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TWO-DIMENSIONAL TRANSONIC WIND TUNNEL TESTS
OF THREE 15-PERCENT THICK CIRCULATION
CONTROL AIRFOILS

by

Robert J. Englar

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WASHINGTON D.C. 20360

AVIATION DEPARTMENT

Technical Note AI-132
TWO-DIMENSIONAL TRANSONIC WIND TUNNEL TESTS
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CONTROL AIRFOILS

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December 1970
Technical Note AL-182
SUMMARY

Two-dimensional transonic wind tunnel tests were conducted on three fifteen percent circulation control elliptic airfoils over the range 0.3 \( \leq M_w \leq 0.9 \). Model configurations included a pure elliptical shape with both jet flap and tangential upper surface trailing edge blowing, plus tangential blowing over an elliptical shape with a rounded trailing edge. Performance of the rounded trailing edge configuration was the best of the three at low speeds, but above \( M_w = 0.55 \), detachment of the Coanda jet caused rapid performance deterioration. Due to its elongated trailing edge and associated larger effective radius downstream of the slot, the tangentially blown pure ellipse was able to extend the jet detachment Mach number to 0.7, where maximum equivalent lift-to-drag ratios of 22 at \( C_L \) of 0.44 were achieved. The jet flap proved to be inferior to the tangentially blown configurations in all respects except in its ability as a thrusting, drag-reducing body.
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LIST OF SYMBOLS

\[ A_e \] slot area, (bh), ft²

\[ a_j \] local speed of sound in the jet, ft/sec

\[ A_j \] nozzle throat area, ft²

\[ b \] model span, ft

\[ c \] model chord, ft

\[ C_d \] two-dimensional drag coefficient from momentum loss in wake, corrected for additional mass efflux of the jet

\[ C_{d_{e_1}} \] force-based equivalent drag coefficient, \( C_d + C_{\mu} + C_{\rho} \frac{V_m}{V_j} \)

\[ C_{d_{e_2}} \] kinetic-energy-based equivalent drag coefficient, \( C_d + \frac{C_{\rho}}{2V_m} + C_{\mu} \frac{V_m}{V_j} \)

\[ C_l \] two-dimensional lift coefficient

\[ C_{m_{so}} \] pitching moment coefficient about the half chord

\[ C_p \] pressure coefficient

\[ C_p^* \] critical pressure coefficient (corresponding to local \( M \) of 1.0)

\[ C_{\mu} \] momentum coefficient, \( \Delta V_j/(q_{\infty}) \)

\[ h \] slot height at nozzle throat, ft

\[ l/d_{e_1} \] force-based equivalent lift-to-drag ratio

\[ l/d_{e_2} \] kinetic-energy based equivalent lift-to-drag ratio

\[ M_{crit} \] critical Mach number

\[ M_{\infty} \] freestream Mach number

\[ M_j \] jet Mach number

\[ \dot{m} \] mass efflux, slug/sec

\[ P_m \] free stream static pressure, lb/ft²

\[ P_{t_{m}} \] free stream total pressure, lb/ft²

\[ P_{t_d} \] duct (plenum) pressure, lb/ft²
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<tr>
<td>$q_m$</td>
<td>free stream dynamic pressure, lb/ft.$^2$</td>
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<tr>
<td>$r$</td>
<td>trailing edge radius, ft</td>
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<tr>
<td>$Re$</td>
<td>Reynolds number, based on chord</td>
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<tr>
<td>$T_t$</td>
<td>total temperature, °R</td>
</tr>
<tr>
<td>$T_j$</td>
<td>static temperature in the jet, °R</td>
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<tr>
<td>$V_m$</td>
<td>free stream velocity, ft/sec</td>
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<tr>
<td>$V_j$</td>
<td>jet velocity, ft/sec</td>
</tr>
<tr>
<td>$x/c$</td>
<td>dimensionless chordwise station</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>geometric angle of attack, degrees</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>ratio of specific heats</td>
</tr>
<tr>
<td>$\theta$</td>
<td>local angle of jet at exit relative to free stream</td>
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<tr>
<td>$\delta$</td>
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INTRODUCTION

Modified elliptic circulation control airfoil sections have been shown subsonically to be very effective generators of high lift coefficients and aerodynamic efficiencies (References 1 and 2). Employing camber and tangential blowing over a rounded trailing edge, these sections have generated lift coefficients greater than 6.0 and efficiencies (equivalent lift-to-drag ratios) above 90 (at $C_L \approx 1.0$). These airfoils thus appear quite promising for application to inboard and mid-span blade sections of rotary wing aircraft. However, due to their camber and relatively large thickness-to-chord ratio (20 to 30 percent or greater), their effectiveness at the high speed rotor tip would tend to be reduced.

Examination of the rotor tip flow regime indicates that present high speed helicopter configurations are limited by three main problem areas: compressibility or Mach number effects, retreating blade stall, and blade structural limitations. These criteria lead to the demand for a tip section designed to (1) increase the drag divergent Mach number, (2) maintain good transonic lift coefficient and equivalent lift-to-drag ratio, and (3) control the shock location and closely related boundary layer separation. In addition, the section must still maintain relatively good subsonic characteristics as the retreating blade would be required to operate in the low speed (or even reverse flow) region. It is this requirement to cyclically operate in alternately subsonic and transonic regions which leads to the mechanical and structural complexities of present day rotor systems. It is felt that these problems may be considerably reduced or eliminated by proper design of a circulation control transonic tip section where the necessary cyclic variations are obtained by programmed air ejection over the trailing edge.

The present tests were intended to investigate the transonic properties of a series of relatively thin (15 percent) elliptic sections with several variations in blowing schemes. In particular, it was desired to determine if the impressive subsonic efficiencies of the tangentially blown ellipse could be maintained at high subsonic and transonic speeds, while simultaneously satisfying the requirements mentioned above for a high speed tip section. Previous tests on transonic circulation control airfoils (Reference 3)
with Coanda effect tangential blowing over rounded trailing edges have shown loss of lift augmentation and section efficiency above a Mach number of 0.55 due to detachment of the jet sheet. Therefore, an important aspect of the present tests was to determine if the Mach number for jet detachment could be increased by variation in trailing edge curvature.

MODELS AND TEST APPARATUS

The series of three models used in the two-dimensional transonic test program was constructed in a manner similar to previous subsonic ellipses tested at NSRDC (see References 1 and 2). However, certain additional steps were taken to strengthen the models to withstand the higher transonic loads and to provide a fine surface finish to prevent misrepresentation of boundary layer separation and shock wave formation.

MODELS

The basic configuration for all three models was an uncambered ellipse of 15 percent thickness-to-chord ratio chosen from the critical Mach number \( M_{\text{crit}} \) consideration shown in Figure 1, which is based on a Karmann-Tsien rule extension of potential flow data. It was expected that the required rotor tip lift coefficient would lie in the region \( 0 \leq C_{L} \leq 1.0 \); thus the best compromise for increased \( M_{\text{crit}} \) was the 15 percent ellipse. In contrast, the thicker 20 percent ellipse would probably not perform as well in the higher Mach number range where viscous and compressibility effects are strong, while the 10 percent section would fare poorly in the subsonic retreating blade regime.

In addition to the pure 15 percent ellipse, a trailing edge more favorable to subsonic circulation control was chosen, i.e., a circular trailing edge with a radius equal to 4 percent of the chord. As shown in Figure 2, at the higher \( C_{L} \) generated subsonically by this rounded trailing edge, suction peaks (minimum \( C_{p} \)) less than for the pure ellipse were present, while the reverse was true at \( C_{L} < 1.0 \). These higher peaks at the expected transonic lift coefficients would reduce the critical Mach number of the section. This airfoil was included primarily to investigate the high speed jet detachment phenomenon, and as a representative low speed profile for
comparison. A third model employing a jet flap was included for comparison purposes with the tangentially blown configurations.

Figure 3 depicts the geometries of the three two-dimensional models. The pure ellipse and the jet flap were unmodified 15 percent thick ellipse sections sharing a common leading edge with interchangeable trailing edge. Both had an 8 inch chord. The tangentially blown pure 15 percent ellipse (hereafter referred to as the "pure ellipse") had an upper surface tangential slot at 92.4 percent chord from the leading edge, while the jet flap had a lower surface slot aligned 30° to the chord and at the 98.3 percent station. The third trailing edge (to be referred to as the rounded ellipse) had a 0.31 inch radius trailing edge in place of the pure elliptic radius (\(r = 0.09\) inch), thus producing a shorter chord of 7.70 inches, an actual thickness of 15.6 percent and a slot location at the 96 percent station. All three models were of 0.25 inch thick fiberglass with a 600 fineness finish. Structural strength as well as trailing edge attachment were provided by a rectangular steel spar, which also served as the forward wall of the blowing plenum chamber in the trailing edge. The slot on the two tangentially blown sections was formed by a steel blade held in place by a series of jack screws which were also used to adjust the slot height. In all three configurations, the plenum exit was carefully designed so that the slot exit was the minimum area throat of a smoothly converging nozzle.

TEST APPARATUS AND TECHNIQUE

The intended two-dimension tests required that a small transonic tunnel be found with air supply for blowing and some means of blockage control for the relatively thick high speed models. A survey of available tunnels (Reference 4) yielded the 12 x 16 inch induction tunnel at the University of Minnesota’s Aero Hypersonic Laboratory (previously Rosemount Aeronautical Laboratories). This facility had the advantages of suction on the slotted floor and ceiling to reduce or eliminate blockage, as well as a high pressure air supply (outlet pressures of 1500 psig). In addition, a preceding blown airfoil test conducted in that tunnel by Honeywell Inc., (Reference 3), made available to NERDC a complete blowing system hookup compatible with the present models, plus a concentric ring
strain gage wall balance with minimized effect due to pressure line connections. The tunnel and wall balance are presented in Figures 4 and 5, obtained from Reference 3. This reference also contains very detailed information on the facility, test setup, and a transonic test technique similar to that employed in the present test.

The difficulty in evaluating several tares (wall boundary layer, wall deflection, wall-airfoil interaction and air supply pressure hose influence) for correction of balance data made balance drag data almost meaningless and had a lesser but still noticeable effect on lift. An alternative means was thus used as the primary data source for lift, drag, and moment. All three models were pressure tapped at the center span (as shown in Figure 3) to obtain lift and pitching moment by numerical integration around the airfoil section. Spanwise pressure taps were employed to confirm two-dimensionality of the flow. A total head $\frac{1}{2}$ tube rake was installed approximately 1.5 chord lengths downstream of the model. Drag was calculated by integration of momentum loss in the wake using a Lock-Goldstein compressible technique (References 5 and 6), corrected for the additional mass efflux of the jet as in Reference 2. All pressure data from the model and rake were recorded on a multiple scannivalve readout system with output on tape for computerized data reduction. It should be noted that the integrated drag data already includes the horizontal thrust component of the jet as detected by the wake rake. However, integration of the normal force to obtain lift does not include the vertical component $C_{\mu} \sin \theta$. This term is difficult to evaluate since $\theta$ (the jet angle relative to the freestream direction) is unknown for the curved jet. The largest contribution of this thrust term in percentage of total lift would occur for the case of the jet flap model.

A nominal slot height of 0.010 inch was employed on each of the three trailing edges. The range of duct (plenum) total pressures and associated jet velocities required to produce desired momentum blowing coefficients ($C_{p}$) based on an isentropic expansion to free stream static pressure is depicted in Figures 6 and 7. These related figures are for a 0.01 slot height and 12 inch span (the remainder of the 15 inch model span extending through the balance side plates and attaching to the external air supply lines).
Ideal jet velocity \( V_j \) and mass flow rate \( \dot{m} \) were calculated based on an isentropic expansion from duct total pressure to free stream static pressure (which varied with Mach number since the tunnel stagnation pressure remained constant at atmospheric):

\[
V_j = a_j H_j = \sqrt{RT} j H_j = \left\{ \frac{2}{2RT} \left( \frac{\gamma}{\gamma-1} \right) \left[ 1 - \left( \frac{P_{\infty}}{P_t} \right)^{\frac{\gamma-1}{\gamma}} \right]^{\frac{1}{2}} \right\}
\]

Choked nozzle: \( \dot{m} = A_j P_{d} \sqrt{\frac{\gamma}{RT}} \left( \frac{2}{\gamma+1} \right) \frac{\gamma+1}{2(\gamma-1)} \)

Unchoked nozzle: \( \dot{m} = A_j P_{d} \left\{ \frac{2\gamma}{(\gamma-1)RT} \left[ \left( \frac{P_{\infty}}{P_{d}} \right)^{\frac{2}{\gamma}} \left( \frac{P_{\infty}}{P_{d}} \right)^{\frac{\gamma+1}{\gamma}} \right]^{\frac{1}{2}} \right\} \)

and \( C_\mu = \frac{\dot{m}V}{q_{in}c} \)

The actual test values varied from the above in that the trailing edge slot deflected under high plenum pressures and nozzle losses existed. To account for this, static tests of the model were conducted and the ratio of measured-to-isentropic mass flow was determined as a function of the pressure ratio \( P_{\infty} / P_{d} \). These ratios were then used to calculate the test values of blowing coefficients.

Plenum air supply was obtained through the high pressure Honeywell lines which were sealed into adaptors on the model endplates by O-rings. These prevented leaks while minimizing any resistance the connections would offer to model pitching moment. Total pressure and temperature in the plenum were measured by internal pressure gage and thermocouple. Tunnel free stream static pressure \( (P_{\infty}) \) was measured in the tanks adjacent to the slotted ceiling and floor of the test section, with blockage being reduced or eliminated at higher Mach numbers by proper adjustment of suction out of
these tanks. Test section Mach number and dynamic pressure were determined from the relations

\[
M_a = \left\{ \frac{2}{\gamma - 1} \left[ \left( \frac{P_t}{P_\infty} \right)^{\frac{\gamma - 1}{\gamma}} - 1 \right] \right\}^{\frac{1}{2}}
\]

\[
q_a = \frac{1}{2} \gamma P_\infty M_a^2
\]

where free stream total pressure \( P_t \) was atmospheric.

DESIGN AND TEST CONSIDERATIONS

It was surmised that generation of high equivalent lift-to-drag ratios in the transonic regime could be accomplished if an effective means of drag reduction could be found which did not demand large additional blowing power penalties. The jet flap has been shown (Reference 7) to shift the shock wave location rearward and thus favorably effect shock induced separation and related drag. It also exhibited good thrust recovery. However, the jet angles for desirable drag characteristics were frequently different from those for good lift augmentation. On the other hand, tangential blowing over a rounded trailing edge was superior subsonically to the jet flap in lift augmentation and equivalent lift-to-drag ratio, but began to lose this superiority transonically due to jet detachment. A compromise between these two configurations was needed and the design criteria became one for favorable transonic lift augmentation and drag reduction (including thrust augmentation). It was felt that this could be accomplished with an elongated trailing edge, i.e., a larger radius after the slot but preceding a relatively small trailing edge radius. The pure 15 percent ellipse with slot at 92.4 percent chord met this criteria, even though its shape was probably not the optimum.

Size of the model was chosen from consideration of Reynolds number effect on scaling. Reference 8 indicates that \((1.5 \text{ to } 2) \times 10^6\) was the
minimum Reynolds number to represent transition and shock-boundary layer interaction phenomenon characteristic of full scale. An 8 inch chord provided Reynolds numbers above this limit throughout the Mach number range above 0.35 (see Figure 8). Natural (free) boundary layer transition was allowed since full scale Reynolds number was expected to be of the same order of magnitude as the model values. The range of momentum coefficients used ($0 \leq C_{\mu} \leq 0.08$) was based on an upper limit of 45 psig plenum pressure, above which pressure seals in the model and supply connection had leaked. The range of indicated geometric angle of attack was small, $0^\circ \leq \alpha \leq 2^\circ$ (which was found to be in actuality $-1.2^\circ \leq \alpha \leq 0.8^\circ$) with practically all of the runs being made at $\alpha = -1.2^\circ$ (actual). The discrepancy is indicated and actual geometric $\alpha$ was due to misalignment of the model relative to the angle of attack setting reference.

**DISCUSSION**

**ROUNDED TRAILING EDGE ELLIPSE**

Test were conducted on the 15.6 percent thick rounded trailing edge ($r/c = 0.04$) configuration at $\alpha = -1.2^\circ$. Lift, drag and moment data are presented in Figures 9 through 20. At Mach numbers of 0.5 and lower, lift variation with blowing showed the characteristic subsonic trend, i.e., continual increase with no apparent drop off at higher values of $C_{\mu}$ (Figures 9 and 10). At higher Mach numbers, ($M_\infty > 0.6$) maximum lift coefficient was reached and soon followed by a decrease in $C_{\mu}$ with added blowing. The critical Mach number at which this "$C_{\mu}$ stall" began was approximately 0.55, very close to the same phenomenon found in Reference 3. That related study attributes the lift loss to detachment of the Coanda jet from the rounded trailing edge and immediate decrease in circulation.

Figure 11 and 12 depict the variation of lift coefficient and lift augmentation ($\Delta C_{\mu}/\Delta C_{\mu}$) with jet velocity ratio ($V_j/V_\infty$) and the associated effect of nozzle choking. Although the lift coefficient continued to increase beyond the choked ($M_j = 1.0$ in the nozzle throat) value of $V_j/V_\infty$, the lift augmentation began to drop off rapidly.
Drag showed an even more pronounced variation than lift with increase in blowing and Mach number (Figures 13 and 14). For $M_\infty > 0.4$, an initial decrease in $C_d$ with increased blowing was followed by a rapid rise in drag. Analysis of the associated pressure distributions showed reductions in the trailing edge suction peaks with increase in Mach number in the regime where this drag rise occurred, thus again indicating jet detachment as the cause of deterioration of model performance. At $M_\infty = 0.9$, appearance of upper and lower surface shocks produced a large wave drag contribution to $C_d$. Associated with the jet detachment phenomenon was the progressive loss of drag reduction with increased Mach number. Figure 15 depicts this trend, where the drag reduction factor is indicative of an increase (positive $\Delta C_d / \Delta C_\mu$) or decrease in drag coefficient relative to the unblown value. In addition, increased blowing above the critical Mach number showed little or no effect on the shock location (Figure 16). Associated lift and drag data are presented in the drag polar (Figure 17), while the effect of trailing edge suction peaks due to higher $C_\mu$ on pitching moment at the half chord is shown in Figure 18.

Model performance was best indicated by an equivalent lift-to-drag ratio which included in the drag term a penalty for blowing. This enabled the blown airfoil to be compared in efficiency to an unblown configuration. A simplified equivalent drag coefficient (essentially a force-based coefficient) could be defined as

$$C_{d,e} = C_d + C_\mu + \frac{\Delta V_s}{q_{\infty} c} = C_d + C_\mu + C_\mu \frac{V_\infty}{V_j}$$

where the third term on the right is an intake penalty described in more detail in Reference 2. Using this parameter the rounded trailing edge yielded a maximum $l/d_{eq}$ of 30 at $M_\infty = 0.4$ and $C_\mu = 0.96$ (Figure 19). A more appropriate equivalent $C_d$ was derived for kinetic energy and power required to produce the necessary blowing:

$$K.E. = \frac{1}{2}mV_j^2$$

$$P = \frac{\Delta K.E.}{\Delta t} = \frac{1}{2} \frac{\Delta m V_j^2}{\Delta t} = \frac{1}{2} \Delta m V_j^2$$
Then the total equivalent drag was

\[ d_e = d + \frac{\frac{1}{2} \rho \beta^2 S}{V_\infty} + \frac{\dot{m} \rho \beta}{V_\infty} \]

or in coefficient form

\[ C_d = C_d + \frac{\frac{1}{2} \rho \beta^2}{\frac{1}{2} \rho V_\infty^2} + \frac{\dot{m} \rho \beta}{\dot{m} \rho V_\infty} = C_d + \frac{\frac{1}{2} \rho V_\infty^2}{\frac{1}{2} \rho V_\infty^2} + \frac{\rho V_\infty^2}{\rho V_\infty^2} \]

where \( C_d \) was the momentum drag coefficient as measured by the wake rake.

The latter parameter \((\dot{d} / d_e)\) is preferred for comparison to other airfoils, but requires that the jet velocity be known. This parameter reduced the maximum \( \dot{d} / d_e \) to 25.9 at \( M = 0.4 \), with efficiencies of 15 or less in the Mach number range \( M \geq 0.55 \) (Figure 20).

**PURE ELLIPTICAL TRAILING EDGE.**

The 15 percent thick pure elliptic section with tangential blowing was tested primarily at \( \alpha = -1.2^\circ \) (for comparison to the preceding model) with several additional runs at \( \alpha = 0.8^\circ \). At low Mach number, the Coanda jet was not as effective over this smaller trailing edge radius \((r/c = 0.01125)\), yielding maximum lift coefficients of 0.91 at \( \alpha = -1.2^\circ \) (Figure 21), about half that of the rounded ellipse (Figure 9). However, at \( M = 0.7 \), \( C_\mu \) was twice that obtained by the rounded trailing edge. In addition, the maximum lift peaks occurred at progressively greater Mach number with decrease in \( C_\mu \) (Figure 22); whereas for the rounded ellipse, maximum \( C_\mu \) always occurred at \( M = 0.3 \) (Figure 10). The limited amount of data at \( \alpha = 0.8^\circ \) showed a \( C_\mu \) increase at \( M = 0.7 \) of as much as 36 percent with the 2° angle of attack change. The effects of slot choking on lift and lift augmentation were not as noticeable as for the rounded ellipse. Figures 23 and 24 indicate that both \( C_\mu \) and \( \Delta C_\mu / \Delta \alpha \) continued to rise beyond the choking value of \( V_j / V_\infty \). A maximum lift augmentation of 13 was realised at \( M = 0.7 \) for the pure ellipse, comparable to a similar maximum for the rounded model which was
reached at $M_w = 0.3$. The pure ellipse's lifting characteristics at higher $M_w$ thus appeared superior, as further emphasized by the comparisons of Figure 25.

Drag characteristics also showed an improvement with the elongated trailing edge. At Mach numbers less than 0.9, an increase in blowing was accompanied by a drag reduction (Figures 26, 27) very similar to trends characteristically exhibited by a jet flap. The drag rise with increased $C_{*}$ experienced by the rounded ellipse was eliminated except at $M_w = 0.9$, where, before the rise occurred, $C_d$ was favorably reduced with blowing. This latter observation was due to the rearward movement of the upper surface shock with an increase in blowing (Figure 28). A rearward shock movement of 20 percent of the chord was possible with a $C_{*}$ increase of 0.0069; additional blowing above that did not relocate the shock. Drag reduction was considerably improved over the rounded ellipse. Figure 29 indicates reduction with increased $C_{*}$ at all Mach numbers, although at 0.9 an initial large reduction at very low $C_{*}$ was rapidly followed by a reversed trend which pointed towards a net drag increase for $C_{*}$ above 0.02. Correlated drag and lift data are presented in the drag polar of Figure 30 while Figure 31 presents variation in half chord moment coefficient with $C_{*}$.

Section performance was again indicated by the two equivalent lift-to-drag ratios (Figures 32, 33). Considering the efficiency based on kinetic energy, the pure ellipse yielded a maximum $(A/d_{e})$ of 22.6 at $M_w = 0.7$, almost 3.3 times greater than the rounded ellipse at the same speed, and only slightly less than the rounded edge's maximum at $M_w = 0.4$. The higher speed superiority of the pure ellipse over the rounded version in lift, drag, and efficiency was thus well demonstrated.

**JET FLAP**

The $30^\circ$ deflection jet flap on the 15 percent thick elliptic section was tested at $\alpha = -1.2^\circ$. Generated lift coefficients (Figures 34 and 35) were considerably smaller than either of the tangentially blown models; maximum $C_A$ was roughly half that of the pure ellipse and 30 percent of the rounded ellipse maximum. However, the jet flap did not experience the "$C_{*}$ stall" phenomenon of the tangential models, probably because the jet was not detachable from the trailing edge. The jet also fixed the rear
stagnation point, and thus reduced the supercirculation capability of the airfoil. It was effectively a thrust producer, and its effect on drag reduction is shown in Figures 36 through 38, where the trends are similar to the pure ellipse for $M_e < 0.8$ and $C_{\mu} < 0.025$. At $M_e = 0.9$, drag continued to be reduced by additional blowing, a trend not present for the tangential models. Pressure distributions at this Mach number (Figure 39) indicated that there was some movement (about 5 percent chord) of the upper surface shock with $C_{\mu}$ variation and the lower surface shock moved rearward approximately 5 percent of the chord also. The lack of high trailing edge suction peaks led to a large reduction in the negative pitching moment typically generated by tangential blowing (Figure 40). Figure 41 depicts the jet-flap lift-drag relationship.

In spite of the large drag reduction from the unblown case, the overall efficiencies of the jet flap were low due to the lack of lift augmentation (Figures 42, 43). A maximum $A/d_{eq}$ of about 8 was generated at $M_e = 0.4$ (and $C_{\mu} = 0.26$), with lesser values at high Mach numbers, all of which were considerably smaller than for the preceding models.

COMPARISON

Characteristics of the blown sections can best be summarized by direct comparison of the three models. Maximum lift generated for $C \leq 0.08$ (due to model limitations) is shown in Figure 44, where the subsonic lifting capability of the rounded ellipse yielded to the better transonic properties of the pure ellipse above $M_e = 0.55$. The jet flap configuration tested was not competitive in either speed regime. Combining Figure 44 with the drag characteristics, Figure 45 presents the efficiency factor $A/d_{eq}$, where again the rounded trailing edge was superior at $M_e \leq 0.5$ and the elongated trailing edge was preferred above $M_e = 0.5$. The data for the jet flap indicated a weakness of the force-based $A/d_{eq}$ parameter. The unexpected high efficiency at $M_e = 0.3$ was due to the large negative drag produced by a momentum coefficient of similar magnitude (but positive), the sum of the two approaching zero and inflating the parameter. The more meaningful parameter $(A/d_{eq})$ avoided this difficulty due to the $V_j/V_e$ term in the denominator, and thus the curves of Figure 46 were more indicative of the trend in efficiency. Again the pure ellipse was the most efficient above $M_e = 0.55$ (with its
maximum at $M = 0.7$). Lift coefficients associated with these maximum efficiencies (Figure 47) remained almost constant for the pure ellipse up to $M = 0.7$, while the rounded configuration reached its maximum at $M = 0.4$ and dropped off rapidly. Associated blowing coefficients (Figure 48) were on the order of $C_\mu \approx 0.02$ for the pure ellipse above $M = 0.5$ and $C_\mu \approx 0.03$ for the rounded trailing edge below $M = 0.5$, indicating a relatively low maximum blowing requirement of $C_\mu \leq 0.03$ throughout the entire Mach number range.

CONCLUSIONS

Transonic tests conducted over the range $0.3 \leq M \leq 0.9$ on a series of three circulation control ellipse airfoils indicated that high speed performance was heavily dependent on maintaining supercirculation primarily by keeping the trailing edge Coanda jet attached. Comparison of experimental results also gave the following conclusions:

- Below $M = 0.55$, the rounded ellipse configuration was the most favorable of the three, developing the highest lift coefficient, lift augmentation, and aerodynamic efficiency. At higher Mach numbers a rapid drag increase with blowing, apparently resulting from Coanda jet detachment and loss of circulation, caused considerable deterioration in overall section performance of this model.

- The pure 15 percent ellipse with tangential blowing displayed superior high speed characteristics in the range $0.55 \leq M \leq 0.9$. Due to the elongated trailing edge, the model was relatively free of jet detachment effects up to $M = 0.7$ and generated greater lift and aerodynamic efficiency, plus reduced drag. The rearward movement of the upper surface shock was beneficial in the latter respect.

- The 30° jet flap configuration was the least effective section of the three, showing promise only in drag reduction (due to its thrusting ability) and lack of lift drop off with increased blowing (although net lift augmentation was small).
For the entire Mach number range, maximum aerodynamic efficiency was obtained at $C_\mu \leq 0.03$; this was reduced to $C_\mu \leq 0.02$ by the pure ellipse at $M_\infty > 0.55$.

The results indicate that the elongated trailing edge was an effective high speed circulation control trailing edge, but that future work should be done to optimize the tangentially blown configuration and extend its range of maximum effectiveness beyond $M_\infty = 0.7$. Of primary importance is a need to understand the phenomenon of high speed Coanda jet detachment and effects upon it of upper surface boundary-layer shock interaction and supersonic expanded flow downstream of the choked nozzle.

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REFERENCES


Figure 1 - Critical Mach Number of Ellipses at $\alpha = 0^\circ$
Figure 2 - Effect of Rounded Trailing Edge Variation on Maximum Suction Peaks (Incompressible)
(a) Internal view showing model, balance system disc, and slotted floor & ceiling

(b) External View, looking upstream

Figure 4 - Transonic Wind Tunnel and Associated Test Equipment
Figure 5 - Concentric Ring Force Balance Schematic

- Drag Levers = 1, 2
- Lift Levers = 3, 4
- Dummy Levers = 5, 6, 7, 8
Assumptions:
1. Isentropic expansion to $P_m$
2. No nozzl. losses

Conditions:
- $h = .01\text{ in}$
- $A_e = 0.12 \text{ in}^2$
- $b = 12\text{ in}$
- $P_{cm} = 14.7 \text{ psia}$
- $T_c = 539.6 \text{ deg}$

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$\phi = -1.2^\circ$
Figure 29 - Pure Ellipse Drag Reduction
Figure 30 - Pure Ellipse Drag Polar
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Figure 36 - Drag Variation with Momentum Coefficient for Jet Flap
Figure 37 - Jet Flap Drag Variation with Mach Number
Figure 33 - Jet Flap Drag Reduction

\[ \Delta C_d = C_{d} - C_{d}(C_\mu=0) \]
Figure 39 - Pressure Distributions for Jet Flap at $M_{\text{nominal}} = 0.9$, $\alpha = -1.2^\circ$
Figure 40 - Half Chord Pitching Moment Variation
With Momentum Coefficient for Jet Flap
Figure 11 - Det Flap Drag Polar
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Figure 44 - Comparative Lift Characteristics of the Three Models

Maximum Lift Coefficient, $C_{L_{\text{max}}}$, for $C_L < 0.08$

$\alpha = -1.2^\circ$

Rounded Ellipse

Pure Ellipse

Jet Flap
Figure 45 - Comparison of Maximum Force-Based Equivalent Lift-to-Drag Ratio for the Three Configurations
Figure 46 - Comparison of Maximum Kinetic-Energy-Based Equivalent Lift-to-Drag Ratio For The Three Configurations
Figure 47 - Lift Corresponding to Maximum Aerodynamic Efficiency
Figure 48 - Momentum Coefficients for Maximum Aerodynamic Efficiencies
Two-dimensional transonic wind tunnel tests were conducted on three fifteen percent circulation control elliptic airfoils over the range 0.3 ≤ Mach ≤ 0.9. Model configurations included a pure elliptical shape with both jet flap and tangential upper surface trailing edge blowing, plus tangential blowing over an elliptical shape with a rounded trailing edge. Performance of the rounded trailing edge configuration was the best of the three at low speeds, but above Mach = 0.55, detachment of the Coanda jet caused rapid performance deterioration. Due to its elongated trailing edge and associated larger effective radius downstream of the slot, the tangentially blown pure ellipse was able to extend the jet detachment Mach number to 0.7, where maximum equivalent lift-to-drag ratios of 22 at C_{L} of 0.44 were achieved. The jet flap proved to be inferior to the tangentially blown configurations in all respects except in its ability as a thrusting, drag-reducing body.