APPLICATION OF A THEORY OF BINARY SOLUTION SURFACE TENSION TO INTERFACIAL TENSION PHENOMENA

By
Donald J. Cotton

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MATERIALS LABORATORY
RESEARCH AND DEVELOPMENT REPORT

July 1969
APPLICATION OF A THEORY OF BINARY SOLUTION SURFACE TENSION TO INTERFACIAL TENSION PHENOMENA

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ABSTRACT

A theoretical equation which describes interfacial tension of binary solutions as a function of concentration and of the interfacial tensions and the molecular areas of the pure components has been applied to organic and aqueous systems against water and mercury.

The derived equation gives information as to molecular area and orientation of adsorbed molecules at an interface. Gibbs' equation, while applicable to all interfaces, generates no detailed structural information. The derived equation is useful for determining the interfacial structure of solutions approximating its theoretical model.
ADMINISTRATIVE INFORMATION

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Dr. J. L. Shereshefsky, Department of Chemistry, Howard University, Washington, D. C., was co-author of the paper on which this report is based.
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NAVAL SHIP RESEARCH AND DEVELOPMENT LABORATORY

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INTRODUCTION

Liquid environments of naval machinery frequently contain dissolved polar molecules which either are deliberately incorporated to provide corrosion and wear resistance or are present as contamination. These polar molecules have a large effect upon the surfaces of immersed machinery. Therefore, it is of importance to the Navy to understand the surface properties of liquid systems.

It is the purpose of this report to show the relevance of a theory of surface tension of solutions by J. L. Shereshefsky to interfacial tension of solutions and to show its application to aqueous solutions of organic acids against mercury, binary organic mixtures against mercury, and binary mixtures against water. It is important to indicate that in these systems neither component of the solution phase is appreciably miscible with the other phase which forms the interface.

THEORETICAL CONSIDERATIONS

The equation which relates the interfacial tension with the concentration of the solution and which may be derived in a manner analogous to that of the surface tension is given by

$$\sigma = \sigma_{13} - \frac{\Delta \sigma \cdot X_{2b} \cdot e^{\Delta F_s/RT}}{1 - X_{2b} \cdot (e^{\Delta F_s/RT} - 1)} \ldots (1)$$

Designating the phase forming the interface with the solution with Subscript 3, and the solvent and solute with the customary Subscripts 1 and 2, respectively, $\sigma$ is the interfacial tension at mole fraction $X_{2b}$, and $\sigma_{13}$ is the tension in the interface.

Superscripts refer to similarly numbered entries in Appendix A.
between pure solvent and Phase 3. The terms \( \sigma_0 \) and \( \Delta F \), are defined by the expressions

\[
\sigma_0 = \sigma_{13} - \sigma_{23}
\]

......(2)

and

\[
\Delta F = \Delta \sigma_0 \frac{A_3}{t}
\]

......(3)

where \( \sigma_{23} \) is the tension between pure solute and Phase 3, \( A_3 \) is the area per mole of solute in a unimolecular layer, and \( t \) is the number of layers in the interface. It is seen that \( \Delta F \) represents the change in the free interfacial energy when a mole of solute of area, \( \frac{A_3}{t} \), and interfacial tension, \( \sigma_{23} \), displaces an equal are of interfacial tension, \( \sigma_{13} \).

The reciprocal form of Equation (1) which lends itself to easier application is given by

\[
\frac{X_{2\beta}}{\Delta \sigma} = \frac{1}{\Delta \sigma_0} e^{-\Delta F_s/RT} + \frac{X_{2\beta}}{\Delta \sigma_0} (1 - e^{-\Delta F_s/RT})
\]

......(4)

where \( \Delta \sigma \), the change in the interfacial tension, is given by

\[
\Delta \sigma = \sigma_{13} - \sigma
\]

......(5)

The constants, \( \Delta F_s \) and \( \Delta \sigma_0 \), of Equation (4) are evaluated from the slope, \( m \), and intercept, \( b \), with the aid of the expressions

\[
m/b = e^{\Delta F_s/RT} - 1
\]

......(6)

and

\[
m + b = 1/\Delta \sigma_0
\]

......(7)
TEST OF THE DERIVED EQUATION WITH INTERFACIAL TENSION DATA

The derived equation was tested with interfacial tension data in literature for solutions of dimethylaniline in heptane and in benzene, of hexanoic acid in benzene, and of decanol and octanol in benzene against water. A linear relationship was obtained for each data set (see Figures 1 and 2), and $\Delta \sigma_0$, $\Delta F$, and $A_s$ were calculated from a least square fit of the data. Results are summarized in Table 1.

Table 1
Surface Energy and Surface Area Constants of Several Binary Systems Against Water

<table>
<thead>
<tr>
<th>System</th>
<th>Figure</th>
<th>$\Delta \sigma_0$ (Obs)</th>
<th>$\Delta \sigma_0$ (Obs)</th>
<th>$\Delta F_s$ x $10^{-3}$</th>
<th>$A_s$</th>
<th>$A_s$ (Dens)</th>
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</thead>
<tbody>
<tr>
<td>Dimethylaniline-heptane/H$_2$O</td>
<td>1</td>
<td>22.0 (9.1)</td>
<td>24.8</td>
<td>58.95 (7.4)</td>
<td>31.8</td>
<td>35.4</td>
</tr>
<tr>
<td>Dimethylaniline-benzene/H$_2$O</td>
<td>1</td>
<td>7.6</td>
<td>9.1</td>
<td>20.8</td>
<td>37.7</td>
<td>35.4</td>
</tr>
<tr>
<td>Hexanoic acid-benzene H$_2$O</td>
<td>2</td>
<td>19.6</td>
<td>30.5</td>
<td>98.7</td>
<td>83.6</td>
<td>35.2</td>
</tr>
<tr>
<td>Octanoic acid-benzene H$_2$O</td>
<td>2</td>
<td>17.2</td>
<td>27.5</td>
<td>105.0</td>
<td>101.2</td>
<td>42.6</td>
</tr>
<tr>
<td>Decanol-benzene/H$_2$O</td>
<td>2</td>
<td>19.9</td>
<td>29.5</td>
<td>95.5</td>
<td>81.2</td>
<td>45.5</td>
</tr>
<tr>
<td>Octanol-benzene/H$_2$O</td>
<td>2</td>
<td>18.8</td>
<td>27.5</td>
<td>111.2</td>
<td>98.0</td>
<td>40.9</td>
</tr>
</tbody>
</table>

Obs - Observed Dens - Density

Interfacial tensions were measured between mercury and aqueous solutions of butanoic, isobutanoic, pentanoic, hexanoic, and heptanoic acid and solutions of nitro-benzene in heptane and benzene.

A capillary rise method described by Bartell and Miller was used to determine the interfacial tensions between mercury and the solutions of interest. A diagram of the apparatus with approximate dimensions appears in Figure 3. Two such apparatuses made entirely of Pyrex glass were used simultaneously for each interfacial tension measurement. Equation (8) was used to obtain interfacial tensions between mercury and the solutions without determining solution density.

*Abbreviations used in this text are from the GPO Style Manual, 1967, unless otherwise noted.
\[ \tau_{ij} = \left( r_{ij} \rho_{ij} / 2 \right) \left( h_{ij} h_{ij} - h_{ij} h_{ij} \right) / \left( r_{ij} h_{ij} - r_{ij} h_{ij} \right) \]

where

- \( \tau_{ij} \) = interfacial tension between Phases i and j
- \( \rho_i \) = density of i-th phase
- \( r_{ij} \) = radius of m-th apparatus
- \( g \) = gravitation constant
- \( h_{ij} \) = height of i-th phase in m-th apparatus.

Equation (8) was obtained by solving simultaneously the equations, described by Equation (9), which resulted from making measurements with the same solutions in different apparatuses.

\[ \tau_{ij} = \left( r_{ij} g / 2 \right) \left( h_{ij} \rho_i - h_{ij} \rho_i \right) \]

The radii of the capillaries were determined by an optical method using a microscope equipped with a movable stage, a filar screw micrometer eyepiece of 6X magnification, and an objective of 10X magnification. The eyepiece micrometer was calibrated against a precision stage micrometer. With the optics described, 1-scale division was equivalent to 0.388 mm, and the eyepiece micrometer could be read to 0.001 scale division. Consequently, maximum precision was 0.388 micron.

The radii were measured at intervals along the length of the capillary. Equation (10) was used to correct for magnification by the cylindrical walls of the capillary:

\[ r = R / n \]

where

- \( r \) = actual radius
- \( R \) = apparent radius
- \( n \) = index of refraction of the walls of the capillary.
Solutions, made by weight, were introduced into the higher reservoir of each apparatus, and pure mercury was placed into the other. The apparatus was placed into a constant temperature water bath at 25°C, maintained to within ±0.01°C. After the stopcock had been opened, the solution was allowed to come to equilibrium for 1 hour before meniscus and reservoir heights were measured with a cathetometer to within ±0.001 centimeter.

Doubly demineralized water was used to make all aqueous solutions. All organic compounds used were Eastman Kodak chromography grade chemicals. The mercury was allowed to drop from a capillary through a 1 meter long 10% nitric-acid column and then double distilled under vacuum for purification.

Interfacial tensions were calculated from the meniscus and reservoir heights data by applying Equation (8). The value of 375 erg per cm² for the interfacial tensions of water against mercury at 25°C, obtained by Bartell and coworkers, was used to obtain the difference between the interfacial tensions of the solutions and pure water. Interfacial tension differences were then used in the derived equation to calculate \( \Delta \sigma_0 \), \( \Delta \sigma_e \), and \( \Delta A \) with the derived equation. The data are summarized in Figures 4 through 6.

**DISCUSSION OF RESULTS**

In reference to Table 1, the deviations of \( \Delta \sigma_0 \) from \( \Delta \sigma_0 \) (observed) apparently reflect the degree of orientation of solute molecules in the surface region; the deviations of \( \Delta A \) from \( \Delta A \) (density) support this conclusion. Dimethylaniline molecules in benzene against water either change their orientation or their packing density in the surface region at higher concentrations, which is evidenced by the existence of different linear relationships in different concentration regions. Consequently, two different values for \( \Delta \sigma_0 \) and \( \Delta \sigma_e \), and \( \Delta A \) were obtained for this system. In Table 1, the values in parentheses were obtained in the region of higher concentration; \( \Delta \sigma_0 \) in this region is the same as \( \Delta \sigma_0 \) (observed) which indicated little orientation, and the small magnitude of \( \Delta \sigma_e \) supports this conclusion. However, \( \Delta A \), which is approximately one-third the molecular surface area obtained in the dilute region, suggests that the surface layer is three molecules thick in the concentrated region.

The experimental molecular areas for hexanoic and octanoic acid- and those of decanol and octanol imply that these molecules are oriented with their long axes parallel to the interface. The difference between the molecular surface area of hexanoic and octanoic acids is 17.6 Å², and of decanol and octanol is 16.8 Å².
Since the molecular surface area of the members of each pair, oriented with major axis parallel the surface, differ by the surface area of two methylene groups, the average molecular area of a methylene group is determined as 8.6Å².

The progressive increase in molecular surface area, \( A_2 \), for butanoic, pentanoic, hexanoic, and heptanoic acids, obtained by interfacial tension against mercury measurements (see Table 2), suggests that these molecules were also oriented with their long axes parallel to the surface. When the molecular area per molecule was plotted versus the number of methylene or methyl groups in the molecule, a straight line resulted (see Figure 7) the slope of which was equal to 9.2Å² per group, and the intercept of which was equal to 28Å². The slope is equivalent to the surface area of a methylene or methyl group, and the intercept is equivalent to the surface area of a carboxyl group. This molecular area, 9.2Å², obtained for a methylene group in a straight chain hydrocarbon oriented with its long axis parallel to a mercury surface, is close to that obtained for similar hydrocarbons similarly oriented toward a water surface. These results demonstrate how the derived equation can be used to ascertain the size, shape, and orientation of molecules at an interface by interfacial tension measurements.

Table 2
Interfacial Energy and Area Constants
For Several Aqueous Solutions Against Mercury

<table>
<thead>
<tr>
<th>Solute</th>
<th>( \sigma_0 ) erg/cm²</th>
<th>( \Delta F \times 10^{-4} ) erg/mole</th>
<th>( A_2 ) Å²</th>
<th>( A_3 ) Å³</th>
</tr>
</thead>
<tbody>
<tr>
<td>Butanoic</td>
<td>24.6</td>
<td>82.4</td>
<td>55.7</td>
<td>28.9</td>
</tr>
<tr>
<td>Pentanoic</td>
<td>24.7</td>
<td>96.8</td>
<td>65.1</td>
<td>32.1</td>
</tr>
<tr>
<td>Hexanoic</td>
<td>24.6</td>
<td>109.8</td>
<td>74.1</td>
<td>35.5</td>
</tr>
<tr>
<td>Heptanoic</td>
<td>10.8</td>
<td>58.6</td>
<td>90.7</td>
<td>38.8</td>
</tr>
<tr>
<td>Isobutanoic</td>
<td>23.0</td>
<td>90.5</td>
<td>65.3</td>
<td>28.9</td>
</tr>
</tbody>
</table>

In Table 3, \( \sigma_0 \) is less than \( \sigma_0 \) (observed) for nitrobenzene dissolved in heptane, and \( \Delta \sigma_0 \) (calculated) approached \( \sigma_0 \) (observed) for nitrobenzene dissolved in benzene.
Table 3
Interfacial Energy and Area Constants
For Nitrobenzene Solutions Against Mercury

<table>
<thead>
<tr>
<th>Solvent</th>
<th>$\omega_0$ (Observed)</th>
<th>$\Delta F \times 10^{-8}$</th>
<th>$A_1$ (Density)</th>
<th>$A_2$ (Density)</th>
<th>t</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heptane</td>
<td>16.4</td>
<td>22.5</td>
<td>22.8</td>
<td>30.8</td>
<td>2</td>
</tr>
<tr>
<td>Benzene</td>
<td>9.6</td>
<td>20.5</td>
<td>45.8</td>
<td>30.8</td>
<td>1</td>
</tr>
</tbody>
</table>

This implies that there is a greater change in surface energy, due to orientation at the interface, for the heptane than for the benzene solution. It is reasonable to assume that the orientation of the nitrobenzene molecule in the interface is predominantly influenced by the mercury phase. From this follows that the area of the molecule in the heptane-mercury interface should be the same as in the benzene-mercury interface. This condition is obtained when $t$ for the heptane-mercury interface is equal to 2, and for the benzene-mercury interface is equal to unity. The area per molecule, namely, $45.6 \AA^2$, thus obtained corresponds approximately to the area of the benzene molecule ($41 \AA^2$) when oriented parallel to the surface. The different thicknesses of the interfacial region are very likely due to the different miscibilities of nitrobenzene in heptane and benzene, the thickness being favored by lower miscibility.

CONCLUSIONS

It has been shown how the derived equation can be employed to generate information as to molecular area and orientation of adsorbed molecules at an interface. Consequently, the derived equation can be a powerful aid in further understanding the interaction of polar molecules at the surfaces of naval machinery. Predictions, for example, can be reliably made as to the behavior of additive molecules in a lubricant medium in which naval machinery is immersed.
Figure 1
Mole Fraction, Divided by \( \Delta \sigma \) Versus Mole Fraction for Solutions of Dimethylaniline in Heptane and in Benzene at 25\(^\circ\) C Against Water

MATLAB 333
Figure 2
Mole Fraction Divided by $\Delta \sigma \times 10^2$, cm$^2$/ERG Versus Mole Fraction for Solutions of Some Organic Compounds in Benzene at 20°C Against Water

- **DECANOL**
- **OCTANOL**
- **HEXANOIC ACID**
- **OCTANOIC ACID**
Figure 3
Interfacial Tension Apparatus
Figure 4
Mole Fraction Divided by \(\Delta\) Versus Mole Fraction for
Aqueous Solutions of Isobutanoic, Butanoic, and
Pentanoic Acid Against Mercury at 25\(^\circ\) C
Figure 5
Mole Fraction Divided by \( \Delta \sigma \times 10^{-4} \), CM\(^2/\text{erg} \) Versus Mole Fraction for Aqueous Solutions of Hexanoic and of Heptanoic Acid Against Mercury at 25° C

MATLAB 333
Figure 6
Mole Fraction Divided by $\Delta \sigma$ Versus Mole Fraction For Solutions of Nitrobenzene in Benzene and in Heptane Against Mercury at 25°C
Figure 7
Molecular Area Versus Number of Methylene Groups per Molecule
for a Homologous Series of Straight Chain Acids at 25° C
Appendix A

Technical References

A theoretical equation which describes interfacial tension of binary solutions as a function of concentration, and of the interfacial tensions and the molecular areas of the pure components has been applied to organic and aqueous systems against water and mercury. The derived equation gives information as to molecular area and orientation of adsorbed molecules at an interface. Gibbs' equation, while applicable to all interfaces, generates no detailed structural information. The derived equation is useful for determining the interfacial structure of solutions approximating its theoretical model.
<table>
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