INVESTIGATIONS ON P-WAVE
ARRIVALS AT LSA

MICHAEL A. CHINNERY
The arrivals of P-waves at the Large Aperture Seismic Array (LASA) from over 3000 earthquakes at various azimuths and distances have been studied. From each set of arrival times a variety of parameters related to the travel time curve are determined. This report consists primarily of a summary of the principal features of these parameters, as functions of epicentral distance and azimuth.
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LASA
Apparent velocities
Travel time anomalies
INVESTIGATIONS OF P-WAVE ARRIVALS AT LASA

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ABSTRACT

The arrivals of P-waves at the Large Aperture Seismic Array (LASA) from over 3000 earthquakes at various azimuths and distances have been studied. From each set of arrival times a variety of parameters related to the travel time curve are determined. This report consists primarily of a summary of the principal features of these parameters, as functions of epicentral distance and azimuth.
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INTRODUCTION

Investigations of the arrival times of P-waves at the Large Aperture Seismic Array (LASA) at Billings, Montana, have been carried out by the principal investigator during the period October, 1965 to July, 1971, under several ARPA contracts. These studies were unusual in that a very large quantity of high-quality data were obtained. Portions of these data, together with interpretations, have been published (see References), but inevitably much remains that cannot be interpreted at present. The purpose of this report is to catalogue as many as possible of the observations that have been made.

Since many similar studies using various arrays have appeared, and continue to appear, in the literature, it is worthwhile to emphasize the uniqueness of the present set of data. The quality of the data is primarily due to the physical size (about 200 km aperture) of the LASA array, and to the availability of recordings that permit the relative timing of arrivals to .05 seconds or better. This immediately suggests that it should be possible to determine $dT/d\Delta$ from these arrivals with a precision of better than 0.1 seconds/degree, and the observed scatter in the determinations agrees with this conclusion. In fact, the observed scatter is between 3 and 10 times smaller than those of most other published studies.

The high quantity of data is partly due to the sensitivity of the array, and partly due to its location. The array lies in such a position that most of the circum-Pacific belt of seismic activity lies within two rather small azimuth ranges.
from the array (see Section 2). The array is therefore particu-
larly suited to observations of the variation of travel-time
parameters with epicentral distance. It is unfortunate that
the azimuthal distribution of events is much less complete. One
important result of the large number of earthquakes studied is
that it has become possible to apply strong criteria in the
selection of data. The data shown in this report represent only
about 70% of those obtained; the rest were eliminated as being
somewhat less reliable for a variety of reasons.

One unexpected problem that results from the high quality
of the present data is that considerable fine structure becomes
apparent. This is shown not only by the distance variation of
dT/dΔ, but also in the differences between observations along
different azimuths. Unfortunately it is not possible to provide
a convincing explanation for most of these features. On the
other hand, smoothing (or averaging) of the data does not seem
justified in view of the small amount of scatter. This leads
to certain ambiguities in the interpretation of the data.

This report concentrates, therefore, on an exposition of
the data, and the methods by which they were obtained. Very
few comments on the possible meanings of the results are included.
I. ANALYSIS OF THE DATA

The data used in this study consists of the first arrivals of P-waves at the Large Aperture Seismic Array (LASA) in Billings, Montana. These arrivals were determined visually from the 16 mm film records of the short period instruments at the array. In particular, the arrivals were recorded for the center seismometer in each of the sub-arrays in the E and F rings, and the center sub-array AO. The locations of these sub-arrays are shown in Figure 1, and their coordinates with respect to a N-S E-W coordinate system centered on the sub-array AO are shown in Table 1.

The recording of a typical earthquake (one of magnitude 4.4 in the Aleutian Islands) is shown in Figure 2a. The lack of coherence of the waveforms beyond the first half-cycle is clearly indicated. For this reason, timing methods that involved correlation of the waveform across the array were tested and eliminated early in the study. Ideally, the "knee" of the onset should be timed, but this was found to be difficult for all but the largest events. As a compromise, all arrival measurements were made on the first peak (or trough) of the arrival. For all the events included in this report, it was possible to time this point with a precision of 0.05 seconds or better. The relative times of arrival with respect to AO were therefore subject to a maximum error of ±0.05 seconds, and in most cases the estimated error is about one half of this.

Many events were not recorded at all nine seismometers, due to equipment failure, excessive noise level, and so on. It was
Fig. 1: Location and Geometry of the Large Aperture Seismic Array (LASA), near Billings, Montana.
A. III: Station Coordinates, in km. The x axis points due East, and the y axis points due North.

<table>
<thead>
<tr>
<th>Subarray</th>
<th>x</th>
<th>y</th>
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<tr>
<td>04</td>
<td>-54.749</td>
<td>80.574</td>
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found in the course of the study that the dT/d\(\Delta\) values for these events showed a significantly larger scatter than for those recorded at all the sites. For this reason, incompletely recorded events have not been included in this study.

The basic data for each event therefore consists of a set of eight times, relative to AO. These times were processed on the IBM 360 computer at Brown University to extract a variety of information. One page of printed output was obtained for each event, and a typical output is shown in Figure 2b, for the event shown in Figure 2a. The various items on this output are described briefly below:

a) Using the USCGS epicenter, the azimuth and distance of the event were calculated, using a sub-program that includes the effect of ellipticity.

b) The distance was corrected for the effect of focal depth, by extrapolating the ray path back to the earth's surface. This correction is small for events at teleseismic distances with focal depths less than about 200 km. It can be estimated accurately enough for the present purposes on the basis of a standard crust and upper mantle structure. The Jeffreys-Bullen structure was used, and the corrections for various focal depths and distances are given in Figure 3. Earthquakes deeper than 200 km were not used in this study.

c) The dT/d\(\Delta\) corresponding to any given model is determined for the corrected distance, and listed as "calculated slope." In this case, the model A (Chinnery, 1969) was used as a standard.
Region: Andreanof Islands, Aleutian Islands
Location: Lat 51.3N  Long 176.5W
Origin Time: 00 25 51    Focal Depth: 58 km
Magnitude: 4.4
**EVENT 18N1**

<table>
<thead>
<tr>
<th>Station</th>
<th>Obs Time</th>
<th>Delay</th>
<th>Delta</th>
<th>Plane Residuals</th>
<th>Standard Deviation</th>
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<td>0.17</td>
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<tr>
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<tr>
<td>D1</td>
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<td>-6.80</td>
<td>-0.8</td>
<td>0.11</td>
<td>0.10</td>
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</tbody>
</table>

**Model A calculated slope = 7.361 secs/deg**

**Plane Wave Fit**
- Observed azimuth = 301.12 degrees
- True - observed azimuth = 1.77 degrees
- Travel time 1st derivative = 7.93 secs/deg
- Standard deviation = 0.168 secs

**First Degree Polynomial Fit**
- Travel-time 1st derivative = 7.92 secs/deg
- Standard deviation = 0.176 secs

**Second Degree Polynomial Fit**
- Travel-time 1st derivative = 7.94 secs/deg
- Travel-time 2nd derivative = -0.68 secs/deg/deg
- Calculated - observed slope = -0.08 secs/deg
- Standard deviation = 0.152 secs

**Third Degree Polynomial Fit with f Fixed**
- Travel time 1st derivative = 7.94 secs/deg
- Travel-time 2nd derivative = -0.66 secs/deg/deg
- Travel-time 3rd derivative = -0.410 secs/deg/deg/deg
- Standard deviation = 0.151 secs

**Third Degree Polynomial Fit**
- Travel-time 1st derivative = 8.19 secs/deg
- Travel-time 2nd derivative = -0.63 secs/deg/deg
- Travel-time 3rd derivative = -2.744 secs/deg/deg/deg
- Standard deviation = 0.143 secs
Fig. 3: Distance corrections for a standard Jeffreys-Bullen structure, as functions of epicentral distance and focal depth.
This facilitates the comparison of this particular event with other results.

d) A plane wave is first fitted to the wavefront. If the arrival time (relative to AO) is \( T_i \) at a site with coordinates \( x_i, y_i \) (again, relative to AO), the data are fitted to an equation of the form:

\[
T_i = \alpha x_i + \beta y_i + \epsilon_i = 0
\]

(1)

The coefficients \( \alpha \) and \( \beta \) were determined by a least squares process, and from them the apparent azimuth and a first estimate of \( \frac{dT}{d\Delta} \) could be obtained. These results are listed under the heading "plane wave fit." The agreement between the apparent and true azimuths was in general very good. This point is discussed further later in this report.

e) Because of the comparatively large aperture of the array, about 200 km, it was necessary to include the possibility of curvature of the wavefront in the vertical plane containing the azimuth to the source. A simple and effective way of doing this is to project the positions of the sub-arrays onto this plane, and replace the coordinates \( x_i, y_i \) by a single variable \( \delta_i \), the distance of the ith sub-array from AO along the azimuth towards the event. In this calculation, the "true" azimuth was used. Now \( T_i \) may be regarded as a function of \( \delta_i \) alone, and first, second and third order relations may be written as:

\[
T_i - T_\nu + \alpha \delta_i = 0
\]

(2)
where \( a-f \) are constant coefficients, and \( T_0 \) is included so that the equations are not constrained to pass through \( AO \).

Equations 2, 3 and 4 were fitted to the observed times by least squares, and it is clear that the first, second and third derivatives of the travel time curve may be determined from the coefficients \( a-f \). The results are listed under first, second and third degree polynomial fit, on the output sheet. In addition, an equation of the form of 4, but with \( d \) constrained to be equal to \( b \), was used. The latter fit was found to give the least scatter in estimates of the second derivative.

f) At the foot of the page, the observed times, the \( \delta_i \), and the residuals from the various fits are listed. In addition, the times predicted by the model and the apparent station correction are included.

g) Also printed out are the differences between the true and observed azimuths, and between the observed and calculated \( dT/d\Delta \), together with the standard deviation of the various polynomial fits.
II. DISTRIBUTION OF EVENTS

Over three thousand events have been processed in the above manner. This covers the operation of the array from its inception, in October, 1965, through the end of 1968. These events are distributed at a variety of azimuths and distances from the array, as shown in Figure 4. It should be noted that only those earthquakes that gave an amplitude of greater than 5 millimicrons at the array have been included. This means that there is a considerable variation in magnitude of the events considered, and accounts for the scarcity of data at distances greater than about 100°.

It is clear from Figure 4 that most of the events recorded lie within two azimuth ranges. A large number of events were recorded from the northwest of the array (azimuth range 290 to 330), and a slightly smaller number were recorded from the south (azimuth range 140° to 170°). In these two ranges of azimuth it has been possible to study the variation of $dT/d\Delta$ with distance, in some detail. Information is available at some other azimuths, but the coverage is much less complete.

It should be noted, too, that the earthquakes are not well distributed in azimuth. One of the interesting results of this study is that there are significant azimuthal variations in the observed quantities. However, the gaps in azimuthal coverage make it difficult to study these azimuthal variations in detail (see section 8).
Fig. 4: Distribution of events studied.
III. OBSERVATIONS OF $dT/d\Delta$  

In this section we show the raw $dT/d\Delta$ data, obtained as described above. The particular value plotted is the derivative resulting from the second degree polynomial fit (Figure 2b). It should be emphasized that none of these data have been corrected for source or array structure. The nature of these corrections will be considered later.  

In order to minimize the effects of the array, the data are presented in a series of azimuth ranges. The differences between these azimuth ranges are considered in section 3. Some comments are made on unusual features in each azimuth range.  

a. Azimuth Range 290-330 (Figures 5 and 6)  

This azimuth range contains the most complete coverage as a function of distance. The scatter of the data is, in general, quite small, of the order of 0.1 seconds/degree. In two regions, one between 33 and 38 degrees and one between 84 and 88 degrees, the scatter is significantly larger than this. As we shall see in sections 7 and 8, there are reasons for proposing that the first of these is the result of mantle structure, and the second is due to source effects. The interpretation of this azimuth range is taken up in detail in section 7.  

b. Azimuth Range 330-60 (Figures 7 and 8)  

The distribution of events in this azimuth range is much poorer than above. The data at distances beyond 75 degrees show little dependence on azimuth. They do, however, show a distinctly
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b. Azimuth Range 330-60 (Figures 7 and 8)

The distribution of events in this azimuth range is much poorer than above. The data at distances beyond 75 degrees show little dependence on azimuth. They do, however, show a distinctly
different behavior from those along the 290-330 direction. In the
distance range 43 to 50 degrees, events from an azimuth of 330-60
depart strongly from those at an azimuth of 20 to 60 degrees.
This may be the result of source structure, but the data are suf-
ficiently sparse that it is hard to investigate the problem further
at present.

c. Azimuth Range 60-130 (Figures 9 and 10)

These data too are quite sparse. This does seem to be a
significant difference between events at 110-130 and those at
60-110, in the distance range 45 to 60 degrees.

d. Azimuth Range 130-170 (Figures 11 and 12)

Good coverage is obtained in this azimuth range. Some of
the apparent scatter in this diagram may be due to errors in
epicentral location. The pronounced difference between the shape
of this curve and that for the azimuth range 290-330 is discussed
in section 8.

e. Azimuth Range 170-290 (Figures 13 and 14)

These events are very poorly distributed in distance.
IV. OBSERVATIONS OF $d^2T/d\Delta^2$

The second derivative of the travel time curve can easily be determined from the analysis outlined in section I, and is included in the printed output for each event (Figure 2b). This is easiest seen if the time $T_i$ at the ith station is related to the distance $S_i$ of the ith station from AO along the event azimuth by a Taylor expansion

$$T_i = T_0 + \left( \frac{dT}{d\Delta} \right) S_i + \frac{1}{2} \left( \frac{d^2T}{d\Delta^2} \right) S_i^2 + \ldots \quad (5)$$

Estimates of $\frac{d^2T}{d\Delta^2}$ may therefore be obtained from the coefficients $d$ and $f$ in equations 3 and 4.

This is the first time that an attempt has been made to directly measure the second derivative of the travel time curve using an array (Chinnery 1968a, 1968b). The results are shown, for the two principal azimuth ranges, in Figures 15-18.

It is clear that the scatter in these data is large, and this is primarily due to the timing accuracy. The absolute value of $d^2T/d\Delta^2$ is quite unreliable, since station corrections have not been applied, and because these corrections could not be estimated accurately enough anyway for the present purpose. However, there is one feature of interest in these curves, for in the vicinity of a cusp or triplication of the travel time curve the magnitude of the second derivative should become large. Some indication of possible cusps may be obtained at those distance ranges where the scatter of these graphs becomes large. These are noted below:
a. Azimuth Range 290-330 (Figures 15 and 16)

Unusually large or small values of $d^2T/d\Delta^2$ are noted in the distance ranges 26-27°, 36-37° (only two points), 60-65°, 68-69°, 75-76°, 86-90° and 96-97°. There is a high correlation between these anomalous regions and those selected on the basis of the $dT/d\Delta$ data (section 7). This suggests that there is some useful information in the $d^2T/d\Delta^2$ data, though the present scatter makes any interpretation of the second derivative data alone quite meaningless.

b. Azimuth Range 130-170 (Figures 17 and 18)

Anomalous distance ranges are 32-34°, 49-50°, 65-67° and 81-83°. The poor correlation of these with the 290-330 azimuth range is striking. We shall see later that the $dT/d\Delta$ data for these two azimuth ranges also show little correlation (section 8).
AZIMUTH RANGE
130 - 170

Fig. 17
V. OBSERVATIONS OF AZIMUTH ERROR

Two estimates of the azimuth to an event may be obtained. The "true" azimuth may be obtained from the published USCGS epicenter for each event. The error in this azimuth from its real value is likely to vary from place to place, and may contain systematic components which may create apparent variations with azimuth and/or distance. However, the error in the "true" azimuth is likely to be small. Most events should be located to within 1° or less of their true epicenters, and the corresponding error in azimuth should be much less than this.

A second estimate, the "observed" azimuth, may be obtained from the coefficients a and b in equation 1. The difference between the true and observed azimuths is a measure of the bending of the ray path out of the vertical plane containing the source and the array. However, where this bending occurs is harder to say. It may be due to source structure, a lateral variation in mantle structure, or local structure under the array.

Figure 19 shows the variation of true minus observed azimuth with distance for events to the Northwest of the array. Clearly there is a strong but apparently continuous variation of this quantity. The continuity suggests that the variation is not due to source structure, though this cannot be proved. The large errors for events at distances greater than 100° is very interesting, since these rays should traverse crustal structure almost vertically, and they should therefore be least affected by the crustal structure.
Figure 20 shows similar data from the Southeast events. The trend of the observations shows a marked similarity with Figure 19 in the distance range 50-90°, but is very different outside this range.

One possible reason for an azimuth error is crustal structure beneath the array. If this structure may be approximated by a dipping interface, the graph of azimuth error against azimuth should be a sine function (Niazi, 1966). Figures 21 and 22 show such graphs, for events in the distance ranges 20-55° and 75-95° respectively. No clear sinusoidal terms are apparent, and in fact there are significant differences between the two sets of data.

It has not proved possible, as yet, to interpret these observations of azimuth error.
VI. OBSERVATIONS OF TRAVEL-TIME ANOMALIES

There is no doubt that the relative arrival times of P-waves across LASA show a surprising complexity. Many studies (e.g., Chiburis, 1966) have confirmed this, and there is little doubt that this complexity is, at least in part, due to structure beneath the array. However, attempts to use this complexity to determine the structure have met with little success.

At least part of the reason for this lies in the problem of defining the nature of the travel time anomalies at each sub-array. There are two basic ways to define these anomalies. First, the arrival times at the sub-arrays can be compared with those predicted by a standard travel-time curve. Second, the arrivals themselves may be fitted with a straight line or a curve, and the residuals from the fit defined as travel time anomalies. Each of these definitions has advantages and disadvantages, and may be applied to the data in various ways. They are discussed below:

(i) Departure from Standard Travel Times.

If the distance of an earthquake from the array is known, then any standard travel-time table may be used to estimate the relative arrival times at the various sub-arrays. Many authors have used the Jeffreys-Bullen Tables for this purpose (e.g., Chiburis, 1966, Lincoln Laboratories Report LL-6, 1967, Greenfield and Sheppard, 1968). Other possibilities may include the Herrin Tables or any velocity model for the earth's interior, such as the model A of Chinnery (1969) (see section 7).
It would be nice if we could define the travel time anomaly at the $i$th station by

$$\Delta t_i = T_i^p - T_i^o$$

(6)

where $T_i^p$ is the predicted time and $T_i^o$ is the observed time. We cannot do this, of course, since (because of origin time errors) the absolute value of $T_i^o$ is not known. We are forced therefore to select some reference time against which to measure the $T_i^o$. The simplest way to do this is to choose the arrival at one sub-array as a reference, and write

$$\Delta t_i - \Delta t_o = (T_i^p - T_o^p) - (T_o^o - T_o^o)$$

(7)

The right hand side of this equation may be determined easily from the observations, and many authors have defined the "travel time anomaly" at the $i$th station as this quantity (Chiburis, 1966, Lincoln Laboratories Report LL-6, 1967, etc.). This definition may be satisfactory for calibrating the array, but is quite inadequate for studies of the crustal structure at the array, for two reasons.

In the first place, this definition includes only the difference between the structural contributions at the $i$th station and the reference station. This is particularly important if the station $AO$ is chosen as reference, since $AO$ is one of the more complex sites. Secondly, this definition of travel time anomaly attributes any difference between the standard model and
the true travel time curve to an effect at the sub-arrays. There is much evidence that any world-wide average travel time table may depart significantly from measurements along an individual profile on the earth's surface, and this is particularly true of the rather out-dated Jeffreys-Bullen Table. Each "travel time anomaly" will therefore be contaminated both by structure at the reference site and structure in the earth's interior.

The second of these problems can be minimized by using a set of travel times determined directly from the LASA data. As an example, Figure 23 shows the travel-time anomalies for sub-array Fl calculated using equation 7, with AO as a reference sub-array, and predicted travel time differences according to model A (Chinnery, 1969; section 7 of this report). The anomalies for events to the Northwest of the array are plotted as a function of epicentral distance, and show a strong variation with distance.

The contribution from AO can be reduced or removed by choosing some other reference for measuring time differences. If the arrival time at the ith station is $T_i$, referred to an arbitrary origin, then we may fit a curve to the data (as in equation 3) of the form

$$T_i - T_o + b \delta_i + c \delta_i^2 = 0$$  \hspace{1cm} (8)

where, as before, $\delta_i$ is the distance from AO along the azimuth to the event. $T_o$ may be determined from the least squares fit and used as a reference time. The travel time anomalies with
SUB ARRAY F1
AZIMUTH RANGE 290-330
RESIDUALS WITH RESPECT TO
EARTH MODEL A, USING
SUB ARRAY AO AS TIME REFERENCE
SUB ARRAY F1
AZIMUTH RANGE 290-330
RESIDUALS WITH RESPECT TO
EARTH MODEL A, USING T₀
AS TIME REFERENCE
respect to this reference for sub-array Fl and velocity model A are shown in Figure 24. There is a considerable difference between this graph and Figure 23. Presumably at least part of the AO contribution has been removed.

Both of the techniques mentioned above may be criticized. The reality of model A is still questionable, and determination of $T_o$ depends on all of the arrivals at the array and may be influenced by large-scale structure. However, these techniques should produce some improvement in the travel-time anomalies.

(ii) Residuals from Curve-Fitting.

Having fitted equation 8 to the data, the residuals at the sub-arrays may be regarded as travel-time anomalies. This definition of travel-time anomalies has the advantage that no assumptions about mantle structure are necessary. It has the same disadvantage as before, that the meaning of a fit such as this is not clear, and it may be influenced by large scale structure beneath the array.

Iyer and Healy (1971) proposed a similar definition for travel time anomalies, though they fitted a first degree equation (essentially equation 2). It turns out that there are only small differences between the 1st degree and 2nd degree residuals. Iyer and Healy then averaged the residuals from 9 events at various azimuths and distances, and used the variation of the average residual across the array to make conclusions about the crustal structure.
Since these residuals have not been studied in detail, the 2nd degree residuals for the 9 sub-arrays used in this study are shown in Figures 25-33. Clearly there are strong variations of the residuals with epicentral distance, at some of the sub-arrays. Similar complex variations occur as a function of azimuth. These variations are of the same order of magnitude as those found by Chiburis (1966), but have a different form since they are defined differently. The apparently small residuals at sub-arrays F2 and F4 are an inevitable result of any fitting process to events at this azimuth, since \( S_4 \) is largest for these sub-arrays. The magnitude of the variations throws some doubt on the averaging method of Iyer and Healy.

The 2nd degree residual for sub-array Fl (Figure 30) is very similar to the anomalies with respect to model A (Figures 24). This is hardly surprising, since model A was determined from the present data. However, this points out the underlying assumption of using least square residuals as travel time anomalies. A velocity structure very like model A is implied to be valid.

These residuals may be contoured across the array, in the same way that the authors mentioned have contoured travel time anomalies. Figure 34 shows an outline of the array, and Figures 35-38 show the mean residuals at distances of 40, 55, 70 and 90\(^\circ\), at the same scale. The contours, though schematic, have several interesting features. The values at 90\(^\circ\) indicate a Northeast-Southwest trend which is similar to the conclusions
of others (e.g., Greenfield and Sheppard, 1968). At closer distances there appears to be evidence for a superimposed Northwest-Southeast trend. The reality of this trend and its interpretation are not clear at present. However, the variation in the contours with distance is significant, and has been disregarded in previous studies.
SUB ARRAY E1
AZIMUTH RANGE 290-330
2ND DEGREE RESIDUALS
SUB ARRAY E2
AZIMUTH RANGE 290-330
2ND DEGREE RESIDUALS
SUB ARRAY E3
AZIMUTH RANGE 290-330
2ND DEGREE RESIDUALS
SUB ARRAY E4
AZIMUTH RANGE 290-330
2ND DEGREE RESIDUALS
SUB ARPAY F1
AZIMUTH RANGE 290-330
2ND DEGREE RESIDUALS
Fig. 34: ARRAY GEOMETRY, AT SAME SCALE AS FIGURES 35-38.
FIG. 35: CONTOURED 2ND DEGREE RESIDUALS (IN SECONDS) FOR EVENTS IN AZIMUTH RANGE 290-330, AT AN EPICENTRAL DISTANCE OF 40°. FOR SCALE SEE FIGURE 34.
FIG. 36: CONTOURED 2ND DEGREE RESIDUALS (IN SECONDS) FOR EVENTS IN AZIMUTH RANGE 290-330, AT AN EPICENTRAL DISTANCE OF 55°. FOR SCALE SEE FIGURE 34.
FIG. 37: CONTOURED 2ND DEGREE RESIDUALS (IN SECONDS) FOR EVENTS IN AZIMUTH RANGE 290-330, AT AN EPICENTRAL DISTANCE OF 70°. FOR SCALE SEE FIGURE 34.
Fig. 38: Contoured 2nd degree residuals (in seconds) for events in azimuth range 290-330, at an epicentral distance of 90°. For scale see Figure 34.
VII. INTERPRETATION OF $dT/d\Delta$ VERSUS DISTANCE (AZIMUTH RANGE 290-330)

An interpretation of the measurements of $dT/d\Delta$ shown in Figures 5 and 6, for the azimuth range 290-330, has been given in Chinnery (1969). The inferred velocity structures are shown in Figures 39-42. The velocity structures were obtained by a two-stage process. First, a curve was fitted visually to the $dT/d\Delta$ data, and then this was inverted into a velocity structure using the well-known Weichert-Herglotz technique. The resulting velocity structure was then used to recalculate $dT/d\Delta$ as a function of distance, and it is this curve that is shown through the data points. This technique largely overcomes any uniqueness problems in the Weichert-Herglotz method, except those introduced by scatter in the data. The additional data points shown in Figures 5 and 6 have not made any significant change to this interpretation.

There are several points about this interpretation that deserve consideration here, in the light of data obtained since the paper was published. First, some doubts were thrown on the interpretation because station corrections at the array were not included. The reason for this given in the paper was that the addition of station corrections will modify the shape of the curve of $dT/d\Delta$ against distance, and so change the travel time residuals of the curve with respect to the Jeffreys-Bullen table. (These residuals are simply the cumulative area between the two curves.) The nature of the modification will depend on the structure assumed in the calculation of the station corrections.
Fig. 39: (After Chinnery, 1969)
Fig. 40: (After Chinnery, 1969)
Fig. 41: (After Chinnery, 1969)
Fig. 42: (After Chinnery, 1969)
A simple dipping interface will raise or lower the observations with respect to the Jeffreys-Bullen curve. More complicated structures will distort the curve. However, the T-JB residuals of the uncorrected observations agree surprisingly well with the T-JB residuals at North American stations from the Longshot nuclear event, in the Aleutian Islands (Figure 43). The travel paths for this event were very similar to those involved in this study. It is therefore concluded that station corrections for the azimuth range 290-330° must be very small, and may to a first approximation be neglected.

More recently a number of other arrays have been used to determine $dT/d\Delta$. Figure 44 shows that results of Johnson (1969), who used the TFSO array, and Corblishley (1970), who combined the data from four arrays. Figure 45 shows the results obtained by Wright (1971) using the Warramunga array in Australia. Although none of these newer studies have the resolution (small scatter) and amount of data contained in Figures 5 and 6, the similarities between the results are striking. Again, this strongly argues that the data in the present study should not be distorted by the addition of station corrections.

Further evidence on this point is obtained from amplitude studies, since the amplitude of an arrival depends strongly on the second derivative $d^2T/d\Delta^2$. Figure 46 shows how the logarithm of the slope of the $dT/d\Delta$ graph varies with distance, compared with the amplitude observations of Carpenter et al. (1967), using an arbitrary zero. Again a remarkable agreement is seen.
Fig. 43: Travel time residuals with respect to the Jeffreys-Bullen Tables; above, observations of the LONGSHOT test, below, corresponding to models A and B in figures 39-42. (After Chinnery, 1969)
Fig. 44: Other observations of dT/dΔ; above, from Johnson (1969), below, from Corbishley (1970).
Fig. 45: Observations of $dT/d\Delta$ by Wright (1971).
Fig. 46: Comparison of the amplitude-distance measurements of Carpenter et al. (1967) with the logarithm of $d^2 T/dA^2$ for model B (figures 39-42) using an arbitrary origin.
We conclude that the smooth model A or the less smooth model B, shown in Figures 39-42, are reliable structures for the paths concerned in this study.

We may also return to our earlier comment that the scatter of the \( \frac{dT}{d\Delta} \) observations is unusually large in two distance ranges, 32-37° and 83-88°. The latter will be discussed in the next section. The former has become interesting because of a suggestion, by Wright (1968, 1971), that a triplication may occur in the vicinity of 35°, as the result of a low velocity layer in the mantle at a depth of about 850 km. Wright's \( \frac{dT}{d\Delta} \) data were obtained using the Warramunga array, and show a very similar structure to those in Figure 5 at this distance. It is very likely, therefore, that this effect is real. A possible interpretation of the present data, in terms of a low velocity layer, is shown in Figure 47. A variety of models are possible, since data in the vicinity of 35° is sparse, but the model AN shown is representative. Further studies of this feature are continuing.
Fig. 47: An alternative interpretation of the scatter of observations in the distance range 33-39°, suggested by the work of Wright (1968). The data points marked by open circles are less reliable than the rest.
VIII. AZIMUTHAL VARIATIONS

Having established an apparently self-consistent interpretation for the data from the azimuth range 290-330, it is natural to attempt the same process for data from other azimuths. It is at this point that the differences between the observations at different azimuths become most apparent.

Fairly complete information as a function of distance is available for events in the azimuth range 130-170 (Figures 11 and 12). In order to make a direct comparison with the 290-330 data, a visual fit to the data in Figures 11 and 12 is shown, together with model A (see previous section) and the Jeffreys-Bullen curve, in Figure 48. The differences between the two sets of data are extreme. This may be a common feature of array measurements; certainly similar differences were observed at the Warramunga array by Wright (1971), as is shown in Figure 49.

There are three possible ways in which these differences may occur; they may be due to crustal effects at the array, or to lateral variations in mantle structure, or to effects in the vicinity of the source (or, most likely, to some combination of all three). These possibilities are discussed separately below.

(i) Effects of Crustal Structure.

Crustal structure at the array must be a major contributor to the differences between the data from these two azimuth ranges. However, the separation of this contribution from the other two possibilities is not easy.
Fig. LE: Comparison of the data in the azimuth ranges 130-170 and 290-330; the Jeffreys-Bullen curve is also shown.
Fig. 49: Comparison of the data observed in two directions from the Warramunga array (after Wright, 1971).
If the paths from 130-170 traversed a simple dipping structure in the vicinity of the array, the $dT/d\Delta$ curve would be displaced parallel to the $dT/d\Delta$ axis. It is interesting to note that the curves from the two azimuth ranges are quite parallel in the distance range 30-55°, with the 130-170° data displaced upward by 0.5 seconds/degree. This is a substantial offset, and indicates a comparatively steeping dipping interface with considerable velocity contrast (Niazi, 1966).

The parallelism disappears at distances greater than about 55°, and it becomes much more difficult (though presumably not impossible) to relate the differences to a specific crustal model.

(ii) Lateral Variations in Mantle Structure.

The problem is compounded when these curves are studied in detail. There are a number of anomalous regions in the 290-330° curve that appear to be due to inhomogeneities in the mantle (Toksoz et al., 1967). None of these, including the feature shown in Figure 47, are apparent in the 130-170° data. This is supported by the $d^2T/d\Delta^2$ observations given in section 4 of this report. On the other hand, there is a variety of evidence to suggest that the interpretation of the 290-330° data is reasonable (see preceding section). We are therefore reluctantly led to the conclusion that the seismic paths from the South American earthquakes traverse a highly anomalous section of the mantle (Chinnery, 1967).
The degree of anomaly implied by these data is very large. The flattened portion of the 290-330 °dT/dΔ curve at about 70° suggests the presence of a phase transition at a depth of about 2000 km in the mantle (Chinnery, 1969b). The continuity of the 130-170 ° data in this region appears to preclude the presence of such a feature anywhere in the depth range 1500-2500 km. On the other hand, the data from the vicinity of Easter Island (azimuth range 170-200°, Figure 14) do appear to indicate the presence of this feature.

It is not clear whether lateral variations in deep mantle structure of this magnitude are permissible. Certain types of convective flow in the mantle might lead to variations like this, but the present data have sufficient ambiguity that they cannot prove the existence of such features. It is even possible that the presence of the phase transitions is obscured in the 130-170 ° data by a complex array structure, though this seems unlikely.

One is led to the following conclusions. If the interpretation of the 290-330 ° data is valid, then seismic rays from this direction see a very simple structure at the array (on the average). Then, the 130-170 ° data imply either an enormously complicated crustal structure at the array for paths from this azimuth, or major lateral variations in mantle velocity structure. Neither of the possibilities are very desirable. The only alternative is that the crustal structure at the array is so complex that a "noise" is added to the observations at all
azimuths. In this case it is surprising that the interpretation of the 290-330° data agrees so well with other studies.

(iii) Source Structure.

The possibility of contamination of $dT/d\Delta$ data by structure close to the source has received little attention in the past. This is not surprising, since the angular separation of the rays that will ultimately arrive at the extremes of the array is very small at the source (much less than 1° for any mantle structure). Only an extraordinary structure could introduce a significant time difference into two rays so close together. However, there is at least one instance in the present data where this appears to have occurred.

Figure 50 shows an enlarged view of the scattered data at distances of 80-90°, in the azimuth range 290-330° (Figure 6). The data have been studied carefully, and all doubtful information removed. At about 80° from the array, the distribution of earthquakes bifurcates at the well-known junction just south of Japan. The data marked by solid circles and triangles are from events in Southern Honshu, Kyushu, and the Ryukyu Islands. Those marked by open circles and triangles are from events in the Bonin and Mariana Islands. The $dT/d\Delta$ values from these two regions, at the same distance, differ by as much as 0.3 seconds/degree. Since the azimuths concerned are so similar, it is unlikely that this could be produced by array structure, and this is substantiated by the agreement between the sets of data at distances less than 80° and greater than 90°.
Fig. 50: Enlargement of a portion of figure 6.
At first sight, it is likely that this difference is the result of source structure. The azimuth to the array from events in the Ryukyu Islands is parallel to the oceanic trench. However, the azimuth to the array lies at a large angle to the island arc marked by the Bonin and Mariana Islands. However, on closer study, it is not easy to account for the observed differences in terms of normal island arc structures, for the dip of the Benioff zone is away from the direction toward the array. This means that the difference must arise either in the lithosphere (all the events are shallow, focal depths less than 100 km), or in the upper mantle on the ocean side of the downgoing slab. Since focal depth appears to have no significant influence on the measured value of dT/dA, it is not clear that the former possibility is reasonable. However, if mantle structure is the cause, large lateral variations in velocity are implied. Until more is known about the structure of the mantle in the vicinity of a downgoing slab, it does not seem possible to produce a consistent interpretation of these data.

It appears, then, that array structure, lateral variations in mantle structure, and source structure, may each at times contribute significantly to contamination of dT/dA measurements. There are severe problems in attempting to separate out anyone of the three for individual study.
CONCLUDING REMARKS

The data set that has resulted from this study consists of the following:

(i) P-wave arrival time information at the 9 subarrays described for the more than 3000 events studied. These are punched on one card for each event, and included are an event code, and the USCGS latitude, longitude and depth of the event.

(ii) A one page computer print-out, as shown in Figure 2b, for each event.

The following programs have been written in Fortran IV for the IBM 360 computer:

(i) EVENTS: a versatile program for the analysis of the travel time data, giving the output shown in Figure 2b.

(ii) TIMDIS: a program that will accept any velocity-depth model, interpolate between data points to improve continuity, and then calculate, for a given value of \( dT/d\Delta \), a variety of travel time information. This includes travel time, distance, depth of lowest point of ray path, residual from the Jeffreys-Bullen travel time table, the second derivative of the travel time curve, PcP times, etc.

(iii) WIEHER: a program for the inversion of \( dT/d\Delta \) data to obtain a velocity-depth model, using the Wiechert-Herglotz method.

The graphs shown in this report are only a small fraction of those that could be drawn using the existing information.
REFERENCES


1.

Department of Geological Sciences
Brown University
Providence, Rhode Island

Final Technical Report
August, 1971

Project: Seismology and Acoustic Gravity Waves
Period Ending: 31 July 1971
Contract No: F44620-68-C-0082
Amendment/Modification No: P002
ARPA Order No: 292-68, Amendment No. 49
Program Code No: SF10
Contractor: Brown University
Data of Contract: 1 August 1968
Amount of Contract: $123,108
Project Scientist: Michael A. Chinnery
401/863-3338
The results of research performed under this contract fall into the following categories:

1. **Task A: Investigations of F-wave Arrivals at LASA.**
   
   This research is discussed fully in the attached technical report.

2. **Task B: Research in Acoustic-Gravity Waves.**
   
   This research was carried out by Professor David G. Harkrider (now at California Institute of Technology). A final technical report of this research has been submitted separately.

3. **Research During the Period 8/1/70 to 7/31/71.**
   
   A no-cost extension of the contract was granted for the period 8/1/70 to 7/31/71, under Amendment/Modification No: P002. Research carried out during this period is described below. Much of this research is still in progress.
3. Research Under Amendment/Modification No. P002

This research has been concentrated on "Continuing Research Objective #4" (see original proposal, page 9), which is concerned with the residual displacements that accompany earthquake sources. Portions of this research are described in three technical papers (one in press, and two in the late stages of preparation).

Abstracts of these papers are given below:

1. On the Correlation between Earthquake Occurrence and Disturbances in the Path of the Rotation Pole, by M. A. Chinnery and F. J. Wells. (Given orally at the International Astronomical Union Symposium #48 on Rotation of the Earth, Morioka, Japan, May, 1971; paper will appear in the proceedings of the symposium.)

   The hypothesis that earthquakes may be the principal excitation of the Chandler motion of the rotation pole is examined in the light of recent theoretical and observational developments. There is some doubt about the amount of excitation by a large earthquake necessary to maintain the Chandler Wobble, but it appears to be about 10 feet. Theoretical calculations for the Alaskan Earthquake (M = 8½) give available excitations in the range 1-5 feet, but there are considerable uncertainties in these calculations. Earthquakes may be able to provide all of the required excitation, or only a small portion (10% or less). The problem is confused by observational studies, which show differences between
various sets of data on polar motion which seem to be larger than the expected error in each set. The earthquake hypothesis, though reasonable, is still very much open to debate.

2. The Inertia Changes due to Faulting in a Homogeneous Sphere, by M. A. Chinnery and J. R. Pice (manuscript, in late stages of preparation).

A very simple and elegant theory for the changes in the inertia tensor due to slip over an arbitrary surface inside a homogeneous sphere is presented. Full expressions are given for the case of a point slip source, for the inertia changes $\Delta I_{13}$, $\Delta I_{23}$ and $\Delta I_{33}$. These results are compared with those of Ben-Menahem and co-workers, and Dahlen.


The method of images is used to evaluate the displacement field due to a very long (2-dimensional) fault in two layers over a half space, with arbitrary rigidities. The model is used to investigate the effect on earthquake displacements of the lithosphere-asthenosphere boundary, the low velocity layer, and possible thin soft layers in the upper mantle. Each of these produce an amplification of the surface displacements over a uniform half-space.
model. It is shown that thin layers of soft material may effectively decouple earthquake displacements from the earth's interior.

Continuing Research

Continuing research, which will be reported later, and which will acknowledge the support received under this contract, is described below.

Considerations such as those contained in reference #3 above have strengthened our interest in the far displacement fields of earthquakes. It is likely that these fields may contain significant information about source mechanism and earth structure, including some information not readily available from seismic wave studies.

It is impossible, at present, to detect these fields directly. Strain step observations permit an indirect method of detection, but relatively few strain meters are available, and the observations of strain steps are contaminated to an unknown extent by local structure and instrumental effects.

Astronomical observations of latitude variation are one possible way to detect the total mass redistribution associated with these displacement fields. In particular, it has been suggested that

(i) The total displacement field of a large earthquake may be sufficient to cause a reasonable change in the moments of inertia of the earth, and so excite the Chandler Wobble.
(ii) This excitation may precede the occurrence of the earthquake by several days.

(iii) A natural corollary to these is that information about large-scale motions in the earth (apart from earthquakes) may be obtained from a detailed study of the path of the rotation pole.

We have therefore been led to examine, in some detail, the astronomical observations of the path of the rotation pole. It turns out that these observations are extremely complex, and are probably much less reliable than has been reported in the literature.

The most serious problem appears to be the separation of the free Eulerian motion of the earth (14 month period) from a variety of effects with a 12 month period. The latter include the forced motion of the earth due to atmospheric motions, together with a series of local effects (local meteorology, star catalogue errors, operator changes, etc.) that each contribute substantially (and with variable phase) to the 12 month component. The separation of these two terms is essential to any study of the excitation of the free motion by earthquakes. However, examination of the published techniques used to carry out the separation has shown that they are quite inadequate. This arises partly because of the small separation between the two spectral peaks, and partly because of the variability of amplitude and phase of the 12 month component.

Present investigations are concentrating on the statistical characteristics of these data, and the extent to which separation
is possible. This in turn will lead to a more complete understanding of the validity of the hypotheses mentioned above. It is not expected that definitive answers to these questions can be obtained from the presently available data. However, within a few years it is expected that satellite data will become available that will permit much more accurate (by an order of magnitude) determinations of pole position. This study is expected to lay the groundwork for the analysis of this new data.