COMBAT OPTIMIZATION AND ANALYSIS PROGRAM—COAP

VOLUME III: PROGRAMMER'S MANUAL

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**Abstract**

COAP is a program for the simulation and optimization of combative and cooperative two-vehicle flight paths. It includes single vehicle flight path problem capability as a subcase. Considerable emphasis is placed on the use of modern optimization.

The program has the ability to perform trajectory optimization by the variational steepest-descent method including search for optimal initial conditions; search for optimal arc (stage) lengths; constraints defined at terminal point, intermediate corners (stage points), or along the path; and optimum parameter (design variable) values. The program can solve two system (vehicle) problems with or without reacting feedback from the second system (vehicle).

Alternatively, the program may be used to apply the direct multivariable search approach to trajectory optimization. A variety of multivariable search algorithms are available in this mode including elemental perturbation (one parameter at a time); organized first- and second-order methods, and randomized methods. A method of solution for problems exhibiting multiple extremals and a procedure for the location of saddle points is also included.

Point mass equations of motion for a two-vehicle system are incorporated in the COAP program. Motion takes place about a rotating oblate planet having up to four harmonics in its gravitational field, non-uniform atmosphere (1959 or 1962 ARDC), and winds. Auxiliary computations for aerodynamic heating are included. The vehicles may have arbitrary and independent aerodynamic and propulsive characteristics. If desired two independent sets of planetary characteristics may be employed.
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13. Abstract (continued)

Combative logic is defined in terms of vehicle relative states. The logic defines feedback control on the basis of relative state. The COAP program may utilize variational optimization procedures to determine optimal open loop control against a reacting opponent employing feedback control defined by combat logic. Alternately, the combative feedback control logic may be parameterized permitting the use of multivariable search for the definition of optimal feedback control parameters against a reacting opponent. Finally, by parameterization of both vehicle feedback control logic, a "mini-max" mode of operation may be employed in which a solution is obtained by multivariable search for a saddle point.

All capabilities described are available in a single general purpose FORTRAN IV digital computer program developed for the CDC 6600 computer. This volume, Volume III, presents a programmer's manual containing instructions regarding

(a) Computer requirements

(b) Program structure

(c) Detailed subroutine descriptions
Parameter optimization, non-linear programming, steepest-descent, "mini-max" solution, saddle point solution, multiple extremal solution
COMBAT OPTIMIZATION AND ANALYSIS PROGRAM - COAP

VOLUME III: PROGRAMMER'S MANUAL

D. S. HAGUE, R. T. JONES, AND C. R. GLATT

AEROPHYSICS RESEARCH CORPORATION

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FOREWORD

The research project outlined in this report was completed in the period from September 1969 to December 1970 under the sponsorship of the Air Force Flight Dynamics Laboratory, Air Force Systems Command, Wright-Patterson Air Force Base, Ohio. This report was prepared by Aerophysics Research Corporation, Bellevue, Washington, under the United States Air Force Contract F33615-70-C-1036. Mr. B. R. Benson and Mr. David T. Johnson of the Air Force Flight Dynamics Laboratory were the cognizant Air Force representatives for the study.

This report was authored by Mr. R. T. Jones, D. S. Hague, and C. R. Glatt of Aerophysics Research Corporation. The report was prepared and organized by Mrs. Jan Yonke of Aerophysics Research Corporation. The report and study benefit directly from a number of previous government-sponsored research studies including:

- USAF Contract AF33(616)-6848, for trajectory equation and program development
- USAF Contract AF33(657)-8829, for development of the variational optimization procedure and program
- USAF Contract AF33(615)-3932, for extension of the variational optimization program
- NASA Contract NAS 2-4507, for development of the parameter optimization procedure and program
- NASA Contracts NAS 2-3691, NAS 2-4880, NAS 1-9936, and NAS 3-13331 for extension of the optimization procedures

This project has resulted in considerable extension of the previously available AFFDL generalized steepest-descent computer program. Notable extensions consist of the addition of equations of motion for a second vehicle, addition of self-contained combative logic, extension of the variational steepest-descent procedure to situations involving a reacting opponent, addition of parameter optimization capability by multivariable search, and the development of a saddle point search procedure for the solution of parametrically defined trajectory or combat performance problems.

The study results are reported in four volumes as follows:

- **Volume I**  - Trajectory, Combat and Variational Optimization Formulation
- **Volume III**  - Programmer's Manual for Trajectory, Combat, and Variational Optimization Subprograms
Volume IV - Programmer's Manual for Parameter Optimization
Subprogram AESOP

This report was submitted by the authors March 1, 1971.

This technical report has been reviewed and is approved.

PHILIP P. ANTONATOS
Chief, Flight Mechanics Division
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ABSTRACT

A program for trajectory optimization by the variational steepest-descent is described in detail. The program capability includes search for optimal initial conditions; search for optimal arc (stage) lengths; constraints defined at terminal point, intermediate corners (stage points), or along the path; payoff function at terminal point or intermediate corner (stage point); search for optimum parameter (design variable) values; and two system (vehicle) problems with or without reacting feed-back from the second system (vehicle).

The program also incorporates an alternative direct multivariable search approach to trajectory optimization employing a variety of multivariable search algorithms including elemental perturbation (one parameter at a time); organized first- and second-order methods, and randomized methods. A method for solution for problems exhibiting multiple extremals and a procedure for the location of saddle points is also included in the program.

Joint mass equations of motion for a two-vehicle system are available in the program. Motion takes place about a rotating oblate planet having up to four harmonics in its gravitational field, non-uniform atmosphere (1959 or 1962 ARDC), and winds. Auxiliary computations for aerodynamic heating are included. The vehicles may have arbitrary and independent aerodynamic and propulsive characteristics.

Combative logic defined in terms of vehicle relative states is available in the program. The logic defines feedback control on the basis of relative state. Variational optimization procedures may be employed to determine optimal open loop control against a reacting opponent employing feedback control defined by combat logic. Alternatively, the combative feedback control logic can be parameterized permitting the use of multivariable search for the definition of optimal feedback control parameters against a reacting opponent. By parameterization of both vehicle feedback control logic, a "mini-max" situation capable of solution by multivariable search for a saddle point can be considered.

All capabilities described are available in a single general purpose FORTRAN IV digital computer program developed for the CDC 6600 computer.
## TABLE OF CONTENTS

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>I INTRODUCTION</td>
<td>1</td>
</tr>
<tr>
<td>II COMPUTER AND SYSTEM REQUIREMENTS</td>
<td>3</td>
</tr>
<tr>
<td>III PROGRAMMING CONCEPTS</td>
<td>4</td>
</tr>
<tr>
<td>- The Use of COMMON</td>
<td>4</td>
</tr>
<tr>
<td>- Table and Table Usage</td>
<td>4</td>
</tr>
<tr>
<td>- Symbolic Input</td>
<td>4</td>
</tr>
<tr>
<td>- Trajectory Printing Method</td>
<td>5</td>
</tr>
<tr>
<td>- Tape Usage</td>
<td>5</td>
</tr>
<tr>
<td>- Overlay Listing</td>
<td>7</td>
</tr>
<tr>
<td>- Program Organization</td>
<td>12</td>
</tr>
<tr>
<td>- Program Generation, Modification, and Execution</td>
<td>13</td>
</tr>
<tr>
<td>- Data Format</td>
<td>20</td>
</tr>
<tr>
<td>- Table Format</td>
<td>22</td>
</tr>
<tr>
<td>- Brief Write-Up on System Routines</td>
<td>23</td>
</tr>
<tr>
<td>- ENCODE/DECODE</td>
<td>25</td>
</tr>
<tr>
<td>IV MAIN PROGRAM AND SUBROUTINE MAIN2</td>
<td>27</td>
</tr>
<tr>
<td>- MAIN and MAIN2</td>
<td>27</td>
</tr>
<tr>
<td>- BDATA1 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA2 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA3 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA4 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA5 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA6 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- BDATA7 - Block Data Subroutine</td>
<td>29</td>
</tr>
<tr>
<td>- SPRANG - Random Number Generator</td>
<td>29</td>
</tr>
<tr>
<td>- CHAIN - Overlay Control Program</td>
<td>30</td>
</tr>
<tr>
<td>- MSGONE - Combat Message Subroutine, Vehicle 1</td>
<td>32</td>
</tr>
<tr>
<td>- MSGTWO - Combat Message Subroutine, Vehicle 2</td>
<td>32</td>
</tr>
<tr>
<td>V PROGRAM MAIN1 AND SUBROUTINE MAIN2</td>
<td>33</td>
</tr>
<tr>
<td>- READA and READA2 - Input Routines for Vehicle 1 and Vehicle 2 Data</td>
<td>37</td>
</tr>
<tr>
<td>- DORDER - Directory Order Output Routine</td>
<td>45</td>
</tr>
<tr>
<td>- FACIL - Pack Routine</td>
<td>46</td>
</tr>
<tr>
<td>- DSKRC and DSKREC - Directory Search Routine for Subscripts</td>
<td>47</td>
</tr>
<tr>
<td>- STOP1 - General Stop Routine</td>
<td>49</td>
</tr>
<tr>
<td>- EXERR - Error Routine</td>
<td>51</td>
</tr>
<tr>
<td>- TSRCH and TSRCH2 - Directory Search for Table Subscript</td>
<td>52</td>
</tr>
<tr>
<td>- READB and READB2 - Binary Stage Data Input Routine</td>
<td>54</td>
</tr>
<tr>
<td>- TABLESOP - Parameter Optimization Input Subroutine</td>
<td>56</td>
</tr>
<tr>
<td>- DIPLAC - Integer Shift Routine</td>
<td>57</td>
</tr>
<tr>
<td>- DEF and DEF2 - Heading and Page Eject</td>
<td>59</td>
</tr>
<tr>
<td>- TABRE and TABRE2 - Table Dimension Subscript Routines</td>
<td>60</td>
</tr>
<tr>
<td>Section</td>
<td>Page</td>
</tr>
<tr>
<td>---------</td>
<td>------</td>
</tr>
<tr>
<td>13. LINES and LINES2 - Lines Accounting Routines</td>
<td>62</td>
</tr>
<tr>
<td>14. PACBCD - Packs Six Character Words</td>
<td>64</td>
</tr>
<tr>
<td>15. PACKR - Packs BCD Characters</td>
<td>66</td>
</tr>
<tr>
<td>16. READ31 - Binary Conversion Routine</td>
<td>68</td>
</tr>
<tr>
<td>17. SVI and SVI2 - Block Save Routines</td>
<td>70</td>
</tr>
<tr>
<td>18. BIBLOCK - Data Output in Blocks</td>
<td>72</td>
</tr>
<tr>
<td>19. SHELL - Numeric Sorting Subroutine</td>
<td>74</td>
</tr>
<tr>
<td>1. DIFEQ - Differential Equation Selector</td>
<td>82</td>
</tr>
<tr>
<td>2. MANTGT and MANTGT2 - Maneuvering Target</td>
<td>84</td>
</tr>
<tr>
<td>3. CTVS and CTVS2 - Control Variable Routine for EXE</td>
<td>90</td>
</tr>
<tr>
<td>4. IFCS - In-Flight Constraints</td>
<td>93</td>
</tr>
<tr>
<td>5. PARTS - Partial Derivatives</td>
<td>96</td>
</tr>
<tr>
<td>6. LINC0M and LINC0M2 - Linear Combination Routines</td>
<td>104</td>
</tr>
<tr>
<td>7. Slack and SLACK2 - Slack Variable Routines</td>
<td>107</td>
</tr>
<tr>
<td>8. PENAL and PENAL2 - Penalty Function Routine</td>
<td>109</td>
</tr>
<tr>
<td>9. PIIT5 and PIITS2 - Data Gathering Routine</td>
<td>112</td>
</tr>
<tr>
<td>10. OBSFUN and OBSFUN2 - Observation Function Routine</td>
<td>115</td>
</tr>
<tr>
<td>11. FILTER and FILTER2 - Repeater Routines for h-Transformation</td>
<td>120</td>
</tr>
<tr>
<td>12. STGTST and STGTST2 - Stage Testing Routine</td>
<td>122</td>
</tr>
<tr>
<td>13. EXTRAN and EXTRAN2 - Driver for h-Transformation</td>
<td>125</td>
</tr>
<tr>
<td>14. INTGRT, INTGRT2 and INTGRTR - Interface for Integration Routine</td>
<td>128</td>
</tr>
<tr>
<td>15. CODES and CODES2 - Code Print Routines</td>
<td>131</td>
</tr>
<tr>
<td>16. ITEMS and ITEMS2 - Variable Print Routines</td>
<td>133</td>
</tr>
<tr>
<td>17. COMBAT and COMBAT2 - Combat Control Routine</td>
<td>135</td>
</tr>
<tr>
<td>18. IMIMINF and IMIMINF2 - Integration Routine</td>
<td>143</td>
</tr>
<tr>
<td>19. TIMID and TIMID2 - Step Function Routines for Time Points</td>
<td>147</td>
</tr>
<tr>
<td>20. VALUES and VALUES2 - Value Print Routines</td>
<td>149</td>
</tr>
<tr>
<td>21. MISCUT and MISCUT2 - Abortion Routine</td>
<td>151</td>
</tr>
<tr>
<td>22. ONLINED - On Line Display Routine</td>
<td>153</td>
</tr>
<tr>
<td>23. DIFEQ1 and DIFEQ2 - Point Mass Equations of Motion</td>
<td>154</td>
</tr>
<tr>
<td>24. DIFEQ3 - Dummy Subroutine</td>
<td>164</td>
</tr>
<tr>
<td>25. TLUREV - Two Dimensional Table Look-Up Routine</td>
<td>165</td>
</tr>
<tr>
<td>26. ACUS - Arc Cosine Routine</td>
<td>167</td>
</tr>
<tr>
<td>27. ASIN - Arc Sine Routine</td>
<td>169</td>
</tr>
<tr>
<td>28. TLU and TLU2 - Two Dimensional Table Look-Up Routine</td>
<td>170</td>
</tr>
<tr>
<td>29. AVAN2 - Arctangent Routine</td>
<td>172</td>
</tr>
<tr>
<td>30. TLU1 - Two Dimensional Table Look-Up Routine</td>
<td>174</td>
</tr>
<tr>
<td>31. TIMREV and TIMREV2 - Time Point Collection Routine</td>
<td>177</td>
</tr>
<tr>
<td>32. FCUBR - Evaluation of Partial Routine</td>
<td>179</td>
</tr>
<tr>
<td>33. FFPACK - Blocking Routine for Partials</td>
<td>182</td>
</tr>
<tr>
<td>34. FLUSH1 and FLUSH12 - Buffer Flush Routine for FPACK</td>
<td>184</td>
</tr>
<tr>
<td>35. SETGRID - Paper Plot Grid Size Routine</td>
<td>186</td>
</tr>
<tr>
<td>36. PAPERP - Printer-Plot Control Routine</td>
<td>187</td>
</tr>
<tr>
<td>Section</td>
<td>Page</td>
</tr>
<tr>
<td>---------</td>
<td>------</td>
</tr>
<tr>
<td>37. DETECT and DETECT2 - Sensor Control Program</td>
<td>188</td>
</tr>
<tr>
<td>38. ROLE1 and ROLE2 - Role Selection Subprogram</td>
<td>190</td>
</tr>
<tr>
<td>39. HLIM1T and HLIM1T2 - Minimum Altitude Constraint Routine</td>
<td>194</td>
</tr>
<tr>
<td>40. ANGLES and ANGLES2 - Relative Angular Orientation Routines</td>
<td>196</td>
</tr>
<tr>
<td>41. CRATE and CRATE2 - Finite Control Rate Routine</td>
<td>198</td>
</tr>
<tr>
<td>42. TIM001 and TIM0012 - Tabular Time Point Routine</td>
<td>204</td>
</tr>
<tr>
<td>43. DEQPRE and DEQPRE2 - Equation of Motion Pre-Data Initialization</td>
<td>206</td>
</tr>
<tr>
<td>44. FTRFUN and FTRFUN2 - Fire Control Subprogram</td>
<td>207</td>
</tr>
<tr>
<td>45. GAM01 and GAM02 - Flight through Vertical Routine</td>
<td>211</td>
</tr>
<tr>
<td>46. DEQINI and DEQINI2 - Equation of Motion Post-Data Initialization</td>
<td>213</td>
</tr>
<tr>
<td>47. DEQBCI and DEQBCI2 - Derivative Calculation Before Control Definition</td>
<td>214</td>
</tr>
<tr>
<td>48. FPPS and FPPS2 - Flight Plan Programmer</td>
<td>215</td>
</tr>
<tr>
<td>49. ONEMO - Transformation of Selected Vehicle 2 to Vehicle 1 COMMON</td>
<td>218</td>
</tr>
<tr>
<td>50. CTLITR and CTLITR2 - Control Dependent Derivative Calculation</td>
<td>219</td>
</tr>
<tr>
<td>51. DEQACI and DEQACI2 - Derivative Calculation after Control Definition</td>
<td>220</td>
</tr>
<tr>
<td>52. FPPG and FPPG2 - Gamma Command Flight Plan Programmer</td>
<td>222</td>
</tr>
<tr>
<td>53. DEQSIP and DEQSIP2 - Derivative Evaluation Initial Point</td>
<td>224</td>
</tr>
<tr>
<td>54. DEQCOD and DEQCOD2 - Trajectory Code Print</td>
<td>225</td>
</tr>
<tr>
<td>55. DEQVAL and DEQVAL2 - Trajectory History Print</td>
<td>226</td>
</tr>
<tr>
<td>56. DEQIV and DEQIV2 - Integrated Variable Specification</td>
<td>227</td>
</tr>
<tr>
<td>57. DEQMT and DEQMT2 - Trajectory h-Transformation Subroutines</td>
<td>228</td>
</tr>
<tr>
<td>58. ERROR and ERROR2 - General Table Error Routine</td>
<td>229</td>
</tr>
<tr>
<td>59. PTBEQN and PTBEQN2 - Driver Routines for Equations</td>
<td>231</td>
</tr>
<tr>
<td>60. TWOONE - Transformation of Selected Vehicle 1 to Vehicle 2 COMMON</td>
<td>234</td>
</tr>
<tr>
<td>61. IZERO and IZERO2 - Packs Non-Zero Numbers</td>
<td>235</td>
</tr>
<tr>
<td>62. PPLNLN - Main Paper Plot Routine</td>
<td>237</td>
</tr>
<tr>
<td>63. SENSOR and SENSOR2 - Vehicle Sensor Routines</td>
<td>239</td>
</tr>
<tr>
<td>64. VISION and VISION2 - Pilot Vision Routines</td>
<td>242</td>
</tr>
<tr>
<td>65. PASSV1 and PASSV2 - Passive Tactics Routine</td>
<td>244</td>
</tr>
<tr>
<td>66. DEFEN1 and DEFEN2 - Defensive Tactics Routine</td>
<td>246</td>
</tr>
<tr>
<td>67. EVADE1 and EVADE2 - Evasive Tactics Routine</td>
<td>249</td>
</tr>
<tr>
<td>68. OFFEN1 and OFFEN2 - Offensive Tactics Routine</td>
<td>252</td>
</tr>
<tr>
<td>69. ATTACI and ATTAC2 - Attacking Tactics Routine</td>
<td>255</td>
</tr>
<tr>
<td>70. OALPBA and OALPBA2 - Subprogram for Instantaneous Control Vector Iteration</td>
<td>258</td>
</tr>
<tr>
<td>71. HIHO and HIHO2 - N-Dimensional Table Call Routine</td>
<td>262</td>
</tr>
<tr>
<td>72. TMTX - Transformation Matrix Routine</td>
<td>264</td>
</tr>
<tr>
<td>73. TRNPOS - A 3 x 3 Matrix Transpose Routine</td>
<td>267</td>
</tr>
<tr>
<td>Section</td>
<td>Page</td>
</tr>
<tr>
<td>---------</td>
<td>------</td>
</tr>
<tr>
<td>74. MULT31 - A Matrix Multiplication Routine</td>
<td>268</td>
</tr>
<tr>
<td>75. HETS and HETS2 - Heating Computations</td>
<td>259</td>
</tr>
<tr>
<td>76. TFFS and TFFS2 - Single Engine Thrust and Fuel Flow</td>
<td>276</td>
</tr>
<tr>
<td>77. SACS and SACS2 - Aerodynamic Routines</td>
<td>279</td>
</tr>
<tr>
<td>78. LATS and LATS2 - Geodetic-Geocentric Conversion</td>
<td>288</td>
</tr>
<tr>
<td>79. ATMS and ATMS2 - Atmosphere Selector</td>
<td>290</td>
</tr>
<tr>
<td>80. GVSP and GVSP2 - Gravitational Routine</td>
<td>291</td>
</tr>
<tr>
<td>81. ANITR and ANITR2 - Throttle Dependent Derivative and Thrust Vector Calculation</td>
<td>293</td>
</tr>
<tr>
<td>82. BAITR and BAITR2 - Bank Angle Dependent Derivative Calculation</td>
<td>294</td>
</tr>
<tr>
<td>83. ASRCH and ASRCH2 - Directory Search Routines for BCD Characters</td>
<td>295</td>
</tr>
<tr>
<td>84. GRIDXY - Paper Plot Grid Routine</td>
<td>297</td>
</tr>
<tr>
<td>85. PLCPTS - Paper Plot Point Placing Program</td>
<td>299</td>
</tr>
<tr>
<td>86. IPICK - Random Tactic Selector</td>
<td>300</td>
</tr>
<tr>
<td>87. DEFEN11 and DEFEN21 - First Defensive Tactic</td>
<td>301</td>
</tr>
<tr>
<td>88. FIXEDR and FIXEDR2 - Fixed Role Selection Routine</td>
<td>307</td>
</tr>
<tr>
<td>89. EVADE11 and EVADE21 - First Evasive Tactic</td>
<td>308</td>
</tr>
<tr>
<td>90. OFFEN11 and OFFEN21 - Lag-Pursuit Offensive Tactic</td>
<td>312</td>
</tr>
<tr>
<td>91. OFFEN12 and OFFEN22 - Lead-Pursuit Offensive Tactic</td>
<td>313</td>
</tr>
<tr>
<td>92. OFFEN13 and OFFEN23 - Reference Vector Offensive Tactic</td>
<td>314</td>
</tr>
<tr>
<td>93. ATTAC11 and ATTAC21 - First Attacking Tactic</td>
<td>315</td>
</tr>
<tr>
<td>94. ATTAC12 and ATTAC22 - Second Attacking Tactic</td>
<td>316</td>
</tr>
<tr>
<td>95. CTLOFT - Internal AESOP Optimization Loop</td>
<td>318</td>
</tr>
<tr>
<td>96. NDTLU - N-Dimensional Table Lookup Routine</td>
<td>320</td>
</tr>
<tr>
<td>97. CHMFP and CHMFP2 - Chemical State Computation</td>
<td>323</td>
</tr>
<tr>
<td>98. CONV - Non-Linear Equation Solver</td>
<td>326</td>
</tr>
<tr>
<td>99. TFFM and TFFM2 - Multiengine Thrust and Fuel Flow</td>
<td>329</td>
</tr>
<tr>
<td>100. ATMS59 and ATMS592 - 1959 Atmosphere Calculation Routine</td>
<td>333</td>
</tr>
<tr>
<td>101. ATMS62 and ATMS622 - 1962 Atmosphere Calculation Routine</td>
<td>335</td>
</tr>
<tr>
<td>102. PUT - Character Manipulation Routine</td>
<td>337</td>
</tr>
<tr>
<td>103. GET - Character Manipulation Routine</td>
<td>338</td>
</tr>
<tr>
<td>104. OPTBA and OPTBA2 - Bank-angle Iteration Routine</td>
<td>339</td>
</tr>
<tr>
<td>105. IMAINOP - Internal Parameter Optimization Interface Routine</td>
<td>341</td>
</tr>
<tr>
<td>106. ISELECT - Interval Search Selection Routine</td>
<td>343</td>
</tr>
<tr>
<td>107. MULT33 - Matrix Multiplication Routine</td>
<td>344</td>
</tr>
</tbody>
</table>

VII PROGRAM CTLS

1. CTLS1 - Original Control System 347
2. CTLS2 - Arbitrary Control System 357
3. DISPLAY - Console Display Routine 362
4. SEARCH - Search Routine 363
<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>5. CARDS - Restart Cards Routine</td>
<td>367</td>
</tr>
<tr>
<td>6. DALCAL - Delta Alpha Calculation</td>
<td>369</td>
</tr>
<tr>
<td>7. KCALC - Step Size Logic Routine for Control System</td>
<td>374</td>
</tr>
<tr>
<td>8. INVERT - Inversion</td>
<td>379</td>
</tr>
<tr>
<td>9. DECIDE - Driver for Decision Routines</td>
<td>384</td>
</tr>
<tr>
<td>10. OFFSW - Display Drop Routine</td>
<td>385</td>
</tr>
<tr>
<td>11. TLUU - Two-Dimensional Table Look-Up Routine</td>
<td>386</td>
</tr>
<tr>
<td>12. UNBLOCK - Unblocking Routine for λ's</td>
<td>388</td>
</tr>
<tr>
<td>13. SUMOLA - Linear Combination Routine for λ's</td>
<td>390</td>
</tr>
<tr>
<td>14. PLOT - Point Plot Subroutine</td>
<td>392</td>
</tr>
<tr>
<td>15. MATINV - Matrix Inversion Routine</td>
<td>398</td>
</tr>
<tr>
<td>16. DECID3 - Step Size Routine for Control Systems</td>
<td>400</td>
</tr>
<tr>
<td>17. DECID2 - Arbitrary Decision Routine</td>
<td>406</td>
</tr>
<tr>
<td>18. PACK - Integer Word Conversion Routine</td>
<td>407</td>
</tr>
<tr>
<td>19. WNORM - Weighting Matrix Norm Calculation</td>
<td>409</td>
</tr>
<tr>
<td>20. UPDK - Convergence Control Routine</td>
<td>411</td>
</tr>
</tbody>
</table>

VIII PROGRAM REV

1. CTVSR - Control Variable Routine for REV | 428 |
2. ADJEQ - Adjoint Equations Routine | 434 |
3. UNPART - Unblocking Routine for Partials | 442 |
4. MIMINR - Integration Routine for REV | 444 |
5. WMA - Weighting Matrix Routine | 446 |
6. DALPACK - Blocking Routine for λ's | 453 |
7. FLUSH - Buffer Flush Routine | 455 |
8. IZUNPK - Switch Testing Routine | 456 |

IX PROGRAM GRAPH

1. Mapping Routines | 458 |
2. Arrow, Line, and Point Plotting Routines | 459 |
3. Character Plotting Routines | 459 |
4. Absolute Plotting Routines | 459 |
5. Utility Routines | 460 |
6. Internal Routines | 460 |
7. PAPLT - Parameter Collection Routine | 472 |
8. PPPLT - Partials Collection Routine | 474 |
9. PLTCUR - Microfilm Plotting Routine | 476 |
10. Dummy Plot Routines | 479 |

X DIRECTORY

1. CTAE - Parameter Optimization Control Program | 482 |

XI ALPHABETIC INDEX OF SUBROUTINES

ix
SECTION I
INTRODUCTION

This report describes a generalized digital computer program for the simulation and/or optimization of arbitrarily defined vehicle flight paths. Two simultaneously coupled three-dimensional point mass trajectories about a rotating oblate planet having a multi-layered atmosphere may be employed. Levels of reduced complexity varying from the generalized problem to straightforward planar point mass, single vehicle, vacuum trajectories may be studied with the aid of the program.

The program itself has evolved over a period of some ten years, mainly on the basis of four Air Force Flight Dynamics Laboratory (AFFDL) sponsored contractor research studies. The program has also been supported by National Aeronautics and Space Administration studies at Ames Research Center, Langley Research Center, and the Manned Spacecraft Center and has received wide distribution throughout the aerospace industry.

In addition to the point mass capability, compatible trajectory equation options of increased complexity up to and including a six-degree-of-freedom single vehicle option employing generalized vehicle and planetary characteristics and a generalized trajectory error and dispersion analysis are available from AFFDL.

PURPOSE

The program reported in this document extends the existing AFFDL single-vehicle point mass program to the two-vehicle point mass problem. Specifically, the original program has been extended to provide a generalized two-vehicle (one-on-one) combative engagement simulation and optimization capability. The combative encounter may be defined at several levels of complexity short of differential game formulation including:

OPTION (A): Self-contained role and tactic selection based on relative vehicle states

OPTION (B): Parameterization of one vehicle's role and tactic selection rules followed by the application of multivariable search procedures to obtain the optimal parameter values. This option defines optimal parameters against a specified opponent employing fixed combat logic parameters.
OPTION (C): Parameterization of both opponent's role and tactic selection rules followed by the application of a multivariable saddle point search technique. This option defines a "mini-max" optimal procedure for opponents employing variable combat logic parameters.

OPTION (D): Open loop, continuous control optimization by the variational calculus against an opponent performing a pre-specified maneuver, the "maneuvering target" option.

OPTION (E): Open loop, continuous control optimization by the variational calculus against a reacting opponent employing fixed parameters and self-contained combat tactics.

It should be noted that the formulation and program include as subcases two-vehicle cooperative problems. This leads to

OPTION (F): Cooperative two-vehicle parametric control

OPTION (G): Cooperative two-vehicle open loop continuous control

These last two options permit the optimization of two-vehicle rendezvous problems and are equally applicable to aircraft or spacecraft problems. Single-vehicle problems may also be studied by means of the program. In this reduced mode, both parametric and variational optimization formulations can be employed.
SECTION II

COMPUTER AND SYSTEM REQUIREMENTS

The combat simulation program has been written for use with the CDC 6600 series computer system using the run compiler. Except for three small subroutines, GET, PUT, and OFFSW, the program is written in CDC FORTRAN IV.

Computer resource requirements are:

1. A CDC 6600 computer with 131k (decimal) core
2. A card reader
3. A line printer
4. A card punch (if restart cards are to be punched)
5. Twenty-two tape transports or a disk to simulate magnetic tape
6. A display console (This requirement is omitted when the display subroutine SCOPE is replaced by a dummy subroutine).
SECTION III

PROGRAMMING CONCEPTS

1. The Use of COMMON

Whenever possible, a variable is placed in the FORTRAN "COMMON" area. There are several reasons for this:

a. The communication between subroutines is simplified

b. The structure of the directory is simplified. Since the number of variables in COMMON is quite large, all COMMON cards are not placed in each assembly/compilation. Instead, access to any quantity in the COMMON blocks is through individual "EQUIVALENCE" statements placed in each deck of source cards. This has in a small manner reduced the number of COMMON cards in each deck.

In order that the user may better obtain the required COMMON location for a given variable, a system of COMMON subscripts is used. The first location of COMMON has a subscript of 1; the second, 2, . . . . The listing of the suffix directory can be obtained by a program user if the data quantity "DLIST" is input as 1.0 to the program.

The data for vehicle one is stored in "blank" COMMON. The data for vehicle two is stored in named COMMON/COMMON2/. Blank COMMON and /COMMON2/ each use 3000 core locations. The COMMON subscript of a given variable is the same for both vehicles. For example, bank angle, "BA77D," is the sixty-fourth location of blank COMMON for vehicle one and is the sixty-fourth location of /COMMON2/ for vehicle 2.

2. Table and Table Usage

One of the usual required modifications of any program is the change of table sizes. With this in mind, a COMMON block of locations has been set aside, and the required number of cells required for each table is specified with data (check TABRE for data preparation). This requires no re-assembly or recompilation unless the total number of cells required exceeds the COMMON block. This has been set at 4000 cells for each vehicle. Table data for vehicle one is stored in numbered COMMON /5/, and table data for vehicle two is stored in numbered COMMON /52/.

3. Symbolic Input

Although the FORTRAN system itself has a system of input routines, the program does the actual translation of cards using special coded routines. Input data may be read using a system of symbols which is designed to give engineering meaning to the analyst. The symbols are internally referenced to actual locations by the use of COMMON and subscripts.
4. Trajectory Printing Method

The printing of a trajectory may be divided into five categories:

a. Initial printing - The printing of specific values of the first stage and at each subsequent major stage. Initial print is designed to print certain values which will be constant during the trajectory and serve as a reminder of what values have been used for these constants.

b. Code printing - The printing of codes which will identify the variables which are to be obtained in the coming time history print. Only those variables to be printed in the time history will have a code name printed. All subprograms being used as well as the differential equations routine will print a set of codes.

c. Time history printing - The printing of values specified at the requested points of the trajectory. If a certain variable is not desired as output, it is not printed, and other desired variables are moved in the print format accordingly.

d. Observation functions - A maximum of thirty-two variables for each vehicle may be designated as observation functions. At the end of each major stage, the time history of all observation functions are printed in tabular format. Observation functions may also be plotted on the line printer. The object of observation function printout is the construction of compact histories for the major trajectory variables.

e. Diagnostic error printing - The printing of errors detected by the program.

The entire printing is controlled to print on a page 11 x 14 inches and will print a maximum of fifty-four lines per page. Page ejection and lines control are provided by the subroutines LINES and DEF.

In addition to the above printout, all input data involved for a case may be printed on the output page preceding the computation of the first stage printout. This printout is user-controlled and will be omitted when IPNAML = 0. This print will occur on the first cycle only.

5. Tape Usage

This section will describe the tape usage other than the FORTRAN system. All modification of tapes required may be made with control cards placed in front of the program before submitting to the computer.

<table>
<thead>
<tr>
<th>TAPE</th>
<th>EQUIPMENT</th>
<th>VEHICLE</th>
<th>USAGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tape 5</td>
<td>Disk or tape</td>
<td>1 &amp; 2</td>
<td>Data input</td>
</tr>
<tr>
<td>Tape 6</td>
<td>Disk or tape</td>
<td>1 &amp; 2</td>
<td>Printed output</td>
</tr>
<tr>
<td>TAPE</td>
<td>EQUIPMENT</td>
<td>VEHICLE</td>
<td>USAGE</td>
</tr>
<tr>
<td>------</td>
<td>-----------</td>
<td>---------</td>
<td>-------</td>
</tr>
<tr>
<td>Tape 10</td>
<td>Disk or tape</td>
<td>1</td>
<td>Save the a history for that valid step for use with all trials until another valid step is found.</td>
</tr>
<tr>
<td>Tape 11</td>
<td>Disk or tape</td>
<td>1</td>
<td>This unit is used in the reverse integration to save data for use in computing the mode shape in the control system.</td>
</tr>
<tr>
<td>Tape 12</td>
<td>Disk or tape</td>
<td>1</td>
<td>Partial variables and control variables are written on this unit for use in the reverse integration.</td>
</tr>
<tr>
<td>Tape 13</td>
<td>Disk or tape</td>
<td>1</td>
<td>Target data is written on this tape when using the maneuvering target option.</td>
</tr>
<tr>
<td>Tape 14</td>
<td>Disk or tape</td>
<td>1 &amp; 2</td>
<td>Used to save the AESOP data base for the outer AESOP parameter optimization loop.</td>
</tr>
<tr>
<td>Tape 15</td>
<td>Disk or tape</td>
<td>1</td>
<td>This tape is used for restart cards. Restart cards for the last completed cycle are written on this tape. The program call card may be used to automatically assign this tape to the punch file.</td>
</tr>
<tr>
<td>Tape 16</td>
<td>Disk or tape</td>
<td>1</td>
<td>Used to prepare the input tape in binary for use in the iterative procedure.</td>
</tr>
<tr>
<td>Tape 17</td>
<td>Disk or tape</td>
<td>1</td>
<td>Collects data for plotting in overlay 5, 0 (GRAPH)</td>
</tr>
<tr>
<td>Tape 18</td>
<td>Disk or tape</td>
<td>1 &amp; 2</td>
<td>Save the AESOP parameter and performance history for the summary report at the end of an optimization cycle.</td>
</tr>
<tr>
<td>Tape 19</td>
<td>Disk or tape</td>
<td>1 &amp; 2</td>
<td>Save the AESOP parameter and performance history for the final summary report.</td>
</tr>
<tr>
<td>Tape 20</td>
<td>Disk or tape</td>
<td>2</td>
<td>Same as unit 10.</td>
</tr>
<tr>
<td>Tape 21</td>
<td>Disk or tape</td>
<td>2</td>
<td>Same as unit 11</td>
</tr>
</tbody>
</table>
Tape 22 Disk or tape 2 Same as unit 12.
Tape 23 Disk or tape 2 Same as unit 13.
Tape 25 Disk or tape 2 Same as unit 15.
Tape 26 Disk or tape 2 Same as unit 16.
Tape 27 Disk or tape 2 Same as unit 17.
FILMPL Disk or tape 1 Used by the CDC 280 recorder and display system.

6. Overlay Listing

The following is a list of the overlay structure of the combat simulation program including the main program, subprograms, subroutines, and system routines used. (Note: System routines appear in italics).

OVERLAY 00.00

1. MAIN 2. BDATA1
3. BDATA2 4. BDATA3
5. BDATA4 6. BDATA5
7. BDATA6 8. BDATA7
9. SPRANG 10. MAIN2
11. CHAIN 12. MSGONE
13. MSGTWO 14. SYSTEM
15. FINBIN 16. ACGOER
17. EXP 18. ANALOG
19. SQRT 20. SECOND
21. OUTPIC 22. OVERLAY
23. REWINM 24. OUTPB
25. SIO$ 26. GETBA
27. KODER 28. OVERLOD

OVERLAY 01.00

1. MAIN1 2. READA
3. DORDER 4. PACKL
5. DSERCH 6. STOP1
7. ERERR 8. TSRCH
9. READB 10. MAIN12
11. BARSOP 12. DIPLAC
13. DEF 14. TABRE
15. LINES 16. PACBCD
17. PACKR 18. READ31
19. SVI 20. BIBLOCK
21. SHELL 22. SHELLX
23. READA2 24. DSERCH2
25. TSERCH2 26. READB2
1. EXE
2. DIFEQ
3. MANTGT
4. CTVS
5. IPCS
6. PARTS
7. LINCOM
8. SLACK
9. PENAL
10. FILTER
11. OBSPUN
12. STGSTT
13. EXE2
14. READB
15. EXTRAN
16. T'NGE
17. INTGRT
18. DEF
19. LINES
20. CODES
21. ITEMS
22. COMBAT
23. COMBATT2
24. OBSPUN2
25. MLMINF
26. MLMLT2
27. STGSTT2
28. TIMID
29. VALUES
30. MISCUT
31. MISCUT2
32. GNINED
33. DIFEQ1
34. DIFEQ
35. DIFEQ3
36. DIFEQ4
37. DIFEQ5
38. DIFEQ6
39. STOP1
40. TSEXCH
41. TLUREV
42. ACOS
43. ASIN
44. TIU
45. ATAN2
46. TAN1
47. TIMREV
48. DSEARCH
49. EXERR
50. ONETWO
51. FSUBR
52. FPACK
53. FLUSH1
54. SETGRD
55. PAPERPP
56. MANTGT2
57. CTVS2
58. IFCS2
59. PARTS2
60. LINKCOM2
61. SLACK2
62. PENAL2
63. PITS2
64. FILTER2
65. EXTRAN2
66. READB2
67. INTGRT2
68. CODES2
69. ITEMS2
60. TIMID2
71. VALUES2
72. DETECT
73. ROLE1
74. HLIMIT
75. ANGLES
76. CRATE
77. DETECT
78. ROLE2
79. HLIMIT2
80. ANGLES2
81. CRATE2
82. DSEARCH2
83. TIK001
84. DEQPBE
85. PIQFUN
86. GAMA91
87. DEQBCI
88. DEQBCI
191. IMAINOP 192. WARPS
193. PENULT 194. OPTBA2
195. PGAIN 196. ALFLIM
197. INFAL 198. FESET
199. SAVLAF 200. PATERN
201. ISELECT 202. PSRCH
203. WEIGHT 204. OUTALF
205. OUTFUN 206. PCYCLE
207. FNEVAL 208. FFINAL
209. SUMARY 210. SECCON
211. CREEPR 212. OUTWGT
213. OUTSUM 214. RANDUM
215. BOUND 216. SECTON
217. ASVCK 218. FESAV
219. RGEN 220. SHELL
221. PUNTP 222. STDALF
223. INPUTB 224. BACKSP
225. SINCOS 226. RGBAEX
227. IFENDF 228. OUTPTS
229. SCOPE 230. RGBAEX
231. TAN 232. RGBAEX
233. TANH 234. ATAN
235. ENDFIL 236. CPC

OVERLAY 03.00
1. CTLS 2. CTLS1
3. CTLS2 4. DEF
5. LINES 6. DISPLAY
7. SEARCH 8. STOP1
9. CARDS 10. DALCAL
11. KCALC 12. INVERT
13. DECIDE 14. OFFSW
15. DSEARCH 16. TLUU
17. UNBLOCK 18. SUMOLA
19. PLOT 20. MATINV
21. DECID3 22. DSCID2
23. PACK 24. WNCRM
25. UIDK 26. INPUTB
27. ENDFIL 28. LOCF
29. OUTPTS 30. RGBAEX
31. INPUTS 32. KRAKER

OVERLAY 04.00
1. REV 2. CTVSR
3. ADJEQ 4. DEF
5. LINES 6. UNPART
7. INTGTR 8. TLUREV
9. MIMINR 10. CODES
11. VALUES 12. TLU1
13. WMA 14. DALPACK
15. FLUSH 16. IZUPK
17. STOP1 18. BACKSP
| Overlay 05.00 | | Overlay 06.00 | | Overlay 07.00 |
|----------------|----------------|----------------|----------------|
| 1. GRAPH       | 2. PAPLT       | 1. DGAMES      |
| 3. PAPLT       | 4. FRAME       | 3. STOPI       |
| 5. PLTCUR      | 6. ABSEAM      | 4. INITOP      |
| 7. ABSEVCT     | 8. MAP         | 5. MAINOP      |
| 9. LINEOPT     | 10. CHAROPT    | 6. CODES       |
| 11. SETBEAM    | 12. NUMBER     | 7. CODES2      |
| 13. SYMBOL     | 14. VECTOR     | 8. VALUES      |
| 15. INPUTB     |                | 9. CODES2      |
|                |                | 10. VALUES2    |
|                |                | 11. SADDLE     |
|                |                | 12. PENLY      |
|                |                | 13. SADDLE     |
|                |                | 14. PGAIN      |
|                |                | 15. ALFILIM    |
|                |                | 16. INEVAL     |
|                |                | 17. FRESST     |
|                |                | 18. SAVALF     |
|                |                | 19. PATTERN    |
|                |                | 20. SELECT     |
|                |                | 21. PSRCH      |
|                |                | 22. WEIGHT     |
|                |                | 23. ENDCYC     |
|                |                | 24. FNIEVAL    |
|                |                | 25. OUTALF     |
|                |                | 26. OUTFUN     |
|                |                | 27. SUMARY     |
|                |                | 28. DEF        |
|                |                | 29. SECCON     |
|                |                | 30. MAGNIFY    |
|                |                | 31. STDESC     |
|                |                | 32. CREEPER    |
|                |                | 33. QUADRA     |
|                |                | 34. DAVIDN     |
|                |                | 35. RPOINT     |
|                |                | 36. RANRAY     |
|                |                | 37. RAISEC     |
|                |                | 38. BESOP      |
|                |                | 39. OUTWGT     |
|                |                | 40. OUTSUM     |
|                |                | 41. FCYCLE     |
|                |                | 42. PFINAL     |
|                |                | 43. RANDOM     |
|                |                | 44. BOUND      |
|                |                | 45. SECTON     |
|                |                | 46. DERIV      |
|                |                | 47. WMAT       |
|                |                | 48. INSTID     |
|                |                | 49. ASVCHK     |
|                |                | 50. FESAV      |
|                |                | 51. MINAFL     |
|                |                | 52. ALPERT     |
|                |                | 53. ALFULL     |
|                |                | 54. QUTRAN     |
|                |                | 55. QUADOP     |
|                |                | 56. MAXRDP     |
|                |                | 57. DMATRX     |
|                |                | 58. SAVDER     |
|                |                | 59. RGEN       |
|                |                | 60. RANCOS     |
|                |                | 61. SHELL      |
|                |                | 62. FUNTYP     |
|                |                | 63. STDALF     |
|                |                | 64. MATMLT     |
|                |                | 65. QMXINV     |
| 67. INPUTN     |                | 66. RBAIEX     |
| 69. ENDPIL     |                | 68. OUTPTN     |
|                |                | 70. INPUTB     |
7. Program Organization

The combat simulation computer program is written in CDC FORTRAN IV except for one small display routine OFFSW and two small character manipulation routines GET and PUT. The program takes advantage of the overlay feature to minimize core requirements.

This section describes the overall organization of the program from the viewpoint of control cards, tape usage, and deck setup. The program is broken into eight overlays as follows:

1. MAIN - MAIN zeros out all of the common locations and moves the directory data to common locations.
2. MAIN1 - Does some data initialization and prepares an input tape for use in the iterative procedure.
3. EXE - Solves the equations of motion and computes the partial derivatives.
4. CTLS - To compute the step size and new control variable table for the next trajectory being computed.
5. REV - The reverse integration program computes integrals which determine the mode shape of the changes in the control variables and puts this out on tape for use in CTLS.
6. GRAPH - Dummy
7. DGAMES - Dummy
8. CTAE - Parameter optimization AESOP

a. Storage References

All variables requiring arrays have been arranged in the standard FORTRAN convention. For example, an array \( A_i \) is stored in increasing storage locations for increasing \( i \). Matrices are stored columnwise.

b. Integers

All integers are assumed to be in a 60 bit word right justified.

c. COMMON

In order to decrease the length and time required in calling sequences, liberal use of COMMON has been made. Three types of COMMON are used: blank, numbered, and labeled. For the actual variables and their arrangement in COMMON, the user is referred to the program listing.

d. Variable Names

Because any variable may be referred to by FORTRAN, all integer variable names begin with the leading letters I, J, K, L, M, or N. This
does not mean that all non-integer variable names begin with letters other than I, J, K, L, M, or N. They may, in some subprograms, be declared integer or real.

8. Program Generation, Modification, and Execution

The following examples are designed to aid the user in utilizing the features of the CDC 6000 series computer for modification and execution in the combat simulation program. All examples shown are based upon an overlayed program organized as follows:

```
OVERLAY(TRAJOPT, 0, 0)
MAIN
OVERLAY(TRAJOPT, 1, 0)
MAIN1
OVERLAY(TRAJOPT, 2, 0)
EXE
OVERLAY(TRAJOPT, 3, 0)
CTLs
OVERLAY(TRAJOPT, 4, 0)
REV
OVERLAY(TRAJOPT, 5, 0)
GRAPH
OVERLAY(TRAJOPT, 6, 0)
DGAMES
OVERLAY(TRAJOPT, 7, 0)
CTAE
```

All control cards are left-justified in card column 1. The end of record is a 7, 8, 9 punched in column 1 and an end of file card is a 6, 7, 8, 9 punched in column 1. In the control card examples, an end of record and an end of file will be used in place of these cards.

a. Building the Program Overlay File

In constructing the program overlay file a CDC-developed utility program COPYLIB is used. COPYLIB is a user library simulation copy routine developed by CDC to take most of the work out of building overlay or normal load files. However, COPYLIB is not a standard CDC utility program; hence, a short description is supplied below with examples of its use.

COPYLIB is called by a control card and reads text cards.

(1) Control Card

```
COPYLIB(OUTFILE, LIB1, LIB2, ..., LIBi)
```

where `OUTFILE` is the name of the disk or tape file upon which the output (the program overlay file) is to be written, and `LIB1, LIB2, ..., LIBi` (1 ≤ i ≤ 6) are the names of the user-supplied library files containing subprograms output from a CDC 6600 compiler or assembler in relocatable object form (odd parity).
(2) Text Cards

The order and content of the text cards define the output file. They are free form in columns 1 through 72, blanks ignored. The text cards are listed as follows:

\textit{id}ent

where \textit{id}ent is a subprogram name. The purpose of the \textit{id}ent card is to name the main program. Once the main program name is known, it and all the routines it calls or references and all they call or reference that were available in the library files are copied onto the output file specified.

Usually, only the one card naming the main program need be given except for certain cases such as Block Data routines that are necessary but not specifically called or referenced by any program. (In the case of an otherwise unnamed Block Data routine, the additional \textit{id}ent card would contain only BLKDATA). Another instance might be one in which the order of loading was important to guarantee that the longest named COMMON reference would come first. The order would be forced by the insertion of additional cards containing the names of the routines in the order required.

\texttt{OVERLAY(}fn, \texttt{I1, I2)}

Overlay text cards are necessary to properly define the structure of the file to be built for overlay loading. These cards cause an overlay loader directive record containing all the information on the text card to be written on the output file. The order and form of this text card must be exactly as defined in the Scope Reference Manual or the FORTRAN Reference Manual, with the exception of the starting column.

An \textit{id}ent text card containing the name of the main program in the overlay must follow each overlay text card.

Given correct overlay and \textit{id}ent text cards, COPYLIB will correctly build an overlay structure file; no routine needed or defined in a more fundamental overlay will be placed in a less fundamental level. If an \textit{id}ent card incorrectly attempts to call a routine that has somehow either through a previous \textit{id}ent text card or through a call by a subroutine at that level already been placed in the more fundamental level, the \textit{id}ent card is ignored and an informative diagnostic is printed. It is possible to have several 0, 0 level overlay cards in the text stream if the purpose is to build different overlay structured programs.

\texttt{*WEOF*}

This text card causes an end of file to be written on the OUTPUT file after all the preceding text cards are processed. (A file mark might be
Interesting Details and Limitations

For perhaps 98 per cent of all the times COPYLIB is used, 500000 will be sufficient field length. COPYLIB will abort if the following internal tables overflows:

<table>
<thead>
<tr>
<th>Name of Table</th>
<th>Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Library Subprogram Name</td>
<td>768</td>
</tr>
<tr>
<td>Subprogram Entry Points</td>
<td>1280</td>
</tr>
<tr>
<td>Subprogram External References</td>
<td>3840</td>
</tr>
<tr>
<td>Current Overlay Need Stack</td>
<td>383</td>
</tr>
<tr>
<td>Working Storage Buffer</td>
<td>variable (see below)</td>
</tr>
</tbody>
</table>

The working storage buffer size can be determined by subtracting 405000 from the field length. It is difficult to determine what the minimum size required will be unless the lengths of the relocatable binary records present on the user library files are known. The length of the longest record determines the minimum working storage buffer size. (Note: this length is not the amount of core required to load the subprogram for execution but the number of words output by the compiler or assembler.) In other words, it is proportional to the number of binary cards that would be punched out were the subprogram punched out, not necessarily related to the size of any arrays dimensioned inside the subprogram. This length can be obtained exactly, if necessary, from the information output by a "LIBLIST" of the library files, and should be rounded upward to the nearest 10000 if figuring the minimum field length necessary for COPYLIB.

COPYLIB rewinds each user library file starting with the first mentioned then transfers every routine contained in it to a random access file, rewinds the library file, and then repeats this process with the next user library file mentioned, for every file given.

If during the transfer process a subprogram is found that has a name duplicating one found previously, the latter subprogram is skipped, an informative diagnostic printed, and the process continues. This is handily put to use when one wishes to use a newer version of a routine instead of the version contained in one of the user library files, e.g., by placing the name of the newer library file to the left of the older version, the user causes the duplicate routines on the later file to be ignored.

Entry points must be unique to one subprogram. If two or more have the same entry point names, COPYLIB output may be scrambled. The responsibility for proper overlay text card sequence is entirely the user's. Incorrect sequencing, as defined in the Scope and FORTRAN Reference manuals, will not be flagged until an attempt is made to load the outfile.
The out file is rewound at the beginning and end of COPYLIB. It will be ended with one end-of-file mark unless more are forced through "*WEOF* cards at the end of the text cards.

The random access file mentioned earlier is called RANSCR and must be a disk file. However, at the conclusion of COPYLIB it can be rewound and copied by the normal control cards (REWIND and COPYBF) if the user wishes to save a new version of the user library. This file contains all of the routines found in the library files input to COPYLIB minus any duplicate routines, overlay cards, and compiler or assembler error records.

The present version does not allow the use of INPUT (the card reader) as a library file.

EXAMPLE 1

The initial installation of COPYLIB as a permanent file.

```
RFL,60000.
UPDATE(N,C)
PIN(I=COMPILE)
LOAD(OGO)
NOOG.
CATALG(COPYLIB,COPYLIB,EX=ARC1,
CN=ARC1,MD=ARC1,RP=999)
end of record
   {COPYLIB source deck}
end of record
```

EXAMPLE 2

The initial installation of the COMBAT simulation program.

The FORTRAN source decks are arranged, sequenced, and stored alphabetically. The following deck set up is used for the initial generation of the COMBAT simulator program overlay file NEWPGM on tape ARCO1.

```
REQUEST NEWPGM,H1. (ARCOL/RING)
RFL,60000.
RUN(S,,,,,,77000)
ATTACH(COPYLIB,COPYLIB)
COPYLIB(NEWPGM,OGO)
   {COMBAT source decks arranged alphabetically
```
EXAMPLE 3

Modification of the combat simulation program

The following deck set up is used when making modifications to the combat simulation program.

REQUEST OLDPM,HI. (ARCL/NORING)
REQUEST NEWPM,HI. (ARCO2/RING)
RFL,60000.
RUN(S,...,77000)
ATTACH (COPYLIB,COPYLIB)
COPYLIB(NEWPM, LOG, OLDPM)

Modified COMBAT source decks

end of record

end of file
EXAMPLE 4

The following deck set up is used to modify and execute the combat simulation program.

REQUEST OLDPGM,HI. (ARCO1/RING)
REQUEST NEWPGM,HI. (ARCO2/RING)
REQUEST ABSPGM,HI. (APC03/RING)
RFL,60000.
RUN(S,77000)
ATTACH(COPYLIB,COPYLIB)
COPYLIB(NEWPGM,LOG,OLDPGM)
REWIND(NEWPGM)
RFL,317000.
SET(0)
MODE(1)
LOAD(NEWPGM)
NOGO.
RFL,20000.
REWIND(TRAJOPT)
REWIND(ABSPGM)
COPYBF(TRAJOPT,ABSPGM,1)
REWIND(TRAJOPT)
RFL,317000.
TRAJOPT.
end of record

} Modified COMBAT source decks

end of record

OVERLAY(TRAJOPT,0,0)
MAIN
OVERLAY(TRAJOPT,1,0)
MAIN
OVERLAY(TRAJOPT,2,0)
EXE
OVERLAY(TRAJOPT,3,0)
CTLs
OVERLAY(TRAJOPT,4,0)
REV
OVERLAY(TRAJOPT,5,0)
GRAPH
OVERLAY(TRAJOPT,6,0)
DGAMES
OVERLAY(TRAJOPT,7,0)
CTAE
end of record

{ data deck for COMBAT program

end of record
end of file

18
EXAMPLE 5

The following deck set up is used to execute the combat simulation program from a tape containing the absolute program element.

REQUEST ABSPGM, HI. (ARCO3/NORING)
REWIND(ABSPGM)
REWIND(TRAJOPT)
RFL.20060.
COPYBF(ABSPGM,TRAJOPT,1)
RFL.317000.
MODE(1)
TRAJOPT.
end of record

| data deck for combat simulation program |
| end of record |
| end of file |

(4) Program Call Card

In the two previous examples the combat simulation program was executed by use of the program call card

TRAJOPT.

where TRAJOPT is the name of a disk file that contains the absolute program element. The program call card may also be used to override file name parameters which appear on the program card of the source deck. The file parameters appear as follows:

PROGRAM MAIN (INPUT=1001, OUTPUT=1001, TAPE5=INPUT, TAPE6=OUTPUT,
$ TAPE10=1001, TAPE11=1001, TAPE12=1001, TAPE13=1001,
$ TAPE14=1001, TAPE15=1001, TAPE16=1001, TAPE17=1001,
$ TAPE18=1001, TAPE19=1001,
$ TAPE20=1001, TAPE21=1001, TAPE22=1001, TAPE23=1001,
$ TAPE24=1001, TAPE25=1001, TAPE26=1001, TAPE27=1001, FILMPL=1001)

The restart cards for the combat program are written on TAPE15. The following call card may be used with any 6000 machine which has a card punch and recognizes the PUNCH file to automatically punch the restart cards at the end of the job.

TRAJOPT(,........, PUNCH)
9. Data Format

Card Format - The program input routine (READA) expects the following format.

Card Columns | 1-6 | 7 | 8-10 | 11 | 12-66 | 67-72 | 73-80
Card Field   | I   | II | III  | IV  | V     | VI    | VII

Card Field I  Contains the symbolic name of the variable into which data contained in Field V begins loading.

Example: Card Column 1 12
GAM7D -1.23
SIG7D 90.

Card Field II Not used.

Card Field III Contains the words DEC, OCT, BCD, TRA, INT, PAR, or is blank depending on the type of data to be loaded. The word OCT indicates that the data is to be interpreted as octal numbers. The word BCD specifies that N binary coded decimal words (N punched in column 12) beginning in column 13 are to be loaded. The word TRA denotes to the input routine that all data has been input and to return control to the calling program. The word PAR indicates that the input quantity is to be treated as a free parameter in a multivariable optimization study. The word DEC and blank are equivalent and specifies that data loaded is decimal data.

OCT Example
Card Column 1 8 12
NPOINT OCT 17

BCD Example
Card Column 1 8 12
REM BCD 2

The 2 in column 12 specifies two words where each word is considered to be six characters including blanks. The largest number of six character words that can be loaded from one card is nine. The analysts should be very careful to see that the BCD information does not get punched into Field VI. This will cause an input error.

DEC Example
Card Column 1 8 12
ATABO1 DEC 2,-100.,1.,100.,1.

Note that the first character in column 12 is an integer and the input routine will load only one integer per DEC card and that has to be the first number punched in Field V.
If the above card is punched, the two will now be loaded into the machine as a binary floating-point number. Likewise, the other numbers will be loaded in the same manner with the decimal point assumed right justified.

If anything other than OCT, BCD, INT, TRA, or blank appears in Field II, then the word DEC is assumed.

**INT Example**

Card Column 1  8  12
JPSCUT  INT  1
JPSCUT  1
JPSCUT  INT  1, 1, 1, 1

When the word INT is used, it is assumed that all numbers on the card will be loaded as integers. If only one integer is punched per card, the INT may be punched or omitted.

**PAR Example**

Card Column 1  8  12
GAM7D  PAR  2

The PAR in column 8 indicates that the input quantity GAM7D is a free parameter. The 2 in column 12 indicates that GAM7D is the second free parameter.

**Card Field IV** - Not used.

**Card Field V** - The actual input data to the program is punched in the Field V. DEC, INT, and OCT must always be left adjusted, that is, it must start in column 12 on the input card. All numbers are separated by a "comma," and the field terminates with the first blank. BCD information begins in column 13, and the maximum number of six character words per card is nine. Note that since Field V ends with the first blank, the user may punch any comments in the remainder of the field.

**Card Field VI** - This field specifies the initial subscript of the data in Field V. If this field is blank, an initial subscript of 1 is implied. The subscript may appear anywhere within the field.

**Example**

Card Column 1  12  67
ATABOl  4,0,20.,10.,18. 1 or blank
ATABOl 20.,17.,30.,15. 6
In the example above the integer 4 is loaded into the first cell of the array ATAB01. On the second card 20. is loaded into the sixth cell of the array. The one and six punched in Field VI indicate the subscript for the array ATAB01.

Card Field VII - Not used as far as the input routine is concerned. This may be used as a sequence number for the card.

10. Table Format

The various types of tables used by the program may be classed as follows:

Two dimensional table.

Example
Card Column
TTAB01 1 12
TTAB01 N, t_1, T_1, t_2, T_2, t_s, T_s, \ldots , t_n, T_n

N equals fixed point number equal to two times the number of independent variables. For a 20 point table N would equal 40. The total number of machine cells required for this table is 41.

\( t_i \) = independent variable values
\( T_i \) = corresponding dependent values

N-dimensional table.

Example
Card Column
ATAB80 1 12
IA80X NX
IA80Y NY
ATAB80 X_1, X_2, X_3, \ldots , X_NX
ATAB80 Y_1, Y_2, Y_3, \ldots , Y_NY
ATAB80 C_x=1, y=1, C_x=2, y=1, \ldots , C_x=NX, y=1
ATAB80 C_x=1, y=2, C_x=2, y=2, \ldots , C_x=NX, y=2
ATAB80 C_x=1, y=ny, C_x=2, y=ny, \ldots , C_x=NX, y=ny

NX and NY are fixed point numbers of independent variables. \( C_x=1, y=1 \) \ldots \( C_x=NX, y=ny \) equal values of independent variables. The table subscripts would apply to the N-dimensional table as well as the two dimensional. The total number of machine cells required for an N-dimensional table equal \( X_N(Y_N) + NX + NY \).

Examples

c = f(x,y)  \quad \text{NX points for } x = 2
\text{NY points for } y = 2
Machine cells requires \(2 \times 2 + 2 + 2 = 8\) cells

\[c = f(X, Y, Z)\]

\[\begin{align*}
NX &= \text{points for } X = 20 \\
NY &= \text{points for } Y = 10 \\
NZ &= \text{points for } Z = 15
\end{align*}\]

Machine cells required \(= 20 \times 10 \times 15 + 20 + 10 + 15 = 3045\) cells.

All tables must have at least two points per table. A check for each individual table should be made to see if an indicator is necessary for the program to read the table.

11. **Brief Write-up on System Routines**

This section is a brief write-up of some of the system subroutines used by the CDC 6000 software. Since the system software is in a state of constant change, this information may be of little or no use.

a. **INPUTB**

Only one logical record is read each time INPUTB is called. If the list is longer than the logical record, the excess words in the list are ignored by the routine.

An attempt to read past an end of file will cause a program short. The end of file condition can be cleared by testing for end file after the file mark has been read and prior to another attempt to read.

INPUTB calls routines GETBA (to locate Buffer Argument address), UMERR (to output Unassigned Medium diagnostic), MARKFI (to end file OUTPUT and position file INPUT), and XRCL (to go on Recall while an I/O transmission is in progress and computation can not continue).

b. **INPUTC**

INPUTC handles the I/O transmission for the input to the computer. It calls routine KRAKER to perform conversion.

An attempt to read past an end of file will cause the program to be aborted.

The end of file condition can be cleared by testing for end file after the file mark has been read and prior to another attempt to read. The end file condition for the file INPUT is set by either an end of file mark or a short record (end of logical record).

INPUTC also calls routines GETBA (to locate Buffer Argument address), UMERR (to output Unassigned Medium diagnostic), MARKFI (to end file output and position file INPUT on program abort), and XRCL (to go on Recall while an I/O transmission is in progress and computation can not continue).
c. **INPUTS**

INPUTS does the core to core transmissions. It calls routine KRAKER to perform conversion.

The parameter specifying the record length may be an arbitrary number of BCD characters less than 150. The record starts with the leftmost character of the location specified by Format and continues ten BCD characters per computer memory word for the BCD characters or until a zero character is encountered. If the record ends in the middle of a word, the remaining characters are ignored. Each record begins with a new computer word. The number of records processed by each call to INPUTS depends on the format and the length of the list. If the number is greater than 150 characters, the routine aborts the program and gives a diagnostic.

INPUTS also calls routines CONADD (to convert the calling address) and MARKFI (to end file OUTPUT and position file INPUT).

d. **KODER**

KODER is a data conversion routine. The necessary conversion is specified by a Format. Any transmission of data is handled by the routine making the call to KODER.

KODER calls routines CONADD (to convert the calling address) and MARKFI (to end file OUTPUT and position file INPUT on the program abort).

e. **KRAKER**

KRAKER is a data conversion routine. The necessary conversion is specified by a Format. KRAKER is a DECODE conversion routine, and KODER is an ENCODE conversion routine.

KRAKER calls routines CONADD (to convert the calling address) and MARKFI (to end file OUTPUT and position file INPUT on program abort).

f. **OUTPTB**

OUTPTB does the I/O for binary output. One logical record is written each time OUTPTB is called; to decrease the number of I/O transmissions, data should be blocked in large arrays before outputting to some I/O device.

OUTPTB calls routines GETBA (to locate Buffer Arguments address), UMERR (to output error message), and XRCL (to go on recall while an I/O transmission is in progress).

g. **OUTPTC**

OUTPTC does the I/O transmission for the output file. The information is stacked into a buffer, and I/O is done when the buffer is filled. It calls KODER for data conversion. For the output file only, a line count is kept, and, if this count is exceeded, it causes an abort.

OUTPTC also calls routines GETBA (to locate Buffer Argument address), UMERR (to output error diagnostic), MARKFI (to end file OUTPUT and position
file INPUT on program abort, and XRCL (to go on recall while an I/O transmission is in progress).

h. **OUTPTS**

OUTPTS performs the reverse of INPUTS. ENCODE routine makes use of OUTPTS where DECODE routine calls INPUTS.

OUTPTS also calls routines CONADD (to convert the calling address) and MARKFI (to end file OUTPUT and position file INPUT).

i. **STOP**

STOP flushes the buffer and places a file mark on the files named OUTPU and PUNCH if they were declared on the Program Header Card.

j. **END**

The purpose of END is to position the file named INPUT to the beginning of the next logical record if it has not been so positioned by the program and if it has been declared on the Program Header Card.

k. **EXIT**

EXIT enters a dayfile message with the name of the routine and, for END and STOP, follows the routine name with an actual number if one appeared on the source statement.

No other files are terminated or positioned by these routines. It is the programmer's responsibility to insure that other buffers are flushed and that their files are properly terminated or positioned at the end of a program.

12. **ENCODE/DECODE**

ENCODE and DECODE are system routines and are comparable to the BCD write/read statements with the essential difference that no peripheral equipment is used in the data transfer. Information is transferred under Format specifications from one area of storage to another.

Entry is made to the routines by the following statements:

```
ENCOD(C,N,V)LIST
DECODE(C,N,V)LIST
```

where N is a Format statement number, a variable identifier, or a formal parameter representing the associated Format list. LIST is the input/output list. V is a variable identifier or an array identifier that supplies the starting location of the records. The identifier may be subscripted.

C is an unsigned integer or an integer variable, simple or subscripted, specifying the length of a record. C may be an arbitrary number of BCD characters. The first record starts with the leftmost character of the location specified by V and contains BCD characters.
a. **ENCODE**

ENCODE converts the information in the list according to Format list N and stores it in locations starting at V,C BCD characters per record. If the Format list attempts to convert more than C characters per record, a diagnostic occurs. If the number of characters converted by the Format list is less than C, the remainder of the record is filled with blanks.

When C is not a multiple of four, the last record does not fill a computer word; the remainder of the word is blank-filled.

b. **DECODE**

DECODE converts and edits information from records consisting of C consecutive BCD characters starting at Address V according to Format list N and stores it in the I/O list. When the Format list specifies more than C characters per record, a diagnostic is provided. If DECODE attempts to process a character illegal under a given conversion specification, a diagnostic occurs. When fewer than C characters are specified, the remainder of the word is ignored.

Since these routines are system routines, no flow charts will be furnished, and all diagnostics will come from the FORTRAN system.
SECTION IV

MAIN PROGRAM AND SUBROUTINE MAIN2

1. MAIN and MAIN2

The MAIN program is a requirement of the CDC system. When called by the system, all of Blank and Numbered COMMON is zeroed. The MAIN program may consist of as many subroutines as necessary. The only functions that MAIN serves to this program besides meeting the system requirement is to move the vehicle table directory from Labeled COMMON to Numbered COMMON to initialize program block data, to initialize the random number generator, and to call MAIN2.

Subroutine MAIN2 moves the vehicle 2 table directory from Labeled COMMON to Numbered COMMON.
MAIN

CALL FTNBIN (1,0,0)

CALL BDATA1
CALL BDATA2
CALL BDATA3
CALL BDATA4
CALL BDATA5
CALL BDATA6
CALL BDATA7

OPTIMA=2

MAXT3=MXT

DO 20 I = 1, MAXT

STAB3(I)=STABLE(I)

RSTART=RUNIF(110)

CALL MAIN2

ICHAN3(2)=1

CALL CHAIN(1)

RETURN

MAIN2

MAXT3=MXT

DO 20 I=1,MAXT

STAB3(I)=STABLE(I)

RETURN

Initialize random number generator

Initialize second vehicle
2. **BDATA1 - Block Data Subroutine**

   This block data subroutine establishes all basic directory available maneuvers.

3. **BDATA2 - Block Data Subroutine**

   This block data subroutine establishes all data table names.

4. **BDATA3 - Block Data Subroutine**

   This block data subroutine establishes control variable table names CTABLE and DALAL1, for vehicle 1.

5. **BDATA4 - Block Data Subroutine**

   This block data subroutine is a dummy routine.

6. **BDATA5 - Block Data Subroutine**

   This block data subroutine establishes control variable table names CTABLE and DALALF for vehicle 2.

7. **BDATA6 - Block Data Subroutine**

   This block data subroutine establishes all additional directory variable names.

8. **BDATA7 - Block Data Subroutine**

   This block data subroutine sets all AESOP parameter optimization variables.

9. **SPRANG - Random Number Generator**

   Random number generator for AESOP program. See Volume IV.
10. **CHAIN - Overlay Control Program**

**Purpose:**
Controls program overlay structure.

**Method:**
CHAIN controls the following seven program overlays:

- **OVERLAY 1,** MAIN-MAIN PROGRAM FOR TRAJECTORY CALCULATION
- **OVERLAY 2,** EXE-EXECUTIVE PROGRAM FOR TRAJECTORY CALCULATION
- **OVERLAY 3,** CTLS-VARIATIONAL OPTIMIZATION CONTROL PROGRAM
- **OVERLAY 4,** REV-TRAJECTORY REVERSE INTEGRATION
- **OVERLAY 5,** GRAPH-GRAPHICAL ROUTINES
- **OVERLAY 6,** DGAMES-DUMMY OVERLAY
- **OVERLAY 7,** CTAE-PARAMETER OPTIMIZATION CONTROL

**Usage:**
Entry is made to the routine with the following statement:

```
CALL CHAIN(N)
```

where

- \( N \) = Overlay number to be loaded
11. **MSGONE - Combat Message Subroutine, Vehicle 1**

Preserves the current combat message for vehicle 1. Message is subsequently printed by EXE.

```
MSGONE
   DO 10 i = 1, 6
   MSG1_1 = MSG1
   10 CONTINUE
   RETURN
```

12. **MSGTWO - Combat Message Subroutine, Vehicle 2**

Preserves the current combat message for vehicle 2. Message is subsequently printed by vehicle 2.

```
MSGTWO
   DO 10 i = 1, 6
   MSG2_2 = MSG1
   10 CONTINUE
   RETURN
```
SECTION V
PROGRAM MAIN1 AND SUBROUTINE MAIN12

This program is executed once per case. The nominal values are set, and subscripts to BCD word input are searched for. DATA2 is read in, and a tape is prepared in binary to be read again in program EXE for each trajectory. DATA1 is read in this chain and never read again for that case. The MAIN1 program determines whether or not the two vehicle option is requested (INDNOM=2) and whether or not a variational optimization formulation option is to be employed (OPTIMA=2).

Subroutine MAIN12 performs the MAIN1 function for vehicle 2. However, since MAIN12 is only called when a second vehicle exists, the test for a second vehicle is omitted. Again, since a variational option is requested, it must be exercised through the first vehicle; the variational test is omitted from MAIN12.

A flow chart for MAIN1 follows; MAIN12 is identical to MAIN1 with the exceptions noted above.
1. **READA and READA2- Input Routines for Vehicle 1 and Vehicle 2 Data**

**Purpose**

To provide a general method of reading a variable field data card and assigning variable length table. Data may be read into symbolic locations in memory.

**Method**

Decimal, Octal, and Integer numbers are converted to binary integers. BCD information is stored in six character words.

**Card Formats**

The variable name punched in columns 1-6 is the location into which the first data word will be loaded. The variable field information is for re-location. A fixed point integer punched anywhere in the field (67-72) will be treated as a subscript to the variable name punched in column 1-6. Negative integers punched in columns 67-72 will be in violation of the subroutine. The first blank character found in the card to the right of column 12 terminates loading from the card. One exception to this is BCD data. Nine 6 character words may be loaded including blanks.

The general character of the data to be loaded is determined by a three letter pseudo-operation punched in columns 8-10. The pseudo-operations are: DEC or blank, OCT, INT, BCD, PAR, and TRA. The pseudo-operation TRA is a method of exit from the subroutine.

**Decimal Data**

Decimal data beginning in column 12 and ending in column 66 is converted to binary and loaded into the symbolic location punched in column 1-6 subscripted by the integer punched in column 67-72. Signs are indicated by + and - preceding the number. All unsigned numbers are treated as positive. If either the characters E or . or both appear in the decimal data word, the word is converted to a floating binary number. The decimal exponent used in the conversion is the number which follows immediately after the character E. This number may have a + or - sign preceding it. If the character E does not appear the exponent is assumed to be zero. If a decimal point does not appear it is assumed to be at the right of the number. Unless it is the only word or the first word on a card then it is assumed to be an integer.
All the examples below are equivalent.

1. 12.345E03
2. 12.345E03
3. 12.345E3
4. 12345E00
5. 12345.
6. 1,234,5E4
7. 1234,500E-02
8. +123,450OE-2

Note that in the examples above all decimal words have decimal points. If the first word on a card, or if it happens to be the only word on a card and it does not contain a decimal point, the word will be converted to binary integer.

**Octal Data - OCT**

The Octal data is loaded the same as decimal data but must have OCT punched in column 8, 9, and 10. All data is converted to binary with binary point assumed at the right end of each word.

**Hollerith Data - BCD**

Hollerith information is loaded from column 13 through 66 and assigned consecutive locations for every 6 characters. A maximum of nine 6 character words may be punched on any one card and the number of words must be punched in column 12. A subscript may also be punched in column 67-72.

**Transfer - TRA**

The purpose of the TRA card is to transfer control from the subroutine back to the main program. TRA must be punched in column 8, 9, and 10. The subscript field is not used. A REWIND may be punched beginning in column 12. Only the R is checked and the only use is for the rewind of a data tape.

**Integer - INT**

Integer data begins in column 12 and ends in column 66. INT is punched in column 8, 9, and 10. It may be relocated with respect to the BCD name by punching a subscript integer in column 67 through 72. If only one data word is punched per card, column 8, 9, and 10 may be left blank.

**Parameter - PAR**

Integer data begins in column 12. PAR is punched in columns 8,9, and 10. It may be relocated with respect to the BCD name by punching a subscript integer in columns 67 through 72.

**Error Messages**

A message is written on the output tape describing the type of error encountered. If an error is encountered, execution of the case is deleted and the subroutine only searches for other possible errors in the data.
The following error messages are possible.

1. Symbol not in directory.
2. Column 12 is blank.

If a bad pseudo-operation is punched in column 8, 9, and 10 the subroutine will treat it as decimal data.

All checking for redundancies, end of tape, format errors, etc., is handled by FORTRAN system input/output routines.

Usage

No initialization is required, the entry is established by a:

    CALL READA  or  CALL READA2

Subroutines called and used by READA and READA2 other than normal FORTRAN system routines.

    DIPLAC  DSERCH(2)  PACBCD
    DEF     PACKR      SVI(2)
    TABRE(2) READ31
    LINES   BIBLOCK

Data Preparation

The first card expected by READA or READA2 is a

    STCASE TAB

with the $S$ beginning in column 1 and $TAB$ punched in 8, 9, and 10. Following this card is a set of cards which define the table sizes necessary for that case.

Example: TTAB01  10

    TTAB02  20

On the above example TTAB01 is punched beginning in column 1. The numbers 10 and 20 are punched in column 12 and indicate the number of machine cells necessary for that table. Any number of tables may be assigned as long as the total number of machine cells does not exceed 4000. Follow all table assignments with a TRA punched in column 8, 9, and 10. The next data required by the subroutine is DATA2 (this is data that is read at the beginning of each trial and valid step) this may be made up with any combination of OCT, BCD, INT cards. All this data is written on a data tape and reserved for future use. If the last TRA card has a $R$ punched in column 12 this data tape will be rewound as soon as the test is made. This is not necessary for the program to work, just more efficient if used.
The next set of data expected by the subroutine is LATAL (this is data which is only read one time per case). This data should begin with:

**STCASE**   **DATA1**

The **STCASE** is punched beginning in column 1 and **DATA1** beginning in column 12. This data is terminated with a **TRA** beginning in column 8.

A flow chart for **READA** is provided. Subroutine **READA2** is identical to **READA** except for the **COMMON** block, tape units, and auxiliary routines employed.
2. **DORDER - Directory Order Output Routine**

**Purpose:**

To provide an ordered listing of the directory on user request.

**Method:**

When the input DLIST = 1, an ordered directory listing is output ahead of the trajectory print. The directory is first sorted in numerical order and printed; then it is sorted in alphabetic order and printed. The sort routines SHELL and SHELLX perform the numeric and alphabetic sorts, respectively.

**Remarks:**

It is assumed that vehicle 1 and vehicle 2 directories are identical; hence, only one directory order output routine is provided.
PACKL - Pack Routine

Purpose:
This routine packs two words into one.

Method:
The routine takes the first five characters of one word and the first character of the second word and packs this into one word.

Usage:
Entry is made to this routine by the following statement:

CALL PACKL (A, ADOT, D)

where,

A = the five character word.
D = the single character word.
ADOT = the result of the packed word.

This subroutine uses ENCODE which is a system subroutine. For more information, check ENCODE write-up.
DSEARCH and DSEARCH2 - Directory Search Routine for Subscripts

Purpose:

To provide a method of searching the directory to find the subscript corresponding to a BCD argument.

Method:

The routine searches the directory for the exact BCD name required by the argument. When an equal compare has been found, the corresponding subscript is returned as a fixed point integer. An error message will result if the BCD name is not in the directory.

Usage:

Entry is made to the routine with the following statement:

CALL DSEARCH (SYM,LOC,ICOM)

where

SYM = BCD name being searched for.

LOC = The location the corresponding subscript will be stored in.

ICOM = Error code in case a compare is not found.

If an error occurs in the BCD name, LOC is set to zero. Location ICOM is set to one and a message is printed stating that the BCD name is not in the directory.

No subroutines are called from these subroutines.

Subroutine DSEARCH2 is identical to DSEARCH except for the COMMON blocks employed. A flow chart of DSEARCH is provided.
5. **STOP1 - General Stop Routine**

**Purpose:**
To print out a stop number and return to the next case.

**Method:**
To initialize ICHAIN, print a stop number and return the program to segment MAIN1 for re-initialization for the next case.

**Note:** STOP1 was used for the name of this routine because there was a system routine by the name of STOP.

**Usage:**
Entry is made to this routine by the statement:

```fortran
CALL STOP1
```

If this routine is called a statement is printed:

```fortran
STOP LINK N
```

where,

- \( N = \) The segment link STOP1 was called from

<table>
<thead>
<tr>
<th>Segment</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>NADNI</td>
<td>1</td>
</tr>
<tr>
<td>HXX</td>
<td>2</td>
</tr>
<tr>
<td>CTLCS</td>
<td>3</td>
</tr>
<tr>
<td>ERP</td>
<td>4</td>
</tr>
<tr>
<td>GRAPH</td>
<td>5</td>
</tr>
<tr>
<td>DGAMES</td>
<td>6</td>
</tr>
<tr>
<td>CTAE</td>
<td>7</td>
</tr>
</tbody>
</table>

Subroutines LINKS, CHAIN and Normal I/O FORTRAN routines are called from this routine.
STOP 1

STOP 2

STOP 12

Stop Link
ICHANNEL(1)

CHAIN(1)

RETURN
6. **EXERR - Error Routine**

**Purpose:**

To provide a method of printing a stop number code and ending the execution of a given case.

**Method:**

The routine obtains the required stop number from the calling program, prints it, and calls the routine **STOPL**. The statement **STOP NUMBER XXX** is printed.

**Usage:**

Entry is made to this routine by the statement:

```
CALL EXERR(N)
```

where N is the stop number desired to print.

This routine calls **STOPL** and the normal I/O FORTRAN routines.

```
EXERR
  \arrow{WRITE}{6,2}
  \arrow{CALL STOP1}
  \arrow{RETURN}
```
7. **TSRCH and TSRCH2 - Directory Search for Table Subscript**

**Purpose:**
To provide a method of searching the directory for table subscripts.

**Method:**
The routine searches the directory for the exact BCD name required by the argument. When an equal has been found the corresponding subscript is returned as a fixed point integer.

**Usage:**
Entry is made to the routine with the following statement:

```
CALL TSRCH (SM2,LOC2,N2,IER)
```

where

- **SM2** = BCD name of argument.
- **LOC2** = Location of first subscript.
- **N2** = Number of sequential subscripts to return with.
- **IER** = Error Code:
  - IER is set to a plus 1 if the BCD argument does not compare.
  - IER is set to a minus 1 if the BCD argument does compare.

No other subroutines are called from these subroutines.

**TSRCH2** is identical to **TSRCH** except for the COMMON blocks employed. A flow chart for **TSRCH** is provided.
TSRCH

DO 1000 I = 1, MAXT

SYMS ¥ STABLE (1)

F

JM = 1

DO 500 J = 1, N2

LOCZ(J) = LOCZ(JM)

500

JM = JM + 1

IER = -1

CONTINUE

1000

IER = -1

RETURN

53
8. **READB and READB2 - Binary Stage Data Input Routines**

**Purpose:**
To read the stage data from the data tape (TAPE16 or TAPE26).

**Usage:**

CALL READB (ISFIN)

ISFIN is returned with the following value:

ISFIN = 0 always.

ISFIN = -10 data for the last stage has been read.

READB rewinds TAPE16 when the data for the last stage has been read. For each call to READB, the stage data for one stage is read in. Stage data is ordered sequentially on TAPE16 in the order that the stage data appears in the input deck.

READB may be called only after READA has been called once, since READA prepares TAPE16 (via the ad-hoc blocking routine BIBLOCK).

READB2 is identical to READB except for the tapes and COMMON blocks employed. A flow chart for READB is presented.
READ8

REWRITE 14
READ(14) ADATA

Read a record of stage data from unit 16

END-OF-FILE ON UNIT 16
YES

EXIT

End-of-file on unit 16 from READ8

II(1)
.GT.
0
YES

set selected trajectory data from ABSSP parameters

II(1)
.LT.
0
NO

REWIND 16

IIID
.EQ.
2
NO

ENTRY SETIAD

.SUMM
.EQ.
2
YES

RETURN

set ABSSP data base for internal loops

55
9. BAESOP - Parameter Optimization Input Subroutine

**Purpose:**

To read in the parameter optimization program AESOP, Volume IV, input data.

**Method:**

Data is read in conventional FORTRAN NAMELIST manner. NAMELIST name is TAESOF.
10. **DIPLAC - Integer Shift Routine**

**Purpose:**

To let the routine right justify a number so that the displacement (col. 67-72) on an input card may be punched anywhere in the field.

**Method:**

The displacement field is read into the machine with an A format and right justified before the conversion is made to a binary integer.

**Usage:**

Entry is made to this routine with the following statement:

```
CALL DIPLAC (RAl, INC, BLANK)
```

where,

- **RAl** - The six character BCD array.
- **INC** - Location that the converted integer will be stored in.
- **BLANK** - Blank character used for comparing.

**Subroutines Called:**

```
PACKR    READ31
```
11. DEF and DEF2 - Heading and Page Eject

Purpose:
To provide page ejection and title print.

Method:
Initially the current page number (NPAGE) is incremented by 1.
The page is ejected and return is made to the calling program.

Usage:
Entry is made by the following statements:

CALL DEF           or           CALL DEF2

Only the normal I/O FORTRAN routines are used with this routine. DEF2
is an entry point used by vehicle 2.
12. **TABRE and TABRE2 - Table Dimension Subscript Routines**

**Purpose:**
This subroutine is called from **READA** or **READA2** and computes subscripts such that the table dimension requirements may be variable.

**Method:**
Uses input data prepared by the user to compute subscripts for variable table assignments.

**Usage:**
This subroutine is called from subroutine **READA** or **READA2** one time per case and linkage is obtained by:

```
CALL TABRE (TABSTP)
```

where **TABSTP** is an indicator set false by **TABRE** or **TABRE2** when **READA** or **READA2** will not recall **TABRE** or **TABRE2**.

**Subroutines Called:**
- **DIPLAC**
- **LINES**

**Error Messages:**
1. Symbol does not exist in table list.
2. Total table size $N$ exceeds maximum size $N_i$ where $N$ is the required and $N_i$ is the maximum.

**Data Preparation:**
Control will be transferred to subroutine **TABRE** or **TABRE2** when **READA** or **READ** processes a control card:

```
STCASE TAB
```

**STCASE** beginning in column 1 and **TAB** punched in column 8, 9 and 10. Following this card will be the cards requesting table sizes.

```
TTABOL 10
ATABOL 20
```

**TTABOL** and **ATABOL** punched beginning in column 1 and the required machine cells (10 and 20 in this case) punched beginning in column 12. Anything punched past column 15 will not be used. After all table assignments a TRA should be punched in column 8, 9 and 10.
TABRE

TAGETUP = TRUE

DO 5   I=1,MXT

I=I+1

READ

CALL DPICR.

CALL READ.

SYNTR.A = SCERA

CALL LRES

CALL LRES

END IF.

CONTINUE

TAGETUP = TRUE

CALL LRES

RETURN

DO 50  I=1,MXT

IF (CRI) = RIGHT

S = RIGHT

RETURN

DO 50  I=1,MXT

IF (CRI) = RIGHT

S = RIGHT

RETURN
13. **LINES and LINES2 — Lines Accounting Routines**

**Purpose:**
To keep an accounting of the number of lines printed per page, and to provide for page control.

**Method:**
If the number of lines to be printed (LCOUNT) is such that it will not fit on the current page, the page is ejected (via DEF) and printing will begin on the new page. Initially, the location LONG, should be set to zero, indicating that currently no lines have been printed on the present page.

**Usage:**
Entry is made to the routine by the following statement:

```
CALL LINES (LCOUNT)  or  CALL LINES2 (LCOUNT)
```

where,

LCOUNT = A fixed point variable or constant indicating the number of lines to be printed.

Subroutine DEF is called from this routine. LINES2 is an entry point used by the second vehicle.
LINES, LINES2

LONG = LONG + LCOUNT

LONG < 54

F

CALL DEF

T

RETURN

LONG = LCOUNT

RETURN

RETURN
14. PACBCD - Packs Six Character Words

Purpose:
To pack BCD words into six character words.

Method:
The first character is converted to an integer by the system routine, DECODE. This integer is the number of six character words contained on the card. ENCODE is then used to pack that number of six character BCD words.

Usage:
Entry is made to this routine by the following statement:

```
CALL PACBCD (RA,FI,JJ)
```

where,

RA - is the first location of the array being converted.
FI - is the first location where the results will be stored.
JJ - is the number of six character words.

This subroutine uses ENCODE and DECODE which are system routines. For more information, check write-up for ENCODE and DECODE.
PACBCD

DECODER
1, 5, RA, JJ

K1 = 2
KK = 7

DO 10 I = 1, JJ

ENCODE
10, 1, PI(i)
RA(

K1 = K1 + 6

10

KK = KK + 6

RETURN

65
15. **PACKR - Packs BCD Characters**

**Purpose:**
Packs BCD Characters into words.

**Method:**
This routine uses ENCODE to convert BCD information to a binary integer. No I/O transmission takes place.

**Usage:**
Entry is made to this routine by the statement:

```plaintext
CALL PACKR (I1,I2,N)
```

where,

- **I1** - Contains the BCD integers to be converted.
- **I2** - Location of where converted numbers are to be restored.
- **N** - Number of words to be converted.

This routine uses ENCODE which is a system routine. For more information check ENCODE write-up.
PACKR

\[ k = 20 - N \]

ENCODE
\[ 10, 1, \text{XMAT} \]
\[ k, N \]

ENCODE
\[ 20, \text{XMAT}, 12 \]
\[ i1(i) \]

RETURN
16. READ31 - Binary Conversion Routine

Purpose:
To convert from BCD to Octal, Floating Point and Integer numbers.

Method:
This routine takes the BCD display code and converts it to the necessary binary data depending on the operation code.

Usage:
Entry is made to this routine by the following statement.

CALL READ31 (IFI, FJ, FI, JJ)

where,

IFI - is a code that determines if its Octal, Floating Point or Integer conversion.
FI - is the location where the answers are stored.
FJ - contains the BCD characters to be converted.
JJ - the number of words to be converted.

This subroutine uses the system routine DECODE. For more information on DECODE check the write-up for DECODE.
17. **SVI and SVI2 - Block Save Routines**

**Purpose:**

To place a number of variables into an array. The location of each piece of data is contained in an array. The routines also equate data flagged by the PAR input subject to the appropriate optimizing parameter.

**Method:**

Each piece of data is picked up sequentially beginning with A and stored into an array beginning with the subscript ISTART.

**Usage:**

Entry is made to the routine with the following statement.

```
CALL SVI (ICOM,N,ISTART,A, IA,PAROPT)
```

where,

- **ICOM** = Type of data being saved.
- **N** = Number of words being saved.
- **ISTART** = Common subscript for A.
- **A** = Location where value is being moved from.
- **IA** = Optimization parameter suffix area.
- **PAROPT** = Flag indicating data is to be set equal to an optimizing parameter.

No other routines are called from this routine.

Subroutine SVI2 is identical to SVI except for certain COMMON blocks. A flow chart is presented for SVI.
SVI

\[ J = \text{ISTART} \]
\[ K = \lfloor z \text{COM} / 4 + 1 \rfloor \]

\[ \text{PHASE,} \]
\[ \text{PHASE,} \]
\[ \text{PHASE,} \]

\[ \text{DATA } (3) = \text{ALPHA} (3) \]
\[ J = J + 1 \]
\[ \text{for } I = 1, N \]

\[ \text{RETURN} \]

\[ K \]

\[ \text{TABLE } (3) = \text{ALPHA} (3) \]
\[ J = J + 1 \]
\[ \text{for } I = 1, N \]

\[ \text{RETURN} \]

\[ =1 \]

\[ =2 \]

\[ =3 \]
18. **BIBLOCK - Data Output in Blocks**

**Purpose**
To prepare and output data in large blocks rather than a card at a time.

**Method**
These dimension arrays are used by this routine to input data too. The data is read into the machine in BCD and then decoded depending on the pseudo-operation punched on the card. After decoding all data is treated as integers, then stored in one of the three dimension arrays. Just prior to this call, a subscript is stored which defines which cell in the array the number will be stored into when it is read back into the machine. When either of three buffers are filled, all three buffers are flushed out on tape. If any of the buffers fail to have anything stored in it a dummy cell is set up. This is necessary because of the way the Fortran system works. It is impossible to store zero words on tape.

**Usage**
Linkage is made by the following call:

```
CALL BIBLOCK(IID,JJ,FI,ITABLE)
```

where
- **IID** = the subscript which relocates the integer in core.
- **JJ** = the number of integers to be stored in the array.
- **FI** = the integer to be stored in array.
- **ITABLE** = contains a number defining which of the three arrays to store into. In this case ITABLE is either 0, 1, or 2.

No initialization or printing is necessary for this routine.

**Subroutines Called**
The only routines called are the normal output FORTRAN routines.
BIBLOCK

Diagram showing a flowchart with various conditional statements and loops.
19. SHELL - Numeric Sorting Subroutine

Purpose:
To store an array in ascending order.
SECTION VI
PROGRAM EXE AND SUBROUTINE EXE2

EXE is the executive program that drives both vehicle forward trajectories. EXE controls the major logical decisions that must be made. The subprograms of EXE are responsible for accomplishing the calculations which fall into their respective domains of specialization. Since, during any one call, it is not feasible for a subprogram to do all types (e.g. initialization, printing, function calculations, etc.) of computations delegated to it, the subprograms are segmented into functional units; access to a particular functional unit of a subprogram is accomplished by calling that subprogram with an argument called the entry point. For most of the subprograms of EXE there is the following correspondence between entry points and functional units:

<table>
<thead>
<tr>
<th>Entry Point</th>
<th>Functional Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>pre-data initialization (to be done at the beginning of each trajectory before data is read)</td>
</tr>
<tr>
<td>2</td>
<td>post-data initialization and/or initial transformation (to be done at the beginning of each stage after data is read)</td>
</tr>
<tr>
<td>3</td>
<td>main calculation (e.g. calculate derivatives)</td>
</tr>
<tr>
<td>4</td>
<td>initial print; generally this is for print of that which is calculated at entry point 2.</td>
</tr>
<tr>
<td>5</td>
<td>code print; to identify the values printed at entry point 6.</td>
</tr>
<tr>
<td>6</td>
<td>value print; for printing time history of variables calculated during trajectory.</td>
</tr>
<tr>
<td>7</td>
<td>for specifying variables that are to be integrated. Each variable that is to be integrated should have its derivative computed at entry point 3.</td>
</tr>
<tr>
<td>8</td>
<td>h-transformation (or miscellaneous chores)</td>
</tr>
</tbody>
</table>

In addition to the so called "standard subprograms" of EXE there are a few which are of such a special nature that the standard entry points no longer apply, or else perhaps an additional entry point is included for some
special purpose. Those subprograms which have multiple entry points which deviate from the standard are MINDINF, INTGRT, EXTRAN, PLTS, MANTOT, and EXE2.

The structure of EXE is integral with the structure for accomplishing the numerical integration. This is necessitated by the premise that EXE should have control. As a result, the numerical integration routines, MINDINF, is a slave to EXE. The relationship between MINDINF and EXE differs distinctly from that of the standard subprograms and EXE. The MINDINF writeup contains a complete description of the entry points and their respective functions. EXTRAN is a special subprogram which is in reality a subdriver for accomplishing the initial transformation and the h-transformation.

One great benefit of this type of organization of EXE is that it is general; any trajectory program may be set up this way. In particular, this fact was used for the programming of the reverse trajectory. REV is the executive program that drives the reverse trajectory and hence the structure of REV is virtually isomorphic to EXE.

Communication between EXE and its subprograms is accomplished by setting indicators. However, of all the indicators used in EXE proper, EXE sets most of them itself. The following is a list of all those indicators that are set by subprograms of EXE for the purpose of communication with EXE proper.

<table>
<thead>
<tr>
<th>Indicator</th>
<th>Subprogram</th>
</tr>
</thead>
<tbody>
<tr>
<td>MINDPAS</td>
<td>MINDINF and MINDINF2</td>
</tr>
<tr>
<td>MINDPA3</td>
<td>MANTOT</td>
</tr>
<tr>
<td>INGHOM</td>
<td>STUTST and STUTST2</td>
</tr>
<tr>
<td>INDSTG</td>
<td>any subprogram (denotes error)</td>
</tr>
<tr>
<td>IWDSTG</td>
<td>STUTST and STUTST2</td>
</tr>
<tr>
<td>LOOK</td>
<td>STUTST and STUTST2</td>
</tr>
</tbody>
</table>

One of the most critical functions of EXE is to control the integration step size. EXE itself actually does very little of the calculation for the step size. Yet, it governs the sequence of calls that are made to subprograms which determine a step size to meet their respective requirements. EXE must then weigh each factor against the other and select that step size which is "most reasonable". A summary of the step size control procedure follows:

The logic in EXE that controls the integration step size, HO, during the forward trajectory is necessarily somewhat complicated because of all the factors that have to be considered. "Staging" and/or "time points" may require the step size to be either cut back or increased. Depending on the situation the integrated variables may have to be backed up one step.

MINDINF(5) and MINDINF2(5) are the entries to the integration routines which check the truncation error; STUTST(3) and STUTST2(3) are the entries to the stage test routines which check the staging variable (s) to see when they pass from one side to the
other of their respective staging values. The MININF and STGTEST writeups should be referred to if it is desired to know how these routines determine the step size when they are granted this responsibility.

The following points summarize the logic involved in controlling the step size:

1. An integration step is a "trial step" until it has been accepted as valid by MININF(5), MININF2(5), STGTEST(3), and STGTEST2(3).

2. If MININF(5) or MININF2(5) rejects the trial step, then the integrated variables are backed up one step, and a new trial step is made with the step size (HO) which MININF(5) and MININF2(5) have determined.

3. Only after MININF(5) and MININF2(5) accept a trial step does STGTEST(3) and STGTEST2(3) have the opportunity to reject it. If STGTEST(3) or STGTEST2(3) reject a trial step, then the integration is backed up one step, and a new trial step is made with the step size (HO) which STGTEST(3) or STGTEST2(3) have determined.

4. It is assumed that the HO determined by (2) or (3) when a trial step is rejected, is less than the HO which produced the bad step.

5. After a valid integration step has been taken, the next time point, TIMPT, is picked up. TIMPT will be the first time point greater than TIMES + AMINT.

6. The next trial step must have an HO ≤ TIMPT - TIMES.

7. After a valid step, the HO for the next trial step will have been determined or at least sanctioned by MININF(5) and MININF2(5). Paragraph (6) merely imposes a further condition in addition to MININF(5) and MININF2(5).

8. Once staging has started; i.e., once STGTEST(3) or STGTEST2(3) has rejected a trial step, MININF(5) and MININF2(5) will be passive. This means that MININF(5) and MININF2(5) accept every trial step and compute no new HO.

9. MININF(5) and MININF2(5) have sole control over increasing the step size HO; MININF(5) or MININF2(5) may increase HO only if they accept the trial step and are not passive.

10. The above procedure insures that all time points are hit, and that variable step integration does not interfere with the staging process.

It should be noted that EXE drives the second vehicle trajectory through EXE2. This routine is virtually a copy of EXE. However, correct interfacing of the two vehicle trajectory integration procedures has required EXE2 to be split into a sequence of entry points. Each entry point carries out a well defined function for Vehicle 2's trajectory control. Control of integration stepsize for both trajectories is carried out by EXE itself.
A flow chart for program EXE is presented. Subroutine EXE2 follows the general computational flow of program EXE. However, the COMMON blocks, tapes, and subroutines employed are differentiated from those of EXE by the numeral 2. For example, COMMON/1/ becomes COMMON/12/; DIFEQ becomes DIFEQ2; and tape 12 becomes tape 22.
1. **DIFEQ—Differential Equation Selector**

**Purpose:**
To enable the user to select which set of differential equations will be used by the program.

**Usage:**

```
CALL DIFEQ(IENTRY)
```

`IRETRY` = indicator which determines what task is to be performed by the differential equations subprogram which will be called by DIFEQ.

`INDSEL` is of the form `10j`. `j` determines which differential equations subprogram will be used. `INDSEL` is nominally 101, so for this `INDSEL`, `j` = 1 and DIFEQ1 will be used.

**Remarks:**

DIFEQ calls EXE, EXTRAN, and PTBQON.

DIFEQ calls DIFEQ1, DIFEQ2, DIFEQ3, DIFEQ4, DIFEQ5, DIFEQ6, and STOP.

`i` determines which control system will be used. It should be noted that in the combat simulation, the first vehicle equations of motion are contained in DIFEQ1, and the second vehicle equations of motion are in DIFEQ2.

DIFEQ3, DIFEQ4, DIFEQ6

These are dummy routines included so that the user may write his own differential equations for use with the optimization program.

In writing a new differential equation subprogram, the entry point pattern established by EXE for such a subprogram must be adhered to. DIFEQ1 and DIFEQ5 are examples of such subprograms.
2. **MANTGT and MANTGT2 - Maneuvering Target**

**Purpose:**

To prepare a target tape containing the time history of a "target trajectory."

To read the target tape as a function of time during a forward trajectory and to compute functions of the variables read from tape or in COMMON together with the variables of the current trajectory.

**Method:**

This subprogram has all the standard entry points of EXE, except that entry point 8 is unique, in that it prepares a target tape.

INDICP = 0: No computations made.

INDICP = 1: A target tape will be prepared; the target tape is TAPE 13. The information put on this tape is the values of the following variables:

\[ \text{TIME, } XE77F, YE77F, ZE77F, UE77F, VE77F, WE77F, UE77Fl, VE77Fl, WE77Fl}. \]

At entry point 1 the tape is rewound and INDPAK is set to 0 (this deletes computation of partials). At entry point 8 the tape is written. None of the other entry points will be effective. EXE proper calls MANTGT (8) at every (ITCNT+1)th valid integration step. ITCNT is input. It is assumed that only a forward trajectory is to be run for a case with INDICP = 1 in the data. This trajectory should be set up to terminate on TMAX.

INDICP = 2: It is assumed that a target tape (TAPE 13) has been prepared by a previous case run with INDICP = 1 (or 3) in the data. During each forward trajectory of the present case, the target tape will be read so that the value of trajectory time of the present case is bracketed between the trajectory time of two adjacent records on the target tape. The instantaneous value of the variables on the target tape are estimated by linear interpolation. Then the necessary functions are computed from these interpolated values and the information available from the present trajectory. Code and value printing of the computed quantities are accomplished at entry points 5 and 6 respectively.
Remarks:

It must be known that the values of TIME on the target tape exceed the largest value of TIME that will be encountered on all trajectories of a case with INDICP = 2.

TIME should be a state variable when INDICP = 2.

INDICP = 3:

This option is designed for the purpose of running a standard case, without maneuvering target, for INDCYC cycles and then defining the last cycle as a target trajectory to be put on the target tape exactly as if INDICP were input as 1. On the last cycle, at MANTGT (1), TMAX is set to TMAX and NCYCLE is set to 0 and INDICP is set to 1 so that the case will terminate just as if one trajectory with INDICP = 1 were run; however, this will not be done until INDPAR has been set ≠ 0 on the last cycle.

The following basic functions are computed at MANTGT (3): (see formulation manual for detail)

\[ \Delta X_E \]
\[ \Delta Y_E \]
\[ \Delta Z_E \]
\[ \Delta X_E \]
\[ \Delta Y_E \]
\[ \Delta Z_E \]
\[ \Delta V \]
\[ \Delta R \]
\[ \bar{V} \cdot \bar{R} \]
\[ \left| \bar{V} \right| \]
\[ \left| \bar{R} \right| \]

\[ \theta_{ASP} \]
\[ \phi_{LA} \]
\[ \sigma_{vA} \]
\[ \sigma_{vL} \]
\[ \Delta \sigma_{LOS} \]
\[ \Delta Y_{LOS} \]

Coordinate differences of the two vehicles
Velocity differences of the two vehicles
Rate of change of \( |R| \)
Aspect angle
Lead angle
Heading of lead angle vector
Heading of line-of-sight vector
Heading error from line-of-sight path
Inclination error from line-of-sight path
In addition, the following missile calculations are made:

- $\Delta \sigma_{LA}$: Heading error from lead angle path
- $\Delta \gamma_{LA}$: Inclination error from lead angle path
- TC: Time to kill

In addition, the following missile calculations are made:

- $R_{\text{min}}$: Minimum missile range
- $R_c$: Range to kill zone
- $\epsilon_{SE}$: Allowable steering error

The input data for MANTGT calculations may consist of:

- INDICP: Option indicator
- ITCONT: Skip indicator
- AC: Arrays of missile range constants
- BC: 
- C1C: Allowable steering error constants
- C3C: 
- D1C: Missile minimum range constants
- D2C: 
- D3C: 
- $R_{\text{MAX}}$: Missile maximum range constants
- DLVMF: Missile $\Delta V$
- GTAB01: Two dimensional table for multiplier in steering error calculation.

A flow chart for MANTGT is presented. MANTGT2 is identical except for use of vehicle 2 COMMON blocks, tapes, and auxiliary subroutines.
3. CTVS and CTVS2 - Control Variable Routine for EXE

Purpose:
During the forward trajectory, to obtain the instantaneous values of the control variables as a function of stage time; to obtain values of the initial conditions at the start of stage 1; to define points in stage time which must be hit in the corresponding stage of the reverse trajectory.

Control Variables

CTABLE is an array of NPOINT stage time values and the corresponding values of the MCONT control variables. The format of the CTABLE array is:

<table>
<thead>
<tr>
<th>t₁</th>
<th>a₁</th>
<th>t₂</th>
<th>a₂</th>
<th>⋯</th>
<th>aMCONT</th>
</tr>
</thead>
<tbody>
<tr>
<td>NPOINT</td>
<td>NPOINT</td>
<td>NPOINT</td>
<td>NPOINT</td>
<td>NPOINT</td>
<td></td>
</tr>
</tbody>
</table>

At CTVS(3), the task of this routine is to interpolate in the CTABLE to obtain the current values of the control variables. This is accomplished trivially by calling the interpolation routine TLIU. CTVS(3) does not allow values of the control variables that exceed the upper or lower boundaries (CTABUB, CTABLB) which may be input for the respective control variables.

CTABLE will be considered to contain stage time values unless INDCTA is 0. When a new CTABLE is prepared (in DALCAL) INDCTA is set to 1; hence on all trajectories after the nominal, CTABLE will contain stage time values. For the nominal trajectory CTABLE may be defined as a function of trajectory time if INDCTA is input 0 in stage 1 data. If the range of the CTABLE for a stage is exceeded, the pertinent end points will be used as the values of the control variables.

Tape Usage

In order that the CTABLE for a particular stage be available for CTVS(3), it must be read from tape before CTVS(3) is first called. This is the task of CTVS(2). For the nominal trajectory, the CTABLE exists in the data; hence after the stage data has been read the CTABLE for that stage may be assumed to be available for CTVS(3). On all trajectories after the nominal, the CTABLE for each major stage resides on tape IATAP. Furthermore, the stages exist in inverse order on IATAP; hence to get the proper stage from IATAP, CTVS(2) does a BACKSPACE, HEAD, BACKSPACE at the beginning of each major stage. It is assumed that IATAP has not been rewound since it was last written (in DALCAL). The information on IATAP is not for the exclusive use of CTVS; in fact, each logical record on IATAP contains much more information than just the CTABLE for that stage.
The complete format of each logical record of IATAP is described in the write-up of the routine (DALCAL) which prepares IATAP.

Initial Conditions

The values of the INDIOP initial conditions (which are not specified categorically in the stage 1 data) may be perturbed from trajectory to trajectory in a manner analogous to the way the control variable values in the CTABLE are perturbed. VALINS is the array of these initial conditions. VALINS is read from IATAP at the same time the CTABLE for stage 1 is read. Hence, at CTVS(2), after IATAP has been read for stage 1, the values in the VALINS array are given to the respective initial conditions. On the other hand, for the nominal, the VALINS array is initialized with the nominal values of the initial conditions specified in the stage 1 data. Just as with the control variables, the values of the initial conditions are not allowed to violate their respective upper or lower boundaries (VALIUB, VALILB).

Time Points

When partials are being computed (INDPAR /= 0), CTVS(3) makes a call to TDREV in order to attempt to insert the current stage time value into the array of points which must be hit in the corresponding stage of the reverse trajectory.

However, the tolerance DELTSA is used in the call to TDREV. This means the points stipulated by CTVS(3) may be no closer than DELTSA from any other point which has already been stipulated as one which the reverse trajectory must hit. The motivation for this feature is to enhance the performance of the variable step integration option by preserving the CTABLE at every point used to generate a trajectory (using DELTSA = 0). DELTSA may be input. It is nominally 1000.

CTVS has the standard entry points. Entry points 2 and 3 have been described in detail above. Code and value printing of the control variables is done at entry points 5 and 6 respectively.

Remarks:

CTVS2 obtains instantaneous values for the second vehicle control variables as a function of stage time, obtains initial second vehicle conditions at the start of stage 1, and defines points in time which must be put in the corresponding points in time of the reverse trajectory. CTVS2 is identical to CTVS except for the use of Vehicle 2's COMMON blocks, auxiliary routines, and tapes. A flow chart of CTVS is presented.
4. IFCS-In-flight Constraints (Boundary Violation Routine)

Purpose:

To calculate the instantaneous boundary violations of given functions and to integrate each of these violations.

IFCS is a subprogram of EXE; it has all the standard entry points. Up to six functions may be specified for IFCS; this is done in the data. If no functions are specified then IFCS is not active.

Method:

The instantaneous violation of the ith IFCS function is computed at entry point 3 as:

\[ \hat{A}_{\text{IFCS}_i} = \begin{cases} \max [0, (y_i - P_i (x_i))]^{\text{INDBND}_i} & \text{if INDBND}_i > 0 \\ \min [0, (P_i (x_i) - y_i)]^{\text{INDBND}_i} & \text{if INDBND}_i < 0 \end{cases} \]

where \( y_i \) is the value of the i'th variable listed in the BFCDV array
\( x_i \) is the value of the i'th variable listed in the BFCDV array
\( P_i \) is the function tabulated as a two dimensional table on the i'th PSTAR data card(s).

\( \text{INDBND}_i \) is an indicator which is input > 0 to define an upper boundary; and which is input < 0 to define a lower boundary.

At entry point 7, the violation \( \hat{A}_{\text{IFCS}_i} \) is integrated.

The names ascribed to the respective violations and their integrals are, in order:

<table>
<thead>
<tr>
<th>Violations</th>
<th>Integrated Violation</th>
</tr>
</thead>
<tbody>
<tr>
<td>AIFCS1</td>
<td>AIFCS</td>
</tr>
<tr>
<td>BIFCS1</td>
<td>BIFCS</td>
</tr>
<tr>
<td>CIFCS1</td>
<td>CIFCS</td>
</tr>
<tr>
<td>DIFCS1</td>
<td>DIFCS</td>
</tr>
<tr>
<td>EIFCS1</td>
<td>EIFCS</td>
</tr>
<tr>
<td>FIFCS1</td>
<td>FIFCS</td>
</tr>
</tbody>
</table>

The first IFCS function for which no computation is requested terminates the list of those IFCS functions for which computations will be made.
Remarks:

IFCS2 calculates instantaneous boundary violations of given functions and their integrals for vehicle 2. A program modification is required to permit specification of second vehicle in-flight constraints in cooperative variational optimization. IFCS2 is identical to IFCS except for the use of the second vehicle's COMMON blocks and auxiliary routines. A flow chart for IFCS is presented.
5. PARTS—Partial Derivatives

Purpose:
To obtain all necessary partial derivatives and put them on the partial tape (TAPE12); also, to transmit information from the forward trajectory to the reverse trajectory by putting it on the partial tape.

Methods:
This subprogram has the standard entry points of all the other subprograms of EXE. The calculation of a particular matrix of partials is accomplished by a call to PSUBR; the particular matrix desired is completely specified in the arguments to PSUBR.

The partials to be computed are:

- $R = \left[ \frac{\partial x_i^0}{\partial x_j^0} \right]$ initial conditions
- $P = \left[ \frac{\partial x_i}{\partial x_j^0} \right]$ h-transformation
- $F = \left[ \frac{\partial x_i}{\partial x_j} \right]$ beginning of a stage
- $G = \left[ \frac{\partial x_i}{\partial \alpha_j} \right]$ during a stage
- $\Phi = \left[ \frac{\partial \Phi}{\partial x_i} \right]$ terminal partials
- $\Psi_k = \left[ \frac{\partial \Psi_k}{\partial x_i} \right]$ PARTS (3) at the end of every major stage
- $\Omega = \left[ \frac{\partial \Omega}{\partial x_i} \right]$ terminal partials
- $\Phi = \dot{\Phi}$
- $\Omega = \dot{\Omega}$
- $\Psi_k = \{ \dot{\Psi}_k \}$
\( \Phi, \dot{\Phi}, \) and \( \{\psi_k\} \) are computed by the chain rule:

\[
\dot{\Phi} = \left[ \frac{\partial \Phi}{\partial x} \right] \{\dot{x}_1\} + \frac{\partial \Phi}{\partial t} 
\]

this is valid since \( \Phi = \Phi(x, t) + C \)

It may be necessary to modify the terminal partials at the end of a stage. If the contribution to the payoff at the end of a given stage is 0, then \( \{\frac{\partial \Phi}{\partial x_i}\} \) and \( \Phi \) are set to 0. Likewise if the contribution to the \( i \)th constraint at the end of stage \( i \) is 0, then \( \frac{\partial \psi_i}{\partial x} \) and \( \psi_i \) are set to 0.

These conditions are determined by the values of \( \text{JPHCUT} \) and \( \text{JPSCUT} \) respectively. For the payoff, the contribution is 0, if \( \text{JPHCUT} \leq 0 \). For the \( k \)th constraint the contribution is 0, if \( \text{JPSCUT}_k \leq 0 \). the analyst has control of \( \text{JPHCUT} \) and \( \text{JPSCUT}_k \) in the input data.

At PARTS (3) a call to TIMREV is made (with 0 tolerance) to define the current stage time as a point which must be hit in the corresponding stage of the reverse trajectory.

At PARTS (2), the \( R \) matrix is calculated at the first stage only (and then only if it is needed). At the beginning of any stage after the first, the \( P \) matrix is calculated but only if it is actually needed. The \( R \) matrix and the \( P \) matrix are put on the partial tape directly within PARTS. The \( F \) matrix, the \( G \) matrix, all terminal partials and other information for reverse is put on the partial tape via the ad-hoc blocking routine PRPACK.

At PARTS (4), the \( R \) matrix or the \( P \) matrix is printed (if it has been computed).

At PARTS (5), code printing is done for the \( F \) and \( G \) matrices.

At PARTS (6), the values of the \( F \) and \( G \) matrices are printed; at the termination of a stage the terminal partials are printed also.

The information (besides the partials) which is transmitted to reverse is:

- \text{TIMES} Stage time
- \text{ND} Indicator determining beginning and type of a major stage.
- \text{ALPHC} Current values of control variables.
- \text{DELT.R} Integration step size for reverse.
INDWMA Weighting matrix option for reverse.
WAI Weighting matrix parameters.
WBI Weighting matrix parameters.

This information is put on the partial tape every time an F and a G matrix are put on the tape.

**Saving α - Points**

There are several ways of preserving the α history which generates a given trajectory. (there will be no reason to preserve the α history on a trial trajectory). The success of the program will depend to some extent on the accuracy in preserving the α-history of a given cycle.

The (TIMES) history exists in tabular form (CTABLE) as a function of stage time for each major stage. During the numerical integration of the forward trajectory the CTABLE is sampled (by some given interpolation formula) at the various points in stage time dictated by the particular numerical integration method. It is only this sampled version of the α-history which determines the trajectory. Hence to preserve the α-history which generated the trajectory it is only necessary to preserve the corresponding sample of the CTABLE that was used.

There are basically three options available for preserving the α-histroy.

**Option I:**

The α-history is preserved at those points in the forward trajectory where partials are computed, and only at those points.

**Option II:**

The α-history is preserved at those points in the forward trajectory where partials are computed (as in Option I), and in addition a subset of the sample points used to effect the numerical integration; the subset is determined as follows:

An α point is preserved if it is no closer than a distance of DELTSA away from the previous α point which was preserved. (distance means distance in stage time). The α time points are preserved in strictly monotonically increasing order; if for any reason the integration is backed up, all α-time points that might have been accumulated in the back-up interval are annihilated.

**Option III:**

Use Option I on the nominal (i.e. first cycle of a run) and Option II on all others.
Every $\alpha$-time point which is preserved in the forward trajectory will be hit in the reverse trajectory and a corresponding $\delta \alpha$ will be produced at this point.

Observations and Remarks

(1) Option I accomplishes precisely what the program has always done.

(2) Option I is a special case of Option II (with $\text{DELTSA} = \infty$). In fact this is the way Option I is selected.

(3) Option II still can fail to preserve all the $\alpha$-history that was used to generate a trajectory even when $\text{DELTSA} = 0$. This may happen because the integration step size control logic has a part in determining the trajectory; if we cannot reproduce the exact step size control logic on the next cycle with a $\delta \alpha$ history identically 0, then we cannot reproduce the same trajectory. Now a trial integration step which was rejected on the nominal does not have an $\alpha$-time point associated with it. Hence this $\alpha$ point was not preserved; hence the next cycle might not obtain the same $\alpha$ value for this point and hence the trial integration step which was rejected on the nominal may be accepted on the next cycle.

(4) A remedy to the problem in (3) would be to have an Option that would preserve every $\alpha$-time point even if it were associated with an integration step that was rejected. However, it is questionable whether the problem is of that much importance.

(5) When utilizing vehicle 2 functions in a cooperative variational optimization problem, care must be taken to insure that

(a) The second vehicle function has a unique name assigned in the vehicle 1 directory.

(b) Appropriate transformations are available in ONETWO and TWOONE.
PARTS (4)

ACCOUNT FOR LINES

PRINT: "PARTS"

PRINT VALUES:
FMATX
i = 1 → NSTATE
j = 1 → NSTATE

PRINT VALUES:
GMATX
i = 1 → NSTATE
j = 1 → MCONT

INDSTG

(INDSTG ≠ 0 AND INDSTG ≠ 1)

NO

ACCOUNT FOR LINES

PRINT: "TERMINAL PARTIALS"

PRINT: "PARTOM"
PRINT VALUES:
PARTOM
i = 1 → NSTATE

PRINT: "PARTPH"
PRINT VALUES:
PARTPH
i = 1 → NSTATE

PRINT: "PARTPS"
PRINT VALUES:
PARTPS
k = 1 → INDPSM
l = 1 → NSTATE

RETURN
6. **LINCOM and LINCOM2 - Linear Combination Routines**

**Purpose:**

To compute new functions as linear combinations of existing functions.

\[ \xi^* = \sum_{i=1}^{n} c_i \xi_i \]

where the \( \xi_i \) are existing functions, the \( c_i \) are fixed coefficients, and \( \xi^* \) is the new function.

**Method:**

The \( c_i \) and the \( \xi_i \) for a particular \( \xi^* \) are specified in the data — the \( c_i \) are input directly; the \( \xi_i \) are input as BCD names, and hence the names for the \( \xi_i \) must be in the directory.

Up to five different linear combination functions, \( \xi^* \), may be defined this way. For each \( \xi^* \), \( n \) must be \( \leq 3 \). If a linear combination is desired with more than three component functions \( \xi_i \), then it must be defined as a linear combination of already computed linear combinations (as will be illustrated in the examples below).

The names of the five available linear combination functions are ALINK, BLINK, CLINK, DLINK, and SLINK. The names of the cost vector for the above linear combination functions are, respectively, ACOST, BOOST, CCOST, DCOST, ECOST. ALINK through BLINK are computed in alphabetical order.

**Example 1:**

To define a linear combination \( \xi^* = (1)h + (2)Vg \), the following input data is sufficient:

```
BLINC BCD 2H up 77F V 777F
BOOST 1., 2.
```

**Example 2:**

To define a linear combination \( \xi^* = (5.2)W + (6.5)h + (2.0)AIFCS + (10.7)V \), the following input data is sufficient:

```
ALINC BCD 3WAC 77P HGC 77P AIFCS
ACOST 5.2, 6.5, 2.0
BLINC BCD 2ALINK V 777777F
BOOST 1., 10.
```
Example 3:

To define a linear combination $\xi = (1/2)m_1 + (1/2)m_2 + h_2$ where $m_1$ denotes the mass in the first stage, $m_2$ denotes the mass in the second stage and $h_2$ the altitude in the second stage, the following data is sufficient:

Stage 1

\[
\begin{align*}
\text{ALINC BCD LAMASS} \\
\text{AOOST} & .5 \\
\text{ALINC BCD Lb}
\end{align*}
\]

Stage 2

\[
\begin{align*}
\text{BLINC BCD 3ALINKbAMASSbHGC7F} \\
\text{BOOST} & 13.5,1.
\end{align*}
\]

Hence, at the end of the last stage, BLINC will be the average of the mass at the termination of the first stage and the last stage plus the altitude at the end of the last stage. Note that when a linear combination function is "blanked out" in the data, the value of that function remains constant.

This subprogram has all the standard entry points. However, entry points 4, 5, 6, and 7 are vacuous. That is, no printing of the values of the linear combinations is done; also, nothing is integrated.

It is well to note that it is possible to take linear combinations involving in-flight constraints and also to take in-flight constraints of linear combinations. The reason is that LINCOM(3) is called before IFCS(3) from EXE.

Remarks:

LINCOM2 computes linear combination functions for the second vehicle. The use of second vehicle linear combination functions in cooperative variational optimization problems will require a program modification. LINCOM2 is identical to LINCOM except for the use of the second vehicle's COMMON blocks and auxiliary subroutines. A flow chart for LINCOM is presented.
7. **SLACK and SLACK2 - Slack Variable Routines**

**Purpose:**

To make available "slack" variables that may be used for various effects including optimal staging and optimizing or constraining the initial value of a variable.

**Method:**

The four slack variables, FLUXA, FLUXB, FLUXC, FLUXD, and their respective derivatives, FLUXA1, FLUXB1, FLUXC1, and FLUXD1, are available. SLACK has all the standard entry points, however, some of the entry points are vacuous.

The first $|\text{INDFLX}|$ slack variables are integrated; $|\text{INDFLX}|$ is input. If $\text{INDFLX} = 0$, no slack variables are integrated. FLUXEQ is an array of BCD names; the BCD name in FLUXEQi equates the ith slack variable with the initial value of that variable. (i.e., the value at the beginning of stage 1.)

Code and value printing of the first $\text{INDFLX}$ slack variables and their derivatives is done if and only if $\text{INDFLX} > 0$.

All variables are nominally 0; FLUXEQ is nominally blank.

**Remarks:**

SLACK2 defines slack variables for the second vehicle. Before use of the second vehicle's slack variables in a cooperative variational optimization problem, a program modification equating the second vehicle's slack variables to names in the first vehicle's directory is required. SLACK2 is identical to SLACK except for the use of the second vehicle's COMMON blocks and auxiliary subroutines. A flow chart for SLACK is presented.
8. **PENAL and PENAL2 - Penalty Function Routine**

**Purpose:**

To compute a penalty function using the values of the variables, \( \bar{v}_i \), whose names are listed in the ENDCON array and/or values \( \bar{v}_i^* \) that have been accumulated at previous stage points for these variables in the PSSTAR table.

**Method:**

PENAL is a standard subprogram of EXE. PENAL will be effective if and only if MAXIM or MINIM contains the name "PNALTY". PNALTY is the name of the function that will be computed at entry point 3:

\[
PP = \sum_{i=2}^{IIIPMT} w_i (\bar{v}_i^* - \bar{v}_i)^2
\]

where \( W_i \) are weights (WGTSI) and

\[
\bar{v}_i^* - \bar{v}_i = \bar{v}_i - \bar{v}_i \quad \text{if} \quad JPSCUT_i = 1
\]

\[
\bar{v}_i^* - \bar{v}_i \quad \text{if} \quad JPSCUT_i < 0
\]

\[
1 \quad \text{if} \quad JPSCUT_i = 0
\]

The - sign is used if the name "PNALTY" is in MAXIM. The + sign is used if the name "PNALTY" is in MINIM.

The weights \( W_i \) may be input or may be controlled by some logic in the control system. JPSCUT_\( i \) is the array of indicators that indicate the stage point to which the corresponding \( \bar{v}_i \) function applies. \( \bar{v}_i \) is an element of the PSSTAR table and is the value of \( \bar{v}_i \) at the most recent stage point for which JPSCUT_\( i \) = 1.

Code and value printing are done at entry points 5 and 6 respectively. The value of PNALTY will be printed.

**Remarks:**

1. WGTSI and DSINL are two names for the same array.

2. Note that the number of functions is taken to be IIIPMT. (This is set in MAIN1.)

3. The penalty function must be computed when using control system CTLS2. Thus, when using CTLS2, MAXIM or MINIM must contain the name "PNALTY", the variable being maximized or minimized must appear as the first name of the ENDCON array and the remaining names of the ENDCON array must be those variables that are being constrained.
4. PENAL2 creates a penalty function from the second vehicle variables, $\Psi_i$. Use of the second vehicle's penalty function in cooperative variational optimization will require a program modification. PENAL2 is identical to PENAL except for the use of the second vehicle's COMMON blocks and auxiliary subroutines. A flow chart for PENAL is presented.
9. PLTS and PLTS2 - Data-Gathering Routine

**PURPOSE:**

To record the time histories of a set of prescribed variables on a tape to be used later (GRAPH segment) for plotting.

**Method:**

The following assumptions are made

1. The variable whose time histories are to be saved are input (PLOTS card(s)).
2. The time histories are to be saved for each pass up to the sixth without requiring the tape.
3. The F and G matrix time histories are to be saved on the last forward trajectory of a cycle on a **different** tape than the other variables.
4. Saving of the F and/or G should be done as an option based on the value of the indicator INDFAG.

Tape 17 is used for the regular variables.
Tape ILTAP is used for the F and/or G.

**Entry Point 1:** Number of points for a trajectory is zeroed.

**Entry Point 2:** Tape 17 is written. NPASS, INDSTG and the point number for the pass, MPT (NPASS), are put on tape 17 along with the values of the variables that have been specified.

**Entry Point 3:** Tape ILTAP is written only if INDFAG ≠ 0. NPASS, INDSTG, the point number (MPTFAG) and TIME are put on ILTAP. In addition the following is put on ILTAP depending on the value of INDFAG:

\[
\begin{align*}
\text{INDFAG} &= 1 \quad \text{FMATX} \\
          &= 2 \quad \text{GMATX} \\
          &= 3 \quad \text{FMATX and GMATX}
\end{align*}
\]

Entry point 2 is called by EXE after every (IGCONT+1) valid integration steps. Entry point 3 is called by EXE after the F and G are computed. IGGONT may be input.

Up to 40 variables may be specified in the PLOTS array by BCD names. Only distinct variables are written on tape. This means that if a variable is specified twice in the PLOTS array, its value will be put on tape only once per record.
The LPLT array is set up in MAIN. LPLT is either the COMMON subscript for the name in PLOTS or is a negative integer j where j points to the cell in the LPLT array which contains the COMMON subscripts for the name in PLOTS. PLTS2 performs the PLTS function for vehicle 2.
10. OBSFUN and OBSFUN2 - Observation Function Routine

Purpose:
To provide an organized time history output of selected trajectory variables, the observation functions.

Method:
Input data defines a set of observation functions for each vehicle. Time histories of these variables are organized and printed in a compact form at set intervals of time. Selected observation functions may also be plotted on the printer using the printer-plotter routine, PAPERP.

Remarks:
A flow chart for OBSFUN is presented. OBSFUN2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary routines.
generate plot frame
LNUM = number of curves
on this frame
NUMP = number of points on
each curve

IS: ISS + 1

YES

NO

I = I + 1

IF (LNUM = 0)
I = 0

ISS = I

YES

NO

I = I + 1

(OBSPLT(I) .EQ. 0)

(LNUM = LNUM + 1)

I .LT. 120

generate plot frame
LNUM = number of curves
on this frame
NUMP = number of points on
each curve

IS: ISS + 1

YES

NO

I = I + 1

(OBSPLT(I) .EQ. 7777)

C

(LNUM .LT. 1)

C

(LNUM .LT. 1)

C

119
11. FILTER and FILTER2 - Repeater Routines for h-Transformation

**Purpose:**

To detect if a change has been made in the value of a prescribed \texttt{COMMON} variable and if a change has been made to produce either the original or the altered value when asked to do so.

**Method:**

There are three entry points to FILTER.

- **FILTER (1):** The current values are saved; a filter is laid over each variable.

- **FILTER (2):** Altered values of variables that are trapped in the filter are saved; the original values of the variables are restored.

- **FILTER (3):** A variable for which there is an altered value is set equal to the altered value.

If FILTER (1) is ever called, FILTER (2) must be called before the values being filtered are ever used. FILTER (3) may be called any number of times after FILTER (1) and FILTER (2) have been called. FILTER (3) is the entry point which reproduces the detected change. FILTER (1) and FILTER (2), in conjunction, detect the change.

The variables to be filtered are prescribed by putting their \texttt{COMMON} locations successively into the cells of the name-common block/\texttt{FILTER/}. At most 14 variables may be filtered.

**Remarks:**

FILTER2 detects changes in the value of specified second vehicle \texttt{COMMON} variables. FILTER2 is identical to FILTER except for the use of vehicle 2's \texttt{COMMON} blocks. A flow chart of FILTER is provided.
13. **STGTST** and **STGTST2** - Stage Testing Routine

**Purpose:**

1. To determine if the trajectory should be terminated (i.e., $\Omega_1 = \bar{\Omega}_1$).
2. To determine if a stage should be terminated (i.e., $\Omega_i = \bar{\Omega}_i$ for $i = 2, \ldots, 4$).
3. To determine an integration step size to use to achieve condition (1) or (2).
4. To communicate the information that is gleaned to EXE proper for the appropriate action.

This subprogram has the standard entry points. Code and value printing are used only for diagnostic purposes and are called if and only if INDSTG is input $\neq 0$.

Up to four variables may be prescribed for terminating the trajectory or the stage by the BCD names in the array CUTOFF. The respective values of these variables at which termination is desired appear in the array CUBAR.

**Termination Criteria**

1. $|\Omega_1 - \bar{\Omega}_1| \leq 10^{-6}|\bar{\Omega}_1| + 1$
2. it is not the first point of a major stage.
3. if $i = 1$ or $\text{TIME} \geq \text{TOMAX} - \text{DTMOD}$

If the above three conditions are satisfied for the $i^{th}$ variable listed in the CUTOFF array, then INDSTG is set equal to $i$ at STGTST (3). This informs EXE to terminate the stage if $i = 2, 3, \text{or} 4$ or to terminate the trajectory if INDSTG = 1.

**Termination Algorithm**

1. $t_p$ is the value of stage time, $t_\Phi$, at the last valid integration step. $\Omega_1^p$ is the value of $\Omega_1$ on the last valid integration step. STGTST(3) updated $\Omega_1^p$ and $t_p$ only if it does not reject the integration step (or if it is the first point of a major stage).
2. STGTST(3) rejects an integration step (sets LOOK $\neq 0$) only if the termination criteria is not satisfied and
   
   $\Omega_1 - \bar{\Omega}_1 (\Omega_1^p - \bar{\Omega}_1) < 0$ for some $i$ and $\text{TIME} > \text{TOMAX} - \text{DTMOD}$ if $i = 1$.
3. For each $i$ which dictates that the integration step be rejected an integration step size $h_1$ is computed.
\[ h_1 = \frac{\Omega_1 - \Omega_1^P}{(\Omega_1 - \Omega_1^P) / (t_s - t_s^P)} \]

This is the step size which the linear prediction estimates should be taken from the last valid integration step in order to exactly satisfy \( \Omega_1 = \Omega_1^p \).

(4) The minimum of all the \( h_1 \)'s is determined; call it \( h^* \). The step size \( h^* \), to use on the next integration step is set equal to \( h^* \) sign (\( h^* \)). LOOK has been set nonzero; this informs EKE that the integration is to be backed up to the last valid step.

(5) INGHOM is set to 1 whenever STGTST(3) rejects an integration step. Within a given stage, STGTST(3) may reject an integration step on account of the behavior of \( \Omega_1 \) at most 20 times. If this limit is reached the staging criteria is assumed to be satisfied (even if it is not in fact) for the variable in question.

(6) Within a given stage, each time STGTST(3) accepts an integration step after INGHOM has once been set to 1, INGHOM is incremented by 1. The iteration is terminated if INGHOM ever reaches 100; if this happens, INDSTE is set to 0 to indicate an error in the trajectory.

**Remarks**

(1) Specifying TOMAX and DTMOD permit dealing with a multiple valued cutoff function; cutoff cannot be achieved until \( \text{TME} > \text{TOMAX} - \text{DTMOD} \). TOMAX and DTMOD may be input; TOMAX is set to the termination time of the trajectory of the previous cycle in CTLS. Care should be exercised when specifying TOMAX and DTMOD.

(2) BCDSIM is equivalenced to the second location of the CUTOFF array (in the directory). Likewise STEST is equivalenced to the second location of the CMBAR array. (Each of these may be input in stage data to define the staging variables and their desired staging values).

(3) Before stage data is read for a given stage, EKE properly blanks out CUTOFF(2), CUTOFF(3), CUTOFF(4), i.e. the BCDSIM array).

(4) There is no restriction on the number of stages.

(5) No provision is made for specifying "increasing" or "decreasing" as an additional requirement of the termination criteria, but such a modification should not be difficult.

(6) STGTST2 extends the stage testing function to the second vehicle. STGTST2 is identical to STGTST except for the use of the second vehicle's COMMON blocks and auxiliary routines. EXE directly controls STGTST2. A flow chart for STGTST is presented.
13. **EXTRAN** and EXTRAN2-Driyer for h-Transformation

**Purpose:**

To drive various combinations of the initial transformation and the h-transformation determined by the value of the indicator `INDHTR`.

**Methods:**

EXTRAN is a special subprogram of EXE. Its entry points are not standard.

**Entry Point**

1. `INDHTR` is set to 0 and the number of the calculation step where the values of the state variables are saved. Values of variables that are to be filtered are saved by a call to `FILTER(1)`.

2. The new values of the filtered variables are picked up by a call to `FILTER(2)`.

3. The initial transformation or h-transformation is driven according to the value of `INDHTR`:

   - `INDHTR = 0` No calculations
   - `-1 or 1` Initial Transformation: \( \xi^+ \frac{\text{DIPEQ}(2)\xi}{\text{DIPEQ}(3)\xi^+} \)
   - `2` h-transformation:
     \[
     x^+ \frac{\xi^- \text{DIPEQ}(3)\xi^-}{\xi^+ \text{DIPEQ}(3)\xi^+} + \text{FILTER}(3)\xi^+ \frac{\text{DIPEQ}(3)\xi^+}{\text{DIPEQ}(3)\xi^+} \]
   - `3` h-transformation:
     \[
     x^- \frac{\xi^- \text{DIPEQ}(3)\xi^-}{\xi^+ \text{DIPEQ}(3)\xi^+} + \text{FILTER}(3)\xi^+ \frac{\text{DIPEQ}(3)\xi^+}{\text{DIPEQ}(3)\xi^+} \]
   - `4` h-transformation:
     \[
     x^- \frac{\xi^- \text{DIPEQ}(3)\xi^-}{\xi^+ \text{DIPEQ}(3)\xi^+} + \text{FILTER}(3)\xi^+ \frac{\text{DIPEQ}(3)\xi^+}{\text{DIPEQ}(3)\xi^+} \]

   where
   - \( x^- \) denotes values of state variables at end of last stage.
   - \( x^+ \) denotes values of state variables at beginning of current stage.
   - \( \xi^- \) denotes values of auxiliary variables (i.e. functions of the state variables) at end of last stage.
   - \( \xi^+ \) denotes values of auxiliary variables at beginning of current stage.
Usage:

At the beginning of the trajectory EXE properly sets INDHTR to 1 in order to accomplish the initial transformation.

EXTRAN(1) is called by EXE at the beginning of every stage after the first, before the stage data for that stage is read. EXTRAN(2) is called after the stage data is read. And, of course, EXTRAN(3) is called to do the initial or h-transformation in order to initialise the values of the variables that are to be integrated.

Remarks:

The reason for having several basic options for the h-transformation is in order to achieve flexibility. It is assumed that DIFEQ(2) is the inverse of the DIFEQ(3) transformation (and vice versa) with respect to the values of the state variables and the auxiliary variables. DIFEQ(8) is either a transformation from the state variables to the state variables directly (INDHTR = 4) or from the auxiliary variables to the auxiliary variables (INDHTR = 3). FILTER (3) is the transformation equivalent to the reading of data for those variables that are set up to be filtered. This permits some simple types of h-transformations (INDHTR = 2) to be accomplished within the data without the need for introducing new code at DIFEQ(8), and also permits the other types of h-transformations to be modified to a limited extent right within the data.

On a trajectory for which partials are being computed EXTRAN(3) will be entered in the process of computing the P matrix and/or the R matrix. This action is initiated by PARTS. Negative values of INDHTR are to indicate that the P-matrix for that particular h-transformation is the identity and hence need not be computed.

The indicator INDHTR plays an important role in EXE proper too. ND is an indicator which is normally 2 to denote the beginning of a major stage after stage 1. If a P matrix is computed at a stage point (i.e. INDHTR > 0) then ND is set to 3 to inform RSV to expect a P matrix on the partial tape.

EXTRAN2 performs the identical and h-transformation for Vehicle 2. It is called by EXE2 and is identical to EXTRAN other than for use of Vehicle 2 COMMON blocks and auxiliary subroutines. A flow chart for EXTRAN is provided.
14. INTGRT, INTGRT2, and INTGRTR - Interface for Integration Routine

Purpose:

To serve as an interface between the integration routine proper (MIMINF or MIMINR) and any routine requesting a variable to be integrated; also to backup the integration.

There are five logical functions which this routine performs depending on the status of the indicator INTCAL. For a particular call to INTGRTR, one of these functions will be enacted. The P array is the array of current derivative values of the variables that are being integrated. The Y array is the array of the current integrated variable values.

Usage:

To integrate XDOT and have the resulting integrated value stored in X use the statement

CALL INTGRT (INTNUM, XDOT, X)

INTNUM must be a distinct call used in, and only in, the calls for the integration of XDOT.

A call of the above form must be made at three different times (when the value of INTCAL is 2, 3, and 4). However, all of this may be accomplished with only one statement if the statement is inserted at the entry point 7 of the calling program.

INTNUM is the subscript in the P and Y arrays for the values XDOT and X respectively.

Method:

INTCAL = 1 the P and Y arrays are set to 0; the number of integrated variable is set to 0.

INTCAL = 2 the subscript INTNUM is computed for the arguments XDOT and X; the number of integrated variables is updated by 1.

INTCAL = 3 the value of XDOT is put into its proper place in the P array.

INTCAL = 4 the value of the integrated variable is picked up from the proper place in the Y array and put in X.

INTCAL = 5 the integration is backed up one step by resetting the Y array to the previous Y array (YO) and by resetting T to TC.
INTGRT will terminate the case if more variables are requested to be integrated than there is room for in the integration arrays; at present, this upper limit is 25 variables in the forward trajectory, and 300 in the reverse trajectory.

EXE proper is the only routine which calls INTGRT when INTCAL = 1 or when INTCAL = 5. EXE has sole control over setting the indicator INTCAL.

INTGRT2 serves as an interface between the integration routine MIMINF2 for the second vehicle and any second vehicle subroutine requesting a variable to be integrated. It is identical to INTGRT except for use of Vehicle 2's COMMON blocks. INTGRT2 is directly controlled from EXE. A flow chart for INTGRT is provided.

INTGRTR serves as an integration interface routine for the reverse time integration of the adjoint equations through MIMINR and the REV program. It is identical to INTGRT other than for use of the UPDCAR COMMON block and subroutine STOP2.
15. CODES and CODES2 - Code Print Routines

Purpose
To print code names of variables to identify the values in the output.

Usage
CALL CODES (L, A1, ..., AL)

L is an integer 0 ≤ L ≤ 8 identifying the number of arguments following it.

A1, ..., AL L calls each containing a Hollerith code word of at most 10 characters.

The above call adds the L Hollerith code words to the list of code words to be output on the next line of print. When 8 code words have been accumulated, the line is printed; any excess code words are added to the list for the next line of print. If L is 0, then the codes in the existing list (the number may be less than eight) are printed immediately.

Lines accounting is taken care of within this routine.

This subroutine is designed to be used in conjunction with the VALUES subroutine.

Codes are printed with a "5X,10" format.

CODES and VALUES control small secondary output buffers within the program itself.

Normally a call to CODES is made before any call to VALUES in order to identify the values. The CALL CODES (0) is necessary to be sure that the codes are printed; the CALL VALUES (0) is necessary to be sure the values are printed. (If this is not done the buffers may never be flushed.)

Remarks:

A flow chart for CODES is presented. CODES2 is identical to CODES but is required to insure correct output function for the second vehicle.
16. **ITEMS and ITEMS2 - Variable Print Routines**

**Purpose:**

To allow printing of variables in addition to those printed by other subprograms of EXE at entry points 5 and 6.

**Usage:**

CALL ITEMS (IENTRY)

IENTRY = 5 prints BCD names of specified variables.
IENTRY = 6 prints values of specified variables.
CODES and VALUES are used for output.

All variables specified on the VPRINT card will be output. Up to twenty variables may be specified.

**Remarks:**

ITEMS is called by EXE.
ITEMS calls CODES and VALUES.
ITEMS2 is identical to ITEMS except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
ITEMS2 is called by EXE2.
A flow chart for ITEMS is presented.
17. COMBAT and COMBAT2 - Combat Control Routine

Purpose:

To set the initial values of the combat parameters and act as the calling program to other subroutines for combat role and tactics selection.

Usage:

Entry is made to this routine by the following statement:

CALL COMBAT (IENTRY)

where IENTRY is a fixed point variable.

IENTRY = 1

This is the pre-data initialization. At this entry the nominal values are established for the following combat parameters.

<table>
<thead>
<tr>
<th>MNEMONIC</th>
<th>NOMINAL VALUE</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>NGSPE</td>
<td>1.0</td>
<td>Load factor to use in the maximum specific energy maneuver.</td>
</tr>
<tr>
<td>DLTSPE</td>
<td>2.0</td>
<td>Number of seconds &quot;Look Ahead&quot; used to determine maximum specific energy path.</td>
</tr>
<tr>
<td>MSURE</td>
<td>1.0</td>
<td>Mach number at which to start &quot;NGSPE/2&quot; path during maximum specific energy maneuver.</td>
</tr>
<tr>
<td>MSUPE</td>
<td>1.2</td>
<td>Mach number at which to end &quot;NGSPE/2&quot; path during maximum specific energy maneuver.</td>
</tr>
<tr>
<td>GAMSPE</td>
<td>-15.0</td>
<td>Lower bound on flight path angle during &quot;NGSPE/2&quot; portion of maximum specific energy maneuver.</td>
</tr>
<tr>
<td>HSURE</td>
<td>25000.</td>
<td>Altitude at which to start &quot;NGSPE/2&quot; path during maximum specific energy maneuver.</td>
</tr>
<tr>
<td>APSURE(1)</td>
<td>1.0</td>
<td>Factor applied to ALFWG to establish lower bound on angle of attack for subsonic portion of maximum specific energy path.</td>
</tr>
<tr>
<td>APSURE(2)</td>
<td>1.5</td>
<td>Factor applied to ALFWG to establish upper bound on angle of attack for subsonic portion of maximum specific energy path.</td>
</tr>
<tr>
<td>MNEMONIC</td>
<td>NOMINAL VALUE</td>
<td>DESCRIPTION</td>
</tr>
<tr>
<td>-----------</td>
<td>---------------</td>
<td>-------------</td>
</tr>
<tr>
<td>AFSUPE(1)</td>
<td>-2.0</td>
<td>Factor applied to ALPBG to establish lower bound on angle of attack for supersonic portion of maximum specific energy path.</td>
</tr>
<tr>
<td>AFSUPE(2)</td>
<td>1.5</td>
<td>Factor applied to ALPBG to establish upper bound on angle of attack for supersonic portion of maximum specific energy path.</td>
</tr>
<tr>
<td>INDDIV</td>
<td>0</td>
<td>Switch indicator set by program (Do not input as data).</td>
</tr>
<tr>
<td>IPCMEG</td>
<td>1</td>
<td>Print control for combat message</td>
</tr>
<tr>
<td>CPCON(1)</td>
<td>1.0</td>
<td>Factor applied to maximum angle of attack (AMAXD) to establish the upper bound on desired angle of attack (ALPDD)</td>
</tr>
<tr>
<td>CPCON(2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CPCON(12)</td>
<td>30.0</td>
<td>Role selection logic: attack incoming targets when CONBD &lt; CPCON(12)</td>
</tr>
<tr>
<td>CPCON(13)</td>
<td>60.0</td>
<td>Role selection logic cone angle for second sector: offensive role when CONBD &lt; CPCON(13)</td>
</tr>
<tr>
<td>CPCON(14)</td>
<td>1.0</td>
<td></td>
</tr>
<tr>
<td>CPCON(15)</td>
<td>0.0</td>
<td></td>
</tr>
<tr>
<td>CPCON(16)</td>
<td>10.0</td>
<td></td>
</tr>
<tr>
<td>CPCON(17)</td>
<td>10.0</td>
<td>Role selection logic, take evasive action when ESERDT &lt; CPCON(17)</td>
</tr>
</tbody>
</table>

136
<table>
<thead>
<tr>
<th>MNEMONIC</th>
<th>NOMINAL VALUE</th>
<th>DESCRIPTION</th>
</tr>
</thead>
</table>
| CPCON(18) | 1.0           | Throttle factor for hard turn defensive maneuver  
|           |               | \[\text{AND} = \text{ANMAX} \times \text{CPCON}(18)\] |
| CPCON(19) | 1.0           | Angle of attack factor for hard turn defensive maneuver  
|           |               | \[\text{ALPDD} = \text{AMAXD} \times \text{CPCON}(19)\] |
| CPCON(20) | 90.0          | Table of desired bank angles for hard turn defensive maneuver |
| CPCON(29) | 90.0          |                     |
| CPCON(3)  |               |                     |
| CPCON(4)  |               |                     |
| CPCON(5)  | 1.0           | Finite control rate logic: factor on angle of attack rate  
|           |               | \[\text{ALPHD1} = \text{ALPDOT} \times \text{CPCON}(5)\] |
| CPCON(6)  | 1.0           | Finite control rate logic: rate adjustment factor for angle of attack  
|           |               | \[\text{RAFALP} = \text{ALPDOT} \times \text{DELTS} \times \text{CPCON}(6)\] |
| CPCON(7)  | 1.0           | Finite control rate logic: factor on bank angle rate  
|           |               | \[\text{BA77D1} = \text{BADOT} \times \text{CPCON}(7)\] |
| CPCON(8)  | 1.0           | Finite control rate logic: rate adjustment factor for bank angle  
|           |               | \[\text{RAFBA} = \text{BADOT} \times \text{DELTS} \times \text{CPCON}(8)\] |
| CPCON(9)  | 1.0           | Finite control rate logic: factor on throttle rate  
|           |               | \[\text{AN7771} = \text{ANDOT} \times \text{CPCON}(9)\] |
| CPCON(10) | 1.0           | Finite control rate logic: rate adjustment factor for throttle  
|           |               | \[\text{RAFAN} = \text{ANDOT} \times \text{DELTS} \times \text{CPCON}(10)\] |

137
<table>
<thead>
<tr>
<th>NOMENCLATURE</th>
<th>NOMINAL VALUE</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPCON(11)</td>
<td>90.0</td>
<td>Role selection logic, outgoing target when PHOFD &lt; CPCON(11)</td>
</tr>
<tr>
<td>CPCON(30)</td>
<td>1.0</td>
<td>Throttle factor for line-of-sight vector rotation defensive maneuver AND = ANMAX * CPCON(30)</td>
</tr>
<tr>
<td>CPCON(32)</td>
<td>1.0</td>
<td></td>
</tr>
<tr>
<td>CPCON(33)</td>
<td>1.0</td>
<td>Angle of attack factor for Split S defensive maneuver ALPDD = AMAXD * CPCON(33)</td>
</tr>
<tr>
<td>CPCON(34)</td>
<td>1.0</td>
<td>Throttle factor for Split S Defensive maneuver AND = AMAXD * CPCON(34)</td>
</tr>
<tr>
<td>CPCON(35)</td>
<td>1.0</td>
<td></td>
</tr>
<tr>
<td>CPCON(36)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CPCON(37)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CPCON(38)</td>
<td>1.0</td>
<td>Angle of attack factor for lag-pursuit offensive maneuver ALPDD = AMAXD * CPCON(38)</td>
</tr>
<tr>
<td>CPCON(39)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MNEMONIC</td>
<td>NOMINAL VALUE</td>
<td>DESCRIPTION</td>
</tr>
<tr>
<td>------------</td>
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<td>----------------------------------------------------------------------------------------------------------------</td>
</tr>
<tr>
<td>CFCON(40)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CFCON(41)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CFCON(42)</td>
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<tr>
<td>CFCON(43)</td>
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<td>CFCON(44)</td>
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<tr>
<td>CFCON(45)</td>
<td></td>
<td></td>
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<tr>
<td>CFCON(46)</td>
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<td></td>
</tr>
<tr>
<td>CFCON(47)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CFCON(48)</td>
<td>1.0</td>
<td>Attacking maneuver: TC * CFCON(48) determines the time constant for elimination of pointing error.</td>
</tr>
<tr>
<td>CFCON(49)</td>
<td>1.0</td>
<td>Attacking maneuver: throttle control if RP RI7T then AND = ANMAX * CFCON(49)</td>
</tr>
<tr>
<td>MNEMONIC</td>
<td>NOMINAL VALUE</td>
<td>DESCRIPTION</td>
</tr>
<tr>
<td>------------</td>
<td>---------------</td>
<td>------------------------------------------------------------------------------------------------------------------------------------------</td>
</tr>
<tr>
<td>CPCON(50)</td>
<td>1.0</td>
<td>Attacking maneuver: throttle control if RP ≤ R177F then AND = ANMAX * COCON(50)</td>
</tr>
<tr>
<td>INDBNC_i</td>
<td>0</td>
<td>Boundary control</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INDBNC_i = 0, i^{th} boundary violation can not be controlled</td>
</tr>
<tr>
<td></td>
<td></td>
<td>= 1, i^{th} boundary violation can be controlled by angle of attack</td>
</tr>
<tr>
<td>ALPDOT</td>
<td>20.0</td>
<td>Maximum rate at which angle of attack can be changed (DEG/SEC)</td>
</tr>
<tr>
<td>BADOT</td>
<td>45.0</td>
<td>Maximum rate at which bank angle can be changed (DEG/SEC)</td>
</tr>
<tr>
<td>ANDOT</td>
<td>.2</td>
<td>Throttle rate (Fraction of full throttle/ sec)</td>
</tr>
<tr>
<td>AMAXD</td>
<td>15.0</td>
<td>Maximum angle of attack (DEG)</td>
</tr>
<tr>
<td>ANMAX</td>
<td>1.0</td>
<td>Maximum throttle setting</td>
</tr>
<tr>
<td>VMINF</td>
<td>200.</td>
<td>Minimum vehicle velocity (Ft/Sec)</td>
</tr>
</tbody>
</table>

**ENTRY = 2**

This is the post-data initialization. At this entry the values of the array CPCON is output on unit 6.

**ENTRY = 3**

At this entry subroutines ANGLES, DETECT, ROLE_i, HLIMIT, and CRATE are called role selection and to determine desired angle of attack, bank angle, and throttle setting.

**ENTRY = 4**

Entry for initial print.
ENTRY = 5

Entry to print mnemonic headings. The following codes are printed:

ALPHDI BA77D1 AN7771 ALPDII BAD7D AND ALPHDI BA77D AN XAIMF

ENTRY = 6

At this entry the corresponding values to the mnemonic codes of Entry 5 are printed.

Remarks:

A flow chart for COMBAT is presented. COMBAT 2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
COMBAT

ENTRY

SET INITIAL VALUES FOR COMBAT PARAMETERS

DETECT(1)
ROLE1(1)
HLIMIT(1)

RETURN

PRINCPRON(I)
I:=1,50
INDCRE

DETECT(2)
ROLE1(2)
HLIMIT(2)

RETURN

VALUES
DETECT(4)
ROLE1(4)
HLIMIT(4)

RETURN

DETECT(7)
ROLE1(7)
HLIMIT(7)

RETURN

DETECT(8)
ROLE1(8)
HLIMIT(8)

RETURN
18. **MIMINF and MIMINF2 - Integration Routine**

**Purpose**

To perform the calculations necessary to integrate an array of variables by the Runge-Kutta method; to determine an estimate of the truncation error and, with this information, to decide whether to accept or reject an integration step; to compute a new step size, \( h \), (based on the truncation error) to be used for the next integration step.

- \( T \) - the independent variable for the integration
- \( T_0 \) - the value of \( T \) at the last valid integration step
- \( Y \) - array of current values of integrated variables
- \( Y_0 \) - an array of the values in the \( Y \) array at the last valid integration step
- \( h \) - array of current values of derivatives of integrated variables

**Usage:**

In general, a numerical integration routine must make several intermediate or preliminary calculations of the integrated variables before an integration step is actually taken. This routine is organized so that for each basic entry point to it, one of the several intermediate calculations of the integrated variables is performed. The reason for organizing it this way is so that MIMINF does not have to be shackled with the responsibility of driving other calculations which need to be performed during an integration step; as a consequence, MIMINF itself is virtually void of complex logic.

EXE proper is the only routine which calls MIMINF. Communication between EXE and MIMINF is accomplished for the most part by the indicator MIMFAS. On the call to MIMINF at which the final values of the integrated variables for an integration step are computed, MIMINF sets MIMFAS = 0 in order to inform EXE that the step is tentatively all right. After each return from a basic call to MIMINF, EXE increases MIMFAS by 1. EXE makes each basic call to MIMINF with (the absolute value of) MIMFAS as the argument. Hence at each basic call to MIMINF the next intermediate calculation of the integrated variable is performed.

Now every integration step that is made has to be double checked by MIMINF; it is only when the next integration step is ready to start that there is enough information for MIMINF to get a good estimate of the truncation error that has occurred on the last integration step. Hence at this time, EXE makes the terminal call to MIMINF (entry point 5) for the truncation error check. If the truncation error is too large MIMINF (5) sets MIMFAS = -1; this informs EXE that the integration is to be backed up and the last integration step is to be attempted again with a smaller step size \( h \), (i.e. \( h_0 \)) determined by MIMINF (5).
Method:

The method employed here performs three intermediate calculations of the integrated variables, \( y_A, y_B, y_C \), before the final value of the integrated variables, \( y_{n+1} \), is calculated.

Entry point 1:
\[
y_A = y_n + \frac{h}{2} \dot{y}_n
\]

Entry point 2:
\[
y_B = y_n + \frac{h}{2} \dot{y}_A
\]

Entry point 3:
\[
y_C = y_n + h \dot{y}_B
\]

Entry point 4:
\[
y_{n+1} = y_n + \frac{h}{6} \left( \dot{y}_n + 2\dot{y}_A + 2\dot{y}_B + \dot{y}_C \right)
\]

(The calculation of the necessary derivatives (i.e. \( \dot{y}_n, \dot{y}_A, \dot{y}_B, \dot{y}_C \)) will have been done elsewhere by the time that entry point of MIMINF is called. The general form of these derivatives is

\[
\dot{y}_n = f(y_n, t_n)
\]
\[
\dot{y}_A = f(y_A, t_n + h/2)
\]
\[
\dot{y}_B = f(y_B, t_n + h/2)
\]
\[
\dot{y}_C = f(y_C, t_n + h)
\]

The derivatives are picked up from the P array. The values of the integrated variables are put in the Y array. At present, at most 25 variables may be integrated.

Entry point 5: Truncation error estimation and step size control

At this entry point, the truncation error \( T_n \) is estimated as

\[
T_n = h \left[ \frac{\dot{y}_{n+1} - \dot{y}_C}{y_{n+1}} \right]
\]

This is done for each integrated variable. Finally, \( T_n^* \) is defined as the maximum in absolute value of all the \( T_n \)'s. Now there are three possibilities:

(a) \( \text{EMIN} \leq T_n^* < \text{EMAX} \): in this case MIMINF (5) accepts the integration step and retains the same value of HO for the next step.

(b) \( T_n^* < \text{EMIN} \): in this case MIMINE (5) accepts the integration step and sets \( HO = \text{sgn}(HO) \min \left[ 2 |HO|, |AMXER| \right] \)

(c) \( T_n^* \geq \text{EMAX} \): if \( |HO| = \text{AMINER} \), the integration step is accepted; otherwise MIMINF (5) rejects the integration step (setting MIMPAS = -1) and sets \( HO = \text{sgn}(HO) \max \left[ 1/2 |HO|, |AMINER| \right] \)
"Variable step" integration is an option (specified in the data by INDVAR = 1). If INDVAR is 0 then the "fixed step" option is used. For the fixed step, the calculations of MIMINF (5) as described above are not used; entry point 5 for fixed step is trivial; NO is set equal to DELTS.

MIMINF2 performs the calculations necessary to integrate the second vehicle array of variables. It is identical to MIMINF except for the use of Vehicle 2 COMMON blocks. It should be noted that MIMINF2 is called directly by EXE. Program EXE thus directly controls both vehicle equation of motion integrations. The indicator INDNUM controls the number of vehicles in EXE; INDNUM = 1 signifies only one vehicle is being employed, and INDNUM = 2 signifies two vehicles are being employed. A flow chart for MIMINF is presented.
19. **TIMID and TIMID2 - Step Function Routines for Time Points**

**Purpose:**

To compute the step function \( y = \tau(x) \) given by

\[
y = \min \{ y \in Y \mid y \geq x \}
\]

where \( Y \) contains the following types of elements

1) all integral multiples of \( \text{DELT} \)

2) \( y_r = \tau_r(x) \) where \( \tau_r \) is the step function evaluated by the TIMID subroutine.

**Usage:**

```fortran
CALL TIMID (XX,YY)
```

where

- **XX** is the argument.
- **YY** is the answer.

**Remarks:**

EXE is the only routine which calls TIMID; it does so to compute the next stage time point that must be hit as a function of the current stage time. In order that TIMID not return a stage time point which is "too close" to the current stage time, EXE calls TIMID as follows:

```fortran
CALL TIMID (TIMES + AMER, TIMPT)
```

**TIMID2 computes** \( y = \tau(x) \) **for the second vehicle. TIMID2 is identical to TIMID except for the use of vehicle 2's COMMON blocks and auxiliary subroutines. A flow chart for TIMID is presented.**
TIMID

START

YY = XX + DELTS - XX MOD DLTSS

CALL TIM001

YY = AMIN(YY, YBOUND)

RETURN
20. **VALUES** and **VALUES2** - Value Print Routines

**Purpose**
To print the values of floating point variables.

**Usage**

```fortran
CALL VALUES (L, X1,...,XL)
```

- **L** is an integer \(0 \leq L \leq 8\) identifying the number of arguments following it.
- **XL** \(i\) \(= 1,...,L\) \(L\) calls containing the value of some floating point variable to be printed.

The above call adds the \(L\) variable values, \(X1,...,XL\), to the list of values to be output on the next line of print. When 8 values have been accumulated, the line is printed, any excess values are added to the list for a next line of print. If \(L = 0\), then the values in the existing list (the number may be less than eight) are printed immediately.

Lines accounting is taken care of within this routine.

This subroutine is designed to be used in conjunction with the **CODES** subroutine.

Values are printed with a "LPE15.7" format.

**CODES** and **VALUES** control small secondary output buffers within the program itself.

Normally a call to **CODES** is made before any call to **VALUES** in order to identify the values. The CALL **CODES** (0) is necessary to be sure that the codes are printed; the CALL **VALUES** (0) is necessary to be sure the values are printed. (If this is not done the buffers may never be flushed.)

**Remarks:**

A flow chart for **VALUES** is presented. **VALUES2** is identical but is required for correct output function for the second vehicle.
VALUES
START
F
N ≤ 0
T

B(i) = A1
B(i) = A2
B(i) = A3
B(i) = A4
B(i) = A5
B(i) = A6
B(i) = A7
B(i) = A8
N

DO: I = 1, N

ICOUNT = ICOUNT + 1
C(ICOUNT) = B(i)

ICOUNT ≥ 8
F
CALL LINES
T
WRITE 5, 000
ICOUNT = 0
CONTINUE
RETURN

ICOUNT = 0
CALL LINES
WRITE 5, 000
21. MISCUT and MISCUT2 - Abortion Routine

Purpose:

To terminate the trajectory if any specified variable lies outside a specified upper or lower bound for that variable.

Usage:

CALL MISCUT

If a specified variable lies outside a specified upper or lower bound, TIME is set to 1.E36. TMAX should not be greater than 1.E36 when use of this routine is specified. Thus the trajectory will terminate on MISSED CUTOFF.

Up to nine variables may be specified for bounding on the MISVAR card. Values for bounding the variables appear in the corresponding positions on the BOUNDS card. Testing of the boundaries is determined by the LUBGLB card.

The integers appearing on the LUBGLB card are of the form

\[ ij \]

\( j \) specifies that the \( j \)th variable on the MISVAR card will be checked.

When \( i = 0 \) the \( j \)th value on the BOUNDS card will be ignored and no check made.

When \( i = 1 \) the \( j \)th value on the BOUNDS card will be an upper bound for the \( j \)th variable on the MISVAR card.

When \( i = 2 \) the \( j \)th value on the BOUNDS card will be a lower bound for the \( j \)th variable on the MISVAR card.

Remarks:

MISCUT is called by EXE. MISCUT2 terminates the trajectory if any specified second vehicle lies outside specified upper and lower bounds. A flow chart for MISCUT is presented; MISCUT2 is identical except for use of second vehicle COMMON blocks.
22. **ONLINED - On Line Display Routine**

**Purpose:**

To display a thirty-nine character message on the CDC display station of a CDC 200 user terminal.

**Method:**

The system routine `encode` is used to construct the message line, and the system routine `SCOPE` is used to display the message on the CRT device.

**Usage:**

Entry is made to this routine with the following statement:

```
CALL ONLINED
```

**Subroutines Called:**

`ENCODE`

`SCOPE`

---

**Flowchart:**

```
ONLINED

NO

OPTIMA

ER. 3

YES

NC = NC CYCLE

ENCOD((NO, MESSAGE)
ESERB, ESERB, MEPL, 
ESERF, JES3)

INDIAN

ER. 0

YES

NC = - NC

NO

SCORE (MESSAGE)

RETURN

ENCOD((NO, MESSAGE)
PSTAR(1), PSTAR(2), 
PSTAR(3), RTSTAR(1), NC)
```

153
DIFFEQ1 and DIFFEQ2 - Point Mass Equations of Motion

Purpose:

For performing all calculations necessary for the three-degree of freedom trajectory equations.

Method:

DIFFEQ1 has several subprograms; in general the subprograms are responsible for performing the calculations made necessary by certain physical attributes of the vehicle, the trajectory or the environment. DIFFEQ1 may be called from EXE, EXTRAN, and PTBQON (by first passing through the interface routine DIFFEQ).

Subprogram

- HETS: Temperature and heating parameters
- TFFS: Thrust force; mass flow
- FPPS: Control variables as functions of already computed variables
- SACS: Wind axes aerodynamic forces on vehicle
- ATMS: Atmospheric parameters
- GVSP: Local geocentric gravitational force components
- LATS: Conversion from geodetic to geocentric latitude and vice-versa

In addition to the vehicle and planetary characteristics subprograms above, DIFFEQ1 is broken down into a sequence of control subroutines.

Subroutine:

- DEQPRE: Used at Entry 1 from EXE
- DEQINI: Used at Entry 2 from EXE
- DEQBCI: Used at Entry 3 from EXE
- DEQACI: Used at Entry 3 from EXE
- DEQSPI: Used at Entry 4 from EXE
- DEQVAL: Used at Entry 5 from EXE
- DEQCOD: Used at Entry 6 from EXE
- DEQIV: Used at Entry 7 from EXE
- DEQHT: Used at Entry 8 from EXE
- PIRFUN: Control computation of fire control functions
GAM91  Controls flight through the vertical

CTLITR  Controls instantaneous control variable iteration process.

With DIFEQ1 itself there is a considerable amount of code that may be by-passed depending on the type of problem being considered. Many of the calculations done at DIFEQ1 (3) would be purely auxiliary. Therefore for calculations of this type, there are indicators which may be input = 0 if it is desired that a particular calculation be performed. Since DIFEQ1 (3) has to be called so many times during a trajectory, any deletions of calculations which are not essential will help to cut down on the machine time.

A general description will be given of each entry point associated with DIFEQ1. Detailed information can be obtained in the user's manual for each entry point used by DIFEQ1.

DIFEQ1 (1)

At this entry point nominal values of indicators are set and the values of the integrated variables are initialized at 0. Also, nominal values are set for the standard constants used in the equations. (e.g. polar and equatorial radius of the earth). See DEQPRE.

DIFEQ1 (2)

This is the initial transformation. It is always performed at the beginning of a trajectory; it may be performed at the beginning of a major stage (see EXTRAN). Also, it may be used in certain combinations for the h-transformation (see EXTRAN). See DEQINI.

DIFEQ1 (3)

The main body of the calculations in DIFEQ1 appear at this entry point. The primary purpose at this entry point is to compute the derivatives of the variables that are being integrated. See DEQBCI, DEQACI, and CTLITR.

DIFEQ1 (4)

At this entry point the variables computed at either the initial transformation or for the h-transformation are printed. See DEQSPI.

DIFEQ1 (5)

At this entry point, the codes are printed, the codes identify the variables printed at DIFEQ1 (4) and DIFEQ1 (6). See DEQUAL

DIFEQ1 (6)

At this entry point the values of the variables computed at DIFEQ1 (3) are printed. Also, the values of the state variables (and perhaps other integrated variables) are printed. Entry is made to DIFEQ1 (6) only at valid integration steps. In some cases the value of a variable is printed only if the corresponding indicator is set in the data. See DEQCOD.
DIPEQI (7)

At this entry point the variables to be integrated are defined by making a call to INTGRT for each variable to be integrated. In some instances this will be done only if the appropriate indicator is set. See DEQIV.

DIPEQI (8)

At DIPEQI (8) an h-transformation is made. This transformation may be performed at a stage point (see EXTRAN). See DEQIV.

Remarks:
Subroutine DIPEQ2 is identical in form to DIPEQ1. DIPEQ2 controls the vehicle 2 equation of motion calculations using appropriate COMMON blocks and auxiliary subroutines. A flow chart of DIPEQ1 is presented. For user convenience, the original single vehicle equation of motion routine, DIPEQ1, is also presented.
ORIGINAL SINGLE VEHICLE EQUATIONS
ORIGINAL SINGLE VEHICLE EQUATIONS
ORIGINAL SINGLE VEHICLE EQUATIONS
24. DIFEQ3 - Dummy Subroutine

DIFEQ4 - Dummy Subroutine

DIFEQ5 - Sample Arbitrary Differential Equations

This is intended only as an example of how a new set of differential equations may be programmed for use in conjunction with the optimization program. The equations of this example are in cylindrical coordinates and describe a two-dimensional point mass with constant thrust in a vacuum having direction of thrust as a control variable. No flow chart is included with this subroutine.

DIFEQ6 - Dummy Subroutine
25. **TLUREV - Two Dimensional Table Look-up Routine** (Special)

**Purpose**
To linearly interpolate in a table which has just two points.

**Usage**

```fortran
CALL TLUREV (X, C, Y, IER)
```

where

- **X** is the argument
- **Y** is the functional value
- **IER** is set to 1 if extrapolation was necessary

**C** is the array containing the points of the table according to the following format

- **C(1)** = Not used
- **C(2)** = **X_1**
- **C(3)** = **Y_1**
- **C(4)** = **X_2**
- **C(5)** = **Y_2**

It is assumed that **X_1** < **X_2**

**Remarks**

**MANTGT** and **REV** are the only routines which use this routine.
\[ Y = C(3) + \frac{(C(5) - C(3)) \times (X - C(2))}{C(4) - C(2)} \]

Flowchart:
- START
- \[ Y = C(3) + \frac{(C(5) - C(3)) \times (X - C(2))}{C(4) - C(2)} \]
- \( X > C(4) \)
  - T
  - F
- \( X < C(2) \)
  - T
  - F \( \text{ERR 1} \)
- RETURN

166
26. **ACOS - Arc Cosine Routine**

**Purpose**
To compute the arc cosine of a normalized floating point argument X.

**Method**
For $|X| < 7.4505806 \times 10^{-9}$ the arc cosine is set equal to $\pi/2$. For $x = 1$, arc cosine is set equal to zero and for $X = -1$, arc cosine is set equal to $\pi$. When the argument $X \neq \pm 1$, the routine gives the arc cosine in radians from 0 to $\pi$.

**Usage**
The arc cosine is computed using the statement

$$Y = \text{ACOS}(X)$$

where, $|X| \leq 1$ and $Y = \cos^{-1}X$.

**Remarks**
No error returns are provided.
27. **ASIN - Arc Sine Routine**

**Purpose**
To compute the arc sine of a normalized floating point argument \( X \).

**Usage**
The arc sine is computed using the statement

\[
\text{ASIN} = 1.5707963 - \text{ACOS}(X)
\]

\[
Y = \text{ASIN}(X)
\]

where \(|X| \leq 1\) and \(Y = \sin^{-1} X\)

**Remarks**
No error returns are provided
28. TLU and TLU2 - Two-Dimensional Table Look Up Routine

**Purpose**

Given an argument \( X \), to compute \( Y = f(X) \) from a table of \( X \) and \( Y \) values by linear interpolation.

**Method**

The table of \( X \) values is searched until for some \( i \), \( X_i < X < X_{i+1} \). Linear interpolation is then performed. If, for some \( i \), \( X = X_i \) then \( Y \) is set to \( Y_i \).

**Usage**

Entry is made via the statement,

\[
\text{CALL TLU (X,C,Y,IND)}
\]

where,

- \( X \) = Variable name of the argument.
- \( C \) = Array name of the curve being used.
- \( Y \) = Variable name of the interpolated value.
- \( \text{IND} = 0 \), no errors indicated.
- \( 1 \), limit of the curve has been exceeded and the result is an extrapolation using the last two points.

The curve \( C \) must be stored as follows:

- \( C(1) = N \) = Number of points in curve (fixed point integer)
- \( C(2) = X_1 \)
- \( C(3) = Y_1 \)
- \( C(4) = X_2 \)
- \( C(5) = Y_2 \)
  ...
- \( C(2N) = X_N \)
- \( C(2N+1) = Y_N \)

**Remarks:**

A flow chart for TLU is presented. TLU2 is identical to TLU except for use of vehicle 2 COMMON blocks.
TLU

LOCZMI=LOZ -1

Z = C (LOCZ)

DO 1 I = 1, N

J + 2 + 1 + LOCZMI

C (J) - X

1 CONTINUE

F \quad J^{*}, (LOCZMI+2)

J + 4 + LOCZMI

CALL ERROR

LOCZ

Y = C_{j+1}

WRITE

6, 10

\[ Y = c_{j+1} + \left( \frac{c_{j+1} - c_{j-1}}{c_{j} - c_{j-2}} \right) (x - c_{j-2}) \]

RETURN

RETURN
29. **ATAN2 - Arctangent Routine**

**Purpose**

To compute the arctangent of the quotient of two normalized floating point quantities, \( A/B \), with proper quadrant control.

**Method**

The routine computes the quotient \( X/Y \). The arctangent is computed with quadrant according to the sign of \( Y \) and \( X \). If \( X = 0 \) and \( Y \neq 0 \), the routine computes

\[
Y = \tan^{-1}\left(\frac{Y}{X}\right) = \frac{Y}{|Y|} \cdot \frac{\pi}{2}
\]

If \( X = 0 \) and \( Y = 0 \), it computes

\[
Y = \tan^{-1}\left(\frac{Y}{X}\right) = 0
\]

**Usage**

The arctangent of \( Y/X \) is obtained via,

\[
Y = \text{ATAN2}(Y,X)
\]
30. **TLUL - Two-Dimensional Table Look-up Routine**

**Purpose**

Given an argument $X$, to compute $Y_i = f(X)$ by linear interpolation, where $i \geq 1$.

**Method**

The table of $X$ values is searched until for some $i$, $X_1 < X < X_{i+1}$. Linear interpolation is then performed on the number of curves requested. If for some $i$, $X = X_i$, then the $Y_i$ are set to that corresponding value of the dependent variable.

**Usage**

Entry is made via the statement.

```fortran
CALL TLUL (N, TABLE, TIME, NDEP, ANS, IND)
```

where,

- $N$ = The number of points in each curve.
- TABLE = The array name containing the sets of curves.
- TIME = The variable name of the argument.
- NDEP = The number of curves contained in the array CURVE.
- ANS = The array name into which the NDEP answers are to be stored.
- IND = 0, no errors indicated and all interpolations seem to be good. 1, the argument $X$ lies outside the range of the independent variable. If less than the range, the first points were used. If greater, the last points were used.

The table "CURVE" must have been set up as follows:

- CURVE(1) = $X_1$
- CURVE(2) = $X_2$
- CURVE(3) = $X_3$
- \[\vdots\]
- CURVE(N) = $X_N$
- CURVE(N+1) = $Y_1$
- CURVE(N+2) = $Y_1$
- CURVE(N+3) = $Y_2$
- \[\vdots\]
- \[\vdots\]
\text{CURVE}(2N) = Y_{1N}
\text{CURVE}(2N+1) = Y_{21}
\text{CURVE}(2N+2) = Y_{22}
\text{CURVE}(2N+3) = Y_{23}
\ldots
\text{CURVE}(3N) = Y_{3N}
\text{CURVE}(3N+1) = Y_{31}
\ldots
\text{CURVE}((\text{NDEP}+1)\times N) = Y_{\text{NDEP}N}

\textbf{Remarks}

No other routines are called from this routine.
31. **TIMREV** and **TIMREV2** - Time Point Collection Routine

**Purpose:**

During the forward trajectory, to build an array of stage time points that must be "hit" during the corresponding stage of the reverse trajectory.

**Usage:**

```fortran
CALL TIMREV (TIMRS, TOL)
```

- **TIMRS** the stage time point that is to be added to the list of points that must be hit in the corresponding stage of the reverse trajectory.
- **TOL** a tolerance: if a previous point of the list differs from the current point to be added by less than TOL, the current point is not added.

The name of the array of points is **TIMESA**. The **TIMESA** array is built in monotonically increasing order. If for any reason **TIMRS** is less than a point in the **TIMESA** array, all points greater than **TIMRS** in the **TIMESA** array are annihilated. **NPT** is the current number of points in the array. **NPT** must not exceed the dimension of the **TIMESA** array; if it does the case will be terminated. The first point of a stage will always be inserted in the **TIMESA** array.

This routine was written in anticipation of the need to hit stage time points in reverse for a number of different reasons. In particular, the routines **PAWTS** and **CTVS** call **TIMREV**. It is imperative that **PARTS** (3) call **TIMREV** with the current stage time and a tolerance of 0.

**TIMREV2** builds the array of stage time points for the second vehicle reverse trajectory. It should be noted that all variational optimization problems must be phrased in terms of the first vehicle data. In cooperative variational optimization, a program modification setting second vehicle control variables to names in the first vehicle directory is required. A flow chart for **TIMREV** is presented. **TIMREV2** is identical to **TIMREV** except for use of the second vehicle's **COMMON** blocks.
32. **PSUBR-Evaluation of Partial Routine**

**Purpose:**
To calculate matrices of partial derivatives numerically.

**Usage:**
This is a general routine; it is used in the following manner:
suppose
\[ y_1 = f_1(x_1, \ldots, x_n) \]
\[ \vdots \]
\[ y_m = f_m(x_1, \ldots, x_n) \]
and we want to compute
\[
J = \begin{bmatrix}
\frac{\partial y_1}{\partial x_1} & \cdots & \frac{\partial y_1}{\partial x_n} \\
\vdots & \ddots & \vdots \\
\frac{\partial y_m}{\partial x_1} & \cdots & \frac{\partial y_m}{\partial x_n}
\end{bmatrix}
\]
then a call to PSUBR should be made as follows:

```fortran
CALL PSUBR (NL,LX,LXST,HB,N2,LY,ANS,JP,P,LFCNS)
```
where
- **NL** is \( n \)
- **LX** is an array containing the COMMON locations of the variables \( x_1, \ldots, x_n \).
- **LXST** is an array containing the COMMON locations of same variables \( x_1^*, \ldots, x_n^* \) to be used in determining perturbation sizes.
- **HB** is an array of the minimum perturbation sizes to be used for the respective variables \( x_1, \ldots, x_n \).
- **N2** is \( m \)
- **LY** is an array of the COMMON locations of the variables \( y_1, \ldots, y_m^* \).
- **ANS** is \( J \), the array in which the answer is to be stored (this must be dimensioned 15 x 15)
- **JP** is an array of indicators one for each variable \( x_i, \ldots, x_m \).
  \( JP_i = 0 \) means that the \( i \)'th column of \( J \) is known to be 0.
P is a constant used to determine the perturbation size.

LFCNS is an indicator used to direct PSUBR to the code for the functions $f_1, \ldots, f_m$.

**Method:**

The elements of $J$ are computed a column at a time by the following approximation

$$\frac{\partial y_j}{\partial x_i} = \frac{f_1(x_1, \ldots, x_j + h_j, \ldots, x_n) - f_1(x_1, \ldots, x_j - h_j, \ldots, x_n)}{2h_j}$$

where $h_j = \max(|HB_j|, |x_j|) \times 10^{-P}$

If $J_{ij} = 0$ then $\frac{\partial y_j}{\partial x_i}$ is set = 0 for $i = 1, \ldots, m$. This eliminates the need for calling the routine to calculate the $f$ functions for column $j$.

The variables in PSUBR are dimensioned to compute a $15 \times 15$ matrix of partials. PSUBR stores the answer in ANS which it expects to be dimensioned $15 \times 15$.

After ANS has been computed and before returning PSUBR makes a final call to compute the $f$ functions with the original values of the $x$'s. This is intended to insure that values of variables after computing partials are the same as the value before computing partials.

**Remarks**

1. PSUBR is called only by PARTS.
2. P is PEXN in all calls; PEXN is input.
3. HB is either HBARN, HBARN, HBARN, HBART depending on the call; all of these are input.
4. PSUBR charges the routine PTBEQN with the responsibility for driving the calculations of the $f$ functions specified by LFCNS.
5. The basic state variables for the second vehicle may be perturbed through PSUBR. Appropriate transformations to permit such perturbations are introduced through subroutines ONETWO and TWOONE.
6. Perturbation of vehicle two's control variables in a cooperative variational optimization requires a program modification in ONETWO and TWOONE.
33. PRPACK — Blocking Routine for Partial.

Purpose

To enter values into an array for output to tape.

Method

All non-zero numbers (integer and floating point) are packed into a large
array before being output to tape.

Usage

Linkage to this routine is made via the statement.

CALL PRPACK (MCONT,NPOINT,NSTATE,IPM,IGM,IT,ND,IALP,IDEL,IWA,
IWAI,IWBI,INDPMT,IPARTS,IK,IENTRY)

where,

MCONT is the number of control variables.
NPOINT is the number of values in CTABLE.
NSTATE is the number of State Variables.
IPM is a (NSTATE\times NSTATE) Matrix.
IGM is a (MCONT\times NSTATE) Matrix.
IT is TIME.
ND is a control that is passed to the reverse, segment 0 at
the beginning of the trajectory, 1 within the stage and
2 at the end of the stage.
IALP is CTABLE points for that time.
IDEL is TIME step.
IWA is Weighting Matrix indicator.
IWAI is Constants used to construct the W' Matrix.
IWBI is Constants used to construct the W Matrix.
INDPMT is Number of end constraints.
IPARTS is array of terminal partials.
IK is not used.
IENTRY serves as an entry point to the subroutine.

COMMON References

CTABLE in numbered COMMON of 1

Subroutines Called

IZERO
PORTRAN I/O routines.
34. **FLUSH1 and FLUSH12 - Effer Flush Routine for PRPACK**

**Purpose**

To write on tape a partially-filled buffer.

**Method**

To test and determine if a buffer is partially filled and if so to write that part out on tape.

**Usage**

Entry is made to this routine by the following statement:

```
CALL FLUSH1
```

**Remarks**

Only the normal I/O FORTRAN routines are used by this routine. A flow chart for FLUSH1 is presented. FLUSH12 is identical except for the use of vehicle 2 COMMON blocks and units.
SETGRD -- Paper Plot Grid Setup Routine

Purpose:
To establish maximum and minimum dimension for x and y axes for each paper plot.

Usage:
Call SETGRD (XMAX, XMIN, YMAX, YMIN, NC)

XMAX - Maximum value in the X array
XMIN - Minimum value in the X array
YMAX - Maximum value in the Y array
YMIN - Minimum value in the Y array
NC   - Number of curves to be plotted

\[
\begin{align*}
DX &= \left| YMAX - XMIN \right| \times 0.075 \\
DY &= \left| YMAX - YMIN \right| \times 0.075 \\
YB &= YMAX + DX \\
XM &= XMIN - DX \\
YB &= YMAX + DY \\
YM &= YMIN - DY \\
NT &= NC
\end{align*}
\]

RETURN
36. **PAPERP - Printer-Plot Control Routine**

**Purpose:**
To provide on-line paper plot capability during equation of motion computation.

**Usage:**
Call PAPERP (X, Y, NX, TITLET, TITLEB)

Where

- **X** is an array that contains the values of the independent variable to be plotted
- **Y** is an array that contains the values of the dependent variable to be plotted
- **NX** is the number of data points to be plotted
- **TITLET** 120 character title that will be placed at the top of the plot area
- **TITLEB** 120 character title that will be placed at the bottom of the plot area

```
PAPERP
   NWT = 12
   NWB = 12
   CALL PPLNLM
   RETURN
```
37. DETECT and DETECT2 - Sensor Control Program

Purpose:

to control the sensor and vision routines.

Remarks:

A flow chart for DETECT is presented. DETECT2 is identical except for the use of vehicle 2 auxiliary subroutines.
DETECT

SENSE1 (1)
VISION (1)
RETURN

SENSE1 (2)
VISION (2)
RETURN

SENSE1 (3)
VISION (3)
RETURN

SENSE1 (4)
VISION (4)
RETURN

SENSE1 (5)
VISION (5)
RETURN

SENSE1 (6)
VISION (6)
RETURN

SENSE1 (7)
VISION (7)
RETURN

SENSE1 (8)
VISION (8)
RETURN

1000

2000

3000

4000

5000

6000
Purpose:
To define each vehicle's combative role on the basis of instantaneous vehicle states.

Method:
Each vehicle role is selected on the basis of their relative states. Role selection includes the following:

a. ATTACK
b. OFFENSIVE
c. DEFENSIVE
d. EVASIVE

An override permits selection of a fifth role
c. PASSIVE

The subprogram contains the standard EXEC ENTRY points.

Remarks:
A flow chart for ROLE1 is presented. ROLE2 is identical except for use of vehicle COMMON blocks and auxiliary subroutines.
39. **HLIMIT and HLIMIT2 - Minimum Altitude Constraint Routine**

**Purpose:**

To force a pull-up maneuver when a minimum altitude boundary is violated.

**Method:**

A minimum altitude is defined as:

a. Constant
b. Function of $\gamma$
c. Function of $\gamma$, $V$

When this minimum altitude limit is not satisfied, the angle-of-attack, bank-angle combination, which maximizes vertical force component, is used. Whenever the altitude limiter is employed, an appropriate message is printed by MSGONE or MSGONE2.

**Remarks:**

A flow chart for HLIMIT is presented. HLIMIT2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
40. **ANGLES and ANGLES2 - Relative Angular Orientation Routines**

**Purpose:**

To compute the relative angular orientation of the two vehicles in body axes and to compute steering errors from the reference vector and associated functions.

**Usage:**

Called from the combat logic during equation of motion computations.

**Remarks:**

A flowchart for ANGLES is presented. ANGLES2 is identical except for the use of vehicle 2 COMMON blocks.
\[ \beta' = \tan^{-1}[\sin\beta \cos\alpha / \cos\beta] \]

**TMTX:**
Compute \([U, V, W]\) matrix
Rotate:
(-\(\alpha\)) about y axis
(\(\beta'\)) about z axis
(0) about x axis

**TMTX:**
Compute \([r, s, t]\) matrix
Rotate:
(-\(\beta\)) about x axis
(-\(\gamma\)) about y axis
(-\(\alpha\)) about z axis

**TRNPOS:**
\([i, j, k]^T = [i, j, k]^T\)

**MULT31**
\[
\begin{bmatrix}
\Delta x_g \\
\Delta y_g \\
\Delta z_g
\end{bmatrix}^T = \begin{bmatrix}
\Delta x_e \\
\Delta y_e \\
\Delta z_e
\end{bmatrix}
\]

**TRNPOS:**
\([r, s, t]^T = [r, s, t]^T\)

**MULT31**
\[
\begin{bmatrix}
\Delta z_A \\
\Delta y_A \\
\Delta x_A
\end{bmatrix} = \begin{bmatrix}
\Delta x_g \\
\Delta y_g \\
\Delta z_g
\end{bmatrix}\]

**TRNPOS:**
\([u, v, w]^T = [u, v, w]^T\)
\[ \begin{align*}
\Delta x_B & = \Delta x_A \\
\Delta y_B & = [u, v, w] \Delta y_A \\
\Delta z_B & = \Delta z_A \\
\end{align*} \]

\[ \theta_{\text{AZIM}} = \tan[\Delta y_B / \Delta x_B] \]

\[ \theta_{\text{ELEV}} = \tan[-\Delta z_B / \Delta x_B^2 + \Delta y_B^2] \]

\[ \theta_{\text{CONE}} = \tan[v / \Delta y_B^2 + \Delta z_B^2 / \Delta x_B] \]

\[ \begin{align*}
\vec{x}_{\text{AIM}} &= x_e + x_{es} \\
\vec{y}_{\text{AIM}} &= y_e + y_{es} \\
\vec{z}_{\text{AIM}} &= z_e + z_{es} \\
\end{align*} \]

\[ \begin{align*}
x_{es} &= \Delta x_e + C_{p15} \cdot (\Delta x_{LA} - \Delta x_e) \\
y_{es} &= \Delta y_e + C_{p15} \cdot (\Delta y_{LA} - \Delta y_e) \\
z_{es} &= \Delta z_e + C_{p15} \cdot (\Delta z_{LA} - \Delta z_e) \\
\end{align*} \]

\[ \begin{align*}
\vec{g} &= x_{es} + y_{es} + z_{es} \\
\vec{F}_T &= F_{xe} + F_{ye} + F_{ze} \\
\varepsilon_s &= \cos^{-1}(\{x_{es} \cdot u_e + y_{es} \cdot v_e + z_{es} \cdot w_e / (v_{vs})\}) \\
F_{STV} &= (x_{es} \cdot F_{xe} + y_{es} \cdot F_{ye} + z_{es} \cdot F_{ze}) / v_{vs} \\
\varepsilon_f &= \cos^{-1}(F_{STV} / \vec{F}_T) \\
\phi_{\text{off}} &= 180 - \theta_{\text{ASP}} \\
\end{align*} \]

RETURN!
41. CRATE and CRATE2 - Finite Control Rate Routines

Purpose:

To introduce a finite control rate capability into combat simulations.

Method:

Desired control vector components are defined by either combative logic COMBAT and COMBAT2 or the flight plan programmer routines, FPPS or FPPS2. The instantaneous control error is then used to define an error magnitude-dependent control rate. Control values are obtained by integration of their rates. Logic to maintain controllable inequalities is incorporated in the finite control rate option.

Remarks:

A flow chart for CRATE is presented. CRATE2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
42. **TIM001 and TIM0012 - Tabular Time Point Routine**

**Purpose:**
To provide additional time points that the integration routine must "hit" in the forward trajectory.

**Usage:**

```plaintext
CALL TIM001 (VAL, TPT)
```

VAL is the current time value.

TPT is the next time point larger than VAL which should be "hit" in addition to other time points normally "hit" in the forward trajectory. TIM001 performs a table look-up on specified 2-dimensional tables to find the smallest time value in these tables which is larger than VAL.

If no tables are specified TIM001 returns 1.E36 for TPT.

TIM001 will use the tables specified on the TIMTAB card.

**Remarks:**
TIM001 is called by TIMID. TIM0012 is called by TIMID2 and provides for additional time points in the vehicle 2 trajectory. TIM0012 is identical to TIM001 except for the use of the vehicle 2 COMMON blocks. A flow chart for TIM001 is presented.
T1M001

ENTER

TPT = 1. x 10^12

NTAB

= 0

IF

(DO 3 I = 1, NTAB)

LOC1 = LOCTAB(I)
NEND = LOC1 + 2 - NVAL (LOC1)
LOC1 = LOC1 - 1

LOC1 = LOC1 + 2

LOC1 = NEND

TVAL = COM5 (LOC1)

TVAL > VAL?

F

T

TVAL = 1. x 10^38

TPT = MIN. OF (TPT, TVAL)

RETURN

205
43. DEQPRE and DEQPRE2 - Equation of Motion Pre-Data Initialization

**Purpose:**

Perform the DIPEQ1(1) and DIPEQ2(1) pre-data read functions for vehicle 1 and vehicle 2.

**Method:**

Nominal values of indicators are set, and the integrated variable values are set to zero. Nominal values are set for standard constraints used in the equations (e.g., polar and equatorial radius of planet).

**Remarks:**

A flow chart for DEQPRE is presented. DEQPRE2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines and subprograms.
44. FIRFUN and FIRFUN2 - Fire Control Subprograms

Purpose:
To compute selected fire control function effective time maneuvers.

Method:
The fire control subroutines integrate the period of time that each of three fire control characteristic function constraints are satisfied. The three fire control functions for each vehicle may involve a combination of up to nine trajectory variable values. FIRFUN and FIRFUN2 have the standard EXE entry points. The subprograms are called by DIFEQ and DIFEQ2, respectively.

Remarks:
A flow chart for FIRFUN is presented. FIRFUN2 is identical to FIRFUN except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
GOO

IF FIRE .EQ. 0

VALUES (L, FIRE, I = 1, 3, FIXED, I = 1, 3)

RETURN

RETURN

700

IF FIRE .EQ. 0

I = 1

INTGR INTERVAL, FIRE(I), FIRE(I)

IF I .LT. 3

I = I + 1

RETURN

RETURN

210
GAM91 and GAM92 - Flight through Vertical Routines

Purpose:
To permit each vehicle to fly through the vertical without "locking on" to the wind axis.

Method:
Whenever programmed logic indicates that a vehicle has flown through the vertical, a 180 degree rotation about the velocity vector is introduced. This rotation is combined with the 180 degree rotation introduced by the wind axis transformation at flight through the vertical. The resulting combined rotation permits a smooth passage through the vertical, and Immelmann- or Split S-like maneuvers can be performed.

Remarks:
A flow chart for GAM91 is presented. GAM92 is identical except for use of vehicle 2 COMMON blocks.
46. DEQINI and DEQINI2 — Equation of Motion Post-Data Initialization

**Purpose:**

Perform the DIFEQL(2) and DIFEQ2(2) post-data read function for vehicle 1 and vehicle 2.

**Method:**

This is the initial transformation. It is always performed at the beginning of a trajectory; it may be performed at the beginning of a major stage (see EXTRAN and EXTRAN2). Also, it may be used in certain combinations for the h-transformation (see EXTRAN and EXTRAN2).

**Remarks:**

A flow chart for DEQINI is presented. DEQINI2 is identical except for the use of vehicle 2 COMMON blocks, auxiliary subroutines, and subprograms.

---

![Flow Chart](image-url)

**SUBROUTINE DEQINI**
47. DEQBCI and DEQBCL2 – Derivative Calculation Before Control Definition

**Purpose:**

Perform that part of the equation of motion derivative calculation which precedes the vehicle control definition.

**Remarks:**

A flow chart for DEQBCI is presented; DEQBCL2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.

**DEQBCL**

```
4~7.

Pvrp~pose:
Perform that part of
the equation of motion
derivative calculation
which precedes the vehicle control definition.

Remarks:
A flow chart for DEQBCL is presented; DEQBCL2 is identical except for
the use of vehicle 2 COMMON blocks and auxiliary subroutines.
```
**Purpose:**

To provide an alternative for computing a variable (which would otherwise be a control variable) as a tabular function of any variable already computed.

**Method:**

It is legitimate to use FPPS only to compute those variables which are allowed to be control variables. Up to six different control type variables may be computed through the use of FPPS. FPPS is a subprogram of DIFEQ1; it has the standard entry points. The data for FPPS may be changed at any major stage at which DIFEQ1(2) is called, FPPS will be active only if there is data for it and only if INDFLT is input non-zero.

**Example**

To compute $\alpha = f(Mach)$ the function $f$ is defined pointwise by a two-dimensional table (in the standard manner for setting up tables). It is imperative that Mach have been computed before FPPS is called to evaluate $\alpha$.

When using FPPS, it is imperative to check the coding to be sure that the independent variable of the "$f$" function has actually been computed at the time FPPS is called; if such is not the case then it is sometimes possible to permute the order of calculations in such a manner that this criteria will be satisfied.

**Input Data**

This data must go in the stage data. The data may be inserted at any stage at which the initial transformation is executed.

**Example**

<table>
<thead>
<tr>
<th>FPPS</th>
<th>BCD</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>FPIV</td>
<td>BCD</td>
<td>2SI07D$^D$AMACH</td>
</tr>
<tr>
<td>FPPD</td>
<td>BCD</td>
<td>2BA77D$^D$ALPHD</td>
</tr>
<tr>
<td>FTAB01</td>
<td></td>
<td>4,-90.,180.,-1,180.</td>
</tr>
<tr>
<td>FTAB02</td>
<td></td>
<td>2,0.,10.,2.,5.</td>
</tr>
<tr>
<td>INDFLT</td>
<td></td>
<td>1</td>
</tr>
</tbody>
</table>

FPPS defines the names (at most 6) of the respective independent variables for the tables FTAB01 through FTAB06.
FPFDV defines the names of the respective dependent variables for the tables FTAB01 through FTAB06.

FTAB01:

two dimensional tables corresponding to the definitions set up in FPFDV and FPFDV.

FTAB06:

INDFLT ≠ 0 turns on FPPS
= 0 turns off FPPS

Great care must be exercised in how FPPS is used.

Pemar:is:

A flow chart for FPPS is presented. FPPS2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
49. ONETWO - Transformation of Selected Vehicle 2 Variable to Vehicle 1 COMMON

Purpose:

ONETWO takes variables having a unique name in vehicle 2's COMMON and transfers the variable value to a specified location in vehicle 1's COMMON. The routine is used for the inverse TWOONE transformation when vehicle 1's perturbation equations are employed to perturb a vehicle 2 function, or when a variational problem is terminated. Additional variable transformations may be introduced by simply adding the transformations to both ONETWO and TWOONE.

ONETWO

\[\text{store } m, \dot{m}, \dot{x}_e, \dot{y}_e, \dot{z}_e, x_e, y_e, z_e \text{ from vehicle two's COMMON into vehicle one's COMMON}\]

\[\text{store fire functions and fire function derivatives from vehicle two's COMMON into vehicle one's COMMON}\]

RETURN
50. CTLITR and CTLITR2 - Control Dependent Derivative Calculation

**Purpose:**

CTLITR and CTLITR2 control the calculation of the portion of the derivative calculation which depends on the instantaneous control variable values.

**Method:**

Angle-of-attack and sideslip functions including the \((u, v, w)\) matrix are computed directly. Throttle effects are computed through ANITR or ANITR2. Bank angle effects are computed in BAITR or BAITR2.

**Remarks:**

A flow chart for CTLITR is provided. CTLITR2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
51. DEQACI and DEQACI2 - Derivative Calculation after Control Definition

Purpose:

To carry out secondary derivative calculations following computation of the control dependent functions (e.g., $\dot{y}$ and $\ddot{u}$ computations).

Remarks:

A flow chart for DEQACI is presented. DEQACI2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
**Purpose:**

To provide the capability for flying a specified flight path angle (\( \gamma \)) time history by computation of the angle of attack,

**Method:**

The change in angle of attack is computed to correspond to the second term of the Taylor expansion of \( \alpha (\gamma) \) plus a small correction term.

\[
\alpha = \alpha_i + C ((\gamma_c - \gamma) + (\dot{\gamma}_c - \dot{\gamma}))
\]

where

\[
C = \frac{m V}{\sqrt{A T \cos \alpha + L/\gamma}}
\]

\[
\dot{\gamma}_c = \frac{[(\gamma_c)_t - (\gamma_c')_t - \Delta t]}{\Delta t}
\]

\( \Delta t \) is set equal to 1 second by the program.

\( \alpha_i \) is either an initial input value of \( \alpha \), or the value remaining from previous computation at the entry into FPPG(3).

\( \alpha \) is then limited between a maximum value (ALIMG) set equal to 24° by the program, and a lower limit (ALIML) set equal to -4° by the program.

**Remarks:**

A flow chart for FPPG is presented. FPPG2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
DEQSPI and DEQSPI2 - Derivative Evaluation Initial Point

Purpose:

To provide an initial print heading for the differential equations of motion output.

Remarks:

A flow chart for DEQSPI is provided. DEQSPI2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
54. DEQCOD and DEQCOD2 - Trajectory Code Print

Purpose:

To provide a trajectory history code print for the selected output variables.

Remarks:

A flow chart for DEQCOD is presented. DEQCOD2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
55. DEQVAL and DEQVAL2 - Trajectory History Print

Purpose:

To provide a history of selected variable values along a trajectory.

Remarks:

A flow chart for DEQVAL which generates the first vehicle output values is presented. DEQVAL2 which provides the second vehicle output values is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
56. DEQIV and DEQIV2 - Integrated Variable Specification

Purpose:
To define active integrated variables.

Remarks:
A flow chart for DEQIV is presented. DEQIV2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
DEQHT and DEQHT2 - Trajectory H-Transformation Subroutines

Purpose:

To carry out specified h-transformations at selected stage points.

Remarks:

A flow chart for DEQHT is presented. DEQHT2 is identical except for the use of vehicle 2 COMMON blocks.
58. ERROR and ERROR2 - General Table Error Routine

**Purpose**

To provide a method of indicating the table which may possibly contain an error.

**Method**

Given the subscript of the curve in error, the routine will search the subscript table and find the corresponding BCD word. This word will then be printed as:

"TABLE ERROR AAAAA"

where AAAAAA is the BCD name of table. If the name cannot be found in the directory

"TABLE ERROR

... Location of table not listed in directory..."

is printed and a return to the calling program is made. In either case ENDSHE is set to zero.

**Usage**

Entry is made to the routine with the following statement:

CALL ERROR (LOCZ)

where LOCZ is the table subscript.

**Subroutines Called**

LINES

AURON

Normal FORTRAN I/O routines.

**Remarks:**

A flow chart for ERROR is provided. ERROR2 is identical to ERROR except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
ERROR

INDSTE=0

CALL LINES (2)

CALL ASRCH LOCZ, NAME

NAME = IBK

WRITE 6,1
RETURN

WRITE 6,2
RETURN

230
59. **PTBEQN and PTBEQN2 - Driver Routines for Equations**

**Purpose:**

To duplicate the sequence of calls to subprograms made by EXE for entry points 2 and 3.

**Usage:**

```plaintext
CALL PTBEQN (IENTRY)

IENTRY = 2    make calls to entry points 2
IENTRY = 3    make calls to entry points 3
```

PTBEQN is called only by the PUBR routine. IENTRY is an argument in the call to PUBR from PUBT; PUBR transmits it to PTBEQN. PTBEQN may be looked upon as that routine which drives the particular functional calculation necessary for computing partial derivatives numerically. The indicator INDEQN is set to 1 upon entering PTBEQN and is set to 0 upon leaving; this indicator is not essential to any of the logic but is designed only for diagnostic purposes.

When IENTRY = 2, PTBEQN only calls EXTRAN(3). EXTRAN(3) takes care of evaluating the functional calculation for the initial transformation of major stages (either initial conditions or h-transformation).

PTBEQN controls the transformation of selected vehicle 2 functions into unique vehicle 1 functions for use in two vehicle variational optimization problems. This is achieved by use of the transformation subroutines TWOONE and ONETWO. The selected vehicle 2 functions are perturbed by PTBEQN2 which is called from PTBEQN.

Flow charts for both PTBEQN and PTBEQN2 are presented.
BEGIN
INDNUM = 2
N
INDEQN = 1

ENTRY
= 1
= 2
= 3
CALL DIFEQ2
CALL MANTGE2
CALL LINCOM2
CALL IFCS2
CALL PENAL2

INDEQN = 0
RETURN

CALL EXTRAN2

RETURN
TWOONE - Transformation of Selected Vehicle 1 Variable to Vehicle 2 COMMON

Purpose:

TWOONE takes variables having a unique name in vehicle 1's COMMON and transfers the variable value to a specified location in vehicle 2's COMMON. The routine is used for the inverse ONETWO transformation when vehicle 1's perturbation equations are employed to perturb a vehicle 2 function. Additional variable transformations may be introduced as discussed in the ONETWO write-up.

```
TWOONE

store m, w, x, v, Y, Z
store x, v, and Z from vehicle one's common into vehicle two's common

store first functions and first function derivatives from vehicle one's common into vehicle two's common

RETURN
```
61. **IZERO and IZERO2 - Packs Non-Zero Numbers**

**Purpose**

Test the argument for non-zero and set up indicators for packing.

**Method**

The argument is tested for zero and a switch is set for each word. The switch is on for zero and off for non-zero.

**Usage**

Entry is made to the routine with the following statement:

```
CALL IZERO(IA)
```

where

IA = The number to be packed.

**Remarks**

No other subroutines are called from this routine.
62. **PPLNLN - Main Paper-Plot Routine**

**Purpose:**
To control scale size, construct grids, plot points, and title each paper plot.

**Usage:**
Call PPLNLN (X, Y, NPTS, XMAX, XMIN, YMAX, YMIN, NPLTS, TITLE, IWORDS, TITLEB, NT)

x is the array that contains the values of the independent variable to be plotted

y is the array that contains the values of the dependent variable to be plotted

NPTS number of points to be plotted

XMAX maximum value of plot grid for x axis

XMIN minimum value of plot grid for x axis

YMAX maximum value of plot grid for y axis

YMIN minimum value of plot grid for y axis

NPLTS number of curves to be plotted on this frame

TITLE title to be printed at the top of the plot

IWORDS number of ten character words in TITLE

TITLEB title to be printed at the bottom of the plot

NT number of ten character words in TITLEB
PPLNLN

N = 0

N > 30

N ≠ NPLTS

NWORS = 510
ICPL = 100
INCHAR = S100
ICPN = 10
IPLOT = 0
DX = YMAX - YMIN
DY = YMAX - YMIN

N = N - 1
IPLOT = IPLOT + 1

CALL PLCPTS

DX = 0.0

DX = 1.0

DY = 0.0

DY = 1.0

XSCALE = DX/10.0
YSCALE = DY/8.33333
XP = 100./DX
YP = 100./DY
IFLAG = 0

CALL GRIDXY

N > 0

DWORDS ≠ 0

WRITE: "TITLE"

INDEX = 0

WRITE: "PLOT"

NT ≠ 0

WRITE: "TITLE"

WRITE: "SCALES"

NFRAME = NFRAME + 1

WRITE: "NFRAME"

RETURN

RETURN

CALL PLCPTS

RETURN
63. **SENSOR and SENSOR2 - Vehicle Sensor Routines**

**Purpose:**

To supply each vehicle with a system of sensors for detection of an opponent. Each vehicle may employ up to seven independent sensors.

**Usage:**

Given the opponent's position each sensor is checked sequentially to see whether or not the opponent can be observed. In the present program an opponent is observed when the target's cone angle (in body axes) is less than the sensor half angles and the target's range lies between minimum and maximum limits. The time each sensor observes an opponent is integrated and the time at which a sensor loses an opponent is preserved.

A call to SENSOR or SENSOR2 is made as follows:

```
CALL SENSOR (IENTRY) or CALL SENSOR2 (IENTRY)
```

IENTRY is the standard EXE entry point indicator.

A flow chart for SENSOR is provided. SENSOR2 is identical to SENSOR except for the use of vehicle 2 COMMON blocks.
64. **VISION and VISION2 - Pilot Vision Routines**

**Purpose:**
To supply each pilot with a visual detection model. Visual scans are made at specified time intervals.

**Usage:**
Given the opponent's position a periodic visual check is made to see if the opponent lies between tabular upper and lower elevation limits as a function of target azimuth. If the opponent lies in these elevation limits and is in visual range, it is assumed that he will be detected. A flag is set whenever an opponent is lost from sight and at all times the last two visual sightings are recorded in time, azimuth, elevation, and range senses.

A call to VISION or VISION2 is made as follows:

```plaintext
CALL VISION (IENTRY) or CALL VISION2 (IENTRY)
```

IENTRY is the standard XSE entry point indicator.

A flow chart for VISION is presented. VISION2 is identical except for the use of vehicle 2 COMMON blocks.
VISION

ENTRY

1
INDVIZ = 0
RETURN

4
RETURN

5
IF INDVIZ = 0 THEN RETURN
CODES: \( t_1, t_2, \phi_1, \phi_2, \theta_1, R_1, R_2 \)
RETURN

6
IF INDVIZ = 0 THEN RETURN
VALUES: \( E_1, E_2, \alpha_1, \alpha_2, \phi_1, \phi_2, R_1, R_2 \)
RETURN

7
IF INDVIZ = 0 THEN RETURN
RETURN

8
RETURN

2
TLOCKV = TIME
DTVIZ = DELTS + (IV(0) + 1)
Find location of VTA001 and VTA002
Set minimum and maximum azimuthal vision angles from vision tables.
RETURN

3
IF INDVIZ = 0 THEN RETURN
RETURN

RETURN

IF \( \Delta R > \text{RVISION} \) THEN RETURN

IF \( \Theta_m \leq \Theta_{0a} \text{ and } \Theta_{0a} \geq \Theta_{0a} \text{ as a function of click angle: (VTA001 and VTA002)} \) THEN RETURN

\( t_1, t_2, \theta_1, \theta_2, \phi_1, \phi_2, R_1, R_2 \)
INDVIZ = 1
RETURN

IF INDVIZ \leq 1 THEN RETURN

RETURN
PASSV1 and PASSV2 - Passive Tactics Routine

Purpose:

PASSV1 and PASSV2 serve to interface flight plan program options or fixed control history flight paths with the combat logic. In particular, it converts all such control specifications to the finite control rate option at the analyst's request. A flow chart for PASSV1 is presented. PASSV2 is identical except for use of vehicle 2 COMMON blocks.
```
PASSVI

ENTRY

1000

2000

3000

4000

5000

RETURN

1000

I_PASSV = 0

RETURN

3000

PSGONE "PAUSE MORE"

A_?BO = A_LPHND
BAQTO = B_A?70
AND = AN

RETURN

2000

RETURN

4000

RETURN

6000

RETURN

1000

RETURN

8000

RETURN

245
```
66. **DEFEN1 and DEFEN2 - Defensive Tactics Routine**

**Purpose:**

To select each vehicle's defensive tactic.

**Method:**

ROLE1 and ROLE2 have selected each vehicle's role. When a defensive role is selected, DEFEN1 and DEFEN2 define a specific defensive tactic for vehicles 1 and 2, respectively. Defensive tactics may be selected in random or ordered manner. An override to another specified role is also possible by use of FIXEDR or FIXED2R. The analyst may also specify a minimum elapsed time between tactic changes.

**Remarks:**

A flow chart for DEFEN1 is presented. DEFEN2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
EVADE1 and EVADE2 – Evasive Tactics Routine

Purpose:

To select each vehicle's evasive tactic.

Method:

ROLE1 and ROLE2 have selected each vehicle's role. When an evasive role is requested, EVADE1 and EVADE2 define a specific evasive tactic for vehicles 1 and 2. Tactics may be selected in random or ordered fashion. An override to another specified role is possible by use of FIXEDR or FIXEDR2. The analyst may also specify a minimum elapsed time between tactic changes.

Remarks:

A flow chart for EVADE1 is presented. EVADE2 is identical except for use of vehicle 2 COMMON blocks and auxiliary routines.
68. OFFEN1 and OFFEN2 - Offensive Tactic Routine

Purpose:
To select each vehicle's offensive tactic.

Method:
ROLE1 and ROLE2 have selected each vehicle's role. When an offensive role is requested, OFFEN1 and OFFEN2 define a specific offensive tactic for vehicles 1 and 2, respectively. Offensive tactics may be selected in random or ordered manner. An override to another specified role is also possible by use of FIXEDR or FIXEDR2. The analyst may also specify a minimum elapsed time between tactic changes.

Remarks:
A flow chart for OFFEN1 is presented. OFFEN2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
OFPEN1

ENTRY

1000

2000

3000

4000

5000

RETURN

2000

TCNG = TIME + TOKEN

MORLEN > 3  
MORLEN = SPICK (3)

MORLEN = 0  
MORLEN = SPICK (3)

MORLEN < -5  
MORLEN = SPICK (1)

i = 1, 10

RETURN

3000

MORLEN

RETURN

RETURN

RETURN

4000

JOFLEN

TIME .LT. TCNG

YES

NO

TCNG = TIME + TOKEN

JOFLEN = JOFLEN + 1

JOFLEN .GT. 10

A

JOFLEN = 1

253
69. ATTAC1 and ATTAC2 - Attacking Tactics Routine

Purpose:

To select each vehicle's attacking tactic.

Method:

RCL1 and ROL2 has selected each vehicle's role. When an attacking role is requested, ATTAC1 and ATTAC2 define a specific attacking tactic for vehicles 1 and 2. Tactics may be selected in random or ordered manner. An override to another specified role is also possible by use of FIXEDR and FIXED32. The analyst may also specify a minimum elapsed time between tactic changes.

Remarks:

A flow chart for ATTAC1 is presented. ATTAC2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
Purpose:

To define instantaneous angle-of-attack and bank-angle on the basis of local optimization and constraint criteria.

Method:

A local minimization criteria, $\phi(t)$, and local constraints criteria, $\psi_i(t)$, are created where

$$\phi(t) = \phi(\alpha, \beta_a) \text{ and } \psi_i(t) = \psi_i(\alpha, \beta_a)$$

An inner loop parameter optimization procedure, CTLOPT, is used to define the angle-of-attack and bank-angle combination which satisfies the resulting local ($t = \text{constant}$) optimization problem. The local minimization criteria involve a variety of combat guidance laws. Constraints include a minimum speed override on angle-of-attack, which reduces the angle-of-attack search range and any in-flight inequality constraint defined by IFCS which is directly affected by the control vector (INDBNC1=1). Final steering and force vector errors are also computed in OALPBA and OALPBA2.

Remarks:

A flow chart for OALPBA is presented. OALPBA2 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
OALPBA

all normal search bands
for bank angle and
angle-of-attack

VATF
GT. VMAINE
NO

Minimum speed limit
and selected Mach limits
for angle-of-attack

CTLOPT

A

optimization loop

set bank angle and angle-
of-attack from "RESOP"
parameter setup

CITERI

NPHIAC

10

200

300

400

500

600

700

800

900

1000

z1

z2

z3

z4

z5

z6

z7

z8

z9

z10

259
HIHO and HIHO2 - N-Dimensional Table Call Routine

Purpose

To set up the NA array and Z location of tables with dimension from 3 to 5 as required by the calling sequence to NDTLU which is

CALL NDTLU (ND, NA, X, Z, XA, ZA; LE, NEXIT),

to make the call to NDTLU, and return the function value or data on a table read error.

Usage

Linkage to the subroutine is made via the statement

CALL HIHO (N, LOCZ, NX1, NX2, NX3, NX4, XIARG, X2ARG, X3ARG, X4ARG, A)

where,

N = Dimension of table look-up. When $A = f(X)$ $N = 2$.
LOCZ = Location of the first value in the table.
NX1 to XIARG = Location of number of points in the X1 to X4 arrays of independent variable values.
XIARG to X4ARG = Name of X1 to X4 argument or a dummy location if $N < 5$.
A = Location of the dependent variable.

Subroutines Called

NDTLU, ERROR, LINES
Normal FORTRAN I/O routines

Remarks:

A flow chart for HIHO is presented. HIHO2 is identical except for the use of vehicle 2 COMMON blocks.
72. **TMTX - Transformation Matrix Routine**

**Purpose**

To calculate the transformation matrix, \( N \) given the angles of transformation \( \theta_1, \theta_2, \theta_3 \) and the desired axes about which rotation is to occur.

**Method**

\[
N = \prod_{i=1}^{3} A_i^{-1}
\]

where \( A_i \) is a matrix determined from angle \( \theta_i \). If \( \theta_i = 0 \), \( A_i = I \) (identity matrix).

\( A_i \) is defined as follows:

\[
A_i = \begin{bmatrix}
1 & 0 & 0 \\
0 & \cos \theta_i & \sin \theta_i \\
0 & -\sin \theta_i & \cos \theta_i
\end{bmatrix} = \text{X axis rotation matrix}
\]

when \( K_i = 1 \)

\[
A_i = \begin{bmatrix}
0 & 1 & 0 \\
0 & 0 & 1 \\
\sin \theta_i & -\cos \theta_i & 0
\end{bmatrix} = \text{Y axis rotation matrix}
\]

when \( K_i = 2 \)

\[
A_i = \begin{bmatrix}
\cos \theta_i & 0 & \sin \theta_i \\
-\sin \theta_i & 1 & 0 \\
0 & 0 & 1
\end{bmatrix} = \text{Z axis rotation matrix}
\]

when \( K_i = 3 \)

**Usage**

The transformation matrix routine is entered by the statement:

`CALL TMTX (\( \theta_1, K_2, \theta_2, K_3, \theta_3, M, V \))` where:

1. \( \theta_1, \theta_2, \theta_3 \) define the transformation angles
2. \( K_1, K_2, K_3 \), as indicated above, determine the axis to which the corresponding \( \theta_i \) refers.
3. \( V \) is a 1-dimensional array containing past values of the following:

\[ \sin \theta_1, \cos \theta_1, \cos \theta_2, \sin \theta_2, \cos \theta_3, \sin \theta_3, \cos \theta_3, \]  

(in that order)

4. \( N \) is the 3 x 3 array where the resultant transformation matrix is to be stored.

\( V \) contains the last computed values of each \( \theta_i, \sin \theta_i \). If the current \( \theta_i \) presented by the call statement is such that

\[ |\theta_{\text{new}} - \theta_{\text{old}}| \leq E, \quad E = 1.0 \times 10^{-6} \]

then \( \sin \theta_i, \cos \theta_i \) are not recomputed. If all \( \theta_i \)'s are such that \( |\theta_{\text{new}} - \theta_{\text{old}}| \leq E \), then \( N \) is not recomputed at all. Any recomputed values are stored in the \( V \) array.

To avoid possible errors in the E-test, \( V(1), V(4), \) and \( V(7) \) should be initialized to angles which would never be encountered in the user's program before the first entry into TMTX.

**Note:** For any given transformation, it is assumed that the order of rotation about the 3 axes will not change.

When \( \theta_1 = 0, K_1 \) is ignored.
73. **TRNPOS - A 3 x 3 Matrix Transpose Routine**

**Purpose**
To transpose a 3 x 3 matrix A to obtain the 3 x 3 matrix A'.

**Method**
The resulting transposed matrix is stored in a separate array. All elements of A must be stored in the normal FORTRAN sense (i.e., columnwise).

**Usage**
The transpose of a matrix A is obtained by the statement,

```
CALL TRNPOS (A,B)
```

where,

- A = The variable name of the 3 x 3 matrix A.
- B = The variable name of the 3 x 3 matrix A'.

**Remarks**
This routine calls no other routines.

**TRNPOS**

```
DO 1 i = 1, 3
DO 1 j = 1, 3

Bi,j = Aj,i

RETURN
```

267
MULT31 - A Matrix Multiplication Routine

Purpose
To post-multiply a 3 x 3 matrix by a 3 x 1 matrix.

Method
The result of \( [A][B] = [C] \) is computed using single precision floating point arithmetic. All elements must be stored in the normal FORTRAN sense (i.e., columnwise).

Usage
The matrix multiplication is obtained by the statement:

```
CALL MULT31 (A, B, C)
```

where,
- \( A \) = Array name of the 3 x 3 matrix \([A]\)
- \( B \) = Array name of the 3 x 1 matrix \([B]\)
- \( C \) = Array name of the resulting 3 x 1 matrix \([C]\)

Remarks
This routine calls no other routine.

```
MULT31

DO 1  i = 1,3

   C(i) = 0

1

DO 1  j = 1,3

   \( C(i) = C(i) + A(i,j) \cdot B(j) \)

RETURN
```
Purpose:
To monitor a characteristic structural temperature and/or aerodynamic heating rate.

Method:
This subprogram has all the standard entry points of EXE.

INDHET = 0: No computations made.
INDHET = 1: Wedge skin temperature computed.
INDHET = 2: Hemispherical nose temperature computed.
INDHET = 3: Both wedge skin and hemispherical nose temperatures computed.

DLTSF = 0: Equilibrium temperature computed for wedge skin. Transient temperature computed for hemispherical nose.
DLTSF ≠ 0: Transient temperatures computed for both wedge skin and hemispherical nose.

Remarks:
The following quantities are computed at HETS(3):

QDOTS Convective heating rate of the wedge skin.
TS77RI Rate of change of wedge skin temperature (set equal to zero if DLTSF = 0).
TS77R Wedge skin temperature.
QDOTE Convective heating rate of the hemispherical nose.
TSTGR1 Rate of change of hemispherical nose temperature.
TSTGR Hemispherical nose temperature.
RN2 Reynolds number at edge of boundary layer.
RNCR Critical Reynolds number at edge of boundary layer.

A flow chart for HETS is presented. HETS2 is identical to HETS except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
Purpose:
The single engine thrust and fuel flow program provides the means of introducing the engine thrust and propellant flow rate data. It corrects the thrust for atmospheric effects and resolves the thrust vector into its components.

Usage:
Linkage to TFFS is accomplished via the general statement:

CALL TFFS (IENTRY)

where IENTRY is a fixed point variable.

IENTRY = 1

This performs the pre-data initialization. At this entry the subscripts for all tables are computed and the following data is initialized:

INDTFF = 0 = thrust option indicator
N = 1. = throttle setting
BURNS = 2. = number of identical engines

In addition, the data initialization of TFFM when its IENTRY is 1 is performed under this entry.

IENTRY = 2

This performs the post-data initialization. At this entry the following data is initialized:

\[ m = 0 \] = rate of change of vehicle mass
\[ m_0 = m \] = mass of vehicle
\[ \dot{m}_f = 0 \] = fuel used
\[ T_x = 0 \] = thrust component along x-axis
\[ T_y = 0 \] = thrust component along y-axis
\[ T_z = 0 \] = thrust component along z-axis
\[ T = 0 \] = thrust after atmospheric effects correction
\[ T_{VAC} = 0 \] = vacuum thrust of engine
\[ \dot{m}_f = 0 \] = fuel flow rate
ENTRY = 3

At this entry the thrust components and fuel flow are computed. If INDTPF = 0 no computations are performed. For values of INDTPF of 1 through 5 the following computations are performed:

\[
\begin{align*}
T &= \text{MAX (0, } T_{VAC} - P A_e) \\
\dot{m}_t &= -\dot{m}_e = \text{total rate of change of vehicle mass}
\end{align*}
\]

\(T_{VAC}\) and \(m_e\) are input as tabular data. The functional relationships for the various options are as follows:

<table>
<thead>
<tr>
<th>Value of INDTPF</th>
<th>Option</th>
<th>Functional Relationship</th>
<th>Relationship</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Single Engine Noncontrolled Thrust</td>
<td>(m_t = f(r))</td>
<td>(T_{VAC} = f(r))</td>
</tr>
<tr>
<td>2</td>
<td>Single Engine Controlled Thrust</td>
<td>(m_t = f(N))</td>
<td>(T_{VAC} = f(m_t))</td>
</tr>
<tr>
<td>3</td>
<td>Single Engine Air Breather</td>
<td>(m_t = f(N, h, \alpha, M_p))</td>
<td>(T_{VAC} = f(N, h, \alpha, M_p))</td>
</tr>
<tr>
<td>4</td>
<td>Fractional or Multiple Identical Engine</td>
<td>(m_t = f(h, M_p, N))</td>
<td>(T_{VAC} = f(h, M_p, N))</td>
</tr>
<tr>
<td>5</td>
<td>Simplified Single Engine</td>
<td>(m_t = f(N, h))</td>
<td>(T_{VAC} = f(N, h))</td>
</tr>
</tbody>
</table>

**NOTES:**

While it is possible to change from the single engine option (TFFS) in a given stage to the multieengine option (TFFM) in a later stage, the opposite is not possible.
77. SACS and SACS2 - Aerodynamic Routines

Purpose:
To compute the aerodynamic forces, side force (SIDEF), drag force (DRAGP) and lift force (ALIPTP). SACS is used for vehicle 1; SACS2, for vehicle 2.

Usage:
Linkage is made via the general statement:

CALL SACS (IENTRY)

where IENTRY is a fixed point number.

IENTRY = 1

At this entry curve read subscripts are found by calling subroutine TSRCH and the following variables are initialized:

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>INDAER</td>
<td>0</td>
</tr>
<tr>
<td>INDBAD</td>
<td>0</td>
</tr>
<tr>
<td>L</td>
<td>ALIPTP = 0</td>
</tr>
<tr>
<td>D</td>
<td>DRAGP = 0</td>
</tr>
<tr>
<td>Y</td>
<td>SIDEP = 0</td>
</tr>
<tr>
<td>C_D</td>
<td>CD4NU = 0</td>
</tr>
<tr>
<td>C_T</td>
<td>CT4NU = 0</td>
</tr>
<tr>
<td>C_L</td>
<td>CL4NU = 0</td>
</tr>
<tr>
<td>h_{aero}^{max}</td>
<td>AMAXH = 10^6</td>
</tr>
<tr>
<td>AMAXA</td>
<td>= 300000.</td>
</tr>
<tr>
<td>AINCD</td>
<td>= 1.</td>
</tr>
<tr>
<td>CPK1</td>
<td>= 0</td>
</tr>
<tr>
<td>CPK2</td>
<td>= 0</td>
</tr>
<tr>
<td>INDAO1</td>
<td>= 0</td>
</tr>
<tr>
<td>INDAO2</td>
<td>= 0</td>
</tr>
<tr>
<td>INDAO3</td>
<td>= 0</td>
</tr>
<tr>
<td>INDAO4</td>
<td>= 0</td>
</tr>
<tr>
<td>Variable</td>
<td>Value</td>
</tr>
<tr>
<td>----------</td>
<td>-------</td>
</tr>
<tr>
<td>INDA07</td>
<td>0</td>
</tr>
<tr>
<td>INDA10</td>
<td>0</td>
</tr>
<tr>
<td>INDA11</td>
<td>0</td>
</tr>
<tr>
<td>INDA12</td>
<td>0</td>
</tr>
<tr>
<td>INDA13</td>
<td>0</td>
</tr>
<tr>
<td>INDA14</td>
<td>0</td>
</tr>
<tr>
<td>INDA17</td>
<td>0</td>
</tr>
<tr>
<td>INDA24</td>
<td>0</td>
</tr>
<tr>
<td>INDA25</td>
<td>0</td>
</tr>
<tr>
<td>INDA26</td>
<td>0</td>
</tr>
<tr>
<td>INDA27</td>
<td>0</td>
</tr>
<tr>
<td>INDA28</td>
<td>0</td>
</tr>
<tr>
<td>INDA31</td>
<td>0</td>
</tr>
<tr>
<td>INDA80</td>
<td>0</td>
</tr>
<tr>
<td>INDA90</td>
<td>0</td>
</tr>
<tr>
<td>INDA91</td>
<td>0</td>
</tr>
<tr>
<td>INDA92</td>
<td>0</td>
</tr>
</tbody>
</table>

**ENTRY = 2**

Checks to see if INDAER is less than 0 and if so sets INDAER to 0.

**ENTRY = 3**

If INDAER is 0 no computation. If INDAER is nonzero a check is made on altitude (HGC7F). If altitude is greater than AMAXH then the following variables are set:

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>ALIPTP</td>
<td>0</td>
</tr>
<tr>
<td>DRAGP</td>
<td>0</td>
</tr>
<tr>
<td>SIDEF</td>
<td>0</td>
</tr>
</tbody>
</table>
If altitude is less than AMAXH a test is made on the data input value (AMAXA). If altitude (HGCTF) is greater than AMAXA then the following variables are set before ALIFTP, DRAGP and SIDEP are computed.

\[
\begin{align*}
CA &= \text{CDMNU} \\
CYA &= \text{CYMNU} \\
CL &= \text{CLMNU}
\end{align*}
\]

If the altitude is less than the input value AMAXA the following variables are set.

\[
\begin{align*}
CA &= 0 \\
CYA &= 0 \\
CN &= 0
\end{align*}
\]

at this time a test is made on the INDAER for the option chosen.

**INDAER = 1**

If INDA90 is 0 then CN is unchanged;

If INDA90 = 1

\[
CN = f(\text{ALPHD}, \text{AMACH}).
\]

If INDA90 = 2

\[
CN = f(\text{ALPHD}, \text{AMACH}, \text{HGCTF})
\]

If INDA91 is 0 then CA is unchanged, if not

\[
CA = f(|CN|, \text{AMACH}).
\]

CYA is set to 0.

If INDA01 is 0 then DELCA is set to 0, if INDA01 is nonzero then

\[
\begin{align*}
\text{DELCA} &= f(\text{AMACH}). \\
\text{CA} &= f(\text{CA} + \text{DELCA})
\end{align*}
\]

If INDA02 is 0 then CPAK1 is unchanged, if INDA02 is nonzero then

\[
\text{CPAK1} = f(\text{AMACH})
\]

If INDA03 is 0 CPAK2 is unchanged, if INDA03 is nonzero then

\[
\text{CPAK2} = f(\text{AMACH})
\]

Cockpit and pitch angle are computed as auxiliary computations as follows:

\[
\begin{align*}
\text{CPA7D} &= \text{Cockpit } \alpha = \text{CPAK1} \cdot \alpha + \text{CPAK2} \\
\text{PA77D} &= \text{Pitch angle} = \gamma + \alpha \cos \beta_A - \text{AINCD}
\end{align*}
\]

After this computation ALIFTP, DRAGP and SIDEP are computed.
\textbf{INDAER} = 2

\begin{align*}
\text{RA} & = \frac{VA77F}{NUA7F} \quad \text{where} \\
\text{RA} & = \text{Reynolds Number} \\
VA77F & = \text{Velocity, } V_A \\
NUA7F & = \text{Kinematic Viscosity, } \nu
\end{align*}

If \text{INDA00} is 0, \text{CA}_0 = \text{CAVAH} = 0, if \text{INDA00} is nonzero then

\[ \text{CA}_0 = \text{CAVAH} = f(RN, AMACH) \]

If any of the following indicators are nonzero, then the respective coefficients are computed as a function of Mach number.

| \text{INDA01} | \text{CAALPH} | \text{CA}_\alpha | f(AMACH) |
| \text{INDA02} | \text{CAALSQ} | \text{CA}_\alpha^2 | f(AMACH) |
| \text{INDA03} | \text{CABETA} | \text{CA}_\beta | f(AMACH) |
| \text{INDA04} | \text{CAETSQ} | \text{CA}_\beta^2 | f(AMACH) |
| \text{INDA07} | \text{CAALBT} | \text{CA}_\alpha \beta | f(AMACH) |
| \text{INDA10} | \text{CNIZER} | \text{CN}_0 | f(AMACH) |
| \text{INDA11} | \text{CNLALP} | \text{CN}_\alpha | f(AMACH) |
| \text{INDA12} | \text{CNALSQ} | \text{CN}_\alpha^2 | f(AMACH) |
| \text{INDA13} | \text{CNLBT} | \text{CN}_\beta | f(AMACH) |
| \text{INDA14} | \text{CNLBSQ} | \text{CN}_\beta^2 | f(AMACH) |
| \text{INDA17} | \text{CNLALB} | \text{CN}_\alpha \beta | f(AMACH) |
| \text{INDA24} | \text{CTZERO} | \text{CT}_0 | f(AMACH) |
| \text{INDA25} | \text{CTALPH} | \text{CT}_\alpha | f(AMACH) |
| \text{INDA26} | \text{CYALSQ} | \text{CY}_\alpha^2 | f(AMACH) |
| \text{INDA27} | \text{CTBETA} | \text{CT}_\beta | f(AMACH) |
| \text{INDA28} | \text{CTBSTSQ} | \text{CT}_\beta^2 | f(AMACH) |
| \text{INDA31} | \text{CYALBT} | \text{CY}_\alpha \beta | f(AMACH) |
From these coefficients \( CA, CN \) and \( CYA \) are computed as:

\[
CA = \frac{1}{2} \left( \alpha \right) \left( CA + CA_0 + \alpha^2 CA^2 + \beta \right) \left( CA_\beta + \beta^2 CA_\beta^2 + CA_\alpha \beta_\alpha \right) \\
CN = \alpha \left( CN_\alpha + CN_0 + \alpha \right) \left( CN_\alpha + CN_0 + \alpha \right) \left( \beta \right) \left( CN_\beta + \beta^2 CN_\beta^2 + \beta \alpha^2 CN_\alpha \beta_\alpha \right) \\
CYA = \frac{1}{2} \left( \alpha \right) \left( CY_\alpha + CY_0 + CY_\alpha^2 + \beta \right) \left( CY_\beta + \beta^2 CY_\beta^2 + \alpha^2 CY_\alpha \beta_\alpha \right)
\]

After this computation \( \text{ALIPFP}, \text{DRAGP} \) and \( \text{SIDEFP} \) are computed.

\text{INDAER} = 3

If \( \text{INDA90}, \text{INDA91} \) and \( \text{INDA92} \) are 0, \( CA, CN \) and \( CYA \) respectively are unchanged but if either indicator is nonzero, the coefficients are computed as follows:

If \( \text{INDA90} \neq 0 \)
\( CA = f(\text{ALPHD}, \text{BETAD}, \text{AMACH}) \)

If \( \text{INDA91} \neq 0 \)
\( CN = f(\text{ALPHD}, \text{BETAD}, \text{AMACH}) \)

If \( \text{INDA92} \neq 0 \)
\( CYA = f(\text{ALPHD}, \text{BETAD}, \text{AMACH}) \)

The routine then computes lift, drag and side force.

\text{INDAER} = 4

If \( \text{INDA90}, \text{INDA91} \) and \( \text{INDA92} \) are 0, then \( CA, CN \) and \( CYA \) are unchanged. If any of the indicators are nonzero, the coefficients are computed as follows:

If \( \text{INDA90} \neq 0 \)
\( CA = f(\text{AMACH}, \text{ALPHD}) \)

If \( \text{INDA91} \neq 0 \)
\( CN = f(\text{AMACH}, \text{ALPHD}) \)

If \( \text{INDA92} \neq 0 \)
\( CYA = f(\text{AMACH}, \text{ALPHD}) \)

With these coefficients lift, drag and sideslip are computed.

\text{INDAER} = 5

If any of the indicators listed are set to 0 the respective coefficient is unchanged. If any indicators are nonzero the coefficients are computed as follows:

If \( \text{INDA10} \neq 0 \)
\( \text{CANIN} = f(\text{AMACH}) \)

If \( \text{INDA11} \neq 0 \)
\( \text{ELPRIM} = f(\text{AMACH}) \)

If \( \text{INDA12} \neq 0 \)
\( \text{ZK} = f(\text{AMACH}) \)

If \( \text{INDA13} \neq 0 \)
\( \text{CLZ} = f(\text{AMACH}) \)

283
CA = CAMIN + ELPRIM (CN-CLZ)^2 + 2K(CN-CLZ)^6 + DELCA

Cockpit alpha and pitch angle are computed as auxiliary computation.

CPA7D = Cockpit \( \alpha \) = CPA10 + CPAK2

PA77D = Pitch angle = \( \gamma + \alpha \cos B_A - \text{AINCD} \)

with the above computation lift, drag and sideslip are computed.

INDA90 ≠ 0, INDA91 = 0

CA = \text{f}(\text{AMACH},HGC7F)

INDA90 ≠ 0, INDA91 ≠ 0

CA = \text{f}(\text{AMACH},HGC7F)

CN = \text{f}(\text{AMACH},HGC7F)

INDA90 = 0, INDA91 ≠ 0

CA = \text{f}(\text{ALPHD})

INDA90 = 0, INDA91 = 0

CN = \text{f}(\text{AMACH})

LIFT, DRAG, SIDE FORCE

If INDBAD ≠ 0, the following computations are made.

CD = CA

CY = CYA

CL = CN

If INDBAD = 0, the following computations are made.

\[
\begin{bmatrix}
-CD \\
CT \\
-CL
\end{bmatrix} = 
\begin{bmatrix}
uvw \\
-CA \\
CTA \\
-CN
\end{bmatrix} 284
\]
With these coefficients lift, drag and side force are computed as follows:

\[
\begin{align*}
\text{LIFT} &= ALIFTP = q S (\epsilon_1 CL + \epsilon_2) \\
\text{DRAG} &= DRAGP = q S (\epsilon_3 CD + \epsilon_4) \\
\text{SIDE FORCE} &= SIDEF = q S (\epsilon_5 CY + \epsilon_6) \\
q &= \text{dynamic pressure}
\end{align*}
\]

\(\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4, \epsilon_5, \text{ and } \epsilon_6\) are input error constants

\(S\) = reference area.

**ENTRY = 4**
Not used.

**ENTRY = 5**
A test is made on INDAER if 0, no computation. If INDAER is equal to 2 the following codes are printed.

\[
\begin{align*}
\text{CAVAH} & \quad \text{CL} \quad \text{CD} \quad \text{CY} \quad \text{L7D}
\end{align*}
\]

If INDAER = 1, the following codes are printed:

\[
\begin{align*}
\text{CL} & \quad \text{CD} \quad \text{CY} \quad \text{L7D} \quad \text{PA77D} \quad \text{CPA7D}
\end{align*}
\]

If INDAER = 5, the following codes are printed:

\[
\begin{align*}
\text{CL} & \quad \text{CD} \quad \text{CY} \quad \text{L7D} \quad \text{PA77D} \quad \text{CPA7D}
\end{align*}
\]

For any other value of INDAER \(\neq 0\), the following codes are printed:

\[
\begin{align*}
\text{CL} & \quad \text{CD} \quad \text{CY} \quad \text{L7D}
\end{align*}
\]

**ENTRY = 6**
With this entry the corresponding values to the code in entry 5 are printed.

\[
\begin{align*}
\text{CL} &= \text{Lift force coefficient} \\
\text{CD} &= \text{Drag force coefficient} \\
\text{CY} &= \text{Aerodynamic side force coefficient} \\
\text{L7D} &= \text{This will be 0 if CD is 0, if not L7D = CL/CD} \\
\text{PA77D} &= \gamma + \alpha \cos \alpha - \sin \alpha \\
\text{CPA7D} &= \text{CPA1} \cdot \alpha + \text{CPA2}
\end{align*}
\]
LATS and LATS2 – Geodetic-Geocentric Conversion

Purpose:
To compute the geocentric latitude in terms of the geodetic latitude and vice versa. LATS is used for vehicle 1; LATS2, for vehicle 2.

Usage:
CALL LATS (IENTRY, PHIC, PHIG, TMP)

IENTRY = 1 compute geocentric latitude in terms of geodetic latitude
= 2 compute geodetic latitude in terms of geocentric latitude

PHIC the geocentric latitude (degrees)
PHIG the geodetic latitude (degrees)
TMP an array of dimension ≥ 7 for temporary calculations

The COMMON variables HGCTF, RP77F, RE77F, R777F are used also.

Method:
IENTRY = 1: h, Rp, Rp, φg given

\[ \phi_c = \tan^{-1} \left[ \frac{R_p \cos \phi_c + h \sin \phi_c}{R_p \cos \phi_c + h \cos \phi_c} \right] \]

IENTRY = 2: R, Rp, RE, φc given

\[ U_o = 1 \]
\[ U_n = \left( \frac{R_p}{R_E} \right) + \left[ \frac{R_p^2 - R_c^2}{R_p R_c + R_c} \right] \left[ \frac{U_{n-1}}{\cos^2 \phi_c + (U_{n-1} \sin \phi_c)^2} \right] \]

\[ U_b = \frac{U_1 \sqrt{U_2 - U_2}}{U_1 + U_2 - 2U_2} \]
\[ \phi_G = \tan^{-1} \left[ \frac{R_p}{R_p \tan \phi_c} \right] \]
79. ATMS and ATMS2 - Atmosphere Selector

Purpose:
To enable the user to select which atmosphere (1959 or the 1962 atmosphere) that will be used by the program.

Usage:
CALL ATMS (HGC7F)

HGC7F = The initial altitude that will be used by ATMS59 or ATMS62.

INDATM = 2 selection of the 1962 atmosphere.
INDATM # 2 selection of the 1959 atmosphere.

Remarks
ATMS59 or ATMS62 is called only by DIFEQ. A flow chart for ATMS is presented. ATMS2 is identical except for the use of vehicle 2 COMMON blocks and subroutines.
80. **GVSP and GVSP2 - Gravitational Routine**

**Purpose**

To compute the components of gravitational acceleration within a local geocentric coordinate system.

**Usage**

CALL GVSP

The equations used were adapted from the gravity potential equation. The number of spherical harmonics included in the computation is determined by inputing an integral value from 0 to 4 for INDGVT. The nominal value for INDGVT is 4.

The equations pertain to the planet Earth; however, it is possible to use these same equations for any other planet. For this reason, the values of the coefficients are placed as an input to the program so that the applicable coefficients may be inserted for the planet under consideration. The following give the necessary planet change as well as the nominal values for the planet Earth.

\[
\begin{align*}
    RE77F & = R_e = 20926428. \text{ ft.} & \text{= equatorial radius} \\
    RP77F & = R_p = 20855965. \text{ ft.} & \text{= polar radius} \\
    \mu & = 1.407698 \times 10^{16} \text{ ft}^2/\text{sec}^2 & \text{= gravity constant} \\
    KGRAV & = K = 6.37 \times 10^{-6} & \text{= 3rd spherical harmonic} \\
    HG & = H = 6.04 \times 10^{-6} & \text{= 2nd spherical harmonic} \\
    AJG & = J = 1.62341 \times 10^{-3} & \text{= 1st spherical harmonic}
\end{align*}
\]

**Remarks:**

A flow chart for GVSP is presented. GVSP2 is identical except for the use of vehicle 2 COMMON blocks.
81. ANITR and ANITR2 - Throttle Dependent Derivative and Thrust Vector Calculation

Purpose:

ANITR and ANITR2 compute that portion of the derivative calculation which directly depends on the throttle setting and thrust angles.

Method:

Propulsion system effects are computed from TFFS and TFFS2. A thrust vector transformation accounts for the possibility of thrust vector control. Load factors are optionally computed. Heating and aerodynamic routines HETS, HETS2, SACS, and SACS2 are called from ANITR and ANITR2 in anticipation of subsequent requirements to account for propulsion system interaction on aerodynamics and heating.

Remarks:

A flow chart for ANITR is provided. ANITR2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
BAITR and BAITR2 - Bank Angle Dependent Derivative Calculation

Purpose:

To carry out that portion of the derivative calculation which is directly dependent on the bank angle.

Method:

Computes the \((r, s, t)\) matrix through TMTX or TMTX2 then computes total force components in the rotating earth-centered coordinate system, \((X_E, Y_E, Z_E)\)

Remarks:

A flow chart for BAITR is provided. BAITR2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
Purpose:
To provide a BCD word look up from a subscript.

Method:
Given a subscript the routine will search the directory for the BCD word corresponding to that subscript. If the subscripts do not compare the BCD name is set to blank and return to the Calling Program is made.

Usage:
Entry is made to the routine with the following statement:

```
CALL ASRCH (LOC1,STM1)
```

where,

- **LOC1** = subscript being searched.
- **STM1** = The variable into which the routine is to store the corresponding BCD name.

No other routines are called from this routine.

Remarks:
A flow chart for ASRCH is presented. ASRCH2 is identical except for use of vehicle 2 COMMON blocks.
ASRCH

DO 2000 I = 1, MAXT

LOC1 ≠ LOCS(i)

SYM1 = STABLE(i)

RETURN

2000 CONTINUE

SYM1 = BLANK

RETURN
GRIDXY - Paper Plot Grid Routine

Purpose:
To set up the grid for paper plots

Usage:
Call GRIDXY (PLOT, XMIN, XMAX, YMIN, YMAX, DX, DY)

Where

PLOT is an array into which the plot characters and grid characters are placed to produce the finished plot. The finished plot will contain 51 lines of 102 characters per line.

XMIN minimum x value for the grid
XMAX maximum x value for the grid
YMIN minimum y value for the grid
YMAX maximum y value for the grid
DX number of divisions on x axis
DY number of divisions on y axis
85. PLCPTS - Paper Plot Point Placing Program

Purpose:
To place plotted points on the grid formed by GRIDXY.

Usage:
Call PLCPTS (PLOT, X, Y, NPTS, IPATH, IPLOT, NFRAME, IFLAG, XMIN, YMAX, XP, YP)

Where
PLOT is an array into which the plot characters and grid characters are placed to produce the finished plot. The finished plot will contain 51 lines of 102 characters per line.

X is the array that contains the values of the independent variable to be plotted.

Y is the array that contains the values of the dependent variable to be plotted.

NPTS number of points to be plotted.

IPATH not used.

IPLOT subscript used to select plot symbol.

NFRAME frame number to be printed at the bottom of the plot.

IFLAG flag set equals 1 if points have fallen off the plotting area.

XMIN minimum x value.

XMAX maximum y value.

XP x plot increment.

YP y plot increment.
PLCPTS

\[ \text{ICHK} = IB \]
\[ \text{NBDPTS} = 0 \]
\[ \text{IPT} = \text{IPTS}(1) \]

Do 600 \( n = 1, \text{NPTS} \)

\[ \text{YE} = (YMAX - YN) * YP + 1.4999 \]

Yes

\[ \text{YN} < 0.0 \]

No

\[ \text{I} = \text{YI} \]
\[ \text{XI} = (XN - XMIN) * XP + 1.4999 \]

Yes

\[ \text{XJ} = XJ - .000001 \]

No

\[ \text{XN} > 0.0 \]

No

\[ \text{J} = \text{XJ} \]

Yes

\[ J < 1, \text{or} \]
\[ J > 10.0 \]

No

\[ \text{I} < 1, \text{or} \]
\[ I > 51 \]

No

\[ \text{NBDPTS} > 0 \]

\[ \text{CALL GET} \]

Yes

\[ \text{ICLK} = \text{IA}_{n+1} \text{.2} \text{.1} \text{.0} \]

No

\[ \text{CALL PUT} \]

\[ \text{CALL PUT} \]

600 Continue

RETURN

WRITE: * IPLUG, NFRAME *

WRITE: * N, X_n, Y_n *

NBDPTS = NBDPTS + 1

IFLAG = 1
86. **IPICK - Random Tactic Selector**

**Purpose:**

Subroutine IPICK nominally fills both vehicle 1 and vehicle 2 role selection tables with random arrays of tactics.

**Usage:**

```plaintext
CALL IPICK(N)
```

where N is the number of random tactics to be selected.

---

**IPICK(N)**

1. \( R = \text{RUNIF}(1.0) \)
2. \( I = 1 \)
3. \( T = \text{FLOAT}(1)/\text{FLOAT}(N) \)
   
   \( IP = I \)

If \( IP = R . \lt T \)

- \( IPICK = IP \)
- **RETURN**

Else

- \( I = I + 1 \)
- If \( I = N \)

```
87. **DEFEN11 and DEFEN21 - First Defensive Tactic**

**Purpose:**
To steer each vehicle along a path giving a maximum rate of turn. The tactic is a hard turn in the vertical plane.

**Remarks:**
A flow chart for DEFEN11 is presented; DEFEN12 is identical except for use of vehicle 2 COMMON blocks.

**DEFEN12 and DEFEN22 - Second Defensive Tactic**

**Purpose:**
DEFEN12 and DEFEN22 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic is a hard turn into the opponent at an altitude dependent bank-angle. A flow chart for DEFEN12 is presented. DEFEN22 is identical except for use of vehicle 2 COMMON blocks.

**DEFEN13 and DEFEN23 - Third Defensive Tactic**

**Purpose:**
DEFEN13 and DEFEN23 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic restates the target's line-of-sight vector at a maximum possible rate. Local angle-of-attack and bank-angle perturbations determine control values which maximize the vector product magnitude,

$$|\overrightarrow{LOS_T} \times \overrightarrow{F_T}|$$

where $\overrightarrow{F_T}$ is the total force vector, and $\overrightarrow{LOS_T}$ is the target's line-of-sight vector. A flow chart for DEFEN13 is presented. DEFEN23 is identical except for the use of vehicle 2 COMMON blocks and auxiliary routines.

**DEFEN14 and DEFEN24 - Fourth Defensive Tactic**

**Purpose:**
DEFEN14 and DEFEN24 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic rotates the target's lead-pursuit vector at a maximum rate. Local angle-of-attack and bank-angle perturbations determine control values which maximize the vector product magnitude

$$|\overrightarrow{LAT_T} \times \overrightarrow{F_T}|$$

where $\overrightarrow{F_T}$ is the total force vector, and $\overrightarrow{LAT_T}$ is the target's lead-pursuit vector. A flow chart for DEFEN14 is presented. DEFEN24 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
**DEFEN15 and DEFEN25 - Fifth Defensive Tactic**

**Purpose:**

DEFEN15 and DEFEN25 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic rotates a proportional vector, $\vec{v}_R$, which is a linear combination of target's lead-pursuit angle and target's line-of-sight vectors at a maximum possible rate. Local angle-of-attack and bank-angle perturbations determine control values which maximize the vector produce magnitude

$$| \vec{v}_R \times \vec{F}_T |$$

Here, $\vec{F}_T$ is the total force, and $\vec{v}_R$ is the target's reference vector.

**Remarks:**

A flow chart for DEFEN15 is presented. DEFEN25 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.

**DEFEN16 and DEFEN26 - Sixth Defensive Tactic**

**Purpose:**

DEFEN16 and DEFEN26 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic performs a "Split-S" under an opponent. The initial maneuver through the vertical is a simple Split-S. Once through the vertical has been accomplished, the reference vehicle maintains the Split-S but banks underneath the opponent.

**Remarks:**

A flow chart for DEFEN16 is presented. DEFEN26 is identical except for use of vehicle 2 COMMON blocks and auxiliary routines.

**DEFEN17 and DEFEN27 - Seventh Defensive Tactic**

**Purpose:**

DEFEN17 and DEFEN27 are ENTRY points in DEFEN11 and DEFEN21, respectively. The tactic develops a maximum specific energy path in a vertical plane. Angle-of-attack, which maximizes $E$ at time $\Delta T$ ahead along the predicted flight path, is determined by local control perturbation. The tactic includes logic to force a transfer to supersonic conditions. A flow chart for DEFEN17 is presented. DEFEN27 is identical except for use of vehicle 2 COMMON blocks and auxiliary routines.

302
DEFEN11

MSGONE
"maximum rate of turn"

BAD70 = SIGN(20., BAD70)
ALPOO = ANMAX
AND = ANMAX

RETURN

DEFEN12

MSGONE
"hard turn"

AND = ANMAX * CPON(18)
ALPOO = ANMAX * CPON(19)

TLU(MGC7F, LOC801, BAD70)

BAD70 = SIGN(BAD70, AL180)

RETURN
DEFEN7

MSCANIE

maximum specific energy path

AMACH

LT. MSUBE

NO

MLC7F

GT. MSUBE

NO

3H2O2V

EQ.

1

NO

AMACH

LT. MSUBE

NO

AMACH

GT. MSUBE

YES

INDDIV = 0

YES

ALPDD = AMAXD

NPHIAC = 10

OALPBA

ALPDD = AMAXD

NPHIAC = 4

OALPBA

RETURN

ALPDD = ALPDD/2.0

INDDIV = 1

OALPBA

RETURN

ALPDD = AMAXD

NPHIAC = 10

OALPBA

GAM70

LT. GAM70

NO

RETURN
**Purpose:**

To provide a means for overriding the combat role selection logic.

**Method:**

When the tactic selection indicator, MOFFENi, is negative, the role selection is overridden, and the role is selected on the basis of MOFFENi as follows:

\[
\begin{align*}
\text{MOFFENi} & = -1, \text{ Passive} \\
& = -2, \text{ Defensive} \\
& = -3, \text{ Evasive} \\
& = -4, \text{ Offensive} \\
& = -5, \text{ Attacking}
\end{align*}
\]

**Remarks:**

A flow chart for FIXEDR is presented. FIXEDR2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
89. **EVADE11 and EVADE21 - First Evasive Tactic**

**Purpose:**
To steer each vehicle into a hard pull-up maneuver. A flow chart for EVADE11 is presented. EVADE21 is identical except for use of vehicle 2 COMMON blocks.

**EVADE12 and EVADE22 - Second Evasive Tactic**

**Purpose:**
EVADE12 and EVADE22 are ENTRY points in EVADE11 and EVADE21, respectively. They steer each vehicle in a random weaving maneuver. A flow chart for EVADE12 is presented. EVADE22 is identical except for use of vehicle 2 COMMON blocks.

**EVADE13 and EVADE23 - Third Evasive Tactic**

**Purpose:**
EVADE12 and EVADE23 are ENTRY points in EVADE11 and EVADE21. They steer each vehicle into a Split-S. A flow chart for EVADE13 is presented. EVADE23 is identical except for the use of vehicle 2 COMMON blocks.

**EVADE14 and EVADE24 - Fourth Evasive Tactic**

**Purpose:**
EVADE14 and EVADE24 are ENTRY points in EVADE11 and EVADE21. They steer each vehicle in a random sequence of hard turns. The direction of the turns is changed at intervals of TIMEWA. A flow chart for EVADE14 is presented. EVADE24 is identical except for use of vehicle 2 COMMON blocks.

**EVADE15 and EVADE25 - Fifth Evasive Tactic**

**Purpose:**
EVADE15 and EVADE25 are ENTRY points in EVADE11 and EVADE21. They steer each vehicle towards a vertical dive. At $\gamma = 90 - \alpha_{max}$, the maneuvers become zero lift dives. A flow chart for EVADE15 is presented. EVADE25 is identical except for use of vehicle 2 COMMON blocks.

**EVADE16 and EVADE26 - Sixth Evasive Tactic**

**Purpose:**
EVADE16 and EVADE26 are entry points in EVADE11 and EVADE21, respectively. They steer each vehicle into a random rolling maneuver with maximum angle-of-attack and sideslip. A flow chart for EVADE16 is presented. EVADE26 is identical except for use of vehicle 2 COMMON blocks.
EVADE 11

MSGONE
"and pull up"

ALPDD = AMAXD
AND = ANMAX
BADDD = 0.0

RETURN

EVADE 12

MSGONE
"random weave"

ALPDD = AMAXD
AND = ANMAX
BETDD = BEMXBD
R = RUNIF(1.0)*20 - 1.0
BADDD = BATTD*SIGN(1000, R)

RETURN
EVADE13

MSGONE "Apply S"

AND = ANMAX
ALPDD = AMAXD
BADDD = SIGN(120.,BADDD)

RETURN

EVADE14

MSGONE "Hard Enact"

ALPDD = AMAXD
AND = ANMAX

TIME
LT.
INEWBA

YES
RETURN

NO

TNF""CA = THGWBA+TEVADE
R = RUNIF(1.0)*2.0 - 1.0
BADDD = SIGN(90.,R)

RETURN
EVADE 15

MSE ONE
"vertical dive"

BAD70 = SIGN(180, BAD70)
ALPDD = AMAXD
AND = ANMAX

GAM70 LT. 90. - AMAXD

YES

ALPDD = 0.0
RETURN

NO
RETURN

EVADE 16

MSE ONE
"rolling"

ALPDD = CRMS511/AMAXD
BET0 = LPMS511 x 8000/D0

BAD70 GR. 18070 + 100.

RETURN

BAD70 = CRMS70 + SIGMA(1000, g)

RETURN
OFFEN11 and OFFEN21 - Lag-Pursuit Offensive Tactic

Purpose:
To steer each vehicle along a lag-pursuit course.

Method:
When the first offensive tactic is selected, a vehicle flies a lag-pursuit course determined by force maximization along the lag-pursuit vector. Instantaneous bank-angle perturbation defines the desired control variable values.

Remarks:
A flow chart for OFFEN11 is presented. OFFEN21 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.
91. OFFEN12 and OFFEN22 - Lead-Pursuit Offensive Tactic

Purpose:
To steer each vehicle along a lead-pursuit course.

Method:
When the second offensive tactic is selected, a vehicle flies a lead-pursuit course determined by force maximization along the lead-pursuit vector. Instantaneous angle-of-attack and bank-angle perturbations define the desired control variable values.

Remarks:
A flow chart for OFFEN21 is presented. OFFEN22 is identical except for use of vehicle COMMON blocks and auxiliary subroutines.

OFFEN12 and OFFEN22 are ENTRY points in OFFEN11 and OFFEN12.
92. OFFEN13 and OFFEN23 - Reference Vector Offensive Tactic

Purpose:
To steer each vehicle along a reference vector course which is a linear combination of the lead-angle and line-of-sight vectors.

Method:
When the first offensive tactic is selected, a vehicle flies a reference vector pursuit course determined by force maximization along the reference vector. Instantaneous angle-of-attack and bank-angle perturbations define the desired control variable values.

Remarks:
A flow chart for OFFEN13 is presented. OFFEN23 is identical except for use of vehicle 2 COMMON blocks and auxiliary subroutines.

OFFEN13 and OFFEN23 are entry points in OFFEN11 a 1 OFFEN21.

[Flowchart diagram of OFFEN13 and OFFEN23]
93. ATTACL1 and ATTAC21 – First Attacking Tactic

Purpose:

To steer each vehicle along a path which simultaneously tracks the firing point and eliminates any steering errors.

Method:

When the first attacking tactic is selected, a vehicle steers in a manner calculated to eliminate steering errors and track the firing point. Instantaneous bank-angle perturbations define the desired bank-angle; angle-of-attack is determined by subsequent minimization of the difference between force magnitude and force magnitude required.

Remarks:

A flow chart for ATTACL1 is presented; ATTAC21 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
94. **ATTAC12 and ATTAC22 - Second Attacking Tactic**

**Purpose:**

ATTAC12 and ATTAC22 are ENTRY points in ATTAC11 and ATTAC21, respectively. The second attacking tactic is identical to the second offensive tactic.

**ATTAC13 and ATTAC23 - Third Attacking Tactic**

**Purpose:**

ATTAC13 and ATTAC23 are ENTRY points in ATTAC11 and ATTAC21, respectively. The third attacking maneuver is identical to the third offensive maneuver.

**ATTAC14 and ATTAC24 - Fourth Attacking Tactic**

**Purpose:**

ATTAC14 and ATTAC24 are ENTRY points in ATTAC11 and ATTAC21, respectively. The fourth attacking maneuver is identical to the first offensive maneuver.
95. CTLOPT – Internal AESOP Optimization Loop

Purpose:

To provide an internal parameter optimization capability independent of the outer trajectory or design optimization loop.

Method:

A control program essentially identical to the AESOP control program is created. The outer parameter optimization data base is preserved on tape at trajectory commencement and is retrieved at trajectory termination. During the trajectory CTLOPT through IMAINOP permits independent access to the AESOP optimization routines. Optimization functions are defined by a variety of control programs embodying combat guidance laws and local inequality information. CTLOPT is used by either vehicle.
96. **NUTLU - M - Dimensional Table Look-up Routine**

**Purpose**

To provide a method of linearly interpolating in a table of n independent variables.

**Method**

Given the arguments \( X(1), X(2), X(3), \ldots, X(N-1) \), the routine computes \( Y = f(X(1)), X(2), X(3), \ldots, X(N-1) \) by linear interpolation from a table. Extrapolation beyond the upper and lower limits is optional.

**Usage**

Entry is made via the statement:

```
CALL NUTLU (ND,NA,X,Z,XAZR,12E,NEXTR)
```

where

- **ND** = Dimension of look-up when \( Y=f(X) \). \( ND = 2 \)
- **NA** = An array of length ND-1. Numbers of values of each table of \( X \). The tables are listed by size, the largest being first.
- **X** = Tables of each \( X \) in order.
- **Z** = Function values. If \( A = f(X,Y,Z) \) the dependent variable array must be in the following order
- **Assume** \( X = 4, Y = 3, Z = 2 \)

\[
\begin{align*}
Z(1) &= f(X1,Y1,Z1) \quad Z(13) = f(X1,Y1,Z2) \\
Z(2) &= f(X2,Y1,Z1) \quad Z(14) = f(X2,Y1,Z2) \\
Z(3) &= f(X3,Y1,Z1) \quad Z(15) = f(X3,Y1,Z2) \\
Z(4) &= f(X4,Y1,Z1) \quad Z(16) = f(X4,Y1,Z2) \\
Z(5) &= f(X1,Y2,Z1) \quad Z(17) = f(X1,Y2,Z2) \\
Z(6) &= f(X2,Y2,Z1) \quad Z(18) = f(X2,Y2,Z2) \\
Z(7) &= f(X3,Y2,Z1) \quad Z(19) = f(X3,Y2,Z2) \\
Z(8) &= f(X4,Y2,Z1) \quad Z(20) = f(X4,Y2,Z2) \\
Z(9) &= f(X1,Y3,Z1) \quad Z(21) = f(X1,Y3,Z2) \\
Z(10) &= f(X2,Y3,Z1) \quad Z(22) = f(X2,Y3,Z2) \\
Z(11) &= f(X3,Y3,Z1) \quad Z(23) = f(X3,Y3,Z2) \\
Z(12) &= f(X4,Y3,Z1) \quad Z(24) = f(X4,Y3,Z2)
\end{align*}
\]

**ZR** = Results

- **NEXTR** = 1 Extrapolate
- **NEXTR** = 0 No extrapolation

**IE** = Error code

- 0 no error
- -1 X array too small
- 1 X array too large
- 2 array not in ascending order

3/0
Let $n$ be number of independent variables, then the table is called an "$(n+1)$ dimensional table."

$$Z = f(x_1, \ldots, x_n)$$

Program

To use a table of dimension $\geq 3$ and $\leq 5$ a call to HIHO should be made with the list of arguments in the calling sequence in the same order as the independent variables are numbered.
CHEMP and CHEMP2 - Chemical State Computation

Purpose:
To provide the thermodynamic and transport properties of air downstream of the shock.

Method:
Linkage to this subprogram is achieved by a statement of the general form:

CALL CHEMP (P,H,T,RHO,AMU,SS,K)

K = 0: The pressure and temperature are assumed to be defined. The enthalpy, density and coefficient of viscosity are computed.

K = 1: The pressure and enthalpy are assumed to be defined. The temperature, density and coefficient of viscosity are computed.

K = -1: The same as the case where K = 1 except that the speed of sound is also computed.

Remarks:
INDGAS = 1: Real gas effects considered.
INDGAS = -1,0: Perfect gas assumed.
CHEMP (1)

ENTER

INDGAS

\( T = H/6008. \)

\( \rho = 1.232819 \times P/T \)

\( \mu = 2.27 \times 10^{-8} \times (T)^{1.5} \)

\( T + 198.6 \)

RETURN
93. CONV - Non-Linear Equation Solver

Purpose

To find a zero of the equation \( g(x) = 0 \) where \( g'(x) \) exists in the vicinity of the zero.

Method

The method of false position is used with the Aitken \( \delta^2 \) process to improve the rate of convergence.

Let \( F(r,s) = \frac{rs - sg(r)}{g(s) - g(r)} \) (False position)

\[ D(r,s,t) = t - \frac{(t-s)^2}{t-2s+r} \] (\( \delta^2 \) process)

Given an estimate \( x_1 \), of the zero, the following steps are executed:

1. \( x_2 = (1.0001)x_1 \) or \( x_2 = x_1 + .0001 \), whichever is larger
2. \( x_3 = F(x_1, x_2) \)
3. Let \( x_4 \) be the \( x_1 \) or \( x_2 \) which produces a \( g \) whose sign is opposite that of \( g(x_3) \). If there is no such \( x_4 \), let \( x_4 \) be the \( x_1 \) or \( x_2 \) producing the smallest value of \( g \). Let \( x_5 = F(x_3, x_4) \)
4. Let \( z = x_1 \) or \( x_2 \) which was not set equal to \( x_4 \). \( x_6 = x_5 - \frac{(x_5 - x_3)^2}{x_5 - 2x_3 + t} = D(x_1, x_3, x_5) \)
5. Let \( x_7 = x_5 \) and \( x_1 \) be the \( x_1 \), \( x_2 \), or \( x_5 \) producing a \( g \) whose sign is opposite that of \( g(x_6) \). If no such \( x \) exists, let \( x_1 = x_5 \). Return to Step 2.

This procedure is repeated until \( |g(x)| < \epsilon \), \( \epsilon \) a given tolerance.

Usage

Given an \( x_n \) and \( g(x_n) \), the routine computes a new value \( x_{n+1} \).

Entry

CALL CONV (EPS, MAX, GXN, XN, IND, K)

An initial call is made with \( K = 0 \). This is done only once in the program, prior to the second entries first call, and initializes EPS, MAX, and indicators in the routine. EPS is the convergence tolerance, \( \epsilon \). MAX is the maximum number of iterations allowed before an error return is made.

After every calculation of \( g(x_n) \), a call is made with \( K = 1 \), and the current values of \( g(x_n) \) and \( x_n \). Return is made with a new estimate \( x_{n+1} \), and a return indicator IND, where
1. Calculate $g(x)$ again
2. Successful convergence (i.e., $|g(x)| < \varepsilon$)
3. Error return, division by zero was imminent, returns with old value of $x_n$.
4. Allowed maximum number of iterations exceeded.

$G_{XN} =$ value of $g(x_n)$

$X_N =$ current estimate of $x$. This is the value $x_n$ corresponding to $g(x_n)$ when the call is made, and is either a new estimate $x_{n+1}$ on return from CONV with IND = 1, or is the old value $x_n$ on return with IND = 2,3,4.

The user first gives the call statement with $K = 0$ for initialization. Then he establishes an initial guess, $x_n$, evaluates $g(x_n)$, and gives the second call, with $K = 1$. If convergence is not obtained, the routine returns with IND = 2 and a new x-guess in $X_N$. The user must now re-evaluate $G_{XN}$ using the new x-guess. The process continues until IND = 2, 3, or 4. For IND = 4, no convergence in MAX tries. For IND = 3 a division by zero has occurred. For IND = 2, the correct x-value is in $X_N$. The following flow diagram is intended to clarify the use of CONVRS.
Purpose:

The multiengine thrust and fuel flow program provides the means of introducing the data for the various engines. It corrects the thrust for atmospheric effects when appropriate and resolves the thrust vectors into their components.

Usage:

Linkage to TFFM is accomplished via the general statement:

```
CALL TFFM (IENTRY)
```

where IENTRY is a fixed point variable.

\[ IENTRY = 1 \]

This is the pre-data initialization. At this entry the subscripts for all tables are computed and the following data is initialized:

- \( \text{INDTFF} = 0 \) = thrust option indicator
- \( N_1 = 1 \) = throttle setting
- \( \text{CNVM}_1 = 1 \) = mass rate units conversion factor
- \( \text{CNVT}_1 = 1 \) = thrust units conversion factor
- \( \text{ENDENG}_1 = 0 \) = engine option indicator
- \( \epsilon_{T1} = 1 \) = propellant mass flow rate factor
- \( \epsilon_{T2} = 1 \) = specific impulse factor
- \( \epsilon_{T3} = 1 \) = action time factor
- \( \epsilon_{T4} = 1 \) = propellant loading factor
- \( \epsilon_{T5} = 1 \) = perturbation factor
- \( \epsilon_{T6} = 1 \) = perturbation factor
- \( \phi_1 = 0 \) = nozzle rotation about x-axis
- \( \lambda_1 = 0 \) = nozzle swivel angle from x-axis
- \( P_{R1} = 0 \) = thrust reference pressure

where \( i \) as used above is the set of integers 1, 2, 3 corresponding to the three engines.
IENTRY = 2

This is the post-data initialization. At this entry no computations are performed if \( \text{INDTFF} = 0 \). If \( \text{INDTFF} \neq 0 \) the number of engines is determined from the indicator \( \text{INDENG} \). If no \( \text{INDENG} \) has been loaded, an error exit occurs.

IENTRY = 3

At this entry the various computations are performed. If \( \text{INDTFF} = 0 \), no computations are performed. When \( \text{INDTFF} \) is 10 or 11 and \( \text{INDENG} \) is defined, for a given engine, the following computations are performed for that engine:

\( \text{INDTFF} = 10 \) when \( \text{INDENG} = 11 \) gives: the Multiengine, Noncontrolled, Perturbed Thrust Option. For this option the tabulated data functional relationships are:

\[
T_R = f(T)
\]

\[
A_p = f(T)
\]

and the computations performed for the engine are as follows:

\[
\tau = \frac{T^2}{T_2} = \text{reference time as a function of stage time}
\]

\[
\dot{m}_{\text{ENG}} = \frac{T_5(T)}{G_{\text{ISP}_{\text{ENG}}}} \cdot \frac{T_4}{T_2} = \text{fuel flow rate} + \text{internal inert product flow rate}
\]

\[
T = \frac{T_1 T_4}{T_3} = \text{total corrected thrust}
\]

\[
\dot{m}_t = \dot{m}_{\text{ENG}} + \dot{A}_p = \text{total mass flow rate}
\]

\( \text{INDTFF} = 10 \) when \( \text{INDENG} = 12 \) gives the Multiengine, Controlled, Perturbed Thrust Option. For this option the tabulated data functional relationships are:

\[
\dot{m}_f = f(N)
\]

\[
A_p = f(T^2)
\]

and the computations performed for the engine are as follows:

\[
\dot{m}_f = \dot{m}_f = \text{perturbed mass flow rate}
\]

\[
\dot{T}' = G_{\text{ISP}_{\text{ENG}}} \cdot \dot{m}_f = \text{perturbed thrust}
\]

\[
T = \frac{T_1 T_4}{T_3} - (P - P_R)A_e = \text{total corrected thrust}
\]

\[
\dot{m}_t = \dot{\dot{m}} = \text{total mass flow rate}
\]

330
II. Thermal

INDTFF = 10 when INDENG = 13 gives the Multiengine, Air Breather, Perturbed Thrust Option. For this option the tabulated data functional relationships are:

\[ T_R = f(N, h, \alpha, M_N) \]
\[ m_T = f(N, \kappa, \alpha, M_N) \]

and the computations performed for the engine are as follows:

\[ m_T' = m_T \epsilon_{T6} \]
\[ T = T_R \epsilon_{T6} \]
\[ m_T = m_T' \epsilon_{T6} \]

INDTFF = 11 when INDENG = 11 gives the Multiengine, Noncontrolled, Perturbed Thrust Having Alternate Table Format. For this option the tabulated data functional relationships are:

\[ m_T = f(\tau^3) \]
\[ \dot{A}_p = f(\tau^3) \]

The computations are identical to the computations in the Multiengine, Controlled, Perturbed Thrust Option, i.e. INDTFF = 10 when INDENG = 12.

NOTES:

While it is possible to change from the single engine option (TFFS) in a given stage to the multiengine option (TFFM) in a later stage, the opposite is not possible.

A flow chart for TFFM is presented. TFFM2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.

The computations are as follows:

\[ m_T' = m_T \epsilon_{T6} \]
\[ T = T_R \epsilon_{T6} \]
\[ m_T = m_T' \epsilon_{T6} \]
Purpose:
To compute the atmosphere characteristics: density, speed of sound, pressure, temperature and kinematic viscosity. All are a function of altitude.

Method:
All atmosphere characteristics are computed using the 1959 ARDC model atmosphere. Values of the atmosphere are computed for positive altitudes. If this altitude is negative, the sea level values will be obtained.

Usage:
Linkage is affected by

CALL ATMS59 (HGC7F)

where

HGC7F = altitude in feet.

Remarks:
ATM59 and ATM592 are identical except for the use of differing vehicle COMELL blocks.
101. **ATMS62 and ATMS622 - 1962 Atmosphere Calculation Routine**

**Purpose:**

To compute the atmosphere characteristics: density, speed of sound, pressure, temperature and kinematic viscosity. All are a function of altitude.

**Method:**

All atmosphere characteristics are computed using the 1962 ARDC model atmosphere. Values of the atmosphere are computed for positive altitudes. If this altitude is negative, the sea level values will be obtained.

**Usage:**

Linkage is affected by

```call ATMS62 (HGC7F)`

where,

```HGC7F = altitude in feet.`

**Remark:**

ATMS622 is identical to ATMS62 except for the use of vehicle 2 COMMON blocks.
102 PUT - Character Manipulation Routine

Purpose:
To replace the Ith character of a string of characters with the first character of another string of characters.

Usage:
Entry is made to this routine by the following statement:

CALL PUT(P, I, L)

where the Ith character of string P will be replaced by the first character of string L.
103. GET - Character Manipulation Routine

Purpose:
To replace the first character of a word with the \textit{1st} character of a string of characters.

Usage:
Entry is made to the routine by the following statement:

\begin{verbatim}
CALL GET(P, I, L)
\end{verbatim}

where the first character of the word \textit{L} will be replaced by the \textit{1st} character of string \textit{P}. The remaining nine characters of word \textit{L} are replaced by blanks.
104. OPTBA and OPTBA2 - Bank-Angle Iteration Routine

Purpose:

To define instantaneous bank-angle on the basis of local optimization criteria.

Method:

A local minimization criteria, \( \phi(t) \), is created where

\[
\phi(t) = \phi(B_A)
\]

An inner loop parameter optimization procedure, CTLOPT, is used to define the bank-angle value which satisfies the resulting local \( t = \text{constant} \) optimization problem. The local minimization criteria is selected from one of several combat guidance laws. Final steering errors and force vector pointing errors are also computed.

Remarks:

A flow chart for OPTBA is presented. OPTBA2 is identical except for the use of vehicle 2 COMMON blocks and auxiliary subroutines.
105. **IMAINOP - Internal Parameter Optimization Interface Routine**

**Purpose:**

To act as an interface between the two vehicle trajectory equations and the parameter optimization routines.

**Method:**

Core size requirements limit the internal optimization capability to

a. Sectioning search
b. Creeping search
c. Pattern search

**IMAINOP** interfaces the trajectory equations to these three search options.
106. ISELECT - Interval Search Selection Routine

Purpose:

To select either sectioning or creeping search in the internal parameter optimization loop.
MULT33 - A Matrix Multiplication Routine

Purpose:
To post multiply a 3 x 3 matrix by a 3 x 3 matrix.

Method:
The result of $A \cdot B = C$ is computed using single precision.

Usage:
The matrix multiplication is obtained by the statement:

```fortran
CALL MULT33 (A, B, C)
```

where
A = array name of the 3 x 3 matrix A
B = array name of the 3 x 3 matrix B
C = array name where results are to be stored as the 3 x 3 matrix

Remarks:
This routine calls no other routines.
Program CTLS controls the variational optimization option. The tasks performed by the CTLS program include the following:

1. Print the CTLS summary, which includes the values of the optimization functions. (E)

2. Evaluate the forward trajectory by considering the improvement or deterioration of the optimization functions. (E)

3. Decide whether to accept a forward trajectory as a valid step, or to reject it. (E)

4. To determine the $\alpha$-perturbation to use on the next forward trajectory.

5. To put together the $\alpha$-perturbation that is desired by using the information from REV on tape ILTAP, constructing the CTABLE and putting it out on tape IATAP.

6. To output the restart cards for trajectories which are accepted as valid steps. (E)

7. Housekeeping - e.g. updating the pass number and cycle number, PHBRST, PSBRST, etc.

The CTLS segment is entered either from EXE or REV. The "E" designates those tasks which pertain only to entry to CTLS from EXE.

CTLS proper allows the user to select which control system will be used in the optimization program.

Usage

CALL CHAIN (CTLS)

Remarks

LNDSEL is of the form i0j. i determines which control system will be used with the optimization program. For $i = 1$, CTLS1 is used. For $i = 3$, CTLS2 is used, $i$ also determines which decision subprogram will be called. Currently $i = 1$ and $i = 3$ are the only usable options. $j$ determines which equations subprogram will be used.

CTLS calls CTLS1 and CTLS2.
Organizational Chart for CTLS

CTLS

CTLS1

KCALC

CTLIST

DECIDE

DECIDE

DECIDE

WHORM

UPDK

DALCAL

SUMOLA

PLT

PACK

CARDS

DISPLAY

OFFSW

SEARCH

TLU

INVERT

MATINV

*DESIGNATES MULTIPLE ENTRY POINTS
1. **CTLS1 - Original Control System**

The control system is a predictor-corrector method of control over the convergence of the end constraints and payoff function. A linear prediction of the changes in end constraints and payoff function, due to a change in the control variable(s), is made and attempted. If the trial is near enough to the linear prediction, the control variable is changed to give the best change in end constraints and payoff function, and the final values of the functions (for the cycle) are computed. If the trial is not near enough, the change in the control variable(s) is reduced and another prediction and attempt are made. If the end points and payoff function are too near the linear prediction, the amount of change is increased. Under normal circumstances, the control will never take more than six passes but if for some reason the INDERR is set positive more passes can be taken. If six or more passes are made by the control system then MINDIC is set to 0 and W and Y and YTO are reset. On return from the reverse integration if $Dp^2 - d\beta_i^{-1} d\beta_i$ is negative then $Dp^2 = 1.1 Dp^2_{n-1}$ and only the $C_i$ corresponding to the constraints which are diverging are decreased.

There are two entries and two exits in this program. One entry is from the program which computes the functions and matrices of partial derivatives (DIFEQ); his entry is to the portion of the control system which compares the linear predictions to the actual values of the end point and payoff function changes. An exit is made, after each cycle is completed, to a program which computes the $[J]$ matrices and other values needed to compute the mode shape of the change in the control variable(s) (REV).

Another entry is made from that program (REV) to the portion which checks for the conditions needed to terminate and computes the control variable change for the first trial of a new cycle. The second exit is to the program which computes the functions and matrices of partial derivatives (DIFEQ).
2. **CTLS2 - Arbitrary Control System**

**Purpose**

To serve as an "arbitrary" control system, namely, to perform the routine chores that must be done in the CTLS segment, but to defer the important decisions to subprogram DECIDE.

**Method**

The flow chart provides the best description of those tasks performed in CTLS2. CTLS2 may be entered at two different parts of the program: when segment CTLS is brought in after segment ME or when segment CTLS is brought in after segment REV. At every point where a critical decision must be made, a call is made to DECIDE with a particular entry point.

There are four primary decisions that must be made by DECIDE:

a. The $6\sigma$ mode shape to use.

b. Whether to accept a pass as a valid step.

c. If the decision concerning (b) is negative, the step size to use for the next pass.

d. Whether to compute partials on the next pass.
### Entry Point for DECIDE

<table>
<thead>
<tr>
<th></th>
<th>Situation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>20 passes have been made; decide whether to terminate.</td>
</tr>
<tr>
<td>2</td>
<td>Initialize parameters on the nominal trajectory.</td>
</tr>
<tr>
<td>3</td>
<td>A pass for which partials were computed has missed cutoff.</td>
</tr>
<tr>
<td>4</td>
<td>A pass for which partials were computed must be accepted or rejected.</td>
</tr>
<tr>
<td>5</td>
<td>To output additional restart cards.</td>
</tr>
<tr>
<td>6</td>
<td>A pass for which partials were not computed has missed cutoff.</td>
</tr>
<tr>
<td>7</td>
<td>A pass for which partials were not computed must be evaluated.</td>
</tr>
<tr>
<td>8</td>
<td>Initialize parameters for each cycle (after REV); set dβ.</td>
</tr>
<tr>
<td>9</td>
<td>The mode shape must be approved (if not, determine a new dβ).</td>
</tr>
<tr>
<td>10</td>
<td>After a pass, to set the number of literal constraints, INDCON; this will be the same as INDPMT if it is not set by DECIDE.</td>
</tr>
<tr>
<td>11</td>
<td>To print any information after the perturbation has been made (i.e. after DALCAL).</td>
</tr>
<tr>
<td>12</td>
<td>(\text{DENOM} = I - I^{-1} I &lt; 0) (This situation is theoretically impossible.)</td>
</tr>
<tr>
<td>13</td>
<td>To set INDCON (see 10) after the reverse integration. Also, to invert (I_{\text{yy}}).</td>
</tr>
</tbody>
</table>
ZLS2 takes care of the following important chores itself:

1. Updating indicators, e.g. INDFST, NCYCLE, NPASS, etc.
2. Outputting the CTLS Summary print.
3. Outputting restart cards for CTABLE and DELP2.
4. Updating PSSTAR, PHSTAR, PSBRST, and PHBRST tables. These tables contain the values printed under "CTLS Summary".
5. Calling the next segment (either GRAPH or REV).
6. Computing \[ \text{DENOM} = I - I \frac{1}{T_1T_2} \] and \[ SSIPH = I \frac{1}{v_T} \]
7. Recalculating parameters (e.g. \( d\theta \)) to be compatible with the change \( \Delta P^2 \) determined by the value of COEFK which is set in DECIDE.\[ SSIDS = d\theta I \frac{1}{v_T} \]
8. Computing \( \text{TADIC} = \sqrt{\frac{\Delta P^2 - d\theta I \frac{1}{v_T}}{I \frac{1}{v_T} - I \frac{1}{v_T} I \frac{1}{v_T}}} \)
9. Calling DALCAL to either compute a new mode shape for \( \phi \) or to change the amplitude of the existing mode shape.
10. Terminating the case when it is impossible to continue.
11. Making sure that \( \Delta P^2 - d\theta I \frac{1}{v_T} \) is not negative. DECIDE will be called repetitively with entry point 9 until this condition is satisfied.

Communication between CTLS2 and DECIDE is accomplished through the calling sequence, primarily. There are three indicators used here which need clarification:

**INDAMP**: Decide sets INDAMP \( \neq 0 \) if the desire is to change the amplitude of the current perturbation (by multiplying the perturbation by COEFK). INDAMP is set to 0 by DECIDE if a new mode shape is to be attempted.

**ITBAL**: ITBAL is updated by CTLS2; it is the number of calls made to DECIDE (9) in order to attempt to find a feasible mode shape.

**INDBAL**: INDBAL is set \( \neq 0 \) by DECIDE(9) to inform CTLS2 that it is satisfied with the mode shape.

**Remarks**

Changes in the step size made by DECIDE, must be done by setting COEFK; S2 will set DELP2 = COEFK^2 * DELP2.
CTLS2 (2)

FROM A TRIAL TRAJECTORY

401 SAVE
402 LOAD
403 READ (77)
404 READ (17)
405 PERFORM FUNCTION
406 DECIDE (4)
407 MPAWS
408 CUTIPS
409 INCONSISTENCY
410 GAMS
411 ARM
412 ATTS
413 SITTS
414 MEAS.
415 PIVIA
416 COL11
417 TIM
418 TOC
419 NLJ (INVERT)
420 INCONSISTENCY
421 NCA
422 NCA
423 RAC
424 GAMINC
425 RAC
426 FST

FROM REV

C

DECIDE (4)
430 MPAWS
431 CUTIPS
432 INCONSISTENCY
433 NCA
434 NCA
435 RAC
436 GAMINC
437 RAC
438 FST

INCONSISTENCY

C

GAMS

INCONSISTENCY

DECIDE (4)

CUTIPS

INCONSISTENCY

MPAWS

DECIDE (4)

CUTIPS

INCONSISTENCY

GAMS

MPAWS

DECIDE (4)

CUTIPS

INCONSISTENCY

GAMS

MPAWS

DECIDE (4)

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3. DISPLAY – Console Display Routine

Purpose:
To output data to the display console on the 10-inch display tube.

Method:
By setting sense switch 6 a peripheral processor is selected and the
CTLS summary is displayed on a 10-inch display tube.

Usage:
Entry is made to the routine by the following statement
CALL DISPLAY (IPAY,IIIPMT)

where
IPAY is payoff function
IIIPMT is the number of constraints.
4. SEARCH - Search Routine

Purpose:

Compute a nominal starting trajectory for the optimization program.

Method:

The search routine allows the user to vary a control parameter to satisfy any single end constraint in the hope this is a better nominal trajectory. Any parameter used in the initial condition optimization or any half point in the CTABLE may be used by the search routine as an adjusting variable. Any trajectory the search routine finds may or may not be a good trajectory for the optimization program. In fact, sometimes what appears to be a good starting trajectory by inspection turns out not to be a good nominal trajectory for the optimization program. Therefore, if one fails to get started with the first nominal, a second attempt should be made with another nominal.

Assume the same test case as before but now set a half point in the CTABLE as the adjusting parameter.

Example:

```
NPOINT  3
CTABLE  0., 100., 300., -1., 2., 0
```

If the above table is assumed to be α then it has the shape as follows:

![Graph showing the trajectory]

LIMDER  BCD  IQF
DESIRE  BCD  IHDCTF
CONVAR  2.
SECLIM  1.
KPOINT  5
LIMIT   2000.
QEXN    270000.

A half point alpha at time 100. seconds is the control variable. LIMDER, DESIRE, LIMIT, and QEXN are unchanged from the previous example. CONVAR is set equal to 2. SECLIM is set to 1. and on the second try the α history would appear as the dotted line. ADJUST is not needed when working with the CTABLE. KPOINT is set equal to 5 which is the 5th location in the CTABLE.
Assume that conditions exist such that one would like to have a trajectory that would terminate at 270,000 feet altitude ± 2000 feet tolerance by adjusting the initial Y.

Entry is made to the search routine with one data card.

**INDMOD**  1

Other data is expected if the above data card is included.

<table>
<thead>
<tr>
<th>LINDER</th>
<th>BCD</th>
<th>LQEXN</th>
</tr>
</thead>
<tbody>
<tr>
<td>DESIRE</td>
<td>BCD</td>
<td>HGC7F</td>
</tr>
<tr>
<td>ADJUST</td>
<td>BCD</td>
<td>GAM7D</td>
</tr>
<tr>
<td>CONVAR</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>SECLIM</td>
<td></td>
<td>2</td>
</tr>
<tr>
<td>KPOINT</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>LIMIT</td>
<td></td>
<td>2000.</td>
</tr>
<tr>
<td>QEXN</td>
<td></td>
<td>270000.</td>
</tr>
<tr>
<td>GAM7D</td>
<td></td>
<td>0</td>
</tr>
</tbody>
</table>

LINDER contains the BCD word of some unused cell in core. QEXN contains the required end value of altitude. DESIRE contains the BCD word of the end constraint. ADJUST contains the BCD word of the control parameter being varied. CONVAR should have the same initial value as the control variable. SECLIM is the value of the control variable on the second try. KPOINT is the location of the half point in CTABLE to be varied. In this case Y is the control variable and KPOINT must be set to zero. LIMIT is the tolerance on altitude. A + or - is assumed on the tolerance.

Any location in CTABLE may be varied the same by changing the necessary data.

**Remarks:**

All data for the search routine should be in DATA1.

The CTABLE must be put in DATA1 as a function of trajectory time (INDCTA = 0).
5. **CARDS - Restart Cards Routine**

**Purpose:**

To output information which may be used to restart the program.

**Usage:**

CALL CARDS (SYM,VAR,N,ITAPE)

- **SYM** = symbol to be output or signal to rewind card tape.
- **VAR** = location of values to be output.
- **N** = number of values to be output.
- **ITAPE** = tape on which printed output occurs or signal to place end of file on card tape.

Restart cards for each cycle are output on the output tape ITAPE. Restart cards for the last completed cycle are output on the card tape KTAPE. ITAPE=6 and KTAPE=15. All values are output in O'HAL.

**Remarks:**

CTLS1 and CTLS2 call CARDS. CARDS calls LINES.
6. DALCAL – Delta Alpha Calculation

**Purpose:**

This subprogram of CTLS computes \( \delta \gamma \) and \( \delta x_0 \) by combining the various linearly independent solutions to the adjoint equations computed in REV. It is necessary that this task be deferred until this time because the coefficients in the linear combination for computing \( \delta \gamma \) and \( \delta x_0 \) are determined by the control system and hence are not available during REV. Also, depending on the control system being used, it may be necessary to change the coefficients from one pass to the next. The values of the coefficients \( \left[ I_{\text{inv}} \right] d\beta = \text{SSIDC} \) determine the mode shape of the perturbation. This subprogram not only computes \( \delta \gamma \) (DEALPH) but it updates (CTABLE) with the perturbation. Perturbations, \( \delta x_0 \) (DELI), to initial conditions, \( x_0 \), (VALINS), are computed and the initial conditions are updated here in a manner analogous to the \( \delta \gamma \) computations.

**Method:**

There are two entry points to this subprogram. The first entry point is for computing the perturbation for the first pass of a cycle or for any pass where the mode shape is being changed. The second entry point is for changing the amplitude of the previous perturbation.

This subprogram will terminate the case, if, for any given stage, the history exceeds the limits of the dimension of CTABLE.

At entry point 1, \( \delta \alpha \) and \( \delta x_0 \) are computed according to:

\[
\delta \gamma = \left[ W^{-1} G_{\alpha,\alpha} W^{-1} G_{\beta,\beta} W^{-1} G_{\gamma,\gamma} \right] \sqrt{ \frac{dp^2}{d\beta} } I_{\text{inv}}^{-1} + W^{-1} G_{\gamma,\gamma} \left[ I_{\text{inv}}^{-1} \right] d\beta
\]

\[
\delta x_0 = \left[ U^{-1} R_{\beta,\beta} U^{-1} r_{\beta,\beta} U^{-1} \right] \sqrt{ \frac{dp^2}{d\beta} } I_{\text{inv}}^{-1} + U^{-1} r_{\beta,\beta} \left[ I_{\text{inv}}^{-1} \right] d\beta
\]

In the above expressions, the radical (RADIc) is available since it has been computed in CTLS. Also \( I_{\text{inv}}^{-1} d\beta = \text{SSIDC} \), and \( I_{\text{inv}}^{-1} \) have been computed in CTLS.

\( \delta \gamma \) calculations will be made for each major stage. \( \delta x_0 \) calculations are made only for the first stage.
The outline of the subprogram follows:

**Entry Point 1**

1. Get $\lambda_{\phi_1}$GW$^{-1}$ and $\lambda_{\psi_1}$GW$^{-1}$, $\alpha$, and $W^{-1}$ for the $i$th major stage from tape ILTAP (last stage comes first).

2. Compute $\delta\alpha$ from $\lambda_{\phi_1}$GW$^{-1}$, $\lambda_{\psi_1}$GW$^{-1}$, RADIC, SSIDS, and SSIPH.

3. Compute the new $\alpha$: $\alpha = \alpha + \delta\alpha$.

4. Plot $\alpha$, $\delta\alpha$ and $W^{-1}$ if requested.

5. If more stages go to (10); otherwise go to (6).

6. Get $\lambda_{\phi_1}$RU$^{-1}$, $\lambda_{\psi_1}$RU$^{-1}$, and $x_0$ from tape ILTAP.

7. Compute $\delta x_0$ from $\lambda_{\phi_1}$RU$^{-1}$, $\lambda_{\psi_1}$RU$^{-1}$, RADIC, SSIDS, and SSIPH.

8. Compute the new $x_0$: $x_0 = x_0 + \delta x_0$.

9. Print the $x_0$, $\delta x_0$, $U^{-1}$ if requested.

10. Put $\alpha$, $W^{-1}$, $\delta\alpha$, $x_0$, $U^{-1}$, $\delta x_0$ on tape IATAP (all in one record).

11. If there are more major stages to go (1); otherwise return.

**Entry Point 2**

1. Get $\alpha$, $W^{-1}$, $\delta\alpha$, $x_0$, $U^{-1}$, $\delta x_0$ from tape IATAP.

2. Recover to the last good $\alpha$: $\alpha = \alpha - \delta\alpha$.

3. Modify $\delta\alpha$: $\delta\alpha = k \cdot \delta\alpha$.

4. Compute the new $\alpha$: $\alpha = \alpha + \delta\alpha$.

5. If more major stages, go to (9); otherwise go to (6).

6. Recover to the last good $x_0$: $x_0 = x_0 - \delta x_0$.

7. Modify $\delta x_0$: $\delta x_0 = k \cdot \delta x_0$.

8. Compute the new $x_0$: $x_0 = x_0 + \delta x_0$.

9. Put $\alpha$, $W^{-1}$, $\delta\alpha$, $x_0$, $U^{-1}$, $\delta x_0$ on tape IATAP (all in one record).

10. If more stages go to (1); otherwise go to (11).

11. Switch IATAP and ILTAP and return.
Once entry point 2 has been called, entry point 1 may not be called again until the next cycle because the information it needs on ILTAP is gone.

The information from REV on ILTAP is blocked. Reading this tape (entry point 1) is accomplished by calls to the ad-hoc unblocking routine UNBLOCK.
7. KCAIC - Step Size Logic Routine for Control System

Purpose

This subroutine determines the "best" step size coefficient based on the given data, and is intended to be a part of the over-all logic necessary for step size evaluation and control.

Usage

CALL KCAIC (ARG1, ARG2,...,ARG14, ARG15)

where

ARG1 = ARG6 = Arg11 = Arg16 = Variable name where K is to be stored.

ARG2 = ARG7 = ARG8 = ARG9 = ARG10 = ARG12 = ARG13 = ARG14 = ARG15 = Variable name where K is to be stored.

This routine is designed for use with the "CTLS1" control system. An initial set of step size coefficients (K1*, K2*, ..., Kn*) is generated from the given data. This initial set of coefficients is used to control the calculation of a "new" set of step size coefficients. (K1', K2', ..., Kn').

The "best" value (K) is then calculated from the new set of coefficients and an exit is made from the subroutine.

The initial set of step size coefficients is generated in the following manner:

GIVEN  φ*, φ*, Δφ, φNL*, vNL1*, vNL1, Δv1

THEN  Δφ = (φ* - φ*); Δv1 = (vNL1* - vNL1);

φNL = (Δφ* - Δφ); vNL1 = Δv1

Kφ* = Δφ NL / vNL1

Kv* = Δv1 NL / vNL1

where i = 1, 2, ..., n.
The values \((K_1^*, K_2^*, K_3^*, ..., K_n^*)\) are re-arranged into descending order \((K_1, K_2, ..., K_{n+1})\). The value \(K_1\) must be such that \(0.5 \leq K_1\).

If this condition is not met, then the "best" value \(K\) is defined to be \(0.5\) and an exit is made from the subroutine.

If this condition is met, then a logic scheme is applied to calculate a new set of coefficients.

The new set of step size coefficients \((K'_1, K'_2, ..., K'_n)\) is calculated as follows:

a) Tolerance check (only for \(Y_i\) constraints)

GIVEN \(Y_i = Y_i^*\);

THEN \(Y_i' = \frac{Y_i - Y_i^*}{Y_i}\),

where \(i = 1, 2, ..., n\).

GIVEN \(Y_i', Y_{ER_i}\);

THEN if \(\left| Y_i' \right| \leq Y_{ER_i}\) Test \(K_i\);

if \(K_i = K_i^*\), then proceed to next \(i\); (*), otherwise perform (b), (c), and (d); where \(i = 1, 2, ..., n\).

b) End point movement (only for \(Y_i\) constraints)

GIVEN \(\bar{Y}_i, \bar{Y}_i^*, \Delta Y_i^*, Y_{BWD_i}, Y_{FWD_i}, C_{Y_i}\);

THEN \(\Delta = (\bar{Y}_i^* - \bar{Y}_i) \Delta Y_i^*\);

if \(\Delta \leq 0\),

\(Y_{MOT_1} = \frac{\Delta Y_i^* \left| (\bar{Y}_i - \bar{Y}_i^*) Y_{BWD_i}, C_{Y_i} \right|}{\Delta Y_i^*}\)

otherwise,

\(Y_{MOT_1} = \frac{\Delta Y_i \left| (\bar{Y}_i - \bar{Y}_i^*) Y_{FWD_i}, C_{Y_i} \right|}{\Delta Y_i^*}\)

where \(i = 1, 2, ..., n\).

c) Calc roots \(K''_1, K''_2\) (only for \(Y_i\) constraints)

GIVEN \(\Delta Y_i', \Delta Y_i^*, Y_{MOT_1}\)

375
THEN  \( (K_i', K_i'') = -B \pm \sqrt{B^2 - 4AC} \) 
\((**)\)

where \( A = (\Delta Y_i - \Delta Y'_i) \),
\( B = \Delta Y_i \),
\( C = -\Delta Y_{\text{hot}} \), and \( i = 1, 2, \ldots, n \).

d) Test \( K_i', K_i'' \) (only for \( Y_i \) constraints)

For all \( i, (i = 1, 2, \ldots, n) \), the value of \( K_i' \) must be chosen such that \( K_i' \) is least positive value and such that \( K_i' \leq K_{i-1}' \), where \( K_0' = K_1' \).

If \( (K_i'' - K_i'') < 0 \), then no new \( K_i' \) value is computed.

The "best" value \( (K) \) then is defined as \( 0.5 \leq K_i' \leq 2.0 \); and an exit is made from the subroutine.

(*)

It should be noted that recycling occurs if the \( Y_i \) constraint error is within the prescribed tolerance \( (Y_{ER}) \) and the controlling step size coefficient \( (K_1) \) is \( K_{\text{opt}} \). At the end of (d) the controlling step size coefficient is changed to \( (K_2', K_3', \ldots, K_{n+1}') \) and the cycle restarted at (a). If recycling is necessary the present "best" value \( (K_i' = K_i) \) is saved and the recalculated "best" value \( (K_i' = K_{i+1}) \) must be such that \( K_{i+1}' \geq K_i' \)

where \( i = 1, 2, \ldots, n \).

If all constraint errors are within the prescribed tolerances, then \( K_{\text{opt}} \) is chosen to be the "best" value \( (K) \) and an exit is made from the subroutine.

(***)
If \( B^2 - 4AC < 0 \), then no \( K_i' \) and \( K_i'' \) is computed.

Remarks

KCALC is called by CTLS1.
KCALC calls DEF and LINES.
8. INVERT - \( I_{\psi\psi} \) Inversion

**Purpose:**
To invert the \( I_{\psi\psi} \) matrix.

**Usage:**
CALL INVERT

From theoretical considerations, \( I_{\psi\psi} \) should be symmetric. If a column (row) of \( I_{\psi\psi} \) is zero and the corresponding row (column) is non-zero, the program is terminated. If a column and corresponding row are both zero, they are eliminated from the matrix. The resulting matrix is inverted and any zero rows or columns are inserted into the inverse. \( I_{\psi\psi} \) is post-multiplied by \( I_{\psi\psi}^{-1} \) as a check.

**Remarks:**
CTLS1 and UPDK call INVERT.
INVERT calls MATINV and STOP.
INVERT (1)
INVERT (2)

A

N = 0

(DO 1220, N, INDPMT)

NRC(I) ≤ 0?

YES

NO

N = N + 1

M = J

(DO 1223, J = ., INDPMT)

NRC(J) ≤ 0?

YES

NO

I = M + 1

PSISII(N, M) = SISII(I, J)

(continue)

(continue)

CALL MATINV

B
INVERT (3)

\[ \text{IF } K = 0, \text{THEN } \text{GOTO 1220} \]

\[ \text{DO } 1220 \quad J = 1, \text{INDPMT} \]

\[ N = N + 1 \]

\[ M = 0 \]

\[ \text{DO } 1220 \quad J = 1, \text{INDPMT} \]

\[ SISM1(I,J) = 0 \]

\[ \text{DO } 1220 \quad J = 1, \text{INDPMT} \]

\[ SISM1(I,J) = SISM1(M,M) \]

\[ \text{CONTINUE} \]

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INVERT (4)

WRITE & 1000

(Do 1001 I = 1, INDPMT)

WRITE & 1002

(Continue)

WRITE & 1003

(Do 1004 I = 1, INDPMT)

WRITE & 1002

(Continue)

WRITE & 1005

RETURN
9. **DECIDE - Driver for Decision Routines**

**Purpose**

To allow the user to select the decision subprogram which will be used with CTLS2 in the optimization program.

**Usage**

CALL DECIDE (IENTRY)

IENTRY = indicator which determines what decision must be made by the decision subprogram.

INDSEL is of the form i0j. The decision subprogram is determined by i. If i = 3, DECID3 is used. If i = 2, DECID2 is called. DECID2 is currently a dummy routine. INDSEL is normally 101. j determines which set of differential equations will be used.
10. OFFSW - Display Drop Routine

**Purpose:**
To drop the on-line display from the console.

**Usage:**
Type "DROP" at console.

**Remark:**
This is a special-purpose ASCENT routine. No flow chart is included.
11. **TLUU - Two Dimensional Table Look-Up Routine**

**Purpose**

Given an argument $X$, to compute $Y = f(X)$ from a table of $X$ and $Y$ values by linear interpolation.

**Method**

Same as for TLU.

**Usage**

Same as for TLU.

**Remarks**

This subroutine is the same as TLU except the table is not given as a common subscript.
12. **UNBLOCK - Unblocking Routine for \( A \)'s**

**Purpose:**
To read and decode the blocked tape (ILTAP) that has been prepared in CHAIN REV.

**Method:**
The values for the \( \Delta \) change in the mode shape of \( A \)'s have been stored in a large array to decrease the number of times an I/O device is selected.

**Usage:**
Entry is made to the routine by the statement:

```fortran
CALL UNBLOCK (PHOLGW, TIMES, NDUMMY, INDPMT, MCONT, PSOLGW, ALPHC, W2, ILTAP)
```

where:

- \( \text{PHOLGW} \) = Mode shape change values
- \( \text{TIMES} \) = Time from beginning stage
- \( \text{NDUMMY} \) = Control word
- \( \text{MCONT} \) = Number of control variables
- \( \text{INDPMT} \) = Number of end and point constraints
- \( \text{PSOLGW} \) = Mode shape change values
- \( \text{ALPHC} \) = \( A \)'s from previous valid step.
- \( \text{W2} \) = Weighting Matrix elements
- \( \text{ILTAP} \) = I/O device

No initialization is necessary outside this routine and no output occurs from this routine. Only the normal I/O FORTRAN routines are called.
13. **SUMOLA - Linear Combination Routine for A's**

**Purpose:**
To compute linear combinations of sensitivities.

**Usage:**

CALL SUMOLA (PHISEN, PSISEN, C, NPSI, NVAR)

PHISEN = the linear combination to be computed.

PSISEN = the component sensitivities which are to be combined.

C = weights to be applied to component sensitivities.

NPSI = number of components

NVAR = length of each component array.

\[ \text{PHISEN}_i = \sum_{j=1}^{NPSI} \text{PSISEN}_{j,i} \cdot C_j, \quad i = 1, \text{NVAR} \]

**Remarks:**
This routine is used with the "CTLS2" control system.
SUMOLA

BEGIN

(Do 10 I = 1, NVAR)

PHISEN(I) = 0

(Do 10 J = 1, NPSI)

PHISEN(I) = PHISEN(I) + PSISEM(J, I) - C(J)

10 CONTINUE

RETURN
14. **PLOT - Point Plot Subroutine**

A point plot subroutine written by Mary Huff of McDonnell Automation Center in December 1965.

**Purpose:**

To plot a graph of one or more curves from given sets of rectangular coordinates using a minimum of storage.

**Method:**

To avoid overlapping characters, the printer limits the characters which can be printed on the plot to 109 per line and 51 per column. To plot a curve, it is therefore necessary for the routine to divide each page of the plot into 109 intervals in the X direction and 51 intervals in the Y direction. The width of the X intervals, called \( \Delta X \), is then \( PXMAX - PXMIN \) where \( PXMAX \) and \( PXMIN \) are the maximum and minimum X values which can be plotted on that page. If a search of the \( \xi \) coordinates of the curves to be plotted then shows an X value falling within the range of the \( n \)-th interval, that is \( PXMIN - \frac{\Delta X}{2} + (n-1)\Delta X \leq X < PXMIN + \frac{\Delta X}{2} \), then a point will be plotted in the column representing the \( n \)-th interval. The routine allows for a multipage option in which the Y axis remains constant but the X axis varies from \( XMIN \) to \( XMAX \) over a range of several pages. The number of pages will equal \( \frac{XRANGE}{PRANGE} \) where \( XRANGE \) is the range of X values over all the curves or \( XMAX - XMIN \) and \( PRANGE \) is the range of X values which could be plotted on a single page or \( \Delta X \cdot 108 \). The maximum X value on one page will become the minimum X value on the succeeding page until \( XMAX \) is reached. \( \Delta X \), which is needed to determine \( PXMAX \) for each page, must be determined before the plot is attempted. It may be supplied to the routine by the user or left to the routine to calculate before plotting the curves. If \( \Delta X \) is left to the subroutine to calculate, a search of the curves to be plotted will find \( \Delta X \) to be the minimum distance between any two points on any curve in the X direction. If the multipage option was specified, then \( \Delta X \) is accepted as calculated by the routine or as specified by the user, and the number of pages will be \( \frac{XRANGE}{PRANGE} \). If the single page option was specified, and \( \Delta X = \frac{XMAX - XMIN}{108} \) then \( \Delta X \) is accepted as specified or calculated, otherwise \( \Delta X \) is set to \( XMAX - XMIN \) to allow the full range of X values to fit on exactly a single page. In order to plot a graph of less than one page, the multipage option must be specified, even if \( \Delta X \) is specified.

The log of \( y \) is plotted if the semilog option is used, and the log of \( X \) and \( Y \) if the log-log option is used. If the value for which the log is to be plotted is negative, the log of the positive value will be plotted, but an N will replace the specified character for that point on the curve.
log of zero will not be attempted, but the zero will be plotted with the character N.

Any number of curves may be plotted on the same graph. The X coordinates of each curve must be stored as one column of the two dimensional X array and Y coordinates of the curve as the corresponding column of the Y array. The points need not be ordered, but the X and Y coordinates of a point must be at corresponding positions in their respective columns. The curves may be distinguished from each other by designating different plotting symbols. Any Hollerith Character may be used; however, the subroutine uses a plus sign for the border, a minus and an I for axes, and an N for attempting the log of a negative or zero number. If a point is common to more than one curve, the symbol of the last curve plotted will be shown.

The subroutine will eject a page and print the title specified by the user at the top of each page of the plot. The border option will outline each page of the graph with + signs. The axis option will print the X and Y axes (plot the curves Y = 0 and X = 0). The X scale is printed at 2" intervals and the Y scale at 1" intervals.

Usage:
The routine is entered by the FORTRAN statement
CALL PLOT(X,Y,M,A,IC,B,MP 'L',DEL,TITLE,IM);

where

X is the name of a 2 dimensional array containing the X coordinates of all the curves to be plotted. The X coordinates of the n-th curve, for example, are stored from X(1,n) to X(m,n) where m is the number of points in the curve.

Y has the same dimensions as X and contains the Y coordinates of the curves.

M and A are the names of one dimensional arrays set up by the user. M(n) is the number of points in the n-th curve, whereas the first point is at X(1,n) and Y(1,n). A(N) is the character—left-adjusted in a 4 byte word—to be used in plotting the n-th curve.

IC is the number of curves to be plotted and must be less than or equal to the second dimension specified for the X and Y arrays in their DIMENSION statement.

B=1 no border, no axis
2 border, no axis
3 no border, X axis only
4 border, X axis only
5 no border, Y axis only
6 border, Y axis only
7 no border, both axes
8 border, both axes
MP = 0 single page plot desired
    1 multiple page or fraction of page plot desired

LL = 1 plot given points
    2 semilog (plot logs of Y coordinates)
    3 log-log (plot logs of X and Y coordinates)

XDEL = 0 indicates ΔX is calculated
      Otherwise specify ΔX in floating point

TITLE is the name of the array in which the title to head each page
      is stored. Only one line may be printed. The array must be
      at least 30 four byte words in length. Any words in excess of
      30 will not be printed.

IDM is the first dimension specified for the X and Y arrays in their
      DIMENSION statement. It must be at least equal to the number of
      points in the curve which has the greatest number of points of
      the curves to be plotted.
15. MATINV - Matrix Inversion Routine

**Purpose:**

FORTRAN subroutine solves the matrix equation $AX = B$, where $A$ is a square coefficient matrix and $B$ is a matrix of constant vectors. $A^{-1}$ is also obtained; indeed, inversion may be the sole aim in a particular usage. Finally, the determinant of $A$ is available.

**Method:**

Jordan's method is used to reduce a matrix $A$ to the identity matrix $I$ through a succession of elementary transformations: $E_nE_{n-1} \ldots E_1$, $A = I$. If these transformations are simultaneously applied to $I$ and to a matrix $B$ of constant vectors, the result is $A^{-1}$ and $X$ where $AX = B$.

**Usage:**

Entrance is made via the FORTRAN statement in the calling program:

```fortran
CALL MATINV (N, B, M, DETER)
```

where

1) $N$ is the order of $A$; $N \geq 1$.
2) $M$ is the number of column vectors in $B$.
3) `DETERM` is the location in which the determinant is to be placed.

Suitable variable names may replace the dummy variables listed above.

At the return to the calling program, $A^{-1}$ is stored at $A$ and $X$ at $B$.

$M = 0$ or negative signals that the routine is to be used solely for inversion; note, however, that in the CALL statement an entry corresponding to $B$ must still be present.
16. DECID3 - Step Size Routine for Control System

**Purpose**

To determine when to accept a pass as a valid step, when to compute partials, the step size to use on the next trial and to invert the \( I_T \) matrix and make other decisions to determine the \( \delta \alpha \) mode shape.

**Usage**

```call DECID3 (IENTRY, D2, D3, D4, D5, D6, D7, D8, D9, DPHI, D3, DK, DE, DF, DG, INDAMP, INDBAL, ITBAL)```

CTLS2, DECID3, UPDZ, and SUMOLIA form a control system referred to in the formulation as "CTLS2". To select this control system input INDSEL of 103 (J01).

Tasks are performed at each entry point as follows:

- **IENTRY = 1** is called when 20 or more passes have occurred on a cycle. The program is terminated.
- **IENTRY = 2** is called for nominal initialization.
- **IENTRY = 3** is called when a trial missed cutoff and computed partials. The step size is noted as a bad step. Partialis are turned off and the next trial step size is set to one-half the current step size.
- **IENTRY = 4** is called after a successful trial is made with partials on. A parabolic prediction is performed. If a gain was made on the trial and the predicted percentage gain for another trial is less than 25% for another trial, the step is accepted. If a gain was made but the predicted percentage gain for another trial is 25% the step is not accepted immediately. Tests to limit the number of passes are applied if the step is not immediately accepted or no gain was made and trial may be accepted if a gain was made or a new step size may be determined for another trial with partials taken.
- **IENTRY = 5** is called for output of restart cards. None are output.
- **IENTRY = 6** is called when a trial missed cutoff and did not compute partials. The same action as IENTRY = 3 is taken.
- **IENTRY = 7** is called after a successful trial is made with partials off. A parabolic prediction is performed. If a gain was made on the trial and the predicted percentage gain for another trial is less than 5% partials will be taken the next trial. Tests to limit the number of passes are applied. These tests may turn on partials if a good step is available but no gain was made in the previous trial. A new step size for another trial is determined.
ENTRY = 8  is called for initialization each cycle.
ENTRY = 9  is called to make decisions for the $\Delta w$ mode shape. If step size is too small the program is terminated.
ENTRY = 10 is called to set INDOON for CRTS2 after a trial. INDCON is set to zero.
ENTRY = 11 is called after DAICAL is computed following the reverse integration. The only action is a RETURN.
ENTRY = 12 is called when DENOM is not positive. The program is terminated.
ENTRY = 13 is called to set INDOON, invert the $I_{yy}$ matrix, and update parameters for $5\sigma$ calculation after the reverse integration. INDOON is set to zero and UPKI is called to calculate parameters for $5\sigma$ calculation and to invert the $I_{yy}$ matrix.

After each trial trajectory, a point is generated on the graph of change in payoff ($\Delta p$) vs. step size, unless cutoff was missed. A point with positive $\Delta p$ is called a good point and the step size is called a good step. A point with negative $\Delta p$ is called a bad point and the step size is called a bad step. The step size on a trial trajectory which misses cutoff is also called a bad step.

From the theoretical considerations the graph of $\Delta p$ vs. step size must rise to a peak from the origin and fall off. Our objective is to arrive at a good point with step size as close to this peak as possible. We attempt to do this by a parabolic search procedure.

After each trial trajectory which has missed cutoff, partials are turned off and another trial will be made with step size 1/2 the last trial step.

After each trial trajectory which has not missed cutoff, a parabolic fit is made to the last trial point and any previous good points. If no previous good points are available, the fit is made to the origin, the last trial point, and the slope at the origin. If only one previous good point is available the fit is made to the origin, the previous good point, and the last trial point. If two previous good points are available, one lying on either side of the last trial point, the fit is made to those three points. If two such good points are not available, but two good points have been found which lie on one side of the last trial point, the fit is made to those three points.

After the fit has been made, a preliminary step size to use for another trial pass is determined. If the parabola is not concave downward the preliminary step will be the smaller of 5 times the last trial step and 9/10 the smallest previous bad step. If the parabola is concave downward, the step size is set to the larger of 1/10 the last trial step and the smallest of 5 times the last trial step size coordinate of the maximum point on the parabola, and 9/10 the smallest previous bad step.
If less than 10 passes have been made and the last trial step had positive $\Delta q$, the parabolic fit and the preliminary step size are used to find the predicted change in payoff from the parabola. If partials were taken and the predicted gain is less than 25% the last trial is accepted as a valid step. If partials were not taken and the predicted gain is less than 5% partials are turned on and another trial trajectory is made using the preliminary step size.

If 10 passes have been made and the peak has not been found the last step will be taken if it is a good step and partials were taken. If it was a bad step, the program will go to the best good step size so far, take another pass with partials on and accept that pass. If no trial so far has produced a good step, the step size is halved and a trial made. Halving will continue until a good step is found or 15 passes have been made and the program terminates. If a good step is found one more pass at that step size will be made with partials on and that pass will be accepted.

Remarks

DECID3 is called only by DECIDE which in turn is called only by CTLS2.

DECID3 calls UPDK, WSNRM, and STOP.
17. **DECID2 - Arbitrary Decision Routine**

This is a dummy routine included so the user may write his own decision subprogram to be used with CTLS2 in the optimization program.

Such a routine must adhere to the entry point pattern established by CTLS2 and make those decisions assigned to it by CTLS2.
18. **PACK** – Integer Word Conversion Routine

**Purpose:**

To insert the character to be plotted into the correct position in an integer type word.

**Method:**

PACK uses DECODE to break a word into 4 words, each containing one character. The $\text{(IPOS+1)}$th word is then set equal to CHAR and ENCODE is used to place the 4 characters back into the word.

**Usage:**

CALL PACK(WORD, CHAR, IPOS)

where

- **WORD** = the word in which the character is to be placed
- **CHAR** = the Hollerith character to be inserted into **WORD**
- **IPOS** = one less than the position in **WORD** into which **CHAR** will be inserted

**Subroutines Called:**

System functions ENCODE and DECODE.
PACK

ENTER

DECODE

SPLIT(IPOS+1)=CHAR

ENCODE

RETURN
19. WNOW - Weighting Matrix Norm Calculation

Purpose:
To compute the current weighting matrix norm when using OPTION 5.

Usage:

\[
\text{CALL WNOW (WNEW)}
\]

\[
WNEW = \left( \sum_{i=1}^{\text{MCONT}} \int_0^T (W_{i,i-1})^2 \, dt + \sum_{j=1}^{\text{INDIOP}} (U_{j-1})^2 \right)^{1/2}
\]

\text{MCONT} = \text{number of control variables}
\text{INDIOP} = \text{number of initial control variables}
\text{T} = \text{terminal trajectory time}
WHEN = 0.

\[ (\text{DO 10 } I=1, \text{MCONT}) \]

\[ \text{WHEN + WHEN + ABS(SINTEG(I))} \]

\[ (\text{CONTINUE}) \]

\[ \text{INDIOP} = 0 \]

\[ (\text{DO 20 } I=1, \text{INDIOP}) \]

\[ \text{WHEN + WHEN + UMATX(I)}^2 \]

\[ (\text{CONTINUE}) \]

RETURN
20. **UPDK - Convergence Control Routine**

**Purpose**

To determine when and how to tighten constraint belts, and to perform the tightening; to test for convergence of the optimization process and terminate the program if convergence is obtained, and to recompute $\Phi$, $\Phi^*$, and the coefficients for the augmented payoff function.

**Usage**

CALL UPDK

CTL32, DECID3, UPDK, and SUMOLA are the routines which implement the control system referred to as "CTL32" in the formulation.

This routine makes those decisions which have most effect on the convergence of the optimization process under "CTL32".

The philosophy of the routine is given in the formulation manual. The procedure by which SIEERR is reduced is referred to as belt tightening. The logic of the routine is given in the accompanying explanatory flowchart.

A tool for investigating the convergence effects of decisions other than those made by the normal logic of this routine is provided. This tool is referred to as "Analyst Control." Using this option, all decisions on tightening and phase selection are superseded by data inputs which completely pre-determine when and how tightening is done and what phase will be entered. This is not intended for normal use.

The normal logic is referred to as "Program Control". Certain parameters used by this option may be modified by data. Modification by data is not recommended.

Parameters for UPDK and their effect on tightening and phase selections are listed under the two options. These parameters may be set to values other than the nominal by input data.

See routine FENAL for a description of the augmented payoff function used by this routine.
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal</th>
<th>Effect</th>
</tr>
</thead>
</table>
| INDIT     | 0       | 0 selects program control  
1 selects analyst control |
| INICYC    | All 1000 | When NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8, belts will be tightened. INTCYC is an array of eight values. |
| INTPH    | All 0  | INTPHZ(J) is the phase to be entered after belt tightening when NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8. INTPHZ is an array of eight values. |
| ITIT     | 0       | If ITIT > 0 and NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8, and INTCYC(J) > 0, INTCYC(J) will be replaced by INTCYC(J) + ITIT after belt tightening. |
| TTIT     | 0       | Basic belt tightening factor. When belts are to be tightened, all are multiplied by TTIT. If all constraint errors are still within their respective belts, the belts are again multiplied by TTIT. This continues until at least one error is outside its belt. Then all belts less than 1/2 their respective tolerances are increased to 1/2 those tolerances. After belt tightening, if TTIT is 0, it is set to .1. TTIT may be modified before tightening by TINT and TDUN. |
| TDUN     | 0       | If NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8, and INTCYC(J) < 0, TTIT is multiplied by TDUN before belt tightening. Total tightening modification factor. |
| TINT     | All 1.  | Partial tightening modification factor. If NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8, and INTCYC(J) > 0, TTIT is multiplied by TINT(J) before belt tightening. TINT is an array of eight values. TINT may be modified by TMOD. |
| TMOD     | 0       | If NCYCLE = | INTCYC(J)|  where 1 ≤ J ≤ 8 and INTCYC(J) > 0 and ITIT > 0, TINT(J) is replaced by TINT(J) - TMOD after belt tightening. |
## Program Control

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>INDINT</td>
<td>0</td>
<td>0 selects program control, 1 selects analyst control</td>
</tr>
<tr>
<td>INTEX</td>
<td>3</td>
<td>The ratios: $\frac{\Phi_i - \Phi_{INTEX}}{\Phi_{INTEX}}$, $i = 1, \text{INTEX}-1$</td>
</tr>
<tr>
<td>TiOL</td>
<td>.005</td>
<td>If all ratios specified by INTEX are less than or equal to TiOL and belt tightening has not been delayed by INTSTY, a check will be made for convergence and belts will be tightened.</td>
</tr>
<tr>
<td>INTSTY</td>
<td>3</td>
<td>Belt tightening is delayed by the INTSTY number of cycles after leaving phase 0 or effecting a belt tightening.</td>
</tr>
<tr>
<td>TTIT</td>
<td>0</td>
<td>Same as for Analyst Control.</td>
</tr>
<tr>
<td>ITIT</td>
<td>0</td>
<td>Same as for Analyst Control.</td>
</tr>
<tr>
<td>INTDUN</td>
<td>3</td>
<td>Total tightening cycle indicator. When ITIT = INTDUN, TTIT is multiplied by TDUN before tightening.</td>
</tr>
<tr>
<td>TDUN</td>
<td>0.</td>
<td>Total tightening modification factor for TTIT.</td>
</tr>
<tr>
<td>TINT</td>
<td>All 1.</td>
<td>Same as for Analyst Control.</td>
</tr>
<tr>
<td>INTPHZ</td>
<td>All 0</td>
<td>Same as for Analyst Control.</td>
</tr>
</tbody>
</table>
### Analyst and Program Control

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENDCON</td>
<td>All blank</td>
<td>Identifiers for payoff and constraints. ENDCON is an array of ten words. The first is the payoff function, the rest are constraint functions. MAXIM or MINIM must be &quot;FNALTY&quot;.</td>
</tr>
<tr>
<td>SIBAR</td>
<td>All 0.</td>
<td>Desired constraint values. SIBAR is an array of ten values. The first is a dummy.</td>
</tr>
<tr>
<td>SITOL</td>
<td>All 0.</td>
<td>Allowable constraint error. SITOL is an array of ten values. The first is a dummy.</td>
</tr>
<tr>
<td>SIERR</td>
<td>All .01</td>
<td>Belt sizes for constraints. SIERR is an array of ten values. The first is a dummy. The rest are belt values for the constraints.</td>
</tr>
<tr>
<td>INDUMY</td>
<td>4</td>
<td>Initial phase for CTLS2 control system. 4 is phase 0. 3 is phase 1.</td>
</tr>
<tr>
<td>P</td>
<td>1</td>
<td>Exponent used in determining phase 1 mode parameters.</td>
</tr>
<tr>
<td>RATIO</td>
<td>2</td>
<td>Step size multiplicative change factor between successive cycles.</td>
</tr>
</tbody>
</table>

**Remark:**

- UPDK is called by DECID3.
- UFDK calls INVERT and STOP.
LOGIC OF UPDK

Enter

Program Control

Type of Control

Are we in phase 0? Yes → A

No

Test for belt tightening

Tighten

Tightening - Delay in effect? Yes → B

No

Determine phase to go into

Modify Tightening Parameters

C

Test for Convergence

Not converged.

Convergence obtained.

Set to terminate

Tighten Belts

B

Tighten belts on this cycle? Yes

Determine phase to go into

Modify Tightening Parameters

B

415
Logic of UPDK (Cont.)

A
Phase 0

B
Go to appropriate phase computations

Phase 1

Test to leave Phase 0

Stay in phase 0

Calculate phase 0 mode parameters

Calculate phase 1 mode parameters

Den Parameter Bad?

Yes

Set to phase 0

C

No

Recalculate

\[ \eta \phi \]

\[ \tilde{a}^\nu \]

\[ \tilde{K}_i, \ i = 1, \ \text{INDPMT} + 1 \]

(augmented payoff coefficients)

Return

\[ \text{Go to appropriate phase computations} \]
\[ (DO503) = 1.e \]

\[ NCYCLE = |INTCYC(i)| \]

\[ NEWTMY = 4 - INTPHZ(i) \]

\[ INTCYC(i) \]

\[ T \]

\[ TTIT = TTIT + TDUN \]

\[ TTIT = TTIT + TINT(i) \]

\[ \text{CONTINUE} \rightarrow \]

\[ \text{CONTINUE} \rightarrow \]

\[ TINT(i) = TINT(i) - TMOD \]
\[ \text{UPDK} \]

1. **WRITE 6 2000**

2. **DO 5401 I, 2, 111PMT**

3. \[ \text{ERR(I)} > \frac{SIERR(I)}{2} \] ?

4. \( \text{CONTINUE} \)

5. **WRITE 6 2100**

6. **NEWTIMY = 3**

7. **INTSTEP = INTSTY**

8. **DO 5403 I = 2, 111PMT**

9. \[ DB(I) = -\text{ERR(I)} \cdot \min(1, \frac{\text{ERR(I)}}{\text{SIERR(I)}}) \cdot TEXP \] ?

10. \( \text{CONTINUE} \)

11. **J**
\begin{itemize}
  \item \texttt{WRITE 6 2800}
  \item \texttt{WRITE 6 2900}
  \item \texttt{CSQ = 0}
  \item \texttt{WRITE 6 2800}
  \item \texttt{WRITE 6 2900}
  \item \texttt{CSQ = CSQ + CSINL(i).CSINL', (i)}
  \item \texttt{CONTINUE}
  \item \texttt{CSQ = \sqrt{CSQ}}
  \item \texttt{(DO 5905 I = 1, I11PMT)}
  \item \texttt{CSINL (i) = CSINL(i) \cdot CSQ}
  \item \texttt{CONTINUE}
  \item \texttt{WRITE 6 2700}
  \item \texttt{WRITE 6 1400}
\end{itemize}

(9)
This program is the program for calculating the solutions to the adjoint
equations. There is a striking similarity between the structure of the EXE
segment and the REV segment. In fact, REV proper was programmed by modifying
the same logic that was used in EXE.

The input to REV comes from three sources: value in COMMON, information
on TAPE12, and sometimes information on IATAP. The output from REV consists
of information on ILTAP and values in COMMON/2/ and values in COMMON.

Large arrays must be dealt with in REV. In order to conserve core, it
is assumed that COMMON/1/ and COMMON/5/ are available for use.

The Partial tape

REV calls the routine UNPART to read the partial tape for everything
except the P matrix. To get the P matrix (if it exists) at the beginning of
a major stage REV itself reads the partial tape. (If the P matrix does not
exist, REV constructs the identity matrix and puts it in P). The reading of
the partial tape is the most critical task of the reverse trajectory. The
trouble occurs because the information that is put on it, sequentially, in the
forward trajectory is needed in the opposite order in the reverse trajectory.
This means that the partial tape has to be read in the reverse direction by
backspacing, reading, backspacing, etc. The F and G matrices are treated as
functions of stage time in the reverse trajectory. The F and G stage time
histories exist on the partial tape. Since the table of F and G's for an
entire stage would be too large to accommodate in the machine, the table of
F and G's which is actually used to do the interpolation is constructed from
the two adjacent points which bracket the current value of stage time in the
reverse trajectory. REV is responsible for updating the F and G tables as
the stage time changes; it does this by shifting the table values and reading
a new F and G point from the partial tape (via a call to UNPART) and putting
the respective values into the vacated spots of the F and G tables.

Staging and Time Points in REV

ND is an indicator set in EXE and transmitted to REV on the partial tape.
It informs REV when the end of a major stage (ND=1) has been reached (i.e., the
beginning of a major stage in the forward trajectory), and also whether a P
matrix exists on tape at the stage point (ND=3) or if the stage point corre-
spends to the very first point of the forward trajectory (ND=0)

The NPT values in the array TIMESA are those values of stage time which
must be hit during a stage of the reverse integration. These points are
determined during the integration of the forward trajectory; NPT and the
TIMESA array go out on the last record written on the partial tape at the end
of a major stage of the forward trajectory. Hence at the beginning of every
major stage of the reverse trajectory this array is read in from TAPE12
(via the call to UNPART). Every stage time value at which there is an F and G matrix on TAPE 12 must appear in the TIMESA array. REV keeps track of the next time point that must be hit in the cell TIMPT. When TIMPT is hit (i.e., when TIMES = TIMPT) this point is defined to be a stage point. The type of stage point is reflected in the value given to INDSTG; this is done in the area labeled "STGTST ROUTINE FOR REVERSE" in the listing. The meaning of the respective values of INDSTG follow:

\[
\begin{align*}
\text{INDSTG} &= 0 \quad \text{not yet at a stage point} \\
&= 1 \quad \text{the end of the reverse trajectory} \\
&= 2 \quad \text{the end of a major stage of the reverse trajectory} \\
&= 3 \quad \text{the end of a minor stage of the reverse trajectory (i.e., get new F and G)} \\
&= 4 \quad \text{merely a time point (Throw away all points of the TIMESA array not needed by decrementing NPT by 1)}
\end{align*}
\]

**INTERPOLATION**

Before REV calls ADJEQ (3) to do the bulk of the calculation of the derivatives, it computes the instantaneous approximation to the F and G matrices by calls to the interpolation routine TLUREV. Also at this time, REV calls TLUREV to obtain the approximation to the instantaneous values of the control variables. (The control variables are put on TAPE12 at the same time F and G are put on TAPE12). This method of preserving the control variables is not always exact. An alternate method which is better but which involves more effort is available; it involves use of the CRVSR routine.

**Integration**

It is assumed that only fixed step integration is to be used in REV. This is not too strong an assumption since the density of points of the TIMESA array will dictate the requirement of taking relatively small steps. The integration step to be used in REV is DELTSR. DELTSR is transmitted to REV on the partial tape. Hence DELTSR may appear in major or minor stage data of EXE. If DELTSR is not input EXE initializes DELTSR to DELTS at every major stage.

**Numbered COMMON Usage**

COMMON /A/ is assumed to be free. Many of the large arrays used in REV are in the COMMON /L/ block. COMMON/2/ is for the matrices Iψ, Iδ, Iσ. COMMON/5/ is assumed to be free and will be used whenever any features of the routine CRVSR are used. The core requirements of REV can be cut down considerably if appropriate arrays are equivalent to one another.

The following is a list of some of the variables used in REV which are important and which may not be described elsewhere since they are not in COMMON:

- **ALPHC(3,6)**: 2 point table of control variable values and the interpolated values.
- **FMATX(3,15,15)**: 2 point table of F matrix values and the interpolated values.
GMATX(3,15,6) 2 point table of G matrix values and the interpolated values.

TDMP(2) 2 point table of the stage times for the above three tables.

NDUMMY an indicator which mimics the indicator ND and which is put on the ILTAP (by ADJEQ(8)) and which serves the same purpose in DALCAL as ND does in REV.

TIMESA (500) an array of stage time points which must be hit.

NPT the number of points in the TIMESA array.

TILPMT the next time point from the TIMESA array which must be hit.
Organizational Chart for REV

*DESIGNATES MULTIPLE ENTRY POINTS
1. CTVSR - Control Variable Routine for REV

Purpose

During the reverse trajectory, to obtain what is needed from the information on IATAP (prepared in DALCAL or MAIN). To accomplish reading IATAP during the reverse trajectory, it is necessary to request this in the data (DATA1): 

<table>
<thead>
<tr>
<th>INDALF</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>IATAP is not read in REV.</td>
</tr>
<tr>
<td>1</td>
<td>IATAP is read in REV on all cycles after the nominal.</td>
</tr>
<tr>
<td>2</td>
<td>IATAP is first prepared with all the information that REV needs from it (on the nominal) in MAIN. Then IATAP is read in REV on every cycle including the nominal.</td>
</tr>
</tbody>
</table>

CTVSR(2) reads IATAP if it is needed. If so, then CTVSR(3) computes the control variable values from the CTABLE which was read from IATAP at CTVSR(2) in the same manner that CTVS(3) does for the forward trajectory. One reason for requesting that this be done is to preserve the CTABLE at time points closer than those time points at which partials are computed. (the CTABLE is always preserved at those time points where partials are computed without the need for doing CTVSR calculations.) To request this optional type preservation of CTABLE requires that DELTSA be input as well as INDALF (see CTVS). Another reason for requesting that IATAP be read is to obtain the weighting matrix table that was used on the previous cycle (this is needed if and only if INDWMA = 5).

Remarks

CTVSR is to REV as CTVS is to EXE.
2. **ADJEQ - Adjoint Equations Routine**

**Purpose**

This is the basic subprogram of REV. ADJEQ is to REV as DIFEQ is to EXE. ADJEQ contains the equations for computing the derivatives of the adjoint variables at ADJEQ(3) and the transformation of the adjoint variable across major stage points at ADJEQ(2). A description of the notation used follows:

\[
\begin{align*}
\text{PHIOLA} & : \lambda \varphi \Omega \\
\text{PSIOLA} & : \lambda \gamma \Omega \\
\text{PHIOLG} & : \lambda \varphi G \\
\text{PSIOLG} & : \lambda \varphi G \\
\text{PHIOLW} & : \lambda \varphi G^{\text{C}}^{-1} \\
\text{PSIOLW} & : \lambda \varphi G^{\text{C}}^{-1} \\
\end{align*}
\]

\[
\begin{align*}
\text{PHIOLI} & : \lambda \varphi \Omega = -F' \lambda \varphi \Omega \\
\text{PSIOLI} & : \lambda \gamma \Omega = -F' \lambda \gamma \Omega \\
\end{align*}
\]

\[
\begin{align*}
\text{PMATX} & : F' \\
\text{GMATX} & : G \\
\text{PNATX} & : P \\
\text{RMATX} & : R \\
\text{PARTOM} & : \frac{\partial \varphi}{\partial x} \\
\text{PARTPH} & : \frac{\partial \varphi}{\partial \phi} \\
\text{PARTPS} & : \frac{\partial \varphi}{\partial \psi} \\
\text{PSI771} & : \dot{\varphi} \\
\text{PHI771} & : \dot{\Omega} \\
\text{OMEGA1} & : \dot{x} \\
\text{X57771} & : \dot{x} \\
\end{align*}
\]

\[
\begin{align*}
\text{PHJUMP} & : \lambda \varphi P \dot{x} \\
\text{PSJUMP} & : \lambda \varphi G P \dot{x} \\
\end{align*}
\]

436
\[
\begin{align*}
\text{SISII} & \quad -\int_T^t \lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' dt = I_{\phi \phi} (+K_{\phi \phi}) \\
\text{PEFEI} & \quad -\int_T^t \lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' dt = I_{\phi \phi} (+K_{\phi \phi}) \\
\text{SIFEI} & \quad -\int_T^t \lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' dt = I_{\phi \phi} (+K_{\phi \phi}) \\
\text{SISIX} & \quad \lambda_{\phi \Omega} U^{-1} (\lambda_{\phi \Omega})' = K_{\phi \phi} \\
\text{SIFEK} & \quad \lambda_{\phi \Omega} U^{-1} (\lambda_{\phi \Omega})' = K_{\phi \phi} \\
\text{PEFEK} & \quad \lambda_{\phi \Omega} U^{-1} (\lambda_{\phi \Omega})' = K_{\phi \phi} \\
\text{PHIOLR} & \quad \lambda_{\phi \Omega} (\text{or } \lambda_{\phi \Omega}) \\
\text{PSIOLR} & \quad \lambda_{\phi \Omega} (\text{or } \lambda_{\phi \Omega}) \\
\text{PHIOLRX} & \quad \lambda_{\phi \Omega} U^{-1} \\
\text{PSIOLRX} & \quad \lambda_{\phi \Omega} U^{-1} \\
\text{ALPSI} & \quad \int_T^t |\lambda_{\phi \Omega}| dt \text{ or } \int_T^t WW' dt \\
\text{ALPSI1} & \quad |\lambda_{\phi \Omega}| \text{ or } WW' \\
\text{ALPHC} & \quad \alpha \\
\text{VALINS} & \quad \chi_0 \\
\text{SISII1} & \quad -\lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' \\
\text{PEFEI1} & \quad -\lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' \\
\text{SIFEI1} & \quad -\lambda_{\phi \Omega} W^{-1} (\lambda_{\phi \Omega})' \\
\text{UNATX} & \quad U^{-1} \\
\text{W} & \quad W^{-1} \\
\text{TIMES} & \quad t_s \text{ (stage time)}
\end{align*}
\]

**Method**

**ALMVEQ(1):** The integrated variables are initialized to 0. These variables include \(\lambda_{\phi \Omega}, \lambda_{\phi \Omega} U, I_{\phi \phi}, I_{\phi \phi}, I_{\phi \phi}, \) and ALPSI. This point of the reverse trajectory corresponds to the last point of the forward trajectory.
ADJEQ(2): Entry is made here at the first point of every major stage of the reverse trajectory; this point corresponds to the last point of the corresponding stage of the forward trajectory.

\[ \begin{align*}
\lambda^+ \varphi_{\Omega} & \rightarrow \lambda^- \varphi_{\Omega} \\
\lambda^+ \zeta_{\Omega} & \rightarrow \lambda^- \zeta_{\Omega} \\
\tilde{x} & \rightarrow \hat{x}
\end{align*} \]

\[ \text{stage } j \quad \text{stage } j + 1 \]

forward trajectory

\( \lambda^+ \) and \( \lambda^- \) will, in general, be discontinuous at a major stage point. The initial conditions for these variables at the beginning of the new stage \((\lambda^+ \varphi_{\Omega}, \lambda^+ \zeta_{\Omega})\) are expressed in terms of their values at the end of the last stage \((\lambda^- \varphi_{\Omega}, \lambda^- \zeta_{\Omega})\) and the values \(\tilde{x}, \tilde{\varphi}, \tilde{\zeta}, \tilde{\Omega}, \frac{\partial \varphi}{\partial x}, \frac{\partial \zeta}{\partial x}\), and \(P\) which have been computed at the corresponding stage point of the forward trajectory and have been transmitted on tape to the REV segment. The transformation is:

\[
\begin{align*}
\lambda^+ \varphi_{\Omega} & = \lambda^- \varphi_{\Omega} + \tilde{\varphi} \frac{\partial \varphi}{\partial x} - \left[ \frac{\tilde{\varphi} + \lambda^- \varphi_{\Omega} \tilde{P}}{\tilde{\varphi}} \right] \frac{\partial \varphi}{\partial x} \\
\lambda^+ \zeta_{\Omega} & = \lambda^- \zeta_{\Omega} + \tilde{\zeta} \frac{\partial \zeta}{\partial x} - \left[ \frac{\tilde{\zeta} + \lambda^- \zeta_{\Omega} \tilde{P}}{\tilde{\zeta}} \right] \frac{\partial \zeta}{\partial x}
\end{align*}
\]

ADJEQ(6): This is entered at the beginning of every major stage, after ADJEQ(2) has been called. At this entry point values of PSJUMP and FSJUMP are output. These had been computed in the process of making the transformation at ADJEQ(2).

ADJEQ(5): Not used.

ADJEQ(6): Code printing and value printing are done for the following variables: \(\lambda^+ \varphi_{\Omega}, \lambda^+ \zeta_{\Omega}\). If the end of the trajectory is at hand, then code and value printing are done also for the following variables: \(I_{\varphi}, I_{\zeta}, I_{\varphi \zeta}, I_{\zeta \varphi}, I_{\varphi^2}, I_{\zeta^2}, \lambda^+ \varphi_{\Omega}, \lambda^+ \zeta_{\Omega}, K_{\varphi \zeta}, K_{\zeta \varphi}, K_{\varphi^2}, K_{\zeta^2}\) (if they have been computed).

ADJEQ(7): This entry point defines the variables that are to be integrated (see ADJEQ(1)).
ADJSEQ(3): This entry point is called immediately after each integration step. The purpose is to put $\lambda_{\chi_G} W^{-1}$ and $\lambda_{\chi_T} G^{-1}$, $W^{-1}$, $t_g$, and $\sigma$ on tape ILTAP so that the information may be used later on to compute the perturbation to make to the $\sigma$ history. In addition, if it is the last point of the reverse trajectory (corresponds to first point of forward trajectory), and if initial conditions are being perturbed, then $\lambda_{\chi_G}$, $\lambda_{\chi_T}$, $\lambda_{\chi_R} U^{-1}$, $\lambda_{\chi_T} R^{-1}$, $K_{\chi_R}$, $K_{\chi_T}$, $K_{\chi_G}$ are computed. The $K$'s are added to the corresponding $I$'s then $\lambda_{\chi_T} R U^{-1}$, $\lambda_{\chi_T} R U^{-1}$ and $\chi_o$ are put on ILTAP. Except for the last record, ILTAP is prepared by calling the ad-hoc blocking routine DALPACK.

Remarks

1. Any computations pertaining to the $\chi$ functions will not be done if $\text{INDPMT} = 0$. $\text{INDPMT}$ is the number of $\chi$ - components in the various vectors and matrices e.g., $\lambda_{\chi_G}$, $\lambda_{\chi_T}$, etc. (The $\chi$-functions are those variables listed in the ENDCON array).

2. Computations for initial condition perturbation e.g. $\lambda_{\chi_R}$, $K_{\chi_R}$, $K_{\chi_T}$, etc. are not done if $\text{INDICP} = 0$.

3. It is assumed that $\text{MCONT} > 0$; i.e. there is at least one control variable.

4. The information that ADJSEQ needs from PARTS is available when ADJSEQ is called. REV proper sees to it that the partial tape is read when it is needed. There is one exception to this: ADJSEQ(8) reads the partial tape to obtain the $R$ matrix (if it is needed).
3. **UNPART - Unblocking Routine for Partials**

**Purpose:**

To unpack TAPE12 which has been packed in large arrays to eliminate unnecessary I/O device selection.

**Method:**

TAPE12 has been prepared in chain EXE. The records only contain non-zero from the output values in chain EXE.

**Usage:**

Entry is made to the routine with the following statement:

```plaintext
CALL UNPART (MCONT, NSTATE, IFM, IGM, IT, ND, IALP, IDEL, IWA, IWAI, CTABUB, INDPMT, IPARTPS, IK, IENTRY)
```

- **MCONT** = Number of control variables.
- **NSTATE** = Number of state variables.
- **IFM** = F from chain EXE.
- **IGM** = G from chain EXE.
- **IT** = Time.
- **ND** = Control words.
- **IALP** = Control Variables.
- **IDEL** = Delta time used in reverse.
- **IWA** = Weighting Matrix indicator.
- **IWAI** = Weighting Matrix data.
- **CTABUB** = Control variable bounds data.
- **INDPMT** = Number of constraints.
- **IPARTPS** = Terminal partials.
- **IK** = Subscript used in storing data.
- **IENTRY** = Entry point to subroutine UNPART.

Subroutines called from this routine include IZUNPK and normal FORTRAN I/O routines.
4. **MIMINR - Integration Routine for REV**

**Purpose**

This routine is essentially the same as MIMINF. MIMINR is used for the reverse trajectory. It does not contain entry point 5 for truncation error estimation and step size control since it is assumed that fixed step integration will always be used in the reverse trajectory.

**Method**

The relationship of MIMINR to REV is analogous to the relationship of MIMINF and EME.

**Remarks**

The MIMINF write-up should be consulted for more detailed information.
5. **WMA - Weighting Matrix Routine**

**Purpose**
To provide optional methods for computing the inverse weighting matrices \((W^{-1})\) and \((U^{-1})\)

**Usage**

CALL WMA (IENTRY)

This routine follows the entry point pattern of ADJSEQ. Several options are available. \(W^{-1}\) and \(U^{-1}\) are determined by the following inputs:

<table>
<thead>
<tr>
<th>INDICATOR</th>
<th>NOMINAL</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>INDWMA</td>
<td>0</td>
<td>Basic option indicator.</td>
</tr>
<tr>
<td>IWCYCL</td>
<td>0</td>
<td>Starting matrix indicator.</td>
</tr>
<tr>
<td>IWDELT</td>
<td>0</td>
<td>Periodic matrix indicator.</td>
</tr>
<tr>
<td>WAI</td>
<td>0</td>
<td>Basic constant input array. WAI is an array of six values.</td>
</tr>
<tr>
<td>WBI</td>
<td>0</td>
<td>Basic constant input array. WBI is an array of six values.</td>
</tr>
<tr>
<td>UMATX</td>
<td>1</td>
<td>Basic initial control variable input array UMATX is an array of fifteen values.</td>
</tr>
</tbody>
</table>

In the following description:

The subscript \(i\) runs from 1 through \(MCONT\).

The subscript \(j\) runs from 1 through \(INDIOP\).

The subscript \(K\) runs from 1 through \(MCONT\).

\(MCONT = \) number of control variables.

\(INDIOP = \) number of initial control variables.

\(SINTxG_i = \) total integral of \(\lambda \cdot \hat{G}
\)

\(t = \) time.

**INDWMA = 0**

(a) \(W_{i,i}^{-1} = 1\).

(b) \(U_{j}^{-1} = UMATX_j\)
**INWMA = 1**

(a) when NCYCLE ≤ IWCYCL - 1:

\[ W_{i,j}^{-1} = 1. \]

(b) when NCYCLE > IWCYCL - 1, the \( W^{-1} \) matrix is time-varying:

\[ W_{i,j}^{-1} = W_{A}^{-1} + W_{B}^{-1} \cdot t \]

(c) \( U_{j}^{-1} = U_{MATX}^{-1} \)

**INWMA = 2**

(a) when NCYCLE ≤ IWCYCL - 1:

\[ W_{i,j}^{-1} = 1. \]

(b) when NCYCLE > IWCYCL - 1 and IWDELT ≠ 0 and NCYCLE is not a multiple of IWDELT:

\[ W_{i,j}^{-1} = 1. \]

(c) when NCYCLE > IWCYCL - 1 and IWDELT = 0 or IWDELT ≠ 0 and NCYCLE is a multiple of IWDELT and no previous cycle has been run:

\[ W_{i,j}^{-1} = 1. \]

(d) when NCYCLE > IWCYCL - 1 and IWDELT = 0 or IWDELT ≠ 0 and NCYCLE is a multiple of IWDELT and a previous CYCLE has been run:

\[ W_{i,j}^{-1} = \frac{W_{A}^{-1} + W_{B}^{-1} \cdot \sum_{K} |SINTEG_{K}| / |SINTEG|}{(MCONT+1)} \]

where \( SINTEG_{K} = \int_{T}^{T} \phi_{K} \cdot \partial t \) from the previous cycle.

(e) \( U_{j}^{-1} = U_{MATX}^{-1} \)

**INWMA = 3**

(a) when NCYCLE ≤ IWCYCL - 1

\[ W_{i,j}^{-1} = 1. \]

(b) when NCYCLE > IWCYCL - 1 and IWDELT ≠ 0 and NCYCLE is not a multiple of IWDELT:

\[ W_{i,j}^{-1} = 1. \]
(c) when NCYCLE ≥ INCYCL - 1 and IWDELT = 0 or INDELT ≠ 0 and NCYCLE is a multiple of IWDELT, the $W^{-1}$ matrix is time-varying:

$$W^{-1}_{i,j} = \frac{\overline{W}_i \cdot \overline{W}_i}{2 \cdot (\text{MCOUNT} + 1)}$$

where $\overline{W}_i = WAI_1 + WAI_4 \cdot B$,

$$\overline{W}_i = WAI_1 + WAI_2 \cdot \frac{h}{|\lambda_i \cdot G|}$$

$B = \max value of \sum K^i \lambda G$ on the previous cycle.

$h = \text{instantaneous value of } \sum K^i \lambda G$.

(d) $U^{-1}_j = \text{UMAT}_j$

INDWMA = 4

(a) when NCYCLE ≤ INCYCL - 1

$$W^{-1}_{i,j} = 1.$$ (b) when NCYCLE > INCYCL - 1

$$W^{-1}_{i,j} = \delta_i,$$

where $\delta_i = 0$, unless $i = \left[ \frac{\text{Remainder upon division of NCYCLE by IWDELT}}{\text{MCOUNT}} \right] + 1$, in which case $\delta_i = 1$.

This allows the user to work with one control variable at a time, staying with each for IWDELT cycles at a time.

(c) $U^{-1}_j = \text{UMAT}_j$

INDWMA = 5

(a) when NCYCLE ≤ INCYCL - 1, or no previous cycle has been run, the $W^{-1}$ matrix is time-varying:

$$W^{-1}_{i,j} = WAI_1 + WBI_1 \cdot t$$

(b) when NCYCLE > INCYCL - 1, and a previous cycle has been run, the $W^{-1}$ matrix is time-varying:

The calculation of this $W^{-1}$ matrix is somewhat complex.

For each new cycle a normalizing factor $W'$ is computed by the formula:

$$W' = \left\{ \frac{1}{T} \int_{-\infty}^{\infty} (W^{-1}_{i,j})^2 dt \right\} + \sum_j (U^{-1}_{j})^2 \right\}^{1/2}$$
where \( W_{i-1} \) and \( U_{j-1} \) are from the previous cycle.

For each stage the quantities \( W_i \) are computed as an average value for \( W_{i-1} \) during the stage on the previous reverse.

At each point the quantity \( W_i \) is computed as the maximum value for \( W_i \) during the stage on the previous reverse. (If \( \lambda_i \) is the value of \( \lambda_i \) at this time during the previous reverse. (If CTABUS or CTABLE is being used to bound a control variable and it lies on its boundary and \( \lambda_i \) and \( \lambda_i \) agree in sign, \( W_i \) is set to 1.).

For the first point computed in the stage:

\[
W_{i,1}^{-1} = \frac{\bar{W}_i}{W^* W_i^{1/2}}
\]

For the \((j+1)\)st point computed in the stage:

\[
W_{i,j+1}^{-1} = \bar{W}_i + \frac{W_j^{1/2} - \bar{W}_i}{W^*_{j+1}}
\]

where \( \bar{W}_i = W_{i,j}^{-1} \) at the \( j \)th point computed.

(c) when \( \text{NCYCLE} < \text{INCYCL} - 1 \)

\( U_{j-1} \) is computed by a formula analogous to that for \( W_{i,j}^{-1} \) at the first point in a stage.

\( \text{INDWMA} = 6 \)

(a) \( W_{i,j}^{-1} = W_{i,j} \)

(b) \( U_{j,j}^{-1} = U_{MATX,j} \)

Remarks

The weighting matrices for \( \text{INDWMA} = 5 \) are designed for use with the CTLS2 control system only.

\( WMA \) is called by ADJSEQ.

\( WMA \) calls CODES and VALUES.
6. DALPACK - Blocking Routine for A's

Purpose:
To store data in large arrays to eliminate unnecessary I/O.

Method:
Data is stored in a large array until it has been filled before being output on tape.

Usage:
Linkage to this routine is accomplished via the statement
CALL DALPACK (IWGTF0,IT,NDUMMY,INDPMT,NCNT,IWGTS0,IALPHA)
IWGTF0 arrays used in the control program.
IWGTS0 arrays used in the control program.
IT TIME.
NDUMMY control word generated in reverse.
INDPMT number of constraints.
NCNT number of control variables.
IALPHA alpha point in CTABLE.
Remarks:
IW Weighting matrix
ILTAP Tape being used
Normal I/O routines are called.
7. **FLUSH - BUFFER FLUSH ROUTINE**

**Purpose**
To flush the ILTAP buffer at the end of the reverse trajectory.

**Usage**
CALL FLUSH(ILTAP)

---

**FLUSH**

1. **ENTER**
2. **IXA=1?**
   - **YES** → **RETURN**
   - **NO** → **WRITE IATAP**
8. **IZUNPK - Switch Testing Routine**

**Purpose:**

The routine tests a set of switches to see if the argument should be set to zero or a number should be pulled out of an array.

**Method:**

A set of switches has been preset by another routine and IZUNPK tests these switches and resets all arrays in proper order.

**Usage:**

Entry is made to this routine by the following statement:

```
CALL IZUNPK(IA)
```

where

IA = The argument to be set by the routine

No other routines are called by this subroutine
IZUNPK

F

IA(KK) > ISWIT(LL)

T

IN = IA(IXA)

IXA = IXA + 1

IN = 0
IA(KK) = IA(KK) - ISWIT(LL)

LL = 59

T

LL = LL + 1
KK = KK + 1

LL = 1

RETURN
A program has been set up in the program as a data gathering chain for plotting purposes. The CDC 280 plotting package set up at AFRL was used in checking out the program. The basic part of the segment is still in the program. To use the plotting equipment, it is only necessary to provide the additional subroutines, normally available on the 6000 series computers, which output information to the 280 for photographing and displaying at the console. A preliminary report on the CDC280 has been included, which gives detailed descriptions of the routines, including purpose, operation, usage and examples.
SOME OF THE ROUTINES HEREIN DESCRIBED WERE ORIGINALLY DEVELOPED FOR USE AT AFML. MOST OF THE REPORT WAS TAKEN FROM "UHRT PLOTTING ROUTINES IN USE AT LRL-LIVERMORE" WRITTEN BY JUDITH D. FORD AND MARILYN J. WELSH (UCHL-14427-T), SINCE MANY OF THE ROUTINES ARE THE SAME IN NAME, AS WELL AS EFFECT, AS THOSE IN USE AT LRL.

ABSTRACT

THIS REPORT DESCRIBES A SYSTEM OF PLOTTING ROUTINES. THERE FORTRAN ROUTINES PROVIDE A FLEXIBLE PACKAGE FOR POINT, LINE, AND CHARACTER PLOTTING VIA A CDC280 DISPLAY DEVICE.

INTRODUCTION

THIS PAPER DESCRIBES THE SUBROUTINES AVAILABLE ON THE 6600 WHICH OUTPUT TO THE 280. THESE ROUTINES GENERATE DATA IN A BUFFER IN THE 6600 CENTRAL MEMORY. A PERIPHERAL PROCESSING UNIT (PPU) CLEARS THE BUFFER AND STORES THE DATA ON FILE NAMED -FIIMFL-. AT THE COMPLETION OF THE RUN A PPU SENDS THIS FILE TO THE CDC280. THE INFORMATION IS THEN PHOTOGRAPHED AT THE RECORDING CONSOLE (OR DISPLAYED AT THE OPERATORS OPTION). THE FILM IS THEN DEVELOPED AND MADE READY FOR DISTRIBUTION.

THIS REPORT GIVES DETAILED DESCRIPTIONS OF THE 280 ROUTINES, INCLUDING PURPOSE, OPERATION USAGE, AND EXAMPLES. THE ROUTINES ARE SEPARATED INTO THE FOLLOWING CLASSES:

1. MAPPING ROUTINES:

   THESE ROUTINES SET UP SCALE FACTORS FOR CONVERTING THE USERS COORDINATES TO THE 280 RASTER POINT COORDINATES (RASER POINT DEFINED LATER). THESE ROUTINES MAY ALSO DRAW SCALES WITH GRID LINES OR SHORT MARKS ALONG THE AXES.

2. ARROW, LINE, AND POINT PLOTTING ROUTINES:

   THESE ROUTINES PROVIDE THE FACILITY FOR PLOTTING VARIOUS TYPES OF CURVES.

3. CHARACTER PLOTTING ROUTINES:

   THESE ROUTINES PROVIDE THE FACILITY FOR PLOTTING ALPHANUMERIC INFORMATION.

4. ABSOLUTE PLOTTING ROUTINES:

   THESE ROUTINES POSITION THE BEAM INDEPENDENT OF THE SCALING DEFINED BY THE MAPPING ROUTINES.
5. **Utility Routines:**

These routines give the facilities for framing, and initializing the plot package.

6. **Internal Routines:**

Internal routines perform various functions necessary to the operation of the system, and the user is normally not aware of their existence.

The CDC280 plane is defined to be a (1024 by 1024) square of addressable points on the face of a cathode ray tube (CRT). These points are called raster points. Information is displayed by unblanking the CRT beam. The beam may be moved to a new position without unblanking (i.e. without plotting a line). Points may only be positioned at a raster point. Lines may only be drawn between two raster points (i.e. the beam unblanked between these two raster points may or may not intersect other raster points.

In the following description of the 280 routines, it is assumed that all arguments are given in the same mode as the dummy arguments, using the standard FORTRAN conventions for the names of integer and floating point variables. The dummy arguments spelled -DUM- are not used by the routine. These arguments are reserved in some cases for future options.

For the purposes of these routines this 280 plane is regarded as having the usual X, Y cartesian coordinates, both of which range from 0. to 1. with the origin at the lower left corner. If no mapping routine is called all coordinates for the plotting routines are assumed to be between 0. and 1.

**MAPPING ROUTINES**

This group of routines makes it unnecessary for the user to scale his own numbers for plotting on the 280. This is accomplished by establishing a mapping from the user's coordinate plane onto some portion of the 280 plane. This, by the way, allows more than one graph to be plotted on a frame. CALL MAP

\[ (XMIN, XMAX, YMIN, YMAX, XMI, XMA, YMI, YMA) \]

are the users maximum and minimum cartesian coordinates.

\[ XMI, XMA, YMI, YMA \] are the maximum and minimum coordinates of the 280 plane desired to be used.

This description encompasses a group of twelve routines, each of which established a mapping from the rectangle in the user's plane with corners \( (XMIN, YMIN) \) to the rectangle in the 280 plane with corners \( (XMI, YMI) \). Unless reset, this mapping applies to all subsequent plotting, except the absolute plotting routines.

Linear mappings are established by -MAP-, -MAPG-, and -MAPS-.

MAP establishes a mapping only
MAPG plots a grid with scale numbers.

MAPS plots a rectangle with scale numbers and short marks along the axes.

The suffixes -LL-, -SL- and -LS- may be used with any of -MAP-, -MAG- or
-MAPS- to modify the mapping as follows:

LL establishes a log-log mapping.

SL establishes a semi-log mapping with the X-axis linear.

LS establishes a semi-log mapping with the Y-axis linear.

The cycles are determined automatically. Examples:

CALL MAP (0.,1.,0.,1.,0.,1.)
sets up a linear-linear mapping,

CALL MAPSLL (1.,10.,1.,100000.,1.,999,1.,999)
sets up a 1 cycle by 5 cycle scale, and

CALL MAPSL (1.,100.,1.,1000.,1.,5.,1.,999)
sets up a linear by 2 cycle grid.

The mapping function is initially set

\[ XMIN = YMIN = XMI = YMI = 0. \quad \text{and} \quad XMAX = YMAX = XMA = YMA = 1. \]

The scale numbers will overplot the grid lines if \( SMI \) or \( YMI \) is less than .078125 for linear scaling or .043 for logarithmic scaling.

Plotting routines specifying point(s) out of the defined user domain are handled in two ways:

1. If the scaled coordinate is within the 280 range then the routine is executed at the scaled coordinate.

2. If the scaled coordinate is outside of the 280 range then this coordinate is projected on the nearest extreme edge and the routine executed there.

An error message is printed whenever a mapping routine is called with \( XMIN \leq XMAX, YMIN \leq YMAX, XMI \geq XMA, YMI \geq YMA \) or a log mapping is called with a non-positive argument.

CALL MAPP(RMAX, XMI, XMA, YMI),

RMAX is the maximum radius for the user's polar coordinates.

XMI, XMA, YMI are the same as in -MAP- above.

-MAPP- establishes a mapping from the circle of radius RMAX in the user's polar coordinate plane into the square in the 280 plane with corners (XMI, YMI), (XMA, YMA) where \( YMA = YMI + (YMA - YMI). \)
Vertical and horizontal reference axes will be plotted, with scale numbers along the zero-degree axis, and with the origin at the center of the square. All (X,Y) pairs given in later plotting routines will be interpreted as polar coordinates \((R,\theta)\) until another mapping routine is called.

```
CALL MAPX (XMIN, XMAX, YMIN, YMAX, XMI, XMA, YMI, YMA, I)
```

I is an integer \(1 \leq I \leq 13\).

The remaining arguments are the same as in \(\text{MAP}\) above.

\(\text{MAPX}\) allows the mapping to be specified at execution time, according to the value of \(I\). A call to \(\text{MAPX}\) is equivalent to a call to one of the above mapping routines, with the integers 1-13 corresponding to these routines in the following order:

\(\text{MAP, MAPSL, MAPLS, MAPG, MAPGSL, MAPGL, MAPS, MAPSSL, MAPSLS, MAPSLL, MAPP}\).

When \(I = 13\) the arguments in \(\text{MAPX}\) correspond to \(\text{MAPP}\) as follows: CALL \(\text{MAPX} (\text{DUM, RMAX, DUM, DUM, XMI, XMA, YMI, YMA, DUM, 13})\).

ARROW, LINE AND POINT PLOTTING ROUTINES

Order Alphabetically

These routines may be used to display and/or photograph data in graphic form. The user's \((X, Y)\) coordinates in these plotting routines are scaling the scale factors set up by a mapping routine. If no mapping routine has been called, these coordinates are assumed to be in the range 0. to 1.

```
CALL SETBEAM (X, Y)
```

\(X\) is the abscissa at which the beam is to be positioned.

\(Y\) is the ordinate at which the beam is to be positioned.

\(\text{SETBEAM}\) causes the beam to be positioned at \((X, Y)\) without unblanking.

```
CALL LINEOPT (DUM, INTEN)
```

\(DUM\) is a dummy argument.

\(\text{LINEOPT}\) is the intensity at which all arrows, lines, points, and vectors will be plotted.

\(0\) low intensity (fine line).

\(1\) high intensity (heavy line).
-LINEOPT- is initially set to low intensity.

The mapping routines reset -LINEOPT- from within.

CALL POINT (X, Y)
X and Y are the coordinates of a point.
-POINT- will plot a point at (X, Y) with intensity set by -LINEOPT-.

CALL LINE (X1, Y1, X2, Y2)
(X1, Y1) and (X2, Y2) are the coordinates of two points. -LINE- will sweep a line from (X1, Y1) to (X2, Y2) with intensity set by -LINEOPT-.

CALL LINEP (X1, Y1, X2, Y2, K)
(X1, Y1) and (X2, Y2) are the coordinates of two points.
K is an integer.
-LINEP- plots a line consisting of every Kth raster point between (X1, Y1) and (X2, Y2). Intensity is set by LINEOPT.

CALL VECTOR (X2, Y2)
(X2, Y2) is the coordinate of a point.
-VECTOR- sweeps a line from the current beam position to (X2, Y2) with intensity set by LINEOPT.

CALL POINTS (X, T, N)
X and T are the names (first word addresses) of arrays of the X and Y coordinates of points.
N is the number of points.
-POINTS- plots the N points given by the arrays X and T. The intensity is set by -LINEOPT-.

CALL ARROW (X1, T1, X2, Y2, I)
(X1, T1) and (X2, Y2) are coordinates of two points.
I is an integer ≥ 1.
-ARROW- sweeps a line from (X1, T1) to (X2, Y2) and draws an arrowhead at (X2, Y2). The arrowhead measures I raster points in length. I = 10 is a small size arrowhead. The intensity is set by -LINEOPT-. The final beam position is (X2, Y2).
CALL LINES (X,Y)

X and Y are the names (first word addresses) of arrays of the X and Y coordinates of points.

N is the number of points.

-LINES- connects the N points given by the arrays X and Y with line segments. The final beam position is (X(N),Y(N)). The lines are swept with intensity as set by -LINEOPT-.

Order Alphabetically

CHARACTER PLOTTING ROUTINES

This group of routines allows the plotting of alphanumeric information, either to label the various curves, lines, etc., produced by the point and line plotting routines, or as more versatile alternative to an off-line printer (this is distinct from the -FILMPR- option. -FILMPR- merely simulates the printer). This versatility derives from:

1. The capability of positioning a line of alphanumeric information anywhere on the current frame (vs. the top-to-bottom progression of a page printer).

2. The two orientations, two intensities and four character sizes that are available, and

3. The expanded character set, which includes many non-key punchable characters. (not immediately available)

CALL CHAROPT (DUM,DUM,ISIZE,IOR,DUM)

ISIZE = 0 miniature
   1 small
   2 medium
   3 large

IOR = 0 horizontal (0°)
   1 vertical (90°)

-CHAROPT- specifies the size (ISIZE) and orientation (IOR) of all characters to be plotted. The option is changed by a second call to -CHAROPT-.

The maximum string length and line limits for the various sizes are:
In the character plotting routines, the 280 plane is considered to be a grid of rectangles, each containing one character of the chosen size. The number and dimensions of these rectangles depend on the character size and orientation. Characters are drawn within the rectangle. The rectangle is positioned such that the current beam position is in the lower left corner of the rectangle. After the character has been drawn, the beam is positioned in the lower right corner of the rectangle.

CALL SYMBOL (A) or CALL SYMBOL (MH...$)

A is the first word of BCD data. The end of string is designated by $.

MH...$ is a Hollerith text of M characters. The last two characters must be $., which designates the end of string.

-SYMBOL- encodes BCD data into the 280 character set and plots it starting at the current beam position with options as given by -CHAROPT-.

If $. does not appear at the end of string -SYMBOL- attempts to plot words up to the field length.

CALL NUMBER (X,F)

X is a variable (fixed or floating).

F is any allowable FORTRAN format ≤ 10 characters.

-NUMBER- converts the variable X under the given format, determines the field width and plots the resulting characters as -SYMBOL- would.

Example:

```
X = 1.E5
CALL NUMBER (X,5HE10.2)
```

465
would plot

bbbl.00005

and

.

.

I = 42

CALL NUMBER (1, 94444IN = ,I3)

.

.

would plot

INb = b42

ABSOLUTE PLOTTING Routines

Order Alphabetically

These routines position the beam independently of the defined mapping function. The arguments range from 0. to 1. Out of range points are projected on the nearest extreme edge of the plotting areas.

CALL ABSEAM (X,Y)

X,Y are coordinates of a point.

-ABSEAM- causes the beam to be positioned at (X,Y) without unblanking.

CALL ABSVECT (X,Y)

X,Y are coordinates of a point.

-ABSVECT- draws a vector from the last beam position to (X,Y).

CALL ABSLINE (X1, Y1, X2, Y2)

(X1,Y1), (X2,Y2) are coordinates of two points.

-ABSLINE- draws a line from (X1,Y1) to (X2,Y2).

CALL ABSPT (X,Y)

X,Y are coordinates of a point.

-ABSPT- plots a point at (X,Y).
UTILITY ROUTINES

CALL INIT280

-INIT280- initializes the 280 routines and must be called before any of
the plotting routines.

CALL FRAME

-FRAME- advances the microfilm to the next blank frame.

INTERNAL ROUTINES

These routines are essential to the plotting routines, but are not called
directly by the user, only by other routines in the system. -GRID80- is called
by the mapping routines which draw scale marks or grid lines and label them
with scale numbers.

-GTRF-, -GEQF-, -EQLF-, -SEQF-, -SMLF-, -UNQF-, and -ZGTRF- are functions
which are used in -GRID80-. Each has two arguments and returns a value of 1
if the first argument stands in the indicated relation to the second, a value
f 0 otherwise.

<table>
<thead>
<tr>
<th>FUNCTION</th>
<th>RELATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>GTRF</td>
<td>greater than</td>
</tr>
<tr>
<td>GEQF</td>
<td>greater than or equal to</td>
</tr>
<tr>
<td>EQLF</td>
<td>equal to</td>
</tr>
<tr>
<td>SEQF</td>
<td>less than or equal to</td>
</tr>
<tr>
<td>SMLF</td>
<td>less than</td>
</tr>
<tr>
<td>UNQF</td>
<td>not equal to</td>
</tr>
</tbody>
</table>

These functions call -ZGTRF- to establish the value.

-TEST- is called by the mapping routines to establish legal arguments.

-ADJUST- is called by some of the plotting routines to convert non-linear
arguments to linear before scaling.

-LENGTH- is called by number to count the number of characters to be
plotted.

-STREND- called by symbol to test for end of string symbol.

-PScale- is called by the mapping routines to establish the scaling.

-PILOTQ- is called by the plotting routines and forms the 280 instructions.
ORGANIZATIONAL CHART FOR GRAPHL
Usage

This is the segment for plotting curves from the forward trajectory on microfilm. GRAPH is called by CTLS before the call is made to REV. Therefore when GRAPH is finished it calls REV. However, CTLS calls GRAPH if and only if there are plots to be made. The number of core locations reserved for setting up the tables for plotting may vary depending on the available core. In general, this array (POINTS) should be dimensioned as large as possible, so that GRAPH takes up almost as much core as the largest of the remaining segments. MAXPOT is the value at which POINTS is dimensioned. To vary the dimension of POINTS it is necessary only to change the dimension statement for POINTS and the data statement for MAXPOT in GRAPH proper.

GRAPH drives the plotting computations by calling PAPLT to plot the regular trajectory curves (those specified in the PLT array) and PRPLT to plot the F and/or G time history.
DATA FOR PLOTTING

Two types of plotting are possible — printing along with the normal output, or by plotting on microfilm.

Printer Plotting: (done in CTLs segment from DIALCAL)

Example: INDPLT INT 39,39

The $\alpha$ and/or $\delta \alpha$ stage time history are plotted for each major stage for the respective control variables if the corresponding two digit integer of the INDPLT array is non-zero and if the second digit is a multiple of the cycle number. The first digit may be either 1, 2, or 3:

1 - $\alpha$ history only (and $w^{-1}$ history if INDWMA = 5)
2 - $\delta \alpha$ history only (and $W^{-1}$ history if INDWMA = 5)
3 - both $\alpha$ and $\delta \alpha$ history (and $W^{-1}$ history if INDWMA = 5)

Microfilm Plotting: (done in GRAPH SEGMENT)

Example:

```
PLOTS BCD 6 TIME bbb HCC777F ALPHAB D4MACH bbb TIME bbb GAM7B
INDFAG 3
IGCONT 2
```

The definition of the abscissa and ordinate variable of each plot are listed successively on the PLOTS card (abscissa, ordinate, abscissa, ordinate, etc.). A plot of up to six passes of each cycle will be made for a given curve, all passes for a cycle for a given curve will appear on the same graph. Values are saved on tape for plotting at every (IGCONT+1)th valid integration step.

INDFAG 0 do not plot partials
1 plot the $F$ matrix vs. time
2 plot the $G$ matrix vs. time
3 plot both the $F$ matrix and the $G$ matrix vs. time.
SEGMENT GRAPH

REWIND 17

REWIND ILTAP

CALL PAPLT (MAXPOT, POINTS)

CALL PRPLT (MAXPOT, POINTS)

CALL FRAME

CALL CHAIN (REV)

END
7. "PAPLT - Parameter Collection Routine"

Purpose:

To read TAPE17, assemble the points to be plotted into arrays and call the routine to do the actual plotting (PLTCUR).

Method:

TAPE17 will be rewound and re-read if there is not enough room to accommodate all the plots at one time. Hence, if there is room to accommodate just one plotting array, all plots will eventually be made; if there is not room for one plot then no plots will be made. PAPLT must be compatible with PLTS of the EYE segment and with the initialization done in MAIN1 for the plotting variables. The format of the POINTS array appears on the flow chart; PAPLT fills this array as it reads TAPE 17 until the last point of the last pass of the forward trajectory is reached. PAPLT does not fill up the POINTS array with those plots that have already been made (i.e., on previous passes through TAPE17). Also, PAPLT does not fill up the POINTS array with those plots for which it does not have room on the current pass through TAPE17.

The following is a description of the important variables that are used internally to the PAPLT routine:

- **INDNTD** the number of plots to be made on a given read through TAPE17
- **JPLT** an array of indicators; a function to the LPLT array
- **KROOM** the maximum number of plots that will fit into the POINTS array
- **MMPT** an array of base subscripts for each pass (for the points array)
- **NPAST** the pass number read from tape
- **IPOINT** the point number read from tape
- **KPASS** min (NPASS, 6)
- **NPLT** an array to indicate if the i'th plot has been made
- **KPLT** array of indicators; may change for each read through TAPE17
- **NPLTS** the number of plots that have been made

For each plot that is made, there will be KPASS curves appearing on the same graph, one for each pass of the forward trajectory. The plots to be made are defined completely in the data on the LOTS card.
8. **P1WLT - Partials Collection Routine**

**Purpose:**

To read ILTAP, assemble the points to be plotted into arrays, and call the routine to do the actual plotting (PLTCUR). ILTAP contains the time histories of the F and/or G matrices.

**Method:**

The organization of this routine is very similar to that of PAPLT. The differences that do exist make this the less complicated routine. The elements of the F and/or G matrices are always plotted as a function of time. P1WLT will make several passes through tape ILTAP in order to get all the plots if it is necessary to do so. For each element of the F and G matrix one plot will be made (consisting of just one curve).

The format of the POINTS array appears on the flow chart; it is different than that from the PAPLT routine.

In addition to the variables described for PAPLT, the following variable definitions are important:

- **NF** number of plots to make from the F matrix.
- **NG** number of plots to make from the G matrix.
- **INL** respectively, the left and right limit subscripts for the array that is read from tape; any variable whose subscript in the array lies within the interval \([INL, INR]\) will be plotted for the current read through tape ILTAP.
9. PLTCUR - Microfilm Plotting Routine

Purpose:
To plot a set of curves on one graph; the output is to be to microfilm.

Usage:
CALL PLTCUR (NI, NPTS, X, Y, CODEX, CODEYA, CODEYB)

where

NI  Number of curves to be plotted on a graph.
NPTS An array containing the number of points for the respective curves.
X   An array containing the abscissa values for each curve.
Y   An array containing the ordinate values for each curve.
CODEX A Hollerith code word for identifying the abscissa; this will be placed under the abscissa axis on the graph.
CODEYA Hollerith code words for identifying the ordinate; these will be placed along the ordinate axis on the graph.
CODEYB

The format of the X and Y arrays must conform to the following standard:

<table>
<thead>
<tr>
<th>Points for curve</th>
<th>Points for second curve</th>
<th>etc.</th>
<th>Points for last curve</th>
</tr>
</thead>
<tbody>
<tr>
<td>X1 or Y1:</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>NPTS(1)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>NPTS(2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>NPTS(NI)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

In addition to identifying each plot with the Hollerith code words from the calling sequence, PLTCUR will put the cycle number, the pass number and the case code in the lower left hand corner of the graph. PLTCUR will put two graphs on a frame; for any given call to PLTCUR the graph for that call will be put at one of these positions in the frame depending on the value of the variable SHIFT. If SHIFT=0 the graph is placed in the first half of a frame; if SHIFT=.5 the graph is placed in the second half. PLTCUR updates SHIFT to the appropriate value and changes frames when necessary just before the return is made to the calling program.

All curves on a given graph will be made in low intensity except the last which will appear in high intensity.

PLTCUR calls a number of routines which must exist in the library "microfilm plot package."

A graph will not be plotted by PLTCUR if the maximum deviation within the X1 or Y1 arrays is less than $10^{-4}$. 

476
CALL CHAROPT (DUM,DUM,0,1,DUM)

CALL ABSBEAM (40..25+SHIFT)

CALL SYMBOL (CODVA)

CALL ABSBEAM (40..31-SHIFT)

CALL SMBOL (CODVB)

CALL LINEOPT (DUM,1)

DO 50 I=1,NI

IF (I.EQ.NI) CALL LINEOPT(DUM,1)

KPTS = 1+PTS(I)

CALL SETBEAM (X1(JSUB+I),Y1(JSUB+I))

DO 45K=1,KPTS

CALL VCTOR(X1(J),Y1(J))
10. **Dummy Plot Routines**

The following dummy routines are included in the deck so that it may be compiled on a machine without attached CDC 280. When using a machine with attached CDC 280 these routines should be replaced by the library routines.
SUBROUTINE ABSHEAM(A+B)
RETURN
END

SUBROUTINE ABSVECT(A+R)
RETURN
END

SUBROUTINE MAP(A+H+C+D+E+F+G+H)
RETURN
END

SUBROUTINE LINEOPT(A+R)
RETURN
END

SUBROUTINE CHAROPT(A+R+C+D+E)
RETURN
END
SUBROUTINE NUMBER(A,R)
RETURN
END

SUBROUTINE SYMBOL(A)
RETURN
END

SUBROUTINE SETBEAM(A,R)
RETURN
END

SUBROUTINE FRAME
RETURN
END

SUBROUTINE VECTOR(A,R)
WRITE(6,1000) A,H
1000 FORMAT(1H,10X,1PE15.7,5X,1PE15.7)
RETURN
END

NUMR0001
NUMH0002
NUMH0003

SYM0001
SYM0002
SYM0003

SET0001
SET0002
SET0003

FRAM0001
FRAM0002
FRAM0003

VECT0001
VECT0002
VECT0003
VECT0004
VECT0005
SECTION X

DIRECTORY

Purpose:

To provide a method of reading input symbolically. This subroutine (Blocked Data) has no executable instructions in it. It is designed merely as a means of getting data symbols loaded with the program. No flow chart accompanies this write-up.

Method:

The format of the directory is described here. The directory is divided into two parts: (1) one list is a list of the BCD symbols. (2) the second part is made up of a set of subscripts which corresponds to the BCD words.

For each variable name desired in the directory there must be a corresponding subscript. Thus, each variable in the directory must be in COMMON in order that a subscript may be assigned at assembly time.

Usage:

This subroutine may not be "USED" by the programmer. Rather, it is referred to by subroutines.
1. CTAE - Parameter Optimization Control Program

Purpose:

To control trajectory and optimization calculation sequence when the parameter optimization option is used.

Method:

The parameter optimization algorithms define a control parameter vector. The control parameter vector elements are equated to specific trajectory data input parameters which have been flagged through the "PAR" input option in READA. A trajectory is generated by a call to CHAIN(2), and the resulting trajectory payoff and constraint functions are retrieved for use in the parameter optimization procedure.

CTAE also controls a multiple extremal search procedure through subroutine WARPS, and a saddle-point search procedure for solution of "mini-max" problems through subroutine SADDLE.

Remarks:

All subroutines employed in the parameter optimization procedure are separately documented in Volume IV of the present report.
STOP 1
OPTEND

TRUE

YES

FALSE

NO

ILPHA .LE. 1

Y

N

"a trajectory law has been converted"

C

YES

NO

INDPHI2 .LT. 1

"set constraint functions for vehicle one"

"set constraint functions for vehicle two"

YES

NO

YES

NO

"set constraint functions for vehicle one"

"set constraint functions for vehicle two"

YES

NO

MOSER .LE. 0

YES

NO

WARPS BESTAF (3)

INIT TOP

INTLWPA=3

B

NOT REPRODUCIBLE

484
START OPTIMIZATION PROCESS

MAINOP

NSR > EQ. 1

YES

SADDLE

YES

NSR > EQ. 1

NO

NO

compute trajectory

CHAIN (2)

INTURP = 2

WARPS

J33 = J33 + 1

NO

INPRE = GT. 0

NO

J33

YES

compute trajectory

J33 = J33 + 1

J33, NE. 1

FUNCTION (WARP) FUNCTION (RWC)

BESTAF (3)

BESTAF (2)

NO

YES

PENLTY

BESTAF (1)

MENTRY = 3

NO

MENTRY = 9

NO

J33 = J33

start point indicators to provide final trajectory
## SECTION XI

### ALPHABETIC INDEX OF SUBROUTINES

<table>
<thead>
<tr>
<th>Subroutine Name</th>
<th>Page No.</th>
<th>Subroutine Name</th>
<th>Page No.</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABSBEAM</td>
<td>480</td>
<td>CRATE2</td>
<td>199</td>
</tr>
<tr>
<td>ABSVECT</td>
<td>480</td>
<td>CTAE</td>
<td>483</td>
</tr>
<tr>
<td>ACOS</td>
<td>167</td>
<td>CITLOFT</td>
<td>318</td>
</tr>
<tr>
<td>ADJEQ</td>
<td>436</td>
<td>CTRITR</td>
<td>219</td>
</tr>
<tr>
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