Design Study for an AURORA Modification Leading to a 100-TeraWatt Nuclear Weapon Radiation Simulator

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The AURORA machine can be converted to provide beam power outputs near the 10^{14} W power level into low impedance loads. The proposed conversion is based on a novel approach to pulse power intensification. The approach can be adapted to AURORA in differing configurations. A device of toroidal geometry utilizes the fast pulse charge capability of the AURORA generator to inject a traveling electromagnetic wave into a toroidal oil-filled coaxial line. From the point of injection, electromagnetic waves are propagated along the axis of the torus in opposite directions and at some time $t$ will...
meet each other at the end of the torus diametrically opposite the injection point. As the electromagnetic waves overlap, that portion of their energy stored in the magnetic field will be transformed into electrostatic energy, and the voltage in this region will double. At some optimum preselected time \( t' \), where \( t' > t \), the toroidal line is then switched circumferentially into an oil-insulated three-electrode parallel-plate transmission line to the diode load. A transmission-line model for the complete system has been developed and analyzed by computer to determine energy transfer efficiencies and power inputs into a matched ohmic load. It has been determined that peak power levels of 90 TW are achievable in a pulse of 30 ns full width at half maximum.
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1. INTRODUCTION

The effectiveness of strategic weapons systems depends on their ability to function in a hostile nuclear environment. For some years now, there has been a shift of emphasis away from systems hardening through underground testing toward laboratory testing in specially equipped simulation centers. These centers employ a variety of pulsed-power sources for the production of intense electron beams, electromagnetic waves, and gamma and neutron pulses. While these test facilities have proved invaluable in simulating certain aspects of a warhead's radiation output, there remains a need for a source more closely approximating the outputs of real weapons. One such source could be the radiation emanating from a highly compressed pellet. Recent studies have shown that a relativistic electron beam with peak powers of $10^{14}$ to $10^{15}$ W would be required for this purpose, or, alternatively, ion beams at $10^{12}$ to $10^{13}$ W could accomplish this same goal. Techniques for the efficient conversion of relativistic electron beams to focused ion beams have been investigated by Humphries and Verdeyen. Electron-to-ion conversion efficiencies as high as 50 percent have been reported.

One limitation to the extraction of very intense power pulses from the Harry Diamond Laboratories AURORA generator in its present form is the rather long discharge time of the blumleins. A second disadvantage is the high internal impedance of these lines ($21 \, \Omega$), which makes them inefficient for energy transfer to low impedance loads. Studies conducted for the present AURORA Modification Project have shown that it is possible to use the AURORA Marx generator to charge a water-insulated pulse-forming network (PFN) to generate 20 TW. This approach, however, does not seem capable of extension to significantly higher power outputs. The purpose of this study is to demonstrate that it may be possible to extract power outputs closer to the 100-TW level and to operate efficiently into loads near 1 $\Omega$.

2. PRINCIPLE OF PULSE COMPRESSION AND IMPEDANCE TRANSFORMATION

The principle of operation of the device is described in detail in U.S. Patent 4,003,007, so only the basic ideas are discussed here.

2.1 Application to Geometries Consisting of Right-Angled Coaxial Cylinders Discharging into Triangular Strip Feed Lines

Referring to figure 1, a pulse of duration $T_0$ is injected into the left-hand side of the center conductor of the coaxial-cylinder element referred to as the longitudinal line. As generally assumed, when the pulse is transmitted into the line and then reflected from the open-circuit end of the line, the line is statically charged all along its length. It is also generally assumed that the length of this line is very much larger than its diameter. A second line, identified as the triangular strip feed line, is attached to the longitudinal line as shown in figure 1. The center conductor of the feed line is separated from the center conductor of the longitudinal line so that, during the charging phase of the latter, the former remains near ground potential. Since the right-hand side of the longitudinal line is an open circuit, the in-
jected pulse is reflected on arrival at this end, and the reversal doubles the amplitude of the incident pulse. This reflected pulse then is propagated back toward the point of origin. The voltage developed across the gap spacing between the two center conductors also is doubled. When the reflected wave has completed approximately two thirds of its travel toward the injection point, a controlled electrical breakdown between the two inner electrodes is initiated at the extreme right-hand side of the system. The propagation of this breakdown (switching) is such that, when the reflected wave finally reaches the point of injection, breakdown also is occurring at this time and place.

\[ Z_0 = \frac{1}{2} \cdot \frac{377}{\sqrt{K}} \cdot \frac{b - a}{L} (\Omega) \]  

where \( K \) is the dielectric constant of the medium between the coaxial cylinders and \( a \) and \( b \) are the inner and outer radii, respectively. The discharge impedance, \( Z_0 \), of this line is, however, governed by the equation appropriate to a triplanar strip line, that is,

The input impedance, \( Z_i \), of the longitudinal line is given by the relationship

\[ Z_i = \frac{60}{\sqrt{K}} \ln \frac{b}{a} (\Omega) \]

Since \( Z_0 \) can be readily made to be significantly lower than \( Z_i \), this technique of energy extraction is capable also of impedance transforming with very high efficiencies.

The impedance of the strip feed line can be readily matched to the discharge impedance of the longitudinal line.

2.2 Application to Toroidal Geometries

A second application is to inject the pulse into a toroidal geometry. Toroidal geometries have the advantage that they can be made more compact than the equivalent straight coaxial-cylinder approach. Also, the switching requirements are less stringent since all the switches are operated synchronously, rather than in a controlled rate of breakdown. Finally, the symmetry of the discharge line is less likely to lead to pulse spreading as the energy is propagated toward the load.

2.2.1 Single-Ended Pulse Injection

The single-ended toroidal pulse injection is illustrated in figure 2. Traveling waves are propagated around both arms of the torus, and their leading edges are allowed to
overlap until the voltage reaches approximately one half of the peak amplitude before synchronous triggering is induced along the inside perimeter of the torus. The output line from the torus is shown in figure 2 configured in cylindrical geometry, which would make it compatible for matching to the type of diode structures which have been developed for other systems, that is, Blackjack and Pithon.* The discharge line need not be directed inward toward the axis of the torus. It could, with equal effectiveness, be directed outward (at 180 deg) away from the torus axis.

![Figure 2. Pulse injection into torus.](image)

**2.2.2 Double-Ended Pulse Injection**

Several studies have been made on the design of a low impedance conversion of AURORA charged directly from the AURORA Marx generator. The major design efforts in these studies were directed toward a two-module output device. As shown in figure 3, it is conceptually feasible to use each of these modules as the pulse injectors into each of the two arms of a half torus and to extract the energy from this half torus in the same manner as described in section 2.2.1. This approach has an additional advantage in that the pulse injection time is very short (~60 ns), which would permit higher fields and, hence, smaller torus dimensions, for the same stored energy. This smaller torus would permit even shorter pulse outputs.

![Figure 3. Use of low impedance converter modules as torus pulse charge injector.](image)

3. **LINES IN CASCADE**

There are distinct advantages to be gained from making the pulse injection time as short as possible, especially if high-energy, ultrashort (<20 ns) pulse outputs are desired. By employing two or more of the injection devices in tandem, this goal of <20 ns can be achieved.

3.1 **Combination of Straight Coaxial Cylinders with Torus**

In figure 4, the two longitudinal lines A and A', pulse-charged from a single-ended injection point, are discharged into the two arms of a half torus. Because the pulse duration at the output of the feed line is significantly shorter than the pulse duration at
the input, the dimensions of the half torus can be considerably smaller than are necessary if the initial pulse alone is used to charge the torus. The smaller the torus, the faster the energy that can be extracted from it and the lower the output impedance of the system.

Figure 4. Pulse charging half torus from triangular strip feed line.

3.2 Combination of Straight Coaxial-Cylinder Geometries

In Figure 5, the output of the first feed line is used as input to a second longitudinal line, which is similarly charged and discharged as the first element, but whose overall dimensions are smaller because of the higher permissible electric-field gradients. Further additions can be made, as shown in Figure 5, each stage leading in principle to pulse outputs of shorter duration, lower impedance, and higher power.

4. DETAILED ANALYSIS OF TOROIDAL GEOMETRY FRONT-END CONVERSION TO AURORA

The various options were reviewed for converting AURORA to a 100-TW generator suitable for the compression of pellets. Such additional factors were considered as ease of conversion to and from the bremsstrahlung mode, initial capitalization costs, and compatibility with existing state-of-the-art high voltage technology. It was decided that the preliminary design study should focus on one particular configuration to obtain first-order estimates of the important design parameters and energy transport efficiencies. The configuration chosen for this study was the toroidal geometry. The conversion system is assumed to be energized from the front end of the AURORA simulator and to be located in the existing test cell.

4.1 Combination of Existing Vacuum Coaxial Lines into Single Coaxial Line

The present AURORA simulator has four separate 50-Ω vacuum coaxial lines feeding four separate field-emission diodes. It would be necessary for these to be filled with some suitable dielectric and, for simplicity, to be the same insulating medium as used in the torus itself—oil. (For short pulse output applications, transformer oil (K = 2.3) is preferred to water as an insulant because of the higher velocity of electromagnetic waves in oil.) Filling each of these coaxial lines with transformer oil without changing either the inner or the
outer radii of the coaxial cylinders would reduce their individual impedances to 33 Ω. To achieve single-point pulse injection into the torus, it is necessary to combine this array of coaxial lines into a single coaxial line (fig. 6). The parallel impedance of the four coaxial lines is 8.24 Ω, and, to eliminate reflections at the junction, the impedance of the single coaxial-line output should be matched to this value.

**Figure 6. Junction of AURORA coaxial lines into single coaxial line.**

4.2 Design Considerations for Torus

To arrive at a feasible conceptual design for the torus, many factors must be considered and analyzed for self-consistency and compatibility with the state of the art of high voltage technology. Principal among these are the dimensions of the torus that determine its input and output impedances and the electric fields experienced within it.

4.2.1 Torus Dimensions and Determination of Input and Output Impedances

The preliminary design chosen for detailed study in this report is shown in figure 7. The dimensions are those that were arrived at after consideration of the various constraints, such as available space in the AURORA test cell, energy transfer efficiencies, and electrical breakdown conditions. The final dimensions of the preliminary study are presented here.

**Figure 7. Low impedance converter.**

The major diameter, D, of the torus is 13.7 m, and the coaxial cylinders have radii b and a of 1.091 m and 0.600 m, respectively, giving a gap separation of 0.491 m. The line impedance, \( Z_0 \), of the torus is therefore given by

\[
Z_0 = \left( \frac{60}{\sqrt{\pi}} \right) \ln \left( \frac{b}{a} \right) = 23.7 \, (\Omega)
\]

For ideal matching to the pulse injection line, this impedance should be twice the impedance of the pulse injection line—16.48 Ω—so some energy is lost due to reflections at this interface. In fact, for ideal matching to the four parallel blumleins (overall \( Z = 5 \, \Omega \)), the torus impedance should be even lower (closer to 10 Ω). This higher impedance torus, on the other hand, presents less stringent requirements on the fields to be sustained in the oil, and, since the intent of this preliminary study was to acquire only first-order design information, this trade-off was judged to be a reasonable one.

The output impedance of the torus is inversely proportional to the length of the element being discharged and, for this case, was chosen to be three quarters of the circumference—270 deg. As will be shown, this gives a discharge impedance of 1.89 Ω, which is not an optimum value in terms of basic design goals, but is sufficiently close to provide
valuable baseline data for development of the concept.

4.2.2 Transmission-Line Analysis

The primary tool for the electrical analysis of the system is a transmission-line model of the blumleins, the oil-filled "vacuum" coaxial lines, and the torus itself. The model is shown in figure 8. The flow of electromagnetic waves through the model was calculated with an expanded form of a computer code supplied by J. Shipman of the Naval Research Laboratory. Since it is assumed that each of the four blumlein subsystems is identical, the entire array of blumleins is represented in the model by elements of one blumlein, each element having one fourth the impedance of the corresponding element in the actual blumlein.

![Figure 8. Transmission-line model for charge phase.](image)

A similar simplification is done for the torus. In actuality, a single oil coaxial line divides at the torus into the two arms, one directed to the left, the other directed to the right. At 180 deg from the torus entry point, these arms join. Because what is happening in the left arm of the torus is assumed to be identical to what is happening in the right arm, the two arms can be replaced in the model by one arm having half the impedance of either actual arm and an identical one-way transmission time from 0 to 180 deg. Waves having passed the 180-deg point in the real torus are produced in the model as reflections from the open end of the single arm in the model.

The charge and the discharge phases are treated as two separate problems in the present analysis. During the charge phase, the calculation shows the appearance given in figure 9 of the two waves overlapping in the torus. At about 350 ns after blumlein switching, the waves in the torus overlap to form the net voltage profile shown in figure 10. At this time, the current throughout the torus is negligible, and almost all the energy is stored electrostatically. This is the time chosen for switching the torus into its discharge configuration.

![Figure 9. Overlapping voltage pulses in torus.](image)

4.2.3 Electric Fields in Torus

At a given time and angular position in the torus, the maximum field, $F$, exists at the surface of the inner coaxial cylinder and is given by the relation

$$F = V_0/[a \ln (b/a)]$$
where \( V_0 \) is the voltage. The negative impulse breakdown strength for transformer oil is given approximately by the relation

\[
F_- = 0.875A^{-0.37}t^{-0.333} \text{ (MV/cm)}
\]

where \( F_- \) is the maximum permissible field, \( A \) is the area of the inner electrode in square centimeters, and \( t \) is the time in microseconds that the voltage exceeds 63 percent of its breakdown value. This equation is most readily applied in situations where a large area of an electrode is exposed uniformly to the same time-dependent field. This uniformity, however, is not the case in the torus as suggested by figures 9 and 10.

Consider the voltage/time profile \( V(t) \) at a given position in the torus. For this \( V(t) \), \( A \) has been calculated (by use of the breakdown formula) over which \( V(t) \) can be

\[
A = \frac{(1.875e^{-t})^{1.333}}{180}
\]

Figure 11 relates \( A \), as determined from the breakdown formula, to angular position in the torus. The horizontal axis is labeled also in terms of area measured along the center conductor. From this graph, the likelihood of an electric breakdown at any position in the torus is determined as follows:

To assess the ability of the torus to withstand breakdown, the function \( V(t) \) was considered at each of 13 positions in the transmission-line model of the torus (every 15 deg from 0 through 180 deg). In using these functions \( V(t) \), it was assumed that the torus would switch at 350 ns, thus drastically reducing the voltage within about 15 ns of the switching time. (Fifteen nanoseconds is the approximate transit time during the discharge phase of the torus.) For argument, it was assumed that the maximum field given by a particular \( V(t) \) was the breakdown field. These peak fields range from 0.47 to 0.90 MV/cm. The time parameters, \( t \), were obtained from \( V(t) \) and ranged from 0.065 to 0.185 us. Then, \( A \) was derived for each position by using the relations above.

Figure 11 relates \( A \), as determined from the breakdown formula, to angular position in the torus. The horizontal axis is labeled also in terms of area measured along the center conductor. From this graph, the likelihood of an electric breakdown at any position in the torus is determined as follows:

Consider the voltage/time profile \( V(t) \) at a given position in the torus. For this \( V(t) \), \( A \) has been calculated (by use of the breakdown formula) over which \( V(t) \) can be
sustained without breakdown. This A is compared with area B in the torus over which V(t)'s of the same or greater severity are experienced. If A is significantly greater than B, the spacing of the inner and outer conductors of the torus is adequate to prevent breakdown at the position under consideration.

As can be seen by looking over the entire torus, the design is favorable. For most positions, tolerable A is well in excess of the total area \(1.62 \times 10^8 \text{ cm}^2\) of the torus. From about 145 to 180 deg, however, the present design is only marginally adequate.

### 4.3 Torus Switch Discharge Characteristics

Experience on the AURORA simulator has shown that reproducible, multichannel switching in oil can be achieved by using positive-field enhanced-edge electrodes, for average fields in the main gap of approximately 25 MV/m. The main gap separation on the AURORA electrodes is typically about 0.46 m, which is almost identical to the gap spacing between the inner and outer cylinders of the torus studied here. Calculations also show that the field in the torus switch region would be about 50 to 100 MV/m. It is not known for certain whether this higher-field operation leads to an overall degradation or improvement of the switch performance. If the switch-breakdown characteristics follow the same general development as that observed for switching in water, then the faster pulse charge coupled with these higher fields should give improved operation with lower impedance and lower jitter. The overall switch inductance should be considerably smaller here than that estimated for AURORA (200 nH) since channels form around three quadrants of the torus perimeter, a distance of more than 30 m, as compared with the 3.7 m of edge of the AURORA midplane. These figures suggest an inductance of ~20 nH for the torus switch. This inductance is incorporated into the discharge phase of the transmission-line calculation. No further development of this triggered switch concept has been undertaken in this study.

### 4.4 Design of Strip Wedge Transformer

The function of the strip wedge transformer is to transport the energy from the discharging torus to the diode. For maximum energy transport, the wedge impedance should be constant all along its discharge path, and, in the present study, this was the design criterion used. However, the wedge could be designed to transform the impedance from a relatively high impedance at the wedge input to a lower impedance at the wedge output with small energy penalty. The impedance can be transformed by taking advantage of the higher fields that can be sustained in the wedge compared with those in the torus primarily because of the shorter times of applied voltages, thus reducing the gap dimensions, and by locating the diode structure at a location other than the axis of symmetry of the torus. This latter technique may be useful also for obtaining higher peak power outputs than the output obtainable from a completely symmetrical discharge. These considerations are not investigated further, however, in the present report.

The impedance of the wedge may be shown to be approximately 2 \(\Omega\) as follows:

In its discharge phase following switching, the torus behaves like an open-ended triplanar strip line with a plate spacing equal to the spacing between the inner and outer conductors of the torus, namely, \(S = 0.491\) m. For this triplanar strip line, with an effective torus diameter \(D = 13.7\) m and switching over 270 deg, the width \(W\) is \((270/360)\pi D = 32.3\) m. By use of equation (1), this gives an impedance of 1.89 \(\Omega\) for the triplanar strip line as formed by the torus itself.

The torus discharges into another triplanar strip line, the wedge transformer of
I1i

4.5 Prepulse Estimates and Effects

Because of capacitive coupling between that portion of the center conductor of the torus and the inner conductor of the strip line wedge transformer in the switch region, some fraction of the voltage impressed on the torus center conductor during the torus charge phase appears on the wedge transformer's inner conductor. This voltage in turn is transmitted to the diode cathode as a prepulse. Depending on the amplitude and the duration of this prepulse, the current emission and beam dynamics in the anode-cathode gap region can be significantly affected. Most of the information on prepulse has been empirically derived, and no comprehensive theory has been developed to predict its effects. It is known that large prepulses can induce premature pinching in the anode-cathode gap of high current diodes, and it is generally desirable to keep this voltage small. It is known also, however, that prepulse effects are sensitive to diode structure; that is, an identical prepulse injected into two dissimilar diode structures produces markedly different effects. Further, some workers have suggested that a well-controlled prepulse of small amplitude can even have beneficial effects on diode performance through preconditioning the cathode. It is not the intent of this study to make a comprehensive review of the literature to investigate these effects in detail, but rather to make an initial first-order calculation of the amplitude and the duration of the prepulse anticipated for the geometry chosen for this study.

When the geometry is considered as a parallel-plate capacitor, the capacitance, $C_r$, between the inner conductor of the torus and

![Figure 12. Center electrode of wedge transformer.](image-url)
the inner conductor of the wedge transformer
is, to a first approximation,

\[ C_1 = K \varepsilon_0 \frac{\text{area}}{\text{separation}} \]

\[ = K \varepsilon_0 \frac{2\pi r w f}{S} = 0.35 \text{ (nF)} \]

where

\[ K = 2.3, \]

\[ \varepsilon_0 = 8.854 \text{ pF/m}, \]

\[ f = 270/360 \text{ deg}, \]

\[ r \approx 6.0 \text{ m}, \]

\[ w \approx 0.3 \text{ m}, \]

\[ S = 0.491 \text{ m}, \]

This value of \( C_1 \) is to be compared with the capacitance, \( C_2 \), between the central conductor of the wedge transformer and the outer conductor (assumed to be at the constant \( S = 0.491 \text{ m} \)).

\[ C_2 = 2K \varepsilon_0 \frac{f n (r_1 - r_i)}{S} = 5.5 \text{ (nF)} \]

where \( r_1 = 5.76 \text{ m}, \) the outer radius of the wedge, and \( r_i = 2.2 \text{ m}, \) a reasonable value for the inner radius of the wedge. The factor of two accounts for both upper and lower gaps in the wedge transformer. Capacitances \( C_1 \) and \( C_2 \) appear in series dividing the voltage applied to the torus. This fact implies that the fraction

\[ C_1'/(C_1' + C_2') = 6 \text{ percent} \]

of the torus voltage appears as a prepulse.

This fraction could be smaller either if the spacing between the central wedge conductor and the outer conductor were to decrease at small radii or if the switch gap were to be increased.

### 4.6 Analysis of Discharge Phase of Torus

The discharge phase of the torus was treated as a problem separate from the charge phase. At the time \( (350 \text{ ns after blumlein switching}) \) chosen for torus switching, the current throughout the torus was found to be negligible. At this time, almost all the energy is stored in the electric field, and this energy is distributed among the 12 transmission-line elements in the model. Since the torus switching has been restricted to 75 percent of the torus, only 9 of the 12 elements partake in the switching.

The discharge of each of the nine elements is handled by a separate circuit. This simplification assumes that there is no flow of energy from one sector of the wedge to the next. In reality, this is not expected to be the situation; nevertheless, for this first-cut analysis, this assumption seems reasonable.

Since each of the nine discharge circuits behaves identically, the calculation was done only for one representative circuit. The impedances of 1.8 \( \Omega \) and an inductance of 20 nH used in the representative circuit were scaled to apply to the entire 270 deg of the discharging torus and are shown in the circuit of figure 13. This analysis assumes that the impedance of the strip-line wedge is matched to that of the torus and is constant right up to the load. The one-way transit time of the element representing the torus is 13.04 ns and is the effective transit time given by
a condition that must be imposed so that the electrostatic energy of the torus in its charge configuration equals the electrostatic energy of the torus in its discharge configuration. Here $Z_{\text{charge}}$ is 23.7 Ω and $T_{\text{charge}}$ is the transit time for 75 percent of the torus circumference ($T_{\text{charge}} = 81.5$ ns).

Figure 13. Representative circuit for discharge phase of torus.

In the representative calculation, a unit voltage was used for the initial voltage on the charged torus in its discharge configuration. The final scaling was later provided by normalizing to the appropriate average over the initial voltages on the nine segments of the torus model in its charge phase. The output voltage shown in figure 14 is scaled according to the average of the individual $V_i$, and the total current shown in figure 15 also is scaled according to the average of $V_i$. The power, however, scales according to the average of $V_i^2$, and it is this scaling that is used in figure 16.

The effect of the prepulse was included in the calculation by imposing an initial voltage on the wedge equal to 6 percent of the unit voltage on the torus. In the calculation, it was assumed that the distribution of the prepulse throughout the wedge corresponds exactly with that of the voltage on the torus, which is not expected in actuality. Nevertheless, the trend of the effect is approximately accounted for and, since the effect of the prepulse on the overall pulse shapes is small anyway, this assumption causes no concern.
4.7 Field Emission Diode Design

A conceptual design for a low impedance diode integrated into the strip-line wedge transformer is shown in figure 17. The insulator rings proposed for this application are identical to those used on the existing AURORA simulator. The vacuum flashover strength for these insulators is given approximately by the relation

\[ E = 552d^{\frac{1}{4}}t^{-\frac{1}{2}} \text{ (kV/cm)} \]

where

- \( E \) = flashover strength,
- \( d \) = surface path length in centimeters,
- \( t \) = pulse duration in nanoseconds.

Each insulator ring has a path length of 14 cm, and the applied pulse duration is 40 ns, giving \( E = 104 \text{ kV/cm} \). If we assume an applied pulse of 14 MV and assume a 70-percent design factor (giving 20 MV), we require a total path length of 20 MV/104 (kV/cm)—that is, 192 cm. Hence, the total number of rings required per side is 14 for a total stack of 28 having a height of 2.84 m. Allowing for the thickness of the gradient rings, a practical stack height of 3.11 m would be required; that is, each side of the diode would be about 1.6 m long.

The existing AURORA system has a total stack height of 4.6 m for an applied voltage of 18 MV for about 200 ns. The time factor is the only important difference, and this would suggest a 60-percent increase in length over the torus diode per megavolt of applied voltage. Even allowing for the fact that good uniform field grading is more difficult for larger stack lengths, this increase still suggests that the torus diode may be marginally designed in terms of voltage hold-off capability. Lengthening the stack, however, does not present any obvious difficulties, and, lacking further corroborating data, we continue to assume that the proposed 3.1-m stack height is adequate for this study.

![Figure 17. Low impedance diode.](image)

5. CONCLUSIONS

A novel approach has been conceived for the production of short duration, ultrahigh power pulses into low impedance loads. The concept has been shown to be extremely versatile and can be adapted to AURORA in a wide variety of configurations. A selected toroidal geometry has been investigated, and analysis has shown that power outputs approaching \( 10^4 \text{ W} \) can be delivered to a low impedance load (1.89 \( \Omega \)) in 30 ns full width at half maximum. Further manipulation of the design should give a factor of two increase over these power output levels. With the exception of the diode, all of the design criteria are known to be compatible with the existing state of the art of high voltage pulsed-power technology.
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