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AN EXPERIMENTAL EVALUATION OF THE CONFORMAL GEAR

By

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February 1966

U. S. ARMY AVIATION MATERIEL LABORATORIES
FORT EUSTIS, VIRGINIA

CONTRACT DA 44-177-AMC-101(T)
VERTOL DIVISION
THE BOEING COMPANY
MORTON, PENNSYLVANIA

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This report represents a part of a continuing research program for investigations of advanced gear design criteria. The main efforts of this program are directed toward dynamic load tests of specimen conformal contact gearing (Wildhaber-Novikov gear tooth form).

This command concurs with the contractor's conclusions reported herein. The results obtained from this specific study indicate that further research investigations must be conducted before a complete evaluation of conformal contact gearing for aircraft application can be made.

This command concurs with the contractor's recommendations, and the continuing program is scheduled on this basis.
AN EXPERIMENTAL EVALUATION
OF THE CONFORMAL GEAR
R-429A

by
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Fort Eustis, Virginia

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SUMMARY

This report concludes Phase II of a study on a new or improved concept of power transmission conducted by the Vertol Division of Boeing under Contract DA 44-177-AMC-101(T) modification 1. The study was initiated upon receipt of the contract modification on 17 June 1964.

Phase II comprised design, fabrication, and load testing of one form of the conformal gear geometry. The gears were hardened and ground in accordance with aircraft gear technology. Capacity was determined by a programmed increase in load until failure was attained. Condition of the gears at the end of testing indicated corrective approaches for increased load-carrying capacity. Measurements of tooth bending strains were made to analyze the effects of conformal gear contact as the load zone passes across the gear face.
FOREWORD

Acknowledgment is made to the following organizations for their assistance and contributions in fabrication and inspection of the conformal gears during this program:

Automation Gages, Inc., Rochester, New York
Fellows Gear Shaper Co., Springfield, Vermont
Michigan Tool Division of Excello Corp., Detroit, Michigan
National Broach and Machine Co., Detroit, Michigan
Steel Products Division of Kelsey Hayes, Springfield, Ohio
ILLUSTRATIONS

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Conformal Gear in Mesh</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>Involute Gear Contact Capacity</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>Equivalent Radius vs Gear Ratio</td>
<td>7</td>
</tr>
<tr>
<td>4</td>
<td>Moment Factor vs Contact Ratio</td>
<td>9</td>
</tr>
<tr>
<td>5</td>
<td>Drawing SK13264</td>
<td>15</td>
</tr>
<tr>
<td>6</td>
<td>Tooth Thickness vs Helix Angle</td>
<td>17</td>
</tr>
<tr>
<td>7</td>
<td>Conformal Pinion Hob</td>
<td>20</td>
</tr>
<tr>
<td>8</td>
<td>Comparator and Chart</td>
<td>22</td>
</tr>
<tr>
<td>9</td>
<td>Coordinate Tracer Schematic</td>
<td>23</td>
</tr>
<tr>
<td>10</td>
<td>Patterns of Dummy Pinion and Gear at Various Center Distances</td>
<td>25</td>
</tr>
<tr>
<td>11</td>
<td>Gear Research Test Stand</td>
<td>27</td>
</tr>
<tr>
<td>12</td>
<td>Test Arrangement</td>
<td>29</td>
</tr>
<tr>
<td>13</td>
<td>Conformal Gear Stress Levels</td>
<td>33</td>
</tr>
<tr>
<td>14</td>
<td>Tooth Patterns During Load Test (Sheet 1, 2, 3, 4, and 5)</td>
<td>34</td>
</tr>
<tr>
<td>15</td>
<td>Gear Condition After Final Run, Gear Set Number 2</td>
<td>41</td>
</tr>
<tr>
<td>16</td>
<td>Pinion Condition After Final Run, Gear Set Number 2</td>
<td>42</td>
</tr>
<tr>
<td>17</td>
<td>Condition of Gear Set Number 2</td>
<td>43</td>
</tr>
<tr>
<td>18</td>
<td>Instrumented Pinion Showing Gage Numbers</td>
<td>46</td>
</tr>
<tr>
<td>Figure</td>
<td>Description</td>
<td>Page</td>
</tr>
<tr>
<td>--------</td>
<td>------------------------------------------------------</td>
<td>------</td>
</tr>
<tr>
<td>19</td>
<td>Oscillograph Record of Strain Gage Data</td>
<td>49</td>
</tr>
<tr>
<td>20</td>
<td>Load Overlapping Effect</td>
<td>56</td>
</tr>
<tr>
<td>21</td>
<td>Maximum Strain Readings</td>
<td>58</td>
</tr>
<tr>
<td>22</td>
<td>Involute Curve Construction</td>
<td>66</td>
</tr>
<tr>
<td>23</td>
<td>Master Profile Curve</td>
<td>67</td>
</tr>
<tr>
<td>SYMBOLS</td>
<td>Description</td>
<td></td>
</tr>
<tr>
<td>----------------------------------------------</td>
<td>-----------------------------------------------------------------------------</td>
<td></td>
</tr>
<tr>
<td>b</td>
<td>Half-length of axial contact</td>
<td></td>
</tr>
<tr>
<td>2b</td>
<td>Length of axial contact</td>
<td></td>
</tr>
<tr>
<td>$\beta$</td>
<td>Helix angle</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Diameter</td>
<td></td>
</tr>
<tr>
<td>$D_p$</td>
<td>Diametral pitch</td>
<td></td>
</tr>
<tr>
<td>$\Delta$</td>
<td>Deviation of circular arc profile from master involute curve</td>
<td></td>
</tr>
<tr>
<td>E</td>
<td>Young's modulus</td>
<td></td>
</tr>
<tr>
<td>$E^0$</td>
<td>Roll angle in degrees to selected point on master involute</td>
<td></td>
</tr>
<tr>
<td>$\bar{E}$</td>
<td>Roll angle in radians</td>
<td></td>
</tr>
<tr>
<td>$E^0_{SAP}$</td>
<td>Roll angle in degrees to start of active profile</td>
<td></td>
</tr>
<tr>
<td>F</td>
<td>Width of face</td>
<td></td>
</tr>
<tr>
<td>$\theta$</td>
<td>Intermediate angle to derive a pressure angle</td>
<td></td>
</tr>
<tr>
<td>i</td>
<td>Reduction ratio</td>
<td></td>
</tr>
<tr>
<td>$K_i$</td>
<td>Moment correction factor</td>
<td></td>
</tr>
<tr>
<td>$K_s$</td>
<td>Stress concentration factor</td>
<td></td>
</tr>
<tr>
<td>$L$</td>
<td>Height of face in transverse plane</td>
<td></td>
</tr>
<tr>
<td>$L_N$</td>
<td>Height of face in normal plane</td>
<td></td>
</tr>
<tr>
<td>OD</td>
<td>Outside diameter</td>
<td></td>
</tr>
<tr>
<td>P</td>
<td>Tangential load in transverse plane (Torque/Pitch radius)</td>
<td></td>
</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
<td></td>
</tr>
<tr>
<td>--------</td>
<td>-------------</td>
<td></td>
</tr>
<tr>
<td>$P_N$</td>
<td>Tangential load in normal plane</td>
<td></td>
</tr>
<tr>
<td>$\phi$</td>
<td>Pressure angle</td>
<td></td>
</tr>
<tr>
<td>$\phi_N$</td>
<td>Pressure angle in normal plane</td>
<td></td>
</tr>
<tr>
<td>$R$</td>
<td>Pinion pitch radius</td>
<td></td>
</tr>
<tr>
<td>$R_b$</td>
<td>Radius of master base circle</td>
<td></td>
</tr>
<tr>
<td>$R_{b1}$</td>
<td>Trial radius of master base circle</td>
<td></td>
</tr>
<tr>
<td>$R_c$</td>
<td>Rockwell hardness</td>
<td></td>
</tr>
<tr>
<td>$R_E$</td>
<td>Equivalent radius of curvature</td>
<td></td>
</tr>
<tr>
<td>$R_m$</td>
<td>Mean radius from outside diameter to start of active profile</td>
<td></td>
</tr>
<tr>
<td>$R_o$</td>
<td>Radius to outside diameter</td>
<td></td>
</tr>
<tr>
<td>$R_{SAP}$</td>
<td>Radius to start of active profile</td>
<td></td>
</tr>
<tr>
<td>$R_1$</td>
<td>Radius to center of conformal tooth profile arc</td>
<td></td>
</tr>
<tr>
<td>$r$</td>
<td>Radius of tooth profile</td>
<td></td>
</tr>
<tr>
<td>$r_1$</td>
<td>Trial radius of tooth profile</td>
<td></td>
</tr>
<tr>
<td>$\rho_p$</td>
<td>Radius of involute pinion tooth profile at selected point</td>
<td></td>
</tr>
<tr>
<td>$\rho_g$</td>
<td>Radius of involute gear tooth profile at selected point</td>
<td></td>
</tr>
<tr>
<td>$S_b$</td>
<td>Bending stress</td>
<td></td>
</tr>
<tr>
<td>$S_c$</td>
<td>Contact stress</td>
<td></td>
</tr>
<tr>
<td>$T_N$</td>
<td>Tooth thickness in normal plane</td>
<td></td>
</tr>
<tr>
<td>$T_{N1}$</td>
<td>Tooth thickness (critical section) in normal plane</td>
<td></td>
</tr>
</tbody>
</table>
Thickness of pinion tooth

Thickness of gear tooth
INTRODUCTION

The need for a power transmission system to match the speed, size, and weight of the gas turbine prompted the Army's funding of Contract DA 44-177-AMC-101(T).

Initial investigations of power transmission indicated that, to obtain the minimum specific weight for the system, the engine rpm should be reduced at the rotor. This requires a high-ratio, high-efficiency reduction mechanism. With this in mind, a study of the conformal contact (Wildhaber-Novikov) gear tooth form was initiated to appraise its potential for aircraft applications. Phase I was devoted to the formulation of analytic method, a photoelastic investigation, and a parametric design study. Detail design, fabrication, and dynamic load testing to failure were performed in Phase II either to verify the analysis established in Phase I or to obtain enough data to modify it.

The conformal contact gear tooth form was first described by Ernest Wildhaber in a United States patent filed in 1923 and issued October 5, 1926. His patent contains every essential feature of the conformal contact gear being investigated today. Wildhaber describes circular arc profiles in both normal and transverse planes, and also the differences between concave and convex profiles to allow change in center distances.* Convex and concave surfaces on mating teeth create a band of contact which spreads to area contact under load. The contact runs axially along the face as the mating gears revolve (see Figure 1). By comparison to involute teeth, the conformal shape is not conjugate in the plane of rotation. For constant velocity transmission, the gear is made helical. To operate without interruption, the gear teeth must have axial overlap; that is, the face width must be wide enough to include at least one pitch, and preferably more.

*This last modification is generally credited to M. L. Novikov, who received a USSR Patent in 1956. The chief value of Novikov's work was to revive interest in the gear form. As has frequently happened, the necessity (in this instance, a requirement for high-duty V/STOL transmissions) came long after the invention.
The particular advantage of the conformal gear is that the two functions of gearing -- transmitting both load and uniform angular motion -- are separate and distinct. The motion-carrying function is entirely axial so that the tooth can have the profile best suited to contact capacity and strength. By contrast, the involute gear is restricted to a conjugate geometry (see Figure 2) which prevents an increase in contact capacity by changing tooth size (diametral pitch). Increases in contact capacity must be obtained by improved ability to withstand high stresses, by case carburizing, for example, rather than by changing tooth form.

Material improvements can be applied to the conformal gear as well. The conformal gear can benefit from the hardened surfaces and ductile core common to modern aircraft involute gearing, and the extent of benefit is consistent with involute-gear experience.

The analysis indicated that the hardened and ground conformal gear required a face-to-diameter ratio of 0.75 or more to realize load-carrying advantage over the involute gear. However, the test gears had a lesser, and entirely practical, face-to-diameter ratio (one-half), yet their load-carrying capacity was found comparable to involutes of similar size and weight. It is important to note that parity was achieved at an early stage of conformal technology, and despite major problems. The capacity of a developed conformal gear should therefore be considerably greater than that indicated by the analysis.
The conformal-contact gear transmits constant angular velocity by successive contacts across the gear face. Each tooth contacts once during a full revolution. Sliding in the profile plane does not theoretically occur. The mating profiles can therefore be designed to conform and thus reduce contact stress as compared to the involute form.

Figure 1. Conformal Gear in Mesh
Contact stress is given by:

$$K = \frac{\sqrt{\text{Tooth Load}}}{\text{Face} \times \cos \phi} \frac{\rho_G + \rho_P}{\rho_G \times \rho_P}$$

- $\rho_p$ and $\rho_G$ are invariable for a given pitch diameter and pressure angle $\phi$. Therefore, contact capacity varies as $\sqrt{\text{Face}}$.

- The effect of face increase is not significant within practical limits.

- Significant increase in contact capacity requires enlargement of diameters.

Figure 2. Involute Gear Contact Capacity
CONCLUSIONS

1. The conformal test gears demonstrated load-carrying ability equivalent to that expected of aircraft involute gears.

2. Load capacity can be increased by modifications in the conformal tooth to distribute load better.

3. Gearing with increased load capacity will improve upon the power-to-weight ratio predicted by the original analytical estimate.

4. Contact stresses at the failure load level correlated with the analytical method developed in Phase I.

5. Inspection techniques and equipment must be developed in parallel with the conformal tooth form.

RECOMMENDATIONS

1. Establish methods and procedures to measure and inspect more accurately the conformal tooth form along the entire face width.

2. Modify the conformal tooth form as indicated by the results of this program. Increase load capacity by eliminating tip interference and by modifying helix angle.

3. Determine the load-carrying capacity of the modified conformal gears.
ANALYSIS OF PROBLEM

The analytical method used to design the test gears was developed in Phase I of the study. This method, like those used in involute gear design, considers beam bending and surface contact stresses.

As in all gear analysis, the stress values obtained are index numbers. Allowable stresses must be empirically determined. The first approach toward this has been made in the testing conducted under this program.

Analysis of the conformal gear is complicated by the allowable latitude of profile shape and profile conformity. The analysis now considers only the circular arc profile with full conformity between concave and convex teeth. Nevertheless, it has proven useful for estimation of load-carrying capacity of the test gear set. The analytical method is described below.

BENDING STRESS

The tooth bending stress depends upon the tooth load and upon the distribution of that load. In the profile plane, the conformal contact system produces a line load perpendicular to the axis when the radii match, and a point load when the radii differ. In the axial plane, the curves of the helixes oppose and produce a point loading. Therefore, when elastic deformation is neglected, the area of loading is normally a point.

Using the Hertz equations for bodies in contact, the area of loading can be determined for a practical case where deformation exists. The two radii of the contact body are calculated, and then the equivalent radius of a curved body in contact with a plane is determined. The equivalent radius depends on the helix angle, the ratio, the size of gear, and the height of the tooth (see Figure 3). From the equivalent radius, the band width of contact axially along the tooth face is obtained.
Figure 3. Equivalent Radius vs Gear Ratio
To relate area of loading to stress at the tooth root, the Wellauer-Seireg paper* was applied. This paper deals with the stress distribution at the base of a cantilever plate. A plate is differentiated in this case from a beam, in that the load is not uniform along its length (spanwise) and in that its aspect ratio is 4 to 1 or more. A concentrated load produces a moment distribution curve of a specific shape along the fixed edge. This shape has been determined analytically and verified experimentally.

With the conformal gear, the problem is to determine the moment intensity under load patterns which extend for various spanwise distances, and in which the load distribution is assumed to be elliptical. The load span is dependent upon the mating radii of the gear and also upon the load deformation. A given gear set will enlarge its loading band as the tangential load is increased. The effect is a nonproportional increase in root bending, nonproportional because as the load is increased it diffuses further into the hitherto unstressed root area.

A correction factor for bending stress (Ki) was obtained and plotted (Figure 4). It can be seen that as contact band-to-total-face-width ratio increases, the correction factor and the bending stress decrease. From a concentrated load to a full-width load, the expected change in bending stress is 3 to 1. However, the majority of study examples had load-width-to-total-width ratios of about one quarter.

The bending stress equation also includes Ks, the stress concentration factor. A conventional equation which accounts for various beam proportions and root radii was used initially. The photoelastic technique was used with varying root shapes to further determine Ks. The results of the photoelastic method agree generally with the analytical factor.

To complete the bending stress determination, the radial compressive stress was calculated. This is caused by the tangential tooth load's acting upon the inclined tooth face. The effective area was assumed as the band width having the same elliptical distribution as previously. Acting as a

bending moment relief, this radial component adds to the stress on the compression side of the beam and subtracts from the tension side. Its effect is therefore beneficial, since tooth fatigue failure occurs on the tension side because of the characteristic lower endurance limit.

**CONTACT STRESS**

The contact stress assumes the same elliptical load distribution over the band of contact. The other axis of the contact area is assumed as the normal height of the tooth profile. This full conformity will not actually pertain, particularly at partial load, but less than full conformity will increase the elastic deformation in the spanwise (axial) direction and increase the length of the band of contact, so the assumption is realistic enough to be useful.

The influence of the tooth geometric variables upon the bending and contact stress levels was considered. It was apparent that the relationship between bending and contact stresses depends upon tooth thickness for beam strength and upon tooth profile radius and helix angle for area of contact. The balance of tooth bending and contact stresses is an important step in optimizing the gear. Detail studies in which one variable was changed to determine the stresses showed that beam strength was the limiting factor. The conformal gear's contact capacity was believed to be superior to its bending capacity, unless the gear tooth is thickened to extremes by normal involute standards.

The following equations were used in this study to obtain bending and contact stresses:

**To Find Normal Load:**

\[
P_N = \frac{p}{\cos \phi} \sqrt{1 + \cos^2 \phi \tan^2 \beta}
\]

Where

- \( P_N \) is load normal to face
- \( P \) is tangential load = \( \frac{\text{Torsque}}{\text{Pitch Radius}} \)
\( \phi \) is pressure angle

\( \beta \) is helix angle

**To Find Height of Contact Band:**

\[
L = 2 \sin \phi \cdot r
\]

\[
L_N = \frac{L \sin \phi}{\sin \phi_N}
\]

\[
\tan \phi_N = \tan \phi \cos \beta
\]

Where \( L \) is height of face in transverse plane

\( L_N \) is height of face in normal plane

\( \phi_N \) is normal pressure angle

\( r \) is radius of tooth profile

**To Find Length of Axial Contact Band:**

\[
2b = 2.15 \sqrt{\frac{2 P_N R_E}{E L_N}}
\]

Where \( 2b \) is length of band

\( R_E \) is equivalent radius (see Figure 3)

\( E \) is Young's modulus

**To Find Bending Stress:**

\[
S_b = \frac{6 K_i K_c P_N \cos \phi_N}{(T_N^1)^2} - \frac{P_N \sin \phi_N}{2T_N^1 b}
\]

Where \( S_b \) is bending stress at tension fillet

\( K_i \) is correction factor (see Figure 3)

\( K_S \) is concentration factor

\( T_N^1 \) is critical section in normal plane

\( b \) is half length of axial contact band
To Find Contact Stress:

\[ T_c = \frac{4}{\pi} \frac{P_N}{2b L_N} \]

To Determine Diametral Pitch:

\[ D_p = \frac{\text{overlap} \times \pi}{\text{Face} \times \tan \beta} \]

To Determine Pinion Thickness:

\[ T_1 = \left( \frac{T_1}{T_2} \times \frac{\pi}{D_p} \right) - \text{Backlash} \]

Where

\[ T_1 \] is pinion tooth thickness
\[ T_2 \] is gear tooth thickness
\[ D_p \] is diametral pitch
DESIGN OF TEST ITEM

DESIGN

The four test gears used in this program were manufactured by the Steel Products Engineering Company, Division of Kelsey-Hayes, Springfield, Ohio, and finish ground by the National Broach and Machine Company, Detroit, Michigan.

The SK13264 conformal test gears were made to the following design specifications (for additional dimensional data, see Figure 5):

<table>
<thead>
<tr>
<th>Gear Set Number 1 SK13264-1</th>
<th>Number 2 -2</th>
<th>-3</th>
<th>-4</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Pressure Angle</td>
<td>30°</td>
<td>30°</td>
<td></td>
</tr>
<tr>
<td>2. Diametral Pitch</td>
<td>4.50</td>
<td>4.50</td>
<td></td>
</tr>
<tr>
<td>3. Number of Teeth</td>
<td>16</td>
<td>38</td>
<td>16</td>
</tr>
<tr>
<td>5. Face Width</td>
<td>1.950</td>
<td>2.132</td>
<td></td>
</tr>
<tr>
<td>6. F/D Ratio</td>
<td>0.50</td>
<td>0.55</td>
<td></td>
</tr>
<tr>
<td>7. Helix Angle</td>
<td>25° 13'</td>
<td>25° 13'</td>
<td></td>
</tr>
<tr>
<td>8. Axial Overlap</td>
<td>1.20</td>
<td>1.40</td>
<td></td>
</tr>
</tbody>
</table>

The two gear sets are identical except that face width was varied to investigate axial overlap, an important design parameter. This variation did not require changes in tooling or manufacturing technique. The design specifications selected for the test gears reflect the assumptions and methods of Phase I. The specifications were chosen to provide equal bending strength and surface contact capacity.
These are at least four important geometric variables that determine strength and contact capacity within a given gear blank size: tooth thickness, overlap ratio, profile radius, and pressure angle. Subsidiary to these, but also important, is the profile mismatch, which is selected from the expected change in operating center distance. By proper portioning of the variables, the necessary balance of strength and contact capacity may be obtained.

A discussion of the test gear design considerations follows:

**Tooth Thickness**

Tooth thickness depends upon helix angle and face width-to-diameter ratio (Figure 6). Face width-to-diameter ratio was made 0.5, on the assumption that this represents a condition where deflection and support problems are minimal.

The analytical method indicated that bending strength should be maximized to balance contact capacity. The helix angle was therefore set at a practical high limit of 25 degrees. This produced a thick tooth, with maximum section modulus at the base. The choice of helix angle also influences the contact capacity. Increasing the helix decreases the curvature radii in the axial direction and thus the axial length of the band of contact is decreased. Contact stress is thereby increased. The choice of helix angle is a powerful stress balancing factor, since it has a reverse effect on the two stress parameters which determine load capacity.

Results of the testing indicate that the design was unduly prejudiced in favor of strength. An immediate reaction would be to reduce helix angle to increase contact capacity.

**Overlap Ratio**

Overlap ratio is the face width divided by the axial pitch. Overlap ratios of 1.2, or more, are recommended to equalize bending stress between middle of tooth and end of tooth. More overlap than is necessary to accomplish this increases face width with no increase in load capacity. Less overlap may result in premature bending failure. It is therefore
Figure 5. Drawing SK13264
INCREASED HELIX ANGLE RESULTS IN INCREASED TOOTH THICKNESS $T_N$

Figure 6. Tooth Thickness vs Helix Angle
desirable to develop an understanding of overlap ratio effect. To this end, the test sets were made in two overlap ratios. Because of other overriding differences, the effect of varying overlap ratio was not observed. However, the strain gage survey undertaken after the load tests provides an insight into the load distribution across the tooth, which will be useful in future designs.

**Profile Radius**

A profile radius of curvature of 10 percent of the pitch radius was a practical maximum to obtain an adequate top land width with the 30-degree pressure angle. The selection of a 10-percent mismatch of convex and concave profile radii was based upon the expected accuracies of aircraft involute manufacturing experience, and the recorded accuracies of center distance and alignment of the test stand.

**Pressure Angle**

The pressure angle of 30 degrees was selected for maximum bending strength. A high angle gives a theoretical load line with minimum moment arm to the critical section, plus a significant compressive relief component.

**FABRICATION**

The manufacturing procedure and process sequence for the conformal contact test gears were as follows:

1. Forge individual biscuit of 9310 vacuum melt steel
2. Rough-machine gear blank and stress relieve
3. Final-machine gear blank
4. Hob (cut) gear teeth
5. Carburize gear teeth
6. Heat treat (harden and draw)
7. Grind faces and journals
8. Grind teeth
9. Make final inspection
10. Shot peen teeth

This sequence is normal for Vertol Division production gears. Standard gear production machine tools were used although special development effort in hob design (see Figure 7), grinding, and inspection was required to produce the conformal tooth.

Checks by optical projection and comparison with the template masters revealed a non-uniform grinding stock allowance on both members. To ensure material cleanup and to equalize stock removal, grinding stock removal was increased 0.005 inch each side of the pinion and decreased 0.008 inch each side of the gear. This reduced the calculated minimum assembled backlash from 0.012 inch to 0.006. In a small test quantity of gears it becomes necessary to increase the grinding stock allowance to compensate for unpredictable distortions during heat treatment. Consequently, more of the carburized compressive layer is removed, and removed less uniformly than in production-quantity gears. Therefore, to compensate for this condition, the two completed sets of conformal test gears were shot-peened at a Vertol-approved facility to improve residual compressive stress.

A review was made to determine the most feasible method for finish grinding the conformal contact gear. Two types of grinding were compared: generated grinding and form grinding. The results indicated that, while either method is suited to the conformal concept, form grinding would be more suitable for the test gears because of the diametral pitch selected. Before finish grinding of the test gears, the form grinding method was evaluated by finish grinding dummy gear blanks. Nital etch inspection of the first ground pinion from the dummy set (verified by subsequent nital etch and magnaglo inspection at Vertol Division) revealed heavy burns at approximately the pitch diameter. The difficulty can be attributed to the profile and large full fillets of the convex tooth and to the resulting
Figure 7. Conformal Pinion Hob
transition portion near the pitch diameter. The problem was overcome by modification of the grinding technique. Grinding damage was not noted on the test gears.

INSPECTION

A study was conducted to determine the most practical method for checking tooth form (including profile) and fillet contour. It was decided to use optical projection by surface illumination on a 30-inch screen optical projector. Charts of the tooth profiles, before and after finish grinding, were made at a magnified scale (20X) for comparison with the projected image (see Figure 8). This method has inherent limitations for direct observation of the conformal gear: helical curvature limits inspection of the tooth profile to the ends of the gear face, and edge breaking of the gear teeth distorts the projected image. An indirect method was employed in this program to eliminate the second problem. A shim 0.002 inch thick was fastened to the end of the gear blank, hobbed and ground with the gear, and then removed and projected for comparison with the charts. The probable inaccuracy of profile measurement by the method used is believed to approximate 0.0005 at the gear. This estimate combines the chart tolerance and the limits of visual discernment.

There is an obvious need to develop an inspection technique that can define the tooth profile at any transverse plane with accuracy comparable to involute gear requirements of within 0.0001 inch. Several such techniques are under consideration. One method, an adaptation of one now used by Automation Gages, Inc., to inspect complex shapes, employs a coordinate tracer and optical projection (Figure 9). It appears to be able to map conformal tooth profiles of any type of curvature, concave or convex. The effort required to adapt the apparatus and techniques has not yet been defined. A developed refinement of the system sketched is the use of photocell pickups to increase accuracy beyond that limitation of the eye. The output of the photocell scanner may be displayed by a digital encoder.
Figure 8. Comparator and Chart
Figure 9. Coordinate Tracer Schematic
A more immediate method, which may be used with existing inspection equipment, adapts an involute checker to the circular-arc profile. At the moment, it appears limited to the convex tooth. The involute checking equipment used industry-wide traces the tooth profile on a strip chart as the gear is rotated. A perfect involute appears as a straight line; departures from the involute cause deviations from the straight line, highly magnified and directly measurable on the chart paper. The technique can thus be adapted to circular-arc profiles, provided only that the reference involute fits the circular arc well enough that the maximum deviation is within the machine range. The reference involute and the offsets are mathematically obtainable (refer to the Appendix). The base circle from which the reference involute is constructed can be readily set into the involute checker, and a circular-arc profile can then be measured. The resulting chart trace is shown in the Appendix. A basic check of machine accuracy is obtainable by the Michigan Tool Company Roll-Pin device; it is widely used as an involute machine checking standard. With proper dimensional selection, it produces a chart identical to that obtained from a convex circular-arc gear profile.

Individual gear tooth element tolerances, such as lead error and tooth-to-tooth spacing error, were measured by conventional inspection machines and methods.

To complement the detail inspection, light load pattern checks and noise level tests (gear speeder) were conducted on the dummy pinion and gear at varied center distances. At the nominal 6.000-inch center distance, the pattern on the gear member was an axial line just beneath the tip radius. The pattern on the pinion member was an axial line just above the pitch diameter. At 5.994-inch center distance, the pattern shifted down on the gear member and up on the pinion member. The noise level was higher than the previous check. At 6.006-inch center distance, the patterns shifted back to high on the gear and low on the pinion, with a more pronounced line evidencing increased tip radius loading. The noise level was comparable to or better than that obtained at the 6.000-inch center distance (see Figure 10).
Figure 10. Patterns of Dummy Pinion (Top Row) and Gear (Bottom Row) at Various Center Distances
LOAD TESTS

EQUIPMENT

Testing was conducted in a Vertol-owned regenerative (four square) load test stand built specifically for gear research (see Figures 11 and 12). The two gear cases are designed to be rigid and stable under all loading conditions. Housings were through-bored for maximum accuracy. Torque, rpm, and lubrication can be varied over a wide range.

Accelerometers were attached to both the slave and test gearboxes and connected to a dual-channel oscilloscope. Changes in vibration signatures for both gear cases can be observed simultaneously and used as an indication of impending gear failure.

Each gearbox lubrication system includes an individual reservoir, pump, control, indicators, filler, and jets. All controls and indicators are mounted in the console. Lubrication oil volume is controlled by a bypass valve. Temperature is indicated both in and out of the test gearbox. Pressure is indicated at a point just upstream of the jets.

Atlantic Refining Company Premier 12 gear lubricant was used throughout the test program; it contains extreme pressure additives in the form of lead soaps. Vertol Division has used Premier 12 in previous gear research testing*; the results of the previous testing were used as a base line for evaluating the conformal gear.

Lubrication was provided by oil jet on the out-of-mesh side. The flow rate, approximately 2.0 gallons per minute for gear set number 1, was increased to 2.9 gallons per minute before testing gear set number 2. The added flow was directed to the entering side of mesh, where surface deterioration had been observed during the tests of gear set number 1. Lubricant pressure, temperature, and viscosity were controlled to the following values during the testing.

Figure 11. Gear Research Test Stand
tests:

1. Operating Temperature: 125 ± 15°F
2. Operating Pressure: 60 ± 15 PSI
3. Viscosity at Operating Temperature: 300 SSU

VARIABLES

The primary test variables were shaft torque and test cycles (time). Gear load is a function of shaft torque.

Torque

Torque was applied with a lever system at the beginning of each test run. Torque levels were observed on an SR-4 instrument. The procedure for this test program was to check torque after 30 minutes of running, then to recheck every 2 hours during the test. Deviation from the initial target torque was held to ± 5 percent.

The torquemeter shaft was calibrated before and after the test series on a Riehle deadweight torsion test machine. The same instrument was used during the calibration and testing. Recalibration curves agreed with the initial curve within 2 percent.

Test Cycles

Test cycles were determined by a log record of running time and an elapsed time meter in the test stand console. An electric motor driving the input shaft through a toothed belt maintained pinion speed at 3600 rpm (346,000 tooth loading cycles per hour).

PROCEDURE

At the initial installation of both gear sets, static tooth patterns were recorded at various load levels, and the gear sets were then run in for 1.73 million cycles (8 hours) at approximately 1260 inch-pounds torque. Gear set number 1
Figure 12. Test Arrangement
was run for an additional 432,000 cycles (2 hours) after initial pitting from run 2 had been removed by stoning.

Each gear set was given three test runs at various load levels. For each load level, the test run was concluded at 3.46 million cycles of load on the pinion tooth. Previous experience with involute spur gears locates the knee of the S-N curve at between two and three million cycles.

The load test program is summarized in Table I. Stress levels associated with test load levels are shown in Figure 13.

RESULTS

Static Pattern Check and Run-in of Gear Set Number 1

Static pattern checks at the various load levels indicated a tapered tooth pattern, larger at the entering side of mesh and smaller at the leaving side (see Figure 14). The pinion member had the deepest extension of the pattern approximately parallel to the outside diameter, with the taper at the top. The gear member had the opposite condition. This tapered pattern became more pronounced with increased load, and it persisted throughout the dynamic testing.

Visual inspection after the initial run-in period did not reveal any adverse conditions.

Load Test Runs of Gear Set Number 1

Test run 1 showed no surface indications.

Test run 2 was completed at 133 percent of design load. Visual inspection at this time revealed conditions similar to gear set number 1 at the completion of test run number 2. See Figure 14, Sheet 1 for this condition. The single pit was not as deep or pronounced as the number 1 gear set, and it originated at the very edge of both members. It should be noted that this gear set had an increased contact ratio (1.4), increased face width over pitch diameter ratio, and increased oil supply to the entering side of mesh. The pitting condition was removed by hand stoning.
# TABLE I
## LOAD TEST PROGRAM

<table>
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<th>Stress Cycles (millions)</th>
<th>Pinion Torque (in.-lb)</th>
<th>End Condition</th>
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<td>Pinion</td>
<td>Gear</td>
<td></td>
</tr>
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<td>0.727</td>
<td>1,260</td>
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<tr>
<td>Run 2</td>
<td>3.460</td>
<td>1.450</td>
<td>8,600</td>
</tr>
<tr>
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<td>0.432</td>
<td>0.182</td>
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</tr>
<tr>
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<td>1.260</td>
<td>13,400</td>
</tr>
<tr>
<td>Set No. 2</td>
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<td>SK13264-4, Ser. P1003</td>
<td></td>
</tr>
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<td>0.727</td>
<td>1,370</td>
</tr>
<tr>
<td>Run 1</td>
<td>3.460</td>
<td>1.450</td>
<td>8,600</td>
</tr>
<tr>
<td>Run 2</td>
<td>3.460</td>
<td>1.450</td>
<td>13,900</td>
</tr>
<tr>
<td>Run 3</td>
<td>1.080</td>
<td>0.470</td>
<td>16,100</td>
</tr>
</tbody>
</table>
Figure 13. Conformal Gear Stress Levels (Not Corrected for Actual $L_N$)
GEAR PATTERNS AFTER RUN-IN, GEAR SET NUMBER 1

PINION SK13264-1, SER. P1009

GEAR SK13264-2, SER. P1001

Figure 14. Tooth Patterns During Load Test (Sheet 1)
GEAR PATTERNS AFTER RUN 2, GEAR SET NUMBER 1

PINION SK13264-1, SER. P1009

GEAR SK13264-2, SER. P1001

GEAR PATTERNS AFTER STONING AND RUN-IN, GEAR SET NUMBER 1

PINION SK13264-1, SER. P1009

GEAR SK13264-2, SER. P1001

Figure 14. Tooth Patterns During Load Test (Sheet 2)
Figure 14. Tooth Patterns During Load Test (Sheet 3)
GEAR PATTERNS AFTER RUN 1, GEAR SET NUMBER 2

PINION SK13264-3, SER. P1005

GEAR PATTERNS AFTER RUN 2, GEAR SET NUMBER 2

PINION SK13264-3, SER. P1005

Figure 14. Tooth Patterns During Load Test (Sheet 4)
GEAR PATTERNS AFTER RUN 3, GEAR SET NUMBER 2

PINION SK13264-3, SER. P1005

180° AWAY

GEAR SK13264-4, SER. P1003

180° AWAY

Figure 14. Tooth Patterns During Load Test (Sheet 5)
below the edge radius. Pitting is generally considered to be a fatigue phenomenon caused by contact pressure between mating tooth profiles repeatedly engaging and disengaging. Magnaglo inspection of both members did not reveal any crack indications.

The pits were removed from both members by hand stoning so that the testing could continue. The gear set was then run in for two more hours (432,000 cycles) to determine the effect of stoning on the tooth patterns. The subsequent visual inspection revealed an inconsistent pattern on most of the teeth (see Figure 14, Sheet 2).

Test run 3, conducted at 205 percent of the design load level, ended with surface fatigue failure — severe spalling and partial tooth breakage — at 2.98 million cycles. Pitting became evident early in the run and progressed across the face width. During the last several hours of this run, scale changes from 0.5 volt per centimeter to 1.0 and 2.0 volts per centimeter were needed to keep the increased accelerometer signature on the oscilloscope. Subsequent magnaglo inspection revealed numerous cracks on both members.

Static Pattern Check and Run-in of Gear Set Number 2

Static pattern checks on gear set number 2 indicated a tapered tooth pattern similar in inclination and direction to the number 1 gear set, but to a much lesser degree — approximately 0.02 inch from end to end (see Figure 14, Sheet 3). Visual inspection upon completion of the run-in period did not reveal any adverse conditions.

Load Test Runs of Gear Set Number 2

Test run 1 was completed at 133 percent of design load. Visual inspection at this time revealed conditions similar to gear set number 2 at the completion of test run number 2. See Figure 14, Sheet 1 for this condition. The single pit was not as deep or pronounced as the number 1 gear set, and originated at the very edge of both members. It should be noted that this gear set had an increased contact ratio (1.4), increased face width over pitch diameter ratio, and increased oil supply to the entering side of mesh. The pitting condition was removed by hand stoning.
Test run 2 was completed at 215 percent of the design load level. Visual inspection at this time revealed minor pitting on the gear member and increased pitting on the pinion member (one tooth in particular). The tooth patterns after stoning were consistent and therefore not similar to gear set number 1. See Figure 14, Sheet 4 for this condition. It was decided to continue running at the next load level without modification.

Test run 3 was conducted at 250 percent of the design load level. This test run resulted in failure at 1.08 million cycles due to surface fatigue and failure of one tooth on the gear member. Subsequent magnaglo inspection revealed 12 cracked teeth on the gear member and no indications on the pinion member. Figure 14, Sheet 5 reflects pattern conditions at the conclusion of this run.

The test gearbox was instrumented for a sweeping wave analyzer during the three load test runs. The analysis of accelerometer data identified the major vibration frequencies as harmonics of the basic tooth frequency. As the test progressed, the amplitude of these harmonics increased and closely associated frequencies appeared.

Figure 15 illustrates the condition of the gear and Figure 16 the pinion at the conclusion of testing.

Metallurgical Findings

A metallurgical analysis of gear set number 2 made upon completion of testing included:

1. Nital Etch Examination

Nital etch examination showed no evidence of grinding damage.

2. Microhardness Traverse

Microhardness traverse was made of the failed tooth on the gear member. The results are plotted in Figure 17. While the top land of the tooth showed a highly acceptable hardness gradient, the
GEAR SHOWING FAILED TOOTH PITTNG EVIDENT ON TEETH. ARROW POINTS TO AN INCIPIENT CRACK.

AREA OF TOOTH FAILURE FAILED SEGMENT

Figure 15. Gear Condition After Final Run, Gear Set Number 2
TYPICAL HEAVY FROSTING

WORST PIT (ENTERING SIDE)

Figure 16. Pinion Condition After Final Run, Gear Set Number 2
SECTION OF FAILED TOOTH
(ARROW INDICATES EFFECT OF IMPINGEMENT
OF DRIVE-SIDE TOOTH TIP)

MICROHARDNESS TRAVERSE OF THE ABOVE SECTION

Figure 17. Condition of Gear Set Number 2
drive flank is marginally acceptable: the gradient is steep, and the minimum specified depth to 50 Rc (0.025 inch) is not met. The conclusion is that too much material had been ground from the flank and this weakened the tooth. Grinding stock removal can be minimized in the future because of the experience gained from this test series. Preservation of the carburized layer requires knowledge of the heat-treat distortion to be expected of this type of gear and also requires a means of inspecting the tooth profile after cutting.

3. **Microexamination**

A microexamination for retained austenite, carbide network, and cleanliness showed that the material was satisfactory in all respects.

4. **Fractographic Examination**

A fractographic examination of the failed tooth located the origin of the fatigue in the drive side fillet. The specimen did not provide enough evidence to tell whether the origin was at the surface or below the surface.
STRAIN SURVEY

To gain additional understanding of the mechanism of conformal contact, a pinion tooth strain survey was performed. Three consecutive pinion teeth were gaged in such a way that a record of load sharing could be obtained as the gear and pinion were rolled through mesh under torque.

Gear set number 2 was used in the strain survey. The test was conducted in the Vertol research test stand used for the load run evaluation. Torque was applied in a direction opposite to that used in load running to apply contact to the unworn (coast side) tooth flanks.

INSTRUMENTATION

Strain gages of type CX-111 (Budd) were applied to the tension root fillet of the pinion. Figure 18 shows the placement of gages and their numeration. Resistance calibration methods were used to establish a known strain level in each gage. Gage location from the pinion outside diameter to gage center was initially held as closely as possible to 0.180 inch. The gages did not extend onto the contact surface of the tooth. Eight gages were applied to the middle tooth at equal spacings of 0.33 inch, with gage numbers 3 and 10 as close as possible to the tooth ends. Gages 1 and 2 were applied to the leaving end of the preceding tooth, at the same spacing between gages. Gages 11 and 12 were similarly applied to the entering end of the succeeding tooth. During the survey, the gages were expected to pick up load in numerical ascending and descending order, according to direction of rotation.

Additional information was obtained from a rotary potentiometer connected to the pinion shaft, and from a continuous record of the torque.
The effect of the tapered tooth patterns is still more difficult to measure. Note, however, that gear set number 2, which had little taper, outperformed gear set number 1, which had a very apparent taper. Gear set number 2 final surface condition after operation at 16,000 inch pounds, was markedly better than that of number 1 at the midpoint of its final run at 13,400. The initial pitting which occurred on both sets was in the area of the full pattern (large end of the taper) and is ascribed to lack of lead-in relief, rather than to pattern deficiency. Lead-in relief is a correction of the helix angle to improve the load transfer from one tooth to the next. It is similar in effect to involute profile modification, in that it compensates for elastic deflections of one tooth relative to the next.

Comparison With The Analysis

The analytical method derived for the conformal gear did not account for maldistribution of load and its effect on contact stress. The analysis assumed full conformity of profile, no tip interference, and equal loading from end to end. The damage observed in the experiment represents different and less favorable conditions.

When the stress analysis was modified for the reduction in \( L_N \) estimated by the effect of tip interference, the computed contact stress appears consistent with the observed damage. The estimate of consistency is based upon involute gear experience using identical material, surface hardness, and lubricating oil. The certainty with which contact deterioration can be related to a stress level may be less than that relating to a tooth bending failure. Nevertheless, it appears that the present contact stress calculation method is valid, and may be used in assessing the capacity of future designs.

The possibility of added capacity improvement by other refinements of the tooth also exists. If these are proven by test, the present contact stress allowables derived from involute gearing may be increased, insofar as sliding velocity due to profile disparities is reduced. As noted in the Phase I report, the literature of surface contact experimentation indicates that a pure rolling contact can withstand higher pressures without distress than is possible when sliding is present.
PROCEDURE

The test procedure was to rotate the gear and pinion slowly through mesh, while observing and recording strain gage outputs, torque, and angular position. The first roll-through was with the gear driving. The return to the starting point was with the pinion driving. The driving member is the one wherein the loaded side of the tooth is advancing. A normal speed-decreasing mesh is pinion driving, and this condition pertained during the load tests.

All information was recorded on a multichannel oscillograph while the gears were being rotated.

RESULTS

A typical record of test results is shown in Figure 19. Outputs of gages 1 through 12 are shown as they rise and fall during the mesh cycle. The middle tooth is in mesh from the first rise of gage 3 to the return to zero of gage 10. The fall to zero of gage 2 indicates the instant of disengagement of the first tooth the rise of gage 11 indicates the engagement of the third tooth. The interim is the period that the middle tooth carries all load. This single-tooth engagement period is of very short duration.

The left-hand peaks were obtained with the gear driving; the right-hand peaks were obtained on the return with the pinion driving. Strain amplitudes during the latter condition were found to be consistently higher, by an average 100 percent. The explanation originally devised centered upon tangential friction forces in the mating teeth. Friction force when the gear drives is opposite in direction to that when the pinion drives. This force increases the tensile stress field at the tooth base when the pinion drives and reduces it when the gear drives. The attempt was made to measure this effect experimentally by lubricating the teeth and comparing the resulting data to the dry state. The results did not substantiate this explanation. It is possible that the slow rate of engagement squeezed out most or all...
Figure 19. Oscillograph Record of Strain Gage Data
of the lubricant and, of course, a hydrodynamic effect was not expected. Therefore, the effect of lubrication on friction reduction may not have been significant. Nevertheless, the hypothesis, while not discarded, appears less probable. At the moment, no other explanation of this phenomenon has been advanced for study.

Variations were observed in the torque trace. The maximum variation shown is 3 percent of the total applied torque. Torque variations did not appear to repeat in a cyclic pattern and were not clearly identifiable with any of the rotating components. Maximum strains at each gage across the pinion face are recorded in Table II. Three test conditions are shown. The average gage output has been corrected by the measured position of each gage relative to the center of the observed band of contact.
<table>
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<tr>
<th>Test No.</th>
<th>Gage No.</th>
<th>Measured Amplitude</th>
<th>Correction Factor</th>
<th>Corrected Average</th>
</tr>
</thead>
<tbody>
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<td>Gear Tooth 28 (dry)</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1.06</td>
<td>1.74</td>
<td>1.40</td>
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</tr>
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<td>2</td>
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<td>1.22</td>
<td>2.33</td>
<td>.77</td>
<td>1.80</td>
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</table>

| Gear Tooth 32 (dry) | | | | |
| 1 | 1.30 | 2.08 | 1.69 | 1.25 | 2.10 | 925 |
| 2 | 1.14 | 2.48 | 1.81 | 1.00 | 1.81 | 796 |
| 3 | .80 | 1.70 | 1.25 | 1.00 | 1.25 | 550 |
| 4 | .55 | 1.71 | 1.13 | 1.43 | 1.62 | 713 |
| 5 | 1.31 | 2.80 | 2.05 | 1.00 | 2.05 | 902 |
| 6 | 1.60 | 3.33 | 2.46 | 1.00 | 2.46 | 1080 |
| 7 | 1.84 | 3.50 | 2.67 | 1.00 | 2.67 | 1175 |
| 8 | 1.34 | 2.65 | 2.00 | 1.00 | 2.00 | 880 |
| 9 | 1.48 | 2.35 | 1.91 | 1.00 | 1.91 | 840 |
| 10 | 2.70 | 3.30 | 3.00 | 83 | 2.50 | 1100 |
| 11 | 1.50 | 2.52 | 2.00 | 1.00 | 2.00 | 880 |
| 12 | 2.00 | 3.78 | 2.89 | .77 | 2.23 | 980 |

| Gear Tooth 32 (Lubed) | | | | |
| 1 | .78 | 2.04 | 1.41 | 1.25 | 1.76 | 775 |
| 2 | 1.00 | 2.53 | 1.76 | 1.00 | 1.76 | 775 |
| 3 | .72 | 1.66 | 1.19 | 1.00 | 1.19 | 524 |
| 4 | .48 | 1.57 | 1.02 | 1.43 | 1.46 | 642 |
| 5 | 1.06 | 2.65 | 1.85 | 1.00 | 1.85 | 814 |
| 6 | 1.10 | 3.04 | 2.07 | 1.00 | 2.07 | 910 |
| 7 | 1.39 | 3.29 | 2.33 | 1.00 | 2.33 | 1025 |
| 8 | 1.12 | 3.52 | 2.32 | 1.00 | 2.32 | 1020 |
| 9 | 1.14 | 2.02 | 1.58 | 1.00 | 1.58 | 695 |
| 10 | 2.42 | 3.13 | 2.77 | .83 | 2.30 | 1010 |
| 11 | 1.22 | 2.40 | 1.81 | 1.00 | 1.81 | 800 |
| 12 | 1.22 | 2.50 | 1.86 | .77 | 1.43 | 629 |
EVALUATION OF RESULTS

The load levels sustained by the second conformal gear test set indicated that its load-carrying capacity was approximately equal to that of its involute-form counterpart. The performance of these gears, despite obvious problems, implies a considerable development potential that remains to be exploited. If the contact condition can be improved, the conformal gear should surpass the involute gear.

CAUSES OF FAILURE

Load testing revealed phenomena which influenced the types of failure and the load levels at which they occurred:

1. Tapered tooth pattern
2. Initial pitting at the entering end
3. Impingement of the gear tooth against the pinion tooth
4. Carburizing depth less than drawing requirement

The tapered pattern, pitting, and tooth impingement caused premature contact failure by decreasing the contact area available. Tooth impingement also increased bending stress in the gear by increasing the bending arm. The shallow carburized layer reduced material strength.

Tapered Tooth Patterns

The exact effect of the tapered tooth patterns is difficult to measure. Note, however, that gear set number 2, which had little taper, outperformed gear set number 1, which has a very apparent taper. Gear set number 2 final surface condition after operation at 16,000 inch-pounds was markedly better than that of number 1 at the midpoint of its final run at 13,400 inch-pounds. The tapered tooth patterns could be attributed to one or more of the following conditions:
1. Misalignment of the gear case bores
2. Deflection of the shaft under load
3. Lead error
4. Gear faces not perpendicular to shaft axis
5. Non-uniform curvature of tooth profile

The following investigations were made to localize the condition:

1. Before the tests, the gear cases and shafts were inspected by Vertol Division's Quality Control Department. Alignment of the case bores was within the 0.0000-to-0.0002-inch limit. Runout and shoulder perpendicularity of the shafts were well within the drawing limits.

2. During the static pattern checks, shaft deflection and gear face runout were inspected and found to be negligible. The fact that the bottoms of the pinion patterns were parallel to the outside diameters is further indication of parallel location.

3. Lead-error checks of each gear and pinion at the National Broach and Machine Company showed that deviations were within 0.0000 to 0.0001 inch across the entire face.

4. The conformity of the profile radii to the specified form could be inspected only at the end of the tooth, rather than across the face width. Therefore, non-conformity of profile radii must be suspected as a cause of tapered patterns.

**Pitting at Entering End**

The initial pitting which occurred on both sets was in the area of the full pattern (large end of the taper), and is ascribed to lack of lead-in relief rather than to pattern deficiency. Modification of the helix angle is needed to compensate for the deflection of the teeth as they pass.
through the load zone and to improve the load transfer from one tooth to the next. It is similar in effect to involute profile modification, in that it compensates for elastic deflections of one tooth relative to the next.

Impingement of Tooth Tip

The pattern ended abruptly with a hard line on the pinions of both test sets. Apparently, without tip modification the profile-radius mismatch at the high load levels was not sufficient to overcome tip interference. Figure 17 shows the tip damage to the gear member of set number 2. This tip (noted by arrow) impinged the pinion low on the pinion tooth flank and caused high localized contact stresses, as evidenced by the hard line.

COMPARISON WITH INVOLUTE GEARING

Disregarding for the moment the maldistribution of load which influenced the test results, the performance of the conformal gears can be compared to involute gears of equivalent size having the same diameter and face width. Previous tests indicate that equivalent size involute gears would sustain a bending fatigue failure between 30,000 and 40,000 inch-pounds of pinion torque. Before this level was attained, severe surface contact deterioration would have occurred between 14,000 and 16,000 inch-pounds of torque. The load-carrying capacity would be determined by surface contact deterioration.

The conformal gear experienced mild pitting at 8,600 inch-pounds of torque, with increasing severity up to the last test at 16,000 pounds. These load levels are thus comparable to expectations for similar distress on an equivalent size involute gear.

GEAR LOAD PATTERN

Axial Overlap

The overlapping effect of the conformal gear load pattern is shown by Figure 20. This information was taken from a non-lubricated run at design torque (6500 inch-pounds). The rise and fall of the strain gage outputs have been plotted against pinion angular motion. Test variations in angular velocity
have been corrected by scaling the rotary potentiometer trace at each significant peak stress. The basic reference is taken as the angle between the peak of gage 3 and the peak of gage 11. These gages are located at identical points on successive teeth. There is thus 22.5 degrees (360 : 16) of pinion travel required to rotate 11 to the same position as 3.

Overlap is shown as nearly 2.0 compared to the 1.4 calculated for the design. The reason for this large increase is that the analytical method assumes point contact, while actually under load there is area contact. The overlap ratio of the calculation is indicated by peak stress points. Considering these, angular motions between gages 2 and 3, and 10 and 11, are each approximately 20 percent of the total travel from end to end of one tooth (3 to 10). This is equivalent to a 1.4 axial overlap.

Contact Area

Length of the contact footprint has been seen to affect overlap. From Figure 20 it is possible to determine the axial length of the footprint experimentally. The assumption is made that the center of footprint is located above the gage with the maximum reading at that instant. When gage 2 is at maximum intensity, the angular position of the pinion is known. When gage 2 goes to zero, it is known that the contact with that tooth is broken. The angular position at that instant is also known. The difference in angular position between the two points is a measure of the half-length of the footprint (dimension b of the analysis). When angular travel was converted to motion along the tooth and the distance from gage to end-of-tooth was subtracted, the value of b was found to be 0.33 inch. Using the analytical solution, b was found to be 0.29 inch. The value of $L_N$ was taken as the height of the contact band observed from the pinion wear pattern. Comparison of the experimental and analytical results indicates that the calculated value for b is substantially correct. If, however, the initial analytical assumption of full tooth profile height for $L_N$ is taken, the footprint length decreases to 60 percent of that found experimentally. The effective overlap decreases as well. However, a compensatory factor appears in that sliding is reduced as point contact is approached. With sliding reduction, there is a lesser tendency for scoring.
Figure 20. Load Overlapping Effect
STRAIN DISTRIBUTION

Corrected average gage outputs (from Table II) are shown in Figure 21. If gage 10 is discarded, a symmetrical rise to a maximum stress at the tooth center may be visualized. At the center, as has been shown, single tooth contact is supported momentarily. There is no evidence that the tooth end stresses are more critical than the midpoint. Corroboration of this is drawn from the load test results, where failure occurred at the middle of the gear face.

A gage's output may be affected by variables such as gage distance, inclination of the gage axis to the vertical, and bonding of the gage to the specimen. Comparison of stresses between individual gages should therefore be made with some caution. For instance, the readings from gage 10, unsupported by neighboring gages, are treated with less confidence than the trends shown between gages 3, 4, 5, 6, and 7.

COMPARISON WITH CALCULATED STRESS

The original analytical method derived for the conformal gear did not account for maldistribution of load and its effect on contact stress. The analysis assumed full conformity of profile, no tip interference, and equal loading from end to end. The damage observed in the experiment represents different and less favorable conditions.

Contact Stress

Contact stress was increased by tip interference. It is reasonable to suppose that the height of the face ($L_N$) was effectively reduced to one-half that of the theoretical during the tests. By substitution in the analysis, contact stress would thereby increase 40 percent, and load capacity would decrease by one-half as compared to full-conformity contact. Contact stress computed from the reduced $L_N$ appears to be consistent with the observed damage. This judgement is based upon involute gear experience using identical material, surface hardness, and lubricating oil. The certainty with which contact deterioration can be related to a stress level may be less than that relating to a tooth bending failure. Nevertheless, it appears that the present contact stress calculation method is valid and that current gear stress allowables may be used in assessing the capacity of conformal designs.
Figure 21. Maximum Strain Readings (Data From Table II)
The possibility of added capacity improvement by other refinements of the tooth also exists. If these are proven by test, the present contact stress allowables derived from involute gearing may be increased, as sliding velocity due to profile disparities is reduced. As noted in the Phase I report, the literature of surface contact experimentation indicates that a pure rolling contact can withstand higher pressures without distress than is possible with sliding contact.

**Bending Stress**

Bending strength analysis was not checked by the load-run results, since bending strength was calculated only for the convex tooth pinion and no representative failure of the pinion was obtained. At the failure loads, the calculated bending stress was not high enough to indicate a pinion tooth failure, and such a failure did not occur. The initial estimates of comparative load capacity between conformal and involute gears were based upon pinion tooth strength. This was also the basis for indicating the high face-to-diameter ratio requirement for conformal gear superiority, at equal bending stresses. Rating the capacity upon pinion tooth strength does not appear entirely realistic and may unduly prejudice the conformal gear.

Examination of the load-test specimens indicates that tip impingement increased bending stress in the concave tooth gear by raising the tangential load point above the theoretical mid-face. A compensatory factor is that such a concentrated tip load would increase the axial length of contact (dimension 2b). However, the formulae indicate that the change in height outweighed the reduction in moment factor (K1). The combined effect was to increase calculated gear bending stress 50 to 75 percent.

In the initial analysis, it has been estimated from photoelastic observation that the gear is the more highly stressed, and in the tests the gear proved to be the weaker member. Because of the peculiar load distribution noted during the test, the failure of the gear is not conclusive proof of the photoelastic estimates; but if testing of improved load patterns continues to fail the gears rather than the pinions, the stress analysis should be revised to calculate gear bending.
Balancing Contact and Bending Stresses

If continued testing with improved contact patterns indicates that the conformal gear is limited by surface durability rather than by tooth failure, the initial design tendency toward high bending strength may be reversed. A revised balance of bending and contact stresses can be attained by lowering the helix angle. A lowered helix angle increases the axial radius (RE) but also decreases tooth thickness. The result is to increase contact capacity while simultaneously raising bending stresses. Increased bending stress may be acceptable for the following reasons:

1. Strain survey has shown that tooth ends are not overloaded, relative to the tooth center.

2. Modern gear materials and processes are believed to be capable of sustaining higher bending fatigue stresses than are presently used in aircraft practice.

CONCLUSIONS AND RECOMMENDATIONS

The conformal test gears demonstrated load-carrying ability equivalent to that expected of aircraft involute gears. At the failure load level, contact stresses correlated with the analytical method developed in Phase I. The final failure of the conformal test gears was induced by surface deterioration, aggravated by load concentrations from tip interference and lack of helix angle modification. There was also a tapering of the wear pattern under load, the reason for which is not completely understood.

It is likely that load-carrying capacity can be increased more than 100 percent if satisfactory distribution of load can be maintained. Load distribution can be improved by modifying helix angle and tooth profile to eliminate tip interference, provide lead-in relief, and equalize wear patterns. The following modifications are indicated:

1. Helix angle adjustment to equalize wear across the face.

2. Modification of the basic tooth profile to obtain a centralized pattern on the height of the tooth and to make tip impingement less probable.
The increased load capacity expected from these modifications will improve on the specific-weight ratios predicted by the analysis.

Inspection techniques and the equipment now available do not provide accurate measurements along the entire width of the conformal tooth face. New techniques and equipment should be developed to keep pace with the advances which the conformal tooth form represents. It will be necessary to measure accurately the profile of at least one member, and preferably both. Given this, present manufacturing techniques should be fully capable of producing any desired conformal tooth form, and modifications thereof, in high-strength carburized gear steels.

It is recommended that the conformal tooth form be modified to reflect the test results, and that the load-carrying capacity of the improved tooth form then be determined by testing.
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APPENDIX

INSPECTION OF CONFORMAL ARC PROFILE

The method for inspecting the conformal gear circular-arc (convex) pinion tooth profile on an involute checking instrument consists of the following steps:

1. By calculation, determine a master base circle diameter which would produce an involute curve most nearly approximating the circular arc of the convex pinion tooth profile (see Figure 22).

2. Establish and plot the master profile curve (see Figure 23) by calculating the deviation of the conformal circular arc profile from the involute profile determined in Step 1.

3. Check the conformal circular arc profile on an involute checking instrument by setting the instrument to the master base radius determined in Step 1 and record the results.

4. Compose the inspected profile per Step 3 to the master profile determined in Step 2.

Deviations of the inspected profile chart from the master profile chart represent errors in the pinion circular arc profile.

Method for calculating the master base circle radius and involute and the deviations of the conformal pinion circular arc profile from the master involute curve.

1. Calculate master base circle radius ($R_b$):

$$R_b = \frac{R_{SAP}}{\left[\left(\frac{E \cdot SAP}{57.3}\right)^2 + 1\right]^{\frac{1}{2}}}$$

$$R_b' = R_m \times \cos \theta$$

$$R_m = \frac{R_{SAP} + R_o}{2}$$

65
Figure 22. Involute Curve Construction
Figure 23. Master Profile Curve
\[
\cos \theta = \frac{(Rm)^2 + (r)^2 - (R_1)^2}{2(Rm) \times r}
\]

\[
\phi = 90^\circ - \theta \quad \text{(Round off } \theta \text{ to nearest degree)}
\]

\[
E^\circ_{SAP} = 57.3 \left[ \left( \frac{RSAP}{R_b} \right)^2 - 1 \right]^{\frac{1}{2}}
\]

(Round off \( E^\circ_{SAP} \) to nearest degree)

2. Calculate deviations of circular-arc profile from master involute curve (\( \Delta \)).

\[
\Delta = R_1 \sin (E^\circ - \phi^\circ) + \frac{\sqrt{r^2 - \left[ R_b - R_1 \cos (E^\circ - \phi^\circ) \right]^2 - R_b \times E}}{2 R_1 (R_b)}
\]

\[
\cos \phi = \frac{(R_1)^2 + (R_b)^2 - (r')^2}{2 R_1 (R_b)}
\]

By layout (30X scale) establish a radius \( (r') \) that will rotate the roll to be checked, which represents the conformal pinion profile, into a position that will result in a desirable deviation from the master involute.

Where

- \( R_b \) is master base circle radius
- \( \Delta \) is deviation of circular arc profile from master involute curve
- \( R_1 \) is radius to center of conformal tooth profile arc
- \( r \) is radius of conformal tooth profile arc
- \( RSAP \) is radius to start of active profile
- \( R_0 \) is radius to outside diameter
- \( E^\circ \) is roll angle to selected point on master involute
EXAMPLE

Given:

\[ R_i = 1.778 \]
\[ r = 0.1778 \]
\[ R_{SAP} = 1.768 \]
\[ R_o = 1.924 \]

Determine:

\[ R_b = \text{master base circle radius} \]
\[ \Delta = \text{deviation of circular arc from master involute} \]

1. \[ R_m = \frac{R_{SAP} + R_o}{2} = \frac{1.768 + 1.924}{2} = 1.846 \]

\[ \cos \theta = \frac{(R_m)^2 + (r)^2 - (R_i)^2}{2 (R_m) x r} = \frac{.2780448}{.6564376} = .4235662 \]

\[ \theta^\circ = 65^\circ \text{ (Rounded off)} \]

\[ \phi = 90^\circ - \theta = 90^\circ - 65^\circ = 25^\circ \]

\[ R_b' = R_m x \cos \phi = 1.846 x .9063078 = 1.6730442 \]

\[ E_{SAP}^o = 57.3 \left[ \left( \frac{R_{SAP}}{R_b'} \right)^2 - 1 \right]^{\frac{1}{2}} = 57.3 \left[ \left( \frac{1.768}{1.6730442} \right)^2 - 1 \right]^{\frac{1}{2}} = 20^\circ \text{ (Rounded off)} \]

\[ R_b = \frac{R_{SAP}}{\left( \frac{E_{SAP}^o}{57.3} \right)^2 + 1}^{\frac{1}{2}} = \frac{1.768}{\left( \frac{20^\circ}{57.3} \right)^2 + 1}^{\frac{1}{2}} = 1.6692271 \]
2. \( r' = 0.2288 \) (by 30X layout)\\

\[
\cos \phi = \frac{(R_1)^2 + (R_b)^2 - (r')^2}{2 R_1 R_b}
\]

\[
= \frac{3.1612840 + 2.7863191 - .0523494}{5.9357716}
\]

\[
= .9931739
\]

\( \phi = 6.70^\circ \)

\[
\Delta = R_1 \sin (E^\circ - \phi^\circ) + \\
\sqrt{r^2 - [R_b - R_1 \cos (E^\circ - \phi^\circ)]^2} - R_b \times E
\]

\[
= 1.778 \times .2300772 + \\
\sqrt{1.778^2 - [1.6692271 - 1.7303005]^2} - \\
1.6692271 \times .3490659
\]

\[
= .4090773 + \sqrt{.0316128 - .0037300 - .5826700}
\]

\[
= .4090773 + .1669814 - .5826700
\]

\[
= -.0066113 \text{ (at 20° of roll)}
\]

The calculation of \( \Delta \) is repeated for all desired degrees of roll. The results for this example are as follows:

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The conformal gear has been studied as a means of improving helicopter final reduction drives. By eliminating certain inherent limitations of the involute gear, the developed conformal tooth form has the potential of bettering current power-to-weight ratios. Under USAAVLABS sponsorship, the Vertol Division of Boeing has conducted an analytical and experimental effort on carburized and ground conformal gears which has resulted in the first published work in this area. (Earlier efforts had used unground, commercial gears.) This report concludes Phase II of the study conducted under Contract DA44-177-AMC-101(T) Modification 1. The study was initiated upon receipt of the contract modification on 17 June 1964.
Conformal Gear Evaluation

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