NONELECTRICAL LANGUAGES SIMULATION
MODULE (NELSIM)

Volume II

TRW Systems Group
Nuclear Survivability Dept.
Redondo Beach, CA 90278

September 1976

Final Report

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Prepared for
Director
DEFENSE NUCLEAR AGENCY
Washington, DC 20305

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Air Force Systems Command
Kirtland Air Force Base, NM 87117
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**NONELECTRICAL LANGUAGES SIMULATION MODULE (NELSIM)**

<table>
<thead>
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<th>REPORT NUMBER</th>
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<th>M. Epstein J.R. Pistacchi</th>
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<tr>
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**KEY WORDS**

Analysis
Computer Aided Analysis
CADA
Network Simulation
Non-electrical Languages for Simulation

**ABSTRACT**

NELSIM is a computer program developed to convert non-electrical system descriptions into electrical analogs or differential equations consistent with existing circuit analysis programs. The program provides an interface between system level problems and electrical simulation programs. The module permits engineers not familiar with disciplines generally associated with circuit simulation programs to solve system problems without manually deriving the electrical analogs and differential equations necessary to utilize such programs.
## CONTENTS

<table>
<thead>
<tr>
<th>SECTION</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>I</strong></td>
<td></td>
</tr>
<tr>
<td>INTRODUCTION</td>
<td>1</td>
</tr>
<tr>
<td>1.1 NELSIM Input/Output Options</td>
<td>1</td>
</tr>
<tr>
<td>1.2 NELSIM Data Organization</td>
<td>3</td>
</tr>
<tr>
<td>1.3 NELSIM Usage Highlights</td>
<td>5</td>
</tr>
<tr>
<td>1.4 Manual Organization</td>
<td>9</td>
</tr>
<tr>
<td><strong>II</strong></td>
<td></td>
</tr>
<tr>
<td>ANALOG SYSTEM INPUT LANGUAGE</td>
<td>10</td>
</tr>
<tr>
<td>2.1 General Analog System Input Language</td>
<td>10</td>
</tr>
<tr>
<td>2.2 Mechanical System Input Language</td>
<td>34</td>
</tr>
<tr>
<td>2.3 Mechanical System State Variables</td>
<td>38</td>
</tr>
<tr>
<td>2.4 Outputs</td>
<td>39</td>
</tr>
<tr>
<td>2.5 Thermal System Input</td>
<td>41</td>
</tr>
<tr>
<td>2.6 Electro-Mechanical Elements and Models</td>
<td>45</td>
</tr>
<tr>
<td>2.7 Electro-Optical System Input</td>
<td>55</td>
</tr>
<tr>
<td>2.8 Units and Scaling</td>
<td>57</td>
</tr>
<tr>
<td><strong>III</strong></td>
<td></td>
</tr>
<tr>
<td>TRANSFER FUNCTION INPUT LANGUAGE</td>
<td>65</td>
</tr>
<tr>
<td>3.1 Flowgraph Input Preparation</td>
<td>66</td>
</tr>
<tr>
<td>3.2 Graph Description</td>
<td>67</td>
</tr>
<tr>
<td>3.3 Branches</td>
<td>67</td>
</tr>
<tr>
<td>3.4 Input/Output Reference</td>
<td>68</td>
</tr>
<tr>
<td><strong>IV</strong></td>
<td></td>
</tr>
<tr>
<td>DIFFERENTIAL EQUATION INPUT LANGUAGE</td>
<td>71</td>
</tr>
<tr>
<td><strong>V</strong></td>
<td></td>
</tr>
<tr>
<td>COMBINED SYSTEM INPUTS</td>
<td>75</td>
</tr>
<tr>
<td><strong>VI</strong></td>
<td></td>
</tr>
<tr>
<td>NELSIM SAMPLE PROBLEMS</td>
<td>76</td>
</tr>
<tr>
<td>6.1 Mechanical System Examples</td>
<td>76</td>
</tr>
<tr>
<td>6.2 Thermal System Examples</td>
<td>80</td>
</tr>
<tr>
<td>6.3 Electro-Mechanical Examples</td>
<td>85</td>
</tr>
<tr>
<td>6.4 Electro-Optical System Examples</td>
<td>90</td>
</tr>
</tbody>
</table>
ILLUSTRATIONS (Cont'd)

Figure 34. Lumped Element Galvanometer Equivalent ............... 85
Figure 35. Galvanometer Electrical Analog ......................... 87
Figure 36. Equivalent Circuit of a Photodiode ...................... 90
TABLES

<table>
<thead>
<tr>
<th>Table</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>Table I.</td>
<td>Standard Thermal Elements</td>
<td>11</td>
</tr>
<tr>
<td>Table II.</td>
<td>Acceptable Constant Formats</td>
<td>15</td>
</tr>
<tr>
<td>Table III.</td>
<td>Program Data Limits</td>
<td>34</td>
</tr>
<tr>
<td>Table IV.</td>
<td>Mechanical Standard Elements</td>
<td>35</td>
</tr>
<tr>
<td>Table V.</td>
<td>Mechanical to Electrical Analog Generation</td>
<td>36</td>
</tr>
<tr>
<td>Table VI.</td>
<td>Mechanical System State Variables</td>
<td>38</td>
</tr>
<tr>
<td>Table VII.</td>
<td>Thermal Elements and State Variables</td>
<td>42</td>
</tr>
<tr>
<td>Table VIII.</td>
<td>System Analogies</td>
<td>62</td>
</tr>
<tr>
<td>Table IX.</td>
<td>Standard System Units</td>
<td>62</td>
</tr>
</tbody>
</table>
SECTION I
INTRODUCTION

NELSIM (Nonelectrical Languages Simulation Module) is a digital computer program written in FORTRAN IV. The program translates non-electrical system descriptions into electrical analogs and differential equations acceptable for execution by the SCEPTRE (System for Circuit Evaluation and Prediction of Transient Radiation Effects) simulation program. The program thus provides an interface between system level problems and electrical simulation programs. The module allows engineers not familiar with disciplines generally associated with circuit simulation programs to solve system problems without manually deriving the electrical analogs and equations necessary to run such programs. The input language allows input of mechanical, thermal, electro-mechanical and electro-optical problems in terms of differential equations, transfer functions, or elements and units familiar to those particular disciplines.

The program features a free-field, user-oriented input language modeled after the SCEPTRE input language. The output is also in terms of the SCEPTRE language and allows direct execution by SCEPTRE. The output of NELSIM can be punched cards if requested by the user. Another option is scaling which allows the user to obtain an electrical analog with the units scaled to the actual response magnitudes expected.

1.1 NELSIM Input/Output Options

The program allows the three types of input to describe system problems illustrated in Figure 1.

The transfer function input allows users to enter the description of a system or part of a system in terms of signal flowgraphs or block
DIFFERENTIAL EQUATIONS

\[ \frac{d^n x}{dt^n} + \ldots + x = 0 \]

\[ \frac{d^k y}{dt^k} + \ldots + a_0 = 0 \]

SYSTEM FUNCTIONAL ELEMENTS

NON-ELECTRICAL LANGUAGE SIMULATION MODULE (NELSIM)

Figure 1. Input/Output of NELSIM
diagrams. The language for this option is nearly identical to the input language of the program SYNAP (Symbolic Network Analysis Program) developed for The Air Force Weapons Laboratory (AFWL) in 1972 and consists of descriptions of S-Domain transfer functions connected between user derived node names.

The differential equations option allows the user to enter problem definitions in terms of sets of \( n^{th} \) order differential equations algebraically coupled together.

The user may also enter problems in terms of functional lumped elements and nodal connections. The program accepts elements of mechanical, thermal, electro-mechanical and electro-optical systems.

The output of the program consists of a set of first order differential equations for all differential equation entries and all transfer function entries. It also consists of electrical lumped element equivalent networks for all entries containing system elements. The user may use any option or combination of options to define the overall system to be analyzed. The user may have the output of NELSIM punched on cards and thus generate an input deck to the SCEPTRE program directly. The user may also call on the scaling algorithm built into NELSIM and obtain a listing of the analog generated with constant element values scaled to improve numerical accuracy upon execution.

1.2 NELSIM Input Data Organization

The data organization and input language of NELSIM have been kept identical to that of SCEPTRE wherever possible and consistent with it in all other cases. Figure 2 illustrates the data organization. As shown, the data are entered following heading and subheading cards. All problem descriptions entered in terms of lumped elements are entered under the
Figure 2. NELSIM Input Data Organization
ANALOG DESCRIPTION heading. All sets of differential equations are entered under the DIFFERENTIAL EQUATIONS heading and all transfer function descriptions are entered under the TRANSFER FUNCTIONS heading. The RUN CONTROLS, RERUN DESCRIPTION and END headings control the execution of the run, parameter value changes and program termination, respectively. The functional subheadings shown in Figure 2 identify the type of system being entered if lumped networks are entered. The functional elements serve to identify the remainder of variable values such as element values and description of equations used. The main headings must appear in the order shown in the figure. Main headings as well as subheadings however need not be included if not utilized. For example, if a problem is described strictly in terms of differential equations, the ANALOG DESCRIPTION headings, TRANSFER FUNCTION heading and all related subheadings may be deleted from the input. Sections II through IV elaborate the details of the input language as applicable to each input type.

1.3 NELSIM Usage Highlights

This paragraph provides the user a quick introduction to the input language by summarizing the input through three sample problem inputs. As discussed above three types of input are allowed in NELSIM. The input data organization for a differential equations problem, the input organization for a transfer function problem, and system element entry for a mechanical problem are shown in Figure 3.

The input data consists of descriptive statements constructed from user-derived component names, node names and value specifications. The information is placed on cards separated by special characters such as a comma, dash, parenthesis, or equal sign. In general, several complete statements can be punched on a card, separated only by a comma. The
\[
\begin{align*}
\text{Equations} & \quad \left\{ \begin{array}{l}
K_1 (V_2 - V_1) + M_2 \left( \frac{d^2 V_2}{dt^2} \right) + B \left( \frac{dV_2}{dt} - \frac{dV_3}{dt} \right) + K_2 (V_2 - V_3) = 0 \\
B \left( \frac{dV_2}{dt} - \frac{dV_3}{dt} \right) + K_2 (V_3 - V_2) + M_3 \frac{d^2 V_3}{dt^2} + K_3 V_3 = 0
\end{array} \right.
\end{align*}
\]

\[
\begin{align*}
\text{Parameter Values} & \quad \left\{ \begin{array}{l}
K_1 = 1 \\
K_2 = 2 \\
K_3 = 3 \\
M_2 = 0.2 \\
M_3 = 0.3 \\
B = 1 \\
V_1 = \cos 2t
\end{array} \right.
\end{align*}
\]

**DIFFERENTIAL EQUATIONS**

**EQUATIONS**

\[PK_1*(PV2-PV1)+PM2*D2PV2+PB*(D1PV2-D1PV3)+PK2*(PV2-PV3)=0\]

\[PB*(D1PV3-D1PV2)+PK2*(PV3-PV2)+PM3*(D2PV3)+PK3*PV3=0\]

**DEFINED PARAMETERS**

\[PK1=1\]

\[PK2=2\]

\[PM2=0.2\]

\[PM3=0.3\]

\[PB=1\]

**NELSIM Input**

\[PV1=Q1(TIME)\]

**FUNCTIONS**

\[Q1(T)=(\cos(2.*T))\]

**OUTPUTS**

\[PV2(V2),PV3(V3),PLOT\]

**RUN CONTROLS**

\[STOP TIME=100\]

\[INTEGRATION ROUTINE=IMPLICIT\]

**END**

a. Differential Equations

Figure 3. NELSIM Inputs
b. Transfer Function

Figure 3. NELSIM Inputs (Cont'd)
c. Mechanical Analog

Figure 3. NELSIM Inputs (Cont'd)
information is all placed under major heading and subheading such as TRANSFER FUNCTIONS and DEFINED PARAMETERS.

1.4 Manual Organization

This section has briefly described the capabilities of the NELSIM program and its general usage, and has given some examples of the input language. The remainder of the manual expands on the topics discussed above. Section II discusses the input language applicable to non-electrical system topologies. Sections III and IV describe the input language applicable to differential equations and transfer functions, respectively. The final section, Section V, contains several example problems varying in complexity and mode of analysis. These examples have been included to help the reader comprehend the wide usage range of NELSIM.
SECTION II
ANALOG SYSTEM INPUT LANGUAGE

As discussed in Section I, NELSIM allows the input of nonelectrical systems in terms of networks made up of lumped elements normally utilized within a particular discipline. The disciplines allowed are mechanical, thermal, electromechanical and electro-optical. The general input language for the analog description is discussed below followed by the documentation of each individual discipline.

2.1 GENERAL ANALOG SYSTEM INPUT LANGUAGE

All problems to be entered utilizing lumped elements must be entered using a nodal topology description. The general features of the network input language are explained using thermal quantities and elements. The entries covered below are applicable to all the systems disciplines allowed. Section 2.2 through 2.5 describe the input of mechanical, thermal, electromechanical and electro-optical systems, respectively.

2.1.1 Network Preparation

For a portion of a system described in terms of thermal elements, the network topology is accepted by NELSIM in terms of the standard elements shown in Table I. Each element may be linear or nonlinear. The six steps to be followed in preparing a network for a NELSIM run are summarized below:

- Draw an equivalent network comprised of thermal resistors, thermal capacitors, and temperature and heat flow sources
- Assign a name or number to all nodes in the circuit
- Give a name to each circuit element (beginning with R, C, T, Q)
• Assume arbitrary heat flow directions in each passive circuit element
• Indicate the direction of positive heat flow in each temperature and heat source
• Choose and record circuit values in a consistent set of parameter units.

A node is defined as the point of common potential (temperature) at the junction created by the connection of two or more network elements. Each node is given an arbitrary name consisting of six alphanumeric characters or less. Element names are chosen arbitrarily but must begin with the letter specified in Table I and must not contain more than 5 characters.

TABLE I. STANDARD THERMAL ELEMENTS

<table>
<thead>
<tr>
<th>ELEMENT</th>
<th>SCHEMATIC REPRESENTATION</th>
<th>PROGRAM NOTATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>Resistor</td>
<td>——- ——</td>
<td>R</td>
</tr>
<tr>
<td>Thermal Capacitor</td>
<td>————</td>
<td>C</td>
</tr>
<tr>
<td>Temperature Source</td>
<td>——— ———</td>
<td>T</td>
</tr>
<tr>
<td>Heat Flow Source</td>
<td>————</td>
<td>Q</td>
</tr>
</tbody>
</table>
2.1.2 Element Input Description and Assumed Polarity

In preparing the circuit a heat flow direction and temperature difference are assumed for each element as shown in Figure 4.

The elements are input into the program following the subheading card ELEMENTS using the format:

```
/ELEMENT, NODE 1 - NODE 2 = VALUE
```

where the heat flow direction is assumed to be from Node 1 to Node 2 and the parameters are defined as follows:

- **ELEMENT** - The name of the element beginning with the letter assigned in Table I and followed by 4 alphanumeric characters or less serving as identifiers. i.e., (R12, TIN).
- **NODE 1** - Initial node connected to the element and denoted by up to six alphanumeric characters. (From node)
- **NODE 2** - Final node connected to the element and denoted by up to six alphanumeric characters. (To node)
• **VALUE** - Value of the element. The form of VALUE may be expressed in six different formats to allow for linear and non-linear values of elements. The six formats available are discussed in Section 2.1.4.

The information may be placed anywhere on the card between columns 1 and 72 with the delimiters (comma, dash, equal sign) placed in the order shown. More than one element may be included on any card if separated by commas.

The heat in a source is assumed to flow from the negative to positive pole and VALUE is positive if the nodal connection is entered with the "FROM" node denoting the negative terminal. The source in Figure 5 for example can be entered in the two ways shown below.

\[
\begin{align*}
&\text{\text{\texttt{TI, 1-2 = 100}}} \\
&\text{\text{\texttt{TI, 2-1 = -100}}} 
\end{align*}
\]

Figure 5. Temperature Source Polarity and Assumed Heat Flow

**Example**

The element entry into the program for the simple schematic shown is given below:

\[
\begin{align*}
&TIN, \text{\texttt{GND-1 = VALUE}} \\
&R1, \text{\texttt{1-A1 = VALUE}} \\
&C1, \text{\texttt{A1-GND = VALUE}} \\
&RA, \text{\texttt{A1-2 = VALUE}} \\
&QOUT, \text{\texttt{2-GND = VALUE}} 
\end{align*}
\]
An equally valid entry is:

\[
\begin{align*}
\text{TIN, GND-1} & = \text{VALUE, R1, 1-A1} = \text{VALUE} \\
\text{CI, A1-GND} & = \text{VALUE} \\
\text{RA, A1-2} & = \text{VALUE, QOUT, 2-GND} = \text{VALUE}
\end{align*}
\]

2.1.3 Element Temperatures, Heat Flows

The temperature or heat flow associated with any element is referred to by placing a T or an Q before the element name. TR1 and QR1 therefore refer to the temperature and heat flow associated with resistor R1.

2.1.4 Element and Circuit Value Formats

An element value or circuit quantity may be expressed in the six formats listed below. Each is explained in detail in the following paragraphs.

- Defined Parameter
- Constant
- Table
- Equation
- FORTRAN Function Subroutine
- Expressions

2.1.4.1 Quantities Expressed as Defined Parameters

A circuit element or circuit quantity (temperature, heat flow, derivative) may be expressed in terms of a DEFINED PARAMETER. The format for an element input is

\[
\text{ELEMENT, NODE 1-NODE 2} = \text{PX}
\]

Where X is the name assigned to the parameter and may contain up to five alphanumeric characters. The prefix, P, must always proceed the name X as follows:
2.1.4.2 Quantities Expressed as Constant

An element value, circuit quantity or defined parameter may be expressed as a numerical constant written in either integer or decimal form with or without an exponent. Up to 13 characters may be used to represent the constant. Table II summarizes the constant forms acceptable to the program. Sample element description cards using the constant notation are illustrated below.

<table>
<thead>
<tr>
<th>Format*</th>
<th>Example</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>+XX</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>+XX.</td>
<td>-10.</td>
<td>-10.</td>
</tr>
<tr>
<td>+X. X</td>
<td>-10.2</td>
<td>-10.2</td>
</tr>
<tr>
<td>+X. XE+Y</td>
<td>10.2E-6</td>
<td>10.2 x 10^-6</td>
</tr>
<tr>
<td>+XXE+Y</td>
<td>-10E-4</td>
<td>-10 x 10^-4</td>
</tr>
</tbody>
</table>

2.1.4.3 Quantities Expressed as TABLES

A variable circuit quantity or defined parameter may be expressed in tabular form. The table format is specified as follows for an element:

/ELEMENT, NODE 1 - NODE 2 = TABLE X (VARIABLE)
\[ \sqrt{\text{ELEMENT, NODE 1 - NODE 2} = TX \ (\text{VARIABLE})} \]

where X is the table name containing up to five alphanumeric characters and the variable in parenthesis is the independent variable. The independent variable may be any circuit variable such as voltage, current, elements and defined parameters.

Source Q1 is a function of the temperature across capacitor C1 as shown in the table:

<table>
<thead>
<tr>
<th>Q1</th>
<th>TC1</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>1.5</td>
<td>2</td>
</tr>
<tr>
<td>1.5</td>
<td>3</td>
</tr>
<tr>
<td>0</td>
<td>3</td>
</tr>
<tr>
<td>0</td>
<td>4</td>
</tr>
</tbody>
</table>

Q1 could be entered as

\[ \sqrt{Q1, 1-2 = \text{TABLE 1(TC1)}} \]

or

\[ \sqrt{Q1, 1-2 = \text{TT(TC1)}} \]

The tabular data shown in the table is entered as input pairs under the subheading FUNCTIONS and its format is discussed in Section 2.1.4.6. If the parentheses and variable are left off the table description, TIME is assumed to be the independent variable. Sample table entries follow.
The occasion often arises that the same table data is utilized by more than one element or parameter. A common situation occurs when two current generators in the network are defined by the same tabular data, differing only in the independent variable. In this case the user may define both generators under ELEMENT as

\[
\begin{align*}
/Q1, 1-2 &= \text{TABLE 1(TC1)} \\
/Q2, 7-8 &= \text{TABLE 1(TC2)}
\end{align*}
\]

2.1.4.4 Quantities Expressed as Expressions

A circuit quality, element or defined parameter may be expressed in terms of an expression. The element input format for this form is:

\[
/\text{ELEMENT}, \text{NODE1-NODE2} = XN (\text{NUMERICAL EXPRESSION})
\]

where N is the expression denotation containing up to five alphanumeric characters. An example is given below for source T1

\[
/T1, G-1 = XI (10.*\text{COS}(2.*3.14*PF)}
\]

\[
\begin{align*}
\text{T1} = 10.\text{COS} 2f & \quad \text{where } PF = f
\end{align*}
\]

2.1.4.5 Quantities Expressed as EQUATIONS

A circuit quantity, element or defined parameter may be expressed in terms of an equation. The element input format for this form is:
\[
\text{ELEMENT, NODE 1-NODE 2 = EQUATION } X(a_1, a_2, \ldots, a_n)
\]

or

\[
\text{ELEMENT, NODE 1-NODE 2 = QX(a_1, a_2, \ldots, a_n)}
\]

where \(X\) is the name containing up to 5 alphanumeric characters given to the equation. The variable \(a_1\) through \(a_n\) are described in the equation and may be any circuit quantity, number, defined parameter or table.

Example

Resistor \(R_3\) between nodes 1 and 2 is defined as:

\[
R_3 = f(QR_3, TC_1, P_4)
\]

where \(f(QR_3, TC_1, P_4) = (QR_3 - TC_1) \cdot P_4\).

The element input entry could be as follows:

\[
/R_3, 1-2 = \text{EQUATION 1A(QR3, TC1, P4)}
\]

or

\[
/L_3, 1-2 = \text{Q1A(QR3, TC1, P4)}
\]

The actual mathematical expression \(f(QR_3, TC_1, P_4) = (QR_3 - TC_1) \cdot P_4\) must be defined under the subheading card FUNCTIONS. The details of this input are discussed in Section 2.9. More sample inputs are provided below.

\[
/C2, 6-1 = \text{EQUATIONS 2(.5, 120., TABLE 4(TC2))}
\]

\[
/R17, 1-12 = \text{Q3(TR3, TR2, T2., T1(QR2))}
\]

NOTE: DECIMAL POINTS MUST BE SUPPLIED FOR ALL CONSTANT QUANTITIES ENTERED IN THE ARGUMENT LIST \(a_1\) THROUGH \(a_n\).
2.1.4.6 Quantities Expressed as FORTRAN FUNCTION SUBROUTINES

The user knowledgeable of FORTRAN may enter circuit elements, quantities and defined parameters as separate FORTRAN function subroutines. This feature is extremely useful when a quantity is too complex to be expressed as an equation. The element input format for this form is

\[
/\text{ELEMENT NAME, NODE 1-NODE 2 = FUNCTION } X(a_1, a_2, \ldots, a_n)
\]

or simply

\[
/\text{ELEMENT NAME, NODE 1 - NODE 2 = } FX(a_1, a_2, \ldots, a_n)
\]

where \( X \) or \( FX \) is the name of the subroutine and contains up to five alphanumeric characters and \( a_1 \) through \( a_n \) are the variables utilized in the function subroutine. These variables may be any circuit quantity, element or defined parameter. The subprogram name must be unique and begin with the letter \( F \) if the short form above is used.

Example

Capacitor \( C_1 \) between nodes 1 and 2 is defined as follows:

\[
C_1 = f(TIN, TC3) \quad \text{for } QC1 \quad 1E-3
\]

\[
C_1 = f(TOUT, TC3) \quad \text{for } QC1 \quad 1E-3
\]

where

\[
f(TIN, QC3) = \frac{TIN-TC3}{1E-6}
\]

and

\[
f(TOUT, TC3) = \frac{TOUT-TC3}{1E-6}
\]

Using the subroutine input option the entry is as follows:

\[
/C1, 1-2 = \text{FUNCTION FCAP}(TIN, TC3, TOUT, QC1)
\]

or

\[
/C1, 1-2 = \text{FCAP}(TIN, TC3, TOUT, QC1)
\]
The function subroutine shown below must then be entered as part of the input deck. The variables A, B, C and D appearing in the parenthesis correspond to :IN, TC3, TOUT and QC1, respectively.

```
FUNCTION FCAP (A, B, C, D)
IF (D.GT.1.E-3) GO TO 10
FCAP = (A-B)/1.E-6
RETURN
10 FCAP = (C-B)/1E-6
RETURN
END
```

2.1.5 Defined Parameters Input Format

Every DEFINED PARAMETER utilized in the element input section must be defined. The parameter definition entries must be proceeded by the subheading card

```
/DEFINED PARAMETERS
```

The format utilized to define each defined parameter used is simply

```
/PX = VALUE
```

where X is up to five alphanumeric characters naming the parameter and VALUE can have the same formats used to define elements except for special values. Defined parameter values can therefore be written in the form of

- Constants
- Defined Parameters
- Tables
- Equations
- FORTRAN Function Subroutines
- Expressions

The formats for each have been explained in detail in paragraphs 2.1.4.1 through 2.1.4.7 and remain the same. It will, therefore, suffice here to
give some samples of possible entries under the DEFINED PARAMETERS card in the input deck.

/DEFINED PARAMETERS
/P1 = 3. E-12 ← Constant Form
/POUT = TABLE A4(TR3) ← Tabular Form
/P3 = P4 ← Defined Parameter Form
/P4 = Q3(TR2, QR1, T0.) ← Equation Form
/P5 = FCAP(TC1, TC2, TIME) ← FORTRAN Function Subroutine Form
/P6 = EQUATION 5(10., 20., P4, P5) ← Equation Form
/P7 = X1(P1 * P2) ← Expression Form

2.1.6 Functions

The FUNCTIONS portion of the input is used to define all TABLES and EQUATIONS called for under the ELEMENTS and DEFINED PARAMETERS subheadings. The input cards for tables and equations are preceded by the card

/FUNCTIONS

Their input formats are discussed in the next two paragraphs.

2.1.6.1 Table Input Format

Every TABLE referred to under ELEMENTS or DEFINED PARAMETERS must be explicitly defined under the FUNCTIONS subheading. The tabular data are entered as coordinate pairs separated by commas preceded by the table name. The independent variable must be the first coordinate and the dependent variable the second. If the data require continuation onto another card, the card must end with a dependent variable value. The next card then
begins with the next coordinate pair.

The data pair points must be supplied such that the independent variable is in increasing algebraic order. No specific limit to the number of point pairs that may constitute any table is defined. Only single value functions are allowed. It is permissible to supply two consecutive independent-variable values that are equal, but which have different dependent variable values. This may be done to produce step functions. The example below serves to illustrate various acceptable forms of table input.

**Example**

Referring to a previous example, the card

\[
/Q1, 1-2 = \text{TABLE 1(TC1)}
\]

was entered under ELEMENTS. The function is redrawn here and several valid inputs shown in Figure 6.

---

**Figure 6. Table T1 Values as a Function of TC1**
When the table values are updated at each solution time step, linear interpolation is used between the points supplied. For independent variable values falling outside the range of values supplied in a table, linear
extrapolation is performed to determine the correct table value, and therefore, proper termination may be necessary. For example, in Figure 6, for any value of TIME in excess of 3 the dependent variable Q1 will be assigned the value zero because of the use of the point pair 4.0. In situations where the same table serves to define more than one quantity, the user need only explicitly define the table once. For example, if the two heat sources Q1 and Q2 were input under ELEMENTS as

\[
/\text{Q1, 1-2 = TABLE 1 (TC1)}
\]

\[
/\text{Q2, 7-8 = TABLE 1 (TC2)}
\]

only one TABLE I need be defined under FUNCTIONS.

2.1.6.2 Equation Input Format

Each unique equation referred to under ELEMENTS or DEFINED PARAMETERS must be explicitly defined under the FUNCTIONS subheading in terms of the mathematical expression it represents. The format utilized to enter the equation definition is as follows:

\[
/EQUATION \text{X}(b_1, b_2, \ldots b_n) = (\text{MATHEMATICAL EXPRESSION})
\]

\[
/QX(b_1, b_2, \ldots , b_n) = (\text{MATHEMATICAL EXPRESSION})
\]

X is the alphanumeric name given to the equation when referred to under ELEMENTS or DEFINED PARAMETERS. b_1 through b_n represents a dummy variable list each containing up to six alphanumeric characters and representing the variables called out in the argument list under ELEMENTS or DEFINED PARAMETERS. One restriction is that the DUMMY VARIABLE NAMES MUST NOT BEGIN WITH THE LETTERS I THROUGH N INCLUSIVE. The mathematical expression must appear on the card inside parentheses and be expressed in terms of the dummy variables b_1 through b_n.
The mathematical expression may be any combination of allowable operations, functions, or variables. The following mathematical operations and corresponding symbols are allowed.

<table>
<thead>
<tr>
<th>OPERATION</th>
<th>SYMBOL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exponentiation</td>
<td>**</td>
</tr>
<tr>
<td>Multiplication</td>
<td>*</td>
</tr>
<tr>
<td>Division</td>
<td>/</td>
</tr>
<tr>
<td>Addition</td>
<td>+</td>
</tr>
<tr>
<td>Subtraction</td>
<td>-</td>
</tr>
</tbody>
</table>

The order in which operations are performed is indicated by the order in which the operators are listed. The use of parentheses, to denote clearly the intended mathematical combination, is suggested to avoid ambiguity. For example, \( X + Y \times Z \) should be written as \((X + Y) \times Z\) if \( X + (Y \times Z) \) is not intended. All standard FORTRAN functions may be used, a few of the most commonly used are listed below.

<table>
<thead>
<tr>
<th>FUNCTION</th>
<th>SYMBOL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Square root</td>
<td>SQRT (argument)</td>
</tr>
<tr>
<td>Sine Function</td>
<td>SIN (argument in radians)</td>
</tr>
<tr>
<td>Cosine Function</td>
<td>COS (argument in radians)</td>
</tr>
<tr>
<td>Exponential Function</td>
<td>EXP (argument)</td>
</tr>
<tr>
<td>Arctangent Function</td>
<td>ATNA (argument in radians)</td>
</tr>
<tr>
<td>Hyperbolic Tangent Function</td>
<td>TANH (argument in radians)</td>
</tr>
<tr>
<td>Natural Logarithm Function</td>
<td>ALOG (argument)</td>
</tr>
<tr>
<td>Common Logarithm Function</td>
<td>ALOG10 (argument)</td>
</tr>
</tbody>
</table>

The argument of any function may be any allowable mathematical expression. Mathematical expressions are not limited to 72 characters (one card) and may be continued on subsequent cards, using as many as necessary. In addition, the user may supply subprogram functions that he has written himself (see Section 2.1.4.7).
Referring to a previous Example, the resistor R3 between nodes 1 and 2 was entered under ELEMENTS as:

\[ R3, 1-2 = Q1A(QR3, TC1, P4) \]

where \( f(QR3, TC1, P4) = (QR3 - TC1)*P4 \).

The definition of equation Q1A is entered under the subheading FUNCTIONS as:

\[ Q1A(A, B, C) = ((A-B) * C) \]

where A, B and C correspond to QR3, TC1 and P4 respectively.

Example

The defined parameter \( P1 = TC1 + QR2 - \text{TABLE 2} \) is entered under DEFINED PARAMETERS as

\[ P1 = Q2A(TC1, QR2, \text{TABLE 2}(TC1)) \]

The equation Q2A is in turn defined under FUNCTIONS as

\[ Q2A(A, B, C) = (A + B - C) \]

At each solution step, the ordinate value of Table II would replace the dummy variable C and the computation \((A + B - C)\) carried out.

When more than one element or defined parameter can be defined by the same equation, only one equation need be defined under FUNCTIONS. For example, if the two sources T1 and T2 are defined as:

\[ T1 = (10*QC1 - TR2)/\text{TIME} \]

\[ T2 = (10*QR4 - TC12)/\text{TIME} \]

The two sources could have been described under ELEMENTS as

\[ T1, 1-2 = Q1(10., QC1, TR2, \text{TIME}) \]
\[ T_2, B-14 = Q_1(10., QR4, TC12, TIME) \]

in which case the definition of \( Q_1 \) need only appear once under FUNCTIONS as:

\[ Q_1(X, Y, Z, T) = \frac{(X * Y-Z)}{T} \]

other equation definition inputs are shown below:

\[ Q_{12}(X_C1, P12, \Theta) = (X_C1 - P12 * \cos(\Theta)) \]

\[ EQUATION 43(EIN, ZIN) = (EIN/ZIN) \]

\[ Q_{16}(A, B, C) = (A ** B - C/12.E-4) \]

2.1.7 **Initial Condition Input**

Unless initial conditions for state variables are entered as input data, all voltage and current values are assumed to be zero at the first solution. Initial conditions other than zero often exist and must be input. For example, in AC analysis, initial conditions are needed by the program to linearize all non-linear functions about their operating points. Initial conditions follow the subheading card

\[ /INITIAL CONDITIONS \]

and are entered in the forms

\[ /TX = NUMBER \]

\[ /QX = NUMBER \]

where \( TX \) and \( QX \) represent the temperature and the heat flow associated with element \( X \). Number represents the value of the temperature or heat flow and must be a constant of the form shown in Table II.

If all initial conditions are zero, neither the subheading card nor the data are required. Care must be taken to establish the proper
polarities for initial conditions. Also, the initial capacitor tempera-
tures are positive when they are consistent with the assumed temperature
polarity for the capacitor. Proper statements are illustrated in Figure 7.

The assumed heat flow direction through capacitor C11 of Figure 7 is
from node 4 to node 5. If the initial heat flow is in this direction, it
is entered under the INITIAL CONDITIONS subheading as a positive quantity.
If, however, the heat flows in the opposite direction, it is preceded by a
negative sign. If the actual initial temperature polarity agrees with the
arbitrarily chosen reference direction, that initial temperature is entered
as positive; if not, it is entered as negative.

Figure 7. Temperature Polarity and Heat Flow Direction

2.1.8 Outputs Requests

Any variable used in the program may be requested as an output
variable under the subheading

\[ \text{OUTPUTS} \]

The variables listed under OUTPUTS will appear in a printed listing as a
function of time. The output variables may be any of the following:
- Temperature or heat flow associated with any element such as TC1, QC1
- Temperature or heat flow associated with any source such as T1, QE1, Q2, TJ2
- Any element value such as C17, R4
- Any DEFINED PARAMETER such as P13, POUT
- Any INTERNAL parameter. These are parameters within the program itself.

A typical output request is shown below:

```
//OUTPUTS

//TC1, QR1, R3, TJ4

//QX14, P16
```

The variables may appear anywhere on the card between column 1 and 72 separated by commas. As many variables as desired may appear on one card and as many cards as desired may be used. If more than one card is used, however, the last variable on any card must be followed by blanks.

The output is plotted if the following format is used:

```
//n1, n2, .., nn, PLOT
```

where n1 through nn are desired to be plotted against time. The output requests below would result in

```
//TRY, TC1, TSUP, PLOT

//QC8
```

a listing and plotting of TRY, TC1 and TSUP. The fourth quantity, QC8 would be output in printed form only. If the word PLOT is used, no other dependent variables may follow it on that card.

If a different independent variable is desired, the following format must be used:
In this case the heat flow through capacitor C14 would be printed as well as plotted as a function of the temperature across it.

Additional flexibility is available to permit the user to attach a different label to any output quantity. Consider that elements C1 and R7 exist in a given network and that the temperature across both (TC1 and TR7) are of interest. If the user desires to rename them as TIN and TOUT, he can request the outputs as TC1(TIN), TR7(TOUT), PLOT. The plot, rename, and choice of independent variable options can be presented in terms of the general format as:

\[ YQTY(YLABEL), \ldots, PLOT(XQTY(XLABEL)) \]

If no rename is desired, the general format reduces to

\[ /YQTY, \ldots, PLOT(XQTY) \]

If, in addition, only time is desired as the independent variable, this can be further reduced to

\[ YQTY, \ldots, PLOT \]

If no plotted information is desired, the simplest form arises as

\[ YQTY, \ldots \]

2.1.9 Run Control Input Data

The RUN CONTROLS subheading card is followed by instructions specifying the type of analysis to be performed and the general parameters to control the run. These parameters include such information as the type integration scheme to be used, time limits set on the run, etc. For all the Run Control input data available, the user is referred to a manual of
the SCEPTRE program. These cards are not processed by NELSIM as they apply strictly to the execution of the problem on SCEPTRE upon NELSIM output. A few of these commands are illustrated below.

2.1.9.1 Stop Time

All transient runs must have a problem duration in terms of time units calculated or assumed. This is the value indicating how far out in time the solutions are to be calculated. This entry is of the form:

/STOP TIME = NUMBER

where NUMBER is a constant in time units chosen.

2.1.9.2 Maximum Integration Passes

Another type of limit is available that operates on the number of passes made by the integration routine. In the absence of any instruction from the user, the program imposes a limit of 20,000 passes. The user may change this limit by entering

/MAX INTEGRATION PASSES = NUMBER

2.1.9.3 Start Time

Most transient analysis problems begin at time zero and for this case no entry is needed. If, however, the user desires to begin the run at other than time = 0, the following card is necessary

/START TIME = NUMBER

where NUMBER is a constant value in units of time assigned to the problem.

2.1.9.4 Minimum Step Size

This quantity is designed to terminate the run automatically whenever a time solution increment is required that is smaller than the minimum increment. If this quantity is not supplied, the program will automatically compute a minimum limit equal to $1 \times 10^{-9}$ times the problem
duration (STOP TIME). If a specific minimum step size independent of the problem duration is desired, the format is

\[ \text{/MINIMUM STEP SIZE = NUMBER} \]

For example if

\[ \text{STOP TIME = 5} \]

is specified, the minimum size would automatically be taken to be \(5 \times 10^{-9}\). If the user is not satisfied with this minimum step-size and desires to change it to \(1 \times 10^{-5}\) he may do so using the following entry

\[ \text{/MINIMUM STEP SIZE = 1E -5} \]

2.1.9.5 Punched Output

Nominal, the output from NELSIN is in printed form and punched card output is suppressed. To obtain SCEPTRE input decks (a copy of the printed output), the punch option must be turned on by inserting a card in the run controls input data as,

\[ \text{/PUNCHED OUTPUT} \]

2.1.10 Mutual Inductance Input Description

Although there is no thermal analogy for an inductor, inductors will appear in other simulations such as the representation of an electromagnetic system. Additionally, the concept of mutual inductance can appear in a simulation such as for a transformer.

Mutual inductance is also entered under the ELEMENTS subheading but has a slightly different format. If coupling exists between inductors L1 and L2, the appropriate entry must include these elements in place of the node identification such as

\[ \text{/Mx, L1-L2 = VALUE} \]
In addition, a physical limitation of the principle of mutual inductance must be observed in order to have a physically realizable circuit. That is, since coefficient of coupling, \( k \), is always less than unity and by definition

\[
K = \frac{M}{\sqrt{L_1 L_2}} < 1
\]

the user should be certain that \( M < \sqrt{L_1 L_2} \). Stated in words, the mutual inductance between any two inductors must be less than the square root of the product of the self-inductances of the components between which the mutual inductance exists. The sign of \( M \) is positive if in a given winding the induced voltage of mutual inductance acts in the same direction as the induced voltage of self-inductance. If the induced voltage of mutual inductance opposes the induced voltage of self-inductance in a given winding, \( M \) is negative. The proper sign for \( M \) for the assumed current directions is illustrated in Figure 8.

![Figure 8. Mutual Inductance Polarities](image)
2.1.11 NELSIM Program Limits

Table III gives the program data limits which have been established in the program. These limits are considered adequate for most normal circuit analysis work. Approximate limits are also given for the number of TABLE and EQUATION functions.

Table III. Program Data Limits

<table>
<thead>
<tr>
<th>Description of Data</th>
<th>Maximum Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elements</td>
<td>300</td>
</tr>
<tr>
<td>Nodes</td>
<td>301</td>
</tr>
<tr>
<td>Defined Parameters</td>
<td>100</td>
</tr>
<tr>
<td>Defined Parameter Differential Equations</td>
<td>100</td>
</tr>
<tr>
<td>Mutual Inductances</td>
<td>50</td>
</tr>
<tr>
<td>Arguments in Equation Value Specification</td>
<td>50</td>
</tr>
<tr>
<td>Output Requests</td>
<td>100</td>
</tr>
<tr>
<td>Supplied Initial Conditions</td>
<td>300</td>
</tr>
<tr>
<td>Equation Functions (1 equation per card)</td>
<td>80 (approximately)</td>
</tr>
<tr>
<td>Cards per Equation Function</td>
<td>20</td>
</tr>
<tr>
<td>Table Functions</td>
<td>80 (approximately)</td>
</tr>
</tbody>
</table>

2.2 MECHANICAL SYSTEM INPUT LANGUAGE

Entry of a mechanical problem into NELSIM is very similar to the entry of an electrical network as explained in Section 2.1. An analog network made up of mechanical elements connected between nodes must be derived by the user. These elements may be defined as linear or non-linear quantities using the six formats outlined in Section 2.1. Two sets of mechanical elements are allowed as input for mechanical problems, one for translational systems, the other for rotational systems. The elements, their schematic
representation, as well as program notation, are shown in Table IV.

### TABLE IV. MECHANICAL STANDARD ELEMENTS

<table>
<thead>
<tr>
<th>Element</th>
<th>Schematic Representation</th>
<th>Program Notation</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Translational</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mass</td>
<td></td>
<td>M</td>
</tr>
<tr>
<td>Dashpot</td>
<td></td>
<td>D</td>
</tr>
<tr>
<td>Spring Stiffness</td>
<td></td>
<td>K</td>
</tr>
<tr>
<td>Friction</td>
<td></td>
<td>B</td>
</tr>
<tr>
<td>Force</td>
<td></td>
<td>F</td>
</tr>
<tr>
<td>Velocity</td>
<td></td>
<td>V</td>
</tr>
<tr>
<td>Moment of Inertia</td>
<td></td>
<td>J</td>
</tr>
<tr>
<td><strong>Rotational</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Friction</td>
<td></td>
<td>B</td>
</tr>
<tr>
<td>Rotational Stiffness</td>
<td></td>
<td>K</td>
</tr>
<tr>
<td>Torque</td>
<td></td>
<td>T</td>
</tr>
<tr>
<td>Angular Velocity</td>
<td></td>
<td>W</td>
</tr>
</tbody>
</table>
The elements must be entered in the format shown in Section 2.1 and begin with the letters indicated in Table IV. Table V shows the electrical analogs that are generated from each mechanical element and the numerical translation.

**TABLE V. MECHANICAL TO ELECTRICAL ANALOG GENERATION**

<table>
<thead>
<tr>
<th>Translational</th>
<th>Rotational</th>
</tr>
</thead>
<tbody>
<tr>
<td>FORCE ⇒ CURRENT (I = F)</td>
<td>TORQUE ⇒ CURRENT (I = T)</td>
</tr>
<tr>
<td>VELOCITY ⇒ VOLTAGE (V = V)</td>
<td>VELOCITY ⇒ VOLTAGE (V = W)</td>
</tr>
<tr>
<td>MASS ⇒ CAPACITANCE (C = M)</td>
<td>MOMENT OF I ⇒ CAPACITANCE (C = J)</td>
</tr>
<tr>
<td>SPRING ⇒ INDUCTOR (L = 1/K)</td>
<td>SPRING ⇒ INDUCTANCE (L = 1/K)</td>
</tr>
<tr>
<td>FRICTION ⇒ RESISTANCE (R = 1/B)</td>
<td>FRICTION ⇒ RESISTANCE (R = 1/B)</td>
</tr>
</tbody>
</table>

### 2.2.1 Mass Connections

The node names are user derived in general. For mass connections, however, a restriction is placed on the user. All masses must be connected to a ground node beginning with the letter G. Further, all masses must appear at node points only. If two or more masses are connected to different points, each must be connected to the common ground node. The following system shows a possible nodal connection for a 2 mass system.
2.2.2 Friction Connections

Friction can occur as the resistive force between two masses or be represented as a dashpot (Figure 9). Two types of nodal connections are, therefore allowed for a friction input, one between masses and one between nodes.

Figure 9. Frictional Elements
The frictional element inputs for Figure 9 are shown below:

```
ELEMENTS

B1, M1-M2 = VALUE
B2, 2-G = VALUE
B3, M2-G = VALUE
```

2.3 MECHANICAL SYSTEM STATE VARIABLES

The state variables applicable to mechanical system and recognized by the program are shown in Table V. These can be referred to in the input language by placing the designation letter of Table V before the element it applies to, for example FK1 represents the force exerted on spring K1.

**TABLE VI. MECHANICAL SYSTEM STATE VARIABLES**

<table>
<thead>
<tr>
<th>Translational</th>
<th>Rotational</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>State Variable</strong></td>
<td><strong>Program Notation</strong></td>
</tr>
<tr>
<td>Force</td>
<td>F</td>
</tr>
<tr>
<td>Velocity</td>
<td>V</td>
</tr>
</tbody>
</table>

The state variables are analogous to **voltage** and current in the electrical case where angular velocity represents voltage and torque represents current.

**INITIAL CONDITIONS**

Initial conditions are handled in a manner similar to the electrical case. The mechanical analog of a capacitor is a mass (M) for the translational case and the moment of inertia (J) for the translational case. The mechanical analog of an inductor is the spring stiffness K. Therefore, the initial conditions of a mechanical system can be entered as the force...
exerted on $K_s$ and velocity on $M_s$ and about $J_s$. Some samples are given below.

**INITIAL CONDITIONS**

$W_5 = 10$

$W_{M10} = 15$

$V_{M2} = 5$

$F_{K12} = -20$

2.4 OUTPUTS

The outputs are entered in the manner described in Section 2.1.10 with the electrical element names replaced by mechanical element names, voltage replaced by velocity ($V$) or angular velocity ($W$) and current replaced by force ($F$) or torque ($T$).

Mechanical System Input Examples. Consider the mechanical problem shown in Figure 10.

![Figure 10. Mechanical Problem](image)

The noded mechanical system and input for NELSIM is shown in Figure 11.
ANALOG DESCRIPTION

MECHANICAL ELEMENTS

V1,6-3=Q1(TIME)
K1,62-3=1
K2,61-2=P2
K3,6-1=3
M2,2-62=.2
M3,1-61=.3
B1,61-2=1

FUNCTIONS
Q1(T)=(COS(2.*T))

DEFINED PARAMETERS
P2=2

OUTPUTS
VM2(V2),VM3(V3),PLOT

RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=10

END

Figure 11. NELSIM Input for Mechanical System
Figure 12 represents a rotational system and its input for the normalized case where all values are set equal to 1.

ANALOG DESCRIPTION
MECHANICAL ELEMENTS
W1, G-1 = 1
K1, 1-2 = 1
J2, 2-G1 = 1
K2, G1-3 = 1
J3, 3-G2 = 1
B3, J3-G = 1
B2, J2-G = 1
OUTPUTS
WJ2, WB2, PLØT
RUN CONTROLS
STOP TIME = 1
END

Figure 12. NELSIM Input for a Rotational Problem

2.5 THERMAL SYSTEM INPUT

The input to NELSIM for a thermal problem is similar to the input of a mechanical problem. The elements for a thermal system are shown in Table VII.
TABLE VII. THERMAL ELEMENTS AND STATE VARIABLES

<table>
<thead>
<tr>
<th>Element</th>
<th>Schematic Representation</th>
<th>Program Notation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thermal Capacitance</td>
<td><img src="image" alt="Schematic" /></td>
<td>C</td>
</tr>
<tr>
<td>Thermal Resistance</td>
<td><img src="image" alt="Schematic" /></td>
<td>R</td>
</tr>
<tr>
<td>Temperature Source</td>
<td><img src="image" alt="Schematic" /></td>
<td>T</td>
</tr>
<tr>
<td>Heat Flow Source</td>
<td><img src="image" alt="Schematic" /></td>
<td>Q</td>
</tr>
</tbody>
</table>

The user must derive a thermal analog network made up of the elements shown in Table VII. The value of these elements may be entered in any of the formats documented in Section 2.1.6.

**Thermal State Variables**

The state variables for thermal input are Temperature (T) and heat flow (Q) and are analogous to voltage (V) and current (I) respectively in the electrical network.

**Initial Conditions**

Initial conditions for a thermal system may be entered as the temperature across a thermal capacitance. This is analogous to a voltage across an electrical capacitance. Some examples follow.
INITIAL CONDITIONS
TC1 = 10
TC2 = 20

Outputs

Outputs are requested as defined in Section 2.1.10 with the electrical elements replaced by the thermal elements of Table VII, voltage (V) replaced by Temperature (T) and current replaced by heat flow (Q).

Thermal Input Example

The following problem illustrates the input of a thermal system. Consider the rocket engine test setup shown in Figure 13 for which it is desired to study the transient temperature response within the engine wall. The input of the problem requires the various subdivisions within the wall to be indicated by nodes (1-3) and shown in Figure 13 (b). The thermal resistance between subdivisions is simulated using resistors and thermal capacitance using capacitors. The element input is shown below.

ANALOG DESCRIPTION
THERMAL
ELEMENTS
TIN, G-1=T1
R1, 1-2=1
C1, 2-G=1
R2, 2-3=1
C2, 3-G=1
R3, 3-4=1
TOUT, G-4=1

FUNCTIONS
T1=0, 1, 2, 10, 5, 10, 6, 1, 10, 1

OUTPUTS
TIN, QC1, QC2, QRC3, PLOT
TR3, TC1, PLOT

RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=15
RUN INITIAL CONDITIONS
END
The elements have all been entered as constant values for simplicity but in general will be non-linear functions of the materials involved and will be entered using a variety of value formats.

(a) Rocket-engine walls

(b) System Model Showing

Figure 13. Heat Transfer Example
2.6 ELECTRO-MECHANICAL ELEMENTS AND MODELS

The entry of electro-mechanical problems into NELSIM is possible in several ways. The differential equation and transfer function entries are deferred until a general treatment of these topics in Sections III and IV, respectively. Two additional modes of entry, however, are available to the user, namely

1) Electro-mechanical element entry
2) Model entry

2.6.1 Electro-Mechanical Element Entry

NELSIM will allow for the input of an electro/mechanical system in terms of the lumped elements of both the electrical and mechanical portions of the system coupled together through common defined parameter names, algebraic or first order differential equations or dependent sources. The mechanical and electrical elements are entered following the subheadings ELEMENTS (MECHANICAL) and ELEMENTS (ELECTRICAL), respectively. The electrical elements allowed are discussed in Section 2.1. The input is better illustrated through an example. Consider the galvanometer sketch provided in Figure 14. A galvanometer ideally produces a deflection that is proportional to an electrical input.

![Galvanometer Schematic Representation](image)

Figure 14. Galvanometer Schematic Representation
Figure 15 represents the equivalent lumped network in terms of its electrical and mechanical parts.

\[ i(t) \]

\[ e_1(t) \]

\[ e_c(t) = D \omega_r(t) \]

\[ \tau(t) = D i(t) \]

where \( J \) and \( B \) represent the moment of inertia of the rotor and the viscous damping that results from air friction. The element \( K_R \) represents the rotational stiffness produced by a spring attached to the rotor. The constant \( D \) is defined to be \( \beta I a \) where \( \beta \) is the magnetic flux density, \( I \) is the total length of the conductor and \( a \) is the radius of the rotor.

The input language where all the elements are normalized to one follows.

\begin{verbatim}
ANALOG DESCRIPTION
ELECMO  MECHANICAL
ELEMENTS  (ELECTRICAL)
E1,6-1=1
R1,1-2=1
EC,6-2=DEC(PD,WR)
ELEMENTS  (MECHANICAL)
T1,6-3=DEC(PD,IR1)
JR,3-6=1
BR,3-6=1
KR,3-6=1
\end{verbatim}

 Electrical Source in terms of rotational Velocity

 Applied Mechanical Torque in terms of current through resistor
The two dependent sources EC and TI provide the interface between the two systems and are entered directly in terms of the elements involved.

**Element NAME uniqueness**

NELSIM converts all mechanical elements to electrical equivalent elements by replacing the first letter of the element. For example, Mass M15 becomes capacitor C15 and spring constant K1 becomes inductor L1. Care must, therefore, be taken by the user to avoid duplication of names in the resulting network. This can be accomplished by checking that all electrical and mechanical elements have unique denotations following the first letter.

2.6.2 Built in Models

This option will allow the user to include models of generally used electro-mechanical devices in his system by simply calling for them. It is difficult to derive models general enough to suit all needs but it should be kept in mind that the capability to input system problems in terms of differential equations or transfer function blocks allows the user to build his own models. The two models presently implemented into NELSIM are that of a rate gyroscope and an accelerometer. The call to a model will be of the form

\[ T1, N1-N2 = \text{MODEL XXXX} \]

where N1 represents the input to the model and N2 the output and XXX is the built in model name. The two models are discussed below. The model entries are submitted following the subheading MODELS.

2.6.2.1 Rate Gyro Model

Rate gyros are used widely in any application requiring tracking and stabilization. Aircraft and missiles utilizes gyros for stabilization when angular deviations are noticed. Rate gyros are also used extensively in conjunction with tracking antennas so that the angular velocity of the
tracked vehicle can be measured. A mathematical block diagram of a rate gyro is given in Figure 16.

![Block Diagram of Rate Gyro](image)

**Figure 16. Block Diagram of Rate Gyro**

In the figure $\omega_i$ represents the rate input to the gyro and $e_o$ the proportional output voltage generated. The $K$'s represent amplifiers within the system to attain the desired signal levels with $K_{SG}$ representing the signal generator which generates an electrical signal proportional to the displacement angle $\theta_0$. The transfer function between $T2$ and $T1$ is calculated as follows:

$$\frac{T2}{T1} = \frac{K/C}{S(1+\frac{J}{C}S)}$$

$$1 + \frac{K/C}{S(1+\frac{J}{C}S)}$$

when simplified the above equation becomes

$$\frac{T2}{T1} = \frac{1}{1 + \frac{C}{K}S + \frac{J}{K}S^2}$$
The above represents the closed loop transfer function of the rate gyro which can be recognized as having the form

\[ F(S) = \frac{1}{1 + \frac{2\xi}{\omega_n} S + \frac{1}{\omega_n^2} S^2} \]

where \( \xi \) is the damping factor and \( \omega_n \) the natural frequency. Like terms yield that

\[ \omega_n = \frac{K}{J} \text{ and } \xi = \frac{C}{2\sqrt{KJ}} \]

which allows the user to adjust both of these quantities by adjusting the various gains.

The model equivalent for NELSIM input is shown in Figure 17 where \( PB = 1/C \) and \( PC = J \). The feedback gain \( PF \) has been added for further generalization of the model and if set equal to one will result in the transfer function \( F(s) \). Use of the model requires the user to input the request under the ELECTRO-MECHANICAL heading and following the MODELS subheading card. Usage also requires the user to define all the gains needed by the model (PA, PB, PC, PD, PF). The letter \( P \) is attached to both the input node and the output node of a model as well as the name assigned by the user. If the model is referred to as M1 for example the input to the model becomes PINM1 and output POUTM1. The model name is also attached to the internal parameters to maintain parameters name uniqueness (i.e., PIM1, PG2M1, PF1). To illustrate consider Figure 18 for which \( H \) represents the gyro model.
Figure 17. NELSIM Equivalent Rate Gyro

Figure 18. NELSIM Gyro Model
2.6.2.2 Accelerometer Model

The accelerometer is the basic measuring element in an inertial navigation and guidance system. It is the function of the accelerometer to provide measurement and integration of linear acceleration to successfully accomplish the functions of position and velocity indication and generation of proper steering signals. Although numerous models are available the double integrating accelerometer shown in Figure 19 has been implemented into NELSIM.

In the model \( a_1 \) represents the input acceleration, \( e_0 \) the signal voltage generated and \( \ddot{\theta} \) the angular acceleration of the motor shaft resulting from the application of \( e_0 \). The double integration of the angular velocity \( (\ddot{\theta}) \) yields the angular velocity \( (\dot{\theta}) \) and relative angle.
Figure 19. Acceleration Model
(θ) of the shaft. These two quantities are proportional to the craft velocity (V) and distance traveled (X). The mathematical formulation is given below.

\[
\frac{T_3}{T_2} = \frac{(K_2K_{SG}K_4)S}{S(1 + \frac{K_3}{K_2}S)(1 + K_5S) + (K_2K_{SG}K_4)S} \\
= \frac{N}{1 + aS + bS^2 + N}
\]

where:

\[
N = (K_2K_{SG}K_4)S \\
a = \frac{K_3}{K_2} + K_5 \\
b = \frac{K_3K_5}{K_2}
\]

inserting \( T = K_1a_1 \) and applying the final value theorem for an assured step input yields

\[
T_3 = KK_1a_1
\]

in the steady state which shows the angular acceleration of the shaft to be proportional to the input acceleration. Another relationship exist for \( T_3 \), namely

\[
T_3 = K_6 \theta S^2
\]

equatting the two yields

\[
KK_1a_1 = K_6 \theta S^2
\]

To determine velocity and distance changes as a function of \( a_1 \) both sides of this equation are integrated.
The model programmed into NELSIM is illustrated in Figure 20.
The usage and response of the model is illustrated for the case where all gains have been normalized to 1 and the input to the model is a unit step. Consider Figure 21 where \( H \) is the accelerometer.

![Figure 21. NELSIM Accelerometer Model](image)

The input to NELSIM is given below:

```
ANALOG DESCRIPTION
ELECTRO MECHANICAL
MODELS
T1, IN-OU=ACCELEROMETER
DEFINED PARAMETERS
PAT1=1
PB1=1
PC1=1
PD1=1
PET1=1
PFT1=1
PGT1=1
PINT1=T1
FUNCTIONS
T1=0, 1, 0, 1, 10, 1
OUTPUTS
PINT1, PAT1, PA2T1, PA3T1, PA4T1, PLOT
PA5T1, POUT1, PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=10
END
```

As was required for the gyro model, all gains within the model must be provided by the user with the model label (T1) added to each name.

2.7 ELECTRO-OPTICAL SYSTEM INPUT

Electro-optical systems are represented in NELSIM as equivalent electrical circuits capable of simulating the AC characteristics of photo diode devices.
The most commonly used circuit is illustrated in Figure 22 followed by the NELSIM input describing the circuitry.

![Equivalent Circuit of a Photo Diode](image)

**Figure 22. Equivalent Circuit of a Photo Diode**
In the above input, the photo current $I_{PH}$ is described by a perfect-square law formulation

$$I_{PH} = (n \eta \frac{P}{hv})$$

where,

$\eta$ = quantum efficiency

$\frac{P}{hv}$ = average number of incident photons per unit time

$\frac{I_{PH}}{q}$ = average number fps unit time of electrons emitted from the photocathode.

Since the input is as an equivalent circuit, the circuit elements are detailed as ELEMENTS (ELECTRICAL) and the element names are consistent with the network preparation rules of Section 2.1.2.

Since the device response is dependent upon the frequency of the energy source it is best to construct a circuit for frequency bands and sum the produced currents linearly, or to restrict the analysis to a certain frequency band.

2.8 UNITS AND SCALING

The following paragraphs describe the scaling option in NELSIMP. In order to allow NELSIMP to be completely compatible with SCEPTRE in the flexibility of its input language the scaling module is semiautomated and requires user interaction.

2.8.1 Units

SCEPTRE allows any set of parameter units as long as the element magnitudes with respect to these are consistent. To maintain the two input languages consistent, the same will be true of NELSIMP. The user is allowed
to enter a problem in any set of units he chooses and is responsible for
compatibility throughout his system.

2.8.2 Scaling Guidelines and Automation

One of the problems encountered in system analysis utilizing numeri-
cal integration is that of maintaining a consistent set of parameter units
such that the magnitudes of all the solution variables are consistent
with the specified error criteria. Numerical inaccuracies result and
excessive solution time is spent when units are not carefully chosen due
to the difficulties in meeting specified error criteria. Previous
experience in the system analysis area and application of SCEPTRE and
other codes to large-scale circuit and system problems has shown that is
desirable to maintain the magnitude of the solution variables in the range
between $10^{-3}$ and $10^3$. For example, voltage and current are the two
solution variables used by SCEPTRE and it is desirable to keep these
variables within the limits shown below

$$10^{-3} \leq |V| \leq 10^3$$

$$10^{-3} \leq |I| \leq 10^3$$

The desired magnitude ranges can be accomplished through knowledge of the
basic laws governing a particular system and a knowledge of the ranges
expected. If the expected units of the solution variables and time are
known, the system element units can be scaled to yield those units. The
above is exemplified through a high speed transistorized circuit in which
the response is known to be in terms of volts, milliamps and nanoseconds.
Equations 1 through 3 illustrates the applicable relationships between
state variables and electrical elements.
\[ R = \frac{V}{I} \quad (1) \]
\[ C = I \frac{dt}{dV} \quad (2) \]
\[ L = V \frac{dt}{dT} \quad (3) \]

Where:
- \( V \) = Voltage
- \( I \) = Current
- \( R \) = Resistance
- \( C \) = Capacitance
- \( L \) = Inductance

To obtain the response in terms of volts, milliamps and nanoseconds the elements are scaled as follows:

\[ R = \frac{V}{I} = \frac{\text{Volts}}{\text{ma}} = \frac{1}{10^{-3}} = 10^3 \, \text{(kiloohms)} \]

\[ C = I \frac{dt}{dv} = \text{ma, nsec} = \frac{(10^{-3})(10^{-9})}{1} = 10^{-12} \, \text{(picofarads)} \]

\[ L = V \frac{dt}{dT} = \text{Volts. nsec} = \frac{(1)(10^{-9})}{10^{-3}} = 10^{-6} \, \text{(microhenries)} \]

Definition of the network elements in terms of these units will bring the solution variables closer to their desired range.

The same procedure is applicable to other systems. Equations 4 through 8 present the relationships necessary for mechanical and thermal systems.
MECHANICAL SYSTEMS

\[ B = \frac{F}{V} \quad (4) \]
\[ M = F \frac{dt}{dV} \quad (5) \]
\[ K = \frac{1}{V} \frac{dF}{dt} \quad (6) \]

Where: 
V = Velocity 
F = Force 
M = Mass 
K = Spring Constant 
B = Viscosity/Friction

THERMAL SYSTEM

\[ C = Q \frac{dt}{dT} \quad (7) \]
\[ R = \frac{T}{Q} \quad (8) \]

Where: 
Q = Rate of heat flow 
C = Thermal Capacitance 
R = Thermal Resistance 
T = Temperature

2.8.3 Automated Scaling

An algorithm has been implemented within the NELSIM program to achieve scaling of a network. The program generates an electrical analog from various types of system inputs. The scaling algorithm scales all the elements to magnitudes consistent with user provided guidelines. The option require the user to input the expected units of the solution variable and time in terms of electrical quantities. Table VIII shows the analogies
between the various systems involved. Both mechanical and thermal quantities are translated into the electrical quantities shown in the table, such that in the translated network the only solution variables are electrical. The user will enter a problem in terms of the standard units familiar to the field involved. Table IX illustrates the units that are expected if the scale option is utilized. The user indicates the scaling to be performed by entering the expected magnitudes of the solution variables and time. For example, consider the electronic network discussed earlier entered in terms of the standard elements shown in Table IX. To obtain the solution in terms of volts, milliamps and nanoseconds the network must be scaled. The user input would consist of the card shown below which states that the scaling option is desired

```
SCALE OPTION, VOLTAGE=1, CURRENT=10E-3, TIME=10E-9
```

and the voltage is to remain in terms of volts but current and time are to be scaled to milliamps and nanoseconds accordingly. Use of the scaling option for all system components will maintain a consistent set of variable values.

The output of the program consists of two listings. The first is a listing of the analog network generated with no scaling applied. The second consists of the analog network with all constant elements scaled and a list of the scale factors used on the elements. The user is then required to scale all non-constant element values to complete the scaling task.

To illustrate the use of the scaling option consider the mechanical problem presented earlier. It is desired to scale time by a factor of $10^{-3}$, force by a factor of $10^{-3}$ and leave the velocity units the same.
### TABLE VIII. SYSTEM ANALOGIES

<table>
<thead>
<tr>
<th>SYSTEM FUNCTION</th>
<th>ELECTRICAL</th>
<th>MECHANICAL</th>
<th>THERMAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>SOLUTION VARIABLES</td>
<td></td>
<td>Translational</td>
<td>Rotational</td>
</tr>
<tr>
<td>Voltage</td>
<td>Voltage</td>
<td>Velocity</td>
<td>Angular Velocity</td>
</tr>
<tr>
<td>Current</td>
<td>Current</td>
<td>Force</td>
<td>Torque</td>
</tr>
<tr>
<td>TIME</td>
<td>TIME</td>
<td>Time</td>
<td>Time</td>
</tr>
<tr>
<td>ELEMENTS</td>
<td>Resistance</td>
<td>Friction</td>
<td>Friction</td>
</tr>
<tr>
<td></td>
<td>Capacitance</td>
<td>Mass</td>
<td>Moment of Inertia</td>
</tr>
<tr>
<td></td>
<td>Inductance</td>
<td>Spring Stiffness</td>
<td>Spring Stiffness</td>
</tr>
</tbody>
</table>

### TABLE IX. STANDARD SYSTEM UNITS

<table>
<thead>
<tr>
<th>PHYSICAL MEDIUM</th>
<th>ELEMENTS</th>
<th>SYMBOL</th>
<th>STANDARD</th>
<th>MKS</th>
<th>ENGLISH</th>
<th>E&quot;&quot;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electrical</td>
<td>Resistance</td>
<td>R</td>
<td>Ohms</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Capacitance</td>
<td>C</td>
<td>Farads</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Inductance</td>
<td>L</td>
<td>Henries</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mechanical</td>
<td>Mass</td>
<td>M</td>
<td>Kilogram</td>
<td></td>
<td>Slug</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Spring Stiffness</td>
<td>K</td>
<td>Newton/ meter</td>
<td></td>
<td>lb/ft</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Friction</td>
<td>B</td>
<td>n-sec/m</td>
<td></td>
<td>lb/ft</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Moment of Inertia</td>
<td>J</td>
<td>mm/(rad/sec^2)</td>
<td></td>
<td>ft lb/(rad/sec^2)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Angular Velocity</td>
<td>W</td>
<td>rad/sec</td>
<td></td>
<td>rad/sec</td>
<td></td>
</tr>
<tr>
<td>PHYSICAL MEDIUM</td>
<td>ELEMENTS</td>
<td>SYMBOL</td>
<td>STANDARD</td>
<td>MKS</td>
<td>ENGLISH</td>
<td>BTU</td>
</tr>
<tr>
<td>-----------------</td>
<td>----------------</td>
<td>--------</td>
<td>----------</td>
<td>-----</td>
<td>---------------</td>
<td>-----------</td>
</tr>
<tr>
<td>Thermal</td>
<td>Temperature</td>
<td>T</td>
<td></td>
<td></td>
<td>$^\circ F$</td>
<td>BTU/sec</td>
</tr>
<tr>
<td></td>
<td>Heat flow rate</td>
<td>Q</td>
<td></td>
<td></td>
<td>BTU/$^\circ F$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Capacitance</td>
<td>C</td>
<td></td>
<td></td>
<td>(BTU/$^\circ F$/ \text{lb})</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Resistance</td>
<td>R</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
As shown in Table VIII, the analog quantities for force and velocity are current and voltage, respectively. The scale request is

SCALE OPTION, TIME=1E-3, CURRENT=1E-3, VOLTAGE=1

The output of NELSIM will first list the network analog generated with no scaling applied, and the second lists, the value of analog elements with all constant elements.
SECTION III
TRANSFER FUNCTION INPUT LANGUAGE

The input language for a network topology was described in the preceding section. For a certain class of problems, a signal flowgraph representation of the system may already be at hand, for example, control systems.

An input language has been devised to allow the direct input of a flowgraph into NELSIM. The program interprets this input, and from it derives the set of first order differential equations necessary to execute the problem in SCEPTRE.

The input utilizes the same type of format available for circuit inputs in SCEPTRE and is nearly identical to SYNAP. The data are placed under headings and subheadings in a similar fashion and is format free. The statements consist of descriptive user-derived names for nodes, components, and value specifications separated by delimiters, such as commas, parentheses, and dashes. The input data may be punched anywhere on the card within the first 72 columns. To continue a statement from one card to another, the only requirement is that the discontinuation be made immediately after delimiters, with the delimiter being the last non-blank character on the card. The input data organization is shown in Figure 23. Each entry is described in the following paragraphs.
3.1 FLOWGRAPH INPUT PREPARATION

The flowgraph description is defined in terms of branch transmittances connected between nodes. The steps listed below should be followed in preparing a signal flowgraph for input.

Assign a name or number to all nodes in the graph (four or less alphanumeric characters).

Assign a name or value to all transmittance parameters (four or less alphanumeric characters). All parameters must begin with the letter P and be defined under the DEFINED PARAMETERS subheading.

Label signal flow direction between node connections using arrowheads.

Figure 24 illustrates a flowgraph ready for input generation.
3.2 GRAPH DESCRIPTION

For Network topologies the first card was ANALOG DESCRIPTION, in the same matter, the first card to describe a signal flow graph is

\[ \text{TRANSFER FUNCTIONS} \]

This card indicates to the program that a flowgraph is being input and allows the program to enter the graph processor directly.

3.3 BRANCHES

The flowgraph is made up of branches containing some transmittance characteristics between one node and another. The format for any branch is shown below where:

\[ \text{NODE1} - \text{NODE2 (BRANCH TRANSMITTANCE)} \]

- NODE1 denotes the initial node from which the signal originates (from node)
- NODE2 denotes the final node of the transmittance (to node)

The general form of the branch transmittance is a rational polynomial of the form

\[
P(S) = \frac{N_0 \cdot B_{01} \cdot B_{02} \cdot ... \cdot B_{0n} + N_1 \cdot B_{11} \cdot B_{12} \cdot ... \cdot B_{1n} S + ... + N_m \cdot B_{m1} \cdot B_{m2} \cdot ... \cdot B_{mn} S^m}{M_0 \cdot C_{01} \cdot C_{02} \cdot ... \cdot C_{0n} + M_1 \cdot C_{11} \cdot C_{12} \cdot ... \cdot C_{1n} S + ... + M_k \cdot B_{k1} \cdot B_{k2} \cdot ... \cdot B_{kn} S^k}
\]

where

- \( N_0, N_1, N_2, \ldots, N_m, M_0, M_1, \ldots, M_k \) are transmittance coefficient parameters
- \( B_{01}, B_{02}, \ldots, B_{0n}, B_{11}, B_{12}, \ldots, B_{1n} \)
- \( C_{01}, C_{02}, \ldots, C_{0n}, C_{11}, C_{12}, \ldots, C_{1n} \)

Polynomials of this form are recognized by the program by using the following input form:
where the expanded form yields

/\NODE - NODE (N_0 \ast B_01 \ast B_02 \ldots B_0n, C_0, N_1 \ast B_11 \ast B_12 \ldots B_1n, T, \\
n_2 \ast B_21 \ast B_22 \ldots B_2n, 2, \ldots, N_m \ast B_{m1} \ast B_{m2} \ldots B_{mn}, m/ \\
M_0 \ast C_01 \ast C_02 \ldots C_0n, 0, M_1 \ast C_{11} \ast C_{12} \ldots C_{1n}, 1, M_2 \ast C_{21} \ast C_{22} \ldots C_{2n}, 2, \\
\ldots, M_k \ast C_{k1} \ast C_{k2} \ldots B_{kn}, K)

3.4 INPUT/OUTPUT REFERENCE

Each node name entered in the branch description is translated into a defined parameter by NELSIM by adding the letter P to each node. This is done to satisfy the SCEPTRE input as well as interfaces requirements that will be discussed later. The user desiring to define or output a node must refer to it as PNODE in the input. An example will illustrate the procedure. The branches of the feedback system shown in Figure 25 are described as indicated below.

![Unity Feedback System](image)

Figure 25. Unity Feedback System
TRANSFER FUNCTIONS
BRANCHES
1-2(1.0,0)
2-3(3.1, 1.00/2.3, 1.2,2, 1.1)
3-2(-1.0,0)

Note: All constant coefficients must include a decimal point as shown above.

Reference to any node is made by adding a P to it. For example, to obtain the output at nodes 2 and 3 the user must refer to these points as P2 and P3 under outputs. A more complete input description of Figure 22 will clarify. As shown below, the input to the system is defined as P1 and described as Table T1.

TRANSFER FUNCTIONS
BRANCHES
1-2(1.0,0)
2-3(3.1, 1.00/2.3, 1.2,2, 1.1)
3-2(-1.0,0)

DEFINED PARAMETERS

Input at
Node 1

P1=TI

FUNCTIONS
TI=0.0, 0.1, 10.1

OUTPUTS
P1,P3,PLOT

RUN CONTROLS
STOP TIME=10

INTEGRATION ROUTINE=IMPLICIT

END

The integer numbers between commas denote the power of S associated with the individual coefficient.

The coefficients can be made up of literal and numerical values.

Several sample branch transmittances will better illustrate the required input:
The branch descriptions for the flowgraph shown in Figure 23 are given below:

**GRAPH DESCRIPTION**

**BRANCHES**

A-B (1., 0/1, 1)
B-C (1., 1/PK1, 2, PTAU, 1, 1, 1)
C-D (PK2, 0)
C-B (-PK3, 0)
D-B (-PK4, 0/1, 1)
SECTION IV
DIFFERENTIAL EQUATION INPUT LANGUAGE

Differential equations are a very general form of system definition and all the systems seen so far can be described in terms of these. NELSIM accepts as input sets of n\textsuperscript{th} order differential linear or nonlinear differential equations of the form given below.

\[ \begin{bmatrix}
a_{11} & a_{12} & \cdots & a_{1m} \\
a_{21} & a_{22} & \cdots & a_{2m} \\
\vdots & \vdots & \ddots & \vdots \\
a_{m1} & a_{m2} & \cdots & a_{mm}
\end{bmatrix}
\begin{bmatrix}
d^n x_1 \\
d^n x_2 \\
\vdots \\
d^n x_m
\end{bmatrix}
+ \begin{bmatrix}
b_{11} & b_{12} & \cdots & b_{1m} \\
b_{21} & b_{22} & \cdots & b_{2m} \\
\vdots & \vdots & \ddots & \vdots \\
b_{m1} & b_{m2} & \cdots & b_{mm}
\end{bmatrix}
\begin{bmatrix}
d^{n-1} x_1 \\
d^{n-1} x_2 \\
\vdots \\
d^{n-1} x_m
\end{bmatrix}
= \begin{bmatrix}
c_{11} & c_{12} & \cdots & c_{1m} \\
c_{21} & c_{22} & \cdots & c_{2m} \\
\vdots & \vdots & \ddots & \vdots \\
c_{m1} & c_{m2} & \cdots & c_{mm}
\end{bmatrix}
\begin{bmatrix}
(x_1)^i \\
(x_2)^j \\
\vdots \\
(x_m)^k
\end{bmatrix}
+ \begin{bmatrix}
d_1 \\
d_2 \\
\vdots \\
d_m
\end{bmatrix}
= \begin{bmatrix}
F_1 \\
F_2 \\
\vdots \\
F_m
\end{bmatrix}
\] (1)

The above equations are a general set of m nonlinear differential equations in m unknowns, \(x_1\) through \(x_m\) and with forcing functions \(F_1\) through \(F_m\). For convenience, the equations are represented in matrix form, but will be
input into NELSIM individually. The term \( \left( \frac{d^n x_1}{dt^n} \right)^i \) is the nth derivative of the variable \( x_1 \) raised to the \( i^{th} \) power where \( i \) can vary from 1 to \( i \) and is not necessarily the same for all derivative orders. For the systems considered in Section II, the highest order of derivative \( n \) generally encountered is two. The coefficients \( a_{11}, b_{11}, \) etc. may be time varying or nonlinear. It will be possible to enter the coefficients into NELSIM as constants, defined parameters, or any other type documented in section.

NELSIM automatically takes equations and separates them into first order differential equations in a format directly compatible with SCEPTRE. It should be realized that to determine the transient response of the system, it will be necessary for SCEPTRE to integrate a number of equations equal to the total number of derivatives - up to \( n \) derivatives for each unknown for a maximum of \( mn \) equations to integrate. The maximum number of first order differential equations currently allowed in SCEPTRE is one hundred, and NELSIM will warn the user if over one hundred equations are generated. If the SCEPTRE limit is increased, NELSIM will be easily modified to accommodate the increase.

VARIABLE PARAMETER NAMES

All names entered in the descriptions must be entered as defined parameter names. For example velocity \( V_1 \) in an equations should be expressed as \( PV_1 \). The value of these variables are then defined under the DEFINED PARAMETERS subheading.

SPECIFICATION OF DERIVATIVE ORDER

The order of a derivative is specified by a \( D \) followed by an integer number indicating the derivative order. For example, \( \frac{d^2V_2}{dt^2} \) is defined as
D2PV2 where PV2 is the defined parameter name given to V2 and D2 denotes the second order derivative of V2.

As an example of the differential equation input in NELSIM, consider the equations below which represent the two second order differential equations

\[ K_1 (V_2 - V_1) + M_2 \ddot{V}_2 + B (\dddot{V}_2 - \dddot{V}_3) + K_2 (V_2 - V_3) = 0 \]
\[ B (\dddot{V}_3 - \dddot{V}_2) + K_2 (V_3 - V_2) + M_3 \ddot{V}_3 + K_3 V_3 = 0 \]

resulting from the mechanical system shown in Figure 10.

The NELSIM input for differential equations (3) and (4) is shown in Figure 26.

**DIFFERENTIAL EQUATIONS**

*UNITS=ENGLISH (MECHANICAL)*

\[ K_1 \times (V_2 - V_1) + M_2 \times D2V2 + B \times (D1V2 - D1V3) + K_2 \times (V_2 - V_3) = 0 \]
\[ B \times (D1V3 - D1V2) + K_2 \times (V_3 - V_2) + M_3 \times (D2V3) + K_3 \times V_3 = 0 \]

*DEFINED PARAMETERS*

- \( K_1 = 1 \)
- \( K_2 = 2 \)
- \( M_3 = 3 \)
- \( B = 1.0 \)
- \( V_1 = X1(\cos(2*\text{TIME})) \)

*OUTPUTS*

- \( V_2, V_3, \text{PLOT} \)

*RUN CONTROLS*

- REQUEST TO OBTAIN DECK OF INPUT CARDS READY FOR SCEPTRE INPUT

\[ \text{END} \]

*Figure 26. NELSIM Differential Equations Input*
The symbols $D_1$ and $D_2$ preceding a variable refer to the first or second

time derivatives of that variable and the defined parameters express the

variables involved.

**INPUT RESTRICTIONS**

To accommodate the SCEPTRE input language, several restrictions are

placed on the input of differential equations and are listed below:

1. The highest order term must be
   a) Uncoupled
   b) Not exceed an order of 9

2. Derivative variables cannot exceed 4 characters
   (6 including the derivative definition), e.g.,
   
   $D_2PV2$
   $D_1PX14$

3. The highest order derivative must appear only once within
   the equation, and be of one of the following forms only:
   
   $\pm (expression) \times \text{derivative}$
   $\pm expression \times \text{derivative}$
SECTION V

COMBINED SYSTEM INPUTS

A complete system is usually made up of a number of subsystems not necessarily each being of the same type. NELSIM accepts as input a combination of systems as well as simple systems as seen in the previous sections. A valid combined system entry of the problem into NELSIM is

ANALOG DESCRIPTION

THERMAL
0
0
0
0

MECHANICAL
0
0
0
0

ELECTRO OPTICAL
0
0
0
0

THERMAL
0
0
0
0

MECHANICAL
SECTION VI
NELSIM SAMPLE PROBLEMS

The following sample problems have been formulated to illustrate the use of NELSIM with each of the four disciplines considered - mechanical, thermal, electro-mechanical, and electro-optical.

6.1 MECHANICAL SYSTEM EXAMPLES

Problem 1 - The problem depicted in Figure 27 can be represented as shown in Figure 28 which carries a NELSIM input as shown below.

**Figure 27. Sample Mechanical Problem 1**

**Figure 28. Sample NELSIM Input for Problem 1**

```
ANALOG DESCRIPTION
MECHANICAL ELEMENTS
V1,C=3=G1(TIME)
K3,G=3
M3,1-G=.3
K2,1-2=2
B1,1-2=1
M2,2-G=.2
K1,2-3=1
FUNCTIONS
G1(T)=(COS(2.*T))
OUTPUTS
VM2(V2),VM3(V3),PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=10
END
```

K₁ = 1
K₂ = 2
K₃ = 3
M₂ = .2
M₃ = .3
B = 1
V₁ = cos 2t
Figure 28. Sample Mechanical Problem 1

Representation to NELSIM

The output from NELSIM will be:

CIRCUIT DESCRIPTION
FUNCTIONS
GDIV(A) = (1./A)
Q1(T) = (COS(2.*T))

ELEMENTS
E1   ,G       -3     =Q1(TIME)
L3    ,G       -1     = 3.3333E-01
C3    ,C       -6     = 3.0000E-01
L2    ,1       -2     = 5.0000E-01
R1    ,1       -2     = 1.0000E+00
C2    ,2       -6     = 2.0000E-01
L1    ,2       -3     = 1.0000E+00

OUTPUTS
V2(V2),PLCT
V3(V3),PLCT

RUN CONTROLS
STOP TIME     = 1.0000E+01
INTEGRATIONROUTINE=IMPLICIT
END

77
This output can be represented by the circuitry as shown in Figure 29.

Figure 29. Equivalent Electric Circuit for Mechanical System Problem 1

Problem 2 - The problem depicted in Figure 30.

Figure 30. Sample Mechanical Problem 2
Can be represented to NELSIM as:

```
ANALOG DESCRIPTION
MECHANICAL
ELEMENTS
W1,C-1=1
K1,1-2=1
J2,2-C=1
K2,2-3=1
J3,3-G=1
G3,.J3-G=1
B2,.J3-G=1
OUTPUTS
WJ2,.WB2,PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=1
END
```

The output from NELSIM will be

```
CIRCUIT DESCRIPTION
FUNCTIONS
QDIV(A)=(1./A)
ELEMENTS
E1 ,G -1 = 1.00000E+00
L1 ,1 -2 = 1.00000E+00
C2 ,2 -G = 1.00000E+00
L2 ,2 -3 = 1.00000E+00
C3 ,3 -G = 1.00000E+00
R3 ,3 -G = 1.00000E+00
R2 ,2 -G = 1.00000E+00
OUTPUTS
VC2,PLOT
VR2,PLOT
RUN CONTROLS
STOP TIME = 1.000E+00
INTEGRATION ROUTINE=IMPLICIT
END
```
6.2 THERMAL SYSTEM EXAMPLES

Problem 1

(a) Rocket-engine walls

(b) System Model Showing

Figure 31. Thermal System Problem 1
The input of the problem requires the various subdivisions within the wall to be indicated by nodes (1-3). The thermal resistance between subdivisions is simulated using resistors and thermal capacitance using capacitors. The input is shown below.

```
ANALOG DESCRIPTION
THERMAL
ELEMENTS
TIN,G-1=T1
R1,1-2=1
C1,2-6=1
R2,2-3=1
C2,3-6=1
R3,3-4=1
TCUT,G-4=1
FUNCTIONS
T1=0,1,1,2,10,5,10,6,1,10,1
OUTPUTS
TIN,OC1,OC2,OR3,PLCT
TR3,TC1,PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME =15
RUN INITIAL CONDITIONS
END
```

The elements have all been entered as constant values for simplicity but in general will be nonlinear functions of the materials involved and depend on assumptions made by the user. All the nonlinear entry capabilities allowed in SCEPTRE apply to the NELSIM modules. The output of NELSIM is shown below with the elements and output requests altered to electrical analogies.
CIRCUIT DESCRIPTION

FUNCTIONS
QDIV(A)=(1./A)
T1=0,1,1,1,2,10,5,10,6,1,10,1

ELEME NTS
<table>
<thead>
<tr>
<th>Ein</th>
<th>G</th>
<th>-1</th>
<th>=T1</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>1</td>
<td>-2</td>
<td>= 1.00000E+00</td>
</tr>
<tr>
<td>C1</td>
<td>2</td>
<td>-6</td>
<td>= 1.00000E+00</td>
</tr>
<tr>
<td>R2</td>
<td>2</td>
<td>-6</td>
<td>= 1.00000E+00</td>
</tr>
<tr>
<td>C2</td>
<td>3</td>
<td>-6</td>
<td>= 1.00000E+00</td>
</tr>
<tr>
<td>R3</td>
<td>3</td>
<td>-4</td>
<td>= 1.00000E+00</td>
</tr>
<tr>
<td>EOUT</td>
<td>3</td>
<td>-4</td>
<td>= 1.00000E+00</td>
</tr>
</tbody>
</table>

OUTPUTS
Ein, PLOT
IC1, PLOT
IC2, PLOT
IR3, PLOT
VR3, PLOT
VC1, PLOT

RUN CONTROLS
STOP TIME = 1.500E+01
INTEGRATION ROUTINE = IMPLICIT
RUN INITIAL CONDITIONS
END
Problem 2 - For the rocket motor shown in Figure 32, heat is transferred by convection and radiation to the chamber wall, then through the wall by conduction, and finally to the coolant by convection.

Figure 32. Thermal System Problem 2

This problem is described to NELSIM as follows:

```
ANALOG DESCRIPTION
THERMAL
ELEMENTS
TGAS,G-1=T1
R1R,1-2=1
R1C,1-2=1
R2K,2-3=1
C2,3-G=1
R3C,3-4=1
TCOLL,G-4=1
FUNCTIONS
T1=0,1,1,1,2,10,5,10,6,1,10,1
OUTPUT
TGAS,TCOLL,PLDT
TR2K,PLDT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=10
END
```

The produced NELSIM output for this case will be:
CIRCUIT DESCRIPTION

FUNCTIONS
CDIV(A)=(1./A)
T1=0,1,1,1,2,10,5,10,6,1,10,1

ELEMENTS
EGAS , C -1 = T1
R1K , 1 -2 = 1.0E+00
R1C , 1 -2 = 1.0E+00
R2K , 2 -3 = 1.0E+00
C2 , 3 -4 = 1.0E+00
R3C , 3 -4 = 1.0E+00
ECOOL , G -4 = 1.0E+00

OUTPUTS
EGAS,PLOT
ECOOQ, PLOT
VR2K, PLOT
RUN CONTROLS
STOP TIME = 1.0E+01
INTEGRATION ROUTINE=IMPLICIT

END
6.3 ELECTRO-MECHANICAL EXAMPLES

Problem 1 - For the galvanometer shown in Figure 33.

Figure 33. Electro-Mechanical Problem 1

Figure 34 represents the equivalent lumped network in terms of its electrical and mechanical parts.

Figure 34. Lumped Element Galvanometer Equivalent
where \( J \) and \( B \) represent the moment of inertia of the rotor and the viscous damping that results from air friction. The element \( K_R \) represents the rotational stiffness produced by a spring attached to the rotor. The constant \( D \) is defined to be \( \beta \alpha \) where \( \beta \) is the magnetic flux density, \( \alpha \) is the total length of the conductor and \( \alpha \) is the radius of the rotor.

The input language where all the elements are normalized to one is shown below.

```plaintext
ANALOG DESCRIPTION
ELECTRO MECHANICAL
ELEMENTS(ELECTRICAL)
E1,G-1=1
R1,1-2=1
EC,G-2=EC(PD,WJR)
ELEMENTS(MECHANICAL)
T1,G-3=EC(PD,IR1)
JR,3-G=1
BR,3-G=1
KR,3-G=1
DEFINED PARAMETERS
PD=OPD(PA,PL,PB)
PA=1
PB=1
PC=1
PL=1
FUNCTIONS
GEC(A,B)=(A*B)
OPD(A,B,C)=(A*B*C)
OUTPUTS
WRK(WKR),TRK(TKR),VR1,PLOT
RUN CONTROLS
STOP TIME=10
INTEGRATION ROUTINE=IMPLICIT
END
```

The two dependent sources EC and T1 provide the interface between the two systems and are entered directly in terms of the elements involved. The output of NELSIM is shown below with the electrical analog represented shown in Figure 35. As can be seen, the network is entirely in terms of electrical quantities.
CIRCUIT DESCRIPTION

FUNCTIONS
GDIV(A)=(1./A)
GEC(A,B)=(A*B)
OPD(A,B,C)=(A-B-C)

ELEMENTS
J1 = 3    -3    =GEC(PD,IR1)
CR = 3    -6
RR = 3    -6
LR = 3    -6
EC = 6    -1
R1 = 1    -2

DEFINED PARAMETERS
PD =OPD(PA,PL,PD)
PA =1.00000E+00
PB =1.00000E+00
PC =1.00000E+00
PL =1.00000E+00

OUTPUTS
VLR(NKR),PLOT
ILR(TKR),PLOT
VRI,PLOT
RUN CONTROLS
STOP TIME = 1.000E+01
INTEGRATION ROUTINE=IMPLICIT

END

Figure 35. Galvanometer Electrical Analog
Problem 2 - Implementation of the accelerometer model built-in to the electro-mechanical system is accomplished below. The usage and response of the model is illustrated for the case where all gains have been normalized to 1 and the input to the model is a unit step. Consider Figure below where H is the accelerometer.

The input to NELSIM is given below:

```
ANALOG DESCRIPTION
ELECTRO MECHANICAL
MODELS
T1,IN-OUT=ACCELEROMETER
DEFINED PARAMETERS
PA1=1
PET1=1
PCT1=1
PDT1=1
PET1=1
PFT1=1
PCT1=1
PINT1=11
FUNCTIONS
T1=0,0,0,1,10,1
OUTPUTS
PINT1,PAT1,PA2T1,PA3T1,PA4T1,PLOT
PAT1,POUT1,PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=10
END
```

All gains within the model are provided by the user with the model label (T1) added to each name.
The output generated by the program is shown below.

CIRCUIT DESCRIPTION

FUNCTIONS
ODIV(A)=(1./A)
T1=0,0,1,10,1
OMA1(A,B,C)=(A*B-C)
OMA2(A,B,C,D)=((A*B-C)/D)
OMA3(A,B)=(A*B)
OMA4(A,B,C)={(A-B)/C)
OMA5(A,B,C,D)=(A*{(B-C)/D))
OMA6(A,B)=(A/B)

DEFINED PARAMETERS
PA11 = 1.00000E+00
PCT1 = 1.00000E+00
PCT1 = 1.00000E+00
PDT1 = 1.00000E+00
PET1 = 1.00000E+00
PFT1 = 1.00000E+00
PG11 = 1.00000E+00
PINT1 =T1
PA1T1=OMA1(PINT1,PA11,PA4T1)
DP2T1=PA7T1
DP2T1=OMA2(PA1T1,PET1,PA7T1,PCT1)
PA3T1=OMA3(PA2T1,PCT1)
DP3T1=OMA4(PA3T1,PA6T1,PFT1)
PA4T1=OMA5(PET1,PA3T1,PA6T1,PFT1)
DP4T1=OMA6(PA4T1,PCT1)
DP5T1=PA5T1
PA2T1=0
PA5T1=0
PA6T1=0
PA7T1=0
POUT1=0

OUTPUTS
PINT1,PLOT
PA11,PLOT
PA2T1,PLOT
PA3T1,PLOT
PA4T1,PLOT
PA5T1,PLOT
PLOT1,PLOT

RUN CONTROLS
STOP TIME = 1.000E+01
INTEGRATOR ROUTINE=IMPLICIT

END
6.4 ELECTRO-OPTICAL SYSTEM EXAMPLES

Figure 36 details the equivalent circuit selected to simulate the AC characteristics of photo diodes.

![Diagram of equivalent circuit](image)

Figure 36. Equivalent Circuit of a Photo Diode

As detailed in Volume I, the photocurrent, $I_{PH}$ is expressed as

$$I_{PH} = (\eta q P/hV)$$

Problem 1

The normalized power input at 5 m to an $I_{NSD}$ device is described as

<table>
<thead>
<tr>
<th>POWER</th>
<th>TIME (SEC)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>.2</td>
<td>2</td>
</tr>
<tr>
<td>.4</td>
<td>6</td>
</tr>
<tr>
<td>.85</td>
<td>10</td>
</tr>
<tr>
<td>.6</td>
<td>1</td>
</tr>
<tr>
<td>0</td>
<td>15</td>
</tr>
</tbody>
</table>
Using

\[ q = 25\% \]
\[ R_s = 18 \Omega \]
\[ C_i = 7.1 \text{ pf} \]
\[ R_i = 6 \Omega \]
\[ R_{\text{LOAD}} = 12 \Omega \]

Plot the current time history at the load and at the source.

The NELSIM input is

```
ANALOG DESCRIPTION
ELECTRO OPTICAL
ELEMENTS(ELECTRICAL)
JPD, G-1=CEO(PEFF, PCHG, PCON, POFR, TPL)
R1, 2-G=6
C1, 3-G=3
RS, 3-4=12
RL, 4-G=12
FUNCTIONS
TPL=0, 0.2, 2, 4, 6, 10, 12, 0, 15
CEO(A, B, C, D, E)=(A*B/(C*D)*E)
DEFINED PARAMETERS
PEFF=.25
PCHG=1E-7
PCON=123E-4
POFR=37
OUTPUTS
JPD, JRL, PLOT
RUN CONTROLS
INTEGRATION ROUTINE=IMPLICIT
STOP TIME=15
END
```

For which the NELSIM output is
CIRCUIT DESCRIPTION

FUNCTIONS

\[ \text{CDIV}(A) = (1/A) \]

TPL = 0, 0, 2, 2, 4, 6, 8, 5, 10, 6, 12, 0, 15

\[ \text{QEO}(A, B, C, D, E) = (A * B / (C * D) * E) \]

ELEMENTS

<table>
<thead>
<tr>
<th>JPD</th>
<th>RI</th>
<th>CI</th>
<th>RS</th>
<th>RL</th>
</tr>
</thead>
<tbody>
<tr>
<td>(G)</td>
<td>(a)</td>
<td>(b)</td>
<td>(c)</td>
<td>(d)</td>
</tr>
</tbody>
</table>

\[ = \text{QEO} (\text{PEFF}, \text{PCHG}, \text{PCON}, \text{PQFR}, \text{TFL}) \]

\[ R_L = 2.00000 \times 10^3 \]

\[ R_S = 1.20000 \times 10^3 \]

\[ C_1 = 3 \times 10^{-3} \]

\[ R_1 = 6 \times 10^{-3} \]

DEFINED PARAMETERS

<table>
<thead>
<tr>
<th>PEFF</th>
<th>PCHG</th>
<th>PCON</th>
<th>PQFR</th>
</tr>
</thead>
<tbody>
<tr>
<td>(2.50000 \times 10^{-1})</td>
<td>(1.60000 \times 10^{-7})</td>
<td>(1.23000 \times 10^{-2})</td>
<td>(3.70000 \times 10^{+1})</td>
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OUTPUTS

| JPD, PLOT | JRL, PLOT |

RUN CONTROLS

<table>
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<tr>
<th>STOP TIME</th>
<th>INTEGRATION ROUTINE</th>
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<td>(1.50000 \times 10^1)</td>
<td>IMPLICIT</td>
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END

Problem 2

Rerun Problem 1 using an \(I_{NS}\) device whose characteristics are

\[ q = 25\% \]

\[ R_S = 12 \Omega \]

\[ C_1 = 3 \text{ pf} \]

\[ R_1 = 6 \Omega \]

For the same load and compare results.

The NELSIM input and output are
ANALOG DESCRIPTION
ELECTRO OPTICAL
ELEMENTS(ELECTRICAL)
JPD, G-1 = QEO(PEFF, PCHG, PCON, POFR, TPL)
R1, 2-G = 6
C1, 3-G = 7.1
RS, 3-4 = 18
RL, 4-G = 12

FUNCTIONS
TPL = 0, 0, 2, 2, 4, 4, 6, 8, 10, 12, 0, 15
QEO(A, B, C, D, E) = (A*B/(C*D)*E)

DEFINED PARAMETERS
PEFF = .25
PCHG = 1E-7
PCON = 123E-4
POFR = 37

OUTPUTS
JPD, JRL, PLOT

RUN CONTROLS
INTEGRATION ROUTINE = IMPLICIT
STOP TIME = 15

END

CIRCUIT DESCRIPTION
FUNCTIONS
QDIV(A) = (1/A)
TPL = 0, 0, 2, 2, 4, 4, 6, 8, 10, 12, 0, 15
QEO(A, B, C, D, E) = (A*B/(C*D)*E)

ELEMENTS
JPD , G -1 = QEO(PEFF, PCHG, PCON, POFR, TPL)
R1 , 2-G = 6
C1 , 3-G = 7.1
RS , 3-4 = 18
RL , 4-G = 12

DEFINED PARAMETERS
PEFF = 2.50000E-01
PCHG = 1.00000E-07
PCON = 1.23000E-02
POFR = 3.70000E+01

OUTPUTS
JPD, PLOT
JRL, PLOT

RUN CONTROLS
STOP TIME = 1.500E+01
INTEGRATION ROUTINE = IMPLICIT
END
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