \]

\[ P_5 = \left[ \frac{(1-C_5)}{C_5} \right] P_1 \quad P_6 = \left[ \frac{(1-C_1)}{C_1} \right] P_5 \]

\[ P_7 = P_1 - \left[ \frac{(\alpha P_5)}{C_5} \right] \quad P_8 = \left[ \frac{(1-C_3)}{C_3} \right] P_7 \]

where:

\[ \alpha = (1-C_5) + \frac{C_5}{C_2} ; \]

\[ \beta = [(1-C_5) - C_1] + C_5 , \text{ and} \]

\[ \gamma = \frac{(C_5 C_1) + C_2 - (C_5 C_2)}{(C_2 C_1)} \]

Using these relationships Mitchell and Tydeman calculate the classical conditional probabilities for each event pair [Ref. 29, p. 140].

\[ P(i|j) = \frac{(P_1 + P_5)}{(P_1 + P_2 + P_5 + P_7)} \]

\[ P(j|i) = \frac{(P_1 + P_5)}{(P_1 + P_3 + P_5 + P_6)} \]

As mentioned earlier, the developers derived a method to calculate non-occurrence if it could not be estimated. To calculate the conditional probabilities without estimating non-occurrence Mitchell and Tydeman adopt the following procedure. To obtain conditional probabilities one of the relationships needed is:
\[ P(i \text{ and } j) = P_1 + P_5 \]

or

\[ P(i \text{ and } j) = P(i \text{ and } j \text{ first}) + P(j \text{ and } i \text{ first}) \]

\[ = P(i|j \text{ first}) P(j \text{ first}) + P(j|i \text{ first}) P(i \text{ first}) \]

This can be obtained by estimating: \( P(i \text{ first}) \) and \( P(j \text{ first}) \)

or this can be approximated by:

\[ P(i_f) = P(i_f|i \text{ } j) P(i) \text{ and similarly for } P(j_f) \]

Substituting:

\[ P(i \text{ and } j) = C_5 C_2 P(i) + (1 - C_5) C_1 P(j) \]

which is:

\[ P(i \text{ and } j) = P_1 + P_5 + E \]

where the error \( E \) is small for independent events, and more significant for highly correlated events (10-20%) [Ref. 29, p. 141].

\[ E = \frac{(P_1/P_1+P_2)[(P_1 P_7 - P_2 P_5)/(P_1+P_5)] + (P_5/P_5+P_6)(P_3 P_5 - P_1 P_6)}{(P_1+P_5)} \]
Inconsistency is manifested when a negative value is calculated for any of the probabilities $P_1$ through $P_8$. Standard fitting procedures may be used to resolve inconsistencies by hypothesizing that there exists a "true" or consistent value (*) for each respondent's estimate. This value is determined to be one which is "as close as possible" to the respondent's estimates and makes all $P_1, \ldots, P_8 > 0$. The developers present two procedures which utilize this hypothesis: least squares, and minimum standard deviations [Ref. 29, p. 142].

The least squares procedure produces a minimization program "with a quadratic objective function and non-linear constraints" [Ref. 29, p. 142]. This program would not be easy to solve by hand. Minimizing the absolute standard deviations produces a moderately sized linear program with linear constraints [Ref. 29, p. 143-4]. In addition this program could be expanded to provide for overall consistency by including scenario probabilities and terms for higher order interactions [Ref. 29, p. 145]. If this correction procedure proves too lengthy, the authors suggest Enzer's boundary rule could be used to resolve pairwise inconsistencies.

2. **Procedure**

To obtain the events for analysis the authors used a procedure they termed "event assessment". For each candidate event, the respondents provide not only the
likelihood that the event occurs within a specified time horizon, but an estimate of its significance given that it occurs. An event impact score is then calculated as a weighted function of the product of probability and significance. In this way an analysis event set can be selected from the events having the highest impact scores, probabilities, or significance ratings [Ref. 23, p. 8].

The next step is to determine the events' time-dependent conditional probabilities by eliciting responses for questions structured to provide values for equations four through eight. These responses are aggregated and used to compute the ordered outcome probabilities $P_1$ through $P_8$, which are used to compute the classical conditional probabilities. If any inconsistencies appear in this phase (any $P_1$ through $P_8 < 0$), they are eliminated using the boundary rule or fitting technique.

The next step is to generate scenarios, or event sequence outcomes. For this procedure Mitchell and Tydeman used a variation of the Duperrin and Godet technique. This technique assumes that for an $n$-event system there are $r = 2^n$ states (scenarios). Each state "$E_k$" has a unique probability $\pi_k$ [Ref. 48, p. 305].

An event's theoretical probability $P^*(i)$ is defined as its frequency of occurrence in all the possible states [Ref. 49, p. 64].
\[ p^*(i) = \sum_{k=1}^{r} \theta_{ik} \pi_k \quad \text{for all } i \]

where

\[ \theta_{ik} = \begin{cases} 1 & \text{if event } i \text{ forms part of } E_k \\ 0 & \text{otherwise} \end{cases} \]

A similar definition can be applied to the theoretical conditional probabilities \( P^*(i|j) \) [Ref. 49, p. 64].

\[ p^*(i|j) = \sum_{k=1}^{r} t(ijk) \pi_k / P^*(j) \quad \text{for all } i,j \]

where

\[ t(ijk) = \begin{cases} 1 & \text{when events } i \text{ and } j \text{ form part of } E_k \\ 0 & \text{otherwise} \end{cases} \]

and

\[ p^*(i|\overline{j}) = \sum_{k=1}^{r} s(ijk) \pi_k / (1 - P^*(j)) \quad \text{for all } i,j \]

where

\[ s(ijk) = \begin{cases} 1 & \text{when events } i \text{ and } \overline{j} \text{ form part of } E_k \\ 0 & \text{otherwise} \end{cases} \]
Recognizing standard probability constraints [Ref. 49, p. 65]:

\[ 0 \leq P^*(i) \leq 1 \]

\[ P^*(i|j) = P^*(j|i)P^*(i) = P^*(ij) \]

\[ P^*(i|j)P^*(j) + P^*(i|\overline{j})P^*(\overline{j}) = P^*(i) \]

produces:

\[ \sum_{k=1}^{r} t(ijk) \pi_k = P^*(ij) = P^*(ji) \]

and

\[ P^*(i|\overline{j})P^*(\overline{j}) = \sum_{k=1}^{r} s(ijk) \pi_k = P^*(i) - P^*(ij) \]

Therefore, given a consistent probability set, any set of \( \pi_k \) values which satisfy:

\[ P^*(i) = \sum_{k=1}^{r} \theta_{ik} \pi_k \quad \text{for } i = 1, 2, \ldots, n \]

\[ P^*(ij) = \sum_{k=1}^{r} t(ijk) \quad \text{for } i = 1, 2, \ldots, n-1; \ i < j \leq n \]

and
\[ \sum_{k=1}^{\infty} \pi_k = 1 \quad \pi_k \geq 0 \quad \text{for all } k \]

are possible solutions to the scenario probabilities [Ref. 49, p. 65].

Instead of the Duperrin and Godet quadratic objective function, Mitchell and Tydeman solve a linear equation in terms of consistent probabilities to obtain a unique solution. This program is [Ref. 49, p. 65-6]:

\[
\begin{align*}
\text{minimize } Z &= \sum_{ij} [P(i|j)P(j) - P^*(ij)]^2 + \sum_{ij} [P(i|j)P(j) - P^*(ij)]^2 \\
&+ P^*(ij) \\
\text{subject to: } &\sum_{i=1}^{n} P^*(i) = \sum_{i=1}^{n} \sum_{j=i+1}^{n} P^*(ij) \leq 1 \\
&\begin{cases}
P^*(ij) > 0 & \text{all } j > i \\
\end{cases} \\
&\begin{cases}
P^*(i) \leq 1 & \text{all } i \\
\end{cases} \\
&\begin{cases}
P^*(i) \geq P^*(ij) & \text{all } j > i \\
P^*(j) \geq P^*(ij) & \text{all } j > i \\
\end{cases}
\end{align*}
\]

3. Analyses Performed

The cross-event approach uses a different method to determine event dominance and sensitivity. An event's dominance may be estimated by summing, for all other events,
the absolute deviation of the conditional probability, given that the event occurred first, minus the event's original probability. This value can be standardized, or an "elasticity" measure adopted to reflect event likelihood. An event's sensitivity can be computed in a similar fashion [Ref. 23, p. 12].

Although it was not demonstrated, causal relationships could be traced as in the other approaches by filling in the cross-event matrix. This would be useful in an analysis Mitchell and Tydeman term "system impact analysis" which evaluates the possible event sequence scenarios' worth.

System impact analysis used additional subjective ratings concerning an event sequence scenario's expected impact (magnitude and direction) on specified system components and the "expected consequences for system outcomes (performance measures)" (i.e., desirability) [Ref. 23, p. 14]. In this manner a different set of possible response actions may be identified for each scenario.

The final analysis they suggest is "strategy evaluation". This procedure relates a set of feasible potential strategies (response actions as determined using system impact analysis) to each event sequence scenario (the most probable ones), and uses a set of objective criteria (obtained from the decision-makers) to evaluate the strategies for each possible situation [Ref. 23, p. 15].
4. Critique

A major advantage in this approach is that it eliminates the difficulty in interpreting estimator responses. Estimators are asked for time-dependent relationships which are then used to calculate classical conditional probabilities. Furthermore, if non-occurrence is too difficult for respondents to conceptualize, it can be calculated, introducing a small error.

The capability to compute the conditional probabilities results in the further advantage of providing a logical background for the analysis. Classical probability relationships, it is suggested, can be used to insure consistency and resolve inconsistencies without requiring respondents to re-estimate. In addition, the procedure develops a method for calculating and ranking event sequence outcome probabilities.

With the scenario ranking, introducing subjective estimates concerning system impact and objective measures for comparison extends the types of decision-aiding analysis which can be performed. With the Mitchell and Tydenman method it is apparently possible to address questions relating to the event sequence scenarios' desirability and strategy effectiveness. However, in system impact analysis:

Problems still face the analyst, for example, eliciting an exhaustive objective set, ensuring mutual independence of objectives, devising procedures for measuring outcomes, determining consistent weightings for the objectives
and specifying procedures for aggregation. [Ref. 23, p. 15].

These problems seem even more complex for decisions involving national objectives and foreign policy options.

A final difficulty lies not in the conceptual realm, but in the method's implementation. Generating the scenario probabilities with the linear equation for a large event set would be very difficult without access to a computer. In order to replicate this process manually it appears necessary to severely limit the event set to be analyzed.

F. OTHER APPROACHES

Besides the approaches to cross-impact analysis discussed so far, several additional techniques have been proposed. These techniques were concerned primarily with assessing the relative rankings among the event sequence scenarios. They also introduced alternative methods to insure estimate consistency, and to resolve inconsistencies.

These techniques took significantly different approaches towards resolving these problems than the techniques just reviewed. However, each approach requires a computer package. Thus they were evaluated as being inappropriate for demonstration and analysis in the present project. It was felt to be impractical to replicate their procedures for confirming consistency, establishing probability bounds and revising estimates using manual methods. However, these approaches have merit in presenting promising alternatives.
to cross-impact analysis and will be discussed briefly. This discussion is offered in the interest of completeness, and to justify the conclusion to omit them from evaluation.

1. **SMIC-74 (Duperrin and Godet)**

Duperrin and Godet felt that cross-impact analysis could be used to construct and rank event sequence scenarios. In recognition of the fact that the estimators could be inconsistent in stating probabilities, they attempted to derive "theoretical" scenario probabilities which were implied by the estimator responses. Using those implied probabilities they attempted to revise the estimated responses to fit the theoretical scenario probabilities and produce a consistent set of estimate. The following diagram summarizes their procedure [Ref. 48, p. 306].

![THE SMIC-74 PROCESS](image)

In order to accomplish this process Duperrin and Godet developed a minimization program to minimize the
difference between the estimated factors $P(i|j)$ resulting from the experts' responses and the theoretical factors, $P^*(i|j)$ and $P^*(i)$, expressed in terms of even sequence scenario probabilities, $\pi_k$, [Ref. 48, p. 306]. The rationale behind this approach was covered in the Mitchell and Tydeman review. The Duperrin and Godet procedure utilized a minimization program of quadratic form with linear constraints [Ref. 48, p. 306-7].

$$\text{minimize } Z = \sum_{ij}^n [P(i|j)P(j) - \sum_{k=1}^r t(ijk)\pi_k]^2$$

$$+ \sum_{ij}^n [P(i|\bar{j})P(j) - \sum_{k=1}^r s(ijk)\pi_k]^2$$

subject to $\sum_{k=1}^r \pi_k = 1$, $\pi_k \geq 0$, for all $k$

Obviously, solving this program would involve utilizing a large computer package.

Furthermore, according to Mitchell and Tydeman the ranking produced is not unique "in that the quadratic programme has other possible solutions", and the "number of probability sets which satisfy the quadratic is potentially very large" [Ref. 49, p. 64]. These conclusions led Mitchell and Tydeman to propose their approach discussed previously.
2. **Sequential Approach (Sarin)**

Sarin's approach is concerned primarily with event sequence scenario generation. Sarin derived a large set of classical probability constraints which information elicited on initial and conditional probabilities must satisfy in order to be consistent (e.g., for a set of six events there are sixty-four conditions the initial probabilities alone must satisfy to be consistent.) [Ref. 38, p. 54-5]. He then develops a set of linear equations with which to compute the \(2^n\) possible event sequence outcome probabilities and satisfy the constraints [Ref. 38, p. 59-60].

Sarin proposes that an interactive computer program be used in conducting the analysis. The program checks the estimator inputs for consistency, computes and supplies bounds for further estimates, and uses the consistent inputs to solve the linear equations producing the scenario probabilities [Ref. 38, p. 58]. This approach solves the consistency problem through providing respondents with immediate feedback.

In this approach, it is possible to consider higher-order interactions with the computer's aid. Because these interactions are often so tightly bound it becomes unnecessary to estimate them [Ref. 38, p. 59]. Sarin also concludes that each discrete event influences only two scenarios, or event outcome sequences, and it is therefore possible to conduct sensitivity analysis through considering, and changing initial values for, only the events which influence the top
ranked scenarios. In this manner it is possible to establish bounds on $P(i)$ under which the scenario ranking does not change [Ref. 38, p. 60]. Similar bounds can be computed for the conditional probabilities, each of which influence only four scenarios.

Once again, the need for an interactive computer program makes demonstrating this approach infeasible in the current study. Furthermore, no mention is made of conducting the other types of analysis (event dominance, sensitivity, and tracing causal effects) which would be necessary in a problem considering short term effects. Although such analyses could undoubtedly be accomplished, it would require making major modifications to the program.

3. KISM (Kane)

In 1972, Kane advanced a cross-impact procedure which dealt with developing trends rather than discrete events. His trend variables behaved in a logistic fashion (as Gordon proposed). In this formulation the net effects of the cross-impact coefficients went to zero as the trends reached their maximum or minimum values [Ref. 47, p. 132]. If these values are restricted to a range between one and zero, the impact of one trend on another is given by [Ref. 47, p. 133]:

$$x_i(t + \Delta t) = x_i(t)^P_i$$

where
\[ P_i(t) = \frac{1 + \frac{\Delta t}{2} \sum_{j=1}^{n} (|a_{ij}| - a_{ij}) x_j}{1 + \frac{\Delta t}{2} \sum_{j=1}^{n} (|a_{ij}| + a_{ij}) x_j} \]

or

\[ P_i(t) = \frac{1 + \Delta t |\text{sum of negative impacts on } x_i|}{1 + \Delta t |\text{sum of positive impacts on } x_i|} \]

where

\[ t = \text{time} \]
\[ a_{ij} = \text{the cross-impact value} \]
\[ x_i = \text{trend } i \]
\[ x_j = \text{trend } j \]

The relationship was modelled on a computer using the differential [Ref. 49, p. 133].

\[ \frac{dx_i}{dt} = - \sum_{j=1}^{n} a_{ij} x_i x_j \ln x_i \]

These developments can be modelled for any time increment and analyzed by varying the initial assumptions regarding the probabilities of the trends and the cross-impacts. Initial
trend and cross-impact values were obtained as in the standard approaches [Ref. 47, p. 131].

This approach's intuitive appeal is apparent from the computer output generated, which shows the interactions as they develop over time. A sample output for a transportation study is presented below along with the cross-impact matrix from which it was derived. The values in the matrix are a series of +'s and -'s which were converted directly to integer values. Another interesting point is that a trend can impact itself in this approach. Initial probabilities for the trends as established by the developer were [Ref. 47, p. 137]:

Auto Use = .8  
Comfort = .6  
and Convenience  
Freedom = .6  
Speed = .5  
Auto Cost= .2

<table>
<thead>
<tr>
<th>Impact</th>
<th>CSS</th>
<th>AUTO USE</th>
<th>C &amp; C</th>
<th>SPEED</th>
<th>OUTSIDE</th>
<th>AUTOMATIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Auto Use</td>
<td>-</td>
<td>++</td>
<td>++</td>
<td>++</td>
<td>++</td>
<td>++</td>
</tr>
<tr>
<td>Comfort</td>
<td>++</td>
<td>-</td>
<td>++</td>
<td>++</td>
<td>++</td>
<td>++</td>
</tr>
<tr>
<td>Freedom</td>
<td>++</td>
<td>-</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>++</td>
</tr>
<tr>
<td>Speed</td>
<td>++</td>
<td>-</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>++</td>
</tr>
<tr>
<td>Auto Cost</td>
<td>++</td>
<td>-</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>++</td>
</tr>
</tbody>
</table>

![Projected Trends]

Figure 1. Projected trends as set by the impact matrix given in Table 2.
Lipinski and Tydeman have attempted recently to extend KISM to include a consideration of discrete events, non-constant trends, and their interactions [Ref. 50]. As with the other approaches discussed in this section this method suffers from the requirement that a large computer package be available for demonstration.

G. MAJOR APPROACH EVALUATION

Four primary approaches to cross-impact analysis have been identified and explained.

The Basic Method — Attempted to elicit quantitative values for interactions among events and revised the initial probability estimates through a quadratic manipulation. The cross-impact concept used was incompletely defined, and subject to several interpretations.

Enzer's Modification — Obtained estimates in terms of likelihood ratios, included non-occurrence, addressed pairwise consistency, and revised the conditional probability estimates.

The Turoff Approach — Assumed estimator consistency, used inputs to derive correlation coefficients, and attempted to identify a unique scenario.

Cross-Event Analysis — Derived conditional probability relationships from causal time-dependent estimates and used a linear program to identify and rank scenarios.

Although the major problems associated with each of these approaches were identified in the discussion, selecting an approach for application cannot be made unless the approaches are systematically compared. The evaluation criteria developed in Chapter Two will be used for this purpose. Those criteria were:
1. Is the event scope adequate?
2. Can events be rated on importance/desirability?
3. What types of analysis are permitted?
4. Is the approach computer adaptable?
5. Are required estimates clearly formulated?
6. Are estimates consistent, or can consistency be obtained?
7. What manipulation algorithm is used?
8. Is the procedure logical/justifiable?
9. How is consistency obtained?
10. How are scenarios generated, can they be ranked?
11. How many estimates are required?
12. What types of computations must be performed?
13. How many terms are involved?
14. How many calculations are required?

1. Evaluation

The following table summarizes the findings discussed in the preceding sections in relation to these evaluation criteria. The four primary cross-impact approaches identified form the column headings. Each entry in the table represents a brief summary of how an approach was evaluated as to meeting the numbered criteria which form the row headings. Specific conclusions based on this evaluation will be presented in the selection section of this chapter which follows Table One.

A few of the criteria were omitted from the table because they were met equally well by all approaches. These
<table>
<thead>
<tr>
<th>CRITERION</th>
<th>BASIC METHOD (GORDON)</th>
<th>MODIFIED METHOD (ENZER)</th>
<th>ALTERNATIVE METHOD (TUROFF)</th>
<th>CROSS-EVENT (MITCHELL AND TYDEMAN)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>sensitivity</td>
<td>sensitivity</td>
<td>for higher order</td>
<td></td>
</tr>
<tr>
<td></td>
<td>b. Sensitivity</td>
<td>b. Trace causal effect</td>
<td>effects and unspecified</td>
<td>b. System Impact</td>
</tr>
<tr>
<td></td>
<td>analysis</td>
<td>more explicitly</td>
<td>events.</td>
<td>Analysis (response</td>
</tr>
<tr>
<td></td>
<td>c. Attempted</td>
<td>c. Estimated uncertain-</td>
<td></td>
<td>options)</td>
</tr>
<tr>
<td></td>
<td>to trace</td>
<td>ty.</td>
<td></td>
<td>c. Scenario evaluation</td>
</tr>
<tr>
<td></td>
<td>causal linkages.</td>
<td>d. Sensitivity</td>
<td></td>
<td>(ranking and</td>
</tr>
<tr>
<td></td>
<td></td>
<td>analysis</td>
<td></td>
<td>desirability)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>e. Evaluated desirability of scenarios.</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.</td>
<td>Cross-impacts not</td>
<td>Possible confusion when</td>
<td>Assumes consistency,</td>
<td>Causal time-dependent relations-</td>
</tr>
<tr>
<td></td>
<td>defined precisely,</td>
<td>relating estimates to</td>
<td>defines estimates as</td>
<td>ships elicited</td>
</tr>
<tr>
<td></td>
<td>ignored non-</td>
<td>conditional probability</td>
<td>conditional probability</td>
<td></td>
</tr>
<tr>
<td></td>
<td>occurrence</td>
<td></td>
<td>computes correlation</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>coefficients.</td>
<td></td>
</tr>
<tr>
<td>6.</td>
<td>Not addressed</td>
<td>Attempts to assure</td>
<td>Assumed</td>
<td>Uses causal time-</td>
</tr>
<tr>
<td></td>
<td></td>
<td>pairwise consistency</td>
<td></td>
<td>dependent estimates</td>
</tr>
<tr>
<td></td>
<td></td>
<td>using classical</td>
<td></td>
<td>to derive classical</td>
</tr>
<tr>
<td></td>
<td></td>
<td>probability.</td>
<td></td>
<td>conditional probabilities</td>
</tr>
<tr>
<td>7.</td>
<td>Quadratic</td>
<td>Estimated factor</td>
<td>Computed factor</td>
<td>Computed factor</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(algebraic)</td>
<td>(algebraic)</td>
<td>(algebraic)</td>
</tr>
<tr>
<td>8.</td>
<td>Several problems.</td>
<td>Some basis. Combining</td>
<td>Assumes consistency which</td>
<td>By completely enumerating event</td>
</tr>
<tr>
<td></td>
<td></td>
<td>causal estimates with</td>
<td>is debatable.</td>
<td>pair outcomes derives</td>
</tr>
<tr>
<td></td>
<td></td>
<td>classical probability</td>
<td></td>
<td>conditional probabilities.</td>
</tr>
<tr>
<td>CRITERIA</td>
<td>BASIC METHOD</td>
<td>MODIFIED METHOD</td>
<td>ALTERNATIVE</td>
<td>CROSS-EVENT</td>
</tr>
<tr>
<td>----------</td>
<td>--------------</td>
<td>-----------------</td>
<td>-------------</td>
<td>-------------</td>
</tr>
<tr>
<td>9.</td>
<td>No</td>
<td>Apply boundary rule (assumed estimator intent correct)</td>
<td>No</td>
<td>Fitting procedures</td>
</tr>
<tr>
<td>10.</td>
<td>By final probability rank. (not unique)</td>
<td>Monte Carlo procedure. (no rank)</td>
<td>Assumed time-independence. (not unique)</td>
<td>Linear program (probability ranking)</td>
</tr>
</tbody>
</table>
| 11.      | a. $P_i's = n$  
b. date = n  
c. $P(i|j)'s = 2(n^2-n)$ (mode and strength)  
Total = $2n^2$ | a. $P_i's = n$  
b. rating = n  
c. $P(i|j) = (n^2-n)$  
d. $P(i|j) = (n^2-n)$ (optional)  
e. $P_i's$ desirability = n  
Total = $n^2+2n$ (option = $2n^2+n$) | a. $P_i's = 2n$  
b. Cond. = $n^2-n$  
c. Gamma = $2n$  
d. $C_5 = \frac{n^2-n}{2}$  
Total = $n^2+n+\left(\frac{n^2-n}{2}\right)$ | |
| 12.      | a. Quadratic | a. Likelihood ratio (Occ. and non-occ.)  
b. Bayesian probability (non-occurrence and consistency) | a. $C_{ij's}$  
b. $\gamma_i$  
c. effect of higher order interactions | a. $P_i=8$  
b. Conditionals  
c. Linear program |
| 13.      | a. 3  
b. 4 | a. 2  
b. $n$  
c. 3 | a. various  
b. 4  
c. 6 | |
| 14.      | a. $n(n-1)$  
b. optional for each event (plus any inconsistencies) | a. for each event pair  
b. each event (n)  
c. each event (n) | a. each event pair (8 $x_{ij}$)  
b. each event (2n)  
c. once | |
general criteria will be commented on below. In considering the last three criteria which addressed the required computations' form and number (criteria 12, 13, and 14), two assumptions were made: (1) The types of computations and number of terms (criteria 12 and 13) include all possible computations which could be necessary (including computing cross-impacts and resolving inconsistencies) in demonstrating the approach, except for those involved in aggregating estimates to produce an average value. These computations would not be approach dependent. (2) The number of computations (criterion 14) does not include computations required in either aggregation nor resolving inconsistencies, as the latter depends on the knowledge of the respondents.

The general criteria were found to be:

a. Event Scope (1)

Event formulation in all the methods can cover any subject or combination of subjects. The only restrictions concern the linkages between events, and the way in which events are stated. These restrictions apply equally to all approaches.

b. Event Rating (2)

Although each approach did not rate events for selection for analysis, the procedures proposed by Enzer and by Mitchell and Tydeman are flexible enough to be applied in any cross-impact analysis. Thus once a technique is selected it is necessary only to select a method to evaluate the events,
and explain the criteria for subjective estimates to the respondents.

c. Computer Adaptability (4)

Each method reviewed acknowledged that a computer would be necessary in order to deal with a large event set. Turoff's approach required that an interactive computer be available to query respondents, and present them with the results produced by their estimates. Enzer proposed that a computer be used to provide probability bounds based on estimator responses for each event pair. It appears that all necessary calculations could be easily programmed, and that a software package could be developed to elicit responses for any type of event. Therefore, it is felt that all the approaches may be considered computer adaptable.

The evaluation of each approach in relation to the remaining criteria is presented in Table One. This evaluation highlights the major differences between each approach.

2. Selection

As the discussion below indicates, of the four major cross-impact approaches evaluated, the Turoff method seems to be the least promising for demonstration in this study. The basic (Gordon) method was developmental and substantially extended by Enzer. Enzer's approach, however, involved difficulties in relating respondents' estimates (which could be interpreted as providing causal time-dependent probabilities)
with classical probability theory. This shortcoming would make it difficult to explain the technique to respondents. In contrast, the Mitchell and Tydeman approach develops procedures to calculate classical conditional probabilities from the apparently time-dependent estimates, and provides a scenario ranking algorithm. For these reasons it was selected for demonstration in this study. The following discussion will present the rationale behind these conclusions, and indicate anticipated problems in implementing the selected approach.

Due to its assumption that estimators are consistent, the Turoff approach requires that they be allowed to revise their estimates until satisfied with the model produced. This requirement, as mentioned previously, would be hard to meet in a manual demonstration. The assumption of consistency cannot be validated because the cross-impacts are calculated in terms of correlation coefficients (ranging, however, from $+\infty$ to $-\infty$), which do not reveal inherent inconsistencies as do probabilities when they exceed unity or become negative.

The Turoff approach is further limited by its time-independence assumption for scenario generation. This produces only one scenario for each set of estimates, and there is no reasonable basis for assuming that it is either a unique or most probable scenario. Finally, the time-independence assumption would be unworkable in an analysis.
attempting to examine the effects produced by discrete response options which might be implemented in reacting to a developing crisis situation. The rationale and structure of this type of analysis will be developed more fully in the extension section of this chapter which follows.

The basic cross-impact approach, developed by Gordon and Hayward, while important in introducing the technique's basic concepts and potential applications was primarily a developmental approach. As such it suffered from several conceptual shortcomings which were eliminated in later approaches. These shortcomings were reviewed extensively elsewhere in this study, and stem from the use of the quadratic manipulation technique, ignoring non-occurrence, and incomplete explanation of the cross-impact factors. Because this approach was greatly modified by Enzer it was decided to eliminate it from further consideration for selection.

Enzer's modified approach dealt with many of the problems inherent in the basic method. He developed an uncertainty measure, addressed non-occurrence and consistency, and eliminated the quadratic manipulation. However, in developing these improvements he failed to solve the problem of how to interpret estimator responses. Enzer recognized that causal relationships were being elicited, but used classical probability relationships to compute non-occurrence and resolve inconsistencies. The cross-impacts were defined as likelihood ratios denoting an event's change in probability given the occurrence of another event. This change was
denoted by the conditional probability relationship \( P(i|j) \), however, the actual relationship seems to involve time-dependence. Therefore, this approach seems to be limited by the incomplete incorporation of two types of probabilistic relationships. In order to demonstrate a technique it will be necessary to explain its rationale to the selected study group. This requirement makes the modified approach unsuitable for demonstration because of the difficulty in explaining these fine distinctions and their implications to respondents unaccustomed to providing this type of information.

Cross-event analysis assumes that respondents normally think in terms of time-dependent probabilities, and uses these estimates to calculate the conditional probabilities from the relationships implied by the estimator's responses. Because this approach seeks to explicitly identify quantitative values for all possible outcomes of each event pair, a greater number of subjective estimates is required. However, the questions used to obtain these estimates are formulated in a manner which appears to be more closely akin to suspected individual thought processes \( P(i|j_{\text{first}}) \).

Since these estimates are used to compute the probabilities of the eight possible ordered outcomes and then to calculate the classical conditional probabilities, more computational steps are involved in using this procedure. These formulae are relatively basic and can be easily programmed on a hand-held calculator. This extra burden is, therefore, not considered excessive in light of the advantages gained.
Using the time-dependent causal estimates, pairwise probabilistic consistency is automatically checked when computing the probabilities of the ordered outcomes. By specifying values for these outcomes it is possible to derive a logical transition to the classical conditional probabilities. This avoids the problem of applying Bayesian probability relationships to causal estimates, and eliminates the need to adopt less supportable assumptions—such as estimator consistency. At the same time, because it is possible to use the classical probability relationships, the Mitchell-Tydeman method is given a firm methodological footing.

Finally, Mitchell and Tydeman's cross-event approach provides an algorithm for computing scenario probabilities. This capability is necessary if decision-makers are to be provided a means of assessing possible courses of action in responding to ongoing developments. Scenario probabilities cannot be obtained under the Turoff method's assumption of time-independence, and could only be derived from the Enzer method by conducting an excessive number of Monte Carlo runs (exceeding the number of possible event sequences).

For these reasons, the Mitchell and Tydeman cross-event analysis method was selected for demonstration and evaluation in this study. Because the purpose of the demonstration is to evaluate cross-impact analysis' potential as a decision aid in crisis situations, several modifications to the approach were considered necessary. These modifications, presented below, were intended to extend the method.
in order to evaluate policy options for response in a developing situation.

H. EXTENSION

This section will discuss several methodological alterations through which cross-event analysis can be extended as a decision-aid for use in crisis situations.

Four aspects of the methodology will be dealt with. These are: (1) the time span of analysis, (2) identifying policy options for inclusion in the event set, (3) the method of analysis, and (4) scenario generation.

1. Time Span

Crisis situations normally occur without adequate warning and allow a short time for response. As Enzer and Alter pointed out, the time span usually considered in a cross-impact analysis is determined by the amount of time required for an event's impact to be felt by another event [Ref. 40, p. 233]. Since the technique being explored here is intended to evaluate response options, it is felt that this time span should be kept relatively short.

In a crisis situation, it seems reasonable to assume that most response options would be designed to have an immediate effect in altering the situation in some desired direction. For this reason, it appears desirable to limit the analysis to a consideration of the two weeks or so following the identification of a crisis. As there is almost no time lag involved, the event prediction need only involve
occurrence and non-occurrence, rather than exact dates. This is a level one analysis described in Johnson [Ref. 40], which predicts only those events which occur by a specific date. In providing initial estimates, respondents will not be asked for occurrence dates, in providing causal time-dependent estimates any event may be considered to occur before any other.

In the analysis, the sequence in which events occur will be revealed through scenario generation. As will be shown below, this will aid in evaluating likely scenarios for plausibility. This assumption would not be valid if the effects of policy options were to be examined in their full context. As has been noted, careful evaluation would require an assessment of a response option's long-term effect, not only on the crisis situation. In a "real world" application the short-term and long-term analyses could be conducted simultaneously to identify a possible response to control the crisis and to evaluate its potential future effects. Such an approach was not adopted here because of this study's developmental and exploratory character.

2. Identifying Policy Options

The normal procedure in cross-impact analysis has been to evaluate the effects produced by implementing policy options through arbitrarily increasing or decreasing selected events' initial probabilities. This seems to be contrary to a basic goal of the approach, which is to identify an event's unanticipated effects. Furthermore, Gordon and Hayward
hypothesized that an event normally has a predecessor or precedes another event [Ref. 26]. It was the purpose of the technique to systematically assess these interactions. In the normal sensitivity analysis, a policy option is excluded from the matrix, and assumed to have only the effect intended.

In the Mitchell and Tydeman approach, subjective assessments are made of the impact that specific strategies have on the various scenarios. This requires a prior "System Impact Analysis" to assess how the occurrence of a scenario impacts identifiable system attributes, and the development of "objective criteria" to evaluate policy strategies. It has been pointed out that the validity of this process would be tenuous for problems involving national objectives. Furthermore, it increases the number and complexity of the subjective estimates required.

In an effort to simplify the process of assessing the impact of policy options on situational outcomes, this study will attempt to identify specific policy responses available for dealing with the hypothetical situation and include them in the original cross-event matrix. These response options will be identified and assessed as any other event which might develop from the given situation under normal circumstances. Using this approach will eliminate the need for "System Impact Analysis". Normal sensitivity analysis will still be conducted to determine response option flexibility in the event that available information was misleading and/or the problem components were evaluated incorrectly.
by the respondents. Including response options in the event set also permits other extensions.

3. **Method of Analysis**

One possible extension involves the type of analysis performed by evaluating the causal relationships contained in the cross-event matrix. If the events representing policy options are separated from the events representing situation developments a four-quadrant matrix is formed as represented below.

**FIGURE THREE**

**FOUR-QUADRANT CROSS-EVENT MATRIX**

<table>
<thead>
<tr>
<th></th>
<th>$D_1$</th>
<th>$D_2$</th>
<th>$D_3$</th>
<th>$O_1$</th>
<th>$O_2$</th>
<th>$O_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_1$</td>
<td></td>
<td></td>
<td></td>
<td>II.</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$D_2$</td>
<td></td>
<td></td>
<td>$P(D</td>
<td>D)$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$D_3$</td>
<td></td>
<td></td>
<td></td>
<td>$P(O</td>
<td>D)$</td>
<td></td>
</tr>
<tr>
<td>$O_1$</td>
<td></td>
<td></td>
<td></td>
<td>III.</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$O_2$</td>
<td></td>
<td></td>
<td>$P(D</td>
<td>O)$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$O_3$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$P(O</td>
<td>O)$</td>
</tr>
</tbody>
</table>

where:

- $D =$ situation development
- $O =$ policy option

(Note: the diagonal cells can still contain the initial probabilities)

Because the subjective estimates used to obtain the conditional probabilities are in a causal time-dependent form, the following interpretations might be given to each of the four quadrants.

114
I. (D|D) -- Represents the situation as it might develop assuming no corrective action is taken. This depicts the results of allowing a given crisis to continue.

II. (O|D) -- Represents how the occurrence of given developments effect the probabilities of various response options. The occurrence of certain developments may make a response option more attractive. (It is felt that at this point not enough information is available to use this interaction to predict which response option may be selected, only whether or not the respondents consider it more attractive.)

III. (D|O) -- Represents the effect on the situation produced by the occurrence of each response option. This would be the primary quadrant with which to evaluate the response options.

IV. (O|O) -- Indicates the interaction among possible response options. This possibly could be used to trace the impacts of a mixed strategy, or to evaluate the effects of implementing more than one response.

As in the traditional approaches, each of these quadrants could be evaluated to determine event dominance, sensitivity, and estimator uncertainty. Other forms of analysis would remain essentially the same. These interpretations can only be hypothesized at this time. It will require experimental data to determine their applicability. Therefore, this type of analysis will be attempted using the results from the demonstration exercise.

4. Scenario Generation

Since specific policy options are to be included in the event set, it is questionable as to whether they should be included in the event sequence scenario generation. The occurrence or non-occurrence of a policy option is not determined solely by the situation developments but also by
the decision-maker's perceptions and the evaluations they make. The policy options are explicitly included in order to facilitate more complete evaluation. Based on this information, the decision-makers would then select the option(s) to be implemented (i.e., decide occurrence).

It might also be argued that by including one, or all, options in event sequence scenario generation it would be possible to determine which option(s) should be implemented (based on their occurrence or non-occurrence in the most probable scenario). In other words, generating and ranking scenarios with N options \((N = 1, 2, 3, \ldots, n)\), and evaluating these scenarios for desirability would indicate which options produced the most desirable outcomes.

However, in a short term situation, the specific event sequence scenario may not be so important. Accurate information is limited, and the unexpected could always happen (including events not specified in the set). Therefore, scenario generation intended to provide specific predictions would be of questionable value unless the problem was clearly understood by the estimators. In view of these considerations, this demonstration will only include the situation developments in event sequence scenario generation.

I. CONCLUSIONS

This chapter described four major approaches to conducting cross-impact analysis, including their basic assumptions, computational procedures, and types of analysis performed.
Based on this discussion, and using consistent evaluation criteria, the approaches were compared and the Mitchell-Tydeman cross-event analysis was selected for us in this study.

Cross-event analysis was selected because, although it required obtaining more numerous subjective estimates, its methodology and underlying assumptions seemed more systematic and thorough as well as intuitively pleasing. In addition, the calculations required in the procedure appeared to be simple enough to perform without using a computer. The Mitchell and Tydeman approach was extended for application in a crisis situation. This extension involved: limiting the time span considered in the analysis, including policy options as discrete events for analysis in the matrix rather than through sensitivity analysis alone, and restricting scenario generation to include only situational developments while excluding policy options.

As indicated in the discussion of the major approaches, several problems may still be encountered in operationalizing this approach. Some of these problems are inherent in conceptualizing the cross-impact technique itself and cannot, therefore, be resolved until data have been collected and analyzed. Such problems include: how estimators can best quantify the interrelationships being sought (probabilistically or as correlations), how to interpret estimator responses (as classical probabilities, causal time-dependent
probabilities, or as correlation coefficients), and how inconsistencies should be treated (ignored, boundary rules, or fitting methods). The selected technique assumes respondents can think in probabilistic terms, indeed, in terms of causal time-dependent probabilities, and that inconsistencies are best resolved using fitting procedures.

Other potential problems arise from dealing with subjective estimates, and from the methodology used in the selected approach. These include how best to aggregate estimates, and how to resolve inconsistencies. Both of these depend on the form in which the estimates are elicited and the actual values obtained. Therefore, these problems will be examined in the context of the selected technique's operationalization.

The next chapter will discuss the actual implementation process and present the demonstration results. The implementation process will describe how the demonstration was structured, and the problems encountered in using the Mitchell and Tydeman approach. The demonstration results will be used to evaluate the accuracy of the approach's assumptions, and its potential utility as a crisis decision-aid.
VI. OPERATIONALIZATION

A. INTRODUCTION

Employing cross-impact analysis in an experimental application requires developing and following a logical implementation process. Due to the approach's information requirements and the type of problem proposed, four preliminary steps are necessary for implementation. The first task is to identify a study group to act as expert respondents. Next, a problem environment for analysis has to be constructed. Then, this problem environment, and the approach's purpose, methodology, and information requirements have to be explained to the study group. Finally, a procedure to elicit the group's subjective estimates has to be devised.

Once the preliminary background has been laid, actual implementation requires collecting and structuring the respondents' estimates into the format required by the cross-event approach, and conducting the analysis. This process includes: identifying candidate events and selecting from these the analysis event set, and aggregating individual estimates into group response values to provide the data for replicating the analysis performed by Mitchell and Tydeman [Ref. 29].

26 The purpose behind using group values is two-fold. First, it should reduce instances of pairwise inconsistency [Ref. 29]. Secondly, as proposed by Enzer, the respondents' opinion spread could serve as an estimator uncertainty indicator [Ref. 27, p. 55].
To replicate the cross-event analysis, as extended in the previous chapter, it is necessary to perform two calculation steps. The first step is to compute the event pair ordered outcome probabilities (P₁ through P₈). These values are then used in the second step which calculates the conditional probabilities implied by the respondents' estimates. The conditional probabilities can then be arranged into a cross-event matrix and scenario generation undertaken. These tools are then used to perform the problem analysis.

This chapter describes the implementation design developed for this study. It discusses how the actual operationalization evolved by reviewing the successes and failures encountered in following the designed implementation. Finally, the data collected are presented and analyzed.

B. IMPLEMENTATION DESIGN

The entire operationalization process was designed to follow the demonstration described by Mitchell and Tydeman [Ref. 29, p. 145-147]. Their "event assessment" procedure was used to select an analysis event set [Ref. 23, p. 6-9], the forms for obtaining subjective estimates were taken from the examples contained in Ref. 29, and the equations used in all calculations were from the derivations presented in the same source.

The procedure used to demonstrate cross-event analysis in a hypothetical situation was constructed to follow five phases. Each phase's purpose and structure will be discussed below.
1. **Scenario Construction**

To establish the problem environment for analysis a hypothetical problem scenario was developed. Several considerations influenced this development. Because the problem was intended to represent an emerging crisis situation, the scenario had to threaten identifiable national interests, suggest potential policy options which could be identified as responses, and involve recognized actors. This last consideration was adopted for two reasons. Using real actors would provide an actual basis for the respondents' perceptions rather than having to structure perceptions by specifying a host of hypothetical historical, social, political, economic, etc. data in the scenario. Also, using real actors was expected to make estimation and analysis more meaningful to the respondents.

To satisfy the above requirements and involve as much current information as possible in the problem environment, the scenario was based on developments in South Asia. A brief justification for this decision will be presented in the next section which describes the actual scenario presented to the respondents.

The scenario was presented in four sections to allow as complete a development as possible. Those sections were: (1) Background — described the primary actors, their internal situations and external relationships. (2) Event Sequence — listed the hypothetical moves and counter-moves taken by the various actors. (3) Resulting Situation — set forth the
actual problem (crisis) to be analyzed and responded to.

(4) U.S. Concerns -- described what appeared to be the
significant U.S. interests in the area. The scenario
presentation was conducted as the second segment of the
design implementation's explanation phase.

2. **Explanation**

This phase described the experiment's purpose and
methodology to the study group. This explanation was in-
tended to help the respondents understand their role in the
experiment. It included: The rationale behind using sub-
jective estimates, the information the respondents would
be asked to provide, the information format, how the infor-
mation would be analyzed, and answered any questions which
arose. In this manner it was hoped to fully involve the
respondents in the project and thereby produce more care-
fully considered responses, while demonstrating to the
respondents the approach's potential as a learning tool.

The explanation phase involved two segments. The
first described cross-impact theory, its assumptions,
methodology and proposed applications. Once the basic
concepts and their use was understood, the Mitchell and
Tydeman approach was described to the study group. This
presentation highlighted the functions the respondents
would be required to perform.

The second explanation segment presented and dis-
cussed the hypothetical scenario. This was presented in
four sections, as previously described, in order that the
participants could fully understand the problem elements involved. In an actual application this segment would be optional, as the "experts" could be expected to be familiar with the problem environment. Once the respondents understood the technique and hypothetical problem the third implementation phase was begun.

3. Elicit Estimates

This phase was designed to obtain the subjective estimates used in the problem analysis. Two estimation procedures were developed for this process. The first used a "brainstorming" technique to elicit a candidate event set. Immediately after the scenario discussion the respondents were asked to suggest developments which might occur resulting from the proposed situation. All subsequent estimates were obtained using an individual response procedure.

Once the candidate event set was established the respondents were asked to individually rate each event's initial occurrence probability and significance. This information was used to conduct an "event assessment" and select a manageable event set for analysis. As discussed previously, this procedure was adopted to reduce both the number of estimates and computations required by concentrating on only the "important" events. Individual estimates were then obtained for the causal time-dependent probability relationships (C₁ through C₅) existing in each event pair. These data were intended for use in the fourth implementation phase.
4. **Conduct Analysis**

The fourth phase was designed to structure the respondents' estimates into the cross-event format and analyze the resulting output. Individual responses were aggregated into group values and used to compute the "cross-impacts" from the formulae developed by Mitchell and Tydeman. This procedure computed the ordered event pair outcome probabilities ($P_1$ through $P_8$) and the resulting conditional probabilities for each event pair. At the same time, pair-wise consistency could be checked and resolved if necessary. Because group values were used, instances of inconsistency were expected to be rare.

Given consistent estimates a cross-event matrix would be constructed and scenarios generated. These data would then be analyzed as described in Chapter Three. The analyses to be performed included: For events -- determining dominance, sensitivity, significance, and uncertainty. For interrelationships -- conducting causal tracings through the event matrix (as discussed in the extension section of Chapter Three), evaluating response options using the matrix and scenarios, performing scenario and sensitivity analysis.

The implementation design included presentation of the analysis results as its final section.

5. **Presentation of Results**

This phase was designed to organize and present the analysis results for evaluation. These results were presented to the study group to close the feedback loop and
complement the learning experience. This phase also involved the participants in evaluating the cross-impact technique.

Respondents were asked to suggest possible reasons for the results obtained, and to assess whether or not the information derived from their estimates met their expectations. They were also asked to comment on their impressions concerning the technique's procedures and potential utility. This information, and the analysis results, were used in evaluating cross-event analysis as a possible crisis decision-aiding methodology. The respondents' feedback and the actual implementation experience were used to evaluate the procedure's ease of application, to identify possible problems and to recommend improvements. The following section recounts how the designed implementation actually evolved, and identifies the successes and problems encountered in operationalizing cross-event analysis.

C. ACTUAL IMPLEMENTATION

The preliminary implementation steps were relatively easy to accomplish. The study group utilized was a Data Analysis for Naval Intelligence class being conducted (Spring Quarter, 1979) at the Naval Postgraduate School, Monterey, California. The class provided ten respondents (nine Naval officers and a civilian Professor). The officers had various types of operational experience in the U.S. Navy, and were undertaking graduate studies in the
school's National Security Affairs Department. Thus, their background was felt to be adequate for demonstration purposes. All respondents had some exposure to probability and statistics, organizational management and decision-making, and various topics in National Security and Intelligence. In addition, most had kept abreast of ongoing developments in South Asia. These characteristics simplified the explanation process as no really "new" material had to be covered.

The explanation phase previously outlined consisted essentially of orally summarizing Chapter Two and the cross-event analysis section in Chapter Three of this study. The explanation also reviewed the procedure designed to elicit the group's subjective opinions. In the second explanation phase, the study group was led through the scenario developed for this demonstration. The problem scenario presented to the respondents will be described below, followed by descriptions of the remaining implementation phases.

1. Scenario Development

Developments in South Asia and around the Persian Gulf have become a focal point for U.S. diplomatic, economic, and military interests. This increasing interest has been well documented by noted political scientists and historians. These authors have detailed increasing U.S. interest in,
and commitment to, the region resulting from numerous interrelated factors.27

Some of the primary factors influencing U.S. interests in the area include, increasing U.S. dependence on imported oil and the tenuous supply links through which it is obtained.28 Another factor is the increased Soviet influence in South Asia, their increasing naval presence in the Indian Ocean, and the purpose behind this presence.29 A third concern is the continuing tension in the region which seems to keep the relationships in the area in a

27 For example, Nadav Safran discusses the U.S. involvement growing out of the Middle East peace process [Ref. 51]. Richard Ullman has examined U.S. policy options in the area in light of continuing tensions and outside pressures [Ref. 52]. Basic considerations for U.S. policy in this area were presented by Campbell and Lenczowski [Refs. 53 and 54]. Inter-regional relationships and super-power roles are examined by Vali [Ref. 55], while Wall has collected papers addressing relevant strategic concerns [Ref. 56]. Many of the interests and concerns developed by these authors are reflected in official U.S. Government documents such as the "Department of Defense Authorization for Appropriations for FY 79" policy statements [Ref. 57].

28 The oil question is explored by analysts such as Lenczowski and Anthony [Refs. 58 and 59]. Its future implications are examined in a CIA forecast [Ref. 60], which indicates that the situation is unlikely to improve.

29 Increased Soviet influence and military presence is discussed by Lenczowski [Ref. 61], Hurewitz [Ref. 62], Tahtinen [Ref. 63], and McConnell [Ref. 64]. The dispute over the intentions behind this presence has produced a resultant U.S. policy debate over its military presence reviewed in Daniel [Ref. 65].
state of flux and instability. The complexities of these problems are indicated by several authors. Although a complete development of these and associated factors is beyond the scope of this study, that the region's importance is an area for continued policy analysis should be self-evident.

Further, recent developments in several South Asian states have thrust the region's problems more prominently into public view.

Among those recent developments is the pro-Soviet coup in Afghanistan coupled with signs of increased Soviet influence within the new regime and subsequent internal turmoil. Another situation causing increased concern was the overthrow of the Shah of Iran and resulting uncertainty over the direction in which the new government would evolve. Adding to general concern for the course of the Iranian situation has been the centrifugal forces set in motion by Kurdish and Arab nationalists as well as politically liberal forces within the country. In addition, the execution of Bhutto by Pakistani authorities has increased internal dissent in that country. This dissent is significant because it occurs during a period of tension between Afghanistan and Pakistan concerning reputed Pakistani support for dissident tribesmen challenging the Taraki regime in Afghanistan.

30 A regional perspective on area tensions is presented by Amire [Ref. 66], and Misra [Ref. 67]. Burrell and Cottrell [Ref. 68] explore specific problems faced by the states of South Asia.

31 These developments are being continuously reported in magazine and newspaper articles. Articles describing these specific developments include: On the Soviet involvement and turmoil in Afghanistan; Sherwell, Chris, "Fighting May Boost Soviet Presence in Afghanistan," The Christian Science Monitor, p. 6, Dec. 29, 1978, and Sherwell, Chris, "Soviet Union Mired
For these reasons it was decided to develop a problem scenario involving relations in South Asia. The study group would be familiar with the basic situation existing in the area, and could easily identify important (as well as plausible) developments reflecting U.S. interests and possible response options. The actual scenario was developed as follows.

a. Background

This section, supported with newspaper clippings, presented the current situation existing within and among the three regional actors being considered. Afghanistan was described as having recently undergone a pro-Soviet coup. Its military was identified as a prime factor in maintaining political control. The country's administrative bodies, including the military, were reported to be heavily influenced by Soviet advisors. In addition, the state's internal situation was characterized as being plagued with anti-government groups, consisting mainly of Moslem tribesmen in the rural areas.

The situation in Pakistan was described as involving increased internal dissent resulting from Bhutto's execution. Problems were also reported to be developing from the influx of Afghan refugees. In addition, the Pakistani military was described as poorly equipped and preoccupied with the Indian threat to Kashmir.

Iran's current government was described as disorganized, composed of several rival factions, and challenged by elements (including leftists and ethnic minorities) desiring more control. The effectiveness and loyalty of Iran's military was also brought into question, due to its history of supporting the Shah and the execution of several important leaders. This development stressed the fact that authority in Iran could still be considered to be in a state of flux. Finally, Iran's historic role in controlling disputes between Afghanistan and Pakistan concerning the territory of Baluchistan was mentioned. Using this simplified background discussion as a basis, a hypothetical sequence of developments was proposed to the study group.

b. Event Sequence

- Tribesmen in Baluchistan (South Afghanistan) begin a national autonomy movement. This movement receives some support from related tribes in Iran and Pakistan.

- Clashes occur between Afghani government forces and rebel tribesmen in Baluchistan.

- The Afghani government dispatches additional troops to control the area. These troops are Soviet supported, but the extent of this support is unknown.

- These forces drive the majority of the rebels across the border into Iran and Pakistan.

- Both sides (rebels and Afghani troops) begin cross-border raids. By this time the majority of the Afghan army is committed.

- Afghanistan charges that Iran and Pakistan are aiding the rebel forces. The Afghan government vows to defeat any outside threat to its territorial integrity.
The Soviet Union supports this declaration and offers to increase assistance to Afghanistan.

- Iran authorities deny the Afghani charges and state that increased Soviet involvement would only worsen the situation. Pakistan charges the Soviet Union with trying to precipitate a crisis in the region, and requests U.S. aid.

- Regular Afghani forces clash with Iranian border troops. This clash erupts into uncontrolled shelling along the border.

- Baluchistan rebels call on Muslim states for support against the communists, suggesting a "holy war" be launched.

- Iranian leftists, reportedly supplied by the Soviets, begin a terrorist campaign to oust the Ayatollah's government.

- Iran announces support for rebel tribesmen and launches a "limited" invasion to pacify the area, and expel "expansionist" communists.

- Pakistani forces join the conflict.

- The Soviet Union sends troops to Afghanistan which check the Iranians. Reports indicate the Soviets have mobilized on Iran's border, that their agents are agitating Iranian Kurds, and that they have sent a secret mission to Iraq.

- Soviet and Afghani forces press attack to the original Afghan border, but show no signs of halting. Steps are being taken to set up a "puppet" government for Baluchistan. Indications are that Soviets and Afghans may attempt to include Baluchistan land in Iran and Pakistan under control of an "autonomous" Baluchi government.

Based on these developments, the following situation was proposed to exist in South Asia. This situation described the crisis problem to be evaluated using cross-event analysis.

c. Resulting Situation

- Open warfare exists in the area south of Afghanistan extending into Iran and Pakistan. This fighting involves Afghanistan, Iran, Pakistan, rebel tribesmen, and (reportedly) some Soviet forces.
- The Soviets have mobilized along Iran's border and are conducting secret talks with Iraq.

- Iranian Kurds and leftists (separately) are almost in open revolt.

- India has mobilized along Pakistan's border, to "prevent the conflict from spilling over."

- Chinese troops have mobilized in Sinkiang in response to "Soviet aggression, and to demonstrate support for the Baluchistan People's Movement".

To guide the respondents in proposing candidate events the following "probable" U.S. concerns were also presented.

d. U.S. Concerns

- The current conflict threatens navigation in the Straits of Hormuz. In addition, the fighting is close to the main oil producing region in Iran, threatening the security of those fields.

- The Soviet Union may extend its influence to the Indian Ocean if it manages to sponsor a client state of Baluchistan. This would permit both overland access to the Indian Ocean and possible naval basing rights.

- The current turmoil directly threatens U.S. civilians in the area and, to a lesser extent, U.S. economic interests.

- The potential involvement of India and China and possible direct Soviet intervention suggest a major confrontation may be developing.

This scenario provided the background against which the respondents were asked to suggest a candidate event set, and formulate the required subjective estimates. This process will be described in the following section which details the implementation design's third phase as it actually developed.
2. **Elicit Estimates**

The next task undertaken in the demonstration required establishing a candidate event set. Before the group was asked to brainstorm possible developments, several procedural points were reviewed. The study group was reminded that suggested events be considered as developing from the given situation. Enzer's criteria for including events in the set were also reviewed. These criteria stress that candidate events be (1) important to the situation, (2) of uncertain outcome, (3) causally related, and (4) specific. Finally, the event formulation rules proposed by Mitchell and Tydeman were reviewed to assure the suggested events could be clearly understood by the group. These procedural points were discussed in Chapter Two.

a. **Establishing the Event Set**

Once the group understood the required event formulation method, a brainstorming session began. As events were suggested they were recorded and posted before the group. This process continued until it became apparent that the participants had exhausted all their ideas. A brief discussion session then was allowed to clear up any uncertainties. Twenty-nine candidate events were proposed during this session. Ten of these represented possible U.S. responses to the situation, the remainder represented situation developments. These events are presented in Appendix A.
In order to select an analysis event set the group was next asked to provide the subjective evaluations required for Mitchell and Tydeman's "event assessment" procedure. These inputs consisted of two estimates. The first required the respondents to evaluate each event's initial occurrence probability. These probabilities were collected individually by having each respondent score every event on the following scale. Each evaluation was to be made without considering the influence any other event in the set might have on the situation.

### TABLE TWO

<table>
<thead>
<tr>
<th>EVENT PROBABILITY DESCRIPTIONS AND RATINGS</th>
<th>RATING</th>
</tr>
</thead>
<tbody>
<tr>
<td>Won't Occur</td>
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<tr>
<td>Very Unlikely</td>
<td>.15</td>
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<td>.50</td>
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<td>.70</td>
</tr>
<tr>
<td>Very Likely</td>
<td>.85</td>
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<td>Certain</td>
<td>.95</td>
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</tbody>
</table>

The second estimate required respondents to evaluate each event's significance should it occur. An event's significance was defined as the influence it would have on the overall problem situation, assuming it did occur. These ratings were based on the following scale, and were again collected individually.
This procedure produced ten values under each criterion for each of the twenty-nine events. These individual scores were aggregated and used to produce an impact rating for each event. The twenty-nine candidate events and their probability, significance, and impact ratings are contained in Appendix A.

Several problems were encountered during this estimation procedure which were unanticipated in the problem design. While eliciting candidate events two tendencies were noticed which seemed to inhibit the formulation process. In brainstorming, the respondents seemed to concentrate on a suggested event and propose subsequent events which would develop should the first event occur. Often this process would lead far afield until interrupted by the facilitator interjecting an alternative event. On other occasions, an event's suggestion seemed to elicit the proposal of a response event aimed specifically at the first event. Another problem encountered stemmed from the respondent's experience level or knowledge.
Some respondents seemed to be intimidated by the ease with which other respondents formulated and justified suggested events. A few respondents stated they felt unqualified to participate, and questioned the validity of their future estimates given their lack of equal knowledge concerning South Asia. These problems seem to be inherent in the "brainstorming" process.

In future applications it is felt that using trained or experienced facilitators could reduce the problem of respondent intimidation, and better control the brainstorming process. In addition, research using the delphi procedure indicates that having respondents rate themselves on their confidence in answering questions provides a criterion with which to weight individual responses to produce improved group values [Ref. 13]. This method might be incorporated in future cross-impact applications.

The fact that suggested events often led to related events being suggested indicates a basic cross-event assumption may be unfounded. The approach operates on the theory that respondents can think in terms of discrete events. Based on this assumption respondents are asked to provide initial probability and significance estimates for each event independently. However, during the brainstorming process, respondents exhibited a tendency to propose events in an iterative manner. This suggests that the group may find it difficult to conceptualize relationships in terms of discrete events, and therefore may conceive of
of related probability and significance questions inter-
dependently, or as contingencies. This in turn indicates
that another approach to quantifying estimates may be more
appropriate. This point will be developed more exten-
sively in the next chapter.

Other problems were encountered when the indi-
vidual estimates were aggregates to produce the impact
ratings. In their procedure, Mitchell and Tydeman use a
weighted product of each event's probability and signifi-
cance scores to produce its impact rating. This procedure
was found to produce inadequate results in this demonstra-
tion. The results obtained seemed to disguise the impact
assigned an event which received a combination of a low
and high rating on the two criteria evaluated. A simpli-
fied, hypothetical example may help to illustrate this point.

Assume three countries are rated on their mili-
tary potential by aggregating scores for their Army, Navy,
and Air Force. Using a multiplicative index produces the
following results.

FIGURE 4
RESULTS OF A MULTIPLICATIVE INDEX

<table>
<thead>
<tr>
<th>COUNTRY</th>
<th>ARMY (x)</th>
<th>NAVY (x)</th>
<th>AIR FORCE (=)</th>
<th>MILITARY POTENTIAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>5</td>
<td>2</td>
<td>3</td>
<td>30</td>
</tr>
<tr>
<td>B</td>
<td>5</td>
<td>1</td>
<td>3</td>
<td>15</td>
</tr>
<tr>
<td>C</td>
<td>5</td>
<td>0</td>
<td>3</td>
<td>0</td>
</tr>
</tbody>
</table>
Using the same values with an additive index seems to produce a more realistic measure.

**FIGURE 5**

RESULTS OF AN ADDITIVE INDEX

<table>
<thead>
<tr>
<th>COUNTRY</th>
<th>ARMY (+)</th>
<th>NAVY (+)</th>
<th>AIR FORCE (=)</th>
<th>MILITARY POTENTIAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>5</td>
<td>2</td>
<td>3</td>
<td>10</td>
</tr>
<tr>
<td>B</td>
<td>5</td>
<td>1</td>
<td>3</td>
<td>9</td>
</tr>
<tr>
<td>C</td>
<td>5</td>
<td>0</td>
<td>5</td>
<td>10</td>
</tr>
</tbody>
</table>

Another, less significant, problem developed because two different scales were employed in the "event assessment." Probability values were quantified between zero and one, while significance scores ranged from one to five. This further distorted the multiplicative index. As a result the impact scores produced an analysis event set which did not seem to accurately reflect the event's relative importance. To overcome this problem two corrections were introduced to the aggregation procedure.

The significance ratings were rescaled to fall between zero and one. The final ratings employed were: 5=.95, 4=.7, 3=.5, 2=.3, and 1=.05. Then the individual probability and significance ratings were summed to produce an individual event impact rating. All three ratings were then averaged to produce a group or mean score, and the standard deviations were computed for
each measure. These are the values presented in Appendix A.

This correction is not without conceptual limitations. The assumption implicit in summing the two evaluation measures is that both probability and significance are equally important in determining an event's impact on the problem environment. It is doubtful whether this assumption would hold up under rigorous examination. It appears that an event's significance would be a more important consideration than its occurrence probability. This is because an event's impact has no meaning should it not occur, therefore, it only becomes important from a policy standpoint once it occurs, and this importance derives from its significance to the situation. This problem relates to Gordon's discussion of the complex factors which make up an event's cross-impact [Ref. 24]. Presently there exists no algorithm relating the many factors (such as probabilities of "feasibility" and "pursuit", and event significance) which compose an event's impact. As a result simple summing was the only approach which could be readily applied.

Candidate events were ranked by impact scores and six events selected to form the analysis set. A final ranking by event impact scores is contained in Appendix A. Because one purpose of the demonstration was to examine the cross-impact technique's applicability to evaluating specific policy response options these six events were not chosen from
the top ranked candidate events. The six top ranked events included only one event identified as a response option (number three). This was because, while most response events were evaluated as having high initial probabilities, their significance was evaluated as being relatively low. To obtain a matrix containing an equal number of response events and situation development events, the events were separated and the top three chosen from each category.

The analysis event set and the mean initial probabilities are presented below. Six events were used because this was felt to be the maximum number which could be effectively manipulated by hand. It should be noted that the initial probability values have been rounded to two decimal places. The averaging technique used retained three decimal place values for comparison purposes. Because these values were averaged subjective estimates, this degree of accuracy would not be justified for use in the actual demonstration. This event set formed the basis for the remaining individual estimates, that is, the five causal time-dependent relationships developed by Mitchell and Tydeman.

\[\text{This result is interesting due to its implications. Although the U.S. is assumed to have an extensive number of responses available which could be employed in a given situation, the respondents obviously felt that the majority of these would be ineffective in this case. Of the three response options included in the analysis, only one had a significance score comparable to that of the situation development events.}\]
TABLE FOUR
SELECTED EVENTS

<table>
<thead>
<tr>
<th>No.</th>
<th>STATEMENT</th>
<th>Avg. $P_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>22</td>
<td>Soviet/Afghan forces gain control of Baluchistan.</td>
<td>.60</td>
</tr>
<tr>
<td>28</td>
<td>Soviet Union builds up Indian Ocean squadron.</td>
<td>.80</td>
</tr>
<tr>
<td>23</td>
<td>Soviet Union airlifts supplies to Afghanistan.</td>
<td>.72</td>
</tr>
<tr>
<td>3</td>
<td>United States deploys CTF to Indian Ocean.</td>
<td>.76</td>
</tr>
<tr>
<td>9</td>
<td>United States evacuates civilians from area.</td>
<td>.84</td>
</tr>
<tr>
<td>8</td>
<td>United States offers to negotiate a cease-fire.</td>
<td>.64</td>
</tr>
</tbody>
</table>

b. Estimate Relationships

The six-event set produced fifteen possible event pairs which required further estimation. The required estimates were the five time-dependent probabilities ($C_1$ through $C_5$) which assessed occurrence, non-occurrence, and joint occurrence. Thus, seventy-five estimates were required from each respondent.

In order to systematically produce and collect these estimates, response forms were duplicated from the examples provided by Mitchell and Tydeman [Ref. 29, p. 146-147]. The forms used are reproduced on the next page.
FIGURE 6
FORM FOR ESTIMATING $C_1$ AND $C_3$

Would the prior occurrence of event # cause your estimate of the Probability of event # to:
Increase Stay the same Decrease

If your estimate of event # probability is changed (increased or decreased) is the magnitude of the change:
Only Slight A Little A Fair Bit A Lot Sufficient to make event # certain or impossible

5 10 25 50 100 (% of total possible change)

FIGURE 7
FORM FOR ESTIMATING $C_2$ AND $C_4$

Would the prior non-occurrence of event # cause your estimate of the Probability of event # to:
Increase Stay the Same Decrease

If your estimate of event # probability is changed (increased or decreased) is the magnitude of the change:
Only Slight A Little A Fair Bit A Lot Sufficient to make event # certain or impossible

5 10 25 50 100 (% of total possible change)
Assuming both events # and # occur within the next 14 days

- Event is certain to occur first
- Event is very likely to occur first
- Event is likely to occur first
- Event and event are equally likely to occur first
- Event is likely to occur first
- Event is very likely to occur first
- Event is certain to occur first

These forms were organized by selecting the first event in the set and pairing it with the remaining five events. The next series of estimates paired the second event with the remaining four events and so on until all fifteen event pairs had been specified. Because there were seventy-five total estimates, the forms were delivered to the respondents in two batches. Each respondent was given two days to complete each batch. The forms were then collected and sorted by event pair and the relationships assessed. The ten responses for each relationship were averaged to produce a mean score for each relationship. These scores are contained in Appendix A.

Several complaints were voiced by the respondents concerning this estimation procedure. This approach made the estimation process monotonous. Three questions were repeated with only different event numbers.
being inserted to complete the seventy-five data points. In addition, the question wording was felt to be tortuous, specifically through use of the terms "prior occurrence", and "prior non-occurrence".

These problems result from manually replicating the cross-event procedure. It was not possible in the time available to devise an optimal question format for each event pair. Such a format could have incorporated the event statements within the question. For example, the following formulation for event pair (28,3) would probably have been more acceptable:

"Assuming the Soviet Union builds up its Indian Ocean fleet, would you estimate the probability that the U.S. deploys a CTF to the Indian Ocean to:"

and for non-occurrence:

"Assuming the Soviet Union does not build up its Indian Ocean fleet, would you estimate the probability ..."

Such a format could obviously be constructed for each event pair. Several advantages might stem from adopting this approach. The more precise wording explicitly incorporates the event statements being considered. The causal time-dependent nature of the relationship being explored is implicit in the question without employing phrases such as "prior occurrence." As a result the responses obtained might be more accurate and consistent, however, this fact cannot be validated without further analysis of how respondents interpret questions.
Another problem encountered in the procedure was not voiced by the respondents, but was hypothesized to account for the responses obtained when the group values were analyzed. The analysis of the responses presented in the next section found that every event pair was inconsistent in terms of the $P_1$ through $P_8$ ordered outcome probabilities computed. This problem was felt to result, at least partially, from the sequence in which estimates had been obtained.

The sequence used in this demonstration was selected because it systematically specified all the event pairs. This was necessary to insure that all respondents received the proper forms and thus provided all required estimates. However, this may have been an inappropriate way to proceed through the event pair set for estimation purposes. In addition, the five relationships being estimated were not presented to the respondents in order. The joint occurrence question ($C_5$) being retained until the end of each series (Event 1|Event 2,..., event 6) of the $C_1$ through $C_4$ questions.

As the respondents answered the questions in the order of presentation, it is possible that they lost track of the values previously specified. It is also possible that the respondents were prevented from considering their previous responses concerning event pairs which might have been felt to be related to each other. Once again these possibilities cannot be verified without
experimental analysis. No doubt, there is an optimal way to present the event set for estimation.

This conclusion is based on two arguments presented in the cross-impact theory discussion. First, Enzer suggested that probabilities of conditional relationships were bounded by the probabilities previously specified for that event pair. If this is true then this condition could also apply to the time-dependent causal probabilities. The second argument is even more basic to cross-impact theory.

Gordon suggested that most events are related in some way. Enzer approached this conclusion in his discussion of coupling. It therefore seems reasonable that the discrete events composing a set may all be coupled in some way. This, it should be noted, is not the concept of higher order interactions which Turoff attempted to measure, but refers to direct relationships among all events in the set. Assuming such a situation is present, then in order to produce a consistent set of estimates, a respondent needs to be able to review and incorporate not only his previous estimates within an event pair but among event pairs as well.

In summary, the problems encountered and suspected in this process were: (1) monotony, (2) imprecise question wording, and (3) inappropriate question sequence. To overcome these problems it would be necessary to devise an estimation procedure which: (1) formulates questions using the event statements, (2) develops a more exact question
structure, (3) allows estimators to review their responses as they estimate, and (4) allows estimators to compare their responses across related event pairs.

One possible approach to overcoming these problems might be to use an interactive computer program to elicit estimator responses. This approach was demonstrated by Turoff. As proposed here, the program would allow the respondent to make estimates on the basis of responses concerning other estimates. Obvious extensions to this approach include computing probability boundaries as suggested by Dalkey, and displaying results to allow re-estimation as suggested by Turoff. Using an interactive computer would aid in obtaining consistent probability estimates (this problem will be returned to in a later section). It might also provide useful data for determining how respondents interpret questions posed, and for devising an optimal estimation sequence.

Despite the problems encountered by the respondents, and because the suspected problems were not immediately apparent, the respondents' estimates were collected and averaged as planned. These values formed the input for computing the eight ordered outcome probabilities for each event pair.

3. Analysis

The next phase in the demonstration was to replicate the analyses performed by Mitchell and Tydeman as extended for this application. This required that the responses
obtained be converted into conditional probabilities, and that these be used to construct a cross-event matrix and generate scenarios. This section will describe the computational procedure used and discuss the results obtained.

a. Computational Procedure

Once the respondents' estimates were averaged and the standard deviations for each relationship computed, mean values were used to compute the ordered outcome probabilities. The $P_1$ through $P_8$ values for each event pair were calculated using the formula derived by Mitchell and Tydeman as presented in Section E of Chapter Three. These values were used to compute the conditional probabilities, however, unlike the Mitchell and Tydeman demonstration, every event pair was found to have inconsistent results.

According to Mitchell and Tydeman inconsistency exists when any outcome probability is negative [Ref. 29, p. 142]. In fact pairwise inconsistency from a probabilistic standpoint is manifested by a value $>1$ or $<0$, and is indicated when the common factors $\alpha$, $\beta$, and $\gamma$ exceed unity or become negative. The calculated outcome probabilities for each event pair are presented in Appendix B.

The cross-event procedure uses a minimum standard deviation fitting technique to resolve pairwise inconsistency. This technique, as described in Chapter Three, was felt to be inappropriate for use in this demonstration. One reason was that it would require an excessive amount of time to resolve fifteen inconsistent sets. Also, the
technique, as demonstrated by the developers in a case resolving individual inconsistency, zeroed the inconsistent values. Of the fifteen event pairs developed in this study, over half the outcomes in twelve pairs were inconsistent while six pairs had seven or more inconsistent values. As a result, it was felt that the fitting technique would destroy too much potentially useful information.

Even though the ordered outcome probabilities were apparently inconsistent, it was still possible to compute conditional probabilities using the formulae devised by Mitchell and Tydeman. These conditional probabilities would doubtlessly also be inconsistent from a probabilistic standpoint, however, in the cases where one conditional probability appeared consistent it would be possible to employ Enzer's boundary rule to resolve the second probability. As in the case of the fitting technique, this procedure was expected to destroy at least half of the potential information. In addition, the boundary rule could not be applied in cases where both conditional probabilities appeared to be inconsistent.

Because the demonstration results were apparently inconsistent, it was not possible to produce all the data required for the intended analysis and evaluation. Having only the ordered outcome probabilities precluded any attempt to determine event dominance and sensitivity. Nor was the required data produced for completing the cross-event matrix and undertaking scenario generation. Therefore, it was not
possible to conduct the analyses which use these tools. In particular, the demonstration could not be used to determine the validity of the proposed extension which included discrete policy options in the event matrix. Even so, it is still felt that this was a practicable extension, given a workable cross-impact format, which could become a useful analytical tool.

Two alternatives for solving the inconsistency problem seemed to present themselves. The designed study could be continued by arbitrarily specifying a consistent set of values. This alternative would have ignored the study's intended purpose of assessing the utility and effectiveness of cross-impact analysis as a possible decision-aid by forcing the methodology to work rather than examining its problems and their implications.

The second alternative was to examine the apparent inconsistencies to determine if they were in fact inconsistent. It would then be possible to determine: a) why the information was inconsistent and what corrective measures could be taken, or b) why the information appeared to be inconsistent, and how it could be used if it was in fact consistent. This alternative was selected. The approach used will be described in the following section.

b. Exploring the Inconsistency Dilemma

The first task in exploring the inconsistency problem was to determine if the demonstration results were in fact inconsistent. To do this the cross-event approach's
assumptions and implications were re-examined. It was obvious that the collected data provided enough information to rank the ordered outcome probabilities. If the outcome probabilities were considered as an eight element set there were $P^8 = \frac{N'}{(N-R)!} = 8!$ possible rank combinations. If it could be shown that the fifteen combinations obtained during the demonstration formed a pattern displaying some underlying logical consistency apart from the consistency demanded by the constraints of probability theory, and if this pattern occurred in a statistically significant number of cases, then the responses could be demonstrated to provide useful information which might otherwise be masked by routine cross-impact analysis techniques.

The respondents had been asked for causal, time-dependent estimates which were used to compute ordered outcome probabilities. The estimates were obtained by assuming the certain occurrence or non-occurrence of an event (cause) and assessing the change in probability this produced in another event's probability (effect). The outcome probabilities computed using these estimates were time sequences, which retained this cause and effect structure. The eight ordered outcomes could, therefore, be paired by opposite cause.33 This resulted in pairing the following

---

33Actually, several pairing methods were possible. For example: Transpose (i,j with j,i), opposite cause (i,j with i,j), opposite effect (i,j with i,j), and opposite cause and effect (i,j with i,j). However, since the relationship being estimated assumed known cause (prior occurrence or non-occurrence), in effect holding cause constant, the opposite cause pairing was considered more relevant for testing.
outcomes: $P_1 - P_3$ (i, j with 1, j), $P_2 - P_4$ (i, j with 1, j), $P_5 - P_7$ (j, i with 1, i), and $P_6 - P_8$ (j, 1 with 1, i). If the respondents had been consistent, it could be argued that the pairing of probability ranks by cause would reveal some logical pattern. To accept this argument, the pattern would have to appear more frequently than could be expected by random chance.

Upon pairing the probability rankings in the fifteen cases (one for each event pair) by cause, several patterns were noted. These are depicted in Appendix B. As stated above 8! combinations are possible. To show consistency a pattern would have to permit prediction (i.e., by knowing one outcome probability's rank it would be possible to determine its pair's rank.) By this criterion one obviously consistent pattern was noted and termed the "Chinese Box".

The "Chinese Box" pattern paired the first and last, second and seventh, third and sixth and, fourth and fifth ranked probabilities. The pattern was intuitively pleasing as it indicated that the respondents had ranked last the opposite cause to the cause ranked first, ranked next to last the opposite cause to the cause ranked second, and so forth. This pattern implied that some logical consistency existed in the way respondents linked cause and effects in the demonstration situation. A second consistent pattern could also be identified although it was intuitively less rigorous. This was actually a family of patterns which
existed when one pair and its opposite pair were located in the upper half and lower half of the scale respectively. This also implies some degree of consistency although it does not allow exact prediction. The "Chinese Box" pattern was selected for testing because it was more rigorous, and could be expected to occur less frequently by random chance than the simple upper-lower split.

A "Chinese Box" occurs when one of the outcome pairs is ranked in position one through four before its pair is ranked in the corresponding position from the bottom up (eight to five). Thus there are $P_4^4 = \frac{4!}{0!} = 4!$ combinations which produce this pattern. But since $P_1$ can be replaced by $P_3$, $P_2$ can be replaced by $P_4$, $P_5$ can be replaced by $P_7$, and $P_6$ can be replaced by $P_8$, the actual number of combinations is given by $4! \times 2 \times 2 \times 2 \times 2 = 384$. Thus the theoretical probability of observing a "Chinese Box" can be determined as $384/8! = .0095 \approx .01$. During the demonstration the following results were obtained. In the fifteen cases, eight obviously inconsistent sets occurred and seven apparently consistent sets were observed. This produces an experimental frequency of .47. Two tests were used to determine if this result was statistically significant.

The Kolmogorov-Smirnov one sample test provided the following results for a sample set of $N = 15$ cases, and two categories (consistent, inconsistent) [Siegel, 1956, p. 47-52].
$F_0(X)$ = the theoretical cumulative distribution of cases

$S_{15}(X)$ = the observed cumulative frequency distribution of a random sample of 15 cases

$D$ = the maximum deviation between $F_0(X)$ and $S_{15}(X)$ or $|F_0(X) - S_{15}(X)|$

The critical value for $D$ at the .01 significance level is .404 for 15 cases [Siegel, 1956, Table E, p. 251].

**TABLE FIVE**

<table>
<thead>
<tr>
<th>f = number of cases in each category</th>
<th>OUTCOME EVALUATED AS</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>CONSISTENT</td>
</tr>
<tr>
<td>$F_0(X)$</td>
<td>.15/15</td>
</tr>
<tr>
<td>$S_{15}(X)$</td>
<td>7/15</td>
</tr>
<tr>
<td>$D =</td>
<td>F_0(X) - S_{15}(X)</td>
</tr>
</tbody>
</table>

Since $D = .456 > .404$, this finding is evaluated as significant at the .01 level. However, as in most cases involving a small $N$ this conclusion would not be justified if the number of consistent outcomes was reduced by one. For six consistent outcomes $D = .39$ and is only significant at the .05 level where the critical $D$ is .338.

As an additional check on the statistical significance of this outcome and in order to determine the probability
that this demonstration represents a random sample, the Binomial Test was applied [Siegel, 1956, p. 36-42]. In this test:

\[
P = \text{proportion of cases expected to be consistent}
Q = 1 - P = \text{proportion of cases expected to be inconsistent}
N = \text{number of cases}
x = \text{number of observed consistent outcomes}
\]

The probability of observing exactly seven consistent outcomes is given by:

\[
p(x) = \binom{N}{x} p^x Q^{N-x} = p(7) = \binom{15}{7} (0.01)^7 (0.99)^8
\]

\[
= 0.0000000001
\]

where

\[
\binom{15}{7} = \frac{15!}{7!8!}
\]

Thus \( p(7) \approx 0 \), and the probability of observing five or more consistent outcomes can be computed similarly as \( p(x \geq 5) \approx 0.0000004 \). Since these tests both indicate that the observed frequency of consistent rankings (0.47) was significant, the following conclusion was reached.

Although all event pairs were evaluated as being inconsistent using the cross-event approach's probabilistic criteria (any \( P_1 \) through \( P_8 < 0 \) or \( > 1 \)), in actuality seven cases were consistent when the probabilities were ranked.
and paired by opposite cause. The implications of this finding will be addressed in the concluding chapter.

D. CONCLUSIONS

This chapter described the implementation process designed to demonstrate cross-event analysis in a hypothetical crisis situation. Several problems were encountered in putting the design into effect. During the estimation phase it was discovered that a "brainstorming" session could get out of control and range far from the intended situation, or intimidate some respondents. It also seemed that the respondents had difficulty thinking in terms of discrete events. Furthermore, the method suggested for conducting "event assessment" was found to be inappropriate because it used two different scales and a multiplicative index.

Other problems were encountered in estimating the interrelationships between event pairs. Some problems arose due to limitations in the implementation design, specifically, the problems of monotony and imprecise question wording. Because inconsistent probabilities were obtained, additional problems were suspected to exist in the estimation process. These problems involved the sequence in which the estimates were asked for and the fact that respondents might have lost track of their previous responses in the course of completing the forms. Finally, the way in which relationships were quantified was suspect.
To overcome these problems, several solutions were proposed. An experienced facilitator was recommended to control the brainstorming process. In addition, incorporating a method for respondent self-evaluation was suggested to permit weighting estimates for reliability. Because respondents apparently had difficulty conceptualizing discrete events it was suggested that they thought in terms of interrelations or contingencies.

Improvements to the "event assessment" process included, using similar scales for the measures being combined, and adopting an additive impact index rather than a multiplicative one. It was also noted that further research into the components which constitute an event's impact, and their relative importance was also desirable in order to devise an appropriate algorithm for combining the various measures. Overcoming the problems of monotony and imprecise question wording in assessing interactions requires devising an improved question format.

This improvement could be realized utilizing an interactive computer program. This would also allow respondents to review their estimates, and could be extended to provide probability bounds for estimates, and to present respondents with a display of the results obtained from their inputs. Such programs have been demonstrated in several applications reviewed in this study. The other problems suspected in the estimation process were only hypothesized and could not be
verified without additional study. Data regarding question sequence and respondents' thought processes could be collected while using the interactive computer program.

Once the implementation problems were discussed and possible solutions suggested, the experiment results were presented and analyzed. It was found that the ordered outcome probabilities for each event pair, as computed from the respondents' estimates using the rules of probability theory, contained inconsistent values. However, when the information required from the respondents was presented as causal, time-dependent estimates, and the information contained by the computed output was presented as the respondents' view of the sequence in which the two paired events were likely to occur, another interpretation was possible.

The ordered outcome values could be ranked and paired according to opposite cause. In seven of the fifteen cases, this procedure produced a pattern suitable for exact prediction. This "Chinese Box" pattern was shown to be intuitively pleasing as an indication that the respondents had been logically consistent in their responses.

In order to determine if this result was statistically significant, two tests were applied to the data. The Binomial Test showed that the probability of obtaining more than five "Chinese Boxes" was close to zero, while the Kolmogorov-Smirnov one-sample test showed that the results obtained were significant at the .01 level. Therefore, it
was decided that the respondents had been consistent in almost half of the event pairs, and that the apparent inconsistency in those cases resulted only because the values computed did not produce valid probabilities.

The next chapter will explore the implications of this finding for the future use of cross-impact analysis. This will require evaluating the approach's basic assumptions regarding how interactions are quantified and manipulated. This evaluation will draw on the impression formed during the brainstorming process that respondents may think in terms of interrelations or contingencies. The future utility of cross-impact analysis as a crisis decision-aid will be assessed using the experience gained in applying the technique in this demonstration, and through drawing on the feedback comments made by the study participants. Finally, it is hoped to suggest possible improvements to the technique, and to recommend further areas for study.
V. CONCLUSION

A. INTRODUCTION

Aside from the several minor problems encountered in implementing the selected cross-impact analysis technique in a hypothetical situation, this study revealed a major conceptual limitation in the technique. This conceptual problem underlies a basic assumption which must be adopted in any cross-impact approach. The problem stems from determining what interpretation should be applied to the estimates provided by the expert respondents. This problem relates to determining how individual thought processes actually work, and how complex relationships are conceptualized. The problem underlies any methodology which attempts to employ subjective estimates.

In reviewing cross-impact analysis' basic concepts and assumptions it was noted that several interpretations could be applied to subjective estimates, depending on the assumption made concerning the way individual's interpret and analyze unfolding situations. These alternative interpretations can be grouped into at least two main categories. The first, which was pursued in this study, viewed the estimates as causal probabilities. Under this interpretation, individuals are assumed to be essentially Bayesian information processors.
The second interpretation views subjective estimates as quantified variation estimates, or, as directly describing how a change in one variable produces a change in another variable. Under this interpretation, an individual is assumed to be a more complex information processor than is described by the Bayesian model. This interpretation was used in the Turoff approach, which represented the results obtained from the respondents' estimates as analogous to correlation coefficients.

How the question of interpreting subjective estimates is resolved forms the basis for the methodological approach used in cross-impact analysis. The assumed interpretation determines how inconsistency is identified and corrected. It also influences the method used to obtain estimates and produce cross-impact factors. For these reasons, determining the appropriate assumption to be used in interpreting estimates is essential to performing reliable, useful cross-impact analysis.

The results obtained in this study indicate that a probabilistic interpretation of estimates may not be appropriate. It was demonstrated that, although the ordered outcome values were inconsistent as probabilities, a significant number of event pairs contained an outcome pattern which indicated that a consistent thought process had occurred. Additionally, during event generation, respondents showed a tendency to think in terms of contingencies or interrelations.
This chapter will address the question of how respondents answer the cross-impact questions posed in light of the study results. This discussion will focus on the alternative interpretations proposed, and how each of them may be used in future cross-impact analysis applications. The final section of this chapter will discuss the technique's use as a decision-aiding methodology as it is currently structured. This discussion will highlight the technique's strengths and weaknesses in problem analysis.

B. INTERPRETING RESPONDENT ESTIMATES

Of the two interpretations proposed, the most frequently employed is probability. The inherent advantages of this interpretation were discussed in the technique selection section of Chapter Three. These advantages were primarily methodological in nature. The probabilistic assumption provided a method for determining if respondents' estimates were consistent. Furthermore, by using probabilistic relationships, a well structured algorithm for manipulating estimates was also developed.

1. Probabilities

Using probability values restricted the estimated and computed values to a range between one and zero. Several procedures were designed to correct values which exceeded these bounds. All of these procedures essentially zeroed or made unity the extreme values. As demonstrated in this study, use of these correction procedures could
destroy much information. This is true especially when a large number of extreme responses are obtained. This study also demonstrated that bounding the estimated values to normal probability limits can disguise otherwise consistent results. A possible explanation behind the excessive number of extreme responses is that the respondents do not easily conceptualize events and their interactions in probabilistic terms.

This problem could be reduced if respondents were trained to make probability estimates. An interactive computer package could aid in this process. As discussed previously, such a package could be structured to provide respondents with the probability bounds for their future estimates based on the values previously specified. The program would also furnish the respondents with results computed from their estimates. Repeated exposure to such outputs could increase the respondents' experience with probabilistic relationships. Eventually, they might become proficient in making consistent probabilistic estimates.

However, aside from the previously mentioned methodological advantages, there does not appear to be any innate justification for pursuing this solution. The results of this study indicate that consistent responses can be obtained when using other than consistent probability values. If respondents do find probabilities difficult to work with, yet can produce consistent responses through some other thought process, it might be more appropriate to devise an
analytic procedure which taps expert opinions by using some other algorithm. In this case, the second interpretation given respondents' estimates might be worthy of increased attention and analysis.

2. Variations

The second interpretation given respondents' estimates suggests that individuals may be more comfortable working with a procedure which quantifies the variations produced by one variable interacting with another variable. The fact that the respondents appeared to think in terms of contingencies during event generation lends some support to this interpretation. If it can be determined that respondents are more comfortable when dealing with relative changes in events, a variation algorithm might be used to collect and manipulate their estimates.

Two measures have been developed which describe the relationships between variables (in this case events). Either, or both might be developed for use in cross-impact analysis. Turoff demonstrated the application of one variation measure, a correlation-based algorithm, in his cross-impact approach. The second variation measure, regression, might also be appropriate for use in cross-impact analysis.

Correlation coefficients range between minus and plus one. These boundaries could produce constraints similar to those encountered in using probabilities. However, using
a correlation algorithm would retain a certain ease of manipulation. In addition, it would also be possible to obtain an indication of estimator consistency.

This capability derives from the fact that under this interpretation the cross-impact matrix would be analogous to a correlation matrix. Consistency could therefore be determined through analyzing the matrix entries. A brief example, using a simplified correlation matrix, will demonstrate this point.

FIGURE 9
SIMPLIFIED CORRELATION MATRIX

<table>
<thead>
<tr>
<th>EVENTS</th>
<th>A</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>B</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

In a correlation matrix, if variable C increases with an increase in variable A; then variable A must increase with an increase in variable C. In other words, the matrix entries above the diagonal must mirror the entries below the diagonal to be consistent.
As a final consideration, the theory describing correlation coefficients is well enough developed that other analysis forms might be attempted. For example, the technique of path analysis could be developed as a method for tracing causal relationships. It might also be possible to trace logical structures on adjacency matrices using the principles developed by Harary [Ref. 42], and demonstrated by Bonham, et al., and Axelrod [Refs. 44, 45, and 43]. The correlation algorithm for cross-impacts might also be extended into a regression algorithm.

Regression coefficients represent the second variation measure which might be applied to cross-impact analysis. Because regression coefficients can range between plus and minus infinity, there would be no constraints imposed by bounding estimate values. However, using a regression algorithm could easily produce extremely large values, limiting the ease with which estimates could be manipulated. This fact is apparent upon recalling that some ordered outcome values computed in this study exceeded a value of thirty, and these were calculated using bounded estimates.

3. Summary

This study’s results indicate that the method used in cross-event analysis to tap expert’s opinions may be inappropriate. Two alternatives might be used to overcome this problem. The first possibility is to train respondents to think in probabilistic terms. The second is to develop
another algorithm for interpreting and manipulating their estimates, possibly through using correlation or regression coefficients.

Choosing between these two alternatives cannot be attempted without further study. The primary focus for this additional study would be to empirically determine how people actually conceptualize relationships between events. Without an understanding of this crucial point, selection of a cross-impact algorithm can only be made arbitrarily. As a result, arbitrary estimate interpretation would preclude giving any confidence to specific results obtained from the analysis. Despite this problem, it is felt that the methodology has some potential as an alternative approach to decision analysis in socio-political applications.

C. CROSS-IMPACT ANALYSIS AS A DECISION-AID

Several advantages can be identified for the cross-impact technique when employed in assessing complex situations. First, its systematic approach assures that all problem elements identified as important are considered. The step by step procedure used can be easily traced to identify important elements in the problem situation, and to suggest areas requiring further study or close monitoring.

Secondly, the technique can serve as a valuable heuristic device. Its systematic approach forces respondents to carefully evaluate each estimate (opinion) in conjunction with
their other estimates, and to consider the estimates' implications in toto. This requires that the experts fully and consistently formulate an underlying paradigm which can aid an individual or organization in problem definition. Thus, cross-impact analysis can be a useful modeling tool and problem specification approach.

In addition, because the technique is time sensitive, its results can be used to monitor problem development, or at least the way in which the experts perceive that development. Through monitoring the development of cross-impact matrices it might also be possible to learn more about how individual, group, and organizational thought processes evolve in response to evolving situations, changing information streams, and differing perceptions of problem components. Thus, the technique's continued use might contribute to an understanding of how individuals process information (providing the data with which to resolve the question of how respondent's estimates should be interpreted), and how they perceive developing systems.

Even without having completed the designed implementation, because inconsistent ordered outcome probabilities were obtained, it is still possible to make some observations regarding cross-impact analysis' utility as a decision-aid. Obviously, there are several problems which must be corrected before the technique can be applied in a "real-world" analysis. Many problems encountered in the
demonstration arose from a lack of experience in conducting subjective estimation sessions. Such "operator" problems included controlling the brainstorming session, and conducting the "event analysis." These problems were discussed, and solutions suggested in Chapter Four. None of the implementation problems appear to inhibit using the technique as much as the conceptual problem previously discussed.

The theory that interactions among discrete events can be quantified and systematically assessed seems to be an appropriate method for approaching complex, ill-defined problems. The technique's demonstrated computer adaptability enhances this attractiveness. Using a computer makes it possible to identify a large number of events for analysis. In some cases, it might be possible to practically specify the entire problem environment. Although this would require a very large number of estimates, they could be obtained and manipulated with the computer. However, until the conceptual question discussed in the previous section is resolved, cross-impact analysis remains a developmental methodology.
APPENDIX A

ESTIMATED RESPONSES

1. Candidate event set, probability and significance ratings, impact scores (standard deviations)

<table>
<thead>
<tr>
<th>No.</th>
<th>Event Statement</th>
<th>Prob (S.D.)</th>
<th>Sig. (S.D.)</th>
<th>Imp. (S.D.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Kurds in Soviet Union revolt.</td>
<td>.115 .08</td>
<td>.48 .31</td>
<td>.62 .27</td>
</tr>
<tr>
<td>2</td>
<td>Egypt closes Suez Canal to Soviets.</td>
<td>.315 .12</td>
<td>.595 .22</td>
<td>.91 .17</td>
</tr>
<tr>
<td>3</td>
<td>United States deploys Carrier Task Force to Indian Ocean.</td>
<td>.755 .19</td>
<td>.62 .19</td>
<td>1.375 .31</td>
</tr>
<tr>
<td>4</td>
<td>Soviet Union initiates military alert along Chinese border.</td>
<td>.53 .28</td>
<td>.71 .25</td>
<td>1.24 .47</td>
</tr>
<tr>
<td>5</td>
<td>Soviet Union blockades Gulf of Oman.</td>
<td>.275 .19</td>
<td>.725 .25</td>
<td>1.0 .32</td>
</tr>
<tr>
<td>6</td>
<td>Soviet Union mines St. of Hormuz.</td>
<td>.185 .14</td>
<td>.77 .25</td>
<td>.955 .26</td>
</tr>
<tr>
<td>7</td>
<td>United States appeals to all parties to cease hostilities.</td>
<td>.805 .13</td>
<td>.18 .17</td>
<td>1.04 .17</td>
</tr>
<tr>
<td>8</td>
<td>United States offers to negotiate cease fire.</td>
<td>.64 .18</td>
<td>.48 .23</td>
<td>1.12 .27</td>
</tr>
<tr>
<td>9</td>
<td>United States evacuates civilians from area.</td>
<td>.835 .10</td>
<td>.305 .14</td>
<td>1.135 .14</td>
</tr>
<tr>
<td>10</td>
<td>China ships arms to Baluchi rebels.</td>
<td>.575 .27</td>
<td>.575 .16</td>
<td>1.15 .39</td>
</tr>
<tr>
<td>11</td>
<td>India lends moral support to anti-Soviet forces.</td>
<td>.685 .14</td>
<td>.405 .22</td>
<td>1.09 .29</td>
</tr>
</tbody>
</table>

170
<table>
<thead>
<tr>
<th>No.</th>
<th>Event Statement</th>
<th>Prob (S.D.)</th>
<th>Sig. (S.D.)</th>
<th>Imp. (S.D.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>Chinese mobilize in Sinkiang.</td>
<td>.505 .25</td>
<td>.715 .20</td>
<td>1.22 .37</td>
</tr>
<tr>
<td>13</td>
<td>Iranian leftists sabotage oil fields.</td>
<td>.485 .16</td>
<td>.715 .16</td>
<td>1.20 .27</td>
</tr>
<tr>
<td>14</td>
<td>United States states it has no intention of becoming involved in the situation.</td>
<td>.275 .10</td>
<td>.675 .31</td>
<td>.945 .28</td>
</tr>
<tr>
<td>15</td>
<td>Leftists seize control in Iran.</td>
<td>.37 .14</td>
<td>.805 .14</td>
<td>1.175 .13</td>
</tr>
<tr>
<td>16</td>
<td>United Nations meets to discuss the problem.</td>
<td>.885 .08</td>
<td>.195 .14</td>
<td>1.08 .17</td>
</tr>
<tr>
<td>17</td>
<td>Iranian and Soviet units skirmish in area around Afghanistan.</td>
<td>.485 .25</td>
<td>.625 .20</td>
<td>1.12 .37</td>
</tr>
<tr>
<td>18</td>
<td>Iranian government clamps down on leftists.</td>
<td>.71 .18</td>
<td>.375 .13</td>
<td>1.09 .13</td>
</tr>
<tr>
<td>19</td>
<td>Civil War breaks out in Iran.</td>
<td>.535 .24</td>
<td>.595 .24</td>
<td>1.22 .18</td>
</tr>
<tr>
<td>20</td>
<td>United States convoys oil shipments with Naval units.</td>
<td>.385 .25</td>
<td>.570 .22</td>
<td>.955 .42</td>
</tr>
<tr>
<td>21</td>
<td>Ayatolla Khomeini calls for Jihad.</td>
<td>.48 .25</td>
<td>.545 .27</td>
<td>1.03 .27</td>
</tr>
<tr>
<td>22</td>
<td>Soviet backed Afghani forces subjugate Baluchistan.</td>
<td>.595 .15</td>
<td>.885 .14</td>
<td>1.48 .19</td>
</tr>
<tr>
<td>23</td>
<td>Soviet Union airlifts supplies to Afghanistan.</td>
<td>.72 .20</td>
<td>.65 .17</td>
<td>1.37 .34</td>
</tr>
<tr>
<td>24</td>
<td>United States sends aid to Pakistan.</td>
<td>.465 .16</td>
<td>.60 .12</td>
<td>1.07 .24</td>
</tr>
<tr>
<td>25</td>
<td>United States sends aid to Iran.</td>
<td>.425 .18</td>
<td>.58 .21</td>
<td>1.01 .37</td>
</tr>
<tr>
<td>No.</td>
<td>Event Statement</td>
<td>Prob (S.D.)</td>
<td>Sig. (S.D.)</td>
<td>Imp. (S.D.)</td>
</tr>
<tr>
<td>-----</td>
<td>----------------------------------------------------------------------------------</td>
<td>-------------</td>
<td>-------------</td>
<td>-------------</td>
</tr>
<tr>
<td>26</td>
<td>United States deploys troops to Saudi Arabia.</td>
<td>.255 .13</td>
<td>.625 .17</td>
<td>.88 .22</td>
</tr>
<tr>
<td>27</td>
<td>United States deploys an F-15 squadron to Saudi Arabia.</td>
<td>.475 .23</td>
<td>.425 .2</td>
<td>.90 .40</td>
</tr>
<tr>
<td>28</td>
<td>Soviet Union builds up its Indian Ocean squadron.</td>
<td>.795 .19</td>
<td>.625 .13</td>
<td>1.42 .28</td>
</tr>
<tr>
<td>29</td>
<td>Soviet Union harasses oil tankers.</td>
<td>.25 .20</td>
<td>.685 .25</td>
<td>.935 .30</td>
</tr>
</tbody>
</table>

2. Ranking by Impact (top ten)

<table>
<thead>
<tr>
<th>No.</th>
<th>Short Name</th>
<th>No.</th>
<th>Short Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>22</td>
<td>S.U./Afghan forces gain control</td>
<td>3</td>
<td>U.S. deploys CTF</td>
</tr>
<tr>
<td>28</td>
<td>S.U. builds up I.O. sqdrn.</td>
<td>9</td>
<td>U.S. evacuates civilians</td>
</tr>
<tr>
<td>3</td>
<td>U.S. deploys CTF</td>
<td>8</td>
<td>U.S. offers negotiation</td>
</tr>
<tr>
<td>23</td>
<td>S.U. supplies Afghanistan</td>
<td>7</td>
<td>U.S. appeals for cease fire</td>
</tr>
<tr>
<td>4</td>
<td>S.U. mobilizes Chinese border</td>
<td>24</td>
<td>Aid Pakistan</td>
</tr>
<tr>
<td>19</td>
<td>Civil War in Iran</td>
<td>20</td>
<td>Convoy oil</td>
</tr>
<tr>
<td>12</td>
<td>Chinese mobilize in Sinkiang</td>
<td>25</td>
<td>Aid Iran</td>
</tr>
<tr>
<td>13</td>
<td>Leftists sabotage oil in Iran</td>
<td>14</td>
<td>Non-involvement</td>
</tr>
<tr>
<td>15</td>
<td>Leftist coup in Iran</td>
<td>27</td>
<td>F-15's to Saudi Arabia</td>
</tr>
<tr>
<td>10</td>
<td>China arms Baluchis</td>
<td>26</td>
<td>Troops to Saudi Arabia</td>
</tr>
</tbody>
</table>

(* indicates events chosen for analysis)

3. Estimated interactions by Event Pair

| Event Pair (i,j) | C_{1} (i|j) | C_{2} (j|i) | C_{3} (i|j) | C_{4} (j|i) | C_{5} (i_e|i&s) |
|------------------|-----------|-------------|-------------|-------------|----------------|
| (22,28)          | .66       | .83         | .56         | .80         | .23            |
| (22,23)          | .72       | .80         | .54         | .70         | .24            |
| Event Pair (i,j) | P(i)|P(j) | $C_1$ (i|j) | $C_2$ (j|i) | $C_3$ (i|i) | $C_4$ (j|i) | $C_5$ (i|j) | $C_6$ (i&j) |
|-----------------|-----|-----|----------|----------|----------|----------|----------|----------|
| (22,3)         | .6 | .76 | .57      | .85      | .67      | .76      | .51      |
| (22,9)         | .6 | .84 | .68      | .92      | .59      | .83      | .51      |
| (22,8)         | .8 | .72 | .58      | .61      | .65      | .68      | .32      |
| (28,23)        | .8 | .76 | .82      | .77      | .79      | .72      | .56      |
| (28,3)         | .8 | .84 | .86      | .87      | .80      | .75      | .61      |
| (28,9)         | .8 | .64 | .81      | .86      | .80      | .84      | .77      |
| (28,8)         | .72| .76 | .66      | .81      | .66      | .74      |
| (23,3)         | .72| .84 | .75      | .81      | .73      | .75      | .56      |
| (23,9)         | .72| .64 | .73      | .86      | .72      | .83      | .78      |
| (23,8)         | .76| .84 | .73      | .70      | .73      | .64      | .69      |
| (23,9)         | .76| .84 | .79      | .86      | .78      | .83      | .80      |
| (3,8)          | .76| .84 | .77      | .65      | .77      | .68      | .52      |
| (9,8)          | .84| .64 | .82      | .66      | .85      | .67      | .35      |
APPENDIX B

CALCULATED RESPONSES

1. Resultant ordered outcome probabilities by Event Pair

<table>
<thead>
<tr>
<th>Event Pair (i,j)</th>
<th>$P_1$ (i,j)</th>
<th>$P_2$ (i,j)</th>
<th>$P_3$ (I,j)</th>
<th>$P_4$ (I,I)</th>
<th>$P_5$ (j,i)</th>
<th>$P_6$ (j,I)</th>
<th>$P_7$ (j,j)</th>
<th>$P_8$ (j,j)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(22,28)</td>
<td>2.6</td>
<td>.53</td>
<td>-9.7</td>
<td>-2.4</td>
<td>8.7</td>
<td>4.5</td>
<td>39.3</td>
<td>30.9</td>
</tr>
<tr>
<td>(22,23)</td>
<td>5.1</td>
<td>.53</td>
<td>-15.3</td>
<td>-7.4</td>
<td>16.3</td>
<td>6.3</td>
<td>-66.6</td>
<td>-56.8</td>
</tr>
<tr>
<td>(22,3)</td>
<td>1.6</td>
<td>.28</td>
<td>-2.5</td>
<td>-.78</td>
<td>1.5</td>
<td>1.2</td>
<td>-2.7</td>
<td>-1.3</td>
</tr>
<tr>
<td>(22,9)</td>
<td>-1.5</td>
<td>-.13</td>
<td>-.6</td>
<td>-.12</td>
<td>-1.5</td>
<td>-.69</td>
<td>3.6</td>
<td>2.5</td>
</tr>
<tr>
<td>(22,8)</td>
<td>4.5</td>
<td>2.9</td>
<td>-18.3</td>
<td>-8.6</td>
<td>6.1</td>
<td>4.5</td>
<td>-22.4</td>
<td>-12.1</td>
</tr>
<tr>
<td>(28,23)</td>
<td>1.3</td>
<td>.38</td>
<td>-1.3</td>
<td>-.51</td>
<td>1.0</td>
<td>.22</td>
<td>-1.3</td>
<td>-.35</td>
</tr>
<tr>
<td>(28,3)</td>
<td>1.2</td>
<td>.12</td>
<td>-1.2</td>
<td>-.39</td>
<td>.75</td>
<td>.12</td>
<td>-.55</td>
<td>-.14</td>
</tr>
<tr>
<td>(28,9)</td>
<td>1.5</td>
<td>.24</td>
<td>-.55</td>
<td>-.10</td>
<td>.44</td>
<td>.10</td>
<td>.16</td>
<td>.04</td>
</tr>
<tr>
<td>(28,8)</td>
<td>-.16</td>
<td>-.1</td>
<td>-.70</td>
<td>-.36</td>
<td>-.06</td>
<td>-.02</td>
<td>.91</td>
<td>.21</td>
</tr>
<tr>
<td>(23,3)</td>
<td>1.4</td>
<td>.32</td>
<td>-1.4</td>
<td>-.47</td>
<td>1.1</td>
<td>.37</td>
<td>-1.5</td>
<td>-.55</td>
</tr>
<tr>
<td>(23,9)</td>
<td>1.2</td>
<td>.19</td>
<td>-.57</td>
<td>-.12</td>
<td>.34</td>
<td>.13</td>
<td>.23</td>
<td>.09</td>
</tr>
<tr>
<td>(23,8)</td>
<td>2.3</td>
<td>.97</td>
<td>-1.2</td>
<td>-.67</td>
<td>1.0</td>
<td>.38</td>
<td>-1.2</td>
<td>-.44</td>
</tr>
<tr>
<td>(3,9)</td>
<td>1.1</td>
<td>.18</td>
<td>-.48</td>
<td>-.10</td>
<td>.28</td>
<td>.07</td>
<td>.37</td>
<td>.08</td>
</tr>
<tr>
<td>(3,8)</td>
<td>1.9</td>
<td>1.0</td>
<td>1.8</td>
<td>-.85</td>
<td>1.7</td>
<td>.30</td>
<td>-3.4</td>
<td>-1.0</td>
</tr>
<tr>
<td>(9,8)</td>
<td>1.2</td>
<td>.63</td>
<td>-2.7</td>
<td>-1.3</td>
<td>2.3</td>
<td>.50</td>
<td>-6.8</td>
<td>-1.2</td>
</tr>
</tbody>
</table>
2. Probability rankings by Event Pair

(22,28) Or: Sov/Afg. forces gain control of Baluchistan, Soviet Union builds up I.O. squadron

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P7</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>2. P8</td>
<td>(j,î)</td>
<td></td>
</tr>
<tr>
<td>3. P5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>4. P6</td>
<td>(j,î)</td>
<td></td>
</tr>
<tr>
<td>5. P1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>6. P2</td>
<td>(i,î)</td>
<td></td>
</tr>
<tr>
<td>7. P4</td>
<td>(î,j)</td>
<td></td>
</tr>
<tr>
<td>8. P3</td>
<td>(î,j)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Inconsistent

(22,23) Or: Sov/Afg. forces gain control of Baluchistan, Soviets airlift supplies to Afghanistan

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>2. P6</td>
<td>(j,î)</td>
<td></td>
</tr>
<tr>
<td>3. P1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>4. P2</td>
<td>(i,î)</td>
<td></td>
</tr>
<tr>
<td>5. P4</td>
<td>(î,j)</td>
<td></td>
</tr>
<tr>
<td>6. P3</td>
<td>(î,j)</td>
<td></td>
</tr>
<tr>
<td>7. P8</td>
<td>(î,i)</td>
<td></td>
</tr>
<tr>
<td>8. P7</td>
<td>(î,i)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Consistent
(22,3) Or: Sov/Afg. forces gain control of Baluchistan, U.S. deploys CTF to I.O.

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P₁</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>2. P₅</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>3. P₆</td>
<td>(j,₁)</td>
<td></td>
</tr>
<tr>
<td>4. P₂</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>5. P₄</td>
<td>(₁,j)</td>
<td></td>
</tr>
<tr>
<td>6. P₈</td>
<td>(₁,j)</td>
<td></td>
</tr>
<tr>
<td>7. P₃</td>
<td>(₁,j)</td>
<td></td>
</tr>
<tr>
<td>8. P₇</td>
<td>(₁,j)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Apparently Inconsistent, however, value difference from rank 7 to rank 8 is only .2; therefore, possibly consistent

(22,9) Or: Sov/Afg. forces gain control of Baluchistan, U.S. evacuates civilians from area

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P₇</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>2. P₈</td>
<td>(j,₁)</td>
<td></td>
</tr>
<tr>
<td>3. P₄</td>
<td>(₁,j)</td>
<td></td>
</tr>
<tr>
<td>4. P₂</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>5. P₃</td>
<td>(₁,j)</td>
<td></td>
</tr>
<tr>
<td>6. P₆</td>
<td>(j,₁)</td>
<td></td>
</tr>
<tr>
<td>7. P₅</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>8. P₁</td>
<td>(i,j)</td>
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</tr>
</tbody>
</table>

Evaluation: Inconsistent
(22,8) Or: Sov/Afg. forces gain control of Baluchistan, U.S. offers to negotiate a cease-fire

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P₅</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>2. P₁</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>3. P₆</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>4. P₂</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>5. P₄</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>6. P₈</td>
<td>(1,1)</td>
<td></td>
</tr>
<tr>
<td>7. P₃</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>8. P₇</td>
<td>(j,1)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Consistent

(28,23) Or: S.U. builds up I.O. squadron, Soviets airlift supplies to Afghanistan

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P₁</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>2. P₅</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>3. P₂</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>4. P₆</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>5. P₈</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>6. P₄</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>7. TIE P₃ &amp; P₇</td>
<td>(1,j) &amp; (j,1)</td>
<td>TIE</td>
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</tbody>
</table>

Evaluation: Consistent because P₃ = P₇.
(28,3) Or: S.U. builds up I.O. squadron
U.S. deploys CTF to I.O.

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P_1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>2. P_5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>3. TIE P_2 &amp; P_6</td>
<td>(i,j) &amp; (j,i)</td>
<td>TIE</td>
</tr>
<tr>
<td>4.</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5. P_8</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>6. P_4</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>7. P_7</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>8. P_3</td>
<td>(i,j)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Consistent due to tie as in previous case.

(28,9) Or: S.U. builds up I.O. squadron,
U.S. evaculates civilians from area

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P_1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>2. P_5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>3. P_2</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>4. P_7</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>5. P_6</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>6. P_8</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>7. P_4</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>8. P_3</td>
<td>(i,j)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Inconsistent
(28,8) Or: S.U. builds up I.O. squadron
U.S. offers to negotiate a cease-fire

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P_7</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>2. P_8</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>3. P_6</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>4. P_5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>5. P_2</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>6. P_1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>7. P_4</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>8. P_3</td>
<td>(1,j)</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Inconsistent

(23,3) Or: S.U. airlifts supplies to Afghanistan,
U.S. deploys CTF to I.O.

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
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<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. P_1</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>2. P_5</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>3. P_6</td>
<td>(j,1)</td>
<td></td>
</tr>
<tr>
<td>4. P_2</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>5. P_4</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>6. P_8</td>
<td>(1,1)</td>
<td></td>
</tr>
<tr>
<td>7. P_3</td>
<td>(1,j)</td>
<td></td>
</tr>
<tr>
<td>8. P_7</td>
<td>(j,i)</td>
<td></td>
</tr>
</tbody>
</table>

| Dif. | = .07 |

Evaluation: Apparently Inconsistent, however, value difference from rank 7 to rank 8 is only .07, therefore, Consistent.
(23,9) Or: S.U. airlifts supplies to Afghanistan, U.S. evacuates civilians from area

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. $P_1$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>2. $P_5$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>3. $P_7$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>4. $P_2$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>5. $P_6$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>6. $P_8$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>7. $P_4$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>8. $P_3$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation: Inconsistent

(23,8) Or: S.U. airlifts supplies to Afghanistan, U.S. offers to negotiate a cease-fire

<table>
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<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
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</thead>
<tbody>
<tr>
<td>1. $P_1$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>2. $P_5$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>3. $P_2$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>4. $P_6$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>5. $P_8$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
<tr>
<td>6. $P_4$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>7. $P_3$</td>
<td>$(i,j)$</td>
<td></td>
</tr>
<tr>
<td>8. $P_7$</td>
<td>$(j,i)$</td>
<td></td>
</tr>
</tbody>
</table>

| | | $|\text{Dif.}| = .01$ |

Evaluation: Apparently Inconsistent, however, value difference between rank 7 and rank 8 is only .01, therefore, Consistent.
(3,9) Or: U.S. deploys CTF to I.O.
U.S. evacuates civilians from area

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
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</tr>
</thead>
<tbody>
<tr>
<td>1. P₁</td>
<td>(i,j)</td>
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</tr>
<tr>
<td>2. P₇</td>
<td>(j,i)</td>
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</tr>
<tr>
<td>3. P₅</td>
<td>(j,i)</td>
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</tr>
<tr>
<td>4. P₂</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>5. P₈</td>
<td>(j,i)</td>
<td></td>
</tr>
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<td>6. P₆</td>
<td>(j,i)</td>
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<td>7. P₄</td>
<td>(i,j)</td>
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<tr>
<td>8. P₃</td>
<td>(i,j)</td>
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</table>

Evaluation: Inconsistent.

(3,8) Or: U.S. deploys CTF to I.O.,
U.S. offers to negotiate a cease-fire

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
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</thead>
<tbody>
<tr>
<td>1. P₁</td>
<td>(i,j)</td>
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</tr>
<tr>
<td>2. P₃</td>
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<td></td>
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<tr>
<td>3. P₅</td>
<td>(j,i)</td>
<td></td>
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<tr>
<td>4. P₂</td>
<td>(i,j)</td>
<td></td>
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<tr>
<td>5. P₆</td>
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</tr>
<tr>
<td>6. P₄</td>
<td>(i,j)</td>
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<td>7. P₈</td>
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</tr>
<tr>
<td>8. P₇</td>
<td>(j,i)</td>
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</tbody>
</table>

Evaluation: Inconsistent.
9,8 Or: U.S. evacuates civilians from area, U.S. offers to negotiate a cease-fire

<table>
<thead>
<tr>
<th>Outcome Ranking</th>
<th>Meaning</th>
<th>Pairing by Opp. Cause</th>
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</thead>
<tbody>
<tr>
<td>1. P5</td>
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</tr>
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<td>2. P1</td>
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</tr>
<tr>
<td>3. P2</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>4. P6</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>5. P8</td>
<td>(j,i)</td>
<td></td>
</tr>
<tr>
<td>6. P4</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>7. P3</td>
<td>(i,j)</td>
<td></td>
</tr>
<tr>
<td>8. P7</td>
<td>(j,i)</td>
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Evaluation: Consistent

3. Summary of Results

<table>
<thead>
<tr>
<th>Case</th>
<th>Pair</th>
<th>Consistent</th>
<th>Order</th>
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<tbody>
<tr>
<td>1</td>
<td>(22,28)</td>
<td>NO</td>
<td>7, 8, 5, 6, 1, 2, 4, 3</td>
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<tr>
<td>2</td>
<td>(22,23)</td>
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<td>5, 6, 1, 2, 4, 3, 8, 7</td>
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<tr>
<td>3</td>
<td>(22,3)</td>
<td>NO</td>
<td>1, 5, 6, 2, 4, 8, 3, 7</td>
</tr>
<tr>
<td>4</td>
<td>(22,9)</td>
<td>NO</td>
<td>7, 8, 4, 2, 3, 6, 5, 1</td>
</tr>
<tr>
<td>5</td>
<td>(22,8)</td>
<td>YES</td>
<td>5, 1, 6, 2, 4, 8, 3, 7</td>
</tr>
<tr>
<td>6</td>
<td>(28,23)</td>
<td>YES</td>
<td>1, 5, 2, 6, 8, 4, 7, 3</td>
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<tr>
<td>7</td>
<td>(28,3)</td>
<td>YES</td>
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</tr>
<tr>
<td>8</td>
<td>(28,9)</td>
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<td>9</td>
<td>(28,8)</td>
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<td>15</td>
<td>(9,8)</td>
<td>YES</td>
<td>5, 1, 2, 6, 8, 4, 3, 7</td>
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All inconsistent outcome orders are unique. The seven consistent outcome patterns occur in 5 sets.
LIST OF REFERENCES


<table>
<thead>
<tr>
<th>No.</th>
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<th>Copies</th>
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Alexandria, Virginia 22314                                                      | 2      |
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Monterey, California 93940                                                     | 2      |
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Naval Postgraduate School  
Monterey, California 93940                                                      | 3      |
| 4.  | LT Ralph Schindler, USN  
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Raleigh, N.C., 27612                                                          | 1      |
| 5.  | Professor Boyd Huff, Code 56Hf  
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Monterey, California 93940                                                      | 1      |