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MEASURED N2O-N2 ABSORPTION AT FIVE DF LASER FREQUENCIES

F. S. Mills, et al

Ohio State University

Prepared for:
Rome Air Development Center
Advanced Research Projects Agency

March 1974
MEASURED N₂-O₂ ABSORPTION
AT FIVE OF LASER FREQUENCIES

The Ohio State University
ElectroScience Laboratory
Department of Electrical Engineering
Columbus, Ohio 43212

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**ABSTRACT**

This report presents measurements of the absorption coefficients of N2O-N2 samples at five DF laser wavelengths (3-2 P6, P7, P8 and 2-1 P10, P11). A small grating-tunable pulsed DF laser was used in conjunction with a multi-traversal absorption cell having a path length for these experiments of 0.732 km. The results are compared with previously available experimental results and with calculated values.
MEASURED N$_2$O-N$_2$ ABSORPTION
AT FIVE DF LASER FREQUENCIES

F. S. Mills
R. K. Long

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Phone: 614 422-6077

Project Engineer: James W. Cusack
Phone: 315 330-3145

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FOREWORD

This report, Ohio State University Research Foundation Report Number 3271-9 (Ninth Quarterly Report), was prepared by The Ohio State University ElectroScience Laboratory, Department of Electrical Engineering at Columbus, Ohio. Research was conducted under Contract F 30602-72-C-0016. Mr. James W. Cusack, RADC (OCSE), of Rome Air Development Center, Griffiss Air Force Base, New York, is the Project Engineer.

This technical report has been reviewed and is approved.

[Signature]

James W. Cusack
RADC Project Engineer
ABSTRACT

This report presents measurements of the absorption coefficients of N$_2$O-N$_2$ samples at five DF laser wavelengths (3-2 P$_6$, P$_7$, P$_8$ and 2-1 P$_{10}$, P$_{11}$). A small grating-tunable pulsed DF laser was used in conjunction with a multi-traversal absorption cell having a path length for these experiments of 0.732 km.

The results are compared with previously available experimental results and with calculated values.
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I. INTRODUCTION

Recent calculations [1], reproduced here as Table I, have predicted that the sea level absorption coefficients for a representative list of 30 DF lines of the 3-2, 2-1, and 1-0 vibrational bands are in the range 0.022 to 0.268 km\(^{-1}\) for a mid-latitude summer atmospheric model. This model assumes 76% relative humidity at 70°F, 9.28 ppm N\(_2\)O, 1.6 ppm CH\(_4\), 0.075 ppm CO, and 330 ppm CO\(_2\) [2].

The purpose of the present work was to experimentally verify, for certain DF lines, that part of the predicted coefficient which is attributable to N\(_2\)O absorption. From Table I we see that this fraction is, for the 3-2 P\(_6\), P\(_7\), and P\(_8\) lines, 7%, 55%, and 32% respectively, whereas for the 2-1 P\(_{10}\) and P\(_{11}\) the fraction is 65% and 27% respectively.

Assuming that the calculations are in error by no more than ±100 percent, it is not possible to measure the N\(_2\)O-\(\text{N}_2\) absorption coefficients with acceptable accuracy using a one kilometer absorption cell unless the absorber amounts are increased above the normally assumed sea level concentrations. This is the approach which has been taken here. N\(_2\)O concentrations used were 10 to 1000 times normal atmospheric abundance (i.e., \(2 \times 10^{-3}\) to \(2 \times 10^{-1}\) torr for a total pressure of 760 torr). These N\(_2\)O concentrations are still quite low and it is shown that the results can be linearly extrapolated to normal N\(_2\)O abundance without distortion caused by self-broadening.

The calculated coefficients require accurate knowledge of the laser line frequencies. At the present time the 3-2 band frequencies are not known as accurately as the 2-1 and 1-0 band frequencies. In the present study it was possible to obtain an approximate value for the separation between the laser frequency and the nearest N\(_2\)O absorption line for the 3-2 P(7) and 2-1 P(10) DF lines from a measurement of the absorption coefficient versus total pressure for a fixed absorber concentration.

II. DESCRIPTION OF EXPERIMENT

A block diagram of the experiment is shown in Fig. 1.

The laser is a small pulse type similar to one originally described by Ultee [3]. The laser tube is constructed of 7 mm id pyrex tubing with two transverse inlet ports and three outlet ports. Electrodes are made of 1/8" copper tubing. The active length is approximately twelve inches. Calcium fluoride brewster windows are employed and a separate flow of helium is introduced near each window to reduce formation of previously troublesome sulphur deposits. This flow is adjusted for 5 torr tube pressure with the other gases shut off. Gases used in the laser are helium, sulfur hexafluoride, oxygen, and deuterium. Active elements are SF\(_6\) and D\(_2\) which react in the electric discharge to produce DF. Helium is added as a heat sink and also probably promotes discharge stability. A small flow of oxygen helps to keep the tube walls clean.
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*Source of laser line data:
a - Mills (OSU)
b - calculated from molecular constants (P.K.L. Yin, OSU Physics Dept.)
c - Deutsch (7)*
A 15 cfm mechanical vacuum pump is used to maintain a discharge tube pressure of 15 torr and a flow rate sufficient to change the gas mixture in the tube between pulses. The optimum pressure varies somewhat according to the laser line which is oscillating. The laser discharge is created by discharging a 0.01 μF capacitor which has been charged to 14 kV. The pulses are 2 microseconds long and occur at a rate of 36 pulses per second. The latter value is vacuum pump limited and determines the maximum average power which can be obtained.

The optical cavity consists of a 300 line/mm grating blazed at 3 μm and a 20 m radius of curvature Germanium mirror coated for greater than 80% reflectivity between 3 μm and 4 μm. The grating and mirror are separated by 121 cm. The mirror is mounted in a piezoelectric drive and a mechanical translation stage to provide cavity length adjustment. The grating mount, laser tube and mirror mount are all attached to a 5' x 1' x 3" limestone slab. This arrangement has proved to be quite stable. Figure 2 shows a photograph of the laser. The entire laser and power supply are placed in a standard electromagnetic shielded room in order to reduce interference with the remainder of the experimental electronics. The optical output is through a hole in the shield and the pulse trigger output required by the boxcar integrator is coupled out of the shielded room by a solid state optical isolator device.

The thirty lines listed in Table I are all observed with this laser. The average power output is approximately one milliwatt per line.

The 21 cm N₂O cell shown in Fig. 1 was used as an attenuator in a detector linearity calibration experiment which was performed prior to the N₂O-N₂ measurements. The details of this somewhat involved procedure are described in Appendix A. The on-line computer data recording program used the calibration data to correct the absorption coefficient measurements for detector non-linearities.

For each experimental run the multi-traversal cell was evacuated and the transmittance of the empty cell was measured. A certain pressure of a mixture of 10,000 ppm N₂O in N₂ (based on manufacturer's analysis) was then admitted to the cell followed by a dry nitrogen fill to 760 torr. Mixing fans were turned on for one hour. This gave a mixture at the highest N₂O concentration to be measured during that run. After the transmittance of that mixture was measured, the absorption cell was partially pumped out, the pressure measured, and the cell refilled to 760 torr with dry N₂. This procedure reduced the N₂O concentration by a known amount. The new sample was allowed to mix for one hour and its transmittance was measured. This procedure was repeated to obtain data at several N₂O concentrations. At the end of the day the cell was again evacuated and the transmittance measured. The entire process was repeated several times on different days for each laser line. All measurements were made at room temperature (72-74°F).
Fig. 2. The pulsed DF probe laser.
Although the laser was tunable from line to line, it was found that the desired repeatability in transmittance (1%) could not be obtained unless the laser was left tuned to one line for the duration of a measurement run. This is presumably due to optical alignment difficulties associated with moving the grating.

III. RESULTS OF ABSORPTION COEFFICIENT MEASUREMENTS

Figures 3-7 show the measured absorption coefficients versus N₂O concentration for the five lines studied. In each case a least squares fit of the data to a straight line through the origin was made. The figures also show the predicted results using the AFCRL data tape [4] and the experimental results of Spencer [5] obtained from measurements on pure N₂O samples in a one meter cell.

Figures 8-11 show computed spectral plots [1] in the vicinity of the five laser lines. The plots are for one km path length, 760 torr total pressure, 72°F, and N₂O partial pressures as given on the figures. Note that in all five cases there is a near coincidence between an N₂O absorption line and a DF laser frequency. For this reason one might expect that errors in the N₂O or DF line frequencies would cause errors in the computed results. In fact the predictions and measurements are in quite good agreement although there is a greater discrepancy for those laser lines whose position is less well known, indicating that uncertainty in laser line position is a significant source of error in the calculations.

The excellent agreement of the measured values with those obtained by Spencer confirms the lack of significant self broadening effects in N₂O.

Assuming a natural N₂O abundance of 0.28 ppm [2], Table II gives the N₂O absorption coefficients for the five laser lines as extrapolated from the measured data. For comparison the calculated values from Table I are also given.

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<th>v (cm⁻¹)</th>
<th>k_{OSU}^{exp} (km⁻¹)</th>
<th>k_{calc} (km⁻¹)</th>
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Fig. 3. Measured $N_2O-N_2$ absorption coefficient for 3-2 P(6) line.
Fig. 4. Measured $\text{H}_2\text{O}$-$\text{N}_2$ absorption coefficient for 3-2 P(7) line.
Fig. 5. Measured H₂O-N₂ absorption coefficient for 3-2 P(8) line.
Fig. 6. Measured $N_2O-N_2$ absorption coefficient for 2-1 P(10) line.
Fig. 7. Measured $N_2O-N_2$ absorption coefficient for 2-1 $P(11)$ line.
Fig. 8. Calculated spectrum for 2545-2555 cm\(^{-1}\).
Fig. 9. Calculated spectrum for 2565-2575 cm⁻¹.
Fig. 10. Calculated spectrum for 2575-2585 cm\(^{-1}\).
IV. LINE SEPARATION EXPERIMENTS

For two of the laser lines, 3-2 P(7) and 2-1 P(10), the assumed laser frequency differs from the assumed frequency of an N2O absorption line by less than one half-width. In this situation it is possible to obtain information about the separation of the laser line and absorption line by plotting the absorption coefficient \( a \) as a function of total pressure with the absorber pressure constant.

This can be shown by the following [6]. For an isolated Lorentz line we have

\[
(1) \quad k = \frac{S}{\pi} \frac{\alpha}{(\Delta \nu)^2 + \alpha^2}
\]

where \( k \) is the absorption coefficient,

\[
\alpha = \alpha_0 \frac{P}{P_0} \left( \frac{T_0}{T} \right)^m
\]

is the half-width of the absorption line, \( P_0 = 1 \text{ atm} \), \( \Delta \nu \) is the difference in the frequencies of the laser line and the absorption line, \( P \) is the total pressure and \( S \) is the line strength. For a constant temperature and \( P \) in atmospheres \( \alpha \) becomes

\[
\alpha = \alpha_0 P.
\]

On a curve of \( k \) versus total pressure \( P \) the condition for zero slope with \( \Delta \nu \) constant is

\[
(2) \quad \frac{dk}{d\alpha} = \frac{S}{\pi} \left[ \frac{(\Delta \nu)^2 + \alpha^2 - 2\alpha^2}{(\Delta \nu^2 + \alpha^2)^2} \right] = 0
\]

or,

\[
(3) \quad \alpha = \Delta \nu.
\]

Therefore, as a first approximation (i.e., assuming a single isolated Lorentz line) the following expression holds:

\[
(4) \quad \alpha_0 P = \Delta \nu.
\]

Thus, if the frequency difference between the laser line and the absorption line is accurately known, the half-width can be accurately determined. Similarly, if the half-width and frequency of the absorption line are accurately known, the laser frequency can be found.
In the present study, the laser frequencies were believed to be more uncertain than the half widths and frequencies of the $\text{NgO}$ absorption lines so the latter procedure was used to more accurately determine the laser frequencies.

It should be mentioned that Eq. (4) is strictly true only if the pressure is high enough that the Voigt profile does not have to be used to describe the absorption line shape, there is no pressure shift in the frequency of the absorption line, and there are no other absorption lines close enough to contribute to the absorption at the laser frequency. In the present study, the first two assumptions are valid, but the third one is not. It can be shown that the effect of considering other absorption lines which are close enough to contribute to the absorption at the laser frequency is to add a small positive term to the right hand side of Eq. (4). For the lines under consideration in the present study, the added term is 4 to 5 percent of $\Delta v$.

For the two lines studied, the experimental plot of absorption coefficient versus total pressure was used to make a first estimate of the laser frequency. Curves of absorption coefficient versus total pressure were calculated for several laser frequencies close to the estimated frequency using the AFCRL line data [4]. These calculated curves were then plotted along with the experimental data. The calculated curve which best fit the experimental data was then taken to represent the correct laser frequency.

Figure 12 shows the experimental data for the 3-2 $P(7)$ line with $\text{NgO}$ pressure constant at $6.51 \times 10^{-3}$ torr and total pressure varying from 50-850 torr along with calculated curves for the same $\text{NgO}$ pressure and laser frequencies $2570.505$ cm$^{-1}$, $2570.510$ cm$^{-1}$, and $2570.515$ cm$^{-1}$. The laser frequency determined from Fig. 12 is $2570.51 \pm 0.01$ cm$^{-1}$.

Figures 13 and 14 show the experimental data for the 2-1 $P(10)$ line with $\text{NgO}$ pressures $6.82 \times 10^{-3}$ torr and $1.73 \times 10^{-2}$ torr respectively and total pressure from 50 torr to 760 torr. Also shown are calculated curves for the same $\text{NgO}$ pressures and laser frequencies $2580.100$ cm$^{-1}$, $2580.105$ cm$^{-1}$, and $2580.110$ cm$^{-1}$. The laser frequency determined from the plots is $2580.10 \pm 0.005$ cm$^{-1}$. This is in agreement with the frequency calculated from molecular constants [7].
Fig. 12. Absorption coefficient vs total pressure for 3-2 P(7) line at 6.51 x 10^{-3} torr N_2O.
Fig. 13. Absorption coefficient vs total pressure for 2-1 P(10) line at $6.82 \times 10^{-3}$ torr $N_2O$. 
Fig. 14. Absorption coefficient vs total pressure for 2-1 P(10) line at $1.73 \times 10^{-2}$ torr $N_2O$. 

Absorption coefficient vs total pressure for 2-1 P(10) line at 1.73 x 10^{-2} torr N_2O.
V. CONCLUSIONS

The measurements presented in this report confirm the previously available experimental work and the calculations based on the AFCRL line data tape. Better DF laser frequency data is needed especially for the 3-2 band.

Techniques developed during this investigation are applicable to the water vapor absorption studies which are now underway. This includes the laser, detector calibration, data integration and recording system, etc.
APPENDIX A
DETECTOR LINEARITY CALIBRATION

The detectors used in these measurements are room temperature lead selenide photo conductive detectors. The rise time of these detectors is about 1 microsecond so that they are fast enough to respond to the peak power of the laser rather than average power. Although the average power is only on the order of 1 milliwatt, the peak power is about 100 watts. The detectors are definitely nonlinear in this region so they must be calibrated for linearity.

The lead selenide detectors were calibrated against an Eppley thermopile which has about a 1 second response time, and therefore measures average power rather than peak power. The thermopile is known to be linear in this range.

The laser line used for calibration was the 3-2 P(7) line since it was one of the lines of interest and it could be easily attenuated using a small absorption cell filled with various amounts of N2O. The calibration should also be good for other lines, although this assumption will need to be tested.

The experimental layout for the calibration experiment is shown in Fig. 1 of the main report. The experiment was done in two parts. For the first part of the experiment, mirror M2 was installed and detector #1 was compared with the thermopile over a wide range of signal levels. The laser was adjusted for optimum operation on the 3-2 P(7) line, and then left undisturbed for the remainder of the experiment. The signal amplitude at the detectors was lowered step by step by introducing N2O into the 21 cm cell. At each step the signals from detector #1 and the Eppley thermopile were read and recorded on the typewriter by the computer. This part of the experiment was repeated three times on three separate days. For the second part of the experiment mirror M2 was removed and detector #1 and detector #2 were compared.

A least squares fit of the data from the first part of the experiment was made to a third order polynomial. This yields an expression of the form

\[ E_1 = A_0 + A_1 X_1 + A_2 X_1^2 + A_3 X_1^3 \]  

relating PbSe detector #1 signal to Eppley thermopile signal where \( X_1 \) corresponds to PbSe #1 signal and \( E \) corresponds to Eppley signal (Fig. 15). Similarly the data from the second part of the experiment was used to obtain an expression of the form

\[ X_1 = C_0 + C_1 X_2 + C_2 X_2^2 + C_3 X_2^3 \] .

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Fig. 15. Eppley thermopile detector calibration signal versus lead selenide detector number one. Units are volts at A/D converter after arbitrary amplifications.
Where $X_2$ corresponds to PbSe #2 signal and $X_1$ corresponds to PbSe #1 signal (Fig. 16). From Eqs. (5) and (6) it is now possible to determine the following expression relating PbSe #2 signal, $X_2$, to Eppley signal, $E_2$ (Fig. 17).

\[ E_2 = B_0 + B_1 X_2 + B_2 X_2^2 + B_3 X_2^3 \]

The calibration was tested by putting Eqs. (5) and (7) in the data taking program and repeating the second part of the calibrating experiment. Figure 18 shows the result of that experiment. If the linearity calibration is good, the data should fall on a straight line through the origin. Figure 18 shows that this is very nearly true. A second check on the calibration is the actual absorption data (Figs. 3-7). Since the data falls on a straight line, this is a second indication that the calibration is good. For low absorber partial pressures, the absorption data is in fact the best check on calibration.
Fig. 16. Calibration of lead selenide detector #2 in terms of lead selenide detector #1. Units are volts at A/D converter after arbitrary amplifications.
Fig. 17. Derived curve relating PbSe #2 detector to Eppley thermopile. Units are volts at A/D converter after arbitrary amplifications.
Fig. 18. Linearity curve derived from data in Figs. 15 and 16. Relative units.
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