SELECTION OF MINIMUM DAY/NIGHT LEVELS FOR NOISEMAP CONTOUR CALCULATIONS

Dwight E. Bishop

Bolt Beranek and Newman Inc.
21120 Vanowen Street
Canoga Park, California

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FOR THE COMMANDER

HENNING E. VON GIERKE
Director
Biodynamics and Bionics Division
Aerospace Medical Research Laboratory
This report discusses guidelines for the minimum Day/Night Level (DNL) values that should be used with NOISEMAP type computations to: (1) insure adequate accuracy of the lowest contour level for a given set of aircraft operations; and (2) minimize the number of machine computations and thereby reduce operating costs. An analysis is made of the errors introduced in the DNL contour values due to truncation of the "partial" DNL cutoff determined.
by the single event noise level or the number of aircraft operations for a particular flight path. For a given airbase and fixed volume of aircraft operations, the cutoff occurs at higher single event noise levels as the number of aircraft flight paths or aircraft classes are increased. Finer detail in describing the aircraft operations results in the cutoff noise levels being raised with an increased error at the edges of the DNL grid computations, but with a corresponding decrease in the machine running time. These DNL cutoff guidelines have been incorporated into version 3.4 of NOISEMAP.
PREFACE

SELECTION OF MINIMUM DAY/NIGHT LEVELS
FOR NOISEMAP CONTOUR CALCULATIONS

I. INTRODUCTION

This technical memo provides recommendations for selecting minimum day/night level (DNL) values in NOISEMAP computations. The recommendations are based upon interpretation and analysis of a simple calculation model which is described in detail in the Appendix.

II. TECHNICAL DISCUSSION

In NOISEMAP computations, two limits for DNL computations can be specified:

(a) Noise contributions from aircraft flight paths may be dropped when the sound exposure level (SEL) for that aircraft drops below a given value. Alternatively, noise level contributions from an aircraft may be dropped when the distance from the aircraft exceeds a maximum value.

(b) Contribution from an aircraft flight path may be dropped when the "partial" DNL value for that particular flight path falls below a minimum value. This cutoff is determined by both the noise level and the number of operations on the flight path. Thus, for a given airport and fixed volume of aircraft operations, the cutoff occurs at higher SEL values as the numbers of aircraft flight paths and aircraft classes are increased. Hence, as one gets more sophisticated by providing finer detail in describing aircraft operations, with an attendant increase in aircraft classes and tracks, the cutoff noise levels are raised with increased error at the edges of the grid computations.
Figure 1 (from Reference 1) provides an estimate of the noise level cutoff as a function of the effective number of operations, for a cutoff value of DNL 42 (or NEF 7). Note that the cutoff result in a truncation of noise levels near the edges of the grid path roughly shown below.

Generally, the errors introduced by truncation will be largest when there are near equal contributions from many flight paths and aircraft. For a given error in grid computations, the resulting contour error will generally be greatest when the noise exposure gradient is small; the contour error will be least when the gradient is large.

One needs to specify a cutoff value in order to limit the number of computations. However, the limit should be set to hold possible truncation errors to a small finite quantity. In practice, one cannot easily determine the number of "partial" DNL values that contribute to the total DNL at each grid point; this number will vary widely with the grid point location. Faced with this situation, one approach is to estimate the likely worst case situation for a given airport, and select a cutoff that would limit the errors of this worst case situation.

To provide some insight into potential DNL calculation errors, a simplified situation is assumed, where a number \( N \) of partial DNL values, \( L_1 \), contribute to a total DNL value, \( L_N \). These partial
values are assumed to be uniformly distributed over a total DNL range, \( \Delta L \), with a constant difference in level, \( K \), between any two partial values. This situation is sketched in Figure 2.

The partial values can be summed to obtain the total DNL value \( L_N \). When a DNL cutoff, \( L_c \), is introduced that exceeds the lowest partial DNL value, one or more DNL values are dropped in calculating the total DNL. Thus, there will be a difference (or error) between the computed DNL value \( \bar{L}_x \) and the true total DNL value.

Using the equations given in the Appendix several series of calculations were made to determine the difference between the total DNL value and the cutoff value (approximately represented by the quantity \( y \) in Figure 2) for specified errors in calculation of 0.5 and 1.0 dB. The results of these calculations are shown in Figure 3 and 4. Figure 3 shows that for a given range of partial DNL values (in this example, 20 dB), the value \( y \) increases almost linearly with the logarithm of the number of partial DNL values.

In Figure 4, the number of partial DNL values is held constant at 21, while the range of the partial DNL values is varied from 5 to 40 dB. In this situation, the value of \( y \) shows a small decrease as the range of partial DNL value is increased beyond about 10 dB.

From inspection of these two figures, the dominating influence on \( y \) is the total number of partial DNL values as indicated in Figure 3. A straight line fitted to the 0.5 dB error curve in Figure 3 over the range from 10 to 100 partial DNL values gives the following:

\[
y = 0.6 + 11.7 \log N
\] (1)
Note that the slope (11.7) is slightly greater than the slope of 10 that would result when the range y goes to zero.

Now in actual computations, it is obvious that not all flight segments will provide significant contributions to the noise at any given spot. For a worst case situation, the number of potential flight segments is proportional to the total number of flight cards reduced by a factor related to the number of active airport runways and gross number of flight tracks. Thus, this consideration, together with Equation (1) leads to the following expression for setting the cutoff limit for individual flight track DNL calculations:

\[
L_c = L_o - 11.7 \log \frac{N}{R+1} \tag{2}
\]

where \( L_o \) = value of the minimum DNL contours of interest
\( L_c \) = cutoff DNL value
\( N \) = total number of flight track cards
\( R \) = number of active physical runways

The above should result in calculation errors that do not exceed 0.5 dB, and, in most situations, should result in errors of appreciably less than 0.5 dB.

REFERENCES

FIGURE 2. RELATIONSHIP OF LEVELS FOR DAY-NIGHT LEVEL CUTOFF ERROR ANALYSIS
APPENDIX

CUTOFF ERROR ANALYSIS

Assume N "partial" DNL values, \( L_1 \), at a given ground position, contributed by individual aircraft flight segments. Assume the \( L_1 \) values are uniformly distributed over a total DNL range, \( \Delta L \), with a constant difference in level, \( K \), between any two partial values. Thus, the \( L_1 \) values are evenly spaced between a maximum value, \( L_M \) and a minimum value, \( L_m \) where:

\[
L_m = L_M - (N-1)K \tag{1}
\]

The "total", or combined DNL value \( L_N \) is:

\[
L_N = 10 \log \frac{L_1}{10} = 10 \log \sum \frac{L_M}{10} + 10 + \ldots + 10
\]

or

\[
L_N = (L_M - (N-1)K) + 10 \log \frac{k^{N-1}}{k-1} \tag{2}
\]

where \( k = 10 \)

When the DNL cutoff \( (L_c) \) exceeds the minimum DNL value, one or more DNL values are dropped in the summation, \( L_x \). Hence, there is a difference (or error, \( E \)) between the computed \( L_N \) and the "true" \( L_x \), where

\[
E = L_N - L_x \tag{dB}
\]
In selecting DNL cutoff values appropriate to the desired noise contour situation, the question arises as to what is the maximum cutoff value for a specified error, E. Or, alternatively stated, for an error equal or less than a specified value of E, what is the value of y where:

\[ y = \bar{L}_N - (L_M - xK) \]

The calculation situation is sketched in Figure 2.

The computed DNL value, \( \bar{L}_x \), is given by:

\[ \bar{L}_x = (L_M - xK) + 10 \log \frac{k^{x+1}}{k-1} \]  

For a specified value of E, the values of x and y can be determined from trial and error solution of the following:

\[
\frac{L_M xK}{10} = \frac{L_M - (N+1)K}{10} \cdot \frac{10}{(k^{x+1})} = \frac{10}{(k^N - 1)} \]

where \( \xi = \frac{E}{10} \)

Equation (4) was used to calculate the curves of Figure 3 and 4.
$E = \text{"ERROR"}, \text{ the difference between the "TOTAL" DNL and the computed DNL with truncation}$

Calculated for a 20 dB Range of Partial DNL Values

**FIGURE 3. CUTOFF ERROR VARIATION WITH NUMBER OF PARTIAL DNL VALUES**
FIGURE 4. CUTOFF ERROR VARIATION WITH THE RANGE OF PARTIAL DNL VALUES