| **STUDY OF THE PHASE TRANSITION IN KIOTIUNI DIOXIDE** |
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| **Final Reports** |
| **1 Apr 76 - 31 Mar 77** |

| **Approved for public release; distribution unlimited.** |

| **KEY WORDS** |
| **Nobium compounds, Oxides, Phonons, Titanium oxides.** |

| **ABSTRACT** |
| **Results are presented on the electronic bands of \( \text{Nb}_2\text{O}_5 \) and \( \text{Ni}_{1-x}\text{Ti}_x\text{O}_2 \).** |

| **and on the phonon structure at \( K=0 \).** |

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A. Introduction

It has long been recognized that the coupling of the cations, via homopolar bonding of the d-electrons, along the preferred c-axis direction plays a crucial role in the SCH transition mechanism.\(^1\) We have tried to identify the p-d and d-d interband transitions in NbO\(_2\) by comparing its normal incidence reflectivity spectra to that of TiO\(_2\). As was shown earlier,\(^2\) the structure of NbO\(_2\) in the semiconducting phase, albeit slightly distorted, is tetragonal as is that of TiO\(_2\) and in first approximation, one would expect that the spectra would look similar except for the d-band's contributions. Such a simple-minded assumption would also lead one to expect the main differences to show in the spectra where the light polarization is parallel to the c-axis.

B. Optical Spectroscopy

The possibility of doping high quality NbO\(_2\) single crystals with TiO\(_2\)\(^3\) suggested another approach. Since Ti\(^{4+}\) has no d-electrons, each substitution of a Ti\(^{4+}\) for an Nb\(^{4+}\) would actually break a Nb-Nb pair and leave the lone Nb\(^{4+}\) ion with a dangling d-bond. Two consequences would follow. The first is that the conductivity and the magnetic moment at a fixed temperature would increase with the Ti\(^{4+}\) concentration and the second is that the optical spectra would be affected mostly where the d-band's contributions dominate.

We have fully carried out these experiments and the results have been accepted for presentation at the International
Semiconductor Conference (Rome, 1976), they will appear shortly in the proceedings. Only the salient features will be discussed below.

The large single crystals of NbO$_2$ and Nb$_{1-x}$Ti$_x$O$_2$ used in our measurements were grown$^3$ by the Czochralski-Kyropoulos technique in a tri-arc furnace built after the original design of Dr. Thomas B. Reed (M.I.T., Lincoln Laboratory); the procedure followed was outlined earlier (see Ref. 5).

B-1. Comparison of the NbO$_2$ and TiO$_2$ Optical Spectra

The normal incidence reflectivity of NbO$_2$ and TiO$_2$ was measured on oriented single crystals using polarized light. The instrument was a rotating light pipe reflectometer of the type originally designed by Dr. G. Rubloff.$^4$

Let us consider first the spectra obtained with light polarization $E$ parallel to the $a$-axis (Fig. 1). For the sake of convenience, we have shifted the entire NbO$_2$ spectrum to the left by approximately 0.7 eV. If one excepts the low energy maximum in the NbO$_2$ trace, the similarity between the spectra is quite conspicuous. This result is consistent with the assumption made earlier and identifies the first extremum in the NbO$_2$ ($E \parallel a$-axis) spectrum as resulting from a d-d transition.

Let us now turn our attention to the $E \parallel c$-axis spectra. Since the d-orbitals are along the $c$-axis, this is where we would expect to see strong differences between NbO$_2$ and TiO$_2$ according to the hypothesis mentioned earlier. The results shown in Fig. 2 are self-explanatory. No amount of shifting of either curve is going to bring about the kind of coincidence exhibited in the $E \parallel a$-axis case.
In order to pursue further our discussion, we now need to perform a Kramers-Kronig analysis of our measurements and obtain the $\varepsilon_2$ (imaginary part of the frequency dependent dielectric constant) spectrum which usually exhibits maxima in reasonable agreement with the extrema in the joint density of states spectrum. However, such an analysis often suffers from a lack of information about strong oscillators lying outside the experimental range. We have palliated this difficulty by measuring the angular dependence of the reflectivity at a few selected wavelengths corresponding to our Ar$^+$ and Kr$^+$ ion laser lines. These measurements allowed us to compute independently $\varepsilon_1$ and $\varepsilon_2$ at a few predetermined frequencies. By forcing the result of the Kramers-Kronig analysis to pass through these independently obtained values of $\varepsilon_1$ and $\varepsilon_2$ one confers a degree of uniqueness and dependability to the transformation.

The results are shown in Fig. 3 for pure NbO$_2$ and the location of interband transitions are indicated by arrows. The considerations presented earlier lead to a tentative set of assignments shown in Fig. 4 and to the following possibilities:

- The direct band gap of 0.3 eV is $a_{1g}$ bonding to $a^*_{1g}$ antibonding

- The transitions at 0.8, 1.5, 2.5 and 3.8 eV are d to d.

The first observation is actually quite interesting because it explains the significant anisotropy observed in the conductivity of single crystal NbO$_2$. The second observation informs us as to the actual hierarchy of d-orbitals sublevels. This information is essential to the derivation of a reliable model for the SCM transition.
B-2. Dependence of the NbO$_2$ Optical Spectrum on Ti Doping

We have measured the normal incidence reflectivity spectra of Nb$_{1-x}$Ti$_x$O$_2$ with $x = 0.0$, 0.05 and 0.20. X-ray and Raman measurements have shown that for $x > 0.17$, the SCM transition is eliminated and the material has the undistorted rutile structure. Our reflectivity measurements therefore, straddle the SCM transition using Titanium doping instead of temperature.

In Fig. 5, we show $r_2$ (E || to c-axis) for all three compositions. It is quite clear that at least two interband transitions indicated by the arrows and located at 2.5 and 3.8 eV are affected by titanium doping and the effect is a steady displacement toward higher energies; implying, that titanium doping increases the $a_{1g} - (e_g, e_{g'})$ splitting.

In Fig. 6, we present the $r_2$ dependence on Ti doping with light polarization E || a-axis. By and large, the only effect is the expected broadening due to disorder, except for the peak at 1.5 eV which increases with Ti concentration. This is not surprising as the peak at 1.5 eV is the only d-d transition observed with light polarization E || to a-axis. Of course, these assignments are only a guess but they are internally consistent and therefore quite plausible.

The result of this analysis is simple. At this point, we already know that the SCM transition in NbO$_2$ results from a type of configurational instability. This is shown not only by the neutron diffraction work, but also by the optical spectroscopy results. They seem to indicate that the direct gap is bonding $a_{1g}$ to antibonding $a^{*}_{1g}$. This type of gap is usually of the order of 3 eV as for instance in Ti$_2$O$_3$; here
we have measured it to be 0.8 eV. This unusual result suggests
a very simple explanation for the SCM transition. It results
from the fact that, similar to Ti$_2$O$_3$, cation-cation pairs are
formed via homopolar hybridization of d-orbitals preferentially
along the c-axis. This, in turn, requires a slight displacement
of the O$^{2−}$ providing a proper Coulombic potential and locking-in
a stable configuration. However, contrary to Ti$_2$O$_3$, pairs here
are contiguous and not separated by a vacancy and it is easy
to see that two contiguous Nb ions bound to two other Nb ions
in two different pairs could choose to break away from their
partners and form a new pair. The only obstacle would be the
oxygen rearrangement necessary to accommodate the new situation.
The optical results suggest, as one possibility, that the energy
needed for such a rearrangement is of the order of 0.8 eV. Now
a look at the actual value of oxygen distortions will be most
convincing as they are extremely small, in fact, at the limit of
accuracy of X-ray techniques. Clearly, there will be a finite
temperature at which the mean square amplitude of vibration of
the oxygen ions will be comparable to the distortion itself at
which point the difference between the two configurations will
vanish provoking a collapse of the direct band gap.

C. Raman Spectroscopy

Our previous work, consistently with the results of Tanaka, had
shown that Ti doping lowered the transition temperature $T_c$
and that by 17 atomic percent of Ti the material has a metallic
conductivity at room temperature. This opened up the possibility
of inducing the phase change at ambient by varying $x$ in Nb$_{1−x}$Ti$_x$O$_2$
and following the process by Raman scattering. In performing
this experiment, which has been reported at the annual solid state meeting of the APS in March 1977, we fully realize its limitation.

a. Ti substitution would simulate temperature only if the determinant factor in the semiconductor to metallic transition mechanism is a pair breaking process instead of a tunneling excitation or a charge density wave.

b. At room temperature, NbO₂ has the C₄ᵥ symmetry and 32 molecules per unit cell while above Tc it has the D₄h symmetry and 2 molecules per unit cell; from which it follows that the k of the transformation is different from zero and we should not expect to see a Raman mode soften as we go from the distorted C₄ᵥ phase to the undistorted D₄h phase.

On the other hand, it was established earlier that the transition is of the second kind and passing from one phase to the other does not generate an entirely new set of phonon branches. Simply the distorted phase exhibits a large number of phonons (actually symmetry indicates that we should expect 54 phonons, 18 A₄ + 18 B₄ + 18 E₄) because of a multiple folding of the Brillouin zone. As the material undergoes the phase transition, the Brillouin zone unfolds and all but four phonon branches (A₁g, B₁g, B₂g and E₄) should disappear.

In Figs. 7, 8, 9 and 10, we present the evolution of the Raman spectra in Nb₁₋ₓTiₓO₂ system as a function of x. The polarization selection rules are fairly well obeyed and Fig. 7 shows the A₄ modes (ZZ polarization), Fig. 8 shows the E₄ modes (XZ polarization), Fig. 9 shows the B₄ modes (XY polarization), finally Fig. 10 (XX polarization) shows simultaneously A₄ and B₄ modes. Obviously
we are not seeing all the Raman active modes, in fact, we are barely able to detect half of them, but the information seems sufficient. In order to interpret the data, one should keep in mind that we are dealing here with an alloy and that we should expect to observe, in the undistorted rutile phase, all the TiO₂ modes in addition to the modes corresponding to the high symmetry rutile NbO₂.

As can be seen, the multiplicity of modes, present in the distorted pure NbO₂ phase, is reduced very fast and by x=0.1 already the spectra is dominated by the TiO₂ and NbO₂ (rutile) lines. If one excludes the TiO₂ rutile lines, one is left with

- ZZ polarization 125 cm⁻¹, 350 cm⁻¹, 390 cm⁻¹, 540 cm⁻¹ and 730 cm⁻¹
- XZ polarization 240 cm⁻¹, 390 cm⁻¹
- XY polarization 350 cm⁻¹, 390 cm⁻¹
- XX polarization 350 cm⁻¹, 390 cm⁻¹

Out of these four (125 cm⁻¹, 390 cm⁻¹, 540 cm⁻¹, and 730 cm⁻¹) are in a constant ratio to the four TiO₂ phonons. Since the phonons in the rutile structure are due to oxygen motions only, one does not expect scaling by \( \left( \frac{\text{mass of Nb}}{\text{mass of Ti}} \right)^{1/2} \) but rather by a ratio of the spring constants \( \frac{K(\text{Nb-O})}{K(\text{Ti-O})}^{1/2} \). The comparison is shown below

<table>
<thead>
<tr>
<th></th>
<th>NbO₂(cm⁻¹)</th>
<th>TiO₂(cm⁻¹)</th>
<th>Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>125 cm⁻¹</td>
<td>390</td>
<td>537</td>
<td>1.144</td>
</tr>
<tr>
<td>350 cm⁻¹</td>
<td>447</td>
<td>612</td>
<td>1.146</td>
</tr>
<tr>
<td>390 cm⁻¹</td>
<td>537</td>
<td>612</td>
<td>1.140</td>
</tr>
<tr>
<td>540 cm⁻¹</td>
<td>612</td>
<td>726</td>
<td>1.138</td>
</tr>
<tr>
<td>730 cm⁻¹</td>
<td>826</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

and the results point out that Nb-O has a weaker spring constant than Ti-O as one would expect.

The two other modes at 240 and 350 cm⁻¹ are particularly interesting as they belong neither to NbO₂ rutile nor to TiO₂ rutile. Since these modes are already dominant by x=0.12, we
intend to investigate them more closely as a function of temperature.

In conclusion, the work to date has informed us extensively on the electronic bands of NbO$_2$ and Nb$_{1-x}$Ti$_x$O$_2$ as well as on the phonon structure at K=0. These results will be used as a stepping stone to analyze the neutrons and magnetic results now in progress.
References


2. B. O. Marinder, Arkiv Kemi, 19, 435 (1963)


(ZZ) Polarization
$A_g$ Modes

- $\text{NbO}_2$ Rutile
- Broad
- $\text{NbO}_2$ Rutile
- $447 \text{ TiO}_2$
- Broad
- $\text{NbO}_2$ Rutile
- $143 \text{ TiO}_2$

$\text{CM}^{-1}$

$\text{NbO}_2$ $x$ $\text{TiO}_2$

$x = 0.1, 0.2$
Fig. 8

(XY) Polarization
$B_g$ Modes

$B_{2g}$

CM$^{-1}$

800
700
600
500
400
300

$NbO_2$

Rutile

$143 TiO_2$

$826 TiO_2$

$100$

$0.1$

$0.2$

$NbO_2$

$TiO_2$
(XZ) Polarization
$E_g$ Modes

- $826 \text{ TiO}_2$
- $400\text{ cm}^{-1}$
- $300\text{ cm}^{-1}$
- $200\text{ cm}^{-1}$
- $143 \text{ TiO}_2$

$\text{Nb}_2\text{O}_5$

Rutile

Strong
(XX) Polarization
$A_g$ and $B_g$ Modes

$B_g$ $ightarrow$ 826 TiO$_2$

$A_g$ $ightarrow$ 612 TiO$_2$, $A_{1g}$

$A_g$ or $B_g$

$B_g$ $ightarrow$ 447 TiO$_2$

$B_g$ $ightarrow$ 143 TiO$_2$, $B_{1g}$

$A_g$ $ightarrow$ 143 TiO$_2$

$X$

$NbO_2$

$TiO_2$